

Informed Neural Networks for Flood Forecasting with Limited Amount of Training Data

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Key Points:

- We developed a methodology to improve the precision of flood forecasting technology, specifically when working with limited amounts of data.
- The methodology incorporates a domain-specific knowledge into the architecture and training procedure of Neural Networks (NN).
- Proposed method has demonstrated superior accuracy compared to conventional methods, even under conditions of data scarcity.

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Abstract

This study presents a novel approach to improving the accuracy of flood forecast models even if training data is limited. Flood forecast information is crucial for early evacuation planning. However, the probability of flooding caused by continuous heavy rainfall is increasing, even in areas for which floods have not been anticipated. While methods exist to provide flood forecasts, they require long-term observations, and regular updating of extensive data on the catchment basin. These requirements impact the construction time and cost of providing flood forecasts. To address this issue, we propose the Informed Neural Network (INN); it draws on existing domain knowledge of river engineering to enhance the performance of flood forecasts with limited amounts of training data. We evaluate the performance of our proposed method by assessing Japanese real-world river water levels and compare the results to those of conventional methods such as artificial neural networks (ANNs). Our results demonstrate that INN can significantly improve forecast accuracy with only a small amount of training data, comparable to conventional methods trained with three times the amount of flood data with three hours forecast. This study highlights the potential of INN as a novel approach for accurate and efficient flood forecasting with limited training data.

Plain Language Summary

This study introduces a new method called the informed neural network to enhance the accuracy of flood forecasting models when the training data is limited. Accurate flood forecasts are crucial for early evacuations, as the risk of flooding due to heavy rainfall is increasing even in areas without existing flood risk. Traditional methods for generating flood forecasts require extensive data and continuous updates, making the process time-consuming and costly. In contrast, the INN approach incorporates existing knowledge of river engineering to improve forecasting performance with a just a small amount of training data. We evaluate the INN method with real-world river water level data from Japan, and compared it to conventional methods such as artificial neural networks. The results demonstrate that the INN approach significantly improves forecast accuracy, even with limited training data, to match conventional methods trained with eight three more flood data with three hours forecast. This study highlights the potential of INN as an innovative and efficient approach for accurate flood forecasting, particularly in situations with limited training data.

1 Introduction

Flood forecast information can enable municipalities to plan proactively and residents to safely evacuate in the event of a flood. Consequently, accurate flood forecasting is crucial in areas susceptible to flooding. Recently, Japan has observed an increase in heavy rainfall compared to the past (Kawase et al., 2020; Hirockawa et al., 2020) Kawase et al. (2020) showed central and western regions experiencing record-breaking total precipitation of 48- and 72-hours at approximately 1,300 precipitation stations in 2018. Weather officials continue to observe such unprecedented heavy rains. Some studies predict that these changes are due to climate change and that the rainfall trend will continue (Kusunoki et al., 2006; Kitoh & Uchiyama, 2006; Duan et al., 2015; Osakada & Nakakita, 2018; Takemi & Unuma, 2020). As a result, such an increase in unexperienced heavy rain cause the risk of flooding in areas previously unaffected by it. There are 30,000 rivers in Japan, of which only 393 provide forecast information. Climate change has increased the risk of thousands of rivers for which flood forecasts are not provided. Therefore, it is necessary to provide flood

62 forecasts at more new locations. The cost of the forecasting system is essential when
63 providing flood forecast information to many new locations.

64 There are two approaches for flood forecasting: rainfall-runoff-based approach
65 and data-driven-based approach. The rainfall-runoff-based approach requires various
66 data types, such as basin characteristics distribution. However, these data require
67 high quality(Hapuarachchi et al., 2011), making it challenging to acquire and contin-
68 uously update the data. In contrast, the data-driven approach requires only rainfall
69 and river water level data but the need for measurements over a more extended pe-
70 riod. Based on existing literature, a training dataset spanning at least five years and
71 containing at least 15 flood events for data-driven methods (Mukerji et al., 2009;
72 Noymanee & Theeramunkong, 2019). Such requirements for long-term data mea-
73 surements make providing flood forecast information for new sites difficult. There-
74 fore, a method to achieve flood forecasting with a few types and a limited amount of
75 training data is an essential issue for flood forecasting.

76 In the field of data-driven methods, one potential solution to address the issue
77 of limited training data is to incorporate prior information into the learning process
78 of NN. This approach is known as Informed Machine Learning (IML), and many
79 groups have applied IML to various domains(Von Rueden et al., 2021). IML can
80 improve model performance by applying various types of prior knowledge, such as
81 knowledge graphs and equations, to the learning process. Many IMLs use NNs as a
82 building block, especially called Informed Neural Networks (INN). INN has achieved
83 improved model performance in many areas. Despite these advancements, identify-
84 ing practical prior knowledge and corresponding Informed Machine Learning meth-
85 ods for flood forecasting remains challenging.

86 This study introduces a novel method to implement INN for flood forecast-
87 ing, suitable for limited training data scenarios. The proposed approach incorporates
88 prior knowledge about the "rainfall-runoff-river water level relationship" and "tank
89 model" derived from river engineering knowledge into a NN. We evaluated the per-
90 formance of INN, To evaluate the INN's performance, We conducted a comparative
91 analysis between the proposed and conventional methods using flood data from a
92 river in the Kyushu region of southwestern Japan. The results indicated that the
93 proposed INN method performed as well as the conventional method when sufficient
94 training data was available. Moreover, the proposed method retained its accuracy
95 even when the training data was limited. In contrast, when training data was lim-
96 ited, the conventional ANN showed a more significant Root Mean Squared Error
97 (RMSE) up to 8 times higher than the proposed INN method. These results suggest
98 that the INN approach is a promising alternative for accurate flood forecasting when
99 limited training data is available. Overall, the proposed method offers an effective
100 solution for improving the accuracy of flood forecasting with limited training data,
101 and its potential applicability to other domains where data availability is restricted
102 warrants further exploration.

