

# 1    **Study on the vorticity field within the tail reconnection jet by** 2    **the MMS spacecraft**

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4    L. Q. Zhang<sup>1</sup>, W. Baumjohann<sup>2</sup>, L. Wang<sup>3</sup>, C. Wang<sup>1</sup>, Y. Ren<sup>1</sup>, James L. Burch<sup>4</sup>, Yu. V.  
 5    Khotyaintsev<sup>5</sup>, J. Y. Wang<sup>6</sup>

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7    1. State Key Laboratory of Space Weather (National Space Science Center, Chinese  
 8    Academy of Sciences), Beijing, 100080, China (e-mail: lqzhang@nssc.ac.cn)

9    2. Space Research Institute, Austrian Academy of Sciences, 8042 Graz, Austria

10    3. Department of Astrophysical Sciences, Princeton University, Princeton, NJ, USA

11    4. Southwest Research Institute San Antonio, San Antonio, TX 78238, USA

12    5. Swedish Institute of Space Physics, Uppsala, Sweden

13    6. Information Engineering College, Central University for Nationalities, Beijing,  
 14    100081, China

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## 16    **Key points:**

17    1) Within the reconnection jet, also named bursty bulk flow (BBF), the vorticity field ( $\omega$ )  
 18    and jet velocity are highly correlated: the higher  $V$ , the stronger  $\omega$ .

19    2) The BBF  $\omega$ -field is dominated by the perpendicular vorticity.

20    3) Concerning  $\beta$ -dependence, the  $\omega$ -field tends to be stronger in super- $M_A$  jet than in  
 21    sub- $M_A$  jet.

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**Abstract** Based on direct measurement by the MMS spacecraft in the years of 2017 and 2018, we perform studies on the vorticity field ( $\omega$ ) within the reconnection jet in the plasma sheet. A typical event on 26 July 2017 shows clearly the evolution of the  $\omega$ -field with the jet velocity:  $\omega$  is weak in the decelerated BBF and strong in the fast BBF. The strongest  $\omega$ -field is in the decaying BBF, around the dipolarization fronts. Despite the evolution of the BBF, the  $\omega$ -field is characterized by the perpendicular vorticity ( $\omega_{\perp}$ ). Statistical results confirm the close correlation between BBF  $V$  and  $\omega$ . Higher  $V$  means stronger  $\omega$ . This accounts for the dawn-dusk asymmetry of the  $\omega$ -field. The anisotropic is more significant in the  $V_{\perp}$ -dominating BBF than in the  $V_{\parallel}$ -dominating BBF. The  $\omega$ -field within the reconnection jet is  $\beta$ -dependence. The  $\beta$ -dependence  $\omega$ -field tends to be stronger in super- $M_A$  jet than in sub- $M_A$  jet.

## 1. Introduction

A reconnection jet, also named BBF, is the most significant and common phenomenon in the Earth's magnetotail [e.g., Angelopoulos et al., 1992; 1994; Baumjohann et al., 1988; 1989; 1990; Zhang et al., 2009; 2010; 2015a,b; 2016a, b]. It provides the main task of the mass, energy, and magnetic flux transport in the tail plasma sheet. A BBF drives serious activities in the magnetosphere and ionosphere [Angelopoulos et al., 2008], by releasing its energy locally in the down-tail region [e.g., Zhang et al., 2020] and/or globally in the near-Earth braking region [Shiokawa, 1997; Shiokawa et al., 1998].

The BBF is inherently a highly turbulent flow, both in its velocity field [e.g., Borovsky et al., 1997; Borovsky and Bonnel, 2001; Borovsky et al., 2003; Zhang et al.,

2019] and in the E/B field [e.g., Tu et al, 2000; Angelopoulos et al., 2002; Wygant et al., 2005; Dai et al., 2011; 2017; Zelenyi et al., 2014; Stawarz et al., 2015]. The kinetic Alfvénic wave (KAW) has been invoked to interpret the E/B turbulence in the course of the BBF. The KAW, including its strength and scaling, depends highly on the flow velocity [Vörös et al., 2004; 2006; Zimbardo, et al., 2010; Chaston et al., 2008; 2012].

The vorticity field ( $\boldsymbol{\omega} = \nabla \times \mathbf{V}$ ) carries the essential information of the turbulence in fluids. Recently, utilizing four-point measurement from the Magnetospheric Multiscale (MMS) spacecraft, Zhang et al. [2019] analyzed the plasma vorticity within a BBF. Their result demonstrates the enhanced vorticity in the course of the BBF. Increase of the vorticity is associated with enhancements of the high-energy ion flux (above 10 keV) and the enhancement of the current  $\mathbf{J}$ . A new scenario of the superposition of the eddy and KAW turbulence is proposed to interpret the BBF turbulence.

