

1                   **Resolving the differences in the simulated and**  
2                   **reconstructed climate response to volcanism over the**  
3                   **last millennium**

4                   **Feng Zhu<sup>1</sup>, Julien Emile-Geay<sup>1</sup>, Gregory J. Hakim<sup>2</sup>, Jonathan King<sup>3,4</sup>, Kevin**  
5                   **J. Anchukaitis<sup>3,4,5</sup>**

6                   <sup>1</sup>Department of Earth Sciences, University of Southern California, Los Angeles, CA USA

7                   <sup>2</sup>Department of Atmospheric Sciences, University of Washington, Seattle, WA USA

8                   <sup>3</sup>Department of Geosciences, University of Arizona, Tucson AZ USA

9                   <sup>4</sup>Laboratory of Tree-Ring Research, University of Arizona, Tucson AZ USA

10                   <sup>5</sup>School of Geography and Development, University of Arizona, Tucson AZ USA

11                   **Key Points:**

- 12                   • We explore model–proxy disagreement on the temperature response to volcanic  
13                   eruptions over the past millennium.
- 14                   • Using paleoclimate data assimilation with both real and synthetic data, we show  
15                   that this discrepancy is due to four main factors.
- 16                   • Agreement is found for tree-ring density records at the place and season these prox-  
17                   ies record.

18                   **Plain Language Summary**

19                   The response to volcanic eruptions is a critical benchmark of the performance of  
20                   climate models. Previous studies of the past millennium have identified discrepancies be-  
21                   tween model simulations and climate reconstructions regarding the temperature response  
22                   to volcanic eruptions, raising concerns regarding the source of this mismatch and impli-  
23                   cations for both models and reconstructions. By evaluating the leading sources of dif-  
24                   ferences between simulations and reconstructions, this study shows that accounting for  
25                   known factors largely bridges the gap.

---

Corresponding author: Feng Zhu, [fengzhu@usc.edu](mailto:fengzhu@usc.edu)

## Abstract

Explosive volcanism imposes impulse-like radiative forcing on the climate system, providing a natural experiment to study the climate response to perturbation. Previous studies have identified disagreements between paleoclimate reconstructions and climate model simulations (GCMs) with respect to the magnitude and recovery from volcanic cooling, questioning the fidelity of GCMs, reconstructions, or both. Using the paleoenvironmental data assimilation framework of the Last Millennium Reanalysis, this study investigates the causes of the disagreements, using both real and simulated data. We demonstrate that the disagreement may be resolved by assimilating tree-ring density records only, by targeting growing-season temperature instead of annual temperature, and by performing the comparison at proxy locales. Our work suggests that discrepancies between paleoclimate models and data can be largely resolved by accounting for these features of tree-ring proxy networks.

## 1 Introduction

Volcanic eruptions substantially affect the climate system through their direct effect on shortwave radiation entering the earth system and the ensuing influences on, and feedback to, major modes of ocean-atmosphere variability (Robock, 2000; Schneider et al., 2009). Eruptions therefore offer unique natural experiments with which to probe the fidelity of climate model simulations, understand the response of the ocean and atmosphere circulation to changes in radiative forcing, assess climate system feedbacks, and evaluate solar radiation management proposals (Soden et al., 2002; Timmreck, 2012). The sporadic and infrequent occurrence of large volcanic eruptions means that developing a deeper understanding of their effect on climate necessarily involves analyzing the response to events prior to the instrumental era. Studies of these historical events using climate models and paleoclimate proxies give conflicting estimates of the average climate response, which we address here using a model–data fusion approach.

Significant disagreements have been identified between paleoclimate reconstructions of the climate system response to volcanic eruptions and climate model simulations (D’Arrigo et al., 2013; Schurer et al., 2013). The IPCC AR5 (Masson-Delmotte et al., 2013) describes a discrepancy in the intensity and duration of the simulated versus proxy-based reconstructed temperature response to explosive volcanism (Fig 1b). CMIP5/PMIP3 model simulations for the last millennium experiment (Schmidt et al., 2012a) show more cooling for a shorter duration than paleoclimate reconstructions. Compounding this uncertainty, the precise timing and location of some volcanic eruptions over the last millennium remain unknown (Sigl et al., 2015; Stevenson et al., 2017) as does the magnitude of the radiative forcing (Timmreck et al., 2009). A critical question is whether this mismatch is an artifact of uncertainties in (1) the paleoclimate proxy observations, (2) the reconstruction process, (3) the forcing estimates, (4) climate model physics, or (5) a combination thereof (Anchukaitis et al., 2012; Timmreck, 2012; D’Arrigo et al., 2013; LeGrande & Anchukaitis, 2015; Stoffel et al., 2015).

Here we explore four major sources of uncertainty in reconstructions of surface air temperature over the past millennium: spatial coverage, seasonality, biological memory, and proxy noise. We do so in the context of a paleoenvironmental data assimilation (PDA) framework, the Last Millennium Reanalysis (LMR) (Hakim et al., 2016; Tardif et al., 2019), which provides an objective basis for optimally combining information from proxies and models. We show here that the discrepancy in Fig. 1b is present in our reconstruction framework (Fig. 1c), but that it can be largely reconciled by accounting for the aforementioned sources of uncertainty.

The remainder of the paper is organized as follows: we first introduce the data and methods (Section 2), then explore the causes of the discrepancy (Section 3), leveraging

76 both real proxy and pseudoproxy experiments (PPEs). A discussion follows in Section  
77 4.

## 78 2 Data and methods

### 79 2.1 Paleoclimate data assimilation

80 We apply the paleoenvironmental data assimilation framework of the Last Millen-  
81 nium Reanalysis (LMR) (Hakim et al., 2016; Tardif et al., 2019) to both pseudoproxy  
82 and real proxy data networks. LMR uses an offline ensemble data assimilation proce-  
83 dure for multivariate climate field reconstruction (Steiger et al., 2014), where informa-  
84 tion from a prior expectation of the climate, derived from a climate model, is weighted  
85 against information in proxy records. Weights are determined from the relative error in  
86 these two estimates of the climate, as defined by the update equation in the Kalman fil-  
87 ter, which is optimal if the errors are normally distributed.

