

1 **Capturing the diversity of mesoscale trade wind cumuli**  
2 **using complementary approaches from self-supervised**  
3 **deep learning**

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7 **Key Points:**

- 8 • Mesoscale cloud organization can be taxonomized by a two-step deep learning ap-  
9 proach in the feature space continuum  
10 • Comparing seven machine-identified classes with humans' four recognized cate-  
11 gories underlines the significance of uncertainty estimates  
12 • New diagnostic is provided to analyze the temporal transition between regimes,  
13 as illustrated for human-labeled sugar-to-flower regimes

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14 **Abstract**

15 At mesoscale, trade wind clouds organize with various spatial arrangements, shaping  
 16 their effect on Earth’s energy budget. Representing their fine-scale dynamics even  
 17 at 1 km scale climate simulations remains challenging. However, geostationary satellites  
 18 (GS) offer high-resolution cloud observation for gaining insights into trade wind cumuli  
 19 from long-term records. To capture the observed organizational variability, this work pro-  
 20 poses an integrated framework using a continuous followed by discrete self-supervised  
 21 deep learning approach, which exploits cloud optical depth from GS measurements. We  
 22 aim to simplify the entire mesoscale cloud spectrum by reducing the image complexity  
 23 in the feature space and meaningfully partitioning it into seven classes whose connection  
 24 to environmental conditions is illustrated with reanalysis data. Our framework fa-  
 25 cilitates comparing human-labeled mesoscale classes with machine-identified ones, ad-  
 26 dressing uncertainties in both methods. It advances previous methods by exploring tran-  
 27 sitions between regimes, a challenge for physical simulations, and illustrates a case study  
 28 of sugar-to-flower transitions.

29 **Plain Language Summary**

30 Clouds are a fundamental player affecting our planet’s energy balance, making their  
 31 accurate representation crucial in climate models. One open question is how they orga-  
 32 nize on a scale of a few 100 km (mesoscale) in the tropical northern Atlantic region east  
 33 of Barbados. Satellite observations can help to categorize these clouds, but previous meth-  
 34 ods had limitations in capturing the full range of cloud arrangements and transitions be-  
 35 tween different cloud forms. We have introduced a novel approach that utilizes machine  
 36 learning and geostationary satellite data to address this issue. Our machine learning model  
 37 autonomously learns to recognize various cloud patterns and distributions. We conducted  
 38 a comparative analysis between the categories generated by the machine and those iden-  
 39 tified by human experts to understand the strengths and weaknesses of both methods.  
 40 Additionally, we explore a case study where clouds undergo a transformation, changing  
 41 from a structure resembling sugar to one resembling flowers. This particular transfor-  
 42 mation was found difficult to capture with physical simulation before. The clear signa-  
 43 tures of the transition identified by our machine learning approach can help to better  
 44 understand cloud evolution, which is crucial for improving climate models and predict-  
 45 ing how cloud behavior may change in a changing climate.

46 **1 Introduction**

47 Shallow convective clouds, though individually small (measuring in tens of meters),  
 48 cover large areas of the tropical oceans, forming distinct cloud fields that span hundreds  
 49 of km. They are vital in regulating the Earth’s energy balance, exerting a net cooling  
 50 effect by reflecting more sunlight than retaining outgoing long-wave radiation (Bony et  
 51 al., 2004). However, the representation of these clouds, even in the advanced 1km scale  
 52 climate simulations, is insufficient (Schneider et al., 2019). This contributes to a signif-  
 53 icant inter-model spread in predicted cloud feedback and climate sensitivity (Bony & Dufresne,  
 54 2005; Nuijens & Siebesma, 2019). To address this challenge, Bony et al. (2017) proposed  
 55 the EUREC<sup>4</sup>A field campaign, organized in January-February 2020, around the Barba-  
 56 dos region of the North Atlantic Trades (NAT) (Stevens et al., 2021). This initiative aimed  
 57 to enhance our understanding of shallow cloud dynamics by leveraging a diverse set of  
 58 observations and thus possibly improving their representation in numerical models.

59 During the preparation of the campaign Stevens et al. (2020) identified four shal-  
 60 low convective organization regimes (*Sugar, Gravel, Flower, Fish*) (SGFF), with frequent  
 61 occurrence on meso- $\beta$  (20 to 200 km) and meso- $\alpha$  (200 to 2,000 km) spatial scale. These  
 62 regimes exhibit differences in net cloud radiative feedback (Bony et al., 2020) and are

63 related to different environmental conditions (Schulz et al., 2021). Of specific interest  
 64 are transitions between different organizations, e.g., from sugar to flower, which has been  
 65 studied in Large-Eddy-Simulation (LES) to understand the governing processes and prove  
 66 to be difficult (Narenpitak et al., 2021; Dauhut et al., 2023).

67 Yet, imposing four distinct classes on the diversity of the observed organization does  
 68 not cover the intermediate cloud patterns or transient states, as highlighted by LES stud-  
 69 ies. Hence, some processes critical for climate feedback may be ignored or neglected. Fur-  
 70 thermore, recent studies trying to quantify these labeled well-organized systems find that  
 71 they occur only around 50% over NAT (Janssens et al., 2021; Schulz et al., 2021; Vial  
 72 et al., 2021) and some ambiguities in agreement from the labeler’s side exist (Schulz, 2022).