Till now, a statistical study on the properties of the vorticity field within the reconnection jet is still lacking. In this paper, we present the first statistical result on the  $\boldsymbol{\omega}$ -field of the BBF based on direct four-point measurement by MMS spacecraft in the tail seasons of 2017 and 2018. Case study and statistical result show clearly the correlation between BBF velocity  $\mathbf{V}$  and vorticity  $\boldsymbol{\omega}$ . Besides, the  $\boldsymbol{\omega}$ -field within the reconnection jet depends highly on plasma  $\beta$  and the Alfvénic March number ( $M_A = V/V_A$ ). MMS observation suggests the significance of the embedded current sheet on the BBF  $\boldsymbol{\omega}$ -field.

## 2. Data description

MMS operates in the magnetotail from May to Oct in the year of 2017 and 2018, with the apogee of  $24.5 R_E$ . The 0.125-s resolution data of fluxgate magnetometers (FGM)

[Russell et al., 2016; Torbert et al., 2016], 0.03-s resolution of Electric Field Instrument (EDP [Lindqvist et al., 2014] and 4.5-s data of Fast Plasma Investigation (FPI) [Pollock et al., 2016] on four MMS satellites during this interval are collected.

The burst flows are selected by the criterion of the duration of  $V_x > 300$  km/s for longer than 15 s. The selection region is confined in the box of  $-25 R_E < X < -7 R_E$ ,  $-15 R_E < Y < 15 R_E$  and  $-5 R_E < Z < 5 R_E$  (GSM coordinates). There are totally 759 bursty flows recorded by MMS. For each event, the curlometer method is applied to calculate the vorticity ( $\omega = \nabla \times \mathbf{V}$ ) [Zhang et al., 2019].

### 3. Typical events

On 27 July 2017 from 17:15 to 17:50 UT, MMS1 locates near the neutral sheet around  $(-23.4 R_E, 6.4 R_E, 4.4 R_E)$  and records the continuous BBF. Overview of the temporal evolutions of the field and plasma during the same interval are shown in Figure 1. The BBF lasts from 17:22 UT (first solid vertical line) to 17:39 UT (last black dashed vertical line), characterized by the finger-like structures of the ion energy spectra [Zhang et al., 2019; 2020]. The ion temperature is higher during the BBF interval. The average Alfvénic velocity ( $V_A = B_0 / \sqrt{4\pi\rho}$ ) is 267 km/s.

The BBF experiences three different stages, including weak-BBF, strong-BBF, and decaying-BBF. The average velocity of the weak-BBF is only  $\sim 200$  km/s, lower than  $V_A$ . At 17:31 UT (marked by the first black dashed line), the BBF is suddenly enhanced. The strong-BBF has significant parallel component ( $V_{||}$ ). After 17:35 UT (marked by the yellow dashed line), the BBF rapidly decays. In the decaying-BBF, the  $V_y$  is strong.

Before and after the BBF, the  $B_z$  component in the background plasma sheet is increased from 0.2 nT to 5 nT. The magnetic field in Panels D and E has slowly large-amplitude fluctuation in the weak-BBF, and rapidly small-amplitude in the strong-BBF. Accompanying with the magnetic field fluctuations, the ion density fluctuates also. In the decaying-BBF, two dipolarization fronts (DFs) emerge, signed by the sharp  $B_z$ -enhancement and the simultaneous  $B_T$ -enhancement. As a contrast, the ion temperature dips at the DFs.

Evolutions of three components of the vorticity field are presented in Panels H to J. The  $\omega$  has substantial enhancement in the course of the BBF. The  $\omega_z$  is generally the main component. The  $\omega_y$  becomes significant in the decaying-BBF. Despite the evolution of the BBF, the  $\omega_\perp$  is the dominant component (Panel K). The anisotropic angle ( $\theta_{AA} = \arctan(\frac{\omega_\perp}{\omega_{//}})$ ) is averagely  $65.3^\circ$ . Apparently, the  $\omega$ -field is characterized by the perpendicular-predominantly vorticity

#### 4. Statistical study

##### Dawn-dusk asymmetry

The BBFs are classified into two groups according to their angels between  $V$  and  $B$  ( $\theta_{VB} = \arctan(\frac{V_\perp}{V_{//}})$ ), i.e.,  $V_{//}$ -dominating BBF ( $\theta_{VB} < 45^\circ$ ) and  $V_\perp$ -dominating BBF ( $\theta_{VB} > 45^\circ$ ). The BBF  $\omega$  and other parameters are the average value in the course of the BBF.

