

# Consecutive Ruptures on a Complex Conjugate Fault System During the 2018 Gulf of Alaska Earthquake

Shinji Yamashita<sup>1, \*</sup>, Yuji Yagi<sup>2, \*\*</sup>, Ryo Okuwaki<sup>2, 3, 4</sup>, Kousuke Shimizu<sup>1</sup>, Ryoichiro Agata<sup>5</sup>, and Yukitoshi Fukahata<sup>6</sup>

<sup>1</sup>Graduate School of Life and Environmental Sciences, University of Tsukuba, Tsukuba, Ibaraki 305-8572, Japan

<sup>2</sup>Faculty of Life and Environmental Sciences, University of Tsukuba, Tsukuba, Ibaraki 305-8572, Japan

<sup>3</sup>Mountain Science Center, University of Tsukuba, Ibaraki 305-8572, Japan

<sup>4</sup>COMET, School of Earth and Environment, University of Leeds, Leeds LS2 9JT, UK

<sup>5</sup>Japan Agency for Marine-Earth Science and Technology, 3173-25 Showa-machi, Kanazawa-ku, Yokohama 236-0001, Japan

<sup>6</sup>Disaster Prevention Research Institute, Kyoto University, Uji, Kyoto 611-0011, Japan

\*Corresponding author: Shinji Yamashita ([syamashita@geol.tsukuba.ac.jp](mailto:syamashita@geol.tsukuba.ac.jp))

\*\*Second corresponding author: Yuji Yagi ([yagi-y@geol.tsukuba.ac.jp](mailto:yagi-y@geol.tsukuba.ac.jp))

## ABSTRACT

We developed a flexible finite-fault inversion method for teleseismic  $P$  waveforms to obtain a detailed rupture process of a complex multiple-fault earthquake. We estimate the distribution of potency-rate density tensors on an assumed model plane to clarify rupture evolution processes, including variations of fault geometry. We applied our method to the 23 January 2018 Gulf of Alaska earthquake by representing slip on a projected horizontal model plane at a depth of 33.6 km to fit the distribution of aftershocks occurring within one week of the mainshock. The obtained source model, which successfully explained the complex teleseismic  $P$  waveforms, shows that the 2018 earthquake ruptured a conjugate system of N-S and E-W faults. The spatiotemporal rupture evolution indicates irregular rupture behavior involving a multiple-shock sequence, which is likely associated with discontinuities in the fault geometry that originated from E-W sea-floor fracture zones and N-S plate-bending faults.

## Introduction

The 23 January 2018 Gulf of Alaska earthquake (moment-magnitude  $M_w$  7.9<sup>1</sup>) struck offshore Kodiak Island (55.9097°N, 149.0521°W, 10.4 km depth; Alaska Earthquake Center, AEC<sup>1</sup>), in the seaward-region of the Alaska-Aleutian subduction zone. The Global Centroid Moment Tensor (GCMT) project<sup>2,3</sup> reported that the 2018 Gulf of Alaska earthquake had strike-slip faulting with a large non-double-couple component (47%). Aftershock seismicity determined by the AEC<sup>1</sup> shows a lineation extending about 120 km N-S near the epicenter and two aftershock clusters centered about 60 km northeast and about 50 km west from the epicenter (Fig. 1). The GCMT

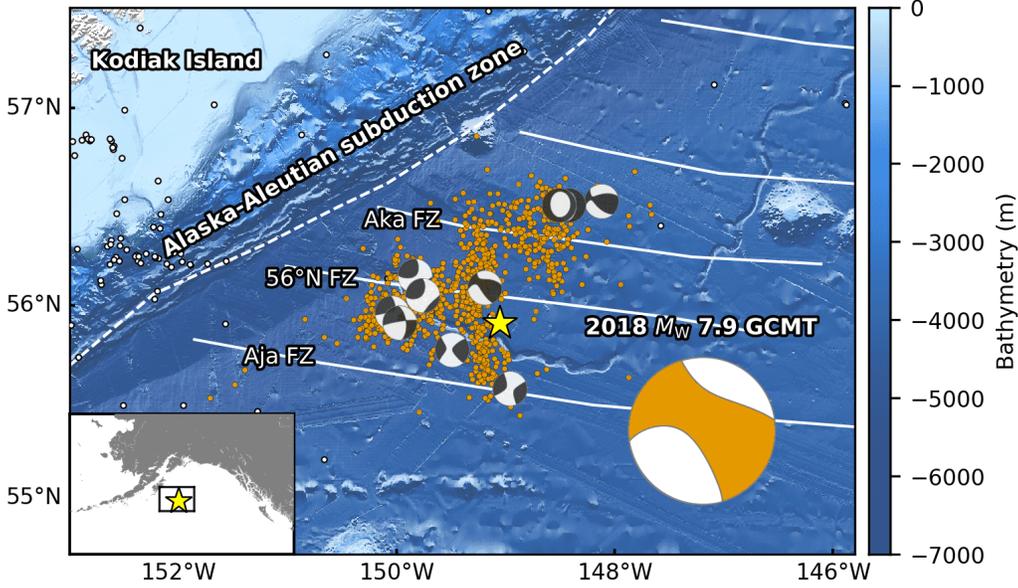
38 solutions of aftershocks are dominated by strike-slip faulting, but include normal and reverse  
39 faulting (Fig. 1).

