

# Key factors determining nightside energetic electron losses driven by whistler-mode waves

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## Key Points:

- Comparing ELFIN data with test particle and quasi-linear simulations, we investigate whistler-driven electron precipitation on the nightside
- A reduction in background plasma density is key to enabling whistler-mode waves to efficiently scatter electrons up to 1 MeV
- Decreasing wave frequency as a function of latitude and wave obliquity, are both integral to capturing realistic nightside electron losses

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## Abstract

Energetic electron losses by pitch-angle scattering and precipitation to the atmosphere from the radiation belts are controlled, to a great extent, by resonant wave particle interactions with whistler-mode waves. The efficacy of such precipitation is primarily controlled by wave intensity, although its relative importance, compared to other wave and plasma parameters, remains unclear. Precipitation spectra from the low-altitude, polar-orbiting ELFING mission have previously been demonstrated to be consistent with energetic precipitation modeling derived from empirical models of field-aligned wave power across a wide-swath of local-time sectors. However, such modeling could not explain the intense, relativistic electron precipitation observed on the nightside. Therefore, this study aims to additionally consider the contributions of three modifications – wave obliquity, frequency spectrum, and local plasma density – to explain this discrepancy on the nightside. By incorporating these effects into both test particle simulations and quasi-linear diffusion modeling, we find that realistic implementations of each individual modification result in only slight changes to the electron precipitation spectrum. However, these modifications, when combined, enable more accurate modeling of ELFING-observed spectra. In particular, a significant reduction in plasma density enables lower frequency waves, oblique, or even quasi-field aligned waves to resonate with near  $\sim 1$  MeV electrons closer to the equator. We demonstrate that the levels of modification required to accurately reproduce the nightside spectra of whistler-mode wave-driven relativistic electron precipitation match empirical expectations, and should therefore be included in future radiation belt modeling.

## Plain Language Summary

Whistler-mode waves are a type of electromagnetic wave that mediate electron dynamics in Earth’s radiation belts and are simultaneously important for energizing electrons and driving loss mechanisms. Most radiation belt models today do not adequately capture the effects of these waves on relativistic electrons, which are important to study because these energetic electrons are often called “Killer Electrons” for their ability to degrade spacecraft electronics. Additionally, when lost into Earth’s atmosphere, these electrons can also change atmospheric chemistry and ionospheric properties, making them an important input parameters for atmospheric, ionospheric, and magnetospheric modeling. This study uses two different modeling methods to determine which properties of whistler-mode waves are most important for accurately capturing these wave-particle interactions on the nightside, where plasma interactions are more dynamic. The results agree well with statistical results from the Electron Losses and Fields INvestigation (ELFING) mission, allowing us to fully explain the mechanisms behind whistler-mode wave-driven electron losses on the nightside.

## 1 Introduction

Earth’s inner magnetosphere is filled with energetic electron fluxes injected from the plasma sheet, that are then further accelerated via resonant interactions with electromagnetic whistler-mode (chorus) waves (Millan & Baker, 2012; Shprits et al., 2008). These wave-particle interactions are, in great part, also responsible for energetic electron pitch-angle scattering into the loss cone and subsequent electron loss through precipitation into Earth’s atmosphere (Millan & Thorne, 2007; Shprits et al., 2008). This contribution to both acceleration and pitch-angle scattering of energetic electrons makes the whistler-mode wave a crucial element of outer radiation belt dynamics (Bortnik & Thorne, 2007; Thorne, 2010; Li & Hudson, 2019). Not only do energetic radiation belt electrons serve as an important space weather proxy (Horne et al., 2013), relativistic electron can also penetrate deep into the thermosphere/mesosphere (Xu et al., 2020) contributing to ozone depletion (Thorne, 1980; Lam et al., 2010; Turunen et al., 2016). Un-

derstanding the mechanisms behind the global distribution of energetic electron losses is therefore important for studying radiation belt dynamics and atmospheric chemistry.

Energetic ( $\gtrsim 100$  keV) electron losses due to whistler-mode waves is one such topic that has yet to be fully investigated. It is known that these waves can scatter electrons up to 1 MeV (O’Brien et al., 2004; Thorne et al., 2005; Blake & O’Brien, 2016; Shumko et al., 2018; Breneman et al., 2017), which is problematic because current radiation belt models typically only incorporate diffusive losses of sub-relativistic electrons (up to  $\sim 500$  keV). Additionally, previous research (Tsai et al., 2023) has revealed a day-night difference in energetic electrons scattered by whistler-mode waves, with more intense electron precipitation on the dayside than on the nightside. This is attributed to two system-level properties – (1) nightside regions generally have a lower plasma density and (2) nightside wave activity is generally more confined to the equatorial plane (Meredith et al., 2001, 2003; Agapitov et al., 2013) – which both cause strong resonant wave particle interactions to preferentially occur on the dayside, resulting in more extreme energetic electron losses (e.g., Thorne et al., 2005; Mourenas, Artemyev, Agapitov, & Krasnoselskikh, 2014; Wang & Shprits, 2019; Aryan et al., 2020). This is supported by Tsai et al. (2023), which used modeled electron precipitation spectra derived from statistically-averaged wave intensity distributions from Agapitov et al. (2018) to directly compare with statistical observations of electron precipitating fluxes from ELFIND (Angelopoulos et al., 2020). Although these model-data comparisons showed good agreement between electron precipitation and wave power in the dusk and daysides, ELFIND-measured nightside relativistic ( $\gtrsim 500$  keV) precipitating flux rates were substantially larger than anticipated (i.e. modeled) and nearly comparable to that on the dayside. Understanding mechanisms that can cause such intense energetic precipitation is a prerequisite for accurately modeling electron loss in the radiation belts, therefore motivating the need to explore what key factors actually determine nightside electron losses.

There are a few prime candidates that determine the efficiency of wave-particle resonant interactions (and, particularly, the energy dependence of whistler-mode wave driven electron scattering):

1. Wave intensity distribution along magnetic field lines (see discussion in Thorne et al., 2005; Wang & Shprits, 2019).
2. Obliquity of wave propagation relative to the background magnetic field (see discussion in Lorentzen et al., 2001; Mourenas, Artemyev, Agapitov, & Krasnoselskikh, 2014; Artemyev et al., 2016).
3. Wave frequency spectrum and its variation along magnetic field lines (see discussion in Agapitov et al., 2018)
4. Equatorial plasma density magnitude (see discussion in Thorne et al., 2013; Agapitov et al., 2019; Allison & Shprits, 2020) and its variation along magnetic field lines (see discussion in Summers & Ni, 2008; Artemyev et al., 2013).

Having already examined the importance of wave amplitude in Tsai et al. (2023), we now study the remaining three mechanisms which could potentially modulate nightside electron precipitating spectra. First, intense nightside whistler-mode waves are typically associated with strong plasma sheet injections (Tao et al., 2011; Fu et al., 2014; X. Zhang et al., 2018) which are often accompanied by the enhanced convection electric field which transports cold plasma Earthward, thereby decreasing equatorial plasma density (Vasko, Agapitov, Mozer, Bonnell, et al., 2017; Agapitov et al., 2019). A lower plasma density results in a lower plasma frequency; a lower plasma frequency to gyrofrequency ratio,  $f_{pe}/f_{ce}$  yields a higher cyclotron resonance energy  $E_R \propto (f_{ce}/f_{pe})^2$  to  $f_{ce}/f_{pe}$  (from low to high energy) of electrons for given wave frequencies, wave normal angles, and electron pitch-angles (Stix, 1962; Summers et al., 2007; Li, Thorne, Nishimura, et al., 2010; Allison et al., 2021). This nightside localized density reduction can thus potentially increase the scattering rate of relativistic electrons.

Second, statistical observations have shown a clear trend of average wave frequency decreasing with latitude along field lines (i.e. increasing distance from the equatorial plane) (Agapitov et al., 2018). This is likely caused by preferential Landau damping of higher-frequency waves resonating with suprathermal electrons (L. Chen et al., 2013; Watt et al., 2013; Maxworth & Golkowski, 2017). A lower normalized wave frequency  $f/f_{ce}$  means a higher cyclotron resonance energy  $E_R \propto (f_{ce}/f)(1-f/f_{ce})^3$  to  $(f_{ce}/f)^{1/2}(1-f/f_{ce})^{3/2}$  from low to high energy (Li, Thorne, Nishimura, et al., 2010; Mourenas et al., 2012). Thus, this reduction in the mean wave frequency in the nightside off-equatorial region may also increase the scattering rate of relativistic electrons.

