

# JOURNAL OF GLACIOLOGY



**CAMBRIDGE**  
UNIVERSITY PRESS

THIS MANUSCRIPT HAS BEEN SUBMITTED TO THE JOURNAL OF GLACIOLOGY AND HAS NOT BEEN PEER-REVIEWED.

## **Ambiguous stability of glaciers at bed peaks**

Journal:	<i>Journal of Glaciology</i>
Manuscript ID	Draft
Manuscript Type:	Letter
Date Submitted by the Author:	n/a
Complete List of Authors:	Robel, Alexander; Georgia Tech, Earth and Atmospheric Sciences Pegler, Sam; University of Leeds, Applied Mathematics Catania, Ginny; University of Texas, Institute for Geophysics felikson, denis; NASA Goddard Space Flight Center, Cryospheric Sciences Laboratory; USRA, Goddard Earth Sciences Technology and Research Studies and Investigations Simkins, Lauren; University of Virginia, Department of Environmental Sciences
Keywords:	Ice-sheet modelling, Subglacial processes, Ice dynamics
Abstract:	Increasing ice flux from glaciers retreating over deepening bed topography has been implicated in the recent acceleration of mass loss from the Greenland and Antarctic ice sheets. We show in observations that some glaciers have remained at peaks in bed topography without retreating despite enduring significant changes in climate. Observations also indicate that some glaciers which persist at bed peaks undergo sudden retreat years or decades after the onset of local ocean or atmospheric warming. Using model simulations, we show that glacier

	<p>persistence may lead to two very different futures: one where glaciers persist at bed peaks indefinitely, and another where glaciers retreat from the bed peak suddenly without a concurrent climate forcing. However, it is difficult to distinguish which of these two futures will occur from current observations. We conclude that inferring glacier stability from observations of persistence obscures our true commitment to future sea-level rise under climate change.</p>

SCHOLARONE™  
Manuscripts

# Ambiguous stability of glaciers at bed peaks

Alexander A. ROBEL,<sup>1</sup> Samuel S. PEGLER,<sup>2</sup> Ginny CATANIA,<sup>3</sup> Denis FELIKSON,<sup>4</sup> Lauren M. SIMKINS,<sup>5</sup>

<sup>1</sup>*School of Earth and Atmospheric Sciences, Georgia Institute of Technology, Atlanta, GA, USA*

<sup>2</sup>*School of Mathematics, University of Leeds, Leeds, UK*

<sup>3</sup>*Institute of Geophysics, University of Texas, Austin, TX, USA*

<sup>4</sup>*NASA Goddard Space Flight Center, Greenbelt, MD, USA*

<sup>5</sup>*Department of Environmental Sciences, University of Virginia, Charlottesville, VA, USA*

*Correspondence: Alexander A. Robel <robel@eas.gatech.edu>*

**ABSTRACT.** Increasing ice flux from glaciers retreating over deepening bed topography has been implicated in the recent acceleration of mass loss from the Greenland and Antarctic ice sheets. We show in observations that some glaciers have remained at peaks in bed topography without retreating despite enduring significant changes in climate. Observations also indicate that some glaciers which persist at bed peaks undergo sudden retreat years or decades after the onset of local ocean or atmospheric warming. Using model simulations, we show that glacier persistence may lead to two very different futures: one where glaciers persist at bed peaks indefinitely, and another where glaciers retreat from the bed peak suddenly without a concurrent climate forcing. However, it is difficult to distinguish which of these two futures will occur from current observations. We conclude that inferring glacier stability from observations of persistence obscures our true commitment to future sea-level rise under climate change.

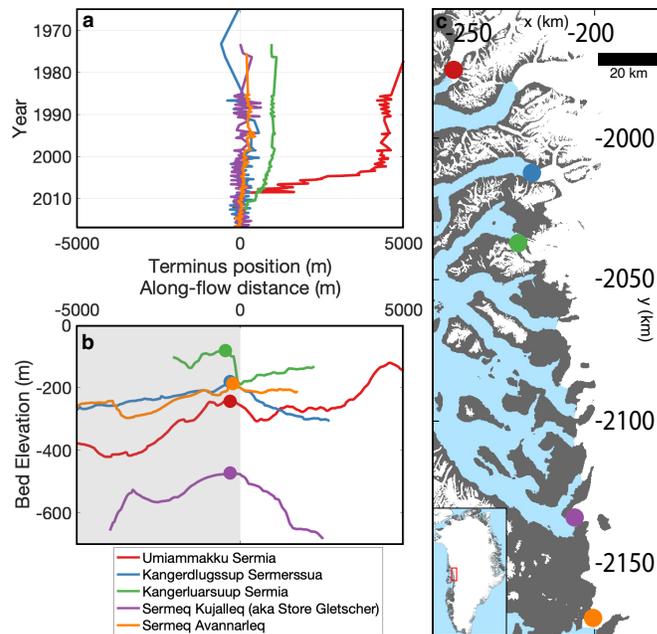
## INTRODUCTION

Mass loss from the Greenland and Antarctic ice sheets has accelerated in recent decades, driven by increasing surface melt and discharge of ice from glaciers (Shepherd and others, 2018; Mouginot and others,

27 2019). The increase in glacier discharge is driven, in part, by glacier retreat over deepening (retrograde) bed  
28 topography, which may initiate a positive feedback known as the “marine ice sheet instability” (Weertman,  
29 1974). However, the climate forcing needed to initiate this positive feedback depends on a range of other  
30 process including ice shelf buttressing and subglacial friction (Gudmundsson and others, 2012; Robel and  
31 others, 2016; Haseloff and Sergienko, 2018; Pegler, 2018; Sergienko and Wingham, 2019), which are not  
32 all represented accurately in theories of marine ice sheet stability and even in complex ice sheet models  
33 which are used to project future ice sheet changes. In particular, bed topography that fluctuates on length  
34 scales of tens to hundreds of kilometers leads to behaviors that are not accurately predicted using classical  
35 theories of marine ice sheet stability (Sergienko and Wingham, 2021).

