



- 18 • Our estimation of ring-fault parameters of an earthquake at the Sierra Negra caldera yields results  
19 consistent with geodetic observations.

20 **Abstract**

21 Large earthquakes ( $M_w > 5$ ) with moment tensors (MTs) dominated by a vertical  
22 compensated-linear-vector-dipole (vertical-CLVD) component are often generated by dip slip along a  
23 curved ring-fault system at active volcanoes. However, relating their MTs to ring-fault parameters has  
24 proved difficult. The objective of this study is to find a robust way of estimating ring-fault parameters  
25 based on their MT solutions obtained from long-period seismic records. We first model the MTs of  
26 idealized ring-faulting and show that an MT component representing the vertical dip-slip mechanism is  
27 indeterminate from long-period seismic waves owing to a shallow source depth, whereas the other MT  
28 components representing the vertical-CLVD and vertical strike-slip mechanisms are resolvable. We  
29 then propose a new method for estimating the arc angle and orientation of ring-faulting using the two  
30 resolvable MT components. For validation, we study a vertical-CLVD earthquake that occurred during  
31 the 2005 volcanic activity at the Sierra Negra caldera, Galápagos Islands. The resolvable MT  
32 components are stably determined from long-period seismic waves, and our estimation of the ring-fault  
33 parameters is consistent with the ring-fault geometry identified by previous geodetic studies and field  
34 surveys. We also estimate ring-fault parameters of two earthquakes that took place during the 2018  
35 activity at the caldera, revealing significant differences between the two earthquakes in terms of slip  
36 direction and location. These results show the usefulness of our method for estimating ring-fault  
37 parameters of vertical-CLVD earthquakes, enabling us to examine the kinematics and structures below  
38 active volcanoes with ring faults that are distributed globally.

## 39 **1 Introduction**

40           Seismological methods can be used for the study of active volcanoes to investigate geometries  
41 of subsurface structures and the physics of fluid transport into the magma plumbing system.  
42 Observations and analyses of shallow earthquakes with volcanic origins provide information on stress  
43 levels in volcanic edifices caused by magmatic pressures ascending from depth. This information is  
44 important for predicting eruptions and assessing hazards related to volcanic activity (e.g., McNutt,  
45 2002; Chouet, 2003; Kawakatsu and Yamamoto, 2015). In most cases, small earthquakes are analyzed  
46 with in situ or near-field observations to infer detailed dynamics of magma transport or brittle fractures  
47 of volcanoes; for example, Kilauea in Hawaii or Bárðarbunga in Iceland. In contrast, larger volcanic  
48 earthquakes are sometimes recorded by regional and global seismic networks (e.g., Kanamori and  
49 Given, 1982; Kanamori et al., 1982; Kanamori and Mori, 1992; Ekström, 1994; Shuler et al., 2013a). If  
50 seismic signals radiated by such earthquakes can be utilized, it is possible to study volcanoes distributed  
51 globally, including those on remote islands or underwater without local observation systems. These  
52 include the submarine Smith caldera, south of Japan, which causes volcanic earthquakes with seismic  
53 magnitudes of  $>5$  (e.g., Kanamori et al., 1993; Fukao et al., 2018; Sandanbata et al., 2018), and  
54 submarine volcanic areas near Mayotte Island in the Comoro Islands, which showed significant  
55 seismicity during 2018–2019 (Cesca et al., 2020; Darnet et al., 2020).

56           One of the most notable types of volcanic earthquake observed at regional or global scales are  
57 those with seismic magnitudes of  $M_w > 5$  that are characterized by moment tensors (MTs) having a  
58 dominant vertical compensated-linear-vector-dipole (vertical-CLVD) component (e.g., Kanamori et al.,

59 1993; Ekström, 1994; Shuler et al., 2013a; 2013b). There are two types of vertical-CLVD earthquake:  
60 one contains a dominant tension axis (vertical-T CLVD earthquakes), and the other contains a dominant  
61 pressure axis (vertical-P CLVD earthquakes) (e.g., Ekström, 1994; Shuler et al., 2013a; 2013b) (Figure  
62 1). Vertical-CLVD earthquakes cannot be explained by shear rupture on a planar fault (e.g., Frohlich,  
63 1994; Ekström, 1994; Shuler et al., 2013b), indicating that their anomalous mechanisms are associated  
64 with complex source structures or magmatic processes. For vertical-CLVD earthquakes at volcanoes,  
65 several models have been proposed, including ring-faulting (e.g., Ekström, 1994), rapid water–magma  
66 interaction initiated by magma intrusion into shallow crust (Kanamori et al., 1993), and opening or  
67 closing of a horizontal crack (e.g., Riel et al., 2015; Fukao et al., 2018).

68         Among the different proposed source models, the ring-faulting mechanism explains many  
69 features of vertical-CLVD earthquakes (e.g., Ekström, 1994; Shuler et al., 2013a; 2013b). Ekström  
70 (1994) showed that MT analyses of long-period seismic signals that are radiated by pure dip slips on a  
71 curved ring fault result in vertical-CLVD focal mechanisms. Shuler et al. (2013a, 2013b) surveyed  
72 vertical-CLVD earthquakes near volcanoes from 1976 to 2009 and located their centroids within the top  
73 10 km of the crust, which is consistent with the formation process of ring faults during caldera collapse  
74 (e.g., Cole et al., 2005; Acocella, 2007; Geyer and Martí, 2014). Those authors showed that most  
75 vertical-CLVD earthquakes were temporally associated with activity at nearby volcanoes with caldera  
76 structures. Vertical-CLVD earthquakes near Bárðarbunga in Iceland and Nyragongo in the Democratic  
77 Republic of the Congo have also been attributed to slips on non-planar ring faults (e.g., Gudmundsson  
78 et al., 2016; Parks et al., 2017; Nettles and Ekström, 1998; Shuler and Ekström, 2009). The recurrence

79 of vertical-CLVD earthquakes at two shield volcanoes showing pronounced surface deformation or  
80 micro-seismicity along well-documented ring-fault structures has indicted their origins related to  
81 ring-faulting at the Rabaul caldera in Papua New Guinea (e.g., McKee et al., 1984; Mori and McKee,  
82 1987; Mori et al., 1989; Shuler et al., 2013b) and the Sierra Negra caldera in the Galápagos Islands (e.g.,  
83 Amelung et al., 2000; Yun et al., 2006; Yun, 2007; Jónsson, 2009).

84 MT inversion using long-period seismic waves has been applied to study the sources of  
85 vertical-CLVD earthquakes from far-field observations (e.g., Shuler et al., 2013b; Duputel and Rivera,  
86 2019; Fontaine et al., 2019). Because of long-period properties, detailed 3D velocity structures of the  
87 volcanic edifices are not required. MT solutions of ring-faulting are known to reflect the properties of  
88 earthquake sources, such as the kinematics of a central block and the dip directions of a ring fault. As  
89 illustrated in Figure 1, when the central block moves upward on the inward-dipping ring fault (Figure  
90 1a), or downward on the outward-dipping ring fault (Figure 1b), vertical-T CLVD earthquakes are  
91 produced; in contrast, if the kinematics of the block are reversed, vertical-P CLVD earthquakes are  
92 produced (Figure 1c and d). Hence, the polarity of the MT solutions (vertical-T or -P) helps to  
93 determine either the kinematics of the central block (upward or downward) or the dip direction of the  
94 ring fault (inward or downward), once either of the two is constrained from other observations such as  
95 crustal deformation or micro-seismicity (e.g., Shuler and Ekström, 2009; Gudmundsson et al., 2016).

96 However, it has proved challenging to relate MT solutions obtained from long-period seismic  
97 waves directly to ring-fault parameters such as arc angle, dip angle, and the location of slip along the  
98 ring fault. One of the reasons for the difficulty is that amplitudes of radiated long-period seismic waves

99 are reduced owing to partial cancellations of long-period seismic waves from different portions of a ring  
100 fault (Ekström, 1994). Another reason is the instability of MT inversion for shallow earthquakes (e.g.,  
101 Dziewonski et al., 1981; Kanamori and Given, 1981). Although Shuler et al. (2013b) related MT  
102 solutions obtained from long-period seismic records to ring-fault parameters using the plunge of the  
103 tension or pressure axis and a parameter representing the dominance of the non-double-couple  
104 component, their estimations were not always consistent with those observed in nature or in analog  
105 models. Contreras-Arratia and Neuberg (2020) showed that detailed ring-fault parameters can be  
106 recovered from near-field seismic stations with good azimuth coverage. However, once reliable  
107 relationships between ring-fault parameters and MT solutions obtained from long-period seismic  
108 records are established, MT inversion will be a more powerful tool to remotely study the kinematics and  
109 subsurface structures of active volcanoes distributed globally that cause ring-faulting.

110         The objective of this study is to find a robust way of estimating ring-fault parameters using the  
111 MT solutions of vertical-CLVD earthquakes. We first model theoretical MTs of idealized ring-faulting  
112 with variable ring-fault parameters and decompose them into MT components. Although the MT  
113 component representing the vertical dip-slip mechanism is difficult to determine with long-period  
114 seismic waves, we show that the remaining MT components can be used to estimate some ring-fault  
115 parameters. To validate the theoretical argument, we estimate the ring-fault parameters of  
116 vertical-CLVD earthquakes at the Sierra Negra caldera by investigating their resolvable components of  
117 MT solutions determined with long-period seismic waves and then compare the estimated parameters  
118 with those identified in previous studies using geodetic observations and field surveys. We also discuss

119 possible bias in MT inversion caused by a seismic source with a volume change close to the  
120 ring-faulting.

## 121 **2 Analysis**

### 122 2.1 Modeling and decomposition of moment tensors of ring-faulting

123 In this section, we theoretically explore robust relationships between MTs and ring-fault  
124 parameters. We define several ring-fault parameters, namely, the arc angle  $\theta$ , the midpoint of the  
125 ruptured arc segment  $M$ , the ring-fault azimuth  $\overrightarrow{OM}$ , and the ring-fault orientation (Figure 2). The  
126 ring-fault orientation is normal to the ring-fault azimuth vector. The azimuth can vary from  $0^\circ$  to  $360^\circ$ ,  
127 whereas the orientation can vary only from  $0^\circ$  to  $180^\circ$ .

128 Here we model theoretical MTs of ring-faulting in a similar way to Ekström (1994) and Shuler  
129 et al. (2013b). We discretize a curved ring fault into planar rhomboidal subfaults and define the MT of  
130 ring-faulting as the sum of the MTs of each subfault (Box 4.4 in Aki and Richards, 1980). As a ring fault  
131 is smaller than the wavelength, and the source time duration is shorter than the wave period of the  
132 long-period seismic waves that we use, the point-source approximation is valid. Here we consider  
133 idealized ring-faulting for a vertical-T CLVD mechanism: a reverse slip of 1 m along a circular  
134 inward-dipping ring fault (5 km radius at the surface) that extends from the surface to a depth of 2 km.  
135 We vary two ring-fault parameters, that is, the dip angle ranging from  $45^\circ$  to  $90^\circ$ , and the arc angle  
136 ranging from  $0^\circ$  to  $360^\circ$  (Figure 2a). Only vertical-T earthquakes are discussed here because MTs of  
137 vertical-P earthquakes can be examined by changing the signs of the MTs.

138 The scalar moment of the theoretical MTs is computed by following the definition given by  
 139 Silver and Jordan (1982) and Dahlen and Tromp (1998):

$$140 \quad M_0 = \sqrt{\sum_{ij} M_{ij} M_{ij} / 2}, \quad (1)$$

141 where  $M_{ij}$  are the  $ij$  elements of an MT in spherical coordinates ( $r$ ,  $\theta$ , and  $\phi$ ) representing up, south,  
 142 and east, respectively. The moment magnitude is computed as:

$$143 \quad M_w = \frac{2}{3} (\log_{10} M_0 - 9.10). \quad (2)$$

144 with  $M_0$  being measured in N m (e.g., Kanamori, 1977; Hanks and Kanamori, 1979).

145 We next decompose the theoretical MTs in a similar way to Kawakatsu (1996). For the  
 146 decomposition, we define three moment scales corresponding to isotropic (*ISO*), vertical-CLVD  
 147 (*CLVD*), and difference (*D*) components with the three diagonal elements ( $M_{rr}$ ,  $M_{\theta\theta}$ , and  $M_{\phi\phi}$ ):

$$148 \quad M_{ISO} = \frac{1}{3} (M_{rr} + M_{\theta\theta} + M_{\phi\phi}), \quad (3)$$

$$149 \quad M_{CLVD} = \frac{1}{3} (2M_{rr} - M_{\theta\theta} - M_{\phi\phi}), \quad (4)$$

150 and

$$151 \quad M_D = \frac{1}{2} (M_{\theta\theta} - M_{\phi\phi}). \quad (5)$$

152 Note that for the MT of ring-faulting, no isotropic component is contained ( $M_{ISO} = 0$ ). Hence, using the  
 153 two moment scales ( $M_{CLVD}$  and  $M_D$ ) and the non-diagonal elements ( $M_{r\theta}$ ,  $M_{r\phi}$ , and  $M_{\theta\phi}$ ), the MT of  
 154 ring-faulting can be uniquely decomposed into three deviatoric MT components in the following form:

155  $\mathbf{M} = \mathbf{M}_{CLVD} + \mathbf{M}_{SS} + \mathbf{M}_{DS}, \quad (6)$

156 where

157  $\mathbf{M}_{CLVD} = M_{CLVD} \begin{bmatrix} 1 & & \\ 0 & -0.5 & \\ 0 & 0 & -0.5 \end{bmatrix}, \quad (7)$

158  $\mathbf{M}_{SS} = \mathbf{M}_D + \mathbf{M}_{\theta\phi} = M_D \begin{bmatrix} 0 & & \\ 0 & 1 & \\ 0 & 0 & -1 \end{bmatrix} + M_{\theta\phi} \begin{bmatrix} 0 & & \\ 0 & 0 & \\ 0 & 1 & 0 \end{bmatrix}, \quad (8)$

159 and

160  $\mathbf{M}_{DS} = \mathbf{M}_{r\theta} + \mathbf{M}_{r\phi} = M_{r\theta} \begin{bmatrix} 0 & & \\ 1 & 0 & \\ 0 & 0 & 0 \end{bmatrix} + M_{r\phi} \begin{bmatrix} 0 & & \\ 0 & 0 & \\ 1 & 0 & 0 \end{bmatrix}. \quad (9)$

161 The three components  $\mathbf{M}_{CLVD}$ ,  $\mathbf{M}_{SS}$ , and  $\mathbf{M}_{DS}$  represent different source types, which are the  
 162 vertical-CLVD (*CLVD*), vertical strike-slip (*SS*), and vertical dip-slip (*DS*) components, respectively  
 163 (Figure 2b). The sign of  $M_{CLVD}$  in Equation (7) depends on the type of vertical-CLVD earthquake:  
 164  $M_{CLVD} > 0$  for vertical-T earthquakes, and  $M_{CLVD} < 0$  for vertical-P earthquakes.

165 Using absolute values defined by  $|M_{CLVD}|$ ,  $M_{SS} = \sqrt{M_D^2 + M_{\theta\phi}^2}$ , and  $M_{DS} = \sqrt{M_{r\theta}^2 + M_{r\phi}^2}$ , we

166 can quantify the ratios of the *CLVD*, *SS*, and *DS* components in the MT of ring-faulting as:

167  $\frac{|M_i|}{|M_{CLVD}| + M_{SS} + M_{DS}} \times 100 \text{ [%]}, \quad (10)$

168 where  $i$  represents *CLVD*, *SS*, or *DS*.