Third, plasma injections are often associated with enhanced electrostatic turbulence (Mozer et al., 2015; Agapitov et al., 2015; Vasko, Agapitov, Mozer, Artemyev, et al., 2017; Malaspina et al., 2018) that forms a plateau in the field-aligned velocity distribution and significantly reduces Landau damping of oblique whistler-mode waves (see discussion in Mourenas et al., 2015; Ma et al., 2017; Artemyev & Mourenas, 2020). In this regime, oblique (with wave normal angles below the Gendrin angle  $\theta_G \approx \text{acos}(2f/f_{ce})$ ) and very oblique (with wave normal angle up to the resonant cone angle  $\theta_r \approx \text{acos}(f/f_{ce})$ ) waves may survive Landau damping (see Min et al., 2014; R. Chen et al., 2019; Sauer et al., 2020; Ke et al., 2022). These waves then become oblique off the equatorial plane (Bortnik et al., 2007; L. Chen et al., 2013), or, in more unusual cases, are generated within the equatorial source region (Artemyev et al., 2016; Li, Mourenas, et al., 2016; Agapitov et al., 2016). Wave obliquity not only increases the resonant interaction energy with electrons as  $E_R \propto 1/k_{\parallel}^2 \propto 1/\cos^2 \theta$  (e.g., Verkhoglyadova et al., 2010; Mourenas et al., 2015), but also allows for interactions with electrons at higher-order cyclotron resonances ( $n \gg 1$ , e.g., Shklyar & Matsumoto, 2009; Mourenas et al., 2012; Artemyev et al., 2013; Albert, 2017) which can drastically increase the resonance energy  $E_R \propto n^2$  (e.g., Lorentzen et al., 2001; Gan et al., 2023). Thus, nightside whistler-mode wave obliquity could also potentially increase the scattering rate of relativistic electrons.

Here, we examine each of these three mechanisms to see whether they can explain the enhanced precipitation of relativistic electrons in the nightside MLT sector using a combination of statistics from ELFIN observations (Angelopoulos et al., 2020), test particle simulations (Tsai et al., 2022, 2023), and quasi-linear diffusion code (Ma et al., 2012, 2015). This paper is organized as follows: Section 2 details ELFIN observations/statistics and presents observational evidence of intense nightside precipitation of relativistic electrons; Section 3 describes the basics of the test particle simulation and quasi-linear diffusion codes; Section 4 compares ELFIN data to results from a variety of runs exploring the three main modifications – reduced plasma density, wave obliquity, wave frequency variation along magnetic field lines; finally, Section 5 summarizes and discusses the obtained results.

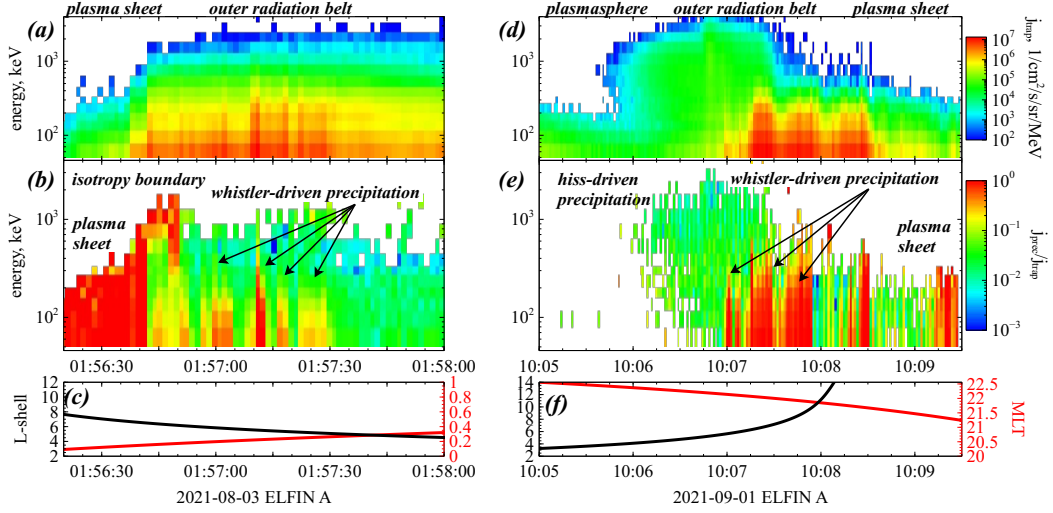
## 2 Data Sets

The ELFIN CubeSats (ELFIN A and B) are identically equipped with an Energetic Particle Detector for Electrons (EPDE), capable of measuring energy and pitch-angle distributions of energetic electrons with  $\Delta E/E = 40\%$  across 16 logarithmically spaced energy channels between 50 keV and 5 MeV (Angelopoulos et al., 2020). Spinning at just over 21 revolutions per minute (spin period  $\approx 2.8$  sec), ELFIN’s 16 sectors per spin yields a spin phase resolution of  $\Delta\alpha = 22.5^\circ$ . The main data product used in this study is the precipitating-to-trapped flux ratio,  $j_{prec}/j_{trap}(E)$ , where  $j_{trap}(E)$  is the locally trapped (outside of the local bounce loss-cone) electron flux and  $j_{prec}(E)$  is the flux integrated over the local loss-cone with a correction to remove the backscattered fluxes from the opposite hemisphere (see details in Mourenas et al., 2021; Angelopoulos et al., 2023). Figure 1 shows two typical examples of ELFIN outer radiation belt crossings on the nightside with  $j_{trap}(E)$  (a,d) and  $j_{prec}/j_{trap}$  (b,e) distributions.

This study utilized 30 months (January 2020 - June 2022) of ELFIN's  $j_{trap}(E)$  and  $j_{prec}(E)$  measurements during strong and bursty energetic electron precipitation events (for details regarding statistical coverage, see Figure 5 in Tsai et al., 2023). In order to obtain a statistical representation of whistler-mode-driven electron precipitation, data was selected based on data quality (minimum 4 counts/second for any given energy or pitch angle bin) and precipitation intensity ( $j_{prec}(E)/j_{trap}(E) > 0.5$  at ELFIN's lowest energy bin of 63 keV). In addition, there were provisions to identify and remove electron precipitation events driven by field-line curvature scattering, EMIC-driven precipitation, and microbursts. Curvature scattering (Imhof et al., 1977; Sergeev et al., 1983; Büchner & Zelenyi, 1989) of plasma sheet and radiation belt electrons can be identified by its sharp energy/latitude dispersion (isotropy boundary) that results in high precipitating-to-trapped flux ratio at relativistic energies closer to the planet (see the IB precipitating pattern in Fig. 1b and statistical results in Wilkins et al. (2023)). Such data, in addition to the isotropic precipitation with  $j_{prec}/j_{trap} \sim 1$  of  $< 300$  keV electrons poleward from the isotropy boundary (Artemyev et al., 2022), are removed from our statistics. Next, electromagnetic ion cyclotron (EMIC) waves, which are caused by nightside ion injections (Jun et al., 2019; Kim et al., 2021) and efficiently scatter and precipitate relativistic electrons (e.g., Blum, Halford, et al., 2015; Blum, Li, & Denton, 2015; Yahnin et al., 2016, 2017; Capannolo et al., 2019, 2023), are excluded. These EMIC-driven observations are identified by precipitating-to-trapped ratios that reach their peak at  $\geq 500$  keV energy (see examples in X. An et al., 2022; Grach et al., 2022; Capannolo et al., 2023; Angelopoulos et al., 2023). Additionally, whistler-mode hiss waves provide a wide energy range of scattering, from weak scattering further from the plasmasphere to precipitation of relativistic electrons within the plasmasphere (see discussion of ELFIN observations of such precipitation in Mourenas et al., 2021; Angelopoulos et al., 2023; X.-C. Shen et al., 2023); these hiss precipitation events are also eliminated. Figure 1e shows this particular pattern, which is recognizable by a low  $j_{prec}/j_{trap}$  ratio peaking at  $\geq 500$  keV energy at low  $L$ -shells. Finally, we exclude all precipitation patterns showing microburst-like flux variation within one spin (such events are characterized by precipitating-to-trapped flux ratio exceeding one for relativistic electron energies, see X.-J. Zhang et al., 2022, for further examples).

All these effects are programmatically eliminated from statistics leaving us with only one type of precipitating energy distribution: a precipitating-to-trapped ratio monotonically decreasing with energy, observed primarily within  $L$ -shells  $\in [4, 8]$ , corresponding to the outer radiation belt outside the plasmasphere (e.g., Mourenas et al., 2021). This type of precipitation can only be caused by whistler-mode waves (see more details and examples in Tsai et al., 2022; X.-J. Zhang et al., 2022, 2023), and is demonstrated in Figure 1(b,e).