103 **2 Related works**

104 There are two kinds of approaches to flood forecasting. One is a rainfall-runoff-
105 based approach, and another is a data-driven approach. Methods based on the rainfall-
106 runoff approach determine the amount of water runoff from the basin and then de-
107 termine river water levels. Methods based on the data-driven approach often predict
108 river water levels directly.

109 Many methods were proposed related to the rainfall-runoff-based approach.
110 This method has some parameters, such as precipitation, discharge, and basin char-
111 acteristics. Especially, to account for the spatial bias of rainfall and the distribu-

tion of land features, the rainfall-runoff method often requires dividing the basin into subregions, and it has been called the distributed rainfall-runoff approach (Brocca et al., 2011). Rainfall-runoff approach has parameters related to catchment characteristics. Basin characteristics include terrain, soil, geology, land cover, and more (Cole et al., 2006). Such parameters are not always available, and even when they are, they are often of poor quality and require improvement (Hapuarachchi et al., 2011). Therefore, they cannot always be the best approach to provide flood forecasting for many rivers in a short period and maintain it in the future.

A typical model in the data-driven approach is the statistical model. The autoregressive moving average (ARMA) (Valipour et al., 2012) and autoregressive integrated moving average (ARIMA) (Valipour et al., 2013) are representative and basic models in this area. A statistical model related to ARMA and ARIMA is reported to be more efficient regarding computational cost and generalization compared to the rainfall-runoff approach (Aziz et al., 2014). In the statistical model, several methods treat floods as stochastic processes and predict probability distributions from historical data (Kroll & Vogel, 2002). However, even the more advanced models need improvement in terms of the accuracy of short-term forecasts and the complexity of their application (Mosavi et al., 2018). The machine learning (ML) model is another data-driven approach. ML models for flood forecasting include a variety of algorithms such as neural networks (NN) (Le et al., 2019; Elsafi, 2014; F.-J. Chang et al., 2007), neuro-fuzzy (Mukerji et al., 2009; Chen et al., 2006; Roodsari et al., 2019), and support vector machines (Han et al., 2007; Yan et al., 2018). ML models also include algorithms such as NNs that can deal with nonlinearities in the rainfall-runoff process. ML models are reported to have better performance and less complexity than physical models (Abbot & Marohasy, 2014). The issue with these data-driven approaches is the long-term measurement data. Several literatures have reported 15 to 45 flood data events or 5 to 20 years of measurements to build ML models (Song et al., 2019; Mukerji et al., 2009; Nguyen & Chen, 2020; Noymanee & Theeramunkong, 2019).

To address the issue of long-term measurement data, Researchers attempt to integrate prior knowledge into the ML models pipeline that has been made in the fields of physical and natural phenomena. These attempts are called informed machine learning (IML). The main goal of this endeavor is to improve accuracy and challenge the problem of limited training data volume. These efforts are based on the taxonomy proposed by Von Rueden et al. (2021) and are divided into several methods depending on the representation of prior knowledge. In particular, for problems involving natural phenomena and physical systems, the type of existing knowledge that describes the system includes algebraic equations. One idea in an attempt to integrate this algebraic equation into the machine learning pipeline is loss function modification. Karpatne et al. (2017) achieved accuracy beyond conventional techniques by adding the equation relating water temperature and density to the loss function for the lake temperature modeling using NNs. Loss function modification by differential equations, another option, is also a subset of Algebraic equations. Zhu et al. (2019) has achieved higher accuracy than conventional methods for the problem of surrogate modeling of systems described by differential equations using NNs, without using training data, by using the equation as a loss function. These improvements show the possibility of INN for a limited amount of data by changing the loss function based on the algebraic equation. The next category of possible prior knowledge is knowledge graphs, which represent the relationships among the elements of the system. M. B. Chang et al. (2016) applies a network structure of NNs that dynamically changes from scene to scene to predict the motion of multiple rigid bodies that affect each other. It achieves improved accuracy over conventional static network structures. This result indicates the possibility of a network structure of NNs suitable for the target system. In flood forecasting by IML, Qian

166 et al. (2019) use simulation results by the finite volume method as training data to
 167 speed up the two-dimensional flood simulation by the shallow water wave equation
 168 and train the neural network. As a result, they achieved 50,000 times faster than the
 169 simulation. Accelerating prediction using such existing simulation results is called
 170 surrogation and is one of the applications of IML. Bhasme et al. (2021) used IML
 171 to improve annual water balance prediction accuracy. In this research, they define
 172 the relationship between the variables of the physical model that predicts runoff by
 173 learning with ML models. Mahesh et al. (2022) used IML to predict spatiotemporal
 174 floods on one-dimensional channels. IML was realized by setting the loss function of
 175 NNs based on the Saint Venant equation. When compared with ML models, IML
 176 showed higher performance. In IML, although there are many studies on physics and
 177 natural phenomena, there are still few studies on hydrology, and there needs to be
 178 knowledge about the problem of a limited amount of training data for flood forecast-
 179 ing. Therefore, we set the following questions to obtain new knowledge about the
 180 applicability of IML, especially INN, in flood forecasting. The overall research ques-
 181 tion this paper tries to answer is, "Can INN be applied to flood forecasting when
 182 flood data are limited?" Consequently, the following two questions about INN is
 183 needed to be answered.