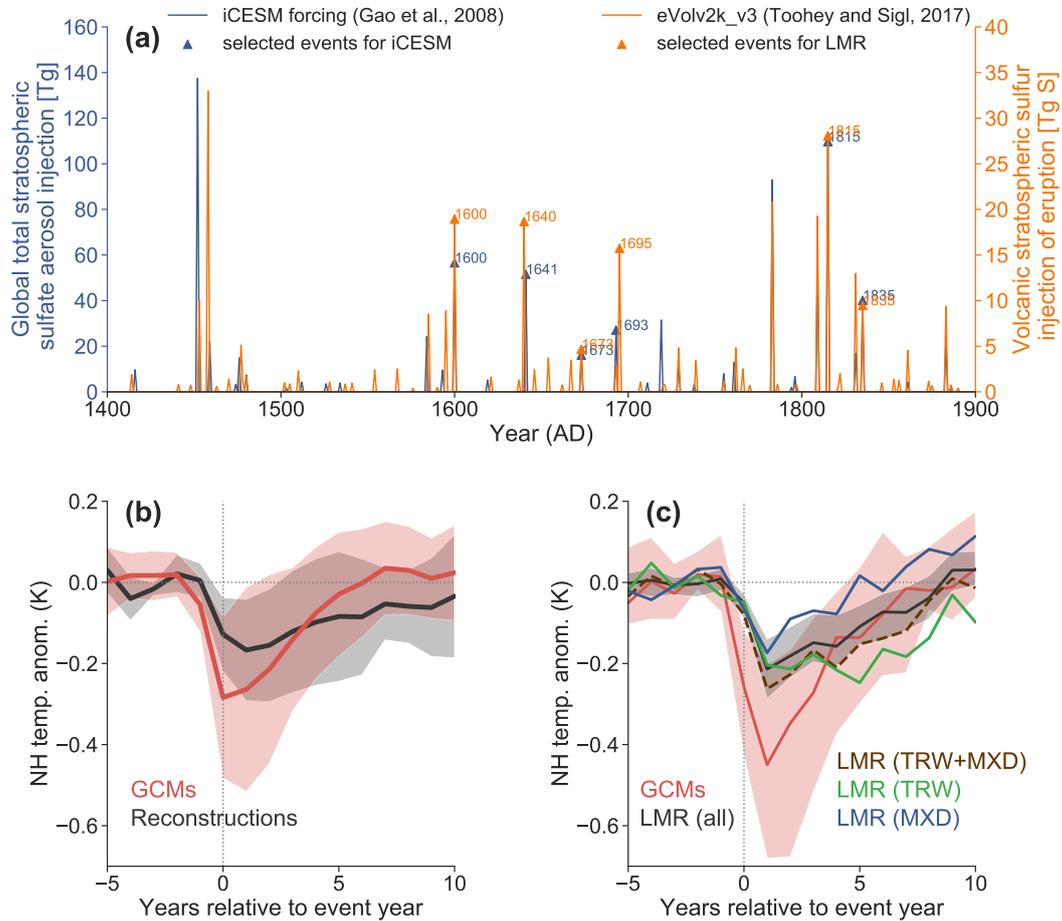
88 The essential components of the procedure are (1) existing climate model data for  
89 the prior expectation, which we take from a last millennium simulation from the isotope-  
90 enabled Community Earth System Model (iCESM) (Stevenson et al., 2019; Brady et al.,  
91 2019); (2) proxy data networks, which we take from the PAGES 2k phase 2 compilation  
92 (PAGES 2k Consortium, 2017, Fig. S1), and the Northern Hemisphere Tree-Ring Net-  
93 work Development (NTREND) compilation (Wilson, Anchukaitis, Briffa, Büntgen, et  
94 al., 2016; Anchukaitis et al., 2017, Fig. S7); and (3) a “forward operator” or proxy sys-  
95 tem model (PSM), which predicts the proxies given the climate state. Here the forward  
96 operator is a linear regression procedure, univariate on annual temperature for corals and  
97 ice cores, and seasonal, univariate on seasonal temperature for maximum latewood den-  
98 sity records and seasonal bivariate (temperature, precipitation) for tree-ring width records,  
99 as in Tardif et al. (2019). Further details of the LMR data assimilation procedure for pa-  
100 leoclimate reconstruction may be found in Hakim et al. (2016).

101 This study utilizes a lightweight implementation of the LMR framework, LMRt (Zhu  
102 et al., 2019). As a benchmark, a reconstruction of the spatiotemporal variations of sur-  
103 face temperature over Common Era is conducted, using iCESM as the model prior and  
104 the PAGES 2k network as observations. As expected, the DA procedure yields a sub-  
105 stantially better estimate of the temporal variability in the temperature field than the  
106 prior, as quantified by the pointwise correlation (Fig. S2c, S2d). This reconstruction skill  
107 level is comparable to a previous implementation of LMR (Tardif et al., 2019), and sup-  
108 ported by the similarity between the reconstructed NHMT using both versions of the code  
109 (Fig. S2a). For a more in-depth evaluation of the LMR framework, see Tardif et al. (2019).

### 110 2.2 Simulated and instrumental temperature observations

111 In order to compare paleoclimate reconstructions to climate models, we consider  
112 simulations of past millennium climate from the following models: iCESM, as well as the  
113 PMIP3 models (Schmidt et al., 2012b; Braconnot et al., 2012), including CESM (Otto-  
114 Bliesner et al., 2015), BCC CSM1.1 (Wu et al., 2014), GISS-E2-R (Schmidt et al., 2006),  
115 HadCM3 (Gordon et al., 2000), IPSL-CM5A-LR (Dufresne et al., 2013), MIROC-ESM  
116 (Watanabe et al., 2011), MPI-ESM-P (Giorgetta et al., 2013), CSIRO (Rotstayn et al.,  
117 2012), CCSM4 (Landrum et al., 2012). For more details on each simulation, see Table  
118 S1.

119 We also use two sets of instrumental temperature observations, including the Berke-  
120 ley Earth instrumental temperature analysis (Rohde et al., 2013) and the Goddard In-  
121 stitute for Space Studies (GISS) Surface Temperature Analysis (GISTEMP) (Hansen et  
122 al., 2010). GISTEMP and the gridded precipitation dataset from the Global Precipita-



**Figure 1.** (a) Comparison between the volcanic forcing (Gao et al., 2008) used in the isotope-enabled Community Earth System Model (iCESM) simulation (Stevenson et al., 2019; Brady et al., 2019) and the eVolv2k version 3 Volcanic Stratospheric Sulfur Injection (VSSI) compilation (Toohey & Sigl, 2017). The triangles denote the selected 6 large events between 1400 and 1850 CE. (b) Superposed epoch analysis (SEA) on simulated and reconstructed temperature response to the 12 strongest volcanic eruptions since 1400 AD, reproduced from IPCC AR5 (Masson-Delmotte et al., 2013) Fig. 5.8b. (c) Superposed epoch analysis on annual Northern hemispheric mean temperature (NHMT) simulated by 9 GCMs Section 2.2, Table S1) and LMR reconstructions assimilating the whole network, the tree-ring network, the tree-ring width (TRW) network, and the maximum latewood density (MXD) network, respectively. The shading encompasses the 5% and 95% quantiles of the ensemble.

123 tion Climatology Centre (GPCC) (Schneider et al., 2014) are also used for PSM calibra-  
 124 tion in the bivariate framework of Tardif et al. (2019).

### 125 **2.3 Superposed epoch analysis (SEA)**

126 Superposed epoch analysis (SEA) (Haurwitz & Brier, 1981) is a frequently used  
 127 measure of temperature response to volcanic eruptions (Adams et al., 2003; Masson-Delmotte  
 128 et al., 2013; Rao et al., 2019). It consists of aligning temperature anomaly series to the  
 129 timing of volcanic eruptions within a fixed time window prior to and following the event,  
 130 and averaging these responses to estimate the typical response to eruptions. The IPCC  
 131 AR5 (Fig. 1b) considered the reconstructed temperature response to the 12 strongest  
 132 eruptions since 1400 AD. For our analysis, we selected 6 large and well-dated eruption  
 133 events over the years 1400-1850 CE that are consistent in timing in both the volcanic  
 134 forcing used in iCESM (Gao et al., 2008) and the most recent compilation of Volcanic  
 135 Stratospheric Sulfur Injection (VSSI) (Toohey & Sigl, 2017) (Fig. 1a). For further de-  
 136 tails, see Text S3. The LMR response to individual events is shown in Fig S10.