73 Denby (2020) and Janssens et al. (2021) argue for a continuum of cloud organiza-  
 74 tion where Denby (2020) employs an unsupervised neural network for grouping similar  
 75 cloud structures and demonstrate its effectiveness via hierarchical clustering (HC) and  
 76 associated radiative properties. However, their training approach involved a possibility  
 77 of false negative sampling (Huynh et al., 2022), where the negative pair’s distant tile (taken  
 78 from a random location on a different day) does not necessarily guarantee a dissimilar-  
 79 ity in their cloud system’s structure and distribution. Further, employing high-dimensional  
 80 features in HC has performance and scalability issues (Du, 2023; Gilpin et al., 2013). Janssens  
 81 et al. (2021) assumes a linear combination of traditional cloud metrics for describing the  
 82 cloud systems. Utilizing these metric scores and a k-means algorithm, they attempted  
 83 to partition their metric space into seven arbitrary clusters, as finding meaningful cloud  
 84 regimes (CRs) seemed non-trivial.

85 The overarching goal of our study is to develop a simplified approach to describe  
 86 cloud organization from high-resolution images. In this way, it should open up new path-  
 87 ways to exploit the information content of existing comprehensive satellite data records.  
 88 Our first objective is to develop a streamlined representation that captures the entire  
 89 cloud spectrum’s organizational relationships, which we call a continuum. Second, we  
 90 target the four somewhat arbitrary classes from Stevens et al. (2020) and delve deeper  
 91 into finding useful CRs from an interpretable continuum. We approach our objectives  
 92 by developing a two-step self-supervised deep learning approach (Section 3) applied on  
 93 GOES – 16 E cloud optical depth (COD) images (Section 2). Section 4.1 delves deeper  
 94 into the representations and their characteristics, highlighting the differences to Denby  
 95 (2023)’s approach. Our work demonstrates that the presence of derived partitions fa-  
 96 cilitates a comparison of human labels with these partitions (Section 4.2). Finally, in Sec-  
 97 tion 5, we illustrate how the partitioning of the continuum supported by environmen-  
 98 tal data allows us to monitor when a particular cloud system transitions to another.

## 99 2 Satellite dataset

100 We use COD retrieved from GOES-16 E Advanced Baseline Imager (Schmit et al.,  
 101 2005) using the daytime cloud optical and microphysical properties algorithm (DCOMP)  
 102 (Walther & Heidinger, 2012) at 2 km horizontal resolution and 10 – 15 minutes tempo-  
 103 ral resolution. Our domain in NAT (5 - 20° N and 40 – 60° W) is similar to domains used  
 104 in past studies (Bony et al., 2020; Schulz et al., 2021). The regional climate defines De-  
 105 cember to May as dry and June to November as wet seasons (Stevens et al., 2016). We  
 106 consider November to April 2017 - 2021 as our study period. November is added to the  
 107 typical dry period because we want to see how stronger convective events influence our  
 108 approach.

109 We chose COD because it is closely related to the cloud radiative effect and mit-  
 110 igates solar and surface influences. The uncertainty associated with COD retrieval re-  
 111 mains below 10% for all ranges in water clouds (see Figure 4 in Walther and Heidinger  
 112 (2012)). Note that some fine-scale cloud systems, such as sugar and gravel (meso- $\beta$  scale),

113 their individual cloud cells might not be fully resolved with the spatial resolution of this  
 114 product. However, since our study focuses on the organizational aspects of shallow con-  
 115 vection clouds (spanning hundreds of km), we expect the resolution limit to have a lim-  
 116 ited impact on our study.

117 Representation learning, also known as feature learning, is a specialized field within  
 118 machine learning that focuses on extracting meaningful features of a given dataset. To  
 119 better represent the mesoscale cloud distributions, we use six images per timestamp, in-  
 120 cluding an additional fixed image over the Barbados domain (see S1). Although they might  
 121 overlap in some instances, random cropping aims to get mesoscale distributions as di-  
 122 verse as possible without human interference. Note that the Barbados domain enables  
 123 comparison with ground-based measurements in future studies. To have an adequate spa-  
 124 tial scale of typical occurring cloud fields over NAT (as discussed in Section 1), we use  
 125  $256 \times 256$  pixels (roughly 512 square km) as also found in Muller and Held (2012). We  
 126 exclude crops affected by glint or poor retrieval quality using the respective data flags.  
 127 Time stamps are limited to 9 am - 3 pm Barbados local time to avoid sun glinting. We  
 128 use land class data to filter out images with convection over land, specifically over the  
 129 northeast of the South American continent. Finally, to mitigate uncertainties at high COD  
 130 from DCOMP retrieval, COD values above a threshold of 50, already indicating deep clouds,  
 131 are clipped to 50. This results in a sample size of 51,000 satellite images.

132 For further analysis, we make use of hourly ERA-5 (Hersbach et al., 2020) large-  
 133 scale environmental parameters (integrated water vapor (IWV), horizontal and vertical  
 134 wind speed, relative humidity) and cloud fraction at a spatial resolution of  $0.25^\circ$ . Hourly  
 135 cloud amount for four vertical ranges (surface-700 hPa, 700 hPa-500 hPa, 500 hPa-300  
 136 hPa, 300 hPa-tropopause) is used from the Clouds and Earth’s Radiant Energy System  
 137 fourth edition (CERES, Edition - 4A) (Wielicki et al., 1996), characterized by a spatial  
 138 resolution of  $1^\circ$ .