- 184 1. Can INNs perform as other conventional flood forecasting methods in the con-
 185 dition of a sufficient amount of training data?
- 186 2. Can INN maintain the performance rather than conventional methods in the
 187 condition of a limited amount of training data?

188 3 Materials and Methods

189 3.1 Study Area and Data Acquisition

190 The study area in this study is shown in 1. Oyodo River is located in the Kyushu
 191 region of southwestern Japan, with a basin area of 2,230 km^2 and a length of 107 km .
 192 The source of the Oyodo River is Nakadake, and the river's main channel passes
 193 through the Miyakonojo Basin, mountainous areas, and the Miyazaki Plain. The
 194 river has caused damage from flooding 12 times between 1936 and 2005 due to rain-
 195 fall during the rainy season. The predicted flood site, Hiwatashi, is located in the
 196 middle reaches of the Oyodo River, 52 km from the source, and has a basin area
 197 of 861 km^2 . At Hiwatashi, the government set the river water level of 6 m as the
 198 flood warning level and 9.2 m as the flood hazard level to warn of flooding. We con-
 199 structed the data used for study validation from the river water level history of the
 200 Oyodo River, following the work of (Hitokoto et al., 2017). Extract flood events ex-
 201 ceeding 6 m from the river water level and precipitation data. One event should
 202 be from 72 hours before to 48 hours after the river water level peak. From 1990 to
 203 2014, we have constructed 23 flood events, of which four flood events (1990, 1993,
 204 2004, and 2005) had river water levels exceeding 9.2 m . We use fourteen rainfall sta-
 205 tions and four river water level stations around and upstream of the basin to obtain
 206 data for the same period. We obtained all data from the Water Information Sys-
 207 tem database of the Ministry of Land, Infrastructure, Transport, and Tourism in
 208 Japan (Ministry of Land, Infrastructure, Transport, and Tourism in Japan, 2021).

209 3.2 Conventional ANN for flood forecasting

210 This section describes the conventional ANN based on the work of Hitokoto et
 211 al. (2017). A schematic diagram illustrating flood forecasting with an ANN is pre-
 212 sented in Figure 2. The model takes three kinds of input data: river water levels at
 213 the forecast location, the river water level at the upstream location, precipitation in
 214 the basin, and outputs predicted river water levels. The river water level data for in-

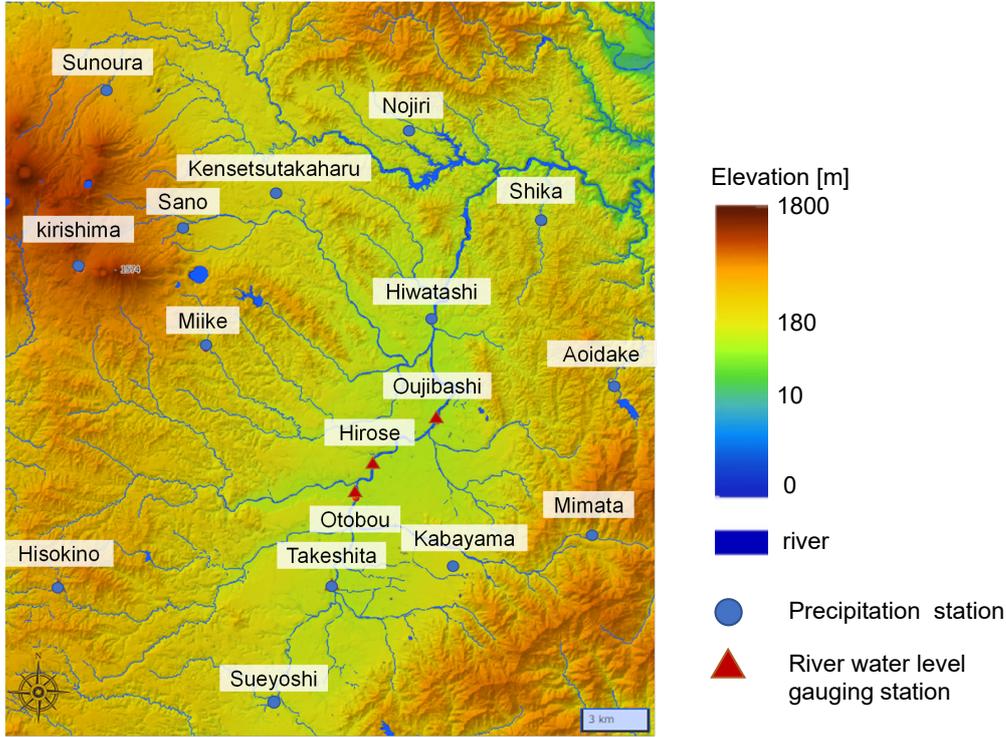


Figure 1. Location of the Hiwatashi gauging station, related rivers and near by stations. This map uses the data from standard elevation map published by Geospatial Information Authority of Japan and edited by NTT Advanced Technology Corporation.

215 put is hourly data for a certain period for the location of the flood forecast and its
 216 upstream locations. The input rainfall is the observed and predicted rainfall at mul-
 217 tiple locations in the basin. The ANN model comprises three fully connected layers,
 218 with ReLu activation functions applied to the first and second layers. We trained
 219 the ANN in two stages. As a pre-training step, the middle layers are optimized as
 220 denoising autoencoders. The denoising autoencoders have the same number of out-
 221 put variables as inputs, and it is trained to regenerate input from noise-added input.
 222 Next, the learning process is performed using the parameters optimized as denois-
 223 ing autoencoders as the initial values. In this learning process, the river water level
 224 and rainfall data are used as input data and river water level data are used as train-
 225 ing data. The river water level data is hourly data for a certain period at the flood
 226 forecasting location and upstream. The precipitation data are also hourly for a cer-
 227 tain period at multiple locations around the basin. This ANN is optimized to min-
 228 imize the mean squared error between the predicted and actual river water levels.
 229 Adam optimizer was used to update parameters. Dropouts were applied to avoid
 230 over-fitting. Learning stops after a predetermined number of epochs. The number of
 231 neurons in the middle layer, batch size, learning rate, dropout rate, and number of
 232 epochs are subject to hyperparameter tuning.