## 137 **3 Causes of the discrepancy**

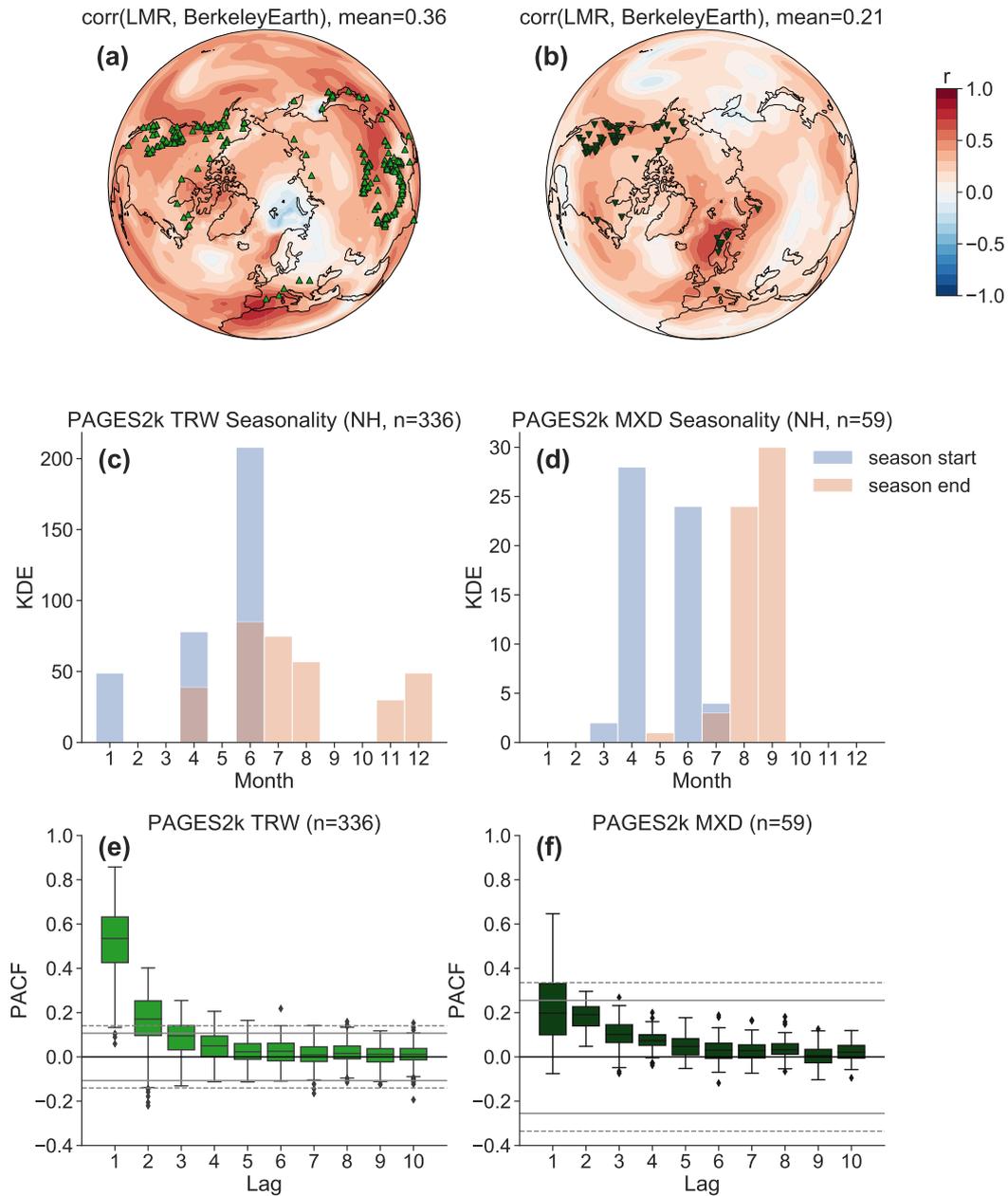
138 Fig. 1b highlights discrepancies between model simulations and reconstructions in  
 139 three aspects: (1) the magnitude of the peak cooling (2) the timing of the peak cooling  
 140 (3) the length of the recovery.

141 Specifically, model simulations show a stronger peak cooling amplitude, a slightly  
 142 earlier peak cooling, and a shorter recovery interval than the reconstructions. A simi-  
 143 lar discrepancy pattern can be seen in the LMR reconstruction assimilating the PAGES  
 144 2k network (Fig. 1c). Comparing results for assimilating the PAGES 2k network as a  
 145 whole (solid dark gray curve) to only its tree-ring records (dashed brown curve), we see  
 146 that the volcanic signal is indeed captured by the tree-ring network alone, which con-  
 147 sists of two main observation types: (1) tree-ring width (TRW) and (2) maximum late-  
 148 wood density (MXD). Assimilating these two proxy types, however, shows different re-  
 149 sponses to volcanism: TRW yields a lagged peak cooling year compared to a more pro-  
 150 longed recovery for MXD.

151 We investigate four factors that we hypothesize may account for these differences,  
 152 motivated by prior studies and existing knowledge of the tree-ring proxy network: (1)  
 153 spatial coverage (Anchukaitis et al., 2012; D’Arrigo et al., 2013) (2) seasonality (D’Arrigo  
 154 et al., 2006; Anchukaitis et al., 2017) (3) biological memory (Fritts, 1966; Krakauer &  
 155 Randerson, 2003; Frank et al., 2007; Esper et al., 2015; Zhang et al., 2015; Lücke et al.,  
 156 2019), and (4) non-temperature ‘noise’ (von Storch et al., 2004; Riedwyl et al., 2009; Neukom  
 157 et al., 2018).

### 158 **3.1 Spatial coverage of tree-ring proxies**

159 There are 336 TRW records and 59 MXD records over the Northern Hemisphere  
 160 (NH) in the PAGES 2k network. MXD records in PAGES2k are mainly limited to North  
 161 America and Scandinavia, while the TRW records cover both North America and Asia.  
 162 Evaluating the correlation between the LMR reconstruction and the Berkeley Earth in-  
 163 strumental temperature analysis (Rohde et al., 2013) over the instrumental era over 1880–  
 164 2000, we see that assimilating the TRW network yields a greater improvement over the  
 165 model prior than assimilating the MXD network (Fig 2a, 2b). Is this difference due to  
 166 the location or the quantity of each type of proxy record? To investigate this question,  
 167 we use a pseudoproxy experiment (PPE) (Smerdon, 2011). We set the annual iCESM  
 168 simulated temperature as our truth, and use it as model prior in the DA framework (a  
 169 “perfect model” scenario). Pseudoproxies are defined as perfect temperature recorders



**Figure 2.** Differences between PAGES 2k TRW and MXD records regarding (a, b) spatial coverage, (c, d) seasonality detected by the algorithm used in Tardif et al. (2019), and (e, f) biological memory quantified by the partial autocorrelation function (PACF). (a) The spatial coverage of TRW network. The color indicates the correlation between LMR reconstruction assimilating the TRW network and the Berkeley Earth instrumental temperature analysis (Rohde et al., 2013). (c) The optimal seasonality of the TRW network. (e) The PACF of the TRW network. (b), (d), and (f) are as (a), (b), and (e), respectively, but for the MXD network.

170 at three sets of locations: (1) all the 336 NH PAGES 2k TRW records (2) 50 records over  
 171 North America and (3) 50 records spread out throughout the NH.

172 The result of assimilating these three pseudoproxy networks is shown in Fig. S3  
 173 (a, b, and c), indicating that better spatial coverage yields a more accurate reconstruction  
 174 in the PDA framework, all other things being equal. This is reflected in SEA as well:  
 175 Fig. 3a shows that assimilating 50 records spread throughout the NH yields a stronger  
 176 and more accurate peak cooling amplitude than assimilating 50 records over North America,  
 177 suggesting that a broad spatial coverage is more important than the sheer number  
 178 of records for resolving peak cooling amplitude. Location does matter to some degree  
 179 with regard to the large-scale teleconnection patterns, and optimal placement could be  
 180 determined with the approach of Comboul et al. (2015), but this is beyond the scope of  
 181 this investigation.

### 182 **3.2 Seasonality**

183 An implicit assumption in reconstructing annual temperature with tree-ring proxies  
 184 is that growing season temperature is representative of annual temperature (PAGES  
 185 2k Consortium, 2017). However, the correlation between summer and annual temperatures  
 186 in the Northern Hemisphere is high for the oceans but relatively low over continents  
 187 (Fig. S3f), where the tree-ring records are located. Trees register climate primarily  
 188 during their growing season, which varies as a function geography, species, and climate  
 189 (Fritts, 1966; St. George, 2014; St George & Ault, 2014; Wilson, Anchukaitis, Briffa,  
 190 Büntgen, et al., 2016). Though the PAGES 2k metadata contain some information about  
 191 the seasonal sensitivity of all proxies, we follow Tardif et al. (2019) and identify optimal  
 192 (in a least square sense) seasonal windows for each proxy record. The start and end month  
 193 of the growing season thus identified are shown in Fig. 2c, 2d. While in the Northern  
 194 Hemisphere both TRW and MXD proxies record largely boreal summer conditions, the  
 195 optimal seasonality for TRW is often broader but typically less consistent than that for  
 196 MXD.