### 139 3 Methods

140 The workflow is as follows: a) A neural network (N1) ingests satellite images to con-  
 141 tinuously sort cloud organizations based on visual similarity, yielding the feature vec-  
 142 tor 'Z' (384 dimensions) for each image. b) Z is reduced to a 2-dimensional (2D) space  
 143 for visualizing a continuous arrangement of images with respect to their cloud structures  
 144 (continuum). c) The optimal number 'K' of meaningful clusters or CRs is derived from  
 145 the 2D representation, d) A second neural network (N2) of similar architecture as N1  
 146 but constrained by 'K' classes ingests the satellite images to finally assign each image  
 147 to a discrete class.

148 a) N1 identifies the structural similarities in the cloud systems and maps the learned  
 149 visual features into the 384-dimensional feature space Z. To learn similar embeddings  
 150 of semantically similar mesoscale structure and distributions, every epoch, we opt for two  
 151 random global crops with a 0.75 fraction ( $192 \times 192$  pixels) within a single parent satel-  
 152 lite image. Each crop is processed in a separate branch (called student and teacher) by  
 153 a Vision Transformer (ViT), which has a sequence of self-attention (Vaswani et al., 2023)  
 154 and feed-forward layers (Bebis & Georgiopoulos, 1994). Note that both branches have  
 155 the same general architecture, but the parameters (weights and biases) learned during  
 156 training are slightly different. As the largely overlapping global-crop pair has very sim-  
 157 ilar cloud structures, the network learns their essential features and puts the pair closer  
 158 to each other in the high-dimensional feature space. A cross-entropy loss function min-  
 159 imizes the difference in the output of both branches and yields the 384-element feature  
 160 vector Z. More details on the implementation are given in S2. This way of training, un-  
 161 like Denby (2020), eliminates the need for a negative pair and avoids linearized assump-  
 162 tions like in Janssens et al. (2021).

163 b) Z includes the continuously sorted representation of cloud organization. We re-  
 164 duce its 384 dimensions to two dimensions using the well-established t-distributed Stochas-  
 165 tic Neighbor Embedding or t-SNE algorithm (van der Maaten & Hinton, 2008). It pre-  
 166 serves relative local positions by using cosine distance in affinity computation and tries  
 167 to retain global structure by initializing with principal components for mapping to a two-  
 168 dimensional space. This proves helpful because high-dimensional data when directly ap-  
 169 plied to cluster analysis, face challenges like the curse of dimensionality (Aggarwal et al.,  
 170 2001), where increased dimensions make distances between data points less meaningful.  
 171 Also, the presence of noise and outliers can distort clusters, hindering the algorithm’s  
 172 ability to identify distinct clusters (Steinbach et al., 2004).

173 c) After obtaining the continuously sorted 2D representation of cloud systems (see  
 174 Fig. 1.a), we intend to find optimal boundary conditions within the sorted order to de-  
 175 rive distinct clusters (CRs). Selecting a meaningful and interpretable number of clus-  
 176 ters is crucial to avoid over-fitting, where excessive clusters can capture noise, and also  
 177 under-fitting, where too few clusters can miss significant patterns in the data. On this  
 178 2D representation space, we apply a set of three statistical approaches, namely metric  
 179 scores of distortion, silhouette (Rousseeuw, 1987), and Calinski-Harabasz (Caliński &  
 180 Harabasz, 1974) to identify the number of optimal classes into which the given features  
 181 could be clustered. Schubert (2023) suggests taking a collective inference from these three  
 182 methods to best fit the spherical k-means clustering algorithm used during the training  
 183 of N2. S3 illustrates how the three metrics point to an optimal clustering of the contin-  
 184 uum into seven CRs. Note that the choice of seven classes is robust, as illustrated by sev-  
 185 eral sensitivity tests (shown in S4), such as the dimensionality-reduction technique, size  
 186 of the dataset, initial weights of the network, and different global crop sizes.

187 d) N2 from Chatterjee, Acquistapace, et al. (2023) is similar to N1 concerning the  
 188 two branches: When the feature vectors of both branches capture similar information  
 189 from the global crops, the loss decreases; conversely, it increases when they diverge. How-  
 190 ever, before the cross-entropy loss is computed in each branch, a spherical k-means clus-  
 191 tering is applied. Herein, the feature vector from the upper branch gets assigned a class  
 192 (target label) based on proximity to its nearest centroid while the lower branch feature  
 193 vector tries to reduce its cosine distance with the allocated centroid (predicted proxy)  
 194 to reduce the loss. In this way, the network learns to allocate both global crops to the  
 195 same class. After obtaining the label of each satellite image, we transfer the assigned class  
 196 to the continuum space, which proves helpful because N1 has learned the sorting arrange-  
 197 ment of keeping similar cloud systems closer. Therefore, it helps to visualize how each  
 198 cluster with distinct characteristics can form a separate local region. Additionally, the  
 199 N2 feature space is i) more sparse than N1 (see S2 for explanation) and ii) arranged by  
 200 closeness to the centroids, which, unlike N1, may not be ideal for representing smooth  
 201 transitions of cloud systems. Note that there are further differences between N1 and N2,  
 202 e.g., image augmentation, which are detailed in S2.