233 3.3 Prior knowledge and proposed INN architecture

234 We propose an INN integrating two prior knowledge into an ANN to prevent
 235 performance degradation on limited training data. The first knowledge is the rainfall-
 236 runoff and water level relationship. The rainfall refers to precipitation, especially
 237 in the basin to be forecasted, and runoff refers to the water moving over and un-

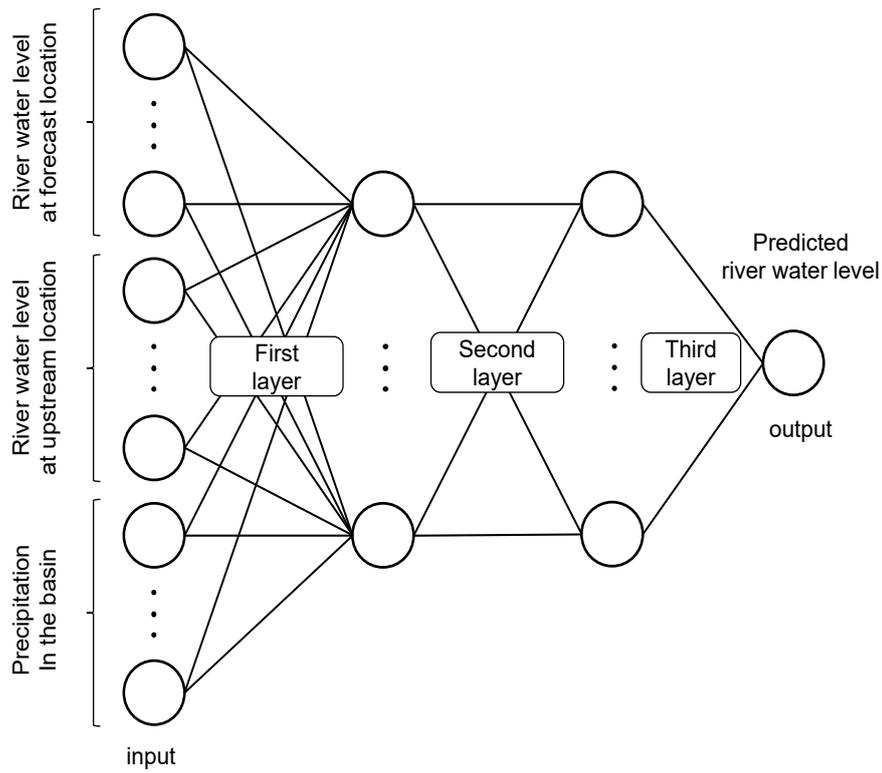


Figure 2. Architecture of conventional ANN. It has three middle layer and with multiple inputs and one output. The input includes river water level at forecast location, river level at upstream location and precipitation in the basin.

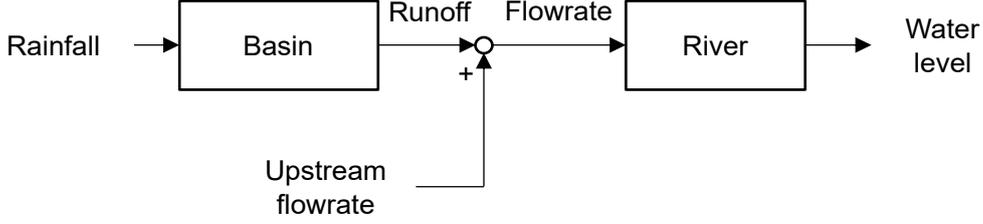


Figure 3. A block diagram showing the relationship between rainfall-runoff and water levels. Rainfall flows into the basin, merges with the upstream flow of the river, and affects water levels.

238 der the surface of the land in the basin area. Understanding this relationship and
 239 deriving flow rate into rivers is one of the significant interests of river engineering.
 240 Then, the rainfall-runoff and water level relationship can be understood as shown
 241 in the block diagram in Figure 3. First, rain falls on the basin, and the water flows
 242 upstream through various pathways. Next, the volume of water from the river up-
 243 stream is combined to form the river. This flow rate and physical shape define the
 244 water level at a point of the river. Integrating this prior knowledge into the ANN is
 245 performed by modifying the structure of the NN as shown in figure 4 to mimic the
 246 block diagram in figure 3. First, the network is divided into two parts. Part 1 is a
 247 NN that converts rainfall in a watershed to river flow. Part 2 is a NN that converts
 248 the amount of water from the basin to the river and the flow rate from upstream
 249 to the predicted water level. The inputs are the precipitation in the basin to Part 1
 250 and the river level upstream to Part 2. Part1 outputs three kinds of vector named
 251 ΔS , R , Q , and ΔS is the input to Part2. This network architecture modification
 252 aims to create a model that suits the task of flood forecasting.