Evolutions of the  $\omega$  field in the dawn-dusk direction for the  $V_{//}$ -dominating BBF and  $V_\perp$ -dominating BBF are shown in Figure 2. The  $\omega$ -field in Panels B and C has significant

113 dawn-dusk asymmetry. As a whole, the BBF  $\omega$  is stronger in the dawn side than in the  
 114 dusk side.

115 The BBF  $V_x$  is shown in Panel A. We can see that the BBF  $V$  and  $\omega$  are highly  
 116 correlated. Higher  $V$  means stronger  $\omega$ . Similar dawn-dusk asymmetry can be seen in the  
 117 BBF  $V_x$ . This accounts for the dawn-dusk asymmetry of the  $\omega$ -field.

### 118 **Anisotropy**

119 Histogram of probabilities of the  $\theta_{AA}$  of the BBF is shown in Figure 3. The  $V_{//}$ -  
 120 dominating and  $V_{\perp}$ -dominating BBF have similar distributions. Both have almost  
 121 symmetric distributions. Both BBFs occur mostly for  $|\theta_{AA}| > 60^\circ$ . Statistically, the BBF  
 122 vorticity is  $\omega_{\perp}$ -dominating. Relatively, the perpendicular BBF have higher  $|\theta_{AA}|$  than the  
 123 parallel BBF. The anisotropy is more significant in the perpendicular BBF than in the  
 124 parallel BBF.

### 125 **$\beta$ -dependence**

126 Scatter plot of  $\beta$  versus  $\omega$  is presented in Figure 4. It can be seen that the small- $\omega$   
 127 field ( $\omega < 1$ ) dominates the regime of  $\beta < 200$  while the large- $\omega$  field ( $\omega > 1$ ) dominates  
 128 the regime of  $\beta > 200$ . As we have known, magnetic Prandtl number ( $Pm = \mu_0 \sigma \mu$ ) is an  
 129 increasing function of the plasma beta value. It can be inferred that within the  
 130 reconnection jet, the  $\omega$ -field is stronger/weaker in the regime of higher/lower  $Pm$   
 131 (magnetic Prandtl number  $Pm = \mu_0 \sigma \mu$ ).

132 The colored  $M_A$  of the BBF is also presented in Figure 4. Clearly, the reconnection  
 133 jet could be super- $M_A$  as well as sub- $M_A$  as well. Note that seldom small- $\omega$  BBF occurs  
 134 for  $M_A > 1.5$  ( $\beta > 1000$ ). It appears that the  $\beta$ -dependence  $\omega$ -field tends to be stronger in  
 135 super- $M_A$  jet than in sub- $M_A$  jet.

## 5. Discussion

A cartoon illustration of the vorticity field within the earthward traveling BBF embedded unsteady current sheet is shown in Figure 5. In the equatorial region (X-Y plane), the  $\omega_z$  is the dominant component. The  $\omega$ -field is stronger on the dawn side than on the dusk side.

Previous studies showed that the plasma  $\omega$  of the KAW is nearly field-aligned [Phan et al., 2016; Hwang et al., 2019; Wang et al., 2019]. This agrees with the perpendicular-cascade of the KAW turbulence. Unlike the KAW-vorticity, the BBF-vorticity is predominantly perpendicular. The  $\omega_\perp$ -dominating vorticity could introduce parallel cascade in the BBF turbulence.

The  $\beta$ -dependence and anisotropic strongly suggests the significance of the embedded current sheet on the  $\omega$ -field of the reconnection jet. This current sheet determines the magnetic structure in the normal direction within the reconnection jet [Nakamura et al., 2006; 2008], hence, the plasma  $\beta$  and the flow structure with respect to the magnetic field (parallel or perpendicular) [Zhang et al., 2010a].

Interaction between the embedded current sheet and the BBF could have substantial influence on the evolution of the  $\omega$ -field. The thin current sheet facilitates the K-H wave/instability [e.g., Horton et al., 1987; Dai, 2009; Dai et al., 2011]. It can be expected the generation of the K-H vortex within the reconnection jet [Turkakin et al., 2014]. On the other hand, emitting KAW by unstable current sheet (kink and/or tear) dissipates the kinetic energy of the BBF [Hoshino and Higashimori, 2015]. This may lead to the decay of the vorticity field.