## 203 4 Results

### 204 4.1 Continuous and discrete representations

205 We now analyze the diversity of cloud systems included in the satellite data record  
 206 within their continuous and discrete representations. Both are visualized in 2D contin-  
 207 uum space using the t-SNE algorithm (Section 3). The organization state captured in  
 208 the satellite images changes smoothly and different cloud organizations can be identi-  
 209 fied in different areas of the continuum (Fig. 1.a). Going anticlockwise from the top, arch-  
 210 shaped cloud systems lie in the top-left, followed by flower-type distributions on the left  
 211 side of the continuum. Close to the flowers in the bottom-left are the flowers spreading  
 212 out into stratocumulus. Note that physically simulating the transition is challenging as

213 modeling studies struggle to capture the stratocumulus to cumulus transition (Sarkar  
214 et al., 2020), although they lie adjacent in the continuum.

215 The bottom part of the feature space contains long bony skeletons, i.e., fish-type  
216 cloud systems, and the bottom-right corner shows an extended part of fish-type cloud  
217 organizations delineated by unusually large cloud-free regions. The top-right region of  
218 the continuum is a collection of deep convective cells. These primarily occur in the month  
219 of November. Arc-shaped cloud systems appear on the left and top-left of the contin-  
220 uum. Vogel et al. (2021) suggest that the horizontal structure of mesoscale arcs is in-  
221 trinsically linked to gravel, flowers, and fish. In sequence, Figure 1a shows a continuous  
222 link in the spatial arrangement of cloud systems rather than the distinct classes. This  
223 demonstrates the good performance of our continuous approach, which is further sup-  
224 ported by the analysis of attention maps in S5. Note that any newly taken satellite im-  
225 age can be placed into this continuum using the weights of N1, allowing a quick assess-  
226 ment of its organizational status. Also, similar trajectories of subsequent images can be  
227 tracked within the continuum space.

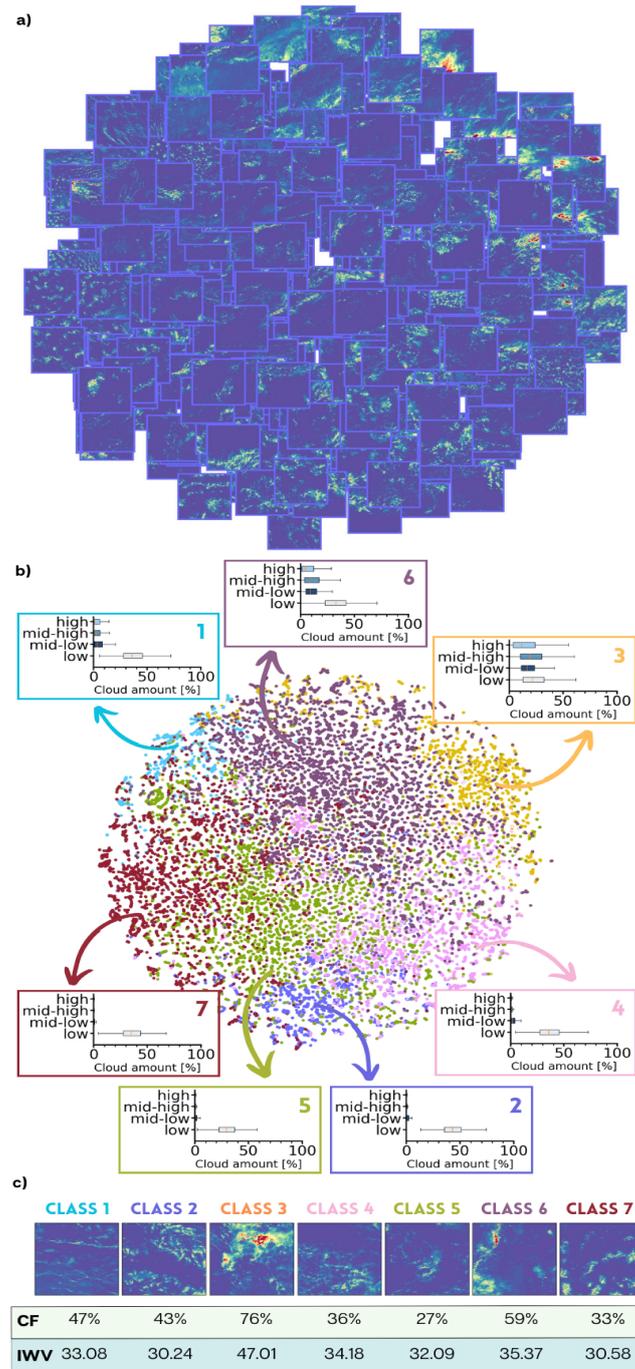
228 After training N2, each of the images can be attributed to one of the seven classes  
229 (refer to Section 3), revealing distinct spaces within the continuum (Fig. 1.b). To assess  
230 how well the seven classes separate, they are evaluated using cloud amounts at four dif-  
231 ferent height levels from CERES data. This analysis, on the one hand, reflects how each  
232 class differs from the others, and on the other hand, it reasons for the underlying close-  
233 ness of each class with neighbor classes in the continuum. The difference between the  
234 seven clusters is especially evident when looking at their centroid images (Fig. 1.c).