253 The second piece of prior knowledge is the tank model. As mentioned above,
 254 the rainfall-runoff relationship is a significant issue in river engineering, and many
 255 models have been proposed to explain its behavior. The tank model simulates a
 256 basin as a tank and models the relationship between rainfall, basin storage, and
 257 runoff. In the tank model, rainfall is fed into the tank, some of it accumulates, and
 258 some water flows out as runoff. This model is one of the simplest rainfall-runoff
 259 models, and this tank model was chosen for its simplicity of integration into the
 260 INN. The tank model is composed of three variables, as follows:

$$261 \quad \Delta S(t) = R(t - \tau) + Q(t) \quad (1)$$

262 t is the time each value was observed. τ is the time delay between rainfall-runoff.
 263 $\Delta S(t)$ is water strage change in the tank(basin). $R(t - \tau)$ is precipitation with time
 264 delay. Q is the runoff flow rate. Equation 1 represents the relationship between rain-
 265 fall with time delay and conservation of tank storage and runoff. The integration
 266 of the tank model into the ANN is done in the following procedure. The output of
 267 Part 1, which is responsible for rainfall-runoff, is divided into the tank model vari-
 268 ables: rainfall R , tank storage change ΔS , and runoff Q . Next, add the penalty term
 269 $loss_{penalty}$ shown below to the loss function.

$$270 \quad loss_{penalty} = \sum_{i \in n} |\Delta S_i(t) - R_i(t - \tau) - Q_i(t)| \quad (2)$$

271 n is a predefined number of elements in each vector output from part 1. This is the
 272 just transition of the term $R(t - \tau)$ and $Q(t)$ in Equation 1 and when $loss_{penalty} = 0$
 273 Equation 2 is equivalent to Equation 1. And each outputs ΔS , R , Q in 4 are cor-
 274 responding to $\Delta S_i(t)$, $R_i(t - \tau)$, $Q_i(t)$ in Equation 2. Since this penalty term is

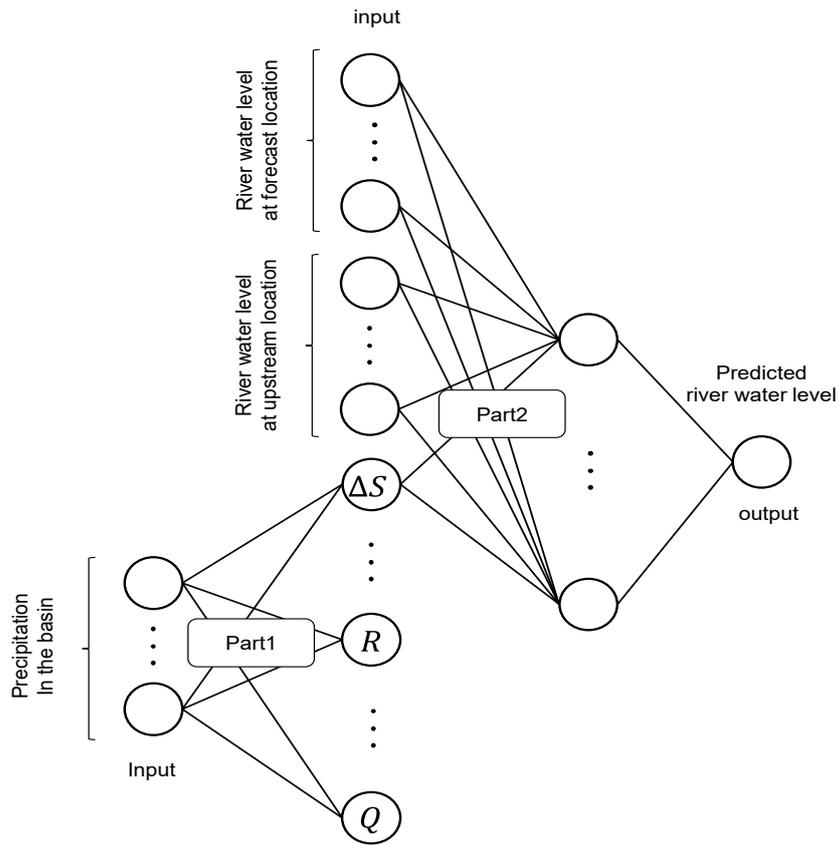


Figure 4. The proposed INN architecture. It is designed to simulate the relationship between rainfall-runoff and water levels. This architecture has two parts: Part1 and Part2. Part1 has precipitation input, and Part2 has Part1 output and water level input.

275 optimized to be zero during the learning process, it is expected that Part 1 will be
 276 optimized to mimic the behavior of the tank model. Moreover, since $\Delta S(t)$ is de-
 277 fined as having a linear relationship with the amount of runoff to the river, $\Delta S(t)$
 278 of Part 1 in Figure 4 is input to Part 2. Note that these two changes are not math-
 279 ematically complete constraints that satisfy the tank model and rainfall-runoff rela-
 280 tionship. Thus the output of Part 1 need not match the values of each variable when
 281 the tank model is built for the same basin. Same as conventional ANN, the number
 282 of neurons in the middle layer, batch size, learning rate, dropout rate, and number
 283 of epochs are subject to hyperparameter tuning.

284 3.4 Model Development

285 The same gauging and perception data are used for the ANN and the devel-
 286 opment of the proposed INN. ANN and INN were optimized to minimize the mean
 287 squared error of training data. The model is trained with the water level at time
 288 $t + n$, n hours ahead of the Hiwatashi gauging station at time t , as the objective
 289 value. The inputs to the model are the water level at Hiwatashi gauging station at
 290 time t and one hour ahead at time $t - 1$, the water level upstream at time $t, t - 1, t - 2$
 291 and the hourly rainfall from $t + n - 1$ to $t + n - 5$ at the precipitation gauging
 292 location. Note that the actual rainfall values are used to train and test even if the
 293 rainfall values are in the future from time t . The Adam optimizer was used in the
 294 training process for each model. Hyperparameter tuning is performed by grid search
 295 for the number of training epochs, the number of neurons in the middle layer, the
 296 learning rate, and the dropout rate. The data used for development is divided into
 297 training data and validation data for hyperparameter tuning, which are separated
 298 from test data.