169 Figures 2c and 2d show the theoretical MTs and components for reverse slips on ring faults with  
 170 dip angles of  $60^\circ$  and  $75^\circ$  that extend along azimuthal arc angles of  $90^\circ$ ,  $180^\circ$ ,  $270^\circ$ , and  $360^\circ$  (2nd–5th

171 rows, respectively). The ring-fault azimuths are  $0^\circ$ . For comparison, MTs of slips on planar faults with  
 172 the same dip angles are shown (1st row). Ring-faulting has a vertical-CLVD mechanism, as long-period  
 173 seismic contributions from different segments along the curved ring fault partially cancel out (Ekström,  
 174 1994). The geometric cancellation can be understood with the decomposition of theoretical MTs. The  
 175 | azimuths of principal axes for the two double-couple components,  $\mathbf{M}_{SS}$  and  $\mathbf{M}_{DS}$ , are determined by  
 176 the strike angle of a planar fault (1st row). Hence, the double-couple components from a portion of the  
 177 ring fault cancel out those from another portion striking in a different azimuth. In contrast, as the *CLVD*  
 178 | component,  $\mathbf{M}_{CLVD}$ , of a planar fault does not change with its strike angle, the component of the ring  
 179 fault accumulates and becomes more dominant in the moment tensor as the arc angle increases.

## 180 2.2 Indeterminate *DS* component at a shallow source depth

181       Once the MT solutions of ring-faulting are determined, the ring-fault parameters, namely, dip  
 182 angle, arc angle, and ring-fault azimuth (Figure 2a), can be estimated from the ratios of the three  
 183 components and azimuths of the principal axes of the *SS* and *DS* components. However, the *DS*  
 184 component of such shallow earthquakes is known to be indeterminate with MT inversion using  
 185 long-period seismic waves (e.g., Dziewonski et al., 1981; Kanamori and Given, 1981). The  
 186 indeterminacy of the *DS* component of shallow earthquakes arises from its small contribution to  
 187 | long-period seismic waves, as the  $r\theta$  and  $r\phi$  elements of the strain tensor ( $\varepsilon_{r\theta}$  and  $\varepsilon_{r\phi}$ ) are nearly  
 188 zero near the solid surface. To confirm the indeterminacy of the *DS* component at a shallow depth, we  
 189 synthesize long-period (0.005–0.0125 Hz) seismic waveforms, including all of the relevant phases (e.g.,  
 190 P, S, and surface waves), at a virtual station from five hypothetical sources representing elementary

191 components,  $\mathbf{M}_{CLVD}$ ,  $\mathbf{M}_D$ ,  $\mathbf{M}_{\theta\phi}$ ,  $\mathbf{M}_{r\theta}$ , and  $\mathbf{M}_{r\phi}$ , with the same scalar moment  $M_0 = 1.0 \times 10^{18}$  N m  
 192 ( $M_w$  5.9) using Equation (1) (Figure 3). Details of the numerical method used are described in the  
 193 caption of Figure 3. For a source at 2.5 km depth, amplitudes of long-period seismic waves radiated  
 194 from the *DS* component ( $\mathbf{M}_{r\theta}$ ,  $\mathbf{M}_{r\phi}$ ) are much smaller than those from the *CLVD* component ( $\mathbf{M}_{CLVD}$ )  
 195 and the *SS* component ( $\mathbf{M}_D$ ,  $\mathbf{M}_{\theta\phi}$ ) (Figure 3a). Because of the inefficient seismic excitation, estimation  
 196 of the *DS* component is unstable. Also, small errors in the depth of the source result in large  
 197 uncertainties in the *DS* components owing to large variations in the amplitudes of synthetic long-period  
 198 seismic waves. If the source is at 10.5 km depth, the *DS* component radiates larger seismic waves  
 199 (Figure 3b).

200 The difficulty in determining the *DS* component of shallow earthquakes is encountered in MT  
 201 inversion of tectonic earthquakes and leads to large uncertainties in the estimation of dip angle and  
 202 seismic magnitude (e.g., Dziewonski et al., 1981; Kanamori and Given, 1981). Similarly, the  
 203 indeterminacy makes it difficult to estimate important ring-fault parameters from long-period seismic  
 204 waves. The dip angle and scalar moment of ring-faulting cannot be well constrained. In addition, we  
 205 cannot determine the ring-fault azimuth, which is reflected in the azimuth of the tension axis of the *DS*  
 206 component.

### 207 2.3 Resolvable MTs of ring-faulting

208 Given the indeterminacy of the *DS* component, we propose a method for estimating two  
 209 ring-fault parameters using only the *CLVD* and *SS* components, which are resolvable with long-period

210 seismic waves. Here we define the resolvable MT ( $\mathbf{M}_{res}$ ) by:

$$211 \quad \mathbf{M}_{res} = \mathbf{M}_{CLVD} + \mathbf{M}_{SS}. \quad (11)$$

212  $\mathbf{M}_{res}$  for the idealized ring-faulting is shown in the 6th column in Figures 2c and 2d. Here, we  
 213 introduce two new dimensionless physical parameters extracted from  $\mathbf{M}_{res}$ , as follows. The first  
 214 parameter,  $k_{CLVD}$ , is the ratio of  $|M_{CLVD}|$  to  $|M_{CLVD}| + M_{SS}$  of  $\mathbf{M}_{res}$  defined by:

$$215 \quad k_{CLVD} = \frac{|M_{CLVD}|}{|M_{CLVD}| + M_{SS}} \times 100 [\%], \quad (12)$$

216 which we call the *CLVD ratio*. This parameter can be used to estimate the ring-fault arc angle  $\theta$   
 217 (Figure 4a). As  $\theta$  increases from  $0^\circ$  to  $180^\circ$ ,  $k_{CLVD}$  increases from 66.7% to 100%. From  $\theta = 180^\circ$ ,  
 218  $k_{CLVD}$  decreases to a local minimum of 90% at  $\sim 255^\circ$ , and then increases to 100% at  $360^\circ$ .  $k_{CLVD}$   
 219 reaches 100% when  $\theta$  is  $180^\circ$  or  $360^\circ$ , where the *SS* component vanishes. The relationship between  
 220  $k_{CLVD}$  and  $\theta$  does not depend on the dip angle because pure dip slip on a planar fault with any dip  
 221 angle in all cases results in the same *CLVD*-to-*SS* component ratio of 2:1 (top row in Figures 2c and 2d).  
 222 Thus, we can use  $k_{CLVD}$  to estimate  $\theta$  even if the *DS* component is indeterminate.

223 The second parameter,  $\psi$ , is defined as follows. The resolvable moment tensor  $\mathbf{M}_{res}$  discussed  
 224 here is given by three orthogonal dipoles. We use the orientation of the dipole with the smallest absolute  
 225 moment to estimate the orientation of the ring fault. As shown in Figures 2c and 2d (4th column), this  
 226 dipole determines the elongation direction of the nodal-line pattern of the mechanism diagrams of  $\mathbf{M}_{res}$ .  
 227 It can also be shown that this orientation is the same as the orientation of the Null (N) axis of the  
 228 *best-fitting double-couple moment tensor* (pp. 248–251 of Shearer, 2009) shown by thin curves on the

229 mechanism diagrams (4th column of Figures 2c and 2d). We refer to the dipole axis as the *N-axis* and  
 230 denote its orientation by  $\psi$ , which is measured from the north, eastward-reckoned positive,  $0 \leq \psi <$   
 231  $180^\circ$ . Figures 4b and 4c show the relationships between the ring-fault orientation and the N-axis for  
 232 vertical-T and vertical-P CLVD earthquakes. The ring-fault orientation is parallel or perpendicular to  
 233 the N-axis depending on  $\theta < 180^\circ$  or  $\theta > 180^\circ$ , respectively. Because  $\psi$  is independent of the dip  
 234 angle, this parameter can be used to estimate the ring-fault orientation without knowing the *DS*  
 235 component. We note that what can be estimated from  $\psi$  is not the ring-fault azimuth but the orientation  
 236 (Figure 2); we cannot distinguish two different ring faults with the same arc angle but rotated by  $180^\circ$  to  
 237 each other.

238 Thus,  $\mathbf{M}_{res}$  for shallow ring-faulting is useful for estimating ring-fault parameters by using  
 239  $k_{CLVD}$  and  $\psi$  together. If  $k_{CLVD}$  is less than  $\sim 90\%$ ,  $\theta$  can be uniquely determined by  $k_{CLVD}$   
 240 because  $\theta$  is a single-valued function of  $k_{CLVD}$  (Figure 4a). In this case, the ring-fault orientation is  
 241 parallel to the N-axis (Figures 4b and 4c). In contrast, if  $k_{CLVD}$  is larger than  $\sim 90\%$ ,  $\theta$  cannot be  
 242 determined uniquely and three values of  $\theta$  are possible for a given  $k_{CLVD}$  (Figure 4a); there also  
 243 remain two possibilities for the ring-fault orientation, parallel or perpendicular to the N-axis,  
 244 depending on  $\theta$  (Figures 4b and 4c). When  $\theta = 180^\circ$ , the N-axis orientation is indeterminate  
 245 (Figures 2c and 2d), and the ring-fault orientation cannot be determined. When  $\theta = 360^\circ$ , the  
 246 ring-fault orientation is irrelevant.

### 247 **3 Case study: Vertical-CLVD earthquakes at the Sierra Negra caldera, Galápagos**

#### 248 **Islands**

249 In the previous section, we showed that the resolvable MTs,  $\mathbf{M}_{res}$ , which are composed of the  
250 CLVD and SS components, of ring-faulting are useful for estimating the arc angle  $\theta$  and the orientation  
251 of the ring fault. Here, we investigate the relationships for a vertical-CLVD earthquake that occurred at  
252 the Sierra Negra caldera prior to the 2005 volcanic activity. We first test the stability of  $\mathbf{M}_{res}$  obtained  
253 from MT inversion using long-period seismic records at far field. Then, we analyze  $\mathbf{M}_{res}$  to estimate  
254 the ring-fault parameters and compare them with other observations. We also investigate two  
255 vertical-CLVD earthquakes during volcanic activity in 2018.

#### 256 **3.1 $M_w$ 5.5 vertical-T CLVD earthquake prior to the 2005 eruption**

257 The Sierra Negra is a shield volcano located at the southern end of Isabella Island, in the  
258 Galápagos Islands (Figure 5a). A shallow 7 km  $\times$  10.5 km caldera structure is formed at the summit of  
259 the 1124-m-high volcano (Figure 5b; Reynolds et al., 1995). On 22 October 2005, the Sierra Negra  
260 caldera started eruption activity at ~23:30 in UTC (e.g., Global Volcanism Project, 2005; Geist et al.,  
261 2008). At 20:34 on the same day, about 3 h before initiation of the eruption, a vertical-T CLVD  
262 earthquake with  $M_w$  5.5 occurred (Chadwick et al., 2006; Jónsson, 2009). Clear long-period seismic  
263 signals from this earthquake were observed at far-field stations (black curves in Figure 6). Geodetic  
264 observations using data obtained from Global Positioning System (GPS) and Interferometric Synthetic  
265 Aperture Radar (InSAR) suggested reverse slips along a sinuous fault system with an inward dip angle

266 on the western to southern parts of the caldera caused by a pressurized sill-like magma chamber lying at  
 267 a depth of about 2 km (Jónsson, 2009). This fault-motion mechanism is termed *trapdoor faulting* (e.g.,  
 268 Amelung et al., 2000; Chadwick et al., 2006; Jónsson, 2009). The mechanism was indicated by a fresh  
 269 fault scarp (dashed and solid curves in Figure 5b) identified by Geist et al. (2008), who conducted field  
 270 surveys at the caldera after the 2005 eruption. The shallow sill-like magma chamber estimated from  
 271 geodetic data (Jónsson, 2009) suggests that the earthquake occurred in the top ~2 km of the crust. For  
 272 this geometry at such a shallow depth, the indeterminacy of the *DS* component is an issue. Thus, this is  
 273 a good example for investigating how the MT solution of a vertical-CLVD earthquake caused by  
 274 ring-faulting is related to the geometry of the ring fault identified by geodetic studies and field surveys.

### 275 3.2 Data & methods

276 We perform MT inversion for the  $M_w$  5.5 vertical-T earthquake near the Sierra Negra caldera.  
 277 We use the W-phase code for the inversion, including filtering, data screening, and convolution of  
 278 Green's functions (Kanamori and Rivera, 2008; Hayes et al., 2009; Duputel et al., 2012). We use the  
 279 normal mode method (e.g., Takeuchi and Saito, 1972) to compute Green's functions for the 1-D  
 280 Preliminary Reference Earth Model (PREM; Dziewonski and Anderson, 1981), in the same way as we  
 281 did for the synthetic test in Section 2.2. Long-period seismic waves are extracted from synthetic and  
 282 observed waveforms by applying a one-pass, fourth-order Butterworth bandpass filter with corner  
 283 frequencies at 0.005 and 0.0125 Hz. The inversion time window is set to include P, S, and surface waves.  
 284 We assume zero contribution by a volume change to the long-period seismic waves by imposing the  
 285 zero-trace constraint,  $M_{rr} + M_{\theta\theta} + M_{\phi\phi} = 0$ . This means that the seismic waves are entirely

286 attributed to ring-faulting. Possible bias caused by a volume change is discussed later in Section 4.2.

287 We use long-period seismic records at far-field stations for the inversion. We download seismic  
 288 records at far-field stations within  $5^{\circ}$ – $60^{\circ}$  of the epicentral distance as obtained from the Data  
 289 Management Center of the Incorporated Research Institutions for Seismology (IRIS). To remove bad  
 290 data (i.e., data with glitch, or low signal-to-noise ratio), we conduct a trial MT inversion using a source  
 291 placed at 2.5 km depth in the crust just below the Sierra Negra caldera ( $0.83^{\circ}$ S,  $91.14^{\circ}$ W), assuming the  
 292 centroid time shift and half duration reported in the Global Centroid Moment Tensor (GCMT) Catalog.  
 293 Using the result of the trial inversion, we select 25 seismic records with a root mean square (RMS)  
 294 misfit smaller than 0.9; the RMS is defined by  $\rho_i = \|\mathbf{s}_w^i - \mathbf{d}_w^i\| / \|\mathbf{s}_w^i\|$ , where  $\mathbf{s}_w^i$  and  $\mathbf{d}_w^i$  are  
 295 synthetic and observed data in the inversion time window at the  $i$ -th station, respectively, and  $\|\mathbf{s}\|$   
 296 represents the L2 norm of data vector  $\mathbf{s}$ . The selected dataset is for the epicentral distance range from  
 297  $12.4^{\circ}$  to  $46.6^{\circ}$  and has a good azimuthal coverage (Figure 6). The stations are from different seismic  
 298 networks: the Global Seismograph Network (II, IU), Broadband Tomography Under Costa Rica and  
 299 Nicaragua (YO, 2003–2006), GEOSCOPE (G), and the United States National Seismic Network (US).

300 To examine the stability of the MT solutions, we repeat MT inversion while moving the centroid  
 301 location in a 3D space around the Sierra Negra caldera. By examining the variation in the MT solutions,  
 302 we can assess the sensitivity of the solutions to small variations in estimated centroid location, noise in  
 303 the data, model imperfections, and unmodeled subsurface velocity structures. For MT inversion in 3D  
 304 space, centroid locations are distributed on two planes: the  $x$ – $y$  (longitude–latitude) plane at a depth of  
 305 2.5 km in the crust (Figure 7a), and the  $x$ – $z$  (longitude–depth) plane along a latitude of  $0.83^{\circ}$ S across the

306 caldera (Figure 7b). The centroid location intervals are  $0.1^\circ$  in the horizontal direction and 2.0 km in the  
 307 vertical direction. At each centroid location, we conduct MT inversion while grid-searching an optimal  
 308 value of the centroid time shift, assuming the half duration to be the same as the centroid time shift. The  
 309 waveform fit for the MT solution is measured with the normalized RMS (NRMS) misfit,  $\sum_{i=1}^N (\rho_i/N)$ ,  
 310 where  $N$  is the number of seismic records, and  $\rho_i$  is the RMS misfit at the  $i$ -th station. Then, we set  
 311  $M_{r\theta} = M_{r\phi} = 0$  for the obtained MT solutions to estimate  $\mathbf{M}_{res}$  defined by Equation (11). Strictly  
 312 speaking, to estimate  $\mathbf{M}_{res}$  exactly with the constraint of  $M_{r\theta} = M_{r\phi} = 0$ , we need to perform  
 313 three-element MT inversions with the three constraints,  $M_{r\theta} = M_{r\phi} = 0$ , and  $M_{rr} + M_{\theta\theta} + M_{\phi\phi} = 0$ .  
 314 However, to compare our solutions with the GCMT solutions which were obtained for the five MT  
 315 elements with the only constraint  $M_{rr} + M_{\theta\theta} + M_{\phi\phi} = 0$ , we here perform five-element MT  
 316 inversions only with the constraint  $M_{rr} + M_{\theta\theta} + M_{\phi\phi} = 0$ , and after the solution was obtained we set  
 317  $M_{r\theta} = M_{r\phi} = 0$ . In Supporting Information, we compare  $\mathbf{M}_{res}$  obtained with these two methods and  
 318 show that the results are very similar when the datasets are good.