We combine all ELFIN observations from the nightside MLT sector (27950 spins across 4458 radiation belt crossings) and plot the averaged precipitating-to-trapped flux spectra for three geomagnetic activity levels and two  $L$ -shell domains (4.5–5.5 and 5.5–7.5) for  $AE \in [100, 300]$  nT in Fig. 2d. Fig. 2(a-c) show that the precipitating-to-trapped electron flux ratio  $j_{prec}/j_{trap}$  above 100 keV increases significantly as  $AE$  increases. The precipitating-to-trapped flux ratio reaches  $j_{prec}/j_{trap} \sim 0.1$  up to 200–400 keV when  $AE > 300$  nT. This result is consistent with past observations of stronger energetic electron injections from the plasma sheet during periods of higher  $AE$  (Tao et al., 2011; Runov et al., 2015; Gabrielse et al., 2014), leading to even more intense whistler-mode waves (Meredith et al., 2001; X. J. Zhang et al., 2018) which can efficiently precipitate 50–500 keV electrons (Summers et al., 2004; Thorne et al., 2005; Aryan et al., 2020; Agapitov et al., 2018). The ratio  $j_{prec}/j_{trap}$  is also higher at  $L = 5.5–7.5$  than at  $L = 4.5–5.5$  in Fig. 2, in agreement with the higher chorus wave power at higher  $L > 5.0–5.5$  in the night sector in spacecraft statistics (Agapitov et al., 2018; Meredith et al., 2020). The smooth decrease of  $j_{prec}/j_{trap}$  as electron energy increases in Fig. 2d is consistent with the expectation that at higher latitudes, wave power decreases while minimum cy-



**Figure 1.** Two examples of ELFIN observations with strong precipitation of energetic electrons in the nightside MLT sector showing locally trapped electron fluxes (a,d), precipitating-to-trapped flux ratio (b,e), and ELFIN’s MLT,  $L$ -shell coordinates from (Tsyganenko, 1989) model (c,f).

clotron resonance energy increases, therefore precipitating higher energy electrons at lower absolute flux levels (Agapitov et al., 2018; Meredith et al., 2020).

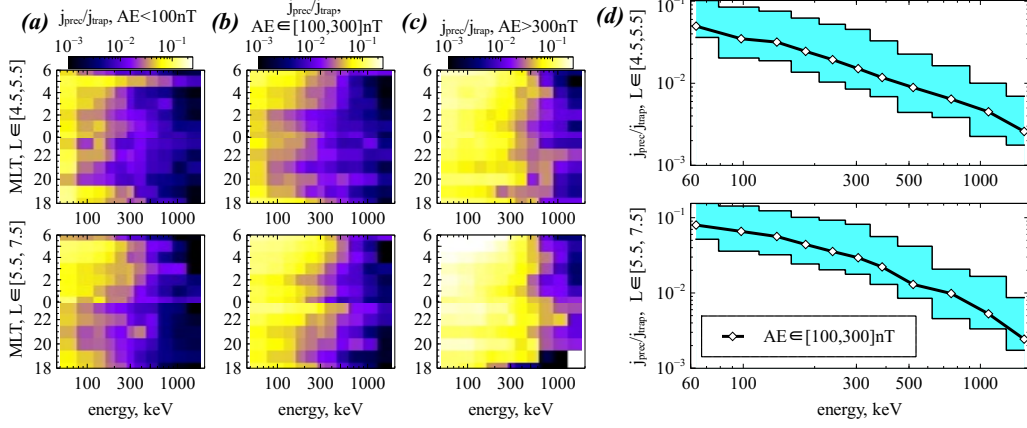
### 3 Simulation

Calculating the precipitating-to-trapped flux ratios is useful because it eliminates the trapped flux variability (which can vary by orders of magnitude). The slope of the ratio’s energy spectra now represents only the relative effects of resonant interactions with whistler-mode waves. To then compare with ELFIN statistics, we obtain modeled precipitating-to-trapped flux ratios using two different types of simulations: (1) a configurable large-ensemble test particle simulation for electron resonant interactions, as used in previous work (Tsai et al., 2022, 2023) and (2) a quasi-linear diffusion code which has been used in previous radiation belt simulations (Ma et al., 2012, 2015). The test particle simulations include potential non-linear resonant effects and consider only purely monochromatic waves, whereas the quasi-linear diffusion code models electron scattering by an ensemble of oblique waves with higher order resonant interactions across a distribution of frequencies. Thus, by comparing results obtained by these two approaches, we can fully capture the importance of different resonant effects for electron scattering and losses.

#### 3.1 Test particle simulation

Our test particle simulation (Tsai et al., 2022, 2023) is designed to compute the expected energy distribution of the electron precipitation flux ratio given realistic wave parameters. In order to obtain enough statistics – especially at higher energies where it is less likely for electrons to be scattered into the loss cone – we use a large number of particles for all test particle simulations in this study with  $N = 5 \times 10^6$ . For this to run in a reasonable amount of time, we parallelize the code and implement it in Julia 1.9.3 (Bezanson et al., 2017) using the differential equations package (Rackauckas & Nie, 2017). The Hamiltonian formulation for wave-particle resonant interactions (Albert et al., 2013; Vainchtein et al., 2018) incorporates nonlinear effects such as phase bunch-





**Figure 2.** Plots (a-c) show the statistical distributions of precipitating-to-trapped electron spectra in (MLT, energy) space for several levels of geomagnetic activity. Plots (d) show energy profiles of precipitating-to-trapped fluxes for three geomagnetic activity levels in the nightside MLT  $\in [18, 4]$ . The shaded blue range regions represent the upper ( $AE > 300$  nT) and lower ( $AE < 100$  nT) bounds of geomagnetic activity levels while the central black curve depicts  $AE \in [100, 300]$  nT.

ing, phase trapping, and anomalous trapping (Demekhov et al., 2006; Bortnik et al., 2008; Katoh et al., 2008; Omura et al., 2007; Kitahara & Katoh, 2019; Albert et al., 2021). The simulation uses monochromatic waves, which is generally valid for describing diffusive scattering in a background dipolar magnetic field due to its strong magnetic field gradient (Albert, 2001, 2010; Shklyar, 2021). Critically, the wave field is modified by the function  $B_w(\lambda, L, \text{MLT}, K_p)$  which describes the wave amplitude variation along magnetic field lines using an empirical chorus wave model built using 14 years of Cluster and Van Allen Probe statistics. The wave model is dependent on latitude, geographic location, and geomagnetic activity (see model and coefficients in Agapitov et al., 2018), which is necessary for realistic modeling of energetic electron losses. Further details of the test particle simulation implementation can be found in Tsai et al. (2022, 2023).

In this study, we have further augmented the test particle simulation to explore the latitudinal dependence of wave frequency and obliquity so that wave frequency  $\omega(\lambda, \theta)$  is a function of both latitude and wave normal angle. Changing into dimensionless variables allows us to provide a mean normalized wave frequency  $\omega_m(\lambda) = \omega(\lambda)/\Omega_{ce,eq}$  and mean wave normal angle  $\theta(\lambda)$  both as functions of magnetic latitude  $\lambda$  (as described in Section 3.3). With dimensionless variables, the normalized plasma frequency is defined as  $\Omega_{pe} = \omega_{pe,eq}/\Omega_{ce,eq}$ .

### 3.2 Quasi-linear diffusion code

To instill further confidence in test particle simulation results, we calculate the quasi-linear diffusion coefficients using the Full Diffusion Code (Ni et al., 2008, 2011; Shprits & Ni, 2009; Ma et al., 2018) and model the precipitating electron flux using the Fokker-Planck diffusion code (Ma et al., 2012, 2015). This quasi-linear diffusion code physically differs from the test particle simulations primarily in the fact that it prescribes Gaussian distributions for the wave frequency (Glauert & Horne, 2005):

$$\hat{B}^2(\omega) \sim \exp \left[ -\frac{(\omega - \omega_m(\lambda))^2}{\delta\omega^2} \right]$$

and the wave normal angle:

$$g(\theta) \sim \exp \left[ -\frac{(\tan \theta - \tan \theta_m(\lambda))^2}{(\tan \delta\theta)^2} \right]$$

where mean values  $\omega_m$  and  $\theta_m$  with bandwidths  $\delta\omega$  and  $\delta\theta$  represent wave frequency and normal angle, respectively. These distributions are provided relative to mean values,  $\omega_m(\lambda)$  and  $\theta_m(\lambda)$ , which are given as functions of magnetic latitude  $\lambda$  and discussed in the next section (see details in Artemyev et al., 2013; Agapitov et al., 2018; Aryan et al., 2020).