197 As before, we use a PPE to investigate the impact of growth seasonality on the temperature  
 198 reconstruction. We generate pseudoproxies as perfect recorders of local summer (JJA)  
 199 temperature and we perform experiments targeting both JJA temperature and annual  
 200 temperature. As expected, a much better reconstruction is obtained for the boreal  
 201 summer temperature field than annual temperature (Fig. S3d, S3e). This is also  
 202 evident in reconstructions using real proxies and instrumental temperature (Fig. S4).  
 203 In summary, summer-sensitive trees can only reconstruct annual temperature to the extent  
 204 that the summer and annual mean are correlated. While such seasonal effects result  
 205 in quite different assessments of reconstruction fidelity, this difference is hardly  
 206 noticeable in SEA (Fig. 3b).

### 207 **3.3 Biological memory**

208 Another important difference between TRW and MXD is biological memory, whereby  
 209 tree growth reflects the influence of climate in previous years (Fritts, 1966; Krakauer &  
 210 Randerson, 2003; Frank et al., 2007; Esper et al., 2015; Zhang et al., 2015). We  
 211 quantify the persistence in TRW and MXD in the PAGES2k using the partial autocorrelation  
 212 function (PACF) (Fig. 2e, 2f). As expected (Breitenmoser et al., 2012; Esper et al.,  
 213 2015; Lücke et al., 2019), we find that biological memory in TRW across the PAGES2k  
 214 network is large and significant for lag-1 and lag-2, while for MXD it is limited.

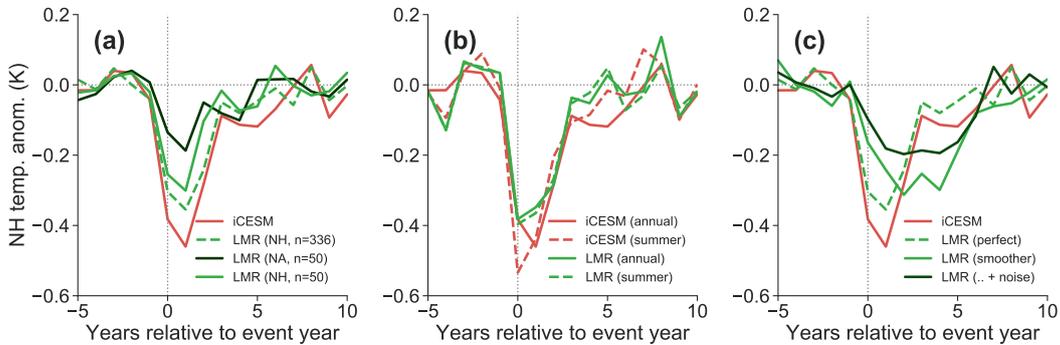
215 Comparing the proxy composites and the corresponding average instrumental temperature  
 216 at proxy locales, we see that the MXD composite captures contemporaneous  
 217 temperature variations, including the accurate timing of cooling events, while the TRW  
 218 composite appears to smooth interannual variability and integrate temperatures over 2

219 to 5 years (Fig. S5a, S5b), leading to lagged and persistent cooling events (Frank et al.,  
 220 2007).

221 To investigate the impact of such biological memory on the magnitude of recon-  
 222 structed volcanic cooling, we again turn to PPEs. We simulate a short-term memory ef-  
 223 fect in ring width by now designing TRW pseudoproxies as a 5-yr moving average of the  
 224 annual temperature simulated by iCESM, as shown in Fig. S5c. Assimilating these ideal-  
 225 ized smoothed pseudoproxies yields a prolonged temperature recovery and a peak cool-  
 226 ing that is both damped and lagged (Fig. 3c, the solid light green curve). We find that  
 227 this overall result is not sensitive to the precise design of the filter used to construct the  
 228 smoothed pseudoproxies, so long as it captures this multiple year climate integration in  
 229 some way.

230 **3.4 Proxy system noise**

231 So far, our PPEs have assumed nearly noiseless temperature recorders for simplic-  
 232 ity (a signal-to-noise ratio (SNR) of infinity, wherein SNR is defined as the ratio of the  
 233 standard deviation of signal and that of noise, following existing practice (Smerdon, 2011)).  
 234 In reality, of course, proxies are imperfect recorders of climate conditions. To make the  
 235 PPE more realistic, we now add uncorrelated Gaussian white noise into the previously  
 236 described pseudo-TRW records. Using a linear regression procedure (Fig. S6), we esti-  
 237 mate a SNR of 0.3, comparable to the estimate of Wang et al. (2014). Since we have al-  
 238 ready emulated the biological memory utilizing the moving average filter, we consider  
 239 white noise instead of red noise to avoid adding more memory into the pseudoproxies.  
 240 The addition of noise to the previous case yields a more similar SEA pattern to the real-  
 241 world case (Fig. 3c, solid dark green curve): a more damped and prolonged recovery com-  
 242 pared to the noiseless case.



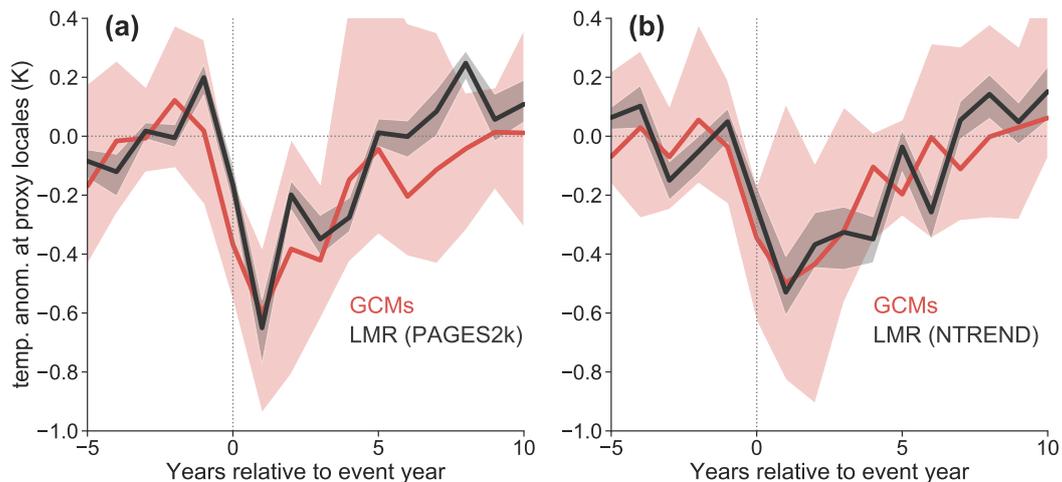
**Figure 3. SEA in pseudoproxy experiments, evaluating the impact of (a) spatial coverage, (b) seasonality, and (c) biological memory and noise.** (a) the red curve indicates the target, and the dashed light green curve, the solid dark green curve, and the solid light green curve indicate the LMR reconstruction assimilating 336 pseudo-TRW records over the NH, 50 records over North America, and 50 records over the NH, respectively. (b) The solid red curve denotes the annual target, the dashed red curve indicates the boreal summer target, and the green curves indicate the LMR annual and summer reconstructions, respectively. (c) The solid red curve indicates the annual target, and the green curves indicate the LMR reconstruction assimilating pseudo-TRW as perfect temperature recorders (dashed), as temperature smoothers (solid), and the temperature smoother with Gaussian noise superposed with a signal-to-noise ratio as 0.3 (dark solid).

243 Considering the four factors above, we are thus able to simulate the observed dis-  
 244 crepancy between simulated and reconstructed NH temperature response to volcanic erup-  
 245 tions. Can this knowledge be used to minimize this discrepancy?

### 246 3.5 Reconciling the model–proxy discrepancy

247 In the present context, noise in proxies reflects non-temperature influence on their  
 248 formation, including biophysical processes and other climate influences, which we are not  
 249 able to model properly due to lack of scientific understanding, lack of site-level calibra-  
 250 tion data, or other practical concerns (e.g., computational efficiency). The other factors  
 251 can, however, be corrected for: to account for the limited spatial coverage, we perform  
 252 SEA at proxy locations instead of the whole NH; to minimize the seasonal bias, we tar-  
 253 get boreal summer temperature instead of annual temperature; and to mitigate mem-  
 254 ory effects, we assimilate MXD records only, leaving out TRW and mixed chronologies.