36 As observations of subglacial bed topography and glacier retreat have improved, we are learning that  
37 bed topography is bumpy at a wide range of length scales (Jordan and others, 2017; Morlighem and others,  
38 2017, 2020) and that many glaciers in Greenland and Antarctica have undergone large retreats (Tinto and  
39 Bell, 2011; Smith and others, 2017; Catania and others, 2018). Still, many glaciers have not retreated  
40 during the observational era, even while nearby glaciers have retreated in response to regional warming of  
41 the ocean and atmosphere. Notable examples includes Thwaites Glacier, West Antarctica, where geological  
42 evidence recorded the persistence of the grounding line at a bed peak for hundreds to thousands of years  
43 (Tinto and Bell, 2011), even amidst significant fluctuations in ocean temperatures (Hillenbrand and others,  
44 2017). Nearby, observations show that Pine Island Glacier persisted at a bed peak until the 1970’s, even  
45 though regional warming of the ocean began in the 1940’s (Smith and others, 2017). As we will discuss  
46 further in section , large portions of the Greenland coast have also been subject to incursions of warm ocean  
47 water, though different glaciers have responded to these incursions in different ways (Catania and others,  
48 2018), with the presence of sharp bed peaks being a key factor both in Greenland and in Antarctica.

49 Here we demonstrate both observationally and using model simulations that the retreat of a marine-  
50 terminating glacier may pause at bed peaks for prolonged time periods even while the glacier continues to  
51 lose mass in response to a current or previous climate forcing. The persistence of glaciers at bed peaks  
52 ultimately leads to one of two very different futures: one in which the glacier continues to persist without  
53 losing mass, and another where retreat occurs suddenly without a concurrent change in climate and leads  
54 to a significant acceleration in mass loss. However, it is difficult to distinguish which of these two possible  
55 futures will occur from current observations of persistent glaciers. We will also discuss how glacier stability  
56 is not necessarily implied by observations of glacier persistence. Ultimately, this ambiguous behavior of

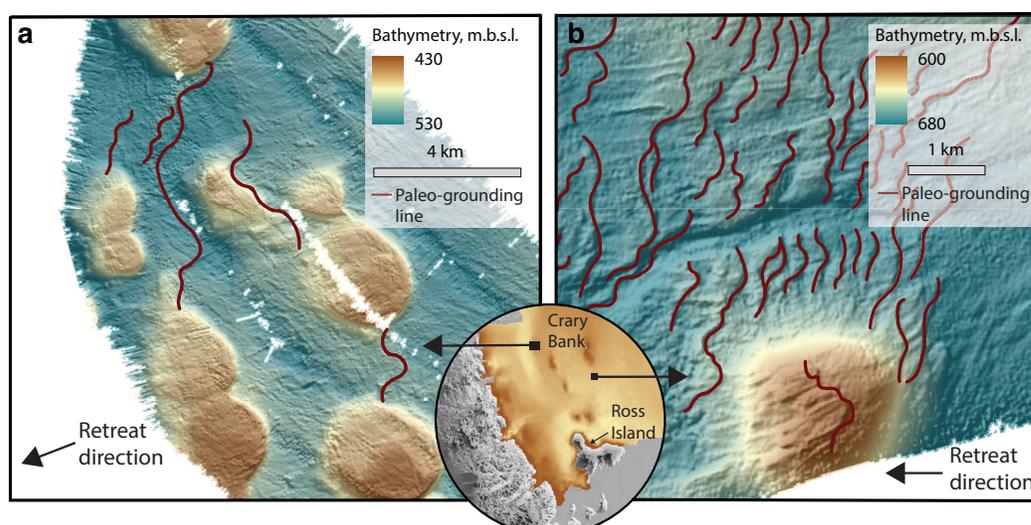


**Fig. 1.** Observational evidence of terminus and grounding line persistence at bed peaks in Central West Greenland (CWG). (a) Terminus positions ( $x$ -axis) over time ( $y$ -axis) at five CWG glaciers derived from satellite-based sensors (Catania and others, 2018). (b) Along-flow bed topography at CWG glaciers in panel (a), with the  $x$ -axis is the along-flow distance relative to recent (2016) terminus position, with  $x = 0$  representing the present position of the glacier termini and gray shading indicating where there is currently grounded glacier ice ( $x < 0$ ). Nearest bed peaks upstream of the current terminus denoted by a filled circle in each case. For glaciers with strong cross-fjord variations in topography (Kangerluarsuup, Kujalleq), the minimum cross-fjord bed topography is used; for the others, mean cross-fjord topography is used. Bathymetry from BedMachine data compilation (panel b) (Morlighem and others, 2017). (c) Location of CWG glaciers in panels (a) and (b) on polar stereographic north projection (EPSG:3413).