We use the bounce-averaged Fokker-Planck equation to model the electron precipitation rate (Lyons et al., 1972; Glauert & Horne, 2005):

$$\frac{\partial f}{\partial t} = \frac{1}{\tau_b(\alpha_{eq}) \sin 2\alpha_{eq}} \frac{\partial}{\partial \alpha_{eq}} \left( \tau_b(\alpha_{eq}) \sin 2\alpha_{eq} \left( \langle D_{\alpha\alpha} \rangle \frac{\partial f}{\partial \alpha_{eq}} \right) \right) - \frac{f}{\tau_{loss}} \quad (1)$$

where  $\alpha_{eq}$  is the equatorial pitch angle,  $\tau_b \approx 1.38 - 0.32 (\sin \alpha_{eq} + \sin^2 \alpha_{eq})$  (see Orlova & Shprits, 2011),  $\langle D_{\alpha\alpha} \rangle$  is the bounce-averaged diffusion rate, and  $\tau_{loss}(t)$  is the bounce loss time (and is set to be a quarter of the bounce period inside the local loss-cone and infinity outside the loss cone). We use the quasi-linear diffusion code to numerically solve Eq. (1), with diffusion rates derived from  $\hat{B}^2(\omega)$  and  $g(\theta)$  distributions (see Ni et al., 2008, 2011; Ma et al., 2015, 2018). Zero-gradient boundary conditions in pitch angle are set to simulate the loss cone filling of electrons due to wave scattering (Ma et al., 2022).

### 3.3 Frequency and Obliquity Models

In both simulations, we use the following two models to compare the effects of whistler wave frequency (normalized to the equatorial gyrofrequency)  $\omega_m = \omega/\Omega_{ce,eq}$ :

**Model 1:** normalized wave frequency held constant at  $\omega_m = 0.35$ , the typical frequency of whistler mode chorus waves near the equator (Agapitov et al., 2018).

**Model 2:** function  $\omega(\lambda)$  linearly decreasing from  $0.41\Omega_{ce,eq}$  at the equator until reaching a constant  $0.16\Omega_{ce,eq}$  for  $\lambda \geq 20^\circ$ . This model is based on statistics of off-equatorial parallel and oblique lower-band chorus waves from the Van Allen Probes (Agapitov et al., 2018).

We use the following four models to describe the mean wave normal angle (WNA)  $\theta_m$ . A scaling factor  $\Theta(\lambda) = \lambda/(15^\circ + \lambda)$  is adopted to modify the WNA increase from 0 at the equator to  $\Theta(45^\circ) = 0.75$  at  $45^\circ$  latitude in WNA1 and WNA2.

**FAW:** a field-aligned wave model (with  $\theta = 0^\circ$  in test particle simulations and  $\theta_m = 0^\circ$ ,  $\delta\theta = 30^\circ$  or  $\delta\theta = 5^\circ$  in the quasi-linear diffusion code) that describes the most intense population of waves (Li, Santolik, et al., 2016; Agapitov et al., 2013) as they remain field-aligned off equator due to wave ducting by small-scale density structures (Hanzelka & Santolik, 2019; Y. Shen et al., 2021; Ke et al., 2021; Hosseini et al., 2021).

**WNA1:** a moderately oblique WNA model with  $\theta_1(\lambda) = \theta_G(\lambda) \cdot \Theta(\lambda)$ , where  $\theta_G = \arccos(2\omega/\Omega_{ce})$  is the Gendrin angle (Gendrin, 1961). This model describes field-aligned waves that are generated at the equator, but become mildly oblique as they propagate through the inhomogeneous plasma (e.g. Breuillard et al., 2012; L. Chen et al., 2013; Ke et al., 2017).

**WNA2:** a very oblique WNA model with  $\theta_2(\lambda) = \theta_r(\lambda) \cdot \Theta(\lambda)$ , where  $\theta_r = \arccos(\omega/\Omega_{ce})$  is the resonance cone angle. This describes field-aligned waves that are generated at the equator, but become very oblique as they propagate through the inhomogeneous plasma in the case of suppressed Landau damping (see discussion in Artemyev & Mourenas, 2020).



**WNA3:** an extremely oblique WNA model with  $\theta_3(\lambda) = \theta_r(\lambda) - 2^\circ$ . This model describes very oblique waves that are generated in the equatorial source region in the presence of field-aligned electron streams suppressing Landau damping (Mourenas et al., 2015; Li, Mourenas, et al., 2016; R. Chen et al., 2019; Kong et al., 2021).

The quasi-linear simulations also require a bandwidth parameter which sets the width of the wave frequency and normal angle Gaussian distributions, defined in Section 3.2. Frequency bandwidth  $\delta\omega$  is set to 0.125, and the lower and upper cutoff frequencies are set to be  $\omega_m - 2\delta\omega$  and 0.5, respectively. Wave normal angle bandwidth is set to either  $\delta\theta = 5^\circ$  or  $\delta\theta = 30^\circ$  for FAW, and  $\delta\theta = 10^\circ$  for the other models; if  $\theta_r(\lambda) - \theta_m(\lambda) < 20^\circ$ , we set  $\delta\theta = (\theta_r(\lambda) - \theta_m(\lambda))/2$ . The lower ( $\theta_{LC}$ ) and upper ( $\theta_{UC}$ ) cutoff wave normal angles are set as  $\tan \theta_{LC} = \max(0, \tan \theta_m - 2 \tan \delta\theta)$  and  $\tan \theta_{UC} = \min(\tan 89.9^\circ, \tan \theta_m + 2 \tan \delta\theta)$ , respectively.

Finally, the magnetic wave power distribution  $B_w^2(\lambda)$  is taken from an empirical statistical model (Agapitov et al., 2018) at 23 MLT and  $L = 6$  for  $Kp = 3$ . Note that we use  $Kp = 3$  as a reasonable estimate of average geomagnetic activity level for ELFIN observations of electron precipitation driven by resonance with whistler-mode waves (see Tsai et al., 2023, for further discussion). For quiet conditions  $Kp \leq 2$ , the wave intensity provides insufficient levels of precipitating electron fluxes, which is generally corroborated by the extremely low levels (i.e. near background) of precipitating fluxes ELFIN observes during quiet periods. During disturbed storm times ( $Kp > 4$ ), the precipitating and locally trapped fluxes are occasionally too large and approach saturation of ELFIN's EPDE instrument (see details in X.-J. Zhang et al., 2022). Both types of ELFIN observations (either background-level precipitation or nearly-saturated measurements) are excluded from the statistical analysis.

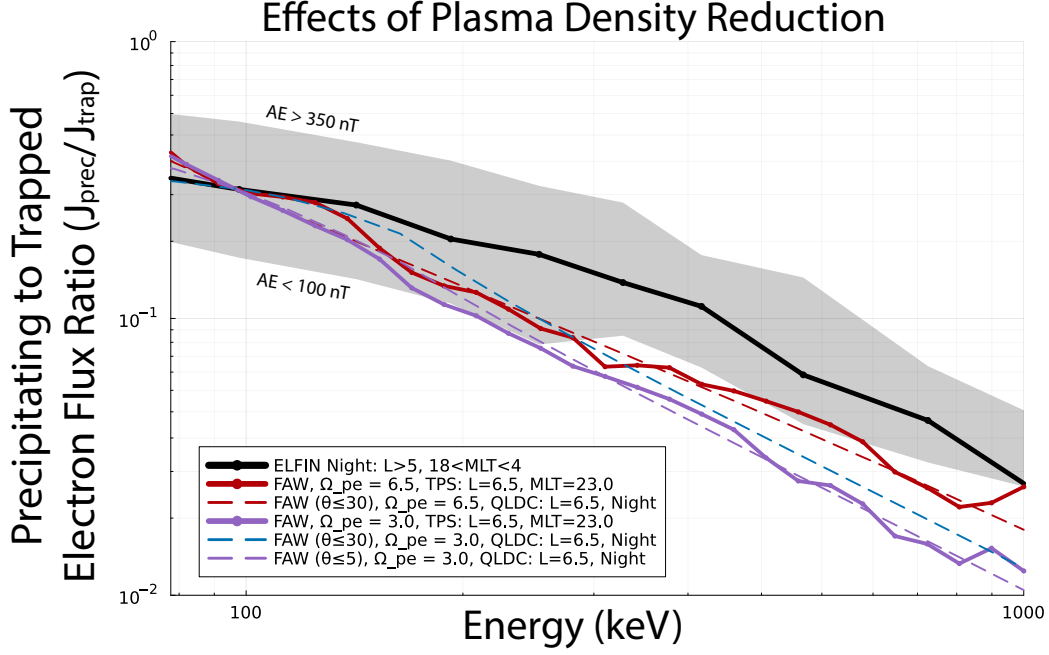
## 4 Data-model comparison

In this section, the precipitating-to-trapped electron flux ratio  $j_{prec}/j_{trap}$ , calculated through test particle simulations (TPS) or Quasi-Linear Diffusion Code (QLDC), are compared with  $j_{prec}/j_{trap}$  as measured by ELFIN. This allows us to assess the different roles potentially played by plasma density, wave obliquity, and wave frequency based on precipitating flux ratio variation with energy.