255 As a result, we are able to almost entirely account for the proxy–model discrep-  
 256 ancy in Fig. 1 with the PAGES 2k network (Fig. 4a, Fig S11). The same strategy can  
 257 be used for other proxy networks. For comparison, applying it to the NTREND network  
 258 (Wilson, Anchukaitis, Briffa, Büntgen, et al., 2016; Anchukaitis et al., 2017) (Fig. S7)  
 259 yields similar agreement between simulated and reconstructed temperature (Fig. 4b, Fig  
 260 S12). These results stand in sharp contrast to results where spatial coverage, seasonal-  
 261 ity, and biological memory are not taken into account (Fig. S8).



**Figure 4.** (a) Same as Fig. 1c, after resolving differences in the model and proxy domains associated with seasonality, spatial distribution, and biological memory. (b) Same as (a) but using the NTREND MXD network. A version of this figure showing each model simulation is available in Fig. S9, and one using more eruption events is available in Fig. S13

262 That the discrepancy of Fig. 1b can be largely reconciled by accounting for known  
 263 characteristics of the proxy data is reassuring, and bodes well for using volcanic erup-  
 264 tions of the past millennium as a test bed for climate models. We now discuss the broader  
 265 implications of this result.

## 4 Discussion

Using recent proxy compilations and climate field reconstruction techniques, we have showed that it is possible to largely resolve the discrepancy between the simulated and reconstructed temperature response to explosive volcanism since 1600 CE. We find that this gap was the result of four main factors: spatial coverage, proxy seasonality, biological memory, and proxy noise. While proxy noise is difficult to account for in model-data intercomparisons, the first three factors can be, if care is taken in evaluating comparable quantities. In particular, since our reconstructions are more reliable at locations where proxy are available than at distal locations (Anchukaitis et al., 2017), carrying out the comparison at proxy sites is a simple and effective way to reduce the mismatch. That this is true even in the data assimilation framework (Steiger et al., 2014) suggests that expanding the spatial extent of proxy network is necessary to resolve global-scale patterns.

Previous studies have argued that the simplified representation of the radiative effects of stratospheric aerosols common to CMIP5-era GCMs can produce overly strong responses to volcanic forcing (Timmreck et al., 2009; Timmreck, 2012; Stoffel et al., 2015; LeGrande et al., 2016). This is due in part to the modeled stratospheric aerosol microphysics not including the self-limiting processes known to operate at large sulfate concentrations (Timmreck et al., 2009). Uncertainties in the timing, location, and magnitude of volcanic forcing itself can also greatly affect the simulated response, independently of simplifications to the model physics. Progress in representing this forcing (Toohey & Sigl, 2017; Aubry et al., 2019), as well as improvements in model resolution and processes (e.g. active stratospheric chemistry) in PMIP4 (Kageyama et al., 2018), may lead to closer model-data matches in future work. Regardless of these factors, our analysis suggests that a critical ingredient of minimizing the model-reconstruction mismatch is to evaluate simulated temperature at the times and places where it is recorded by the proxy sensors.

Naturally, reconstructions may be improved as well. While this study has focused on the uncertainties in proxy measurements in the context of paleoenvironmental data assimilation, more work should be done to reduce sources of uncertainty within the data assimilation method itself, such as the forward operator error, the model prior, and the localization scheme, as the coupling of all these uncertainty sources can potentially affect the SEA comparison. In particular, forward operators that allow for non-contemporaneous influences of the state on the proxies (e.g. time-integration, as is believed to be the case for TRW (Vaganov et al., 2006; Anchukaitis et al., 2006)) would enable us to make better use of the information contained in TRW records. While such process-oriented models have been proposed (Tolwinski-Ward et al., 2011), their application to the DA context is contingent upon accurate specification of observation error variance and correcting for biases in the model prior. Both tasks remain active research areas (Dee et al., 2016).

With regard to proxies, we have shown that the lagged cooling exhibited in previous reconstructions can be explained as the consequence of using TRW records. Other proxies that integrate climate information over multiple years likely have a similar impact in multiproxy reconstructions. Since MXD records are more faithful paleo-temperature sensors than TRW records (Esper et al., 2015, 2018), we call here for increased collection and development of MXD records (St. George & Esper, 2019), particularly at locations where they are presently absent or cover only part of the last millennium, e.g. the North American treeline and at high elevations in Asia (Anchukaitis et al., 2017; Esper et al., 2018).

That the LMR-reconstructed boreal summer temperature at proxy locations lies within the range of simulated responses (Fig. 4) suggests that, based on this metric alone, there is no strong evidence that GCMs from the PMIP3 and CESM Last Millennium En-

semble taken as a whole systematically overestimate the climate response to explosive volcanism since 1600 CE. Nonetheless, we also find evidence that the model response is larger than the reconstructed response (Fig S11, S12). In the presence of noise, statistical reconstructions are inevitably damped because of regression dilution (Frost & Thompson, 2000; Wang et al., 2015; Neukom et al., 2018), a caveat that applies to LMR as well, to the extent that it uses regression-based forward operators to translate climate states to proxy values. Here we have mitigated this problem by focusing on the recent period with relatively high proxy coverage, but it is undoubtedly an ingredient in the mismatch observed for earlier eruptions. Indeed some of the largest documented discrepancies in the magnitude of peak cooling are for earlier eruptions like 1257 (Samalas) (Lavigne et al., 2013; Wilson, Anchukaitis, Briffa, Büntgen, et al., 2016), with its extremely large inferred forcing (Timmreck et al., 2009) and proportionally large response, which far exceeds what is seen in existing reconstructions (Fig. S10-S12, (Stoffel et al., 2015)). There is also lingering uncertainty as to the magnitude, timing, and location of two major events during the 1450s (Sigl et al., 2015; Toohey & Sigl, 2017; Hartman et al., 2019). These earlier and quite large eruptions register as the largest sulfate depositions of the past millennium ( $59.42 \pm 10.86$  Tg in 1258 CE and  $32.98 \pm 4.8$  Tg in 1458 CE, according to Toohey and Sigl (2017)), but are not clearly expressed in our reconstructions (Figs. S11–12). Nonetheless, the composite changes very little when these and weaker events are included (Fig S13).

The key contribution of this work is to demonstrate that it is possible to largely resolve most of the discrepancies between simulated and reconstructed responses to volcanic cooling by explicitly accounting for the characteristics of the proxy network in this comparison. The agreement over the past 400 years, while comforting, is a rather mild test of model performance. Indeed, these eruptions, while larger than the 1991 Pinatubo eruption used to calibrate radiative forcing (Gao et al., 2008; LeGrande et al., 2016), are relatively small compared to the recorded range of the past 2,500 years (Sigl et al., 2015). Thus, parameterizations based on Pinatubo scaling between sulfate aerosols and radiative forcing would be expected to be relatively accurate for these events, though they might not be for larger eruptions. In addition, the last 400 years are more data-rich than earlier periods (Figures S1, S7), leading to relatively well-constrained reconstructions. As we explore earlier, larger eruptions, proxy attrition and its attendant bias in the spatial sampling of volcanic cooling episodes leads to wider differences between simulations and reconstructions. Only with denser observational coverage will this comparison become more informative of model performance.

### Acknowledgments

The authors acknowledge support from the Climate Program Office of the National Oceanographic and Atmospheric Administration (grants NA18OAR4310426 to USC, NA18OAR4310422 to UW, and NA18OAR4310420 to UA) GJH also acknowledges support from the NSF through grant AGS0–1702423. Code and data are available at <https://github.com/fzhu2e/lmrvolc> (a placeholder for now, to be filled upon paper acceptance).