40 Several pioneering studies that built finite-fault models based on the aftershock distribution  
41 demonstrated that the 2018 Gulf of Alaska earthquake ruptured a quasi-orthogonal multiple-fault  
42 system oriented approximately N-S and E-W<sup>4-8</sup>. However, it is difficult to adopt a reasonable fault  
43 model because the fault model parametrization, number of fault segments, and fault geometries  
44 differ by study, partly due to the spatial spread of the aftershock distribution (Fig. 1). Based on the  
45 static slip distribution estimated from Global Navigation Satellite System and tsunami data, major  
46 slips occurred on E-W-striking segments<sup>5,7,8</sup>. Finite-fault inversions estimated that the maximum  
47 slip occurred around the boundary between the crust and uppermost mantle in the N-S-oriented  
48 segment<sup>4,6</sup>, which would have played a significant role in tsunami generation. However, it remains  
49 challenging to adequately explain the complex characteristics of the observed teleseismic body  
50 waveforms by conventional finite-fault inversion methods due to the uncertainty on the fault  
51 geometry, which lead to significant model errors.

52 In the framework of finite-fault waveform inversion, uncertainties on the Green's function  
53 and fault geometry have been the major sources of model errors<sup>9-13</sup>. Those due to uncertainty on  
54 the Green's function arose from a discrepancy between the true and calculated Green's functions.  
55 To mitigate the effect of this uncertainty, Yagi and Fukahata<sup>13</sup> explicitly introduced the error term  
56 of the Green's function into the data covariance matrix. As a result, their inversion framework  
57 allowed the stable estimation of the spatiotemporal distribution of slip-rate, usually without the  
58 non-negative slip-rate constraint, which had been commonly applied in conventional waveform  
59 inversion methods to obtain a plausible solution<sup>14,15</sup>.

60 Model errors due to uncertainty on the fault geometry arose from inappropriate  
61 assumptions about the fault geometry<sup>11,12</sup>. For strike-slip earthquakes, many seismic stations are  
62 distributed in the vicinity of nodal planes where the radiation pattern is sensitive to the assumed  
63 fault geometry. An obtained solution can easily be distorted by inappropriate assumptions of strike  
64 and dip<sup>12</sup>. These effects can be mitigated by increasing the degrees of freedom in the assumed  
65 seismic source model. Shimizu et al.<sup>12</sup> proposed an inversion method to express slip vectors on  
66 the assumed model plane as the seismic potency tensor. Because their method adopts a linear  
67 combination of five basis double-couple components<sup>16</sup>, the slip direction is not restricted to the  
68 two slip components compatible with the fault direction. Of course, the true fault geometry should  
69 be compatible with the actual slip direction. Whilst the teleseismic *P*-wave Green's function is  
70 insensitive to slight changes in the absolute source location, it is sensitive to the assumed focal  
71 mechanisms<sup>12,16,17</sup>, and their inversion method enabled the spatiotemporal resolution of not only  
72 the detailed rupture evolution, but also variation of the focal mechanism, including information on  
73 the fault geometry, which may differ from the assumed model plane.

74 In this study, we developed a flexible finite-fault inversion framework that can estimate  
75 both the rupture evolution and focal mechanism of earthquakes that ruptured along multiple  
76 complex fault segments. This method incorporates appropriate smoothness constraints and a high-  
77 degree-of-freedom planar model into the inversion framework of Shimizu et al.<sup>12</sup>. Application of  
78 our framework to the 2018 Gulf of Alaska earthquake shows that our source model sufficiently  
79 reproduced the observed complex waveforms without assumptions on fault geometry. The model  
80 also clarified multiple, distinct rupture events in the conjugate fault system that have not been  
81 revealed by conventional finite-fault inversion methods.



82

83 **Figure 1.** Overview of the source region of the 2018 Gulf of Alaska earthquake. The star is the  
 84 mainshock epicenter, orange dots are aftershocks ( $M \geq 3$ ) that occurred within one week of the  
 85 mainshock, and white dots show background seismicity before the mainshock ( $M \geq 3.5$ , 1 January  
 86 2008 to 22 January 2018); all epicentral locations are from AEC<sup>1</sup>. The ‘beachball’ diagrams show  
 87 the GCMT solutions for the mainshock (large, bottom right) and aftershocks with  $M \geq 3.5$ . White  
 88 dashed lines represent plate boundaries<sup>18</sup>, and white solid lines represent fracture zones<sup>19,20</sup>. The  
 89 background bathymetry is derived from the GEBCO 2020 Grid<sup>21</sup>. The inset map shows the  
 90 regional setting. This figure was made with matplotlib (v3.1.1)<sup>48</sup>, ObsPy (v1.1.0)<sup>49</sup>, and Generic  
 91 Mapping Tools (v5.4.5)<sup>50</sup>.

## 92 Method

93 In the inversion framework of Shimizu et al.<sup>12</sup>, the seismic waveform  $u_j$  observed at a station  $j$  is  
 94 given by

$$95 \quad u_j(t) = \sum_{q=1}^5 \int_S (G_{qj}(t, \xi) + \delta G_{qj}(t, \xi)) * \dot{D}_q(t, \xi) d\xi + e_{bj}(t), \quad (1)$$

96 where  $G_{qj}$  is the calculated Green’s function of the  $q$ th basis double-couple component,  $\delta G_{qj}$  is  
 97 the model error on  $G_{qj}$ <sup>13</sup>,  $\dot{D}_q$  is the  $q$ th potency-rate density function on the assumed model plane  
 98  $S$ ,  $e_{bj}$  is background and instrumental noise,  $\xi$  represents a position on  $S$ , and  $*$  denotes the  
 99 convolution operator in the time domain.

