

Supplementary Material

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1 Here, we discuss additional material for the lithospheric complement
2 computation discussed in the main text. Whenever we estimate average
3 asthenospheric anisotropy, we compute an arithmetic average of tensors
4 and then use the Christoffel matrix approach and that mean tensor to get
5 average SKS. To match average splitting, we align and scale a lithospheric
6 tensor before averaging by means of a parameter space search. When
7 accounting for back-azimuth dependence, we use a parameter space
8 search and Silver and Savage's (1994) approach.

9 To illustrate that our approach of inverting for best-fit lithospheric
10 anisotropy layer gives reliable results, we picked 11 stations throughout
11 the study area, and show in Fig. S1 that the apparent splitting parameters
12 from the resulting hypothetical two-layer anisotropy are similar to the
13 station averaged splitting parameters from SWS. Moreover, the two layer
14 model from the constrained inversion where we fix the asthenospheric
15 (lower) layer to that expected from an average of our flow model predicted

16 LPO is usually similar to that of a station measurement only based two
17 layer model.

18 We do not expect the resulting lithospheric complement to be exactly
19 the same as the top layer from SWS two-layer inversion. However, when
20 the flow predicted anisotropy has similar orientation with the bottom
21 layer from the two-layer inversion of SWS, the hypothetical lithospheric
22 anisotropy is also similar to the top layer of the SWS two-layer inversion
23 (Fig. S1), suggesting the validity of this approach.

24 Figs. S2a and b show a comparison between the SWS top layer
25 anisotropy and our hypothetical lithospheric complement. The SWS top
26 layer anisotropy has a wider range of azimuthal orientations and delay
27 times (Fig. S2a), while the hypothetical lithospheric complement shows
28 more smooth and regionally consistent anisotropy patterns, and less
29 variation in delay times. Although differences exist, we see consistency
30 between the two top layer anisotropy estimations in the central U.S. where
31 there is relatively small delay time, in the Great Basin where there is the
32 near circular anisotropy pattern, in the southern Basin and Range where
33 there is the NE-SW anisotropy pattern, and in the eastern U.S. where there
34 is the Appalachian Mountain parallel anisotropy pattern.

35 We also explore a simple method of matching the SWS observation
36 by inverting for the best-fit thickness and anisotropy orientation of a
37 lithospheric layer that consists of frozen-in anisotropy represented by a
38 single elastic tensor. The tensor used here is an averaged single-crystal

39 tensor with 70% olivine and 30% pyroxene from Estey and Douglas
40 (1986). Instead of using a two layer fit and accounting for back-azimuth
41 dependence of splits, we then only seek to match the average fast
42 axes by means of a simple averaging approach. Using this simple
43 method, the resulting hypothetical lithospheric anisotropy show similar
44 orientations to our two layer inversion approach, but the delay time is
45 overall larger (Fig. S2b and c). With the result from this, we can try fit
46 the two-layer anisotropy from this simple method for $\pi/2$ backazimuth
47 distribution, and compare it to the fit from our two layer inversion
48 approach of computing the lithospheric complement. In Fig. S1, the
49 current lithospheric complement approach (solid curve) fits well with the
50 *SKS* splits, while the simple method (dashed curve) fitting is off at some
51 stations.

52 **References**

- 53 Estey, L. H., Douglas, B. J., 1986. Upper mantle anisotropy: A preliminary
54 model. *J. Geophys. Res.* 91 (B11), 11393.
- 55 Silver, P. G., Savage, M. K., 1994. The Interpretation of Shear-Wave
56 Splitting Parameters In the Presence of Two Anisotropic Layers.
57 *Geophys. J. Int.* 119 (3), 949–963.