### 319 3.3 Results

#### 320 3.3.1 Indeterminate *DS* component and stability of the resolvable MT

321 Figure 7a shows NRMS values for the MT solutions at locations on the x–y plane at a depth of  
 322 2.5 km. In the area around the Sierra Negra caldera (white rectangle in Figure 7a), NRMS values are  
 323 small. Figure 7b shows NRMS values for the MT solutions on the x–z plane along latitude  $0.83^\circ\text{S}$   
 324 (dashed line in Figure 7a). Similarly, small NRMS values are given by most MT solutions in the top ~15

325 km of the crust. For example, the MT solution at the caldera (0.83°S, 91.14°W; red circle in Figure 7a)  
 326 at a depth of 2.5 km reproduces the observed records well with an NRMS value of 0.365 (Figure 6).  
 327 From the MT solutions in 3D space, 53 solutions at different centroid grids yield NRMS values of  
 328  $\leq 0.365$ , which we refer to as *acceptable solutions* hereafter.

329 Figure 7c shows the MT solutions on the x–y plane at a depth of 2.5 km in the area around the  
 330 caldera (white rectangle in Figure 7a), and Figure 7d shows them on the x–z plane along a latitude of  
 331 0.83°S (white dashed line in Figure 7a) in the top ~10 km of the crust. The solutions on the two planes  
 332 differ significantly depending on centroid locations in the 3D space, although they yield similar small  
 333 NRMS values. Notably, at shallower depths in the crust, estimated  $M_w$  values and ratios of the *DS*  
 334 component are larger (Figure 7d). For the 53 acceptable solutions,  $M_w$  values are distributed widely  
 335 from 5.50 to 6.49 (Figure 8a), and the ratio of the *DS* component, computed with Equation (10), ranges  
 336 from 44.8% to 97.7% (Figure 8b). These results demonstrate the instability of MT inversion caused by  
 337 the indeterminate *DS* component discussed in Section 2.2.

338 From the MT solutions at centroid locations on the x–y and x–z planes, we extract  $\mathbf{M}_{res}$   
 339 defined by Equation (11) (Figures 7e and 7f).  $\mathbf{M}_{res}$  on the two planes have similar focal mechanisms  
 340 and  $M_w$ .  $M_w$  values are in a narrow range ( $5.33 \pm 0.04$ ) for the 53 acceptable solutions (Figure 8c). Also,  
 341  $\mathbf{M}_{res}$  for the acceptable solutions contain stable values of the CLVD ratio  $k_{CLVD}$  ( $73.0\% \pm 3.0\%$ ;  
 342 Figure 8d) and the N-axis azimuth  $\psi$  ( $102.7^\circ \pm 3.0^\circ$ ; Figure 8e). These results confirm that  $\mathbf{M}_{res}$  is  
 343 stably obtained for vertical-CLVD earthquakes, even in the cases where centroid locations are not  
 344 accurately determined, indicating its stability under the presence of noise in observed data, and in cases

345 where there are imperfections in simulation models or velocity structures. Therefore, we reemphasize  
 346 that the two physical parameters (i.e.,  $k_{CLVD}$  and  $\psi$ ) obtained from  $\mathbf{M}_{res}$  can be used to reliably  
 347 estimate ring-fault parameters.

348 In Figure 9 and Table 1, we compare the MT solution obtained for the centroid location at a  
 349 depth of 2.5 km just below the caldera (0.83°S, 91.14°W) with the solution from the GCMT Catalog.  
 350 The centroid depth of the GCMT solution is 12.0 km. The two MT solutions, including the  
 351 indeterminate  $DS$  component, have very different focal mechanisms,  $M_w$  values, and ratios of the  $DS$   
 352 component (Figures 9a and 9b). In contrast,  $\mathbf{M}_{res}$  extracted from the two different solutions show  
 353 similar values for  $M_w$  (5.31 and 5.31),  $k_{CLVD}$  (73.4% and 77.3%), and  $\psi$  (101.9° and 96.3°; Figures 9c  
 354 and 9d). These results demonstrate that  $\mathbf{M}_{res}$  can be reliably estimated from various available catalogs  
 355 such as the GCMT, even if the centroid depth and the complete MT are not accurately determined for  
 356 shallow earthquakes (e.g., Chu et al., 2009; Wimpenny and Watson, 2020).

### 357 3.3.2 Ring-fault parameters inferred from the resolvable MT

358 We next estimate ring-fault parameters for the 2005 vertical-T CLVD earthquake at the Sierra  
 359 Negra caldera from  $\mathbf{M}_{res}$  of the MT solution (Figure 9c). If we assume that the seismic waves are  
 360 generated entirely from idealized ring-faulting (uniform slip along a circular ring fault),  $\mathbf{M}_{res}$  with a  
 361 value of  $k_{CLVD}$  of 73.4% indicates a ring fault extending along an arc angle  $\theta$  of  $\sim 80^\circ$  (Figure 4a). In  
 362 such a case of  $\theta < 180^\circ$ , the N-axis with  $\psi$  of 101.9° suggests that the ring-fault orientation is a  
 363 direction rotated slightly clockwise from the E–W. On the other hand, the intra-caldera fault (black

364 curve in Figure 5b), which was attributed to the earthquake source (Amelung et al., 2000; Chadwick et  
365 al., 2006; Jónsson, 2009), has an arc angle a little smaller than  $90^\circ$  and its orientation is slightly rotated  
366 clockwise from the E–W, if we approximate the fault as a circular arc. Although here we do not consider  
367 complexities of the actual fault geometry and slip distributions, the overall agreement of the ring-fault  
368 parameters with the well-documented intra-caldera fault geometry strongly suggests that we can study  
369 geometries of ring faults at volcanoes by analyzing the  $M_{res}$  of MT solutions obtained from  
370 long-period seismic records at far field.

### 371 3.4 Insights into two vertical-CLVD earthquakes prior to and during the 2018 eruption

372 The Sierra Negra caldera renewed its eruption activity at ~19:40 on 26 June 2018 (UTC), which  
373 lasted until 23 August (Global Volcanism Program, 2018; Vasconez et al., 2018). The activity included  
374 fissure eruptions from several fissure vents along the northern part of the caldera rim and on the  
375 northern side of the volcanic flank, and large volcanic deformations with increased seismicity at the  
376 caldera. Prior to and during the eruption, two vertical-CLVD earthquakes with  $M_w > 5$  were reported  
377 near the Sierra Negra caldera: an  $M_w$  5.3 earthquake at 9:15 on 26 June, about 10 h before the initiation  
378 of the eruption, and an  $M_w$  5.1 earthquake at 0:30 on 5 July. The two earthquakes were attributed to  
379 trapdoor faulting events on the intra-caldera fault structure by La Femina et al. (2018), who analyzed  
380 GPS records at the caldera. This indicates the ring-faulting origin of the earthquakes.

381 To provide insights into the sources of two vertical-CLVD earthquakes, we here analyze their  
382 MT solutions from the GCMT Catalog (Table 1, Figures 10a and 10c). A vertical-T earthquake occurred

383 on 26 July before the eruption (Figure 10a), and a vertical-P earthquake on 5 July after the eruption  
 384 started (Figure 10c). Focal mechanisms and the parameters ( $k_{CLVD}$  and  $\psi$ ) of  $M_{res}$  extracted from the  
 385 MT solutions of the vertical-T and P earthquakes are shown in Figures 10b and 10d, respectively. For  
 386 the vertical-T earthquake,  $k_{CLVD}$  is 72.2% and  $\psi$  is 86.4° (approximately E–W), and for the vertical-P  
 387 earthquake,  $k_{CLVD}$  is 71.9% and  $\psi$  is 55.5° (approximately NE–SW).

388 Here we suggest source kinematics and geometries of the earthquakes from the GCMT solutions  
 389 together with pre- and co-seismic deformation reported by La Femina et al. (2018). First, the difference  
 390 in the types of vertical-CLVD earthquake (vertical-T or -P) may be explained by flipped kinematics of  
 391 slips on inward-dipping ring faults. La Femina et al. (2018) reported that the first (vertical-T)  
 392 earthquake took place during the inflation phase of the caldera, preceding the eruption, whereas the  
 393 second (vertical-P) earthquake occurred during a rapid deflation phase that began following the  
 394 initiation of the eruption. Considering the co-seismic deformation patterns of the caldera at the times of  
 395 the earthquakes, it is reasonable to attribute the vertical-T earthquake during the inflation phase to  
 396 upward motion of the central block along an inward-dipping ring fault (Figure 1a), and the vertical-P  
 397 earthquake during the deflation phase to a drop of the block slipping on an inward-dipping ring fault  
 398 (Figure 1c).

399 On the basis of  $M_{res}$  values of the GCMT solutions, we further investigate ring-fault  
 400 parameters of the two vertical-CLVD earthquakes. The small values of  $k_{CLVD}$ , 72.2% for the vertical-T  
 401 earthquake and 71.9% for the vertical-P earthquake (Figures 10b and 10d), indicate that both  
 402 earthquakes occurred along short ring faults with arc angles  $\theta$  of  $\sim 80^\circ$ , according to the relationship

403 | between  $k_{CLVD}$  and  $\theta$  (Figure 4a). In contrast, the significant difference in  $\psi$  of  $\sim 31^\circ$  (compare  
404 | Figures 10b and 10d) implies that the earthquakes occurred on different segments of the intra-caldera  
405 | fault system. On the basis of the relationship between the N-axis of  $\mathbf{M}_{res}$  and the orientation of the ring  
406 | fault with  $\theta < 180^\circ$  (top row in Figure 4b), the N-axis of  $\mathbf{M}_{res}$  is expected to be parallel to the  
407 | ring-fault orientation. Therefore, we suggest that the vertical-T earthquake occurred on a ring fault  
408 | oriented in the E–W direction, whereas the vertical-P earthquake occurred on a different ring-fault  
409 | segment oriented in the NE–SW direction. La Femina et al. (2018) suggested that co-seismic  
410 | deformation occurred in the western caldera at the times of the two earthquakes. This implies that  
411 | ring-faulting occurred somewhere along the western half of the intra-caldera fault system. Given the  
412 | fault structures exposed at the surface in the western half of the caldera (Figure 5b), we suggest that the  
413 | vertical-T earthquake was generated by reverse slip on a southern intra-caldera fault oriented in the E–  
414 | W direction, which may correspond to the southeastern part of the fault estimated as generating the  
415 | 2005 earthquake (the southeastern part of the black curve in Figure 5b). By contrast, we infer that the  
416 | vertical-P earthquake occurred on a ring-fault segment oriented in the NE–SW direction in the  
417 | northwestern part of the caldera. For reference, we indicate a possible example of such ring-fault  
418 | geometry that may have generated the vertical-P earthquake by a dashed white curve in Figure 5b. We  
419 | emphasize that these ring-fault geometries need to be investigated together with other observations such  
420 | as co-seismic deformation or near-field seismic waves. Although some uncertainties remain, we  
421 | suggest that the clear differences between the parameters of  $\mathbf{M}_{res}$  for the two vertical-CLVD  
422 | earthquakes offer information about significant differences in slip kinematics and source locations

423 along the intra-caldera fault system.

## 424 **4 Discussion**

### 425 4.1 Efficiency of long-period seismic excitation from ring-faulting

426 As demonstrated above, the nature of seismic excitation from ring-faulting is very different  
 427 from that of regular tectonic earthquakes. In general, despite the spectacular surface expression of ring  
 428 faults, the seismic excitation, especially at long periods (greater than  $\sim 100$  s), is inefficient, which often  
 429 causes difficulty in interpretation. We have already discussed several specific cases above, and here we  
 430 add some general discussion to clarify the problem of the inefficient seismic excitation.

431 There are two aspects to this problem. First, as previously discussed by Ekström (1994) and  
 432 Shuler et al. (2013b), the ring-fault geometry results in cancellation of the source strength, as measured  
 433 by the scalar moment. As discussed in Section 2, we represent the MT of ring-faulting by the sum of  
 434 MTs of planar rhomboidal subfaults under the point-source approximation. We then compute the scalar  
 435 moment  $M_0$  of the ring-faulting using Equation (1). Figure 11a shows the ratio:

$$436 \quad \frac{M_0}{\sum_i \Delta M_0^i} \quad (13)$$

437 as a function of the dip and arc angles, where  $\Delta M_0^i$  is the scalar moment of the  $i$ -th subfault along the  
 438 ring fault computed using Equation (1). This ratio is generally smaller than 1 owing to the geometrical  
 439 cancellation of the double-couple components (i.e.,  $\mathbf{M}_{SS}$  and  $\mathbf{M}_{DS}$ ).

440 In addition to this geometrical cancellation, the efficiency of seismic excitation of ring-faulting

441 is reduced because of its shallow source property. As expressed by Equation (6), the MT of ring-faulting  
 442 can be expressed by the sum of three components,  $\mathbf{M}_{CLVD}$ ,  $\mathbf{M}_{SS}$ , and  $\mathbf{M}_{DS}$ . Because of the very shallow  
 443 depth,  $\mathbf{M}_{DS}$  does not contribute to seismic excitation; by contrast, the other two components ( $\mathbf{M}_{CLVD}$ ,  
 444  $\mathbf{M}_{SS}$ ), which we referred to as resolvable components, have contributions to seismic excitation. The  
 445 effect of little or no seismic property of  $\mathbf{M}_{DS}$  can be expressed by the following ratio of scalar moment  
 446 of  $\mathbf{M}_{res}$  to that of the theoretical MT (Figure 11b):

$$447 \quad \frac{M_0^{res}}{M_0}, \quad (14)$$

448 where  $M_0^{res}$  is the scalar moment based on Equation (1) for  $\mathbf{M}_{res}$  (defined by Equation (11)).

449 Then, the combined effect can be given by the ratio (Figure 11c):

$$450 \quad \frac{M_0}{\sum_i \Delta M_0^i} \times \frac{M_0^{res}}{M_0} = \frac{M_0^{res}}{\sum_i \Delta M_0^i}. \quad (15)$$

451 As shown in Figure 11c, the excitation efficiency of long-period seismic waves from ring-faulting at a  
 452 shallow depth is generally low, being lower for ring faults dipping more steeply.

453 The inefficient excitation of long-period seismic waves explains many peculiar characteristics  
 454 of vertical-CLVD earthquakes. Ring-faulting may generate greater surface deformation than expected  
 455 empirically from their seismic magnitudes estimated with long-period seismic waves. This may explain  
 456 the discrepancy between seismic magnitudes estimated for slip on the intra-caldera fault at the Sierra  
 457 Negra caldera from geodetic and seismic data (Jónsson, 2009). If vertical-T CLVD earthquakes at  
 458 submarine volcanoes near Torishima Island in Japan (Satake and Kanamori, 1991; Fukao et al., 2018)

459 and near Curtis Island in New Zealand (Gusman et al., 2020) are related to ring-faulting, the  
 460 disproportionately large tsunamis for their seismic magnitudes may be partially a result of the  
 461 inefficient seismic excitation. Kanamori et al. (1993) identified an azimuthally uniform radiation  
 462 pattern of Rayleigh waves and an absence of Love waves from a vertical-T earthquake. This  
 463 peculiarity can also be explained by the geometrical cancellation of the double-couple components and  
 464 inefficient excitation of the *DS* component.