100 Shimizu et al.<sup>12</sup> represented the assumed model plane  $S$  as a rectangle horizontally  
 101 covering the seismic source region. However, for earthquakes with complex fault geometries, such  
 102 as the 2018 Gulf of Alaska earthquake, such a horizontal rectangular model plane includes areas  
 103 beyond the seismic source region. Therefore, we further extended their inversion framework such  
 104 that a horizontal non-rectangular model plane can be set according to the shape of the ruptured  
 105 region as estimated from other information (e.g., aftershock seismicity). In other words, we  
 106 introduced *a priori* information about the possible ruptured area into the inversion framework. In

107 numerical tests, the use of a non-rectangular model plane improved spatial resolution and  
 108 computation costs compared to a rectangular one (see Supplementary Material S1 and Figs. S1–  
 109 S4).

110 In general, inversions are stabilized by adding smoothness constraints either implicitly or  
 111 explicitly<sup>22–24</sup>. In the formulation of Shimizu et al.<sup>12</sup>, the smoothness constraints on each potency-  
 112 rate density function  $\dot{D}_q$  in space and time are represented as

$$113 \quad \nabla^2 \dot{D}_q(t, \xi) + \alpha_q = 0, \quad (2)$$

$$114 \quad \frac{\partial^2}{\partial t^2} \dot{D}_q(t, \xi) + \beta_q = 0, \quad (3)$$

115 where  $\alpha_q$  and  $\beta_q$  are assumed to be Gaussian noise with zero mean and covariances of  $\sigma^2 \mathbf{I}$  and  
 116  $\tau^2 \mathbf{I}$ , respectively, where  $\mathbf{I}$  is an  $M \times M$  ( $M$  is the number of model parameters) unit matrix.  
 117 Because they introduced identical Gaussian distributions for all basis components and determined  
 118 the optimal values of the hyperparameters  $\sigma^2$  and  $\tau^2$  by Akaike’s Bayesian information criterion  
 119 <sup>23,25</sup>, the potency-rate density functions of basis components with relatively high amplitudes  
 120 become smoother than those of basis components with relatively low amplitudes, which may bias  
 121 the solution. Thus, when the amplitudes of the potency-rate density functions differ for each basis  
 122 component, the standard deviations of the smoothness constraints should depend on the amplitude  
 123 of each basis component.

124 In this study, we set the standard deviation of the smoothness constraints for each basis  
 125 double-couple component to be proportional to its amplitude. That is, instead of  $\alpha_q$  and  $\beta_q$ , we  
 126 directly introduced Gaussian noise with zero mean and covariances  $\sigma_q^2 \mathbf{I}$  and  $\tau_q^2 \mathbf{I}$ , respectively, as

$$127 \quad \sigma_q^2 \mathbf{I} = k^2 m_q^2 \sigma^2 \mathbf{I}, \quad (4)$$

$$128 \quad \tau_q^2 \mathbf{I} = k^2 m_q^2 \tau^2 \mathbf{I}, \quad (5)$$

129 where  $k$  is a scaling factor and  $m_q$  is the total potency of the  $q$ th basis double-couple component,  
 130 which is independently derived from the moment tensor solution. To avoid extremely small  
 131 standard deviations destabilizing the solution, we adjusted  $k|m_q|$  so that it does not fall below  
 132 10% of its maximum absolute value. Following Yagi and Fukahata<sup>13</sup>, we determined the  
 133 hyperparameters  $\sigma^2$  and  $\tau^2$  by Akaike’s Bayesian information criterion<sup>23,25</sup>. In numerical tests,  
 134 these improved smoothness constraints mitigated the excessive smoothing of the dominant basis  
 135 component imposed by conventional smoothness constraints and, when combined with a non-  
 136 rectangular model plane, outperformed the conventional framework (see Supplementary Material  
 137 S1, Figs. S1–S4 and Table S1).

## 138 Data and Fault Parameterization

139 We used teleseismic  $P$  waveforms (vertical components) recorded at stations with epicentral  
 140 distances of 30–90° (downloaded from the Incorporated Research Institutions for Seismology Data  
 141 Management Center). Of these, we selected 78 stations, ensuring a high signal-to-noise ratio and  
 142 an azimuthal coverage<sup>26</sup> (Fig. 2c), and converted the  $P$  waveforms to velocity waveforms at a  
 143 sampling rate of 0.8 s. The theoretical Green’s functions for teleseismic body waves were  
 144 calculated by the method of Kikuchi and Kanamori<sup>16</sup> at a sampling rate of 0.1 s, and the attenuation  
 145 time constraint  $t^*$  for the  $P$  wave was taken to be 1.0 s. We adopted a 1-D velocity structure derived

146 from the CRUST1.0 model <sup>27</sup> (see Supplementary Table S2) to calculate the theoretical Green's  
147 functions. Following Shimizu et al. <sup>12</sup>, we did not low-pass filter the observed waveforms or  
148 calculated Green's functions. For the smoothness constraints, we calculated  $m_q$  based on the  
149 GCMT solution of the 2018 Gulf of Alaska earthquake. The GCMT solution shows that the M1  
150 (strike-slip) component <sup>16</sup> is more prominent than the others (see Supplementary Table S3),  
151 including the M4 (dip-slip) component <sup>16</sup> (see Supplementary Fig. S4). The scaling factor  $k$  in eqs.  
152 (4) and (5) was set such that  $\min(k|m_q|) = 1$  (Table S3).