### References

- Adams, J., Mann, M. E., & Ammann, C. M. (2003, November). Proxy evidence for an El Niño-like response to volcanic forcing. *Nature*, *426*(6964), 274–278. doi: 10.1038/nature02101
- Anchukaitis, K. J., Breitenmoser, P., Briffa, K. R., Buchwal, A., Buntgen, U., Cook, E. R., ... Wilson, R. J. S. (2012, 12). Tree rings and volcanic cooling. *Nature Geosci*, *5*(12), 836–837.
- Anchukaitis, K. J., Evans, M. N., Kaplan, A., Vaganov, E. A., Hughes, M. K., Grissino-Mayer, H. D., & Cane, M. A. (2006, February). Forward modeling of regional scale tree-ring patterns in the southeastern United States and

- 369 the recent influence of summer drought. *Geophys. Res. Lett.*, *33*, L04705. doi:  
370 10.1029/2005GL025050
- 371 Anchukaitis, K. J., Wilson, R., Briffa, K. R., Büntgen, U., Cook, E. R., D'Arrigo,  
372 R., ... Zorita, E. (2017, 5 1). Last millennium Northern Hemisphere summer  
373 summer temperatures from tree rings: Part II, spatially resolved reconstructions.  
374 *Quaternary Science Reviews*, *163*, 1–22. doi: 10.1016/j.quascirev.2017.02.020
- 375 Aubry, T. J., Toohey, M., Marshall, L., Schmidt, A., & Jellinek, A. M. (2019). A  
376 new volcanic stratospheric sulfate aerosol forcing emulator (eva\_h): Compar-  
377 ison with interactive stratospheric aerosol models. *Journal of Geophysical*  
378 *Research: Atmospheres*, *n/a(n/a)*. doi: 10.1029/2019JD031303
- 379 Braconnot, P., Harrison, S. P., Kageyama, M., Bartlein, P. J., Masson-Delmotte,  
380 V., Abe-Ouchi, A., ... Zhao, Y. (2012, June). Evaluation of climate mod-  
381 els using palaeoclimatic data. *Nature Climate Change*, *2*(6), 417–424. doi:  
382 10.1038/nclimate1456
- 383 Brady, E., Stevenson, S., Bailey, D., Liu, Z., Noone, D., Nusbaumer, J., ... Zhu, J.  
384 (2019). The Connected Isotopic Water Cycle in the Community Earth Sys-  
385 tem Model Version 1. *Journal of Advances in Modeling Earth Systems*, *11*(8),  
386 2547–2566. doi: 10.1029/2019MS001663
- 387 Breitenmoser, P., Beer, J., Brönnimann, S., Frank, D., Steinhilber, F., & Wanner,  
388 H. (2012, January). Solar and volcanic fingerprints in tree-ring chronologies  
389 over the past 2000years. *Palaeogeography, Palaeoclimatology, Palaeoecology*,  
390 *313–314*, 127–139. doi: 10.1016/j.palaeo.2011.10.014
- 391 Comboul, M., Emile-Geay, J., Hakim, G. J., & Evans, M. N. (2015). Paleoclimate  
392 sampling as a sensor placement problem. *Journal of Climate*, *28*, 7717–7740.  
393 doi: 10.1175/JCLI-D-14-00802.1
- 394 D'Arrigo, R., Wilson, R., & Anchukaitis, K. J. (2013). Volcanic cooling signal in  
395 tree ring temperature records for the past millennium. *Journal of Geophysical*  
396 *Research-Atmospheres*, *118*(16), 9000-9010. doi: {10.1002/jgrd.50692}
- 397 D'Arrigo, R., Wilson, R., & Jacoby, G. (2006). On the long-term context for late  
398 twentieth century warming. *Journal of Geophysical Research: Atmospheres*,  
399 *111*(D3). doi: 10.1029/2005JD006352
- 400 Dee, S. G., Steiger, N. J., Emile-Geay, J., & Hakim, G. J. (2016). On the utility of  
401 proxy system models for estimating climate states over the common era. *Jour-*  
402 *nal of Advances in Modeling Earth Systems*, *8*. doi: 10.1002/2016MS000677
- 403 Dufresne, J.-L., Foujols, M.-A., Denvil, S., Caubel, A., Marti, O., Aumont, O., ...  
404 Vuichard, N. (2013, May). Climate change projections using the IPSL-CM5  
405 Earth System Model: from CMIP3 to CMIP5. *Climate Dynamics*, *40*(9-10),  
406 2123–2165. doi: 10.1007/s00382-012-1636-1
- 407 Esper, J., George, S. S., Anchukaitis, K., D'Arrigo, R., Ljungqvist, F. C., Luter-  
408 bacher, J., ... Büntgen, U. (2018). Large-scale, millennial-length temperature  
409 reconstructions from tree-rings. *Dendrochronologia*, *50*, 81–90.
- 410 Esper, J., Schneider, L., Smerdon, J. E., Schöne, B. R., & Büntgen, U. (2015,  
411 October). Signals and memory in tree-ring width and density data. *Den-*  
412 *drochronologia*, *35*, 62–70. doi: 10.1016/j.dendro.2015.07.001
- 413 Frank, D., Büntgen, U., Böhm, R., Maugeri, M., & Esper, J. (2007, December).  
414 Warmer early instrumental measurements versus colder reconstructed tem-  
415 peratures: shooting at a moving target. *Quaternary Science Reviews*, *26*(25),  
416 3298–3310. doi: 10.1016/j.quascirev.2007.08.002
- 417 Fritts, H. C. (1966). Growth-rings of trees: their correlation with climate. *Science*,  
418 *154*(3752), 973–979.
- 419 Frost, C., & Thompson, S. G. (2000). Correcting for regression dilution bias: com-  
420 parison of methods for a single predictor variable. *Journal of the Royal Statis-*  
421 *tical Society: Series A (Statistics in Society)*, *163*(2), 173–189. doi: 10.1111/  
422 1467-985X.00164
- 423 Gao, C., Robock, A., & Ammann, C. (2008). Volcanic forcing of climate over