#### 465 4.2 Effect of volume change on the zero-trace estimate of the *CLVD* component

466 In previous sections, we estimated the CLVD moment scale  $M_{CLVD}$  of ring-faulting, defined by  
 467 Equation (4), at a very shallow depth, with the assumption of a vanishing isotropic component  $M_{ISO}$ ,  
 468 defined by Equation (3). If a volume change occurs near ring-faulting, the estimated  $M_{CLVD}$  might be  
 469 biased. As the bias depends on the geometry of the magma reservoir, we discuss three cases below.

##### 470 Horizontal tensile crack

471 The moment tensor for a horizontal tensile (or compressional) crack with a volume change  $\Delta V$   
 472 is given in the  $(r, \theta, \phi)$  coordinate system by (e.g., Kawakatsu and Yamamoto, 2015)

$$473 \quad \mathbf{M}_{Tensile} = \Delta V \begin{bmatrix} \lambda + 2\mu & & & \\ & 0 & \lambda & \\ & & 0 & \lambda \\ & & & & \lambda \end{bmatrix}. \quad (16)$$

474 As seismic excitation of a moment tensor  $\mathbf{M}$  is determined by  $(\mathbf{M} : \boldsymbol{\varepsilon})$ , where  $\boldsymbol{\varepsilon}$  is the strain tensor at the  
 475 source (Gilbert, 1971), the excitation by the horizontal tensile crack is proportional to  $(\lambda + 2\mu)\varepsilon_{rr} +$   
 476  $\lambda\varepsilon_{\theta\theta} + \lambda\varepsilon_{\phi\phi}$ , which is equal to  $\sigma_{rr}$ , where  $\varepsilon_{rr}$ ,  $\varepsilon_{\theta\theta}$ , and  $\varepsilon_{\phi\phi}$  are the  $rr$ ,  $\theta\theta$ , and  $\phi\phi$  elements of

477 the strain tensor, respectively, and  $\sigma_{rr}$  is the  $rr$  element of the stress tensor. For a very shallow source,  
 478  $\sigma_{rr} \approx 0$ . This means that a very shallow horizontal tensile crack has no or little seismic excitation (pp.  
 479 180–183 of Dahlen and Tromp, 1998; Fukao et al., 2018).

480 Previous studies have suggested that the Sierra Negra caldera has a sill-like magma reservoir at  
 481 a depth of  $\sim 2$  km (e.g., Amelung et al., 2000; Chadwick et al., 2006; Jónsson, 2009). Because a volume  
 482 change of such a shallow sill-like reservoir involves a moment tensor defined by Equation (16) and does  
 483 not contribute to long-period seismic waves, it is reasonable to attribute the seismic waves from the  
 484 vertical-CLVD earthquakes at the caldera only to ring-faulting, as done in Section 3.

485 The case for a horizontal tensile crack has an important implication for other types of volume  
 486 change.  $\mathbf{M}_{Tensile}$  can be decomposed as:

$$487 \quad \Delta V \begin{bmatrix} \lambda + 2\mu & & & \\ & 0 & \lambda & \\ & & 0 & \lambda \end{bmatrix} = \left( \lambda + \frac{2}{3}\mu \right) \Delta V \begin{bmatrix} 1 & & \\ 0 & 1 & \\ 0 & 0 & 1 \end{bmatrix} + \frac{4}{3}\mu \Delta V \begin{bmatrix} 1 & & \\ 0 & -0.5 & \\ 0 & 0 & -0.5 \end{bmatrix}. \quad (17)$$

488 The first and second terms on the right-hand side represent isotropic and CLVD sources, respectively.

489 Thus, the vanishing excitation by a horizontal tensile crack simply means that a unit isotropic tensor

$$490 \quad \begin{bmatrix} 1 & & \\ 0 & 1 & \\ 0 & 0 & 1 \end{bmatrix} \text{ is equivalent to a CLVD tensor } -\frac{4\mu}{3\lambda+2\mu} \begin{bmatrix} 1 & & \\ 0 & -0.5 & \\ 0 & 0 & -0.5 \end{bmatrix} \text{ for seismic excitation at a very}$$

491 shallow depth.

#### 492 Spherical source

493 If the deformation below ring-faulting is represented by a spherical source given by a moment  
 494 tensor

$$\begin{aligned}
 495 \quad \mathbf{M}_{Sphere} &= \Delta V \begin{bmatrix} \lambda + \frac{2}{3}\mu & & \\ 0 & \lambda + \frac{2}{3}\mu & \\ & 0 & \lambda + \frac{2}{3}\mu \end{bmatrix} = \left(\lambda + \frac{2}{3}\mu\right) \Delta V \begin{bmatrix} 1 & & \\ 0 & 1 & \\ 0 & 0 & 1 \end{bmatrix} = \\
 496 \quad M_{ISO}^{Sphere} &= \begin{bmatrix} 1 & & \\ 0 & 1 & \\ 0 & 0 & 1 \end{bmatrix}, \quad (18)
 \end{aligned}$$

497 where

$$498 \quad M_{ISO}^{Sphere} = \left(\lambda + \frac{2}{3}\mu\right) \Delta V, \quad (19)$$

499 then, using the equivalence relation between the isotropic and CLVD tensors, the CLVD moment scale  
 500 of ring-faulting at a shallow depth is observed as a CLVD source with

$$501 \quad M'_{CLVD} = M_{CLVD} - \frac{4\mu}{3\lambda+2\mu} M_{ISO}^{Sphere} = M_{CLVD} - \frac{4}{3}\mu \Delta V. \quad (20)$$

502 Thus, to estimate  $M_{CLVD}$  for ring-faulting, we need to add  $\frac{4}{3}\mu \Delta V$  to the observed  $M'_{CLVD}$  estimated  
 503 with the assumption of  $\Delta V = 0$ .

#### 504 Vertical cylindrical source

505 If the deformation below ring-faulting is represented by a vertical cylindrical source given by a  
 506 moment tensor

$$\begin{aligned}
 \mathbf{M}_{Cylinder} &= \Delta V \begin{bmatrix} \lambda & & \\ 0 & \lambda + \mu & \\ 0 & 0 & \lambda + \mu \end{bmatrix} = \left(-\frac{2}{3}\mu \Delta V\right) \begin{bmatrix} 1 & & \\ 0 & -0.5 & \\ 0 & 0 & -0.5 \end{bmatrix} + \left(\lambda + \frac{2}{3}\mu\right) \Delta V \begin{bmatrix} 1 & & \\ 0 & 1 & \\ 0 & 0 & 1 \end{bmatrix} \\
 507 \quad &= M_{CLVD}^{Cylinder} \begin{bmatrix} 1 & & \\ 0 & -0.5 & \\ 0 & 0 & -0.5 \end{bmatrix} + M_{ISO}^{Cylinder} \begin{bmatrix} 1 & & \\ 0 & 1 & \\ 0 & 0 & 1 \end{bmatrix}, \quad (21)
 \end{aligned}$$

508 where

509  $M_{CLVD}^{Cylinder} = -\frac{2}{3}\mu \Delta V$  (22)

510 and

511  $M_{ISO}^{Cylinder} = \left(\lambda + \frac{2}{3}\mu\right) \Delta V$ , (23)

512 then, considering the additional isotropic and CLVD components from the vertical cylindrical source,

513 the CLVD moment scale of ring-faulting is equivalent to a CLVD source with

514 
$$M'_{CLVD} = M_{CLVD} + \left(M_{CLVD}^{Cylinder} - \frac{4\mu}{3\lambda+2\mu} M_{ISO}^{Cylinder}\right)$$

515 
$$= M_{CLVD} + \left\{-\frac{2}{3}\mu \Delta V - \frac{4\mu}{3\lambda+2\mu} \left(\lambda + \frac{2}{3}\mu\right) \Delta V\right\}$$

516 
$$= M_{CLVD} - 2\mu \Delta V. \quad (24)$$

517 Thus, we need to add  $2\mu \Delta V$  to the observed  $M'_{CLVD}$  to estimate  $M_{CLVD}$  for ring-faulting.

518 To illustrate the equivalence relation between the isotropic and CLVD tensors discussed above,

519 we show synthetic long-period waveforms computed for a CLVD source, an isotropic source, and a

520 horizontal tensile crack source (Figure 12). For this comparison, we use a common metric for  $\mathbf{M}_{CLVD}$ ,

521  $\mathbf{M}_{ISO}$ , and  $\mathbf{M}_{Tensile}$ . If we use the definition of a scalar moment  $M_0$ , given by Equation (1), then a

522 CLVD source,  $\begin{bmatrix} 1 & & \\ 0 & -0.5 & \\ 0 & 0 & -0.5 \end{bmatrix}$ , an isotropic source,  $\begin{bmatrix} 1 & & \\ 0 & 1 & \\ 0 & 0 & 1 \end{bmatrix}$ , and a horizontal tensile crack

523 source,  $\begin{bmatrix} \lambda + 2\mu & & \\ 0 & \lambda & \\ 0 & 0 & \lambda \end{bmatrix}$ , can be written, respectively, as

524 
$$M_0 \begin{bmatrix} \sqrt{4/3} & & \\ 0 & -\sqrt{1/3} & \\ 0 & 0 & -\sqrt{1/3} \end{bmatrix}, \quad (25)$$

$$M_0 \begin{bmatrix} \sqrt{2/3} & & \\ 0 & \sqrt{2/3} & \\ 0 & 0 & \sqrt{2/3} \end{bmatrix}, \quad (26)$$

526 and

$$M_0 \sqrt{\frac{2}{(\lambda+2\mu)^2+2\lambda^2}} \begin{bmatrix} \lambda+2\mu & & \\ 0 & \lambda & \\ 0 & 0 & \lambda \end{bmatrix}. \quad (27)$$

528 Here, we use the same scalar moment of  $M_0 = 1.0 \times 10^{18}$  Nm ( $M_w$  5.9). The waveforms for the CLVD  
 529 and isotropic sources are quite similar to each other, except for the polarity and amplitude (Figures 12a  
 530 and 12b). Figure 12c shows waveforms for the horizontal tensile source. The amplitudes are very small,  
 531 reflecting the cancellation effects of  $\mathbf{M}_{CLVD}$  and  $\mathbf{M}_{ISO}$ .

## 532 5. Conclusions

533 In previous studies, vertical-CLVD earthquakes were attributed to ring-faulting at active  
 534 volcanoes. However, the relationship between detailed ring-fault parameters and their MT solutions  
 535 obtained from long-period seismic waveforms has been poorly understood. In Section 2, we showed  
 536 theoretically that the main cause of the difficulty in relating them is the instability of MT inversion for  
 537 earthquakes in the top part (shallower than ~10 km) of the crust due to inefficient excitation of seismic  
 538 waves from some components. We then proposed reliable relationships of MT solutions with ring-fault  
 539 parameters based on two physical parameters, namely, the CLVD ratio  $k_{CLVD}$  and the N-axis azimuth  
 540  $\psi$ , of the resolvable MT  $\mathbf{M}_{res}$ , which is composed of the vertical-CLVD and vertical strike-slip  
 541 components. In Section 3, through a case study of the 2005 vertical-CLVD earthquake at the Sierra

542 | Negra caldera, we verified the stability of  $M_{res}$  obtained by MT inversion using long-period seismic  
543 | records at far field. We also demonstrated that the ring-fault parameters estimated with  $M_{res}$  were  
544 | consistent with the geometry of the ring fault identified by geodetic observations and field surveys. In  
545 | addition, we pointed out a clear difference between  $M_{res}$  values of two vertical-CLVD earthquakes  
546 | during the 2018 activity at the caldera and proposed significant differences in the kinematics and source  
547 | locations of the two ring-faulting events.

548 |         The present study demonstrates the usefulness of MT inversion using long-period seismic  
549 | waveforms for investigating the slip kinematics and geometries of ring faults at active volcanoes,  
550 | particularly those with caldera structures. Analyses of long-period seismic records at far field allow  
551 | remote estimation of ring-fault parameters at active volcanoes even without local observation networks  
552 | or detailed 3D velocity structure. At a wider scale, vertical-CLVD earthquakes have been observed at  
553 | tens of active volcanoes (e.g., Shuler et al., 2013a; 2013b). Large seismic events with vertical-CLVD  
554 | components can be used to investigate the ring-fault systems of remote volcanoes including not only  
555 | well-monitored volcanoes, such as Kilauea (e.g., Neal et al., 2019; Tepp et al., 2020) and Bárðarbunga  
556 | (e.g., Gudmundsson et al., 2016; Riel et al., 2015), but also remote volcanic islands or submarine  
557 | volcanoes, whose activities cannot be investigated easily, such as the Smith caldera (Satake and  
558 | Kanamori, 1991; Kanamori et al., 1993, Fukao et al., 2018) and Curtis Island, north of New Zealand  
559 | (Gusman et al., 2020).

560 |         However, limitations of seismological investigations for vertical-CLVD earthquakes using  
561 | long-period seismic records at far field remain. Some moment tensor elements of ring-faulting are

562 inefficient for generating long-period seismic waves, so that parts of source parameters cannot be fully  
563 determined only from the records. The temporal–spatial history of rupture propagation along a fault  
564 may not be resolved owing to the long-period property. It is also difficult to constrain a source with a  
565 volume change accompanying ring-faulting. To recover more information regarding ring-faulting,  
566 shorter-period seismic waves may be utilized with heterogeneous 3-D velocity structures around the  
567 calderas (e.g., Contreras-Arratia and Neuberg, 2019; Hejrani and Tkalčić, 2019). Combinations of  
568 seismic analyses with other observations may also provide more details about fracture processes of  
569 earthquakes involving ruptures of subsurface fault systems and fluid or gas transportation. To constrain  
570 the mechanism of a source with a change in volume, geodetic observations of surface deformation using  
571 such as GPS, tiltmeters, or InSAR are commonly required (e.g., Yun, 2007; Anderson et al., 2019;  
572 Segall et al., 2019, 2020). Such improvements in seismological investigations and combinations with  
573 other geophysical observation techniques have the potential to broaden our knowledge about active  
574 volcanoes generating ring-faulting. A better understanding of vertical-CLVD earthquakes will provide  
575 insights into the interaction of subsurface volcanic processes with fault systems of volcanic edifices and  
576 magmatic processes, potentially leading to assessments of volcanic hazards.

## 577 **Acknowledgments**

578 We thank K. Nishida, S. Takemura, and T. Saito for helpful discussion. This work is funded by  
579 the JSPS KAKENHI (grant numbers JP17J02919, JP20J01689, and JP19K04034) and by the JST  
580 J-RAPID (grant number JPMJRR1805). O.S.'s travel to California Institute of Technology was  
581 supported by the Oversea Internship Program of Earthquake Research Institute, the University of Tokyo.

582 This manuscript has been edited by Stallard Scientific Editing (<https://www.stallardediting.com/>).

### 583 **Data Availability Statement**

584 We used topography and bathymetry data downloaded from the Advance Land Observation  
585 Satellite (ALOS) World 3D–30 m DEM (AW3D30; available from  
586 <https://www.eorc.jaxa.jp/ALOS/en/index.htm>) provided by the Japan Aerospace Exploration Agency  
587 (JAXA), and from GEBCO\_2020 Grid (available from  
588 [https://www.gebco.net/data\\_and\\_products/gridded\\_bathymetry\\_data/](https://www.gebco.net/data_and_products/gridded_bathymetry_data/)). The W-phase code can be  
589 downloaded from <http://wphase.unistra.fr/wiki/doku.php/wphase>. We obtained earthquake information  
590 from the GCMT Catalog (<https://www.globalcmt.org/>). We plotted focal mechanisms representing  
591 moment tensors with a MATLAB code developed by James Conder (available from MATLAB Central  
592 File Exchange  
593 ([https://www.mathworks.com/matlabcentral/fileexchange/61227-focalmech-fm-centerx-centery-diam-](https://www.mathworks.com/matlabcentral/fileexchange/61227-focalmech-fm-centerx-centery-diam-varargin)  
594 [varargin](https://www.mathworks.com/matlabcentral/fileexchange/61227-focalmech-fm-centerx-centery-diam-varargin))). Data of MT solutions obtained in this study and used for Figure 7 is provided in an open  
595 access repository, Zenodo (<https://doi.org/10.5281/zenodo.4442967>).