235 Deep convective class three has by far the highest cloud fraction of 76% and a third  
236 more water vapor ( $47.0 \text{ kgm}^{-2}$ ) than all other classes (mean =  $32.5 \text{ kgm}^{-2}$ ). We use IWV  
237 as a fingerprint for the origin of air masses and intend to test it later to investigate the  
238 connection between CR and air mass origin. Figure 1.b already shows that class 3, which  
239 by far has the highest IWV, is also related to the deepest convection. Neighboring class  
240 six includes less frequent higher-level clouds and has a reduced CF of 59% compared to  
241 class three. All other classes are dominated by low-level clouds with lower than 50% CF.  
242 Classes one and four (neighbor to class six) still have some mid to high-level cloud amounts  
243 (below 10%). Class one can be interpreted as representing arch-shaped cloud systems,  
244 and four resembles the fish class with a more open sky (also shown by reduction in CF).

245 Classes two, five, and seven, being close in the continuum, have similar cloud verti-  
246 cal distributions and IWV ranging from 30 to  $32 \text{ kgm}^{-2}$ ; however, their organization  
247 is very different, as illustrated by the centroids (Fig. 1.c) and mean CFs (43%, 27%, and  
248 33%, respectively). Class two primarily comprises shallow cloud cover, corresponding to  
249 cloud systems resembling fish-type formations. Class five has the lowest CF and is an  
250 intermediary class type between classes two and seven. Finally, class seven has a pres-  
251 ence of low cloud amounts and negligible mid to higher cloud amounts, which visually  
252 resembles flower-type cloud distributions. Therefore, discretizing the continuum helps  
253 us visually find three main classes (one, two, and seven) frequently resembling features  
254 identified by humans, i.e., sugar, fish, and flower, respectively. However, it also shows  
255 the remaining diversity and their characteristics in a cohesive approach. Note that in con-  
256 trast to the challenges faced by Denby (2023) or Janssens et al. (2021) in isolating mean-  
257 ingful clusters, our N1 + N2 framework excels in simplifying the cloud organization com-  
258 plexities by efficiently categorizing the continuum into seven interpretable classes.

## 259 4.2 Machine versus human labels

260 While we checked for visual correspondence and class-wise characteristics in Sec-  
261 tion 4.1, our framework now creates the opportunity to quantify how human labels com-  
262 pare to the machine’s seven clusters. For this, we use the dataset from Schulz (2022),  
263 which is a 1km x 1km resolution manually labeled dataset for the NAT region and EUREC<sup>4</sup>A



**Figure 1.** a) Visualization of four hundred randomly selected satellite images arranged in the continuum space. b) Same as a), but now, instead of an image, the discrete class determined by N2 is shown (colored). For each class, statistics on low, mid-low, mid-high, and high cloud amount (%) obtained from the CERES hourly data set are provided. c) Centroid COD images belonging to seven clusters as identified by the discrete neural network (N2). The table shows per class the average of cloud fraction (CF, %) from the GOES retrieval and integrated water vapor (IWV,  $\text{kgm}^{-2}$ ) from ERA-5.

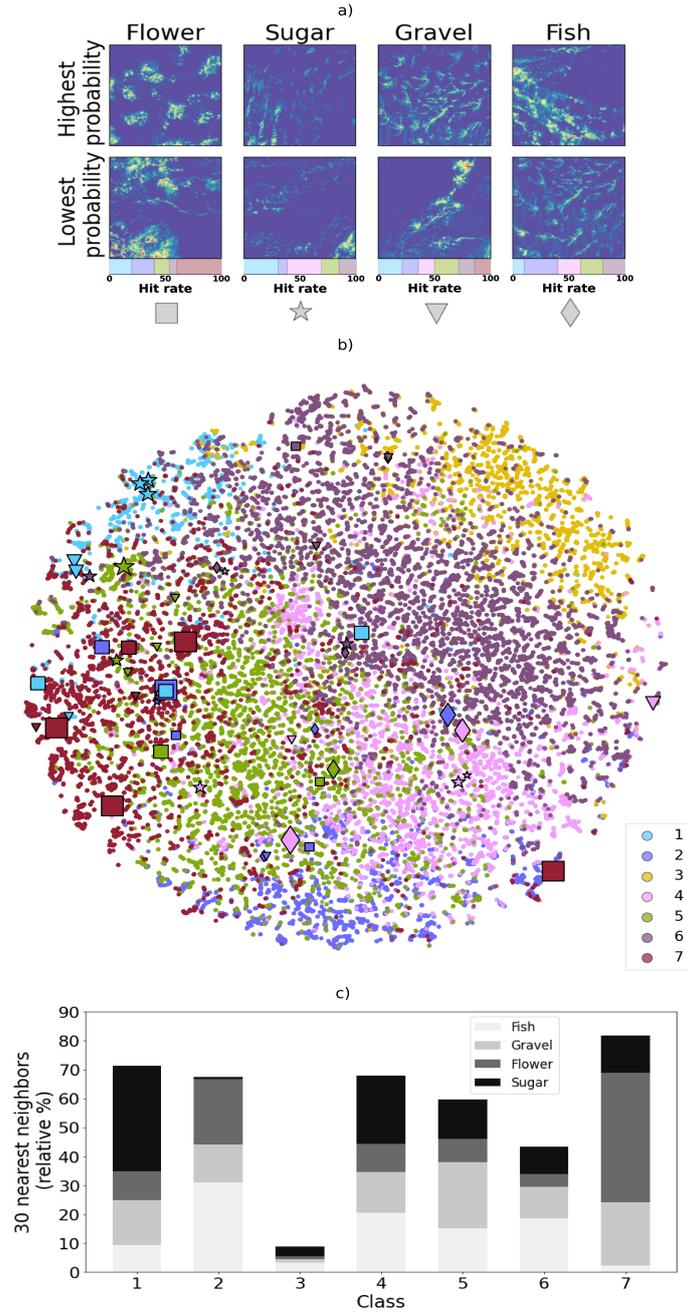
time period (47 days). Approximately 50 scientists generated the dataset by identifying mesoscale patterns (SGFF) and marking variable-sized rectangles around homogeneous organization states. Overlapping rectangles allowed a single grid point to be labeled with multiple patterns by a scientist. Individual uncertainty is expressed through each pattern’s classification mask ( $c_m$ ) (Schulz, 2022). For example, if a grid point is within both gravel and sugar rectangles, the  $c_m$  would be 0.5 for both and 0 for the other two patterns. Mutual agreement among scientists for each pattern at a grid point is determined by averaging  $c_m$  values, ranging from 0 to 100%.