299 4 Result

300 Two comparisons were conducted to compare the INN and some conventional
 301 methods. The results were evaluated in terms of RMSE. The RMSE is obtained by
 302 the following,

$$303 \quad RMSE = \sqrt{\frac{1}{N} \sum_t (L(t) - L_{prediction}(t))^2} \quad (3)$$

304 N is the number of water level samples. $L(t)$ is the water level at time t , $L_{prediction}$
 305 is the predicted water level at time t .

306 4.1 Comparison with conventional methods for a sufficient amount 307 of training data

308 The result of the conventional ANN and the proposed method forecast for the
 309 Hiwatashi gauging station is shown in Figure 5 and Figure 6 The prediction results
 310 follow the transition of the ground truth. During periods of water level over three
 311 meters (between two gray dashed lines), the predictions are more consistent with
 312 the ground truth than the results of ANN in case of the year 2004 and 2005. Both
 313 the ANN and the INN predictions are unstable in the year 1990 and 1993. These
 314 unstable predictions may be due to noise in the input observed variables in these
 315 test sets.

316 The RMSE of the flood forecast results at the Hiwatashi gauging station is
 317 shown in Figure 7. Conventional methods are ANN, a hybrid of ANN and distributed
 318 runoff model (hybrid), distributed runoff model (runoff), embedding, and the pro-
 319 posed method. In addition, ANN1 is the result traced from Hitokoto et al. (2017),
 320 and ANN2 is the result of in-house code. The difference between ANN1 and ANN2

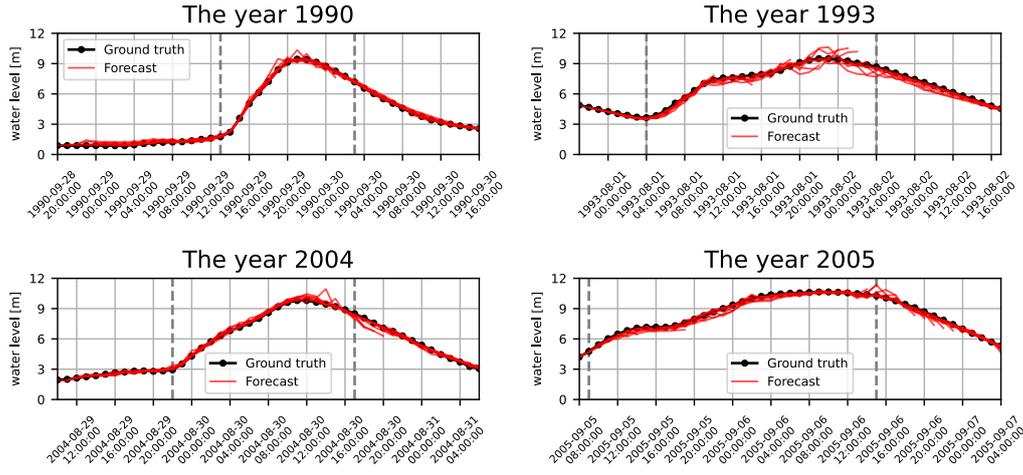


Figure 5. Forecast for the Hiwatashi gauging station in the year 1990, 1993, 2004, and 2005 by conventional ANN2 model. The black points with black lines denote the observed river level as ground truth, and the red solid line shows the forecast river level up to 6 hours ahead. The area between the two gray dotted lines displays the range of data over which the RMSE was evaluated.

321 is that it uses a framework for implementation, and hyperparameter tuning is per-
 322 formed on a test set and a separate validation set. Figure 7 -(a), (b), (c), and (d)
 323 show the results for 1990, 1993, 2004, and 2005. The RMSE for ANN1, hybrid, runoff,
 324 and embedding is traced from Hitokoto et al. (2017) and Okuno et al. (2021). Each
 325 figure shows the RMSE of the predicted and actual values for the 1 to 6 hourly fore-
 326 cast horizons. Each method's RMSE is distributed in the 0.04 *m* to 1.2 *m* range. In
 327 the case of the proposed method, the values are distributed in the range of 0.038 *m*
 328 to 0.85 *m*, and it was never the worst accuracy in all cases. In case (a) Year 1990,
 329 the RMSE proposed becomes large when forecasting 5 hours, but in all other years,
 330 the RMSE is about the same compared to other methods. Unlike other results, the
 331 proposed method and ANN2 are hyperparameter-tuned with a test set and a com-
 332 pletely isolated validation set. Considering this difference in experimental conditions,
 333 the proposed method has sufficient performance. Based on this result, the domain
 334 knowledge which was combined with INN does not cause performance degradation
 335 even in the condition of not limited training data.