596 **References**

- 597 Acocella, V. (2007). Understanding caldera structure and development: An overview of analogue  
598 models compared to natural calderas. *Earth-Science Reviews*, 85(3–4), 125–160.  
599 <https://doi.org/10.1016/j.earscirev.2007.08.004>
- 600 Aki, K., & Richards, P. G. (1980). *Quantitative seismology*. Sausalito, CA: University Science  
601 Books.
- 602 Amelung, F., Jonsson, S., Zebker, H., & Segall, P. (2000). Widespread uplift and “trapdoor” faulting  
603 on Galapagos volcanoes observed with radar interferometry. *Nature*, 407(6807), 993–996.  
604 <https://doi.org/10.1038/35039604>
- 605 Anderson, K. R., Johanson, I. A., Patrick, M. R., Gu, M., Segall, P., Poland, M. P., et al. (2019).  
606 Magma reservoir failure and the onset of caldera collapse at Kīlauea Volcano in 2018. *Science*,  
607 366(6470). <https://doi.org/10.1126/science.aaz1822>
- 608 Cesca, S., Letort, J., Razafindrakoto, H. N. T., Heimann, S., Rivalta, E., Isken, M. P., et al. (2020).  
609 Drainage of a deep magma reservoir near Mayotte inferred from seismicity and deformation.  
610 *Nature Geoscience*, 13(1), 87–93. <https://doi.org/10.1038/s41561-019-0505-5>
- 611 Chadwick, W. W., Geist, D. J., Jónsson, S., Poland, M., Johnson, D. J., & Meertens, C. M. (2006). A  
612 volcano bursting at the seams: Inflation, faulting, and eruption at Sierra Negra volcano,  
613 Galápagos. *Geology*, 34(12), 1025–1028. <https://doi.org/10.1130/G22826A.1>

614 Chouet, B. (2003). Volcano Seismology. *Pure and Applied Geophysics*, 160(3), 739–788.

615 <https://doi.org/10.1007/PL00012556>

616 Chu, R., Zhu, L., & Helmberger, D. V. (2009). Determination of earthquake focal depths and source  
617 time functions in central Asia using teleseismic P waveforms. *Geophysical Research Letters*,

618 36(17), 7–10. <https://doi.org/10.1029/2009GL039494>

619 Cole, J. W., Milner, D. M., & Spinks, K. D. (2005). Calderas and caldera structures: A review.

620 *Earth-Science Reviews*, 69(1–2), 1–26. <https://doi.org/10.1016/j.earscirev.2004.06.004>

621 Contreras-Arratia, R., & Neuberg, J. W. (2019). Complex seismic sources in volcanic environments:

622 Radiation modelling and moment tensor inversions. *Journal of Volcanology and Geothermal*

623 *Research*, 381, 262–272. <https://doi.org/10.1016/j.jvolgeores.2019.06.005>

624 Contreras-Arratia, R., & Neuberg, J. W. (2020). Towards reconciling seismic and geodetic moment

625 estimations: Case Bárðarbunga. *Journal of Volcanology and Geothermal Research*, 107034.

626 <https://doi.org/10.1016/j.jvolgeores.2020.107034>

627 Dahlen, F. A., & Tromp, J. (1998). *Theoretical global seismology*. *Theoretical global seismology*.

628 <https://doi.org/10.1029/99eo00054>

629 Darnet, M., Wawrzyniak, P., Tarits, P., Hautot, S., & D’Eu, J. F. (2020). Mapping the geometry of

630 volcanic systems with magnetotelluric soundings: Results from a land and marine

631 magnetotelluric survey performed during the 2018–2019 Mayotte seismovolcanic crisis.

632 *Journal of Volcanology and Geothermal Research*, 406, 107046.

633 <https://doi.org/10.1016/j.jvolgeores.2020.107046>

634 Duputel, Z., & Rivera, L. (2019). The 2007 caldera collapse of Piton de la Fournaise volcano:

635 Source process from very-long-period seismic signals. *Earth and Planetary Science Letters*,

636 527, 115786. <https://doi.org/10.1016/j.epsl.2019.115786>

637 Duputel, Z., Rivera, L., Kanamori, H., & Hayes, G. (2012). W phase source inversion for moderate to

638 large earthquakes (1990-2010). *Geophysical Journal International*, 189(2), 1125–1147.

639 <https://doi.org/10.1111/j.1365-246X.2012.05419.x>

640 Dziewonski, A. M., Chou, T. A., & Woodhouse, J. H. (1981). Determination of earthquake source

641 parameters from waveform data for studies of global and regional seismicity. *Journal of*

642 *Geophysical Research*. <https://doi.org/10.1029/JB086iB04p02825>

643 Dziewonski, A. M., & Anderson, D. L. (1981). Preliminary reference Earth model. *Physics of the*

644 *Earth and Planetary Interiors*, 25(4), 297–356.

645 [https://doi.org/10.1016/0031-9201\(81\)90046-7](https://doi.org/10.1016/0031-9201(81)90046-7)

646 Ekström, G., Nettles, M., & Dziewoński, A. M. (2012). The global CMT project 2004-2010:

647 Centroid-moment tensors for 13,017 earthquakes. *Physics of the Earth and Planetary Interiors*,

648 200–201, 1–9. <https://doi.org/10.1016/j.pepi.2012.04.002>

649 Ekström, G. (1994). Anomalous earthquakes on volcano ring-fault structures. *Earth and Planetary*

- 650 *Science Letters*, 128(3–4), 707–712. [https://doi.org/10.1016/0012-821X\(94\)90184-8](https://doi.org/10.1016/0012-821X(94)90184-8)
- 651 Fontaine, F. R., Roullet, G., Hejrani, B., Michon, L., Ferrazzini, V., Barruol, G., et al. (2019). Very- and  
652 ultra-long-period seismic signals prior to and during caldera formation on La Réunion Island.  
653 *Scientific Reports*, 9(1). <https://doi.org/10.1038/s41598-019-44439-1>
- 654 Frohlich, C. (1994). Earthquakes with Non-Double-Couple Mechanisms. *Science*, 264(5160), 804–  
655 809. <https://doi.org/10.1126/science.264.5160.804>
- 656 Fukao, Y., Sandanbata, O., Sugioka, H., Ito, A., Shiobara, H., Watada, S., & Satake, K. (2018).  
657 Mechanism of the 2015 volcanic tsunami earthquake near Torishima, Japan. *Science Advances*,  
658 4(4). <https://doi.org/10.1126/sciadv.aao0219>
- 659 Geist, D. J., Harpp, K. S., Naumann, T. R., Poland, M., Chadwick, W. W., Hall, M., & Rader, E.  
660 (2008). The 2005 eruption of Sierra Negra volcano, Galápagos, Ecuador. *Bulletin of*  
661 *Volcanology*, 70(6), 655–673. <https://doi.org/10.1007/s00445-007-0160-3>
- 662 Geyer, A., & Martí, J. (2014). A short review of our current understanding of the development of ring  
663 faults during collapse caldera formation. *Frontiers in Earth Science*, 2(September), 1–13.  
664 <https://doi.org/10.3389/feart.2014.00022>
- 665 Gilbert, F. (1971). Excitation of the Normal Modes of the Earth by Earthquake Sources. *Geophysical*  
666 *Journal of the Royal Astronomical Society*, 22(2), 223–226.  
667 <https://doi.org/10.1111/j.1365-246X.1971.tb03593.x>

- 668 Global Volcanism Program. (2005). Report on Sierra Negra (Ecuador). *Bulletin of the Global*  
669 *Volcanism Network*, 30(9). <https://doi.org/10.5479/si.GVP.BGVN200509-353050>
- 670 Global Volcanism Program. (2018). Report on Sierra Negra (Ecuador). *Bulletin of the Global*  
671 *Volcanism Network*, 43(9). <https://doi.org/10.5479/si.GVP.BGVN201809-353050>
- 672 Gudmundsson, M. T., Jónsdóttir, K., Hooper, A., Holohan, E. P., Halldórsson, S. A., Ófeigsson, B. G.,  
673 et al. (2016). Gradual caldera collapse at Bárðarbunga volcano, Iceland, regulated by lateral  
674 magma outflow. *Science*, 353(6296). <https://doi.org/10.1126/science.aaf8988>
- 675 Gusman, A. R., Kaneko, Y., Power, W., & Burbidge, D. (2020). Source model for two enigmatic  
676 repeating vertical-T CLVD tsunami earthquakes in the Kermadec Ridge. *Geophysical*  
677 *Research Letters*, 47(16). <https://doi.org/10.1029/2020gl087805>
- 678 Hanks, T. C., & Kanamori, H. (1979). A moment magnitude scale. In *Journal of Geophysical*  
679 *Research B: Solid Earth*. <https://doi.org/10.1029/JB084iB05p02348>
- 680 Hayes, G. P., Rivera, L., & Kanamori, H. (2009). Source inversion of the W-phase: Realtime  
681 implementation and extension to low magnitudes. *Seismological Research Letters*, 80(5), 817–  
682 822. <https://doi.org/10.1785/gssrl.80.5.817>
- 683 Hejrani, B., & Tkalčić, H. (2020). Resolvability of the centroid-moment-tensors for shallow seismic  
684 sources and improvements from modelling high-frequency waveforms. *Journal of*  
685 *Geophysical Research: Solid Earth*, (February 2019), 1–13.

- 686 <https://doi.org/10.1029/2020JB019643>
- 687 Jónsson, S. (2009). Stress interaction between magma accumulation and trapdoor faulting on Sierra  
688 Negra volcano, Galápagos. *Tectonophysics*, 471(1–2), 36–44.  
689 <https://doi.org/10.1016/j.tecto.2008.08.005>
- 690 Kanamori, H., Given, J. W., & Lay, T. (1984). Analysis of seismic body waves excited by the Mount  
691 St. Helens eruption of May 18, 1980. *Journal of Geophysical Research: Solid Earth*, 89(B3),  
692 1856–1866. <https://doi.org/10.1029/JB089iB03p01856>
- 693 Kanamori, H. (1977). The energy release in great earthquakes. *Journal of Geophysical Research*.  
694 <https://doi.org/10.1029/jb082i020p02981>
- 695 Kanamori, H., Ekström, G., Dziewonski, A., Barker, J. S., & Sipkin, S. A. (1993). Seismic radiation  
696 by magma injection: An anomalous seismic event near Tori Shima, Japan. *Journal of*  
697 *Geophysical Research: Solid Earth*, 98(B4), 6511–6522. <https://doi.org/10.1029/92JB02867>
- 698 Kanamori, H., & Given, J. W. (1982). Analysis of long-period seismic waves excited by the May 18,  
699 1980, eruption of Mount St. Helens-A terrestrial monopole? *Journal of Geophysical Research:*  
700 *Solid Earth*, 87(B7), 5422–5432. <https://doi.org/10.1029/JB087iB07p05422>
- 701 Kanamori, H., & Given, J. W. (1981). Use of long-period surface waves for rapid determination of  
702 earthquake-source parameters. *Physics of the Earth and Planetary Interiors*, 27(1), 8–31.  
703 [https://doi.org/10.1016/0031-9201\(81\)90083-2](https://doi.org/10.1016/0031-9201(81)90083-2)

- 704 Kanamori, H., & Mori, J. (1992). Harmonic excitation of mantle Rayleigh waves by the 1991  
705 eruption of Mount Pinatubo, Philippines. *Geophysical Research Letters*, *19*(7), 721–724.  
706 <https://doi.org/10.1029/92GL00258>
- 707 Kanamori, H., & Rivera, L. (2008). Source inversion of W phase: Speeding up seismic tsunami  
708 warning. *Geophysical Journal International*, *175*(1), 222–238.  
709 <https://doi.org/10.1111/j.1365-246X.2008.03887.x>
- 710 Kawakatsu, H., & Yamamoto, M. (2015). *Volcano Seismology. Treatise on Geophysics: Second*  
711 *Edition* (Vol. 4). Elsevier B.V. <https://doi.org/10.1016/B978-0-444-53802-4.00081-6>
- 712 Kawakatsu, H. (1996). Observability of the isotropic component of a moment tensor. *Geophysical*  
713 *Journal International*, *126*(2), 525–544. <https://doi.org/10.1111/j.1365-246X.1996.tb05308.x>
- 714 La Femina, P. C., Ruiz Paspuel, A. G., Higgins, M., Geirsson, H., Geist, D., & Mothes, P. A. (2018).  
715 The June 26, 2018 Eruption of Sierra Negra Volcano, Galapagos Islands, Ecuador: Pre-,  
716 Co-and Post-Eruptive Deformation from GPS Geodesy. *AGUFM 2018*, V31C-08. Retrieved  
717 from <https://ui.adsabs.harvard.edu/abs/2018AGUFM.V31C..08L>
- 718 McKee, C. O., Lowenstein, P. L., De Saint Ours, P., Talai, B., Itikarai, I., & Mori, J. J. (1984). Seismic  
719 and ground deformation crises at Rabaul Caldera: Prelude to an eruption? *Bulletin*  
720 *Volcanologique*, *47*(2), 397–411. <https://doi.org/10.1007/BF01961569>
- 721 McNutt, S. R. (2002). 25 Volcano seismology and monitoring for eruptions. *International*

- 722 *Geophysics*, 81(A), 383–406. [https://doi.org/10.1016/S0074-6142\(02\)80228-5](https://doi.org/10.1016/S0074-6142(02)80228-5)
- 723 Mori, J., & McKee, C. (1987). Outward-dipping ring- fault structure at Rabaul Caldera as shown by  
724 earthquake locations (Papua New Guinea). *Science*, 235(4785), 193–195.  
725 <https://doi.org/10.1126/science.235.4785.193>
- 726 Mori, J., McKee, C., Itikarai, I., Lowenstein, P., de Saint Ours, P., & Talai, B. (1989). Earthquakes of  
727 the Rabaul Seismo-Deformational Crisis September 1983 to July 1985: Seismicity on a  
728 Caldera Ring Fault (pp. 429–462). Springer, Berlin, Heidelberg.  
729 [https://doi.org/10.1007/978-3-642-73759-6\\_25](https://doi.org/10.1007/978-3-642-73759-6_25)
- 730 Neal, C. A., Brantley, S. R., Antolik, L., Babb, J. L., Burgess, M., Calles, K., et al. (2019). The 2018  
731 rift eruption and summit collapse of Kīlauea Volcano. *Science*, 363(6425), 367–374.  
732 <https://doi.org/10.1126/science.aav7046>
- 733 Nettles, M., & Ekström, G. (1998). Faulting mechanism of anomalous earthquakes near Bárðarbunga  
734 Volcano, Iceland. *Journal of Geophysical Research: Solid Earth*, 103(8), 17973–17983.  
735 <https://doi.org/10.1029/98jb01392>
- 736 Parks, M. M., Heimisson, E. R., Sigmundsson, F., Hooper, A., Vogfjörd, K. S., Árnadóttir, T., et al.  
737 (2017). Evolution of deformation and stress changes during the caldera collapse and dyking at  
738 Bárðarbunga, 2014–2015: Implication for triggering of seismicity at nearby Tungnafellsjökull  
739 volcano. *Earth and Planetary Science Letters*, 462, 212–223.  
740 <https://doi.org/10.1016/j.epsl.2017.01.020>