For proper comparison, the simulated  $j_{prec}/j_{trap}$  flux ratio is normalized to the observed  $j_{prec}/j_{trap}$  flux ratio at ELFIN's second energy bin ( $\sim 97$  keV), thereby removing wave amplitude variability such that the spectral slope can be compared for across various scenarios. This is valid because the  $\sim 30 - 100$  keV precipitating-to-trapped electron flux ratio correlates well with the equatorial wave amplitude (Li et al., 2013; Ni et al., 2014). In addition, spurious variations in  $j_{prec}/j_{trap}$  modeled using our test particle simulations tend to become larger below 97 keV, despite the large number of particle runs per energy bin. These oscillations are absent from results of the quasi-linear diffusion code, which correlate well with test particle simulation results above 97 keV after normalization.

### 4.1 Role of plasma density

Figure 3 shows a comparison between the precipitating-to-trapped electron flux ratio  $j_{prec}/j_{trap}$  measured by ELFIN at  $L > 5$  and 18-4 MLT (black) with  $j_{prec}/j_{trap}$  obtained from TPS (solid red) and QLDC (dashed red) with parallel (FAW model) lower-band chorus waves (adopting  $\theta = 0^\circ$  in test particle simulations,  $\delta\theta = 30^\circ$  in the quasi-linear diffusion code), using wave frequency Model 1 of constant frequency ( $\omega_m = 0.35$ ) chorus waves and a typical plasma frequency to gyrofrequency ratio  $\Omega_{pe} = 6.5$  at  $L = 6.5$  and 23 MLT (Sheeley et al., 2001). In this plot (and remaining Figures 3-7), the gray shaded regions of ELFIN data denote the boundaries of quiet (AE < 100 nT) and ac-



**Figure 3.** ELFIN-measured precipitating-to-trapped electron flux ratio at  $L > 5$  on the night-side (18 – 4 MLT) as a function of energy (black curve). The corresponding  $j_{prec}/j_{trap}$  flux ratio obtained from test particle simulations is shown for parallel (FAW model,  $\theta = 0^\circ$ ) lower-band chorus waves, using frequency Model 1 ( $\omega_m = \text{constant}$ ) and a typical  $\Omega_{pe} = 6.5$  at  $L = 6.5$  and 23 MLT (solid red). Results from the quasi-linear diffusion code using the same parameters is shown in dashed red. Similarly, the cases of reduced density  $\Omega_{pe} = 3$  modeled with test particle simulation (solid purple), quasi-linear diffusion code using narrow-band field aligned waves ( $\delta\theta = 5^\circ$ , dashed purple), and more quasi-linear field aligned waves ( $\delta\theta = 30^\circ$ , dashed blue), are shown. All simulation results are normalized to observations at 97 keV.

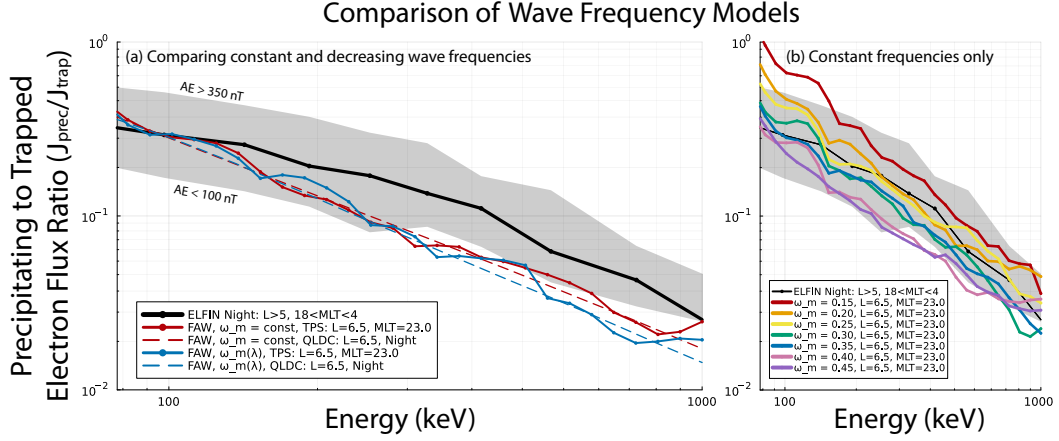
tive ( $AE > 350$  nT) times. The normalized ratios  $j_{prec}/j_{trap}$  obtained from TPS and QLDC are quite similar (compare solid with dashed lines of the same color), validating the reliability of the quasi-linear approach (Kennel & Engelmann, 1966; Lyons et al., 1972; Albert, 2005; Glauert & Horne, 2005; Mourenas et al., 2012; Mourenas, Artemyev, Agapitov, & Krasnoselskikh, 2014), especially in the case of field aligned waves, as demonstrated in previous studies (Tao et al., 2012; Mourenas, Artemyev, et al., 2022; Gan et al., 2022; Z. An et al., 2022). However, despite their normalization to the measured  $j_{prec}/j_{trap}$  at 97 keV, these similar ratios of  $j_{prec}/j_{trap}$  (red curves) obtained from test particle simulations and from the quasi-linear diffusion code become  $\sim 1.5 - 2$  times smaller than the measured  $j_{prec}/j_{trap}$  at 200–1000 keV (black), corresponding to a deficiency of pitch-angle diffusion occurring at higher energies. For reference, this baseline case (red) represents the same discrepancy on the nightside as first described in Tsai et al. (2023).

A reduced plasma density should lower the latitude of first-order cyclotron resonance with chorus waves for electrons near the loss-cone (Mourenas et al., 2012). Since chorus wave power  $B_w^2$  is higher at lower latitudes (Agapitov et al., 2018), a reduced density is therefore expected to yield higher electron pitch-angle diffusion rate  $D_{\alpha\alpha} \propto B_w^2$  near the loss-cone leading to higher precipitation rates and fluxes at all energies. However, adopting a reduced plasma density ( $\Omega_{pe} = 3$ ) in test particle simulations (purple line in Fig. 3) and normalizing the flux ratio at 97 keV leads to an even larger discrepancy across the 300 – 1000 keV range with a  $\sim 2 - 3$  times smaller  $j_{prec}/j_{trap}$  ratio than ELFIN statistics show. We therefore interpret this density effect as more important at lower energies ( $\sim 100$  keV) compared to higher energies ( $> 300$  keV) due to  $B_w^2(\lambda)$  increasing, in our model and in observations, more steeply towards lower latitudes at  $\lambda \lesssim 25^\circ$  (where resonance with  $\sim 100$  keV electrons occurs) than at  $\lambda > 25^\circ$  (where resonance with  $\sim 1$  MeV electrons occurs) during disturbed periods at 21-3 MLT (Agapitov et al., 2018). Therefore, the wave power  $B_w^2(\lambda)$  seen by electrons near the loss-cone increases only marginally at higher energies for both  $\theta = 0^\circ$  in test-particle simulations and  $\theta < 5^\circ$  or  $\theta < 30^\circ$  in QLDC simulations (solid/dashed purple and dashed blue lines). This then reduces the normalized pitch-angle diffusion rate  $D_{\alpha\alpha}$  near the loss-cone and the normalized  $j_{prec}/j_{trap}$  flux ratio, which varies roughly like  $\approx \sqrt{D_{\alpha\alpha}}$  (Kennel & Petschek, 1966; Li et al., 2013; Mourenas, Zhang, et al., 2022; Mourenas et al., 2023).