153         Based on the aftershock distribution, the 2018 Gulf of Alaska earthquake is considered to  
154 have occurred on a quasi-orthogonal multiple-fault system <sup>4-8</sup>. To cover the high point density area  
155 of aftershocks within one week of the event <sup>1</sup> (Fig. 2a), we set up a non-rectangular horizontal  
156 model plane with a maximum width and length of 130 km, which was expanded using a bilinear  
157 B-spline with a knot spacing of 10 km. We adopted the epicenter as that determined by the AEC  
158 <sup>1</sup>: 55.9097°N, 149.0521°W. The depth of the model fault plane was set at 33.6 km according to  
159 the GCMT centroid depth. For the inversion analysis, we adopted a potency-rate density function  
160 on each knot, each representing a linear combination of B-splines at an interval of 0.8 s. The  
161 maximum rupture-front velocity, which defines the rupture starting time at each knot, was set to  
162 7.0 km/s to account for the possibility of supershear rupture propagation. The rupture ending time  
163 at each knot was set to 65 s from the origin time based on previous inversion results <sup>4,6</sup>. We  
164 evaluated the sensitivity of our model by perturbing the model parameters, and the robustness of  
165 the new method (see Supplementary Material S2, and Figs. S5, S6 and S9).

## 166 **Results**

167 We estimated the spatiotemporal distribution of the potency density tensor for the 2018 Gulf of  
168 Alaska earthquake by applying our flexible finite-fault inversion method to teleseismic  $P$   
169 waveforms. The estimated total moment tensor, calculated by taking the spatial and temporal  
170 integrals of the potency-rate density functions, expresses strike-slip faulting, including 36% non-  
171 double-couple components (Fig. 2a). The spatial distribution of the potency density tensor,  
172 obtained by temporally integrating the potency-rate density functions at each knot, is also  
173 dominated by strike-slip focal mechanisms, with a maximum slip of 6 m about 50 km north of the  
174 epicenter (Fig. 2a). The moment rate function is elevated over two time periods, separated at 27 s  
175 from the origin time: the first period is characterized by three large spikes and the second by  
176 numerous smaller spikes (Fig. 2b). The total seismic moment is  $14.9 \times 10^{20}$  N m ( $M_w$  8.05). The  
177 synthetic waveforms from the obtained source model well reproduce the observed waveforms (see  
178 Supplementary Fig. S11), including those at stations near the nodal planes (Fig. 2d).

179         Based on the moment rate function and snapshots of the potency-rate density tensors (Figs.  
180 2b and S12, respectively), we report the detailed rupture history by dividing it into main (A, 0–27  
181 s) and secondary rupture stages (B, 27–65 s). Based on the location, timing, and continuity of the  
182 rupture, we further identified three phases (A1–A3) during the main stage and five (B1–B5) during  
183 the secondary stage (Figs. 3 and 4).

### 184 **Main Rupture Stage (A)**

185 The initial phase, A1 (0–9 s), started at the hypocenter and propagated bilaterally northward and  
186 southward with strike-slip focal mechanisms (snapshot at 2 s in Fig. 3a). Although it is generally  
187 difficult to identify the preferred fault plane from the two possible nodal planes in this earthquake,  
188 the direction of rupture propagation during phase A1 coincided with the N-S directed nodal plane.

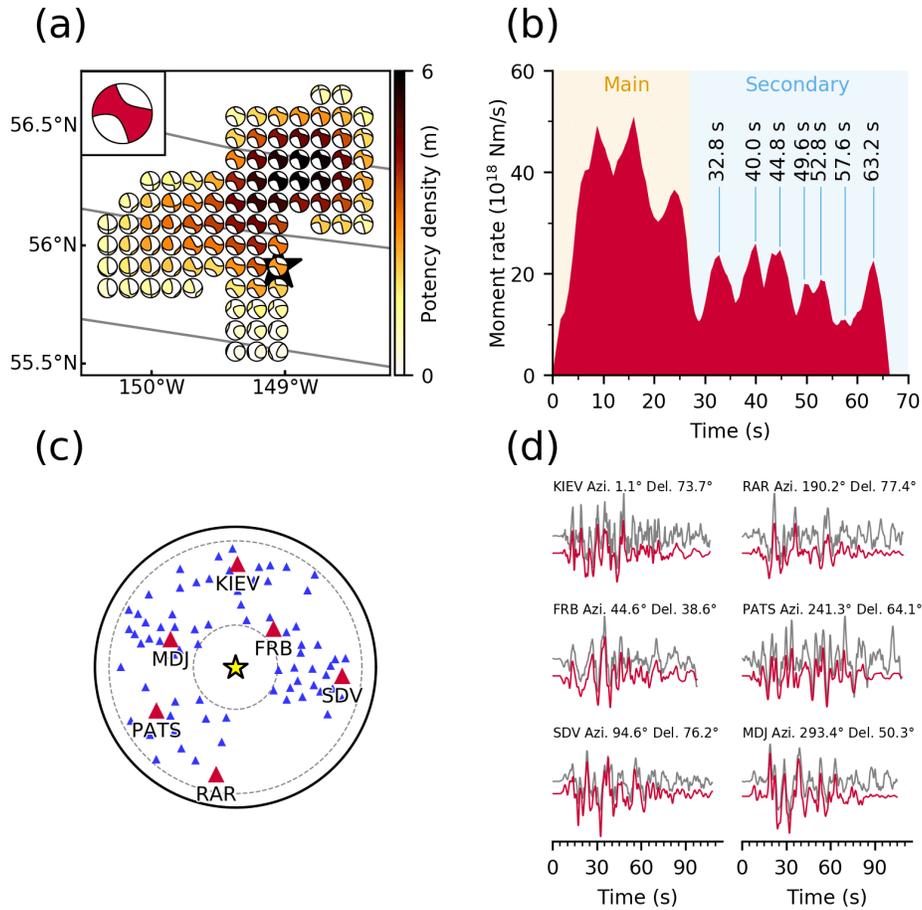
189 The spatial distribution of focal mechanisms shows that the strike of the fault plane gradually  
190 rotated counterclockwise from north to south of the epicenter; we obtained a strike/dip of  $174^{\circ}/82^{\circ}$   
191 around 20 km north of the epicenter, but  $163^{\circ}/76^{\circ}$  around 20 km south of the epicenter (6 s in Fig.  
192 3a). The northward rupture seems to have stagnated near the  $56^{\circ}\text{N}$  fracture zone<sup>28</sup> (FZ) after about  
193 9 s (Fig. 4a).