57 seemingly “stable” glaciers obscures the true commitment to future sea level rise under anthropogenic  
 58 climate change.

## 59 OBSERVATIONS OF GLACIER PERSISTENCE

60 Central West Greenland provides a particularly well-observed laboratory for understanding glacier retreat  
 61 over bumpy beds. As in most of Greenland, surface melting has been persistently intensifying since the  
 62 1970’s (or potentially earlier; Trusel and others, 2018). In the late 1990’s an influx of warm water from the  
 63 North Atlantic arrived in glacier fjords in this region (Holland and others, 2008). A compilation of terminus  
 64 positions recorded by visible satellite imagery (Catania and others, 2018) show that many glaciers in Central



**Fig. 2.** Bathymetry (in meters below sea level) of the south-western Ross Sea (inset bottom) with grounding zone wedges indicated by brown lines, which are generally perpendicular to the local retreat direction (indicated by black arrows). Multibeam echo sounding bathymetry collected on cruise NBP1502A (Simkins and others, 2017; Greenwood and others, 2018).

65 West Greenland (CWG) retreated between the late 1990's and the early 2000's when ocean temperatures  
 66 were warm. However, some glaciers in this region have not retreated during the observational record, despite  
 67 experiencing the same influx of warm ocean water. Figure 1a shows observations of terminus positions at  
 68 four such persistent glaciers, Kangerdlugssup Sermerssua (blue), Kangerluarsuup Sermia (green), Sermeq  
 69 Kujalleq (purple, aka Store Gletscher), and Sermeq Avannarleq (orange). Figure 1b shows the along-flow  
 70 bed topography at these same glaciers from the BedMachine v3 dataset (Morlighem and others, 2017).  
 71 These glaciers have persisted less than one kilometer downstream of bed peaks, indicating the critical  
 72 importance of peaks in bed topography in potentially delaying or preventing rapid glacier retreat. Glaciers  
 73 in this region that did retreat following the ocean warming event in the late 1990's mostly retreated away  
 74 from bed peaks (on which they had previously persisted) and all have since ceased retreat upon reaching  
 75 a new bed peak. In Figure 1, we show one example of such a glacier, Umiammakku Sermia (red), which  
 76 began rapidly retreating approximately 5 years after the arrival of warm waters in the region, before ceasing  
 77 retreat at a bed peak around 2010.

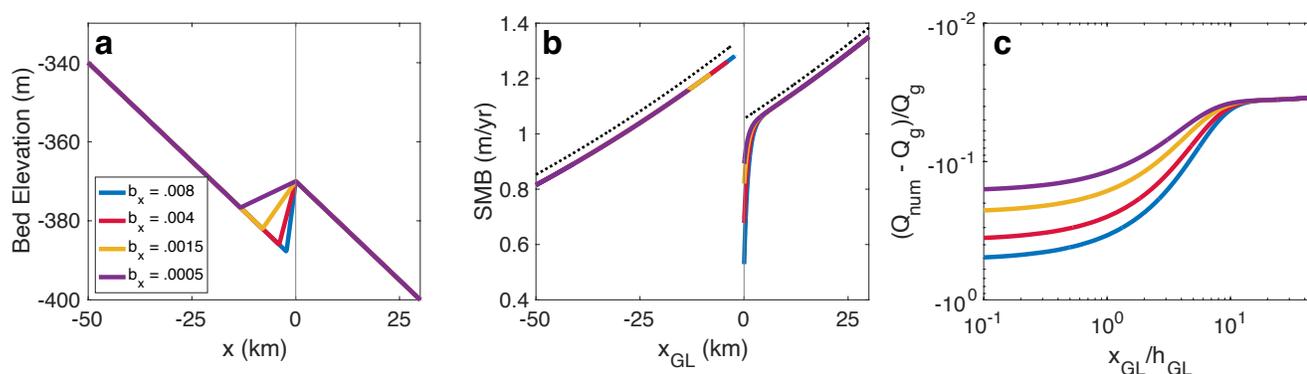
78 Geological evidence from regions of past glacier retreat further demonstrates the importance of bed  
 79 peaks in the response of glaciers to climate change. The bathymetry of the Ross Sea, Antarctica is  
 80 composed of smooth, flat troughs separating large plateaus. Amid this smooth bathymetry, localized

81 recessional moraines and grounding zone sediment wedges record locations where the deglacial retreat  
82 of glaciers in the Ross Sea embayment paused for prolonged time periods (Simkins and others, 2017;  
83 Greenwood and others, 2018). Figure 2 focuses on two particular locations in the Ross Sea where high-  
84 resolution multibeam bathymetric observations show pervasive grounding zone wedges connecting, parallel  
85 to, and on top of seamounts on otherwise flat topography. Such evidence of grounding line persistence is not  
86 present in surrounding flat portions of the seafloor, indicating that these bed peaks (which are generated by  
87 non-glaciological processes) exert an important control on glacier retreat. Other marine geophysical surveys  
88 of the seafloor in regions of past glacier retreat also reveal widespread geological evidence for prolonged  
89 periods of terminus persistence at bed peaks over a wide range of time periods and local conditions (Stoker  
90 and others, 2009; Greenwood and others, 2017; Todd and Shaw, 2012).