Adopting a more realistic spread of WNAs for quasi-field aligned waves ( $\delta\theta = 30^\circ$ , blue dashed line) in the quasi-linear diffusion code leads to the effects of additional, higher-order cyclotron resonances to become more significant (Artemyev et al., 2016), which is clearly shown as the difference between the blue and purple dashed lines in Figure 3. Due to moderate obliqueness, this effect is most prominent in the lower energies – resonating with waves around the equator – extending now to about 180 keV. However, it is not enough to reproduce ELFIN observations up to 1 MeV, because the relative scattering efficiency decreases with the purple curve at higher energies, causing the blue curve to underestimate ELFIN statistics beyond  $> 250$  keV. Despite the fact that, in observations, the plasma frequency to gyrofrequency ratio  $\Omega_{pe}$  does decrease at 18-4 MLT during disturbed periods (O’Brien & Moldwin, 2003), often down to  $\Omega_{pe} \approx 3 - 4$  at  $L \sim 6$  when  $AE > 150$  nT (Agapitov et al., 2019), results in Figure 3 show that plasma density reduction alone cannot account for a relative increase of electron scattering at higher energies.

## 4.2 Role of wave frequency

As noted earlier, statistical observations of lower-band chorus waves show that their normalized frequency is not constant as a function of latitude (as assumed in frequency Model 1), but rather, decreasing due to preferential Landau damping affecting higher frequencies at higher latitudes (Agapitov et al., 2018; Bunch et al., 2013; L. Chen et al., 2013), as reflected by frequency Model 2. Figure 4a shows that the  $j_{prec}/j_{trap}$  ratios obtained for wave normal angle model FAW from test particle simulations (solid curves)



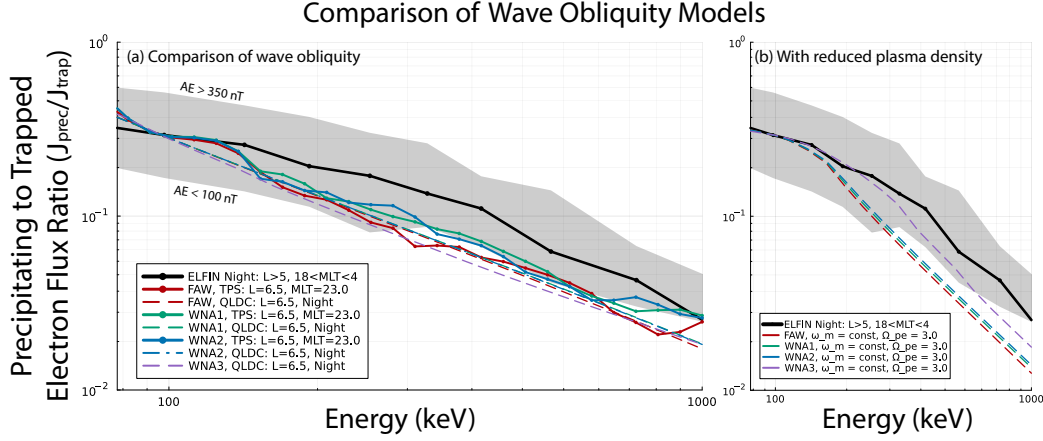
**Figure 4.** To compare the effects of two frequency models, precipitating-to-trapped electron flux ratio  $j_{prec}/j_{trap}$  plotted for ELFIN statistics on the nightside (black) is shown in comparison with  $j_{prec}/j_{trap}$  ratios obtained from test particle simulations (TPS, solid lines) and quasi-linear diffusion code (QLDC, dashed lines). In (a), Frequency Model 2 (frequency decreasing toward higher latitudes, blue) produces slightly higher precipitation rates at 100 keV relative to 1 MeV as compared to a constant  $\omega_m = 0.35$  (red). Plot (b) shows results from a variety of normalized wave frequency values that do not vary as a function of magnetic latitude, demonstrating that absolute frequency has little effect on the slope of the precipitation energy spectra.

and from the quasi-linear diffusion code (dashed curves) are both slightly decreased at  $E = 200 - 1000$  keV when wave frequency Model 2 is used (blue curves), rather than when using Model 1. This is because a reduction of wave frequency alone, when adopting a fixed plasma density  $\Omega_{pe} = 6.5$  at  $L = 6.5$ , has essentially the same effect as decreasing plasma density in Section 4.1 – albeit weaker in magnitude – by allowing first-order cyclotron resonance for electrons near the loss-cone to occur at lower latitudes (Mourenas et al., 2012). In turn, this preferentially increases precipitation rates at low energies  $E \lesssim 100$  keV, the typical resonance energies at low-latitude plasma conditions.

Figure 4b shows that decreasing the wave frequency by a fixed amount significantly increases electron precipitation rates by lowering the latitude of resonance with chorus waves. But at the same time, it leads to only a slight increase of the slope of the energy spectrum once normalized to ELFIN statistics, because the amplitude of resonant waves is slightly more increased for 100 keV electrons than for 1 MeV electrons. For a large plasma density,  $\Omega_{pe} = 6.5$ , this effect on the normalized  $j_{prec}/j_{trap}$  remains weak, and both wave frequency Model 1 and 2 end up giving very similar results. Therefore, the effects of frequency variation with latitude alone cannot account for the spectral shape of the precipitation ratio in ELFIN’s nightside observations.

### 4.3 Role of wave obliquity

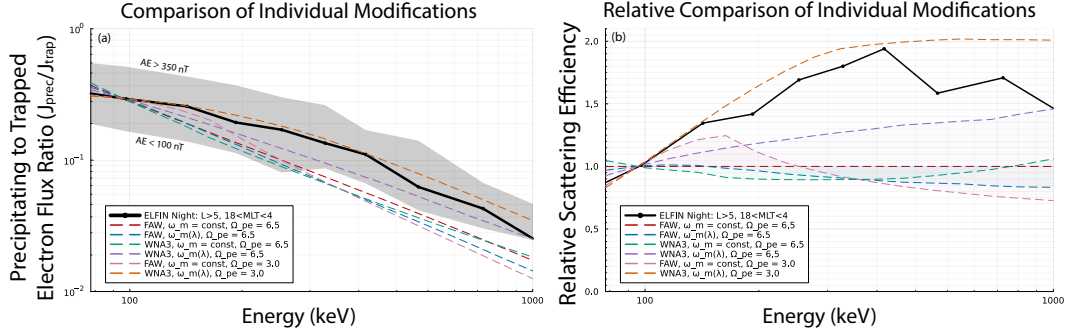
Figure 5a compares ELFIN-observed precipitating-to-trapped flux ratio on the nightside (black) with that of simulations in order to explore the effects of a variety of wave-normal angle distributions paired with constant wave frequency (Model 1) and baseline plasma density (Sheeley et al., 2001). Results from test particle simulations (solid curves) and from the quasi-linear diffusion code (dashed curves) are displayed for four different models of wave normal angle: FAW (red), WNA1 (green), WNA2 (blue), and WNA3 (purple), corresponding to a progressively larger amount of wave power in oblique waves closer to the resonance cone angle (see Section 3.3). Despite the large number of particles ( $N =$



**Figure 5.** ELFIN-observed  $j_{prec}/j_{trap}$  flux ratio at  $L > 5$  on the nightside (18 – 4 MLT) as a function of electron energy (black). The corresponding ratios  $j_{prec}/j_{trap}$  obtained from test particle simulations (TPS, solid curves) and from the quasi-linear diffusion code (QLDC, dashed curves) are displayed for lower-band chorus waves in (a), using frequency Model 1 of constant frequency, and parameterized by four wave normal angle models: FAW (red), WNA1 (green), WNA2 (blue), and WNA3 (purple), with a normalization to observations at 97 keV, adopting a typical  $\Omega_{pe} = 6.5$  at  $L = 6.5$  and 23 MLT. (b) shows QLDC results for the same four wave normal angle models but for a reduced plasma density of  $\Omega_{pe} = 3.0$ .

$5 \times 10^6$ ), unnatural oscillations in the test particle simulations make it difficult to quantify the exact contribution differences among the FAW, WNA1, and WNA2 models. Especially because the test particle simulation only includes first-order oblique wave interactions, it is reasonable to conclude that including wave obliquity in the TPS does not significantly alter precipitation efficiency. However, results from the quasi-linear diffusion code generally agree with test particle simulation results, indicating the reliability of the quasi-linear approach (described, e.g., by Kennel & Engelmann, 1966; Lyons et al., 1972; Albert, 2005; Glauert & Horne, 2005; Mourenas et al., 2012; Mourenas, Artemyev, Agapitov, & Krasnoselskikh, 2014). Our quasi-linear simulations show that wave obliquity is ineffective at increasing high energy electron precipitation compared to low energy electron precipitation (in the case of  $\Omega_{pe} = 6.5$ ). Note that WNA1 and WNA2 models correspond to wave-normal angle distributions that extend up to three-quarters of the Gendrin angle and resonance cone angle, respectively, at  $\lambda > 45^\circ$ , while the WNA3 model corresponds to highly oblique waves, at about  $2^\circ$  from the resonance cone angle. Yet the results are nearly identical (dashed blue, dashed green, and dashed purple curves).