- 741 Reynolds, R. W., Geist, D., & Kurz, M. D. (1995). Physical volcanology and structural development  
742 of Sierra Negra volcano, Isabela Island, Galapagos archipelago. *Geological Society of America*  
743 *Bulletin*, 107(12), 1398–1410.  
744 [https://doi.org/10.1130/0016-7606\(1995\)107<1398:PVASDO>2.3.CO;2](https://doi.org/10.1130/0016-7606(1995)107<1398:PVASDO>2.3.CO;2)
- 745 Riel, B., Milillo, P., Simons, M., Lundgren, P., Kanamori, H., & Samsonov, S. (2015). The collapse of  
746 Bárðarbunga caldera, Iceland. *Geophysical Journal International*, 202(1), 446–453.  
747 <https://doi.org/10.1093/gji/ggv157>
- 748 Sandanbata, O., Watada, S., Satake, K., Fukao, Y., Sugioka, H., Ito, A., & Shiobara, H. (2018). Ray  
749 Tracing for Dispersive Tsunamis and Source Amplitude Estimation Based on Green's Law:  
750 Application to the 2015 Volcanic Tsunami Earthquake Near Torishima, South of Japan. *Pure*  
751 *and Applied Geophysics*, 175(4), 1371–1385. <https://doi.org/10.1007/s00024-017-1746-0>
- 752 Satake, K., & Kanamori, H. (1991). Abnormal tsunamis caused by the June 13, 1984, Torishima,  
753 Japan, earthquake. *Journal of Geophysical Research*, 96(B12), 933–939.  
754 <https://doi.org/10.1029/91jb01903>
- 755 Segall, P., Anderson, K. R., Johanson, I., & Miklius, A. (2019). Mechanics of Inflationary  
756 Deformation During Caldera Collapse: Evidence From the 2018 Kīlauea Eruption.  
757 *Geophysical Research Letters*, 46(21), 11782–11789. <https://doi.org/10.1029/2019GL084689>
- 758 Segall, P., Anderson, K. R., Pulvirenti, F., Wang, T., & Johanson, I. (2020). Caldera collapse  
759 geometry revealed by near-field GPS displacements at Kīlauea Volcano in 2018. *Geophysical*

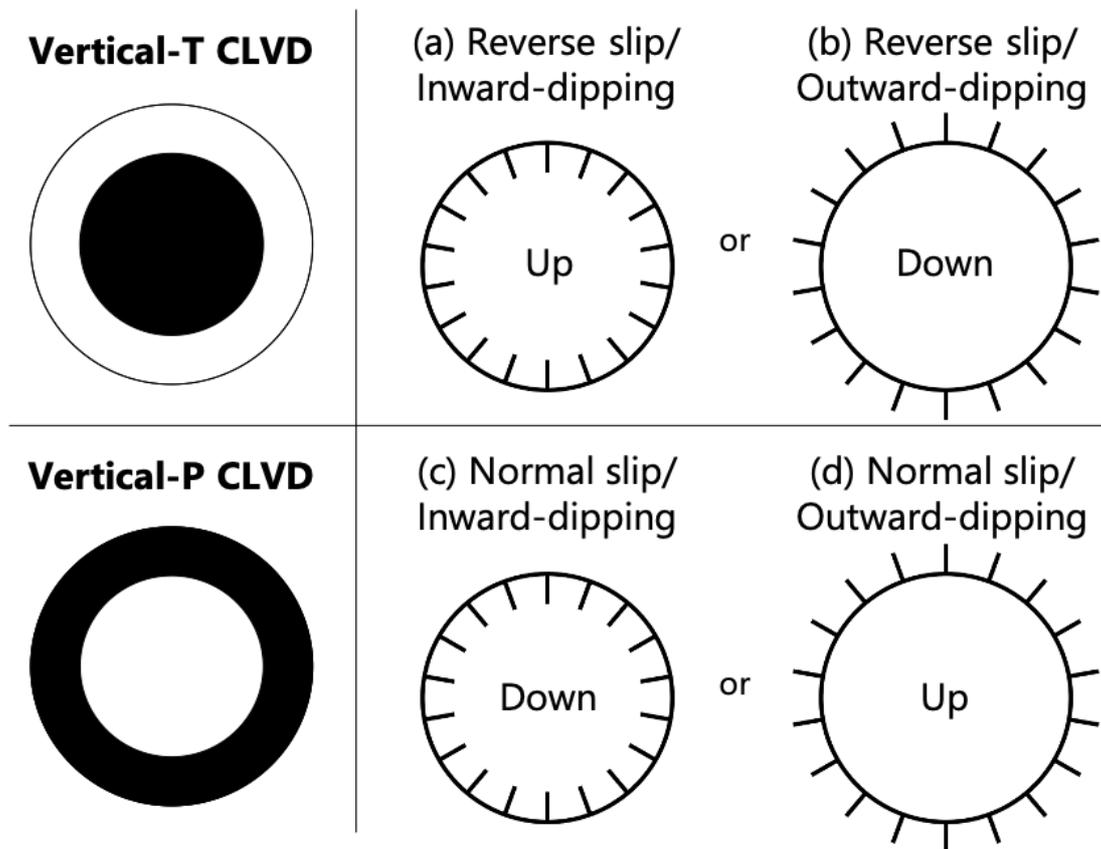
- 760 *Research Letters*, 1–17. <https://doi.org/10.1029/2020GL088867>
- 761 Shearer, P. M. (2009). *Introduction to Seismology. Geophysical Journal of the Royal Astronomical*  
762 *Society* (Vol. 40). Cambridge: Cambridge University Press.  
763 <https://doi.org/10.1017/CBO9780511841552>
- 764 Shuler, A., & Ekström, G. (2009). Anomalous earthquakes associated with Nyiragongo Volcano:  
765 Observations and potential mechanisms. *Journal of Volcanology and Geothermal Research*,  
766 *181*(3–4), 219–230. <https://doi.org/10.1016/j.jvolgeores.2009.01.011>
- 767 Shuler, A., Nettles, M., & Ekström, G. (2013a). Global observation of vertical-CLVD earthquakes at  
768 active volcanoes. *Journal of Geophysical Research: Solid Earth*, *118*(1), 138–164.  
769 <https://doi.org/10.1029/2012JB009721>
- 770 Shuler, A., Ekström, G., & Nettles, M. (2013b). Physical mechanisms for vertical-CLVD earthquakes  
771 at active volcanoes. *Journal of Geophysical Research: Solid Earth*, *118*(4), 1569–1586.  
772 <https://doi.org/10.1002/jgrb.50131>
- 773 Silver, P. G., & Jordan, T. H. (1982). Optimal estimation of scalar seismic moment. *Geophysical*  
774 *Journal of the Royal Astronomical Society*, *70*(3), 755–787.  
775 <https://doi.org/10.1111/j.1365-246X.1982.tb05982.x>
- 776 Tadono, T., Ishida, H., Oda, F., Naito, S., Minakawa, K., & Iwamoto, H. (2014). Precise Global DEM  
777 Generation by ALOS PRISM. *ISPRS Annals of Photogrammetry, Remote Sensing and Spatial*

- 778 *Information Sciences*, II-4(May), 71–76. <https://doi.org/10.5194/isprsannals-ii-4-71-2014>
- 779 Takeuchi, H., & Saito, M. (1972). Seismic Surface Waves. In *Methods in Computational Physics: Advances in Research and Applications* (Vol. 11, pp. 217–295).  
780  
781 <https://doi.org/10.1016/B978-0-12-460811-5.50010-6>
- 782 Tepp, G., Hotovec-Ellis, A., Shiro, B., Johanson, I., Thelen, W., & Haney, M. M. (2020). Seismic and  
783 geodetic progression of the 2018 summit caldera collapse of Kīlauea volcano. *Earth and Planetary Science Letters*, 540, 116250. <https://doi.org/10.1016/j.epsl.2020.116250>  
784
- 785 Vasconez, F., Ramón, P., Hernandez, S., Hidalgo, S., Bernard, B., Ruiz, M., et al. (2018). The  
786 different characteristics of the recent eruptions of Fernandina and Sierra Negra volcanoes  
787 (Galápagos, Ecuador). *Volcanica*, 1(2), 127–133. <https://doi.org/10.30909/vol.01.02.127133>
- 788 Wimpenny, S., & Watson, C. S. (2020). gWFM: A Global Catalog of Moderate-Magnitude  
789 Earthquakes Studied Using Teleseismic Body Waves. *Seismological Research Letters*.  
790 <https://doi.org/10.1785/0220200218>
- 791 Yun, S., Segall, P., & Zebker, H. (2006). Constraints on magma chamber geometry at Sierra Negra  
792 Volcano, Galápagos Islands, based on InSAR observations. *Journal of Volcanology and Geothermal Research*, 150(1–3), 232–243. <https://doi.org/10.1016/j.jvolgeores.2005.07.009>  
793
- 794 Yun, S.-H. (2007). A mechanical model of the large-deformation 2005 Sierra Negra volcanic  
795 eruption derived from InSAR measurements. *PhD Thesis, Department of Geophysics, Stanford*

796 *University.*

797

798 **Figures and tables**

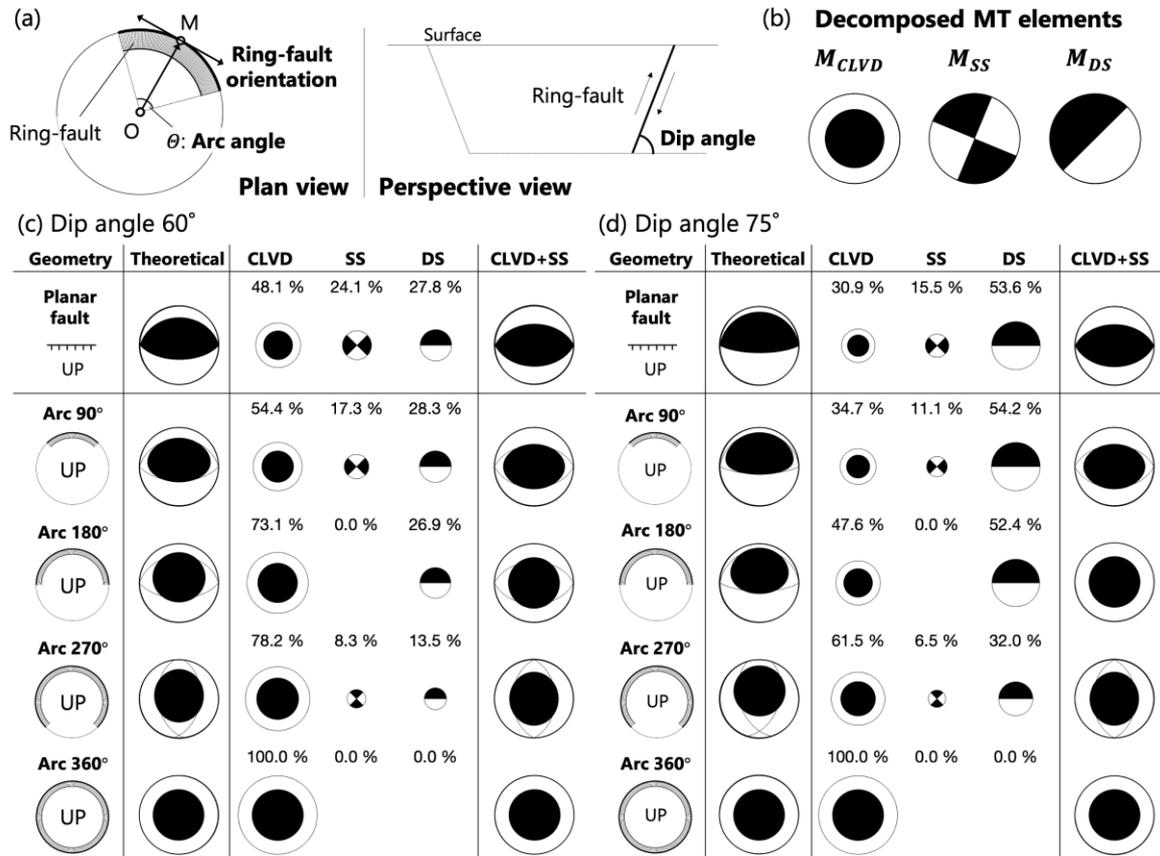


799

800 **Figure 1 Two types of vertical-CLVD earthquake caused by ring-faulting.**

801 (a–d) The kinematics and geometry of ring-faulting corresponding to the two endmembers of  
 802 vertical-CLVD earthquakes (shown on the left). The circle represents the up-dip end of the ring  
 803 fault, with short lines indicating the dip direction to the down-dip end. The direction of motion of  
 804 the central block is indicated at the center of the circle.

805



806

807 **Figure 2 Modeling and decomposition of theoretical moment tensors of idealized ring-faulting.**

808 (a) Ring-fault parameters. Thick and thin arc curves represent up-dip and down-dip ends,

809 respectively. The ring fault is discretized by rhomboidal planar faults with an arc angle of  $1^\circ$ , each

810 of which has a reverse slip of 1 m. Arc and dip angles and the *ring-fault azimuth* ( $\overrightarrow{OM}$ ) are variable

811 parameters. The *ring-fault orientation* is perpendicular to the ring-fault azimuth. The *dip angle* is

812 uniform along the ring fault. (b) Three decomposed moment tensor (MT) components. (c–d)

813 Theoretical MTs of ring-faulting with arc angles of  $90^\circ$ ,  $180^\circ$ ,  $270^\circ$ , and  $360^\circ$  and with dip angles

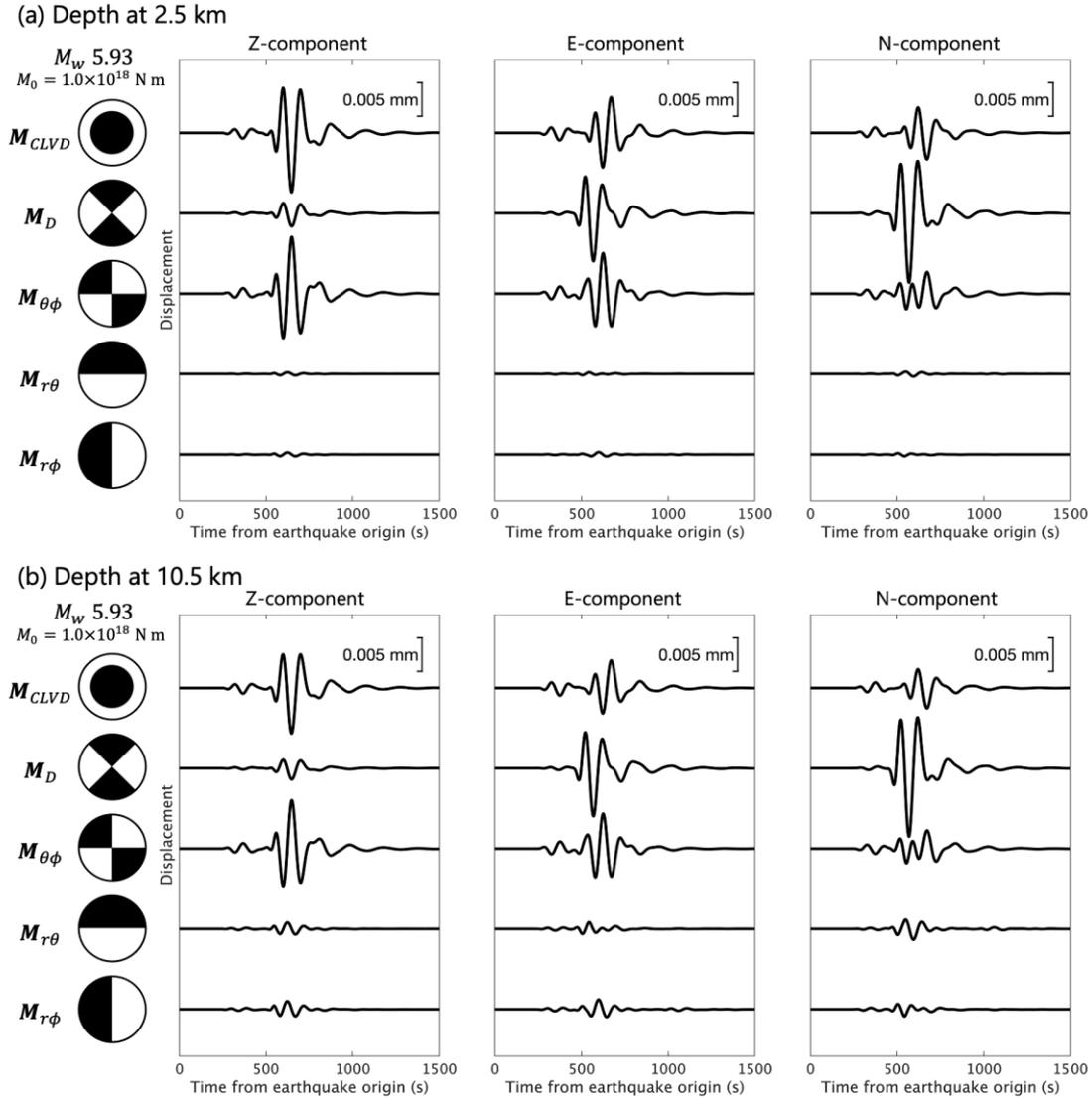
814 of (c)  $60^\circ$  and (d)  $75^\circ$ . Columns: (1) kinematics and geometry of ring-faulting, (2–6) focal

815 mechanism diagrams of the theoretical MT (2), decomposed MT components (*CLVD*, *SS*, and *DS*)

816 with their ratios (3–5), and resolvable MTs (6). The orientation of the *best double-couple solution*

817 is shown by thin curves in columns 2 and 6. All focal mechanisms are shown by projection of the  
818 lower focal hemisphere. The diameter of the focal mechanism diagram is proportional to its scalar  
819 moment but slightly exaggerated for the component with percentages of <10% for clear  
820 visualization. Thin curves on the diagram represent the nodal planes of the best-fitting  
821 double-couple moment tensor (see text in Section 2.2).