194 Phase A2 (7–27 s) started about 50 km northeast of the epicenter at around 7 s after the  
195 origin time and propagated west along the Aka FZ<sup>28</sup> (8 s in Fig. 3a). This rupture direction is  
196 consistent with the obtained E-W strike directions (e.g., 10 s in Fig. 3a). The westward rupture  
197 propagated to  $149.2^{\circ}\text{W}$ , where the Aka FZ intersects the N-S aftershock lineation, until 11 s, then  
198 turned southward, indicating that the N-S strike direction is the preferred fault plane (12 s in Fig.  
199 3a). The southward rupture halted at around 12 s at the same location where the northward rupture  
200 of phase A1 had stagnated at about 9 s (Fig. 4a). After 12 s, a discontinuous rupture occurred along  
201 the Aka FZ: ruptures propagating southward and northward from the Aka FZ near  $148.6^{\circ}\text{W}$  are  
202 detected at around 16 and 20 s, respectively (Fig. 3a). The rupture on the Aka FZ near  $149.2^{\circ}\text{W}$  is  
203 again apparent at around 24 s, and gradually ceased by 27 s.

204 Phase A3 (16–27 s), started about 40 km northwest of the epicenter, near the  $56^{\circ}\text{N}$  FZ,  
205 around 16 s after the origin time (Fig. 3a). This rupture propagated bilaterally to the northeast and  
206 southwest until around 18 s, then gradually abated until around 20 s. At that time, another western  
207 rupture occurred at the northwest end of the model region and propagated to the south (20 s in Fig.  
208 3a), stagnating at the  $56^{\circ}\text{N}$  FZ about 50 km west of the epicenter at around 22 s (24 s in Fig. 3a).

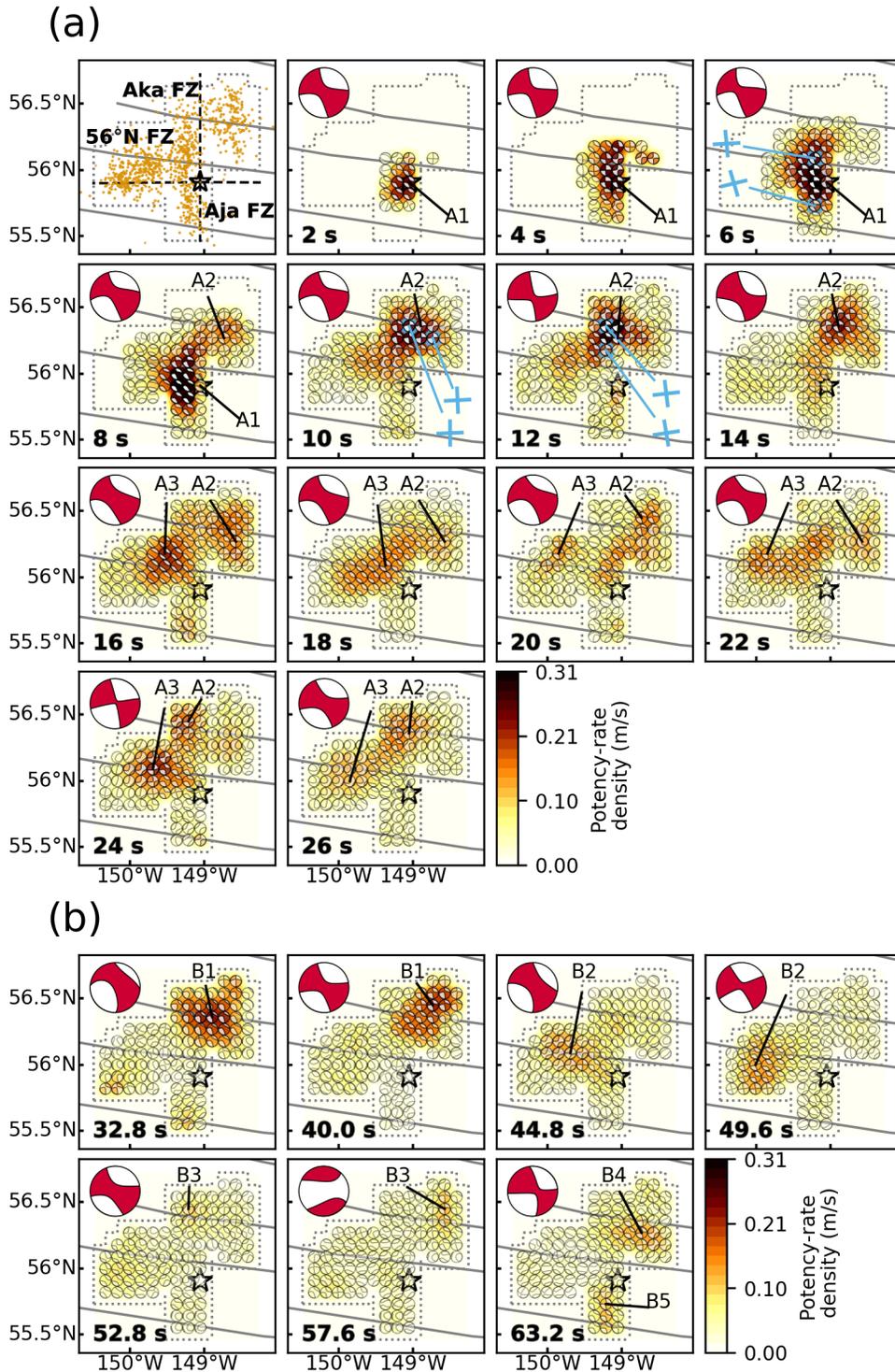
## 209 Secondary Rupture Stage (B)