## 6. Conclusions

As a conclusion, the BBF  $\mathbf{V}$  and  $\omega$  are highly correlated. Higher  $\mathbf{V}$  means stronger  $\omega$  is. The  $\omega$ -field within the reconnection jet is characterized by the perpendicular-predominantly component. The anisotropic, quantified by the anisotropic angle ( $\theta_{AA} = \arctan(\frac{\omega_{\perp}}{\omega_{\parallel}})$ ), is more significant in the  $V_{\perp}$ -dominating BBF than in the  $V_{\parallel}$ -dominating BBF. Besides, the BBF  $\omega$  is  $\beta$ -dependence. The  $\beta$ -dependence  $\omega$ -field tends to be stronger in super- $M_A$  jet than in sub- $M_A$  jet. MMS result highlights the potential significance of the embedded current sheet on the  $\omega$ -field in the course of the BBF.

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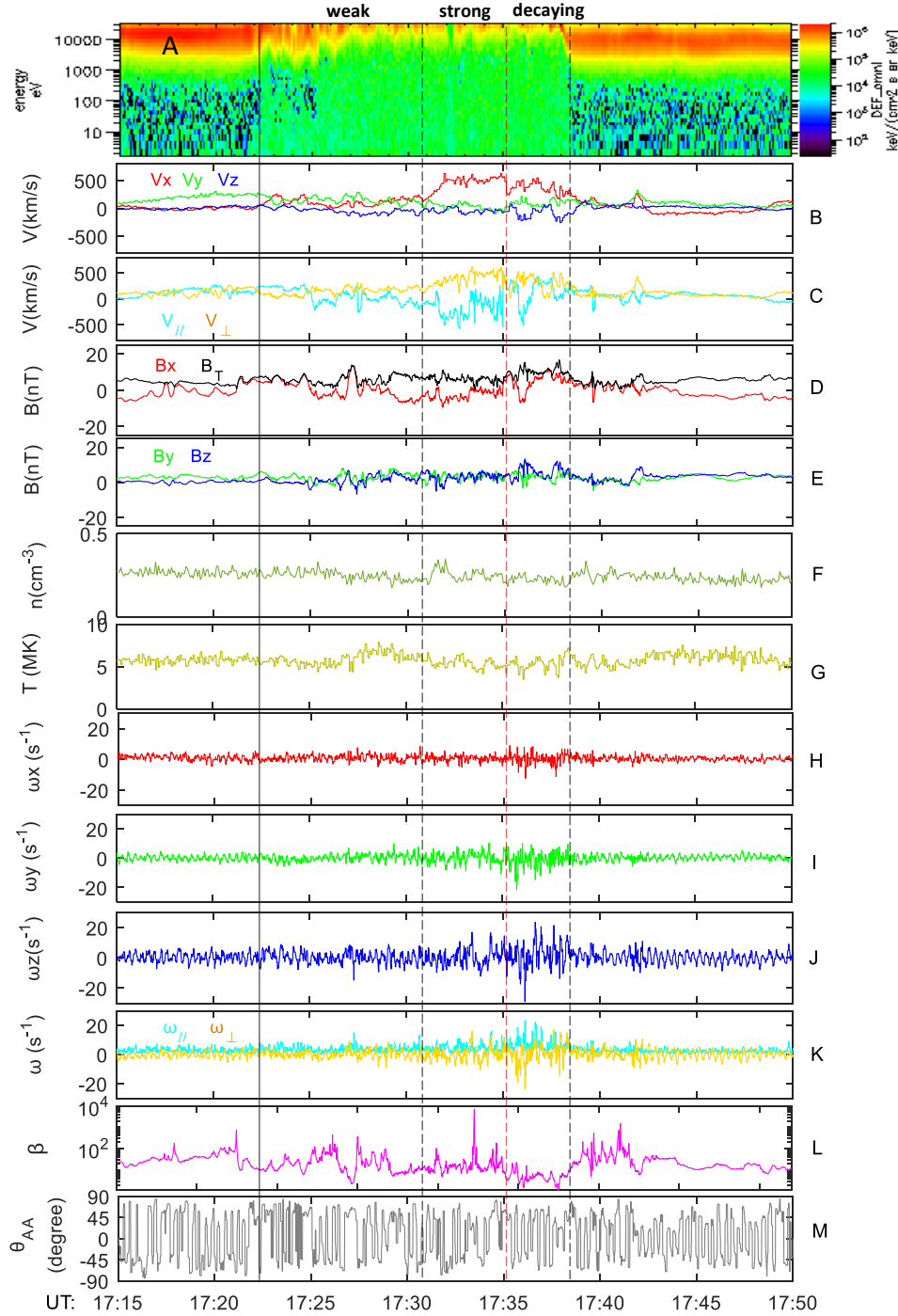
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