## 91 **ENHANCED GLACIER STABILITY AT BED PEAKS**

92 To understand how bed peaks affect glacier stability, we consider first their effect on steady-state terminus  
93 positions, before considering their effect on transient evolution of the terminus position in the next section.  
94 To simulate a typical marine-terminating glacier near a bed peak, we use a one-dimensional flowline model  
95 of a marine-terminating glacier which solves the shallow stream/shelf approximation (SSA) and mass  
96 conservation equations to determine the evolution of ice thicknesses, velocities, and terminus position (as  
97 described in Schoof, 2007a, and many other studies). The glacier is assumed to terminate where it goes  
98 afloat in seawater, and in the cases we consider in this study, ice flow is dominated by sliding over a  
99 moderately slippery bed (parameters listed in Table 1). We simulate the glacier velocity, thickness, and  
100 terminus position for prescribed surface mass balance (SMB, net annual snowfall and surface melt), which  
101 we assume to be uniform over the surface of the glacier. The position of the terminus is accurately modeled  
102 using a refined moving mesh. Glacier steady-states are determined by numerically solving for glacier states  
103 with rates of change that are zero to within machine precision (and with transient perturbations to glacier  
104 state to confirm stability). We have also replicated the substance of the steady-state and transient results  
105 described hereafter using very high-resolution simulations of the Elmer/Ice Full-Stokes numerical glacier  
106 model (see Figure S1), indicating that the SSA simplification does not affect the substance of the conclusions  
107 in this study.

108 The four idealized bed topographies we consider (Figure 3a) all have a single bed peak, but with  
109 different reverse bed slopes just upstream of the peak, and otherwise the same forward-sloping bed (i.e.



**Fig. 3.** Simulated stable grounding line positions in the vicinity of a bed peak. (a) Four idealized bed topographies with differing bed slope just upstream of bed peak. (b) Bifurcation diagrams showing steady-state grounding line positions over a range of surface mass balance and initial grounding line positions. The dotted line is the stable grounding line positions predicted from an approximation for ice flux based on neglecting the effect of local slope,  $Q_g$  (Schoof, 2007b). (c) The proportional difference between the ice flux at the terminus predicted from our numerical solution,  $Q_{num}$ , and the ice flux that would be predicted on neglect of the effect of local slope,  $Q_g$ , as a function of distance from the bed peak (normalized by grounding line ice thickness).

110 shallowing towards the interior). Simulations show that over a wide range of SMB, glacier termini persist  
 111 indefinitely (i.e. reside at a stable steady-state) near bed peaks (Figure 3b). We find that at the sharp  
 112 bed peaks we consider in this study, which entail a rapid spatial transition from a forward-sloping bed to  
 113 a sufficiently reverse sloped bed (i.e. over a horizontal length scale of several kilometers), lead to glacier  
 114 stability over a wider range of SMB than what is predicted in prevailing theories of terminus stability  
 115 (dotted line in Figure 3b, reproduced from Schoof, 2012). The steeper the reverse sloped bed upstream  
 116 of the bed peak, the wider the range of SMB over which the glacier will remain stable. For the steepest  
 117 reverse slope (shown in blue), the glacier remains stable a short distance downstream of the topographic  
 118 high for a significant range of SMB from from 0.5 to 1.0  $\text{m yr}^{-1}$ .

119 The cause of enhanced glacier stability at bed peaks can be explained by examining how ice flux out  
 120 of the glacier changes as the glacier gets close to the bed peak. As the terminus approaches within  $\sim 10$  ice  
 121 thicknesses of the bed peak, the ice flux (Figure 3c) decreases much more rapidly than is predicted under  
 122 the assumption of negligible bed slope near the terminus. Indeed the magnitude of this reduction in ice  
 123 flux near the bed peak (10-50% in these examples) is comparable to the effect of ice shelf buttressing on  
 124 grounding line ice flux (Reese and others, 2018; Mitcham and others, 2021). The cause of this rapid decline  
 125 in ice flux is a lowered driving stress on the ice flowing uphill to the bed peak, which lowers ice velocity

**Table 1.** Parameter values for steady-state and transient retreat simulations (unless otherwise specified in text)

Parameter	Description	Value
$A_g$	Nye-Glen Law coefficient ( $\text{Pa}^{-n} \cdot \text{s}^{-1}$ )	$4.2 \times 10^{-25}$
$b_x$	Prograde bed slope	$1 \times 10^{-3}$
$C$	Basal friction coefficient ( $\text{Pa} \cdot \text{m}^{-1/n} \cdot \text{s}^{1/n}$ )	$1 \times 10^6$
$g$	Acceleration due to gravity ( $\text{m} \cdot \text{s}^{-2}$ )	9.81
$m$	Weertman friction law exponent	1/3
$n$	Nye-Glen Law exponent	3
$\Delta t$	Time step (yr)	1
$\rho_i$	Ice density ( $\text{kg} \cdot \text{m}^{-3}$ )	917
$\rho_w$	Seawater density ( $\text{kg} \cdot \text{m}^{-3}$ )	1028

126 just upstream of the bed peak and influences terminus ice flux through longitudinal viscous stresses. This  
 127 reduced terminus ice flux is in balance with the total ice flux arriving at the terminus from upstream,  
 128 maintaining a stable terminus position, even under dramatically lower SMB.