We hypothesize patterns with higher agreement are most likely attributed to their meaningful partitions within the continuum (as discussed in Section 4.1). For each time-stamp where at least one of the four patterns was identified within our domain, we select a 256 x 256-pixel satellite image centered over the area of highest human agreement. In this way, we ensure the best possible intercomparison. This leaves us with 52 samples of human-labeled satellite images (fish: 19.3%, gravel: 26.9%, flower: 28.8%, sugar: 25.0%). Note that even with the highest consensus criteria, there’s still diversity in agreement. The inter-quartile agreement range is 35%, while the minimum and maximum agreements show consensus levels of 7% and 91%, respectively.

The framework classifies 40% flower-labeled cloud systems in class seven (see the hit rate for each class in Fig. 2.a) while sugar-labeled cloud systems are 31% classified in class one and 20% in class four. Gravel has a total of 44% representation in classes one and five, whereas fish annotated labels are allocated 30% in class two and 20% each in classes four and five. Further, examining example images visually (Fig. 2.a), it becomes apparent that images with lower human agreement notably diverge from the established definitions (provided in Stevens et al. (2020)) of SGFF cloud structures, in contrast to images with high human agreement.

Within the continuum (Fig. 2.b), flowers detected with high probability mostly occur in areas of class seven, which was already well reflected in the centroids. Following a similar agreement is sugar (street-type cloud systems), which can be found in areas of class one. However, 38% of sugar samples, with a low agreement, lie in classes four and five, which are extended fish and flower type classes (Section 4.1). Note that even though these samples reside in those regions of the feature space, their confidence is less than 25%. Similarly, in the gravel pattern, 21% samples belong to class six and exhibit minimal human confidence. In contrast, the rest from the gravel class are positioned between classes one and seven, suggesting that gravel cloud cell sizes fall between sugar and flower. Rightly, no human-labeled samples are found in class three, which predominantly comprise deep convective cells. Finally, the fish class exhibits relatively higher confidence in human labels, aligning well with the feature space characteristics, and lies in class two (fish) and four (extended fish-type cloud structures with large cloud-free regions). Hence, cloud systems characterized by higher agreement among human observers are situated within the designated regions, while those with lesser consensus are positioned within the ambiguous regions of the continuum.

To compensate for the limited number of human label samples, we analyze the 30 nearest satellite images to each human label as identified by N1 (Fig. 2.c). The majority of neighbors in human-identified fish-type cloud systems (more than 50%) belong to machine-identified classes two and four. The gravel regime includes members of all classes, with notable contributions from classes one, five, and seven, which exhibit cloud cell characteristics similar to gravel systems. The variability in the spread can be linked to the limited representation of gravel glass in Schulz (2022)’s dataset, as gravel occurrences were sporadic during the EUREC<sup>4</sup>A campaign. Additionally, 75% of gravel labels in our sub-samples had agreement levels below 0.25. In contrast, the flower regime mainly belongs to class seven (46 %), further aligning with the high confidence of human labels. Regarding sugar-type cloud systems, 37 % of the neighbors fall into class one, while those with low human agreement are scattered across the remaining classes. Therefore, we find



**Figure 2.** a) To enhance visualization and reference for human labels, each column displays 256 x 256 COD images of a specific class, with the highest and lowest human agreement shown in two rows. Below, the images in each column show the hit rate, representing the N2-predicted class for each human label. b) Continuum space colored with different classes (1-7) in the background, along with Human labels (fish, sugar, flower, gravel) in the foreground. Ascending symbol sizes with low (0-0.25), mid-low (0.25-0.50), mid-high (0.50-0.75), and high (0.75-1.00) agreement are shown. c) Relative occurrence of 30 nearest neighbors to human-labeled fish, gravel, flower, and sugar along the seven machine-labeled classes.

317 that machine-labeled classes of the 30 nearest neighbors encompass the human-labeled  
 318 ones, especially for sugar, flower, and fish, but not so clearly for gravel.

319 Further, in S6, using ERA-5 large-scale environmental variables and cloud physical  
 320 properties, we demonstrate that the neighbors and the human crops share a similar,  
 321 homogeneous distribution of physical properties. Therefore, this analysis, for the first  
 322 time, shows how to exploit the labels and physical properties of the semantically similar  
 323 nearest-neighbors of any cloud system of interest further to enhance our understand-  
 324 ing of the connection between organizations.