Oblique chorus waves can resonate with electrons via high-order cyclotron resonances ( $n \geq 1$  or  $n \leq -2$ , e.g., Shklyar & Matsumoto, 2009; Mourenas et al., 2012; Artemyev et al., 2013, 2016; Albert, 2017), which can significantly increase diffusion rates at high energy (Lorentzen et al., 2001; Gan et al., 2023). However, diffusion rates near the loss cone due to higher-order cyclotron resonances rapidly decrease in magnitude as  $|n|$  increases, especially from  $|n| = 1$  to  $|n| = 2$  (Shprits & Ni, 2009), although this reduction is weaker for highly oblique waves (Artemyev et al., 2016). To increase the ratio of 1 MeV to 100 keV pitch-angle diffusion rates near the loss cone, therefore, the waves must be sufficiently oblique and/or plasma density and wave frequency should be sufficiently low to enable only first-order resonance at  $\sim 100$  keV, but higher-order resonances at 1 MeV (Artemyev et al., 2016; Mourenas & Ripoll, 2012; Shprits & Ni, 2009; Gan et al., 2023). Figure 5b indeed shows that when plasma density is reduced to  $\Omega_{pe} = 3$  (or equiv-



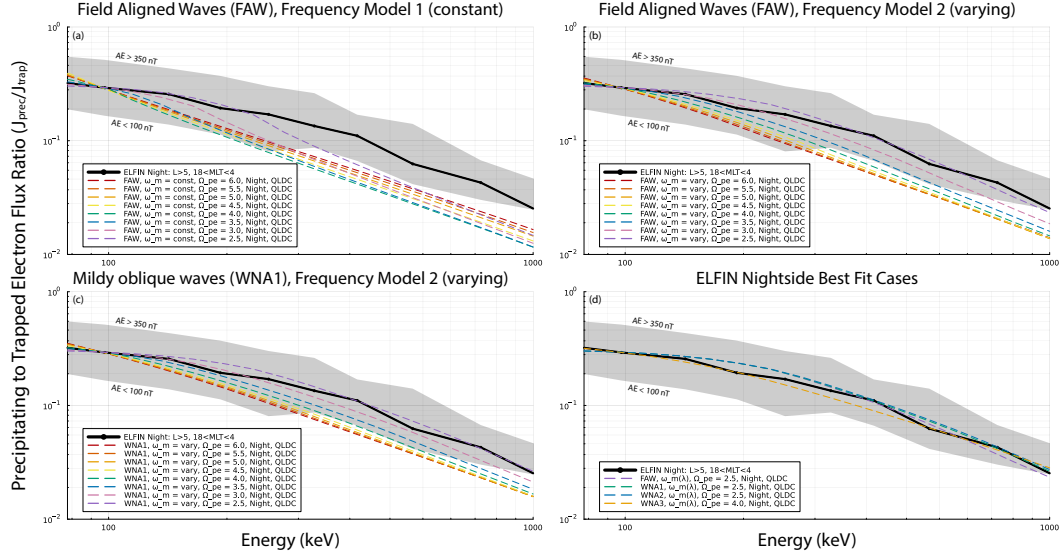
**Figure 6.** ELFIN-observed nightside ( $18 - 4$  MLT)  $j_{prec}/j_{trap}$  electron flux ratio shown as a function of energy (black). (a) shows  $j_{prec}/j_{trap}$  flux ratios obtained from quasi-linear diffusion code (QLDC) for parallel (FAW) lower-band chorus waves (red), very oblique waves using wave normal angle model WNA3 (green), waves with a realistic wave frequency distribution (blue), WNA3 with a realistic wave frequency distribution (purple), FAW with reduced density (pink), and everything combined (orange). (b) shows the same flux ratios all normalized to the base case with no modifications (red) demonstrating which energy range each modification is most effective at on a linear scale. This shows that each effect examined alone cannot reproduce results from ELFIN individually.

alently, when wave frequency decreases with latitude, see Section 4.4), electron precipitation is greatly increased at 1 MeV relative to 100 keV as wave obliquity increases, especially in the case of highly oblique waves (WNA3). These results therefore suggest that wave obliquity, alone, has a near-negligible effect on the high-energy to low-energy electron loss ratio; however, when combined with a density reduction, it can significantly enhance energetic electron losses.

#### 4.4 Combined results

Figure 6a shows comparisons between the precipitating-to-trapped electron flux ratio  $j_{prec}/j_{trap}$  measured by ELFIN at  $L > 5$  on the nightside (black), overlaid with  $j_{prec}/j_{trap}$  obtained from the quasi-linear diffusion code for the three modifications in question – reduced plasma density  $\Omega_{pe} = 3$ , Frequency Model 2, and WNA3 – alone or in combination. As surmised in previous sections, each individual modification fails to agree with the observed spectrum. With wave frequency Model 2 (blue) and WNA3 (green) underestimating across entire energy range (i.e., increasing precipitation at 100 keV) and reduced density (pink) providing a relative efficiency bump of  $j_{prec}/j_{trap}$  only at  $E < 200$  keV. Interestingly, however, ELFIN’s statistical observations are only slightly underestimated when combining WNA3 and Frequency Model 2 (purple), and best matched when all three modifications are combined (orange). Figure 6b shows the relative difference produced by each modification compared to the baseline red curve. We see that these effects synergistically enhance  $j_{prec}/j_{trap}$  flux ratios at higher energies. For example, Model 2 (blue) becomes relatively less effective at higher energy, while WNA3 (green) immediately loses effectiveness, but catches back up closer to 1 MeV. However, when combined (purple), the relative precipitation is drastically enhanced in the entire 200–1000 keV range, leading to far better agreement with observations. Further combining WNA3 and Frequency Model 2 with a reduced plasma density (orange) significantly enhances precipitation past levels observed by ELFIN (black). This is likely due to two phenomena: first, the combined effects of a reduced plasma density and a decreasing wave frequency decrease the latitude at which cyclotron resonance with quasi-parallel waves oc-





**Figure 7.** The comparison between observed electron precipitation ratios and simulation results using different wave frequency models,  $\Omega_{pe}$  ratios, and wave normal angle models. In each plot, the black line denotes statistical averages of  $j_{prec}/j_{trap}$  flux ratios for nightside ELFEN observations with  $L > 5$ . Plots (a-c) show QLDC results with various modifications parameterized by  $\Omega_{pe}$ : (a) shows field aligned waves with Frequency Model 1; (b) shows field aligned waves with Frequency Model 2; and (c) shows WNA1 combined with Frequency Model 2. (d) shows that all three effects –  $\omega_{pe} \in [2.5, 4]$ , combined with Frequency Model 2 and some level of wave obliquity – are necessary for recreating ELFEN nightside statistics.

curs far more significantly than each effect alone (Mourenas et al., 2012), leading to a larger increase of resonant wave power for higher energy electrons that best match ELFEN’s observed precipitation spectra; second, the supplementary higher-order cyclotron resonances contributing at  $\sim 1$  MeV, but not at  $\sim 150$  keV, are of lower order ( $|n| = 2$ ) than for higher density or frequency, allowing for a more dramatic increase of the 1 MeV to 150 keV pitch-angle diffusion rate ratio (Artemyev et al., 2016; Mourenas & Ripoll, 2012; Shprits & Ni, 2009; Gan et al., 2023).

Figure 7 summarizes the findings from each wave parameter combination throughout a range of reduced equatorial plasma densities for a better understanding of the interplay between the three effects considered. Figure 7a shows that only below a certain threshold of  $\Omega_{pe} \lesssim 4$  does the interaction of higher-order resonances start to increase precipitation at higher energies. Using the total electron density with  $\Omega_{pe} = 2.5$ , this effect becomes very pronounced above 100 keV and up to 300 keV, whereas above that energy this effect alone is still incapable of matching observations, as discussed in Section 4.1. The effect of plasma density combined with wave frequency becomes significantly more pronounced throughout the whole energy range when  $\Omega_{pe} \lesssim 4$ , as shown in Figure 7b, and matches very well with ELFEN’s nightside observations when a more extreme  $\Omega_{pe} = 2.5$  is used. Adding mild wave obliquity (Figure 7c) results in the best match with ELFEN statistics, demonstrating that all three effects combined are necessary.