822



823

824 **Figure 3 Synthetic long-period seismic waves from five components of a moment tensor.**

825

Synthetic long-period seismic waveforms from sources representing five components of a moment

826

tensor. The centroid depth is (a) 2.5 km and (b) 10.5 km below the solid surface.  $M_D$  and  $M_{\theta\phi}$

827

determine the *SS* component, and  $M_{r\theta}$  and  $M_{r\phi}$  determine the *DS* component. The virtual

828

station is located at  $(\varphi, \Delta) = (19.2^\circ, 17.8^\circ)$ , where  $\varphi$  is the station azimuth from north (eastward

829

positive), and  $\Delta$  is the distance from the source. We used the W-phase code (Kanamori and Rivera,

830

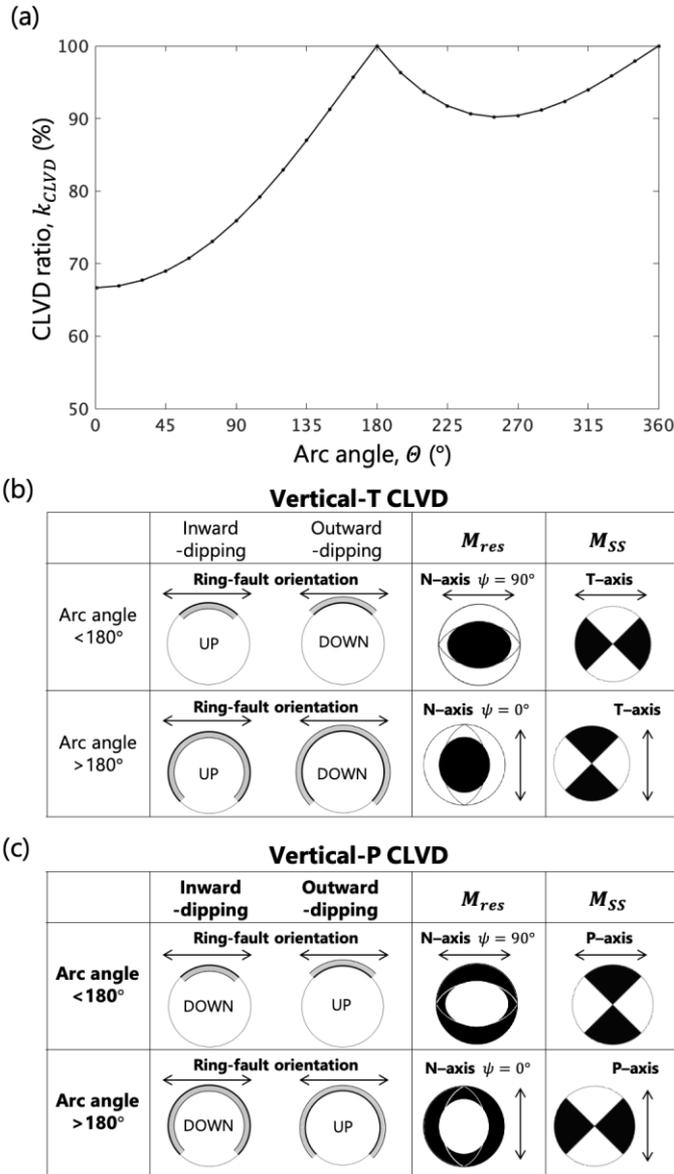
2008; Hayes et al., 2009; Duputel et al., 2012) for the convolution of Green's functions and

831

filtering. Green's functions are computed by the normal mode method (e.g., Takeuchi and Saito,

832 1972), with the 1-D Preliminary Reference Earth Model (PREM; Dziewonski and Anderson,  
833 1981). A one-pass and fourth-order Butterworth Bandpass filter with corner frequencies of 0.005  
834 and 0.0125 Hz was applied.

835



836

837 **Figure 4 Relationship between  $M_{res}$  and fault parameters of ring-faulting.**

838

(a) The CLVD ratio,  $k_{CLVD}$ , in the resolvable MT,  $M_{res}$ , as a function of arc angle  $\theta$ . Note that

839

the relationship between  $k_{CLVD}$  and  $\theta$  is independent of the dip angle of the ring fault. (b–c)

840

Relationship between ring-fault geometry and  $M_{res}$  for (b) vertical-T earthquakes and (c)

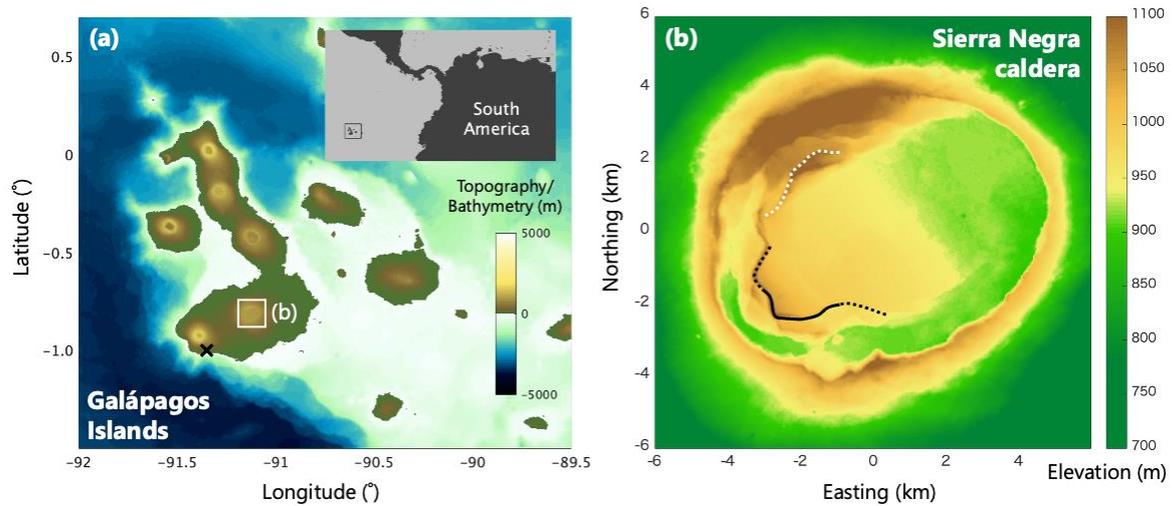
841

vertical-P earthquakes. In the 2nd column, the dip direction of the ring fault (inward or outward),

842

the kinematics of the central block (up or down), and the ring-fault orientation (an arrow) are also

843 shown. In the 3rd column,  $\mathbf{M}_{res}$  is shown with the orientation of its *N-axis* (arrow). In the 4th  
844 column, the *SS* component is shown with its T- or P-axis (arrow). Note that the N-axis of  $\mathbf{M}_{res}$  is  
845 the same as the T- and P-axes of the *SS* component for vertical-T and vertical-P earthquakes,  
846 respectively.

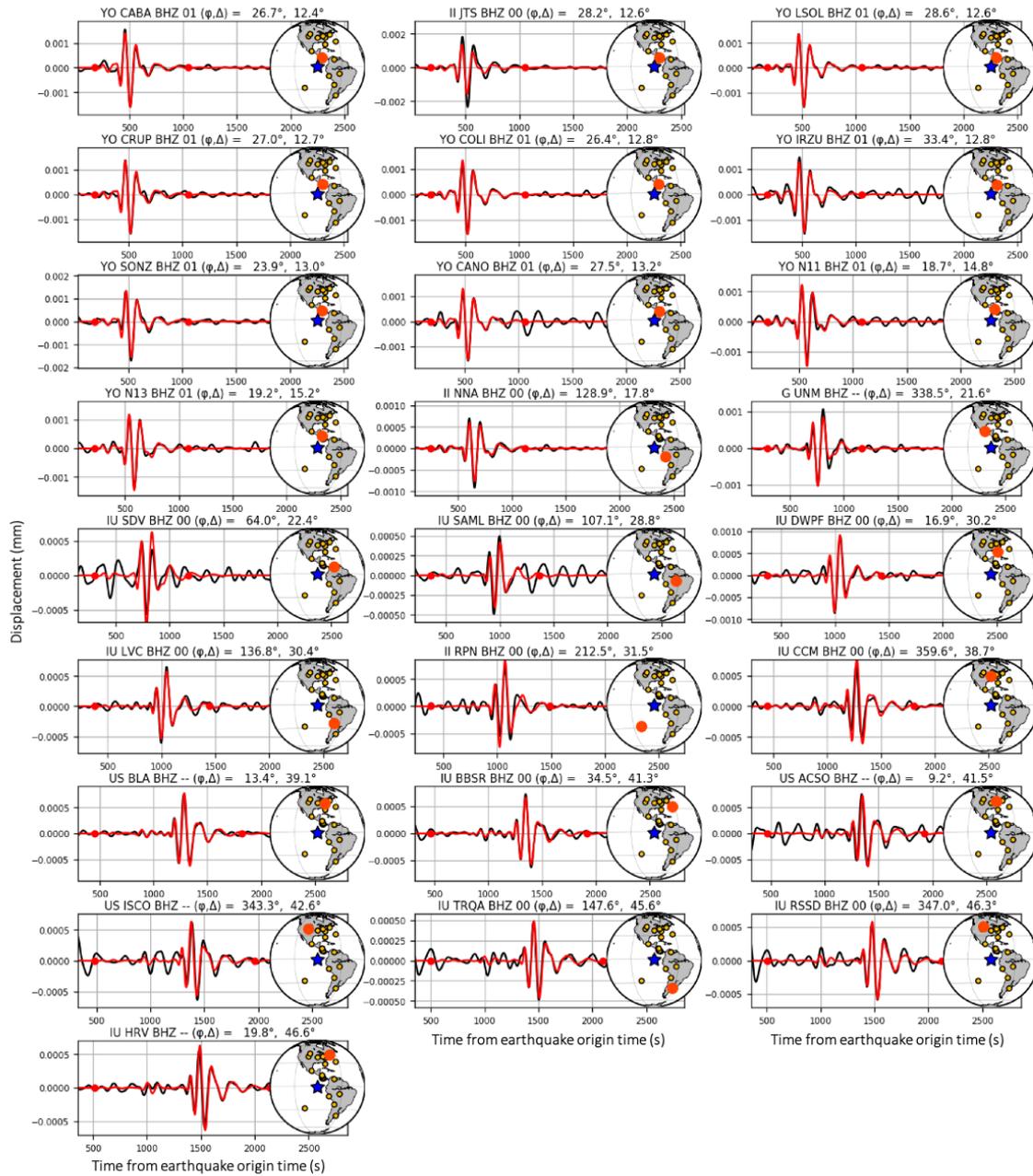


847

848 **Figure 5 Maps of the Galápagos Islands and the Sierra Negra caldera.**

849 (a) Map of the Galápagos Islands. Topographic and bathymetric data were downloaded from  
 850 GEBCO 2019. The black rectangle in the inset panel indicates the area shown in (a). The black  
 851 cross represents the centroid location of the vertical-T earthquake of 22 October 2005 reported in  
 852 the GCMT Catalog. (b) Map of the Sierra Negra caldera. Topographic data were downloaded from  
 853 the Advance Land Observation Satellite (ALOS) World 3D–30 m DEM (AW3D30) provided by  
 854 the Japan Aerospace Exploration Agency (JAXA) (e.g., Tadono et al., 2014). The black curve  
 855 indicates the fresh vertical scarp identified by Geist et al. (2008) during a field survey in June 2006.  
 856 The part represented by the solid curve was clearly identified, whereas those along the dotted  
 857 curves were less clearly defined. The dotted white curve indicates a possible geometry inferred in  
 858 this study for the 2018 vertical-P earthquake (see text in Section 3.4).

859



860

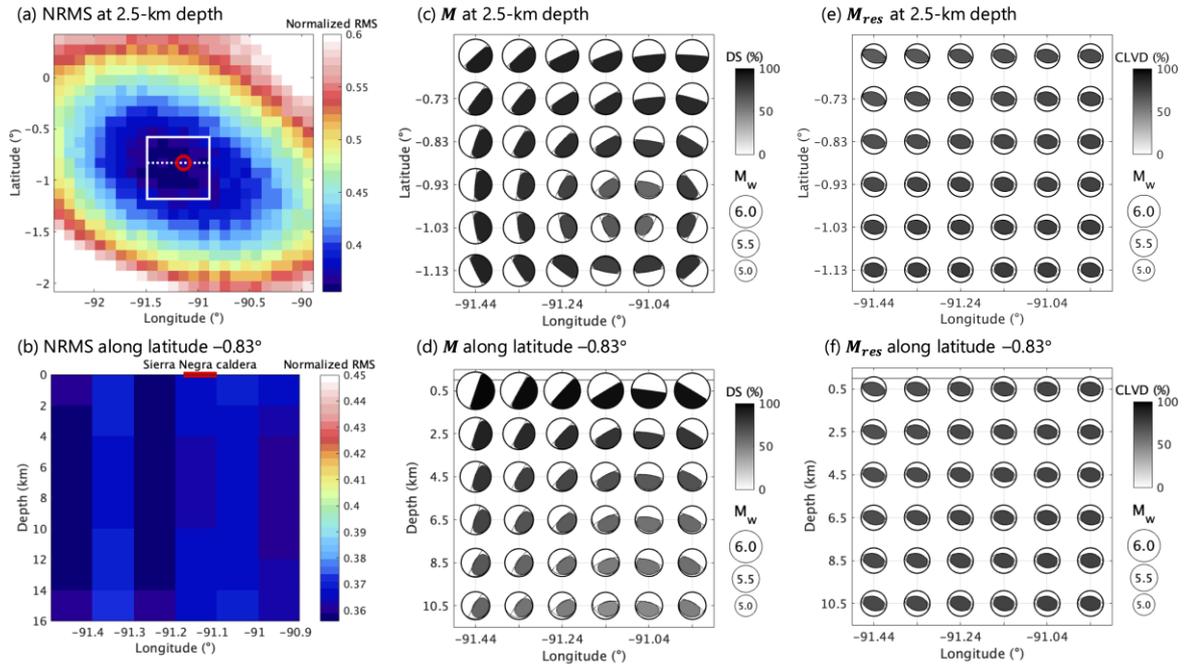
861 **Figure 6 Model performance of MT inversion for the  $M_w$  5.5 vertical-T CLVD earthquake of 22**

862 **October 2005.**

863 Red and black lines represent synthetic and observed waveforms, respectively. The start and end

864 points of the inversion time window are indicated by red circles. In each inset map, the blue star

865 and large red circle represent locations of the epicenter (0.83°S, 91.14°W) and the station. The  
866 station azimuth ( $\varphi$ ) and epicentral distance ( $\Delta$ ) are indicated at the top of each panel.