- 424 the past 1500 years: An improved ice core-based index for climate mod-  
 425 els. *Journal of Geophysical Research: Atmospheres*, 113(D23). doi:  
 426 10.1029/2008JD010239
- 427 Giorgetta, M. A., Jungclaus, J., Reick, C. H., Legutke, S., Bader, J., Böttinger,  
 428 M., ... Stevens, B. (2013). Climate and carbon cycle changes from 1850 to  
 429 2100 in MPI-ESM simulations for the Coupled Model Intercomparison Project  
 430 phase 5. *Journal of Advances in Modeling Earth Systems*, 5(3), 572–597. doi:  
 431 10.1002/jame.20038
- 432 Gordon, C., Cooper, C., Senior, C. A., Banks, H., Gregory, J. M., Johns, T. C.,  
 433 ... Wood, R. A. (2000, February). The simulation of SST, sea ice ex-  
 434 tents and ocean heat transports in a version of the Hadley Centre coupled  
 435 model without flux adjustments. *Climate Dynamics*, 16(2-3), 147–168. doi:  
 436 10.1007/s003820050010
- 437 Hakim, G. J., Emile-Geay, J., Steig, E. J., Noone, D., Anderson, D. M., Tardif, R.,  
 438 ... Perkins, W. A. (2016). The last millennium climate reanalysis project:  
 439 Framework and first results. *Journal of Geophysical Research: Atmospheres*,  
 440 121, 6745 – 6764. doi: 10.1002/2016JD024751
- 441 Hansen, J., Ruedy, R., Sato, M., & Lo, K. (2010). Global surface temperature  
 442 change. *Rev. Geophys.*, 48, RG4004. doi: 10.1029/2010RG000345
- 443 Hartman, L. H., Kurbatov, A. V., Winski, D. A., Cruz-Uribe, A. M., Davies, S. M.,  
 444 Dunbar, N. W., ... Yates, M. G. (2019). Volcanic glass properties from 1459  
 445 c.e. volcanic event in south pole ice core dismiss kuwae caldera as a potential  
 446 source. *Scientific Reports*, 9(1), 14437. doi: 10.1038/s41598-019-50939-x
- 447 Haurwitz, M. W., & Brier, G. W. (1981, October). A Critique of the Superposed  
 448 Epoch Analysis Method: Its Application to Solar–Weather Relations. *Monthly*  
 449 *Weather Review*, 109(10), 2074–2079. doi: 10.1175/1520-0493(1981)109<2074:  
 450 ACOTSE>2.0.CO;2
- 451 Kageyama, M., Braconnot, P., Harrison, S. P., Haywood, A. M., Jungclaus, J. H.,  
 452 Otto-Bliesner, B. L., ... Zhou, T. (2018, March). The PMIP4 contribution  
 453 to CMIP6 – Part 1: Overview and over-arching analysis plan. *Geoscientific*  
 454 *Model Development*, 11(3), 1033–1057. doi: https://doi.org/10.5194/  
 455 gmd-11-1033-2018
- 456 Krakauer, N. Y., & Randerson, J. T. (2003). Do volcanic eruptions enhance or di-  
 457 minish net primary production? Evidence from tree rings. *Global Biogeochemi-*  
 458 *cal Cycles*, 17(4). doi: 10.1029/2003GB002076
- 459 Landrum, L., Otto-Bliesner, B. L., Wahl, E. R., Conley, A., Lawrence, P. J.,  
 460 Rosenbloom, N., & Teng, H. (2012, 2014/05/05). Last millennium climate  
 461 and its variability in cesm4. *Journal of Climate*, 26(4), 1085–1111. doi:  
 462 10.1175/JCLI-D-11-00326.1
- 463 Lavigne, F., Degeai, J.-P., Komorowski, J.-C., Guillet, S., Robert, V., Lahitte,  
 464 P., ... de Belizal, E. (2013). Source of the great a.d. 1257 mystery erup-  
 465 tion unveiled, samalas volcano, rinjani volcanic complex, indonesia. *Pro-*  
 466 *ceedings of the National Academy of Sciences*, 110(42), 16742-16747. doi:  
 467 10.1073/pnas.1307520110
- 468 LeGrande, A. N., & Anchukaitis, K. J. (2015). Volcanic eruptions and climate.  
 469 *PAGES Magazine*, 23(2), 46–47.
- 470 LeGrande, A. N., Tsigaridis, K., & Bauer, S. E. (2016, September). Role of atmo-  
 471 spheric chemistry in the climate impacts of stratospheric volcanic injections.  
 472 *Nature Geoscience*, 9(9), 652–655. doi: 10.1038/ngeo2771
- 473 Lücke, L., Hegerl, G., Schurer, A., & Wilson, R. (2019, September). Effects of mem-  
 474 ory biases on variability of temperature reconstructions. *Journal of Climate*.  
 475 doi: 10.1175/JCLI-D-19-0184.1
- 476 Masson-Delmotte, V., Schulz, M., Abe-Ouchi, A., Beer, J., Ganopolski, A., Rouco,  
 477 J. G., ... Timmermann, A. (2013). Information from Paleoclimate Archives.  
 478 In T. F. Stocker et al. (Eds.), *Climate Change 2013: The Physical Science*

- 479 *Basis. Contribution of Working Group I to the Fifth Assessment Report of*  
 480 *the Intergovernmental Panel on Climate Change* (pp. 383–464). Cambridge,  
 481 United Kingdom and New York, NY, USA: Cambridge University Press. doi:  
 482 10.1017/CBO9781107415324.013
- 483 Neukom, R., Schurer, A. P., Steiger, N. J., & Hegerl, G. C. (2018, May). Possi-  
 484 ble causes of data model discrepancy in the temperature history of the last  
 485 Millennium. *Scientific Reports*, *8*(1), 1–15. doi: 10.1038/s41598-018-25862-2
- 486 Otto-Bliesner, B. L., Brady, E. C., Fasullo, J., Jahn, A., Landrum, L., Stevenson, S.,  
 487 ... Strand, G. (2015). Climate variability and change since 850 CE: An ensem-  
 488 ble approach with the community earth system model. *Bull. Amer. Meteor.*  
 489 *Soc.*, *97*(5), 735–754. doi: 10.1175/BAMS-D-14-00233.1
- 490 PAGES 2k Consortium. (2017, 07). A global multiproxy database for temperature  
 491 reconstructions of the Common Era. *Scientific Data*, *4*, 170088 EP. doi: 10  
 492 .1038/sdata.2017.88
- 493 Rao, M. P., Cook, E. R., Cook, B. I., Anchukaitis, K. J., D’Arrigo, R. D., Krusic,  
 494 P. J., & LeGrande, A. N. (2019). A double bootstrap approach to Super-  
 495 posed Epoch Analysis to evaluate response uncertainty. *Dendrochronologia*, *55*,  
 496 119–124.
- 497 Riedwyl, N., Küttel, M., Luterbacher, J., & Wanner, H. (2009). Comparison of cli-  
 498 mate field reconstruction techniques: Application to Europe. *Climate Dynam-*  
 499 *ics*, *32*(2-3), 381–395.
- 500 Robock, A. (2000). Volcanic eruptions and climate. *Rev. Geophys.*, *38*, 191-220. doi:  
 501 10.1029/1998RG000054
- 502 Rohde, R., Muller, R., Jacobsen, R., Perlmutter, S., Rosenfeld, A., Wurtele, J., ...  
 503 Mosher, S. (2013). Berkeley Earth Temperature Averaging Process. *Geoinfor-*  
 504 *matics & Geostatistics: An Overview, 2013*. doi: 10.4172/2327-4581.1000103
- 505 Rotstayn, L. D., Jeffrey, S. J., Collier, M. A., Dravitzki, S. M., Hirst, A. C., Syk-  
 506 tus, J. I., & Wong, K. K. (2012, July). Aerosol- and greenhouse gas-induced  
 507 changes in summer rainfall and circulation in the Australasian region: a study  
 508 using single-forcing climate simulations. *Atmos. Chem. Phys.*, *12*(14), 6377–  
 509 6404. doi: 10.5194/acp-12-6377-2012
- 510 Schmidt, G. A., Jungclaus, J. H., Ammann, C. M., Bard, E., Braconnot, P., Crow-  
 511 ley, T. J., ... Vieira, L. E. A. (2012a). Climate forcing reconstructions for  
 512 use in pmip simulations of the last millennium (v1.1). *Geoscientific Model*  
 513 *Development*, *5*(1), 185–191. doi: 10.5194/gmd-5-185-2012
- 514 Schmidt, G. A., Jungclaus, J. H., Ammann, C. M., Bard, E., Braconnot, P., Crow-  
 515 ley, T. J., ... Vieira, L. E. A. (2012b, January). Climate forcing reconstructions  
 516 for use in PMIP simulations of the Last Millennium (v1.1). *Geosci. Model*  
 517 *Dev.*, *5*(1), 185–191. doi: 10.5194/gmd-5-185-2012
- 518 Schmidt, G. A., Ruedy, R., Hansen, J. E., Aleinov, I., Bell, N., Bauer, M., ... Yao,  
 519 M.-S. (2006, January). Present-Day Atmospheric Simulations Using GISS  
 520 ModelE: Comparison to In Situ, Satellite, and Reanalysis Data. *Journal of*  
 521 *Climate*, *19*(2), 153–192. doi: 10.1175/JCLI3612.1
- 522 Schneider, D. P., Ammann, C. M., Otto-Bliesner, B. L., & Kaufman, D. S. (2009).  
 523 Climate response to large, high-latitude and low-latitude volcanic eruptions  
 524 in the Community Climate System Model. *Journal of Geophysical Research:*  
 525 *Atmospheres*, *114*(D15). doi: 10.1029/2008JD011222
- 526 Schneider, U., Becker, A., Finger, P., Meyer-Christoffer, A., Ziese, M., & Rudolf,  
 527 B. (2014, January). GPCP’s new land surface precipitation climatol-  
 528 ogy based on quality-controlled in situ data and its role in quantifying the  
 529 global water cycle. *Theoretical and Applied Climatology*, *115*(1), 15–40. doi:  
 530 10.1007/s00704-013-0860-x
- 531 Schurer, A. P., Hegerl, G. C., Mann, M. E., Tett, S. F., & Phipps, S. J. (2013). Sep-  
 532 arating forced from chaotic climate variability over the past millennium. *Jour-*  
 533 *nal of Climate*, *26*(18), 6954–6973.