## 325 5 Transitions

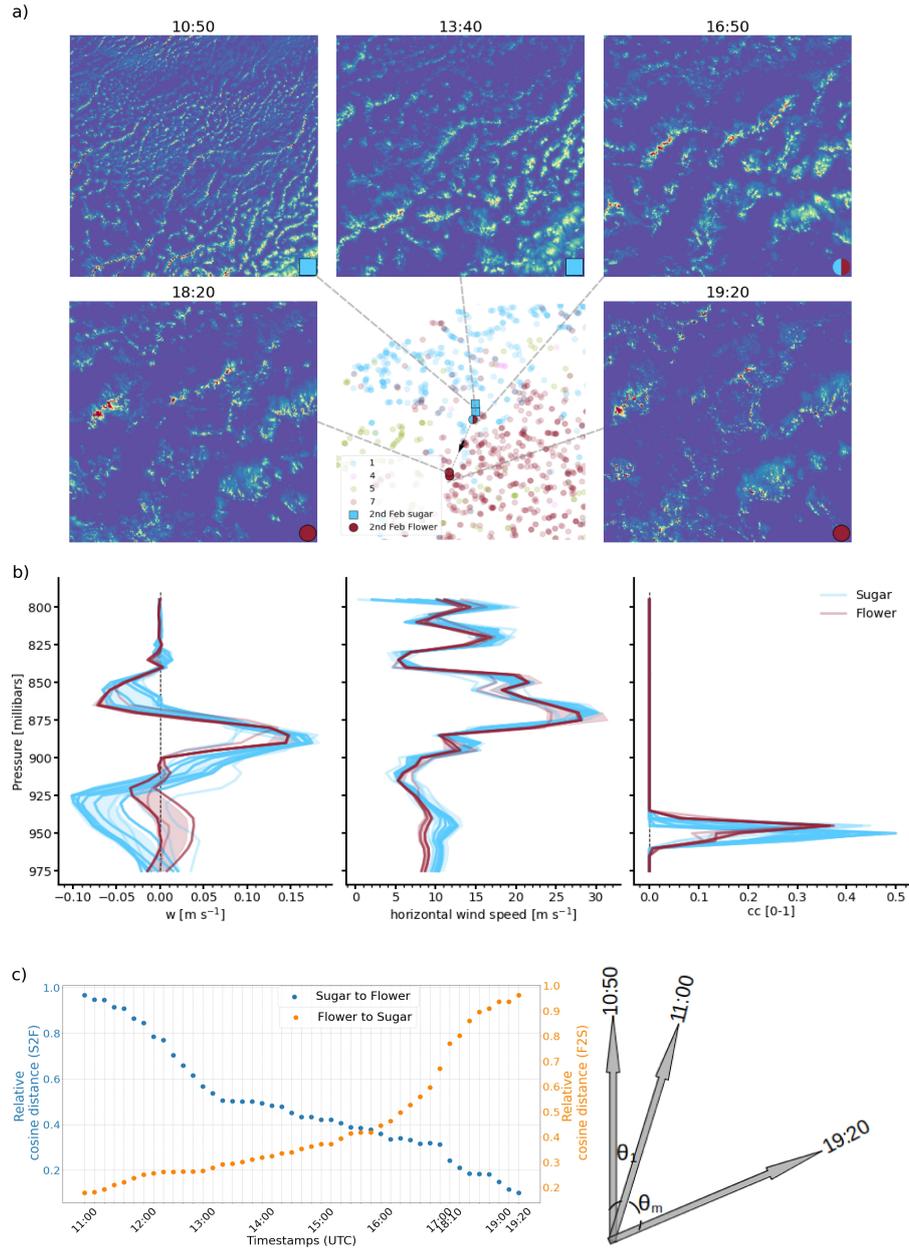
326 To showcase an application that highlights the intelligible partitioning of the con-  
 327 tinuum, we explore the "sugar" to "flower" (S2F) cloud system transition on February  
 328 2, 2020. Using LES, Narenpitak et al. (2021) showed a strengthening of large-scale up-  
 329 ward wind motion and an increase in total water path and optical depth as the trans-  
 330 formation develops towards the flower. Here, we look at how the transition in COD is  
 331 represented in the feature space. For example, where do the representations of transi-  
 332 tions lie in the feature space? How smooth is the transition in the feature space?

333 Covering the temporal developments, 47 COD images were collected (after apply-  
 334 ing quality filter checks (see Section 2)), centered at 12.5° N, 50° W. They cover the time  
 335 from 10:50 to 19:20 UTC, with a gap between 17:00 to 18:00 UTC likely caused by lo-  
 336 cal sun glint. We ingested the available samples into the trained framework and collected  
 337 their features (from N1) and machine labels (from N2).

338 Sugar systems comprise small and shallow clouds with a large spread of individ-  
 339 ual cloud cells in a domain, as evident in the beginning (10:50, Fig. 3.a). In contrast,  
 340 flower systems appear in multiple deeper aggregates surrounded by large dry areas and  
 341 are detected first in the southeast cover at 16:50 before becoming dominated at 19:20  
 342 over the full domain. In general, the transition features lie at the border of well-defined  
 343 clusters one ('sugar') and cluster seven ('flower') (Fig. 3.a), and the framework is able  
 344 to capture their intermediary nature as they are neither perfect sugar nor flower type.  
 345 We use wind speed (vertical and horizontal) to represent changes in atmospheric dynam-  
 346 ics and changes in cloud cover to account for the changes in mesoscale structure from  
 347 the ERA-5 product. A gradual increase in vertical velocity is observed as the system tran-  
 348 sitions from S2F, and consequently, the surface wind speed gradually reduces its strength  
 349 (Fig. 3.b). In addition, as expected, cloud fraction profiles show a gradual decrease as  
 350 the transition progresses with time.