867

868 **Figure 7 MT inversion for the vertical-T CLVD earthquake of 22 October 2005 at the Sierra**

869 **Negra caldera.**

870 (a–b) NRMS misfits of MT solutions at source locations distributed on (a) the x–y plane at a depth

871 of 2.5 km and (b) the x–z plane along a latitude of 0.83° (dashed white line in (a)). The red circle in

872 (a) and the red line in (b) represent the approximate locations of the Sierra Negra caldera. (c) MT

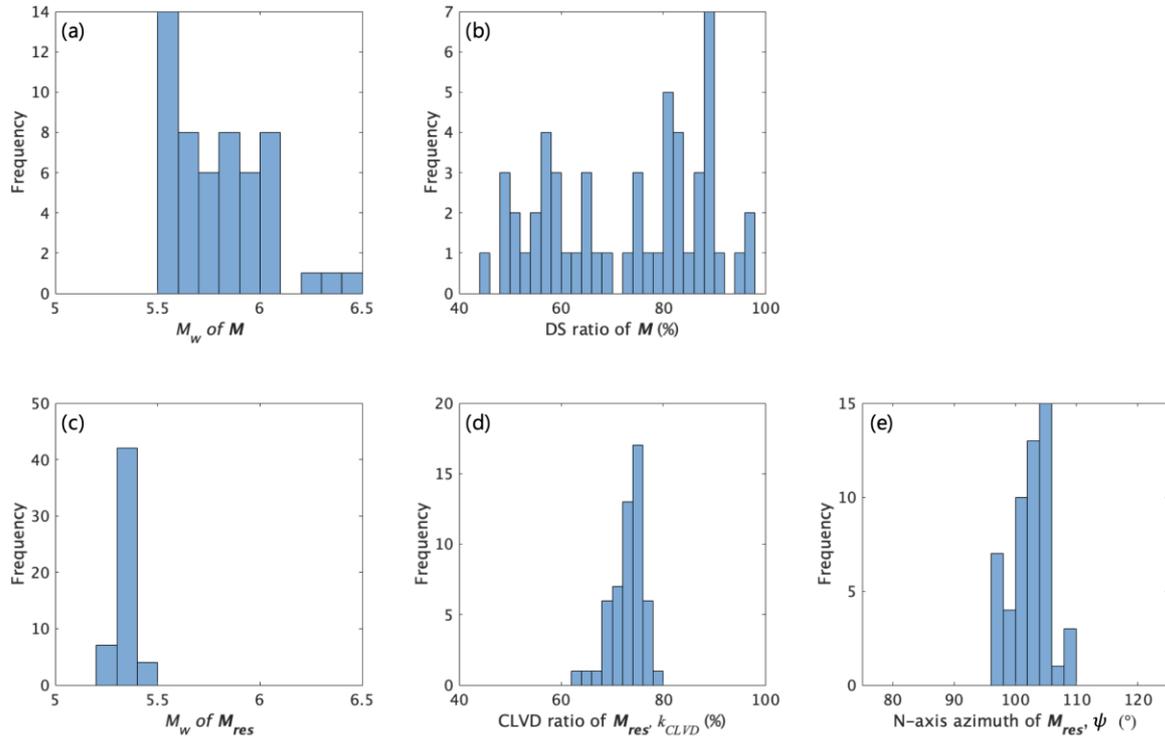
873 solutions at different centroid locations on (c) the x–y plane at a depth of 2.5 km in the area shown

874 by the white rectangle in (a) and (d) the x–z plane along a latitude of 0.83°. (e–f) Resolvable MTs

875 on (e) the x–y plane and (f) the x–z plane. All focal mechanisms are shown by projection of the

876 lower focal hemisphere.

877



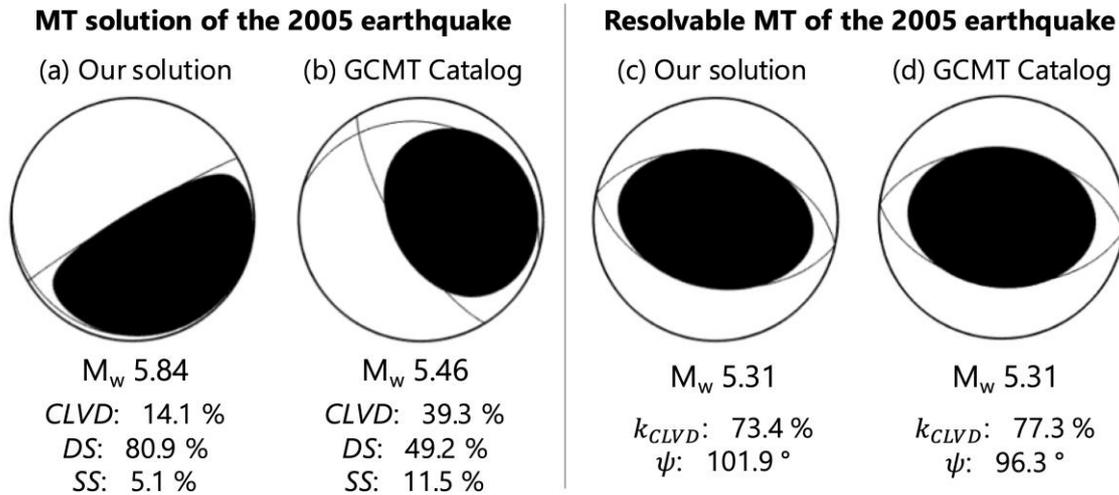
878

879 **Figure 8 Histogram of the parameters of acceptable MT solutions.**

880 (a)  $M_w$  and (b) the ratio of the  $DS$  component of acceptable MT solutions. (c)  $M_w$ , (d) the CLVD

881 ratio  $k_{CLVD}$ , and (e) the N-axis azimuth  $\psi$  of  $M_{res}$  extracted from acceptable MT solutions.

882



883

884 **Figure 9 MT solutions and resolvable MTs of the  $M_w$  5.5 vertical-T CLVD earthquake of 22**

885 **October 2005.**

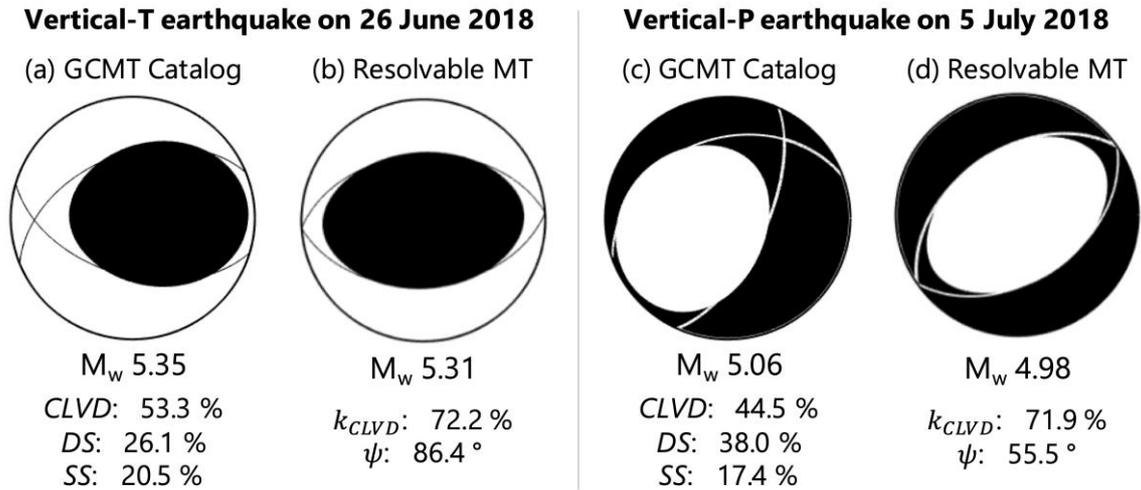
886 (a) MT solution with the ratios of components and (c) resolvable MT with the ratio of the CLVD

887 component  $k_{CLVD}$  to the N-axis azimuth  $\psi$  obtained from our MT inversion at a depth of 2.5 km

888 just below the caldera. (b) MT and (d) resolvable MT obtained from the GCMT Catalog. All focal

889 mechanisms are shown by projection of the lower focal hemisphere.

890



891

892 **Figure 10 GCMT solutions for two vertical-CLVD earthquakes during the 2018 volcanic activity.**

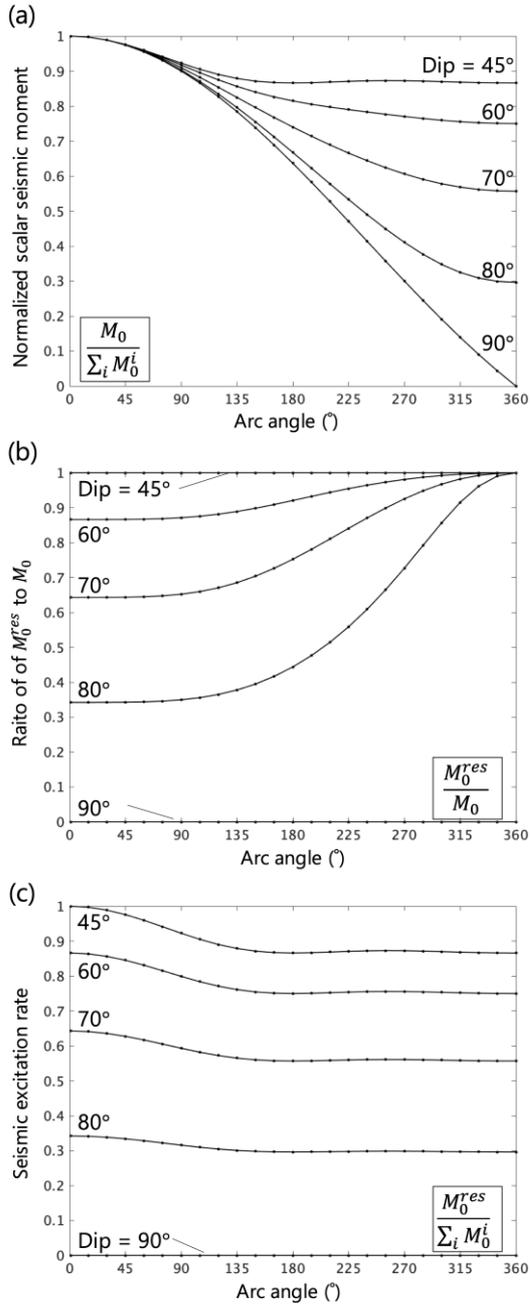
893 (a) MT solution with the ratios of components and (b) resolvable MT of the  $M_w$  5.3 earthquake of

894 26 June 2018 with the ratio of the *CLVD* component  $k_{CLVD}$  to the N-axis azimuth  $\psi$  obtained

895 from the GCMT Catalog. (c–d) The same as (a–b) but for the  $M_w$  5.1 earthquake of 5 July 2018. All

896 focal mechanisms are shown by projection of the lower focal hemisphere.

897



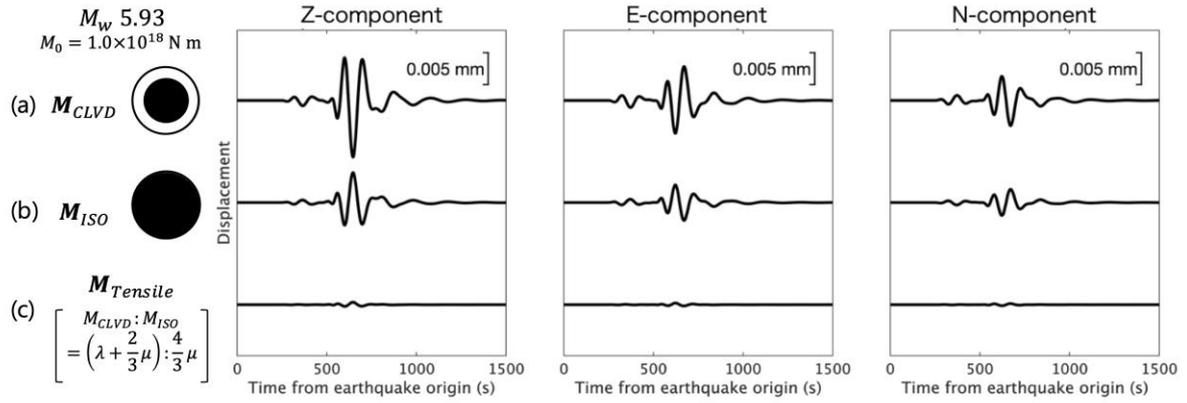
898

899 **Figure 11 Seismic excitation rate of ring-faulting at a shallow source depth.**

900 (a) Geometrical cancellation of the scalar moment of idealized ring-faulting, calculated using

901 Equation (13). (b) The ratio of  $M_0^{res}$  to  $M_0$  of idealized ring-faulting, calculated using Equation

902 (14). (c) The combined effect of (a) and (b), calculated using Equation (15).



903

904 **Figure 12 Effects of an isotropic source on estimation of the CLVD source.**

905 Synthetic long-period seismic waveforms of (a) a CLVD source (Equation 25), (b) an isotropic

906 source (Equation 26), and (c) a horizontal tensile source (Equation 27). The MT of the horizontal

907 tensile crack consists of *CLVD* and *ISO* components with a ratio of  $M_{ISO} : M_{CLVD} = \left( \lambda + \frac{2}{3}\mu \right) : \frac{4}{3}\mu$ ,

908 as given in Equation (17). The centroid depth is assumed to be 2.5 km below the solid surface. The

909 station location and filtering procedure are the same as those used for Figure 3.

910

Event date	Source of solution	Longitude (°W)	Latitude (°S)	Depth (km)	Elements of moment tensor (dyne cm)						Scale factor (10 <sup>19</sup> )	$M_w$
					$M_{rr}$	$M_{\theta\theta}$	$M_{\phi\phi}$	$M_{r\theta}$	$M_{r\phi}$	$M_{\theta\phi}$		
22 October 2005	This study	91.14	0.83	2.5	1.246	-1.035	-0.210	-6.127	-3.718	0.182	24	5.84
22 October 2005	GCMT	91.35	1.00	12.0	1.260	-0.989	-0.268	0.459	-1.510	0.080	24	5.46
26 June 2018	GCMT	91.33	0.96	12.0	1.230	-1.090	-0.148	0.118	-0.592	-0.059	24	5.35
5 July 2018	GCMT	90.98	0.88	12.0	-3.880	2.490	1.400	0.314	-3.300	1.420	23	5.06

911

912 **Table 1 Moment tensor solutions of vertical-CLVD earthquakes for the Sierra Negra caldera.**

913 Centroids and moment tensor solutions of vertical-CLVD earthquakes for the Sierra Negra caldera

914 obtained by MT inversion in this study or taken from the GCMT Catalog. Note that the centroid

915 depth of the GCMT Catalog may be determined at a greater depth (12 km) than the accrual

916 centroid depth of the earthquakes to maintain the stability of the solutions (Ekström et al., 2012).