- 534 Sigl, M., Winstrup, M., McConnell, J. R., Welten, K. C., Plunkett, G., Ludlow,  
535 F., ... Woodruff, T. E. (2015, 07 30). Timing and climate forcing of volcanic  
536 eruptions for the past 2,500 years. *Nature*, *523*(7562), 543–549.
- 537 Smerdon, J. E. (2011). Climate models as a test bed for climate reconstruction  
538 methods: pseudoproxy experiments. *WIREs Clim Change*. doi: 10.1002/wcc  
539 .149
- 540 Soden, B. J., Wetherald, R. T., Stenchikov, G. L., & Robock, A. (2002). Global  
541 Cooling After the Eruption of Mount Pinatubo: A Test of Climate Feedback  
542 by Water Vapor. *Science*, *296*(5568), 727–730.
- 543 St. George, S. (2014). An overview of tree-ring width records across the North-  
544 ern Hemisphere. *Quaternary Science Reviews*, *95*, 132–150. doi: 10.1016/j  
545 .quascirev.2014.04.029
- 546 St George, S., & Ault, T. R. (2014). The imprint of climate within Northern Hemi-  
547 sphere trees. *Quaternary Science Reviews*, *89*, 1–4.
- 548 Steiger, N. J., Hakim, G. J., Steig, E. J., Battisti, D. S., & Roe, G. H. (2014,  
549 2014/04/08). Assimilation of time-averaged pseudoproxies for climate re-  
550 construction. *Journal of Climate*, *27*(1), 426–441. doi: 10.1175/JCLI-D-12  
551 -00693.1
- 552 Stevenson, S., Fasullo, J. T., Otto-Bliesner, B. L., Tomas, R. A., & Gao, C. (2017).  
553 Role of eruption season in reconciling model and proxy responses to tropical  
554 volcanism. *Proceedings of the National Academy of Sciences*, *114*(8), 1822–  
555 1826. doi: 10.1073/pnas.1612505114
- 556 Stevenson, S., Otto-Bliesner, B. L., Brady, E. C., Nusbaumer, J., Tabor, C., Tomas,  
557 R., ... Liu, Z. (2019). Volcanic Eruption Signatures in the Isotope-Enabled  
558 Last Millennium Ensemble. *Paleoceanography and Paleoclimatology*, *0*(0). doi:  
559 10.1029/2019PA003625
- 560 St. George, S., & Esper, J. (2019, January). Concord and discord among Northern  
561 Hemisphere paleotemperature reconstructions from tree rings. *Quaternary Sci-  
562 ence Reviews*, *203*, 278–281. doi: 10.1016/j.quascirev.2018.11.013
- 563 Stoffel, M., Khodri, M., Corona, C., Guillet, S., Poulain, V., Bekki, S., ... Masson-  
564 Delmotte, V. (2015, October). Estimates of volcanic-induced cooling in the  
565 Northern Hemisphere over the past 1,500 years. *Nature Geoscience*, *8*(10),  
566 784–788. doi: 10.1038/ngeo2526
- 567 Tardif, R., Hakim, G. J., Perkins, W. A., Horlick, K. A., Erb, M. P., Emile-Geay,  
568 J., ... Noone, D. (2019, July). Last Millennium Reanalysis with an expanded  
569 proxy database and seasonal proxy modeling. *Climate of the Past*, *15*(4),  
570 1251–1273. doi: https://doi.org/10.5194/cp-15-1251-2019
- 571 Timmreck, C. (2012). Modeling the climatic effects of large explosive volcanic erup-  
572 tions. *Wiley Interdisciplinary Reviews: Climate Change*, *3*(6), 545–564. doi: 10  
573 .1002/wcc.192
- 574 Timmreck, C., Lorenz, S. J., Crowley, T. J., Kinne, S., Raddatz, T. J., Thomas,  
575 M. A., & Jungclaus, J. H. (2009). Limited temperature response to the very  
576 large AD 1258 volcanic eruption. *Geophysical Research Letters*, *36*(21). doi:  
577 10.1029/2009GL040083
- 578 Tolwinski-Ward, S. E., Evans, M. N., Hughes, M. K., & Anchukaitis, K. J. (2011).  
579 An efficient forward model of the climate controls on interannual varia-  
580 tion in tree-ring width. *Climate Dynamics*, *36*(11-12), 2419–2439. doi:  
581 10.1007/s00382-010-0945-5
- 582 Toohey, M., & Sigl, M. (2017, November). Volcanic stratospheric sulfur injections  
583 and aerosol optical depth from 500 BCE to 1900 CE. *Earth System Science  
584 Data*, *9*(2), 809–831. doi: https://doi.org/10.5194/essd-9-809-2017
- 585 Vaganov, E. A., Hughes, M. K., & Shashkin, A. V. (2006). *Growth dynamics of  
586 conifer tree rings* (Vol. 183). New York, NY: Springer-Verlag.
- 587 von Storch, H., Zorita, E., Jones, J. M., Dimitriev, Y., González-Rouco, F., & Tett,  
588 S. F. B. (2004, October). Reconstructing Past Climate from Noisy Data.

- 589 *Science*, 306, 679–682. doi: 10.1126/science.1096109
- 590 Wang, J., Emile-Geay, J., Guillot, D., McKay, N. P., & Rajaratnam, B. (2015).  
 591 Fragility of reconstructed temperature patterns over the common era: Implica-  
 592 tions for model evaluation. *Geophysical Research Letters*, 42, 7162–7170. doi:  
 593 10.1002/2015GL065265
- 594 Wang, J., Emile-Geay, J., Guillot, D., Smerdon, J. E., & Rajaratnam, B. (2014).  
 595 Evaluating climate field reconstruction techniques using improved emu-  
 596 lations of real-world conditions. *Climate of the Past*, 10(1), 1–19. doi:  
 597 10.5194/cp-10-1-2014
- 598 Watanabe, S., Hajima, T., Sudo, K., Nagashima, T., Takemura, T., Okajima, H., ...  
 599 Kawamiya, M. (2011, January). MIROC-ESM 2010: Model description and  
 600 basic results of CMIP5-20c3m experiments. *Geoscientific Model Development*,  
 601 4(4), 845–872. doi: 10.5194/gmd-4-845-2011
- 602 Wilson, R., Anchukaitis, K., Briffa, K. R., Büntgen, U., Cook, E., D’Arrigo, R., ...  
 603 Zorita, E. (2016, February). Last millennium northern hemisphere summer  
 604 temperatures from tree rings: Part I: The long term context. *Quaternary*  
 605 *Science Reviews*, 134, 1–18. doi: 10.1016/j.quascirev.2015.12.005
- 606 Wilson, R., Anchukaitis, K., Briffa, K. R., Büntgen, U., Cook, E., D’Arrigo, R., ...  
 607 Zorita, E. (2016, 2 15). Last millennium northern hemisphere summer tem-  
 608 peratures from tree rings: Part I: The long term context. *Quaternary Science*  
 609 *Reviews*, 134, 1–18. doi: 10.1016/j.quascirev.2015.12.005
- 610 Wu, T., Song, L., Li, W., Wang, Z., Zhang, H., Xin, X., ... Zhou, M. (2014, Febru-  
 611 ary). An overview of BCC climate system model development and application  
 612 for climate change studies. *Journal of Meteorological Research*, 28(1), 34–56.  
 613 doi: 10.1007/s13351-014-3041-7
- 614 Zhang, H., Yuan, N., Esper, J., Werner, J. P., Xoplaki, E., Büntgen, U., ... Luter-  
 615 bacher, J. (2015, August). Modified climate with long term memory in  
 616 tree ring proxies. *Environmental Research Letters*, 10(8), 084020. doi:  
 617 10.1088/1748-9326/10/8/084020
- 618 Zhu, F., Emile-Geay, J., Hakim, G. J., Tardif, R., & Perkins, A. (2019, December).  
 619 *LMR Turbo (LMRt): a lightweight implementation of the LMR framework*.  
 620 Zenodo. doi: 10.5281/zenodo.3590258