210 We identified seven peaks in the moment rate function during the secondary rupture stage (Fig.  
211 2b), which we attribute to five phases in the snapshots (Fig. 3b). Phase B1 (28–44 s) occurred  
212 along the Aka FZ. In particular, phase B1 ruptures at around 32.8 and 40.0 s were relatively large,  
213 and appear as individual peaks in the moment rate function (Figs. 2b and 3b). Phase B2 (44–52 s)  
214 mainly ruptured the region west of the epicenter. The rupture at around 44.8 s occurred along the  
215  $56^{\circ}\text{N}$  FZ and that at around 49.6 s struck about 30 km south of the  $56^{\circ}\text{N}$  FZ (Fig. 3b). Phase B3  
216 (53–60 s) occurred mainly northeast of the epicenter, but also struck the intersection of the Aka  
217 FZ and the N-S aftershock lineation at around 52.8 s (Fig. 3b). A northward rupture from the Aka  
218 FZ was also detected at around 57.6 s. The last peak of the moment rate function corresponds to  
219 two independent phases that occurred at around 63.2 s: B4 (62–65 s) ruptured about 20 km south  
220 of the Aka FZ and B5 (62–64 s) ruptured about 30 km south of the epicenter (Fig. 3b).



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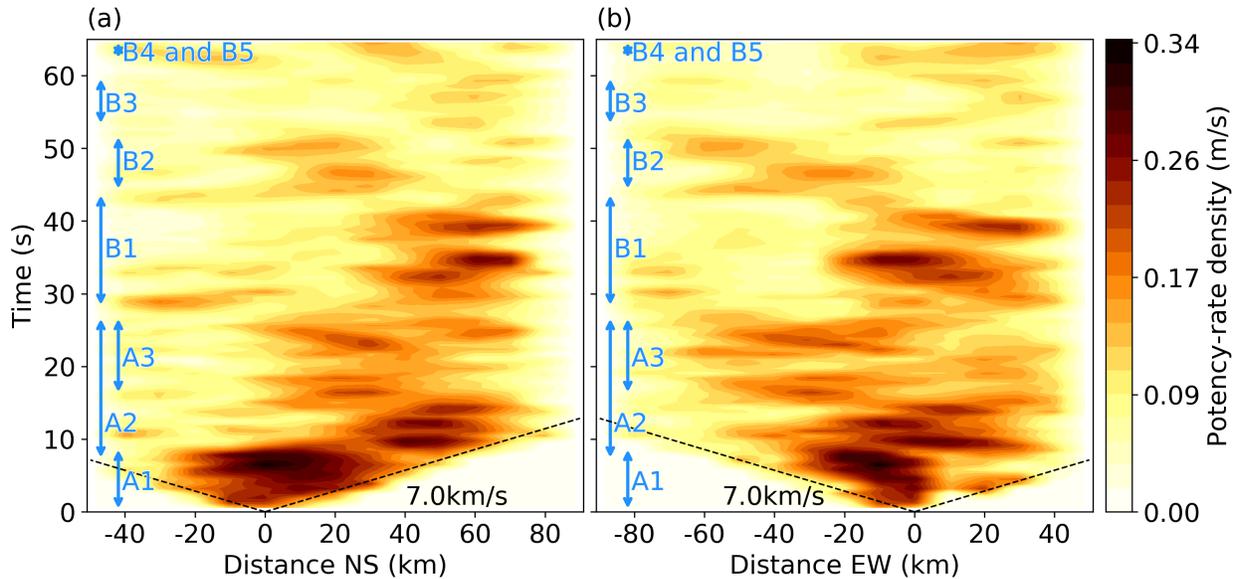
222 **Figure 2.** Model setting and summary of results. (a) Map projection of the potency density tensor  
 223 distribution on the assumed model plane. The star and solid lines indicate the epicenter <sup>1</sup> and  
 224 fracture zones <sup>19,20</sup>, respectively. Inset is the total moment tensor. (b) The moment rate function is  
 225 divided into the main and secondary rupture stages at 27 s. The individual peaks during the  
 226 secondary stage correspond to snapshots in Fig. 3b. (c) Azimuthal equidistant projection of the  
 227 station distribution used in the inversion. The star denotes the epicenter, and triangles denote  
 228 station locations (waveforms for red stations are shown in (d)). The inner and outer dotted lines  
 229 show epicentral distances of 30° and 90°, respectively. (d) Comparison of observed waveforms  
 230 (gray) with synthetic waveforms (red) at the selected stations in (c). Each panel is labeled with the  
 231 station name, azimuth (Azi.), and epicentral distance (Del.) from the mainshock. Waveform  
 232 comparisons for all stations are shown in Supplementary Fig. S11. This figure was made with  
 233 matplotlib (v3.1.1) <sup>48</sup> and ObsPy (v1.1.0) <sup>49</sup>.