Figure 7d shows the best fit scenarios for forward-modeling ELFEN-observed precipitating-to-trapped flux ratios, which all require the varying frequency model in addition to reduced plasma density to various degrees. Here, we show that it is possible to obtain decent agreement without the need for wave obliquity by significantly reducing  $\Omega_{pe}$  to 2.5

(purple). By adding moderately oblique waves (green and blue), more  $\sim 1$  MeV electrons are precipitated, doing a marginally better job of matching observations. Using extremely oblique waves (WNA3) – which describes a population of very oblique waves generated around the equator when the Landau damping is largely reduced by field-aligned electron streams (Mourenas et al., 2015; Li, Mourenas, et al., 2016) – requires increasing plasma density  $\Omega_{pe} = 4$  in order to avoid significant overestimation. Therefore, ELFIN observations of nightside electron precipitation spectra (from 50–1000 keV) can be described either under the assumption of a significant plasma density reduction or a more moderate plasma density reduction coupled with a strongly oblique wave population. This required plasma density ( $\omega_{pe} \in [2.5, 4]$ ) is fully consistent with the average measured  $\omega_{pe}$  levels at 18–4 MLT and  $L = 5–6.5$  in Van Allen Probes statistics during disturbed periods with  $AE \in [150, 600]$  nT (Agapitov et al., 2019). These conditions indicate the importance of plasma injections and/or enhanced convection periods and how they cause enhanced nightside electron losses. Such Earthward plasma transport (convection and injections), especially during increased geomagnetic activity, justifies our choice of the cold plasma density reduction (Agapitov et al., 2019). These injections are also associated with electron field-aligned streams caused by the electrostatic turbulence around injection regions or the ionosphere outflow of secondary electrons in response to the enhanced precipitation of plasma sheet electron fluxes (see Khazanov et al., 2014, 2018; Artemyev & Mourenas, 2020; Artemyev et al., 2020, and references therein).

## 5 Discussion and Conclusions

Today’s radiation belt simulations primarily rely on EMIC-driven electron precipitation to explain relativistic electron losses (see, e.g., Ma et al., 2015; Drozdov et al., 2017, and references therein), in addition to dropouts related to magnetopause shadowing loss (e.g., see Shprits et al., 2006; Turner et al., 2014; Boynton et al., 2016, 2017; Olfier et al., 2018; Xiang et al., 2018). Analysis presented here shows that the inclusion of realistic whistler-mode wave properties can meaningfully enhance relativistic electron scattering rates, thereby reducing the relative importance of EMIC waves on the nightside, at least for electrons below 1 MeV. While it has been known for a long time that whistler-mode waves can accelerate electrons to relativistic energies (Thorne et al., 2013; Li et al., 2014; Mourenas, Artemyev, Agapitov, Krasnoselskikh, & Li, 2014; Omura et al., 2015; Hsieh & Omura, 2017; Allison & Shprits, 2020), contribution of this wave mode to relativistic electron losses may be underestimated in modern-day simulations due to the lack of observations that can reliably quantify it. This has recently changed with the availability of ELFIN’s unique precipitation observations, which now allow us to quantify how well modeling – based on statistical averages of wave properties and plasma density – reflects the observed precipitation energy spectra of energetic electrons.

We previously showed that using only field-aligned, monochromatic whistler-mode waves with realistic wave amplitudes as a function of magnetic latitude was sufficient to approximate relativistic electron losses at the dawn, noon, and dusk sectors (Tsai et al., 2023). However, the modeled precipitating-to-trapped flux ratio significantly underestimated ELFIN-obtained statistics of precipitation energy spectra in the nightside MLT sector. Pertinent to ELFIN statistics, we specifically excluded all data exhibiting signatures of field-line curvature scattering, EMIC waves, and any signatures of noise or poor statistics. The resulting ELFIN statistics are 3 years of unambiguous whistler-mode wave-driven energetic electron precipitating-to-trapped flux ratios across a range of MLT,  $L$ -shells, and geomagnetic activity. At first, we used test particle simulations to examine various wave and plasma characteristics that may potentially cause this discrepancy. However, test particle simulations showed that, while some effects led to better agreement, the discrepancy was still large. However, by additionally utilizing a state-of-the-art quasi-linear diffusion code, we were able to quantify each key wave parameter – alone and in combination – relative to ELFIN observations, thereby determining the importance of

including empirically-obtained equatorial plasma frequency, wave-normal angle distributions, and wave frequency distributions. We found that, in addition to the prerequisite, empirically-provided  $B_w(\lambda)$  (Tsai et al., 2023), inclusion of all three modifications – realistic  $\Omega_{pe}$ ,  $\omega_m(\lambda)$ , and  $\theta(\lambda)$  – were sufficient to recover the more intense nightside energetic precipitation observed by ELFIN. A reduced plasma density, indicative of geomagnetically active times, results in relative enhancement of precipitation in the sub-relativistic regime ( $< 300$  keV), while wave obliquity significantly enhances relativistic electron scattering  $> 500$  keV. It seems that a decreasing wave frequency as a function of latitude helps balance the two out, leading to a smooth recovery of the 200–600 keV range, without severely overestimating either ends of the precipitation flux ratio spectrum.

The equatorial confinement of whistler-mode waves is attributed to the increase of wave obliquity – or more precisely, the increase of statistical averages of wave normal angles – as expected from wave propagation away from their equatorial source (L. Chen et al., 2013; Breuillard et al., 2012; Agapitov et al., 2013) due to the associated severe damping by Landau resonance with suprathermal electrons (e.g., Bell et al., 2002; Bortnik et al., 2007). This effect is substantially less important on the dayside as compared to the nightside, as evidenced by the significantly larger amplitudes of waves at higher latitudes on the dayside (Meredith et al., 2012). Reduced Landau damping is caused by a milder ambient dayside magnetic field gradient (due to magnetospheric compression) and a lower density of suprathermal electrons (Li, Thorne, Bortnik, et al., 2010; Walsh et al., 2020). As a result, waves on the dayside propagate in higher densities, are less oblique, and have a less pronounced decrease in wave frequencies, in direct opposition to what is observed on the nightside. This explains why an empirical model of  $B_w(\lambda)$  and field aligned waves is sufficient for recovering dayside energetic electron precipitation (Tsai et al., 2023), while further indicating the importance of including realistic wave and background plasma characteristics for such precipitation modeling on the nightside.

To conclude, these results highlight the importance of combining whistler-mode wave characteristics and background plasma for accurately modeling relativistic electron losses from the outer radiation belt. Specifically, we note that:

- The latitudinal distribution of wave amplitude alone cannot account for the intense nightside precipitation of  $\sim 0.1$ – $1$  MeV electrons scattered at mid-to-high latitudes relative to precipitation of  $\sim 100$  keV electrons scattered near the equator.
- Very oblique waves are important for scattering more energetic electrons – becoming more effective in the  $\sim 1$  MeV range – but only in the presence of reduced plasma density or decreasing wave frequency.
- The decrease of wave frequency with latitude, caused by high-frequency wave damping, is not very important on its own. However, together with a reduced plasma density (with or without oblique waves), it can lead to more precipitation of high energy electrons relative to  $\sim 100$  keV electrons.
- Equatorial plasma density decrease during geomagnetically active conditions (characterized by enhanced whistler-mode wave intensity) improves the relative efficiency of resonant electron scattering toward the loss-cone at 100 keV compared to 1 MeV, but alone, it is in poor agreement with ELFIN statistics. However, when combined with increasing WNA and decreasing wave frequency as a function of latitude, this plasma density reduction becomes a catalyst, significantly boosting electron precipitation rates across the energy range up to 1 MeV.

So, in order to best explain the increased precipitation observed by ELFIN on the nightside, modeled whistler-mode waves must have a realistic latitudinally-dependent wave frequency model (Model 2) coupled with a reduced plasma density ( $\Omega_{pe} \in [2.5, 4]$ ) and an associated range of wave obliquity from quasi-field aligned ( $\theta < 30^\circ$ ) to extremely

oblique (WNA3) waves. Any further investigation of these effects likely requires either detailed and comprehensive simulations using modern ray-tracing techniques (e.g., L. Chen et al., 2021, 2022; Hosseini et al., 2021; Hanzelka & Santolík, 2022; Kang et al., 2022; Kang & Bortnik, 2022) or a new generation of satellite missions equipped to make simultaneous measurements of whistler-mode waves and precipitating/trapped electron populations.

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## Open Research

ELFIN data is available at <https://data.elfin.ucla.edu/> and online summary plots at <https://plots.elfin.ucla.edu/summary.php>. Data access and processing was done using SPEDAS V4.1, see Angelopoulos et al. (2019). Test-particle simulation code is found at <https://github.com/ethantsai/nlwhistlers> (Tsai, 2023).

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