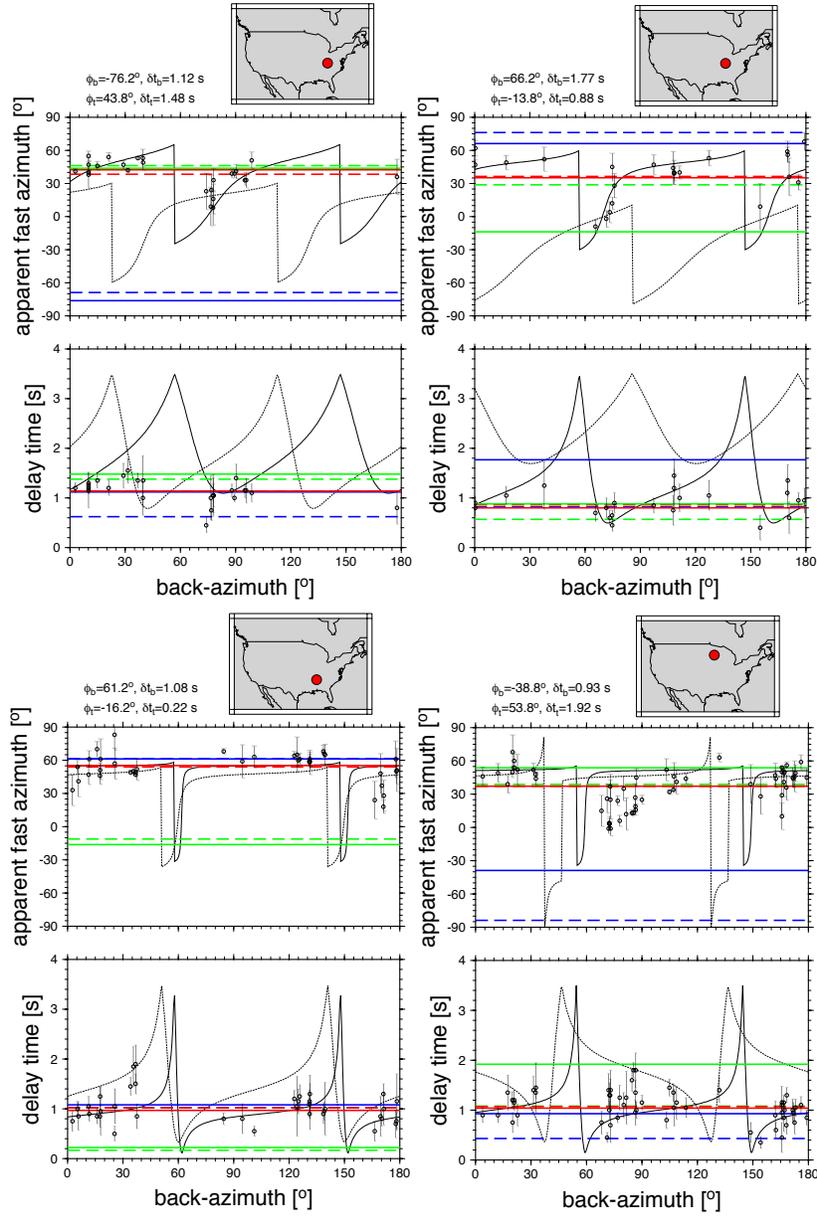


Figure S1: Examples of statistics at stations showing the shear wave splitting (SWS) two-layer inversion results, and the flow model (Model 5) hypothetical two layer anisotropy (top layer: flow model predicted anisotropy, and bottom layer: the hypothetical lithospheric complement).
Caption continues on next page.