234

235 **Figure 3.** Snapshots of the potency-rate density tensors for (a) the main rupture stage A and (b)  
 236 the secondary rupture stage B. The corresponding time after onset for each snapshot is noted at the  
 237 bottom-left of each panel. The dotted line shows the border of the assumed model plane. The star  
 238 and solid lines indicate the epicenter<sup>1</sup> and fracture zones<sup>19,20</sup>, respectively. Blue crosses show the  
 239 strike directions of small beachball diagrams derived from the potency-rate density tensor. The

240 top-left panel in (a) is the epicentral distribution of aftershocks ( $M \geq 3$ ) that occurred within one  
 241 week of the mainshock<sup>1</sup>. The large beachball in each panel indicates the corresponding total  
 242 moment tensor at each time. The dashed lines on the left-top panel of Fig. 3a are the projection  
 243 lines used for Fig. 4. This figure was made with matplotlib (v3.1.1)<sup>48</sup> and ObsPy (v1.1.0)<sup>49</sup>.



244  
 245 **Figure 4.** Time evolution of potency-rate density distribution, projected along (a) north-south and  
 246 (b) east-west directions, where the positive distance directs toward (a) north and (b) east from the  
 247 epicenter. North-south and east-west distances are measured along the dashed lines on the left-top  
 248 panel of Fig. 3a. The dashed line represents the reference rupture speed. Each rupture phase is  
 249 annotated on left of each panel. This figure was made with matplotlib (v3.1.1)<sup>48</sup>.

## 250 Discussion

251 Our inversion results indicate that the main rupture stage (0–27 s after origin) affected segments  
 252 oriented both N-S and E-W, suggesting that the 2018 Gulf of Alaska earthquake ruptured a  
 253 conjugate fault system, as proposed in previous studies<sup>4–8</sup>. Our source model suggests that the  
 254 rupture occurred along weak zones in the sea floor: fracture zones extending E-W and plate-  
 255 bending faults parallel to N-S magnetic lineaments<sup>29,30</sup>. The N-S plate bending faults have been  
 256 interpreted as pre-existing oceanic spreading features that were reactivated by subduction of the  
 257 Pacific Plate<sup>30</sup>. Krabbenhoft et al.<sup>28</sup> associated these pre-existing features with the radiation of  
 258 high-frequency waves based on back-projection and the aftershock distribution (see  
 259 Supplementary Fig. S13).

260 A notable irregular rupture propagation highlighted by our inversion results is the  
 261 northward rupture at around 9 s in phase A1 and the southward rupture at around 12 s in phase A2,  
 262 both of which stopped near the 56°N FZ (8 and 12 s, respectively, in Fig. 3a and Fig. 4a). The N-  
 263 S aftershock lineation is divided into northern and southern clusters across the 56°N FZ (Fig. 3a).  
 264 Given the phase A1 and A2 ruptures and the geometrical offset of the N-S aftershock lineation,  
 265 the northern and southern fault system crossing the 56°N FZ can be regarded as a strike-slip step  
 266 over. Based on our obtained focal mechanisms, these two N-S faults are both right-lateral strike-  
 267 slip faults that dip steeply to the west (8 and 12 s in Fig. 3a), and the counterclockwise rotation of  
 268 the strike angle during phase A1 is consistent with the southern N-S aftershock lineation (6 s in

269 Fig. 3a). Because irregular rupture behaviors are generally a result of geometric complexities,  
270 including barriers caused by discontinuous fault steps<sup>31–33</sup>, we interpret that this fault step over  
271 caused the rupture to stagnate at around 9 and 12 s.