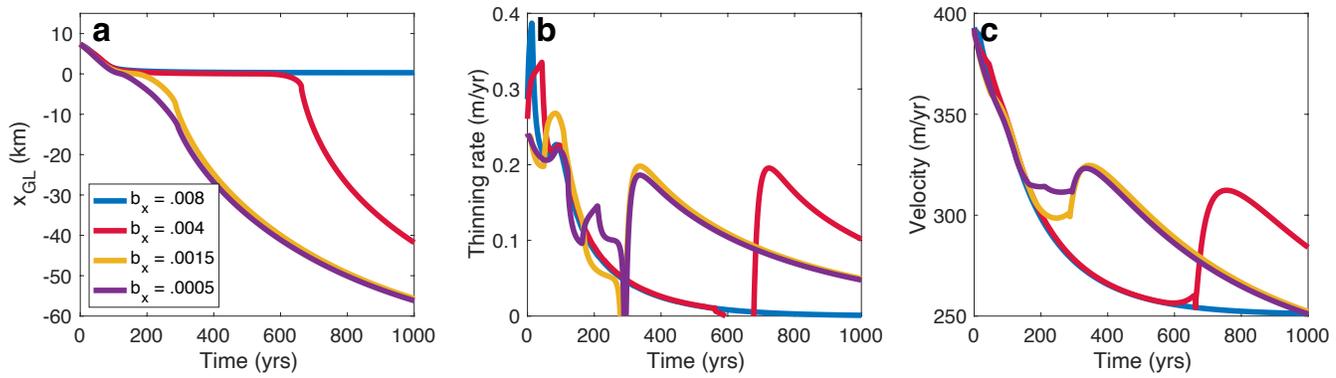
129 The enhanced stability of simulated termini near bed peaks, as compared to prior theory, explains  
 130 counterintuitive aspects of observations. There is a wide range of external forcing over which a terminus  
 131 will persist at a bed peak, explaining why so many glacier termini are observed at bed peaks on bumpy bed  
 132 topography. Indeed, repeating these steady-state simulations for corrugated bed topography (a regular  
 133 series of peaks and troughs) indicates stable glacier terminus positions exist almost exclusively at bed  
 134 peaks (Figure S2). The reduced glacier sensitivity to climatic changes at bed peaks also explains why  
 135 many glaciers are observed to persist, seemingly on the precipice of instability, even while experiencing  
 136 substantial fluctuations in local climate (Tinto and Bell, 2011; Hillenbrand and others, 2017; Catania and  
 137 others, 2018). Such enhanced stability of glaciers at bed peaks is in contrast to the prevailing idea that  
 138 glaciers at bed peaks are particularly “vulnerable” to fluctuations or trends in climate due to their proximity  
 139 to reverse-sloping beds over which the marine ice sheet instability occurs (Gladstone and others, 2012; Ross  
 140 and others, 2012; Morlighem and others, 2020).

141 The enhanced stability near points of destabilization and non-smooth changes in bed topography is  
 142 also a hallmark of a “crossing-sliding bifurcation” (di Bernardo and others, 2008). The system behavior  
 143 in the vicinity of such bifurcations is different from the canonical “saddle-node bifurcation”, which has  
 144 previously been identified as the route through which grounding lines lose stability (Mulder and others,

145 2018; Pegler, 2018). In a saddle-node bifurcation, the loss of stability occurs smoothly and suddenly upon  
146 approach of the system state to the bifurcation point. In a crossing-sliding bifurcation, the loss of stability  
147 instead occurs due to an abrupt (i.e., non-smooth) change in the system properties. In the case of a sharp  
148 bed peak, smooth parameter variations causes the stable glacier state to reach the bifurcation point and  
149 then remains there, before eventually crossing the bed peak and initiating a large change in glacier state.  
150 This distinction in type of bifurcation can be important because it leads to larger “jumps” in the system  
151 state (i.e., ice volume loss) upon crossing the bifurcation. In other words, as the forcing gradually changes  
152 (i.e., SMB decreases), the onset of rapid ice loss is delayed, leading to a higher rate of ice loss if and when  
153 the terminus crosses the bed peak. In Figure 3b, this amounts to the difference between a 30 km jump in  
154 grounding line position for a relatively smooth bump (i.e. the dotted or purple lines), compared to a jump  
155 of 50-100 km for sharper peaks (yellow, red, blue lines). As we will show next, even when climate trends  
156 or fluctuations exceed the threshold for instability identified in Figure 3b, the onset of rapid glacier retreat  
157 may be substantially delayed.

## 158 **DISTINGUISHING GLACIER STABILITY FROM TRANSIENT PERSISTENCE**

159 In transient simulations of terminus retreat over idealized bed peaks (the same as in the previous section),  
160 a glacier is initialized at a steady state with its terminus just downstream of a bed peak, and is then  
161 subjected to a 40% step reduction in SMB uniformly over the glacier catchment. Figure 4a shows that  
162 some of the simulated glaciers retreat up to, then transiently persist, just downstream of the bed peak for  
163 a period of time spanning decades to centuries (yellow and red lines), before eventually crossing the bed  
164 peak and rapidly retreating over the reverse sloping bed. There are also cases where there is merely a brief  
165 slowdown in the rate of retreat at the bed peak (purple line), and other cases where the persistence continues  
166 indefinitely (blue line). We define such an indefinitely persistent case as “stable” in the mathematical sense,  
167 where a system state persists forever with no change in forcing. Similar behaviors of transient and indefinite  
168 persistence of grounding lines at bed peaks also occur in equivalent full-Stokes simulations of grounding  
169 line retreat over bed peaks (Figure S3) and in SSA simulations of glacier retreat with different types of  
170 forcing and smoothed bed peaks (Figures S4-S6). These transient simulations show that even for SMB  
171 values that do not correspond to a stable glacier configuration (shown in Figure 3b), there may still be  
172 prolonged periods of transient terminus persistence. Longer periods of transient persistence lead to more  
173 rapid subsequent retreat, which continues even as the terminus encounters forward-sloping bed topography.



**Fig. 4.** Simulated terminus retreat in the vicinity of a bed peak. (a) Evolution of a terminus from steady state, in response to an instantaneous 40% reduction in surface mass balance over the glacier catchment, for a variety of upstream bed slopes. Grounding line position ( $y$ -axis) is relative to bed peak location as in Figure 3a. (b) Thinning rate 50 km upstream of grounding line in transient simulations. (c) Ice velocity 50 km upstream of grounding line in transient simulations.

174       Glaciers that persist at bed peaks continue to lose mass through thinning upstream of the grounding line  
 175 following changes in climate forcing, as seen in observations of recent thinning upstream of the terminus at  
 176 persistent glaciers throughout Greenland (Kjeldsen and others, 2015; Mouginot and others, 2019; Shepherd  
 177 and others, 2020; Felikson and others, 2017). At persistent glaciers in CWG, this thinning is mostly  
 178 being driven by negative surface mass balance anomalies, which are largely offset by dynamic thickening  
 179 bringing ice from upstream portions of glacier catchments (Felikson and others, 2017). Ultimately, this  
 180 upstream-intensified thinning leads a decrease in ice surface slope and upstream slowing, which is captured  
 181 in observations of persistent CWG glaciers (Joughin and others, 2010) and our simulations (Figure 4b-  
 182 c). Though such thinning is less than that occurring at retreating glaciers through dynamic thinning, it  
 183 nonetheless shows that persistence of a glacier terminus is not necessarily indicative of a glacier in mass  
 184 equilibrium.

185       We can compare our simulated glaciers which stabilize at bed peaks to those which merely pause at  
 186 bed peaks to ascertain whether observations of persistent glaciers may provide evidence of their eventual  
 187 fate. We find that, regardless of their eventual fate (remaining or retreating), the glaciers we simulate  
 188 which persist at bed peaks have upstream thinning rates within millimeters/year of each other (Figure 4b  
 189 and Figure S8), and ice velocities within meters/year of each other (Figure 4c and Figure S7). It would  
 190 thus be exceedingly difficult to observationally distinguish glaciers that are merely paused from those that  
 191 have stabilized indefinitely at bed peaks. Other studies have also found that, in realistic simulations of

192 the future retreat of glaciers away from bed peaks, small uncertainties in the observed glacier state, bed  
193 topography, or the climate forcing produce large uncertainties in the timing of the onset of rapid glacier  
194 retreat which is then amplified by the divergence of retreat predictions due to marine ice sheet instability  
195 (Gladstone and others, 2012; Robel and others, 2019). Ultimately, the delicate balance between advection  
196 and thinning at persistent glaciers makes it exceedingly difficult to project retreat of glaciers over bumpy  
197 bed topography, and further emphasizes the need for more accurate observational constraints on glacier  
198 state and rate of change, bed topography, and local climate change.

## 199 **DISCUSSION AND CONCLUSIONS**

200 We have shown that glaciers observed at bed peaks have two possible futures: they may remain at the  
201 bed peak indefinitely (i.e., stabilize) or initiate retreat, potentially long after the onset of climate change.  
202 Glaciers persisting at bed peaks may continue to lose mass in response to a previous or sustained climate  
203 change, though there will be an increasing “disequilibrium” between this mass loss and the total committed  
204 glacier mass loss implied by contemporaneous climate forcing (Christian and others, 2018). If the terminus  
205 does eventually cross the bed peak, terminus retreat and total glacier mass loss accelerates rapidly, relaxing  
206 the glacier disequilibrium between instantaneous and total committed mass loss. Eventually, the total sea  
207 level contribution from non-persistent and transiently persistent glaciers may be similar, though the timing  
208 and rate of peak mass loss may be very different (e.g., Figure 4).

209 In attempting to infer the future behavior of glaciers persisting at bed peaks, observations can be  
210 deceptive. We have shown that ice flux and thickness may change considerably with relatively little  
211 change in the terminus position. Thus, interpreting observations of terminus change requires accurate  
212 measurements of bed topography and the critical context of changes in other aspects of glacier state  
213 (particularly interior thickness and velocity) to assess whether the glacier is in balance. Additionally, the  
214 slow response time scale of glaciers, particularly those that have encountered bed peaks, indicates that  
215 the utility of “stability” as a tool for categorizing observed glacier changes is limited without the critical  
216 context of multi-centennial (or millennial) glacier changes, and the climate forcing over that time period.  
217 The scope of these challenges and potential impacts indicate that we should direct a similar degree of  
218 attention and resources to closely observing and carefully simulating persistent glaciers as we do to rapidly  
219 changing glaciers, as it is possible and perhaps likely that they will eventually contribute just as much to  
220 future sea level rise.

221 **ACKNOWLEDGEMENTS**

222 S. Buzzard, Z. Rashed and O. Sergienko contributed to helpful discussions during this project. We  
223 thank M. Morlighem for providing the ISMIP6 basal shear stress inversions and to Cheng Gong for as-  
224 sistance with configuring Elmer/Ice simulations. Financial support was provided by NSF grant 1947882  
225 (to A.A.R) during the completion of this project. Computing resources were provided by the Partner-  
226 ship for an Advanced Computing Environment (PACE) at the Georgia Institute of Technology, Atlanta.  
227 We are thankful for PACE Research Scientist Fang (Cherry) Liu's assistance on HPC challenges. All  
228 code used to generate the figures in this study are available as a persistent Zenodo repository: avail-  
229 able on publication. Model codes used for conducting numerical experiments are also available as per-  
230 sistent Zenodo repositories (MATLAB SSA model: <https://doi.org/10.5281/zenodo.5245271>, Julia SSA  
231 model: <https://doi.org/10.5281/zenodo.5245331>). Full-stokes simulations conducted with Elmer/Ice which  
232 is openly available at: <http://elmerice.elmerfem.org/>.

233 **REFERENCES**

- 234 Catania G, Stearns L, Sutherland D, Fried M, Bartholomaeus T, Morlighem M, Shroyer E and Nash J (2018) Geometric  
235 controls on tidewater glacier retreat in central western Greenland. *Journal of Geophysical Research: Earth Surface*,  
236 **123**(8), 2024–2038
- 237 Christian JE, Koutnik M and Roe G (2018) Committed retreat: controls on glacier disequilibrium in a warming  
238 climate. *Journal of Glaciology*, **64**(246), 675–688
- 239 di Bernardo M, Budd C, Champneys AR and Kowalczyk P (2008) *Piecewise-smooth dynamical systems: theory and*  
240 *applications*, volume 163. Springer Science & Business Media
- 241 Felikson D, Bartholomaeus TC, Catania GA, Korsgaard NJ, Kjær KH, Morlighem M, Noël B, Van Den Broeke M,  
242 Stearns LA, Shroyer EL and others (2017) Inland thinning on the greenland ice sheet controlled by outlet glacier  
243 geometry. *Nature Geoscience*, **10**(5), 366–369
- 244 Gladstone RM, Lee V, Rougier J, Payne AJ, Hellmer H, Le Brocq A, Shepherd A, Edwards TL, Gregory J and  
245 Cornford SL (2012) Calibrated prediction of Pine Island Glacier retreat during the 21st and 22nd centuries with  
246 a coupled flowline model. *Earth and Planetary Science Letters*, **333**, 191–199
- 247 Greenwood SL, Clason CC, Nyberg J, Jakobsson M and Holmlund P (2017) The Bothnian Sea ice stream: early  
248 Holocene retreat dynamics of the south-central Fennoscandian Ice Sheet. *Boreas*, **46**(2), 346–362

- 249 Greenwood SL, Simkins LM, Halberstadt ARW, Prothro LO and Anderson JB (2018) Holocene reconfiguration and  
250 readvance of the East Antarctic Ice Sheet. *Nature communications*, **9**(1), 1–12
- 251 Gudmundsson G, Krug J, Durand G, Favier L and Gagliardini O (2012) The stability of grounding lines on retrograde  
252 slopes. *The Cryosphere*, **6**(4), 2597–2619
- 253 Haseloff M and Sergienko OV (2018) The effect of buttressing on grounding line dynamics. *Journal of Glaciology*,  
254 **64**(245), 417–431 (doi: 10.1017/jog.2018.30)
- 255 Hillenbrand CD, Smith JA, Hodell DA, Greaves M, Poole CR, Kender S, Williams M, Andersen TJ, Jernas PE,  
256 Elderfield H and others (2017) West antarctic ice sheet retreat driven by holocene warm water incursions. *Nature*,  
257 **547**(7661), 43–48
- 258 Holland DM, Thomas RH, De Young B, Ribergaard MH and Lyberth B (2008) Acceleration of Jakobshavn Isbrae  
259 triggered by warm subsurface ocean waters. *Nature Geoscience*, **1**(10), 659–664
- 260 Jordan TM, Cooper MA, Schroeder DM, Williams CN, Paden JD, Siegert MJ and Bamber JL (2017) Self-affine  
261 subglacial roughness: consequences for radar scattering and basal water discrimination in northern greenland. *The*  
262 *Cryosphere*, **11**(3), 1247–1264
- 263 Joughin I, Smith BE, Howat IM, Scambos T and Moon T (2010) Greenland flow variability from ice-sheet-wide  
264 velocity mapping. *Journal of Glaciology*, **56**(197), 415–430
- 265 Kjeldsen KK, Korsgaard NJ, Bjørk AA, Khan SA, Box JE, Funder S, Larsen NK, Bamber JL, Colgan W, Van  
266 Den Broeke M and others (2015) Spatial and temporal distribution of mass loss from the greenland ice sheet since  
267 ad 1900. *Nature*, **528**(7582), 396–400
- 268 Mitcham T, Gudmundsson GH and Bamber JL (2021) The impact of recent and future calving events on the larsen  
269 c ice shelf. *The Cryosphere Discussions*, 1–23
- 270 Morlighem M, Williams CN, Rignot E, An L, Arndt JE, Bamber JL, Catania G, Chauché N, Dowdeswell JA, Dorschel  
271 B and others (2017) Bedmachine v3: Complete bed topography and ocean bathymetry mapping of Greenland from  
272 multibeam echo sounding combined with mass conservation. *Geophysical research letters*, **44**(21), 11–051
- 273 Morlighem M, Rignot E, Binder T, Blankenship D, Drews R, Eagles G, Eisen O, Ferraccioli F, Forsberg R, Fretwell  
274 P and others (2020) Deep glacial troughs and stabilizing ridges unveiled beneath the margins of the Antarctic ice  
275 sheet. *Nature Geoscience*, **13**(2), 132–137
- 276 Mouginit J, Rignot E, Bjørk AA, Van Den Broeke M, Millan R, Morlighem M, Noël B, Scheuchl B and Wood  
277 M (2019) Forty-six years of Greenland Ice Sheet mass balance from 1972 to 2018. *Proceedings of the National*  
278 *Academy of Sciences*, **116**(19), 9239–9244

- 279 Mulder T, Baars S, Wubs F and Dijkstra H (2018) Stochastic marine ice sheet variability. *Journal of Fluid Mechanics*,  
280 **843**, 748–777
- 281 Pegler SS (2018) Suppression of marine ice sheet instability. *Journal of Fluid Mechanics*, **857**, 648–680
- 282 Reese R, Winkelmann R and Gudmundsson GH (2018) Grounding-line flux formula applied as a flux condition in  
283 numerical simulations fails for buttressed antarctic ice streams. *The Cryosphere*, **12**(10), 3229–3242
- 284 Robel AA, Schoof C and Tziperman E (2016) Persistence and variability of ice-stream grounding lines on retrograde  
285 bed slopes. *The Cryosphere*, **10**(4), 1883
- 286 Robel AA, Seroussi H and Roe GH (2019) Marine ice sheet instability amplifies and skews uncertainty in projections  
287 of future sea-level rise. *Proceedings of the National Academy of Sciences*, **116**(30), 14887–14892
- 288 Ross N, Bingham RG, Corr HF, Ferraccioli F, Jordan TA, Le Brocq A, Rippin DM, Young D, Blankenship DD and  
289 Siegert MJ (2012) Steep reverse bed slope at the grounding line of the weddell sea sector in west antarctica. *Nature*  
290 *Geoscience*, **5**(6), 393–396
- 291 Schoof C (2007a) Ice sheet grounding line dynamics: Steady states, stability, and hysteresis. *Journal of Geophysical*  
292 *Research - Earth Surface*, **112**(F3), ISSN 0148-0227 (doi: 10.1029/2006JF000664)
- 293 Schoof C (2007b) Marine ice-sheet dynamics. Part 1. The case of rapid sliding. **573**, 27–55, ISSN 0022-1120 (doi:  
294 10.1017/S0022112006003570)
- 295 Schoof C (2012) Marine ice sheet stability. *Journal of Fluid Mechanics*, **698**, 62–72
- 296 Sergienko OV and Wingham D (2019) Grounding line stability in a regime of low driving and basal stresses. *Journal*  
297 *of Glaciology*, **65**(253), 833–849
- 298 Sergienko OV and Wingham DJ (2021) Bed topography and marine ice-sheet stability. *Journal of Glaciology*, 1–15
- 299 Shepherd A, Ivins E, Rignot E, Smith B, Van Den Broeke M, Velicogna I, Whitehouse P, Briggs K, Joughin I, Krinner  
300 G and others (2018) Mass balance of the Antarctic Ice Sheet from 1992 to 2017. *Nature*, **558**, 219–222
- 301 Shepherd A, Ivins E, Rignot E, Smith B, van Den Broeke M, Velicogna I, Whitehouse P, Briggs K, Joughin I, Krinner  
302 G and others (2020) Mass balance of the greenland ice sheet from 1992 to 2018. *Nature*, **579**(7798), 233–239
- 303 Simkins LM, Anderson JB, Greenwood SL, Gonnermann HM, Prothro LO, Halberstadt ARW, Stearns LA, Pollard  
304 D and DeConto RM (2017) Anatomy of a meltwater drainage system beneath the ancestral East Antarctic ice  
305 sheet. *Nature Geoscience*, **10**(9), 691–697

- 306 Smith JA, Andersen TJ, Shortt M, Gaffney A, Truffer M, Stanton TP, Bindschadler R, Dutrieux P, Jenkins A,  
307 Hillenbrand CD and others (2017) Sub-ice-shelf sediments record history of twentieth-century retreat of Pine  
308 Island Glacier. *Nature*, **541**(7635), 77–80
- 309 Stoker MS, Bradwell T, Howe JA, Wilkinson IP and McIntyre K (2009) Late glacial ice-cap dynamics in nw scotland:  
310 evidence from the fjords of the Summer Isles region. *Quaternary Science Reviews*, **28**(27-28), 3161–3184
- 311 Tinto K and Bell RE (2011) Progressive unpinning of Thwaites Glacier from newly identified offshore ridge: Con-  
312 straints from aerogravity. *Geophysical Research Letters*, **38**(20)
- 313 Todd BJ and Shaw J (2012) Laurentide Ice Sheet dynamics in the Bay of Fundy, Canada, revealed through multibeam  
314 sonar mapping of glacial landsystems. *Quaternary Science Reviews*, **58**, 83–103
- 315 Trusel LD, Das SB, Osman MB, Evans MJ, Smith BE, Fettweis X, McConnell JR, Noël BP and van den Broeke  
316 MR (2018) Nonlinear rise in Greenland runoff in response to post-industrial Arctic warming. *Nature*, **564**(7734),  
317 104–108
- 318 Weertman J (1974) Stability of the junction of an ice sheet and an ice shelf. *Journal of Glaciology*, **13**, 3–11