351 Sugar-type mesoscale organizations typically occur during the daytime with shal-  
 352 low boundary layers, while flowers occur at night with deeper boundary layers (Vial et  
 353 al., 2021). We use the cosine distance between features, a unique quantifiable distance  
 354 metric derived from N1, to show the gradual development of the S2F transition inside  
 355 the feature space (Fig. 3.c). The transformation appears smooth initially, with relatively  
 356 more significant changes occurring later (post-18:00 UTC) as the system approaches the  
 357 flower state. We link the relatively high changes in cosine distance during flower stages,  
 358 as opposed to initial sugar stages, to the progression of convective developments. It be-  
 359 comes more accelerated as the system approaches the well-defined flower state.

360 Therefore, the framework reveals unbiased relative changes from the point of in-  
 361 terest (in space or time) solely based on changes captured in high-dimensional feature  
 362 space. Also, unlike previous works of Denby (2020) or Janssens et al. (2021), the intel-  
 363 ligible partitioning of the continuum allows us to see when a particular system transi-  
 364 tions to another. S7 provides insights into the transition probability of one class trans-  
 365 forming to another over the Barbados domain.



**Figure 3.** a) Five COD images covering the transition period between sugar and flower on the second of February 2020. Their position in the continuum is indicated in the center of the bottom row. b) Individual and standard deviation profiles of 1) vertical, 2) horizontal wind speed describing the atmospheric dynamics, and 3) cloud cover showing changes in mesoscale structure of the transition samples. c) Illustration of temporal transition development inside the feature space: cosine distance of the first daytime image feature obtained at 10:50 UTC compared with the cloud system evolution features for the rest of the day (blue). The last obtained image at 19:20 UTC towards the first image (orange) and  $\theta_m$  represents the increasing cosine distance.

## 366 6 Conclusion

367 In this work, we develop a two-step self-supervised learning framework to study shallow convective organization properties and their transitions. By analyzing organization  
368

369 in a continuous approach without imposing predefined classes, we include all occurring  
 370 patterns and transitional states in our analysis. Moreover, the approach shows that mesoscale  
 371 cloud organizations in NAT can be partitioned into seven reasonable CRs for the time  
 372 period considered. Exploiting the cloud amount at different vertical levels from CERES  
 373 measurements, we show how the classes are interlinked with each other within the con-  
 374 tinuous space and thus capture the variability of tropical clouds in more detail.

375 We compare human-labeled cloud systems (Schulz, 2022) with the machine-identified  
 376 partitions and underscore challenges in human-labeling of cloud organizations. Cloud  
 377 systems with higher agreement among humans lie in the "correct" region of the feature  
 378 space, while the ones with less consensus are in the "wrong" regions of the feature space.  
 379 Also, the potential and interpretability of the continuum space become more evident when  
 380 examining the classification and physical properties between human labels and their near-  
 381 est neighbors.

382 Two of the seven CRs are strongly related to sugar and flower. Representing the  
 383 S2F transition case study (Narenpitak et al., 2021) for February 2, 2020, in the contin-  
 384 uum illustrates the capability to identify and represent the observed transformations smoothly  
 385 in their clearly interpretable regions. We evaluate the transition's large-scale environ-  
 386 mental parameters and observe a gradual increase in vertical wind speed and a gradual  
 387 decrease in cloud amount. Finally, we showcase the use of cosine distance metric in cap-  
 388 turing clear signatures of the S2F transition, which can help better understand cloud evo-  
 389 lution. This is crucial for improving climate models and predicting how cloud behavior  
 390 may change in a changing climate.

391 One of the limitations of this study is the use of only daytime cloud retrievals; hence,  
 392 the organizations' nocturnal nature cannot be captured. Future studies will use infrared  
 393 satellite measurements for 24-hour coverage. We aim to fine-tune our framework with  
 394 ground-based observations of the EUREC<sup>4</sup>A campaign and extend our analysis to a cli-  
 395 mate scale. The developed workflow could be a testing ground for investigating the newly  
 396 adjusted subgrid parameterization effects in high-resolution global digital twins (Hoffmann  
 397 et al., 2023) for mesoscale cloud systems or atmospheric processes at different scales.

## 398 7 Open Research

399 CERES, Edition-4A is available at (NASA et al., 2017), and ERA-5 reanalyses data  
 400 (Hersbach et al., 2023) is available from the Copernicus climate change services. GOES-  
 401 16 data has been accessed from the National Oceanic and Atmospheric Administration  
 402 (NOAA), Climate Data Records (CDR) facility NOAA (2024b). Here, the COD retrieved  
 403 using DCOMP algorithm (Walther & Heidinger, 2012) from GOES-16 measurements is  
 404 available at NOAA (2024a). The code to produce this work and pre-trained weights of  
 405 N1 and N2 can be accessed at Chatterjee, Schnitt, et al. (2023).

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