272 Multiple sub-events occurring in a conjugate strike-slip fault system have been reported in  
273 previous studies<sup>34–38</sup>. In this study, we have shown a causal link between the multiple rupture  
274 episodes during the 2018 Gulf of Alaska earthquake (stages A and B) and pre-existing bathymetric  
275 features by resolving both the rupture evolution and variation of fault geometry using only  
276 teleseismic body waves. Similar observations were made during the  $M_W$  8.6 2012 Sumatra  
277 earthquake in the Wharton basin. That earthquake involved multiple  $M_W > 8$  sub-events along a  
278 conjugate fault system<sup>37,39</sup>, which developed by deep ductile shear localization beneath the brittle  
279 upper lithosphere of the oceanic plate<sup>40</sup>.

280 We evaluated how the newly developed method improved the source model of the 2018  
281 Gulf of Alaska earthquake by performing the inversion analysis with the conventional smoothness  
282 constraints<sup>12</sup> (Fig. S7). The inversion result with the conventional smoothness constraints show  
283 general agreement with that obtained by the improved smoothness constraints (Fig. S7). However,  
284 the spatiotemporal rupture propagation of the conventional smoothness constraints is smoother  
285 than that of the improved ones by the excessive smoothing for the most dominant  $M1$  component  
286 for the earthquake (Fig. S8), which provides the blurrier image, making it difficult to clearly  
287 resolve the multiple sub-events (Figs. 3 and S7).

288 It is possible that the complex waveforms observed during the 2018 Gulf of Alaska  
289 earthquake were contaminated by reverberations due to the bathymetric setting that cannot be  
290 reproduced by the theoretical Green's function, resulting in dummy multiple events<sup>41–44</sup>. We  
291 evaluated this possibility by using empirical Green's functions<sup>45,46</sup> and confirm that it is unlikely  
292 that the multiple rupture stages originated from such reverberations (see Supplementary Material  
293 S3 and Fig. S10).

294 The sub-events that occurred after the main A1 phase can be regarded as early aftershocks  
295 missing from global catalogs<sup>47</sup>. Although it is difficult to distinguish whether such early near- to  
296 intermediate-field aftershocks were dynamically or statically triggered<sup>47</sup>, it is noteworthy that the  
297 rupture propagated from A1 to A2 at more than 5 km/s (see Supplementary Material S2 and Fig.  
298 S6); this is faster than the surface wave velocity (3–4 km/s), suggesting that the A2 rupture was  
299 triggered by the A1 rupture.

## 300 **Conclusions**

301 We developed a finite-fault inversion method for teleseismic  $P$  waveforms with improved  
302 smoothness constraints to obtain source processes for earthquakes with complex multiple-fault  
303 ruptures. We applied our inversion method to the 2018 Gulf of Alaska earthquake and estimated  
304 its spatiotemporal rupture process. Although the observed waveforms are very complicated,  
305 reflecting the complex rupture process and fault geometry, the waveforms calculated from our  
306 source model fit well. The obtained source model suggests a complex multiple-shock sequence on  
307 a conjugate fault system, consistent with pre-existing bathymetric features. Irregular rupture  
308 stagnation about 20 km north of the epicenter may have been promoted by a fault step across a  
309 sea-floor fracture zone.

310 **References**

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## 440 Author contributions

441 S.Y. and Y.Y. conceptualized this study, compiled the data and conducted the analyses. S.Y., Y.Y.,  
442 R.O., K.S, R.A. and Y.F. contributed to the methodology. S.Y., Y.Y., R.O. and K.S. processed and  
443 interpreted the data. S.Y. and Y.Y. wrote the manuscript which was revised and edited by R.O.,  
444 K.S., R.A. and Y.F. All authors approved the submitted manuscript. All authors agreed both to be  
445 personally accountable for the author's own contributions and to ensure that questions related to

446 the accuracy or integrity of any part of the work, even ones in which the author was not personally  
447 involved, are appropriately investigated, resolved, and the resolution documented in the literature.

#### 448 **Additional information**

449 Correspondence and requests for materials should be addressed to S.Y. or Y.Y.

#### 450 **Data Availability**

451 Waveform data was downloaded through the IRIS Wilber 3 system  
452 ([https://ds.iris.edu/wilber3/find\\_stations/10607586](https://ds.iris.edu/wilber3/find_stations/10607586)). Teleseismic waveforms were obtained from  
453 the following networks: the Canadian National Seismograph Network (CN;  
454 <https://doi.org/10.7914/SN/CN>); the Caribbean USGS Network (CU;  
455 <https://doi.org/10.7914/SN/CU>); the GEOSCOPE (G; <https://doi.org/10.18715/GEOSCOPE.G>);  
456 the Hong Kong Seismograph Network (HK; <https://www.fdsn.org/networks/detail/HK/>); the New  
457 China Digital Seismograph Network (IC; <https://doi.org/10.7914/SN/IC>); the IRIS/IDA Seismic  
458 Network (II; <https://doi.org/10.7914/SN/II>); the International Miscellaneous Stations (IM;  
459 <https://www.fdsn.org/networks/detail/IM/>); the Global Seismograph Network (IU;  
460 <https://doi.org/10.7914/SN/IU>), and the Pacific21 (PS; <https://www.fdsn.org/networks/detail/PS/>).  
461 The moment tensor solutions are obtained from the GCMT catalog  
462 (<https://www.globalcmt.org/CMTsearch.html>). The CRUST 1.0 model is available at  
463 <https://igppweb.ucsd.edu/~gabi/crust1.html>. The fracture zone data is obtained from the Global  
464 Seafloor Fabric and Magnetic Lineation Data Base Project website  
465 (<http://www.soest.hawaii.edu/PT/GSFML/>).

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