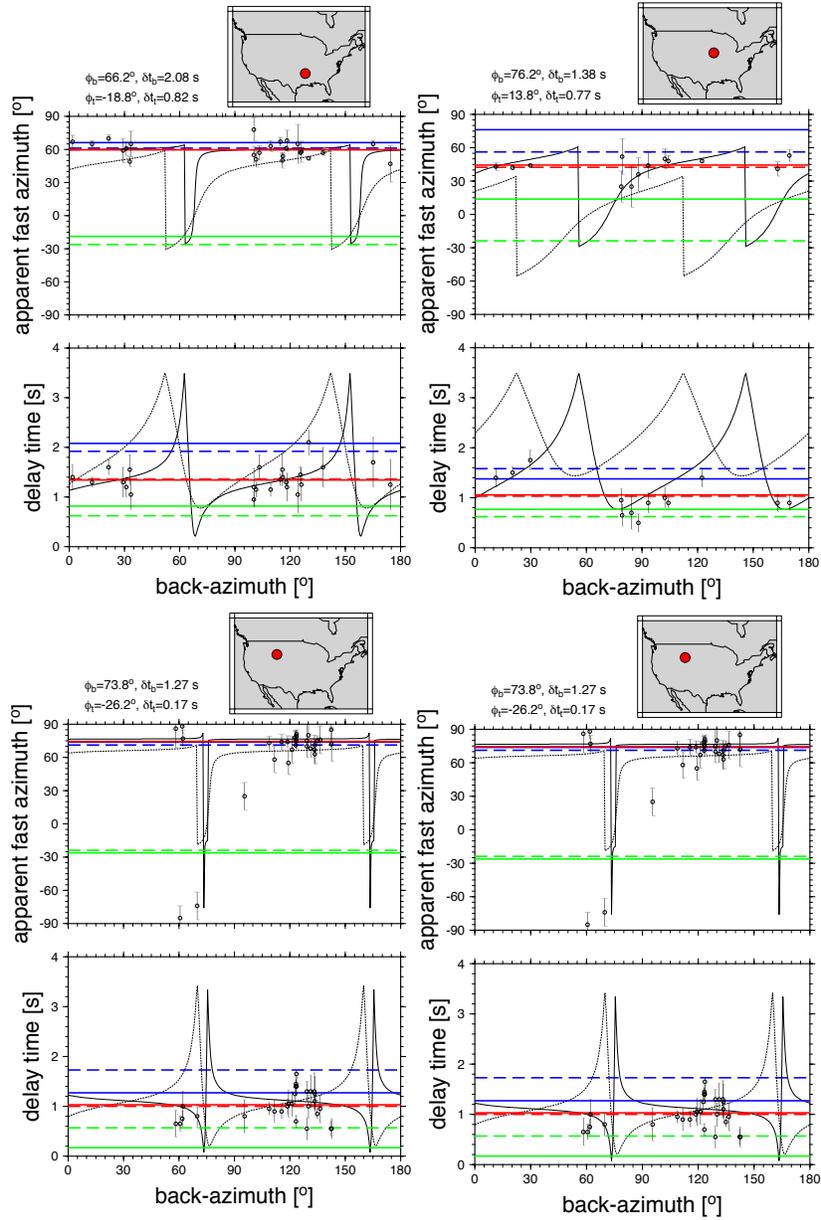


Figure S1: Continues from last page. The average values of the SWS top layer, bottom layer, and station average are shown by the solid blue line, solid green line, and solid red line, respectively. The average values of the top layer, bottom layer, and station average from the hypothetical two layer anisotropy are shown by the dashed blue line, dashed green line, and dashed red line, respectively. Caption continues on next page.