336 4.2 Sensitivity analysis about the number on the flood data in the 337 training data

338 The proposed method should maintain high performance even under condi-
 339 tions where there is not a sufficient amount of data. To verify the performance of
 340 INN under such conditions, we performed a sensitivity analysis. The RMSE at the
 341 Hiwatashi gauging station with different test data is shown in Figure 8 and Figure
 342 9. We compared the conventional method (ANN2) and the proposed method in this
 343 study. Each figure shows the result for 1993 and 2004. In Figure 8, for (a)1 hour
 344 forecast and (b)3 hours forecast, the RMSE of INN does not increase as the number
 345 of flood events in the training data decreases. On the other hand, in conventional
 346 ANN2, the RMSE tends to rise rapidly as the number of flood data becomes smaller.
 347 The RMSE value of Proposed is smaller than that of ANN2 when the training set
 348 has less number of flood data ($6 >$). In the (c)6 hours forecast, the magnitude of

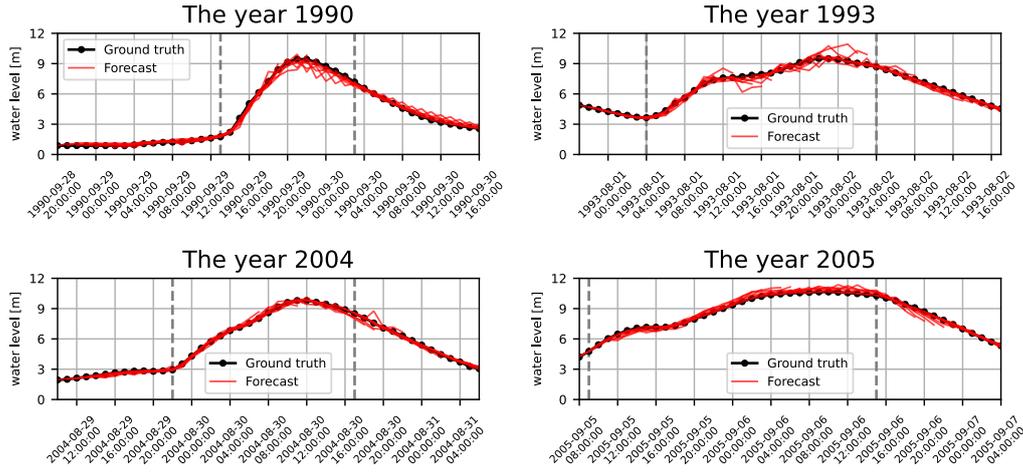


Figure 6. Forecast for the Hiwatashi gauging station in the year 1990, 1993, 2004, and 2005 by proposed INN model. The black points with black lines denote the observed river level as ground truth, and the red solid line shows the forecast river level up to 6 hours ahead. The area between the two gray dotted lines displays the range of data over which the RMSE was evaluated.

349 Proposed RMSE changes more than in (a) and (b) for the number of flood data.
 350 Under conditions where the number of flood data is five or less, three-quarters of the
 351 cases have a smaller RMSE than ANN2. The result in Figure 9 has the same trend
 352 as in Figure 8. The RMSE value of Proposed is smaller than that of ANN2 when the
 353 training set has less number of flood data ($5 >$). In the (c)6 hours forecast, the mag-
 354 nitude of Proposed RMSE changes more than in (a) and (b) for the number of flood
 355 data. Same as Figure 8, under conditions where the number of flood data is five or
 356 less, three-quarters of the cases have a smaller RMSE than ANN2.

357 5 Discussion and Conclusion

358 In this study, we proposed a novel approach to flood forecasting methods with
 359 NNs. The proposed method is an INN that integrates existing knowledge of rainfall-
 360 runoff, river-level relationships, and the tank model in river engineering with con-
 361 ventional ANNs. Integrating the existing knowledge into the INN was performed by
 362 modifying the network architecture and adding a penalty term. These two changes
 363 aim to improve the initial conditions and the learning process of NNs. We applied
 364 the proposed INN to a real-world river in Japan to test its performance. Under con-
 365 ditions where there was sufficient training data, the proposed INN was performed,
 366 as well as several critical conventional methods. When the training data was lim-
 367 ited, it significantly outperformed the conventional ANN. This difference tended to
 368 increase as the forecast horizon became small. The improvement in results is due to
 369 changes in the network architecture based on existing knowledge and the addition of
 370 a penalty term. This change is assumed to be due to the initial learning conditions
 371 and the optimizer's contribution to improving the learning process. These results are
 372 a new contribution that shows a practical way to improve the accuracy of INNs with
 373 a limited amount of training data. The proposed INN will enable the provision of
 374 flood forecasting systems with a short development time in areas where flood fore-
 375 casting has not been installed, thereby reducing the risk to life during floods. INN

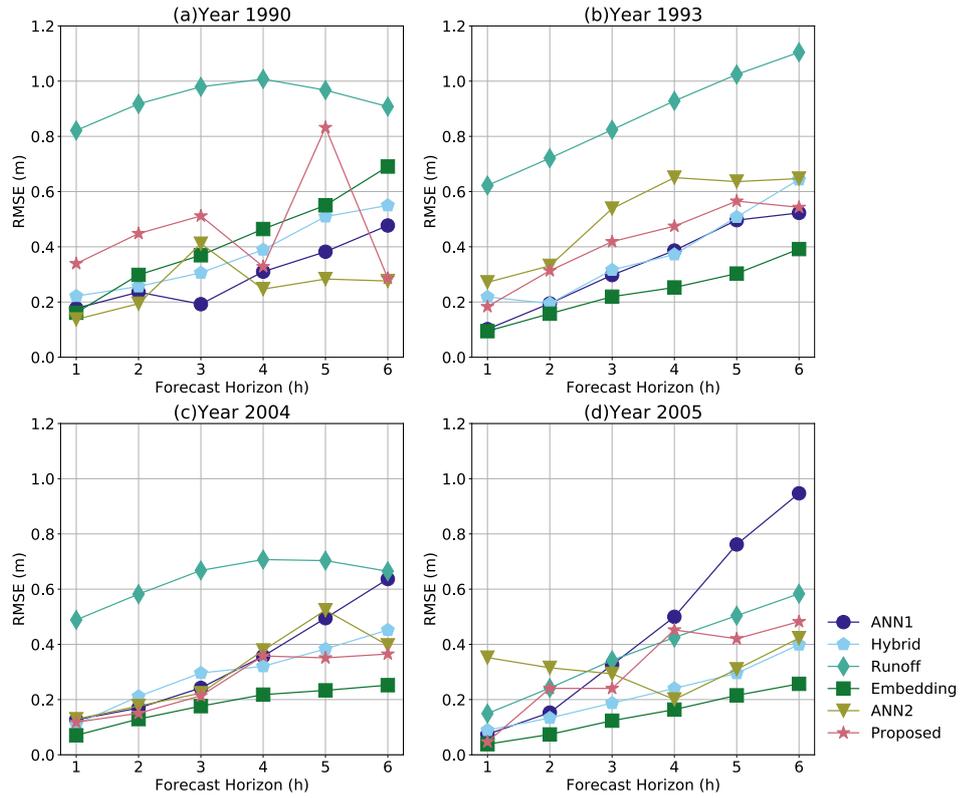


Figure 7. RMSEs of 1 to 6-hour forecasts for 4 test cases (a)year 1990,(b) year 1993,(c)year 2004, and (d)year 2005. We compared the performance of the proposed method with that of ANNs from the literature (ANN1), the distributed runoff-rainfall model (runoff), the hybrid model of ANN and runoff (hybrid), predictions based on dynamical system theory (embedding), and the performance of ANNs based on in-house experimental codes (ANN2). Note that the results for ANN1, runoff, hybrid, and embedding were scanned for values from Hitokoto et al. (2017) and Okuno et al. (2021)

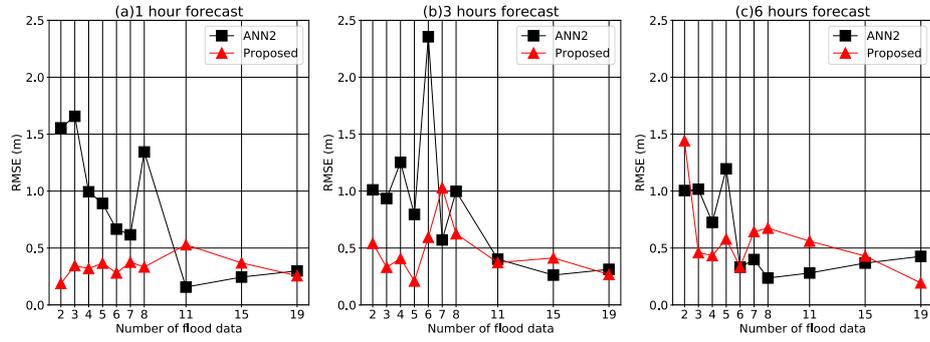


Figure 8. RMSE for 1993 test data versus the number of flood data in the training data set. The red line is the proposed method, and the black line is the conventional ANN with in house implementation (ANN2).

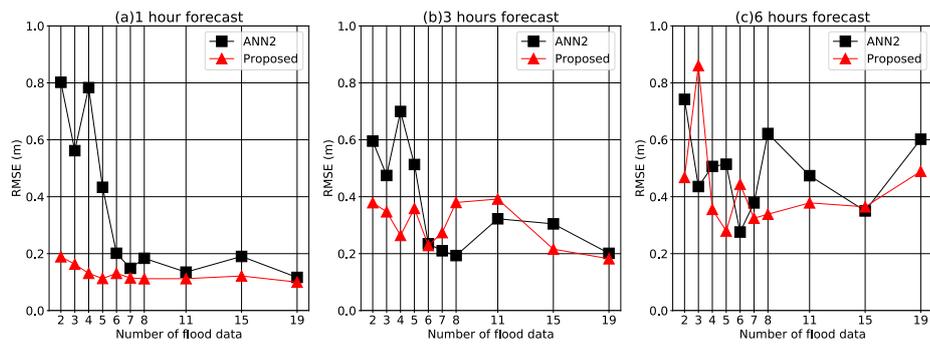


Figure 9. RMSE for 2004 test data versus the number of flood data in the training data set. The red line is the proposed method, and the black line is the conventional ANN with in house implementation (ANN2).

376 will help to cope with heavy rainfall in unprecedented areas due to recent climate
377 change. Overall, we obtained favorable results for the questions set in section 2.

378 The future work of this research is the following two. First, the INN proposed
379 in this study was designed to integrate two simple pieces of existing knowledge for
380 ease of implementation. Therefore, the performance when other existing knowledge
381 is integrated has yet to be discovered, and what kind of existing knowledge is more
382 suitable for integration is an important question. Second, the river tested in this
383 study is the only one in Japan, and its performance in other Japanese rivers and
384 rivers around the world with larger basins is still being determined. So, evaluation of
385 the proposed INN on more diverse rivers is necessary. In addition, the performance
386 of the proposed technology for more complex phenomena where factors other than
387 rainfall affect floods is also the subject of future research.

388 6 Open Research Section

389 The rainfall and river water level data used in this study are freely available at
390 (Ministry of Land, Infrastructure, Transport, and Tourism in Japan, 2021)(<http://www1.river.go.jp/>).
391 The data is freely accessible, but you must select a location and time period. Re-
392 lated metadata (location name and time period) is listed in (Hitokoto et al., 2017).
393 The elevation map data is freely available at (Geospatial Information Authority of
394 Japan, 2020)(<https://maps.gsi.go.jp/vector/#7>).

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