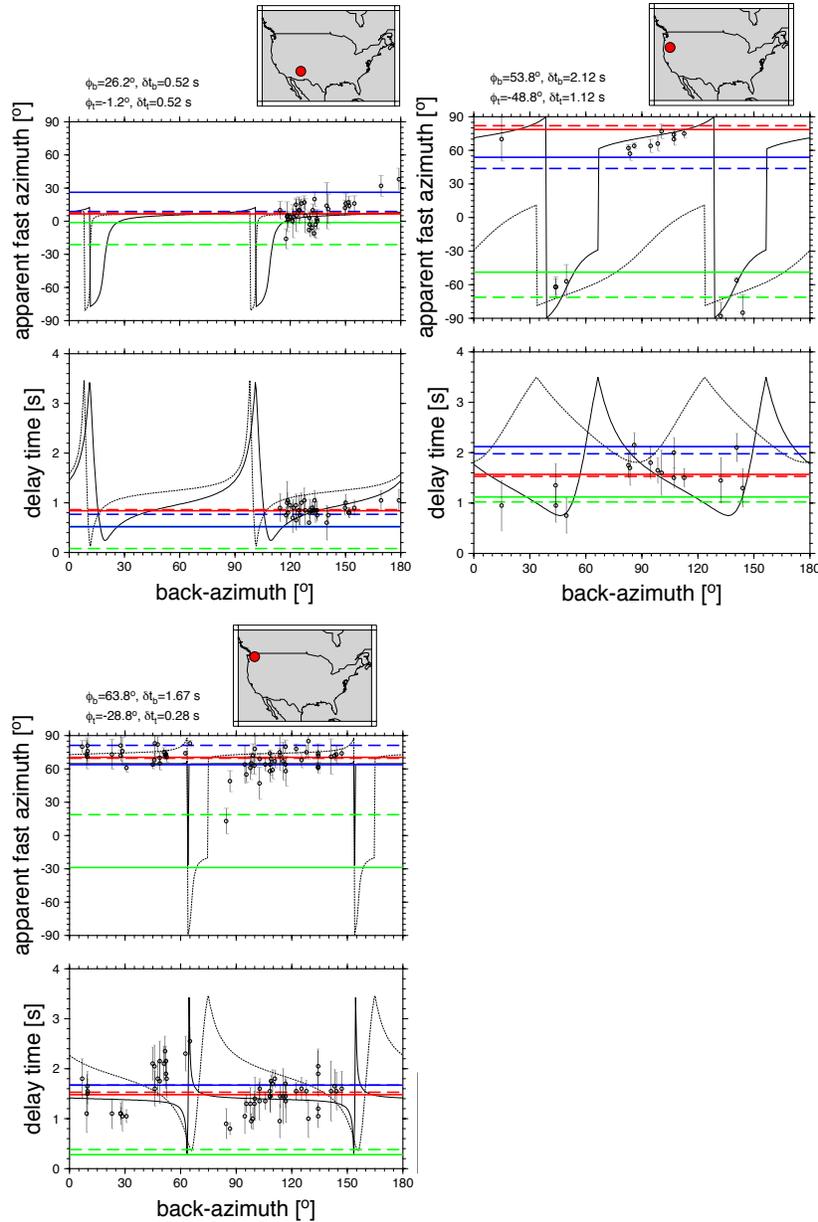


Figure S1: Continues from last page. Splitting parameters from SWS are shown by the black circles, and the vertical lines through the circles show estimated errors. The solid black curve shows the two-layer fitting of the hypothetical two layer anisotropy. The dashed black curve shows the two layer fitting for the simple method of computing lithospheric complement. The location of each station is shown by red dot on the map.

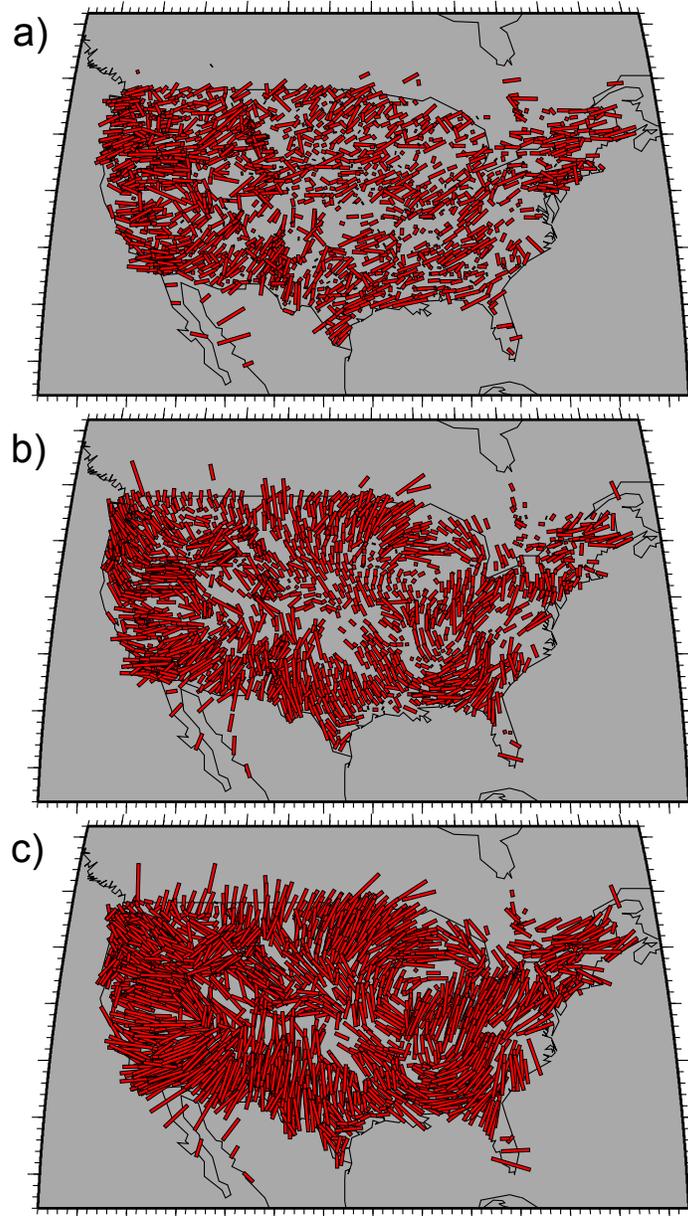


Figure S2: The top-layer anisotropy from a) station by station SWS two-layer inversion, b) method used for the main text of computing the lithospheric complement, and c) the simple method of computing lithospheric complement based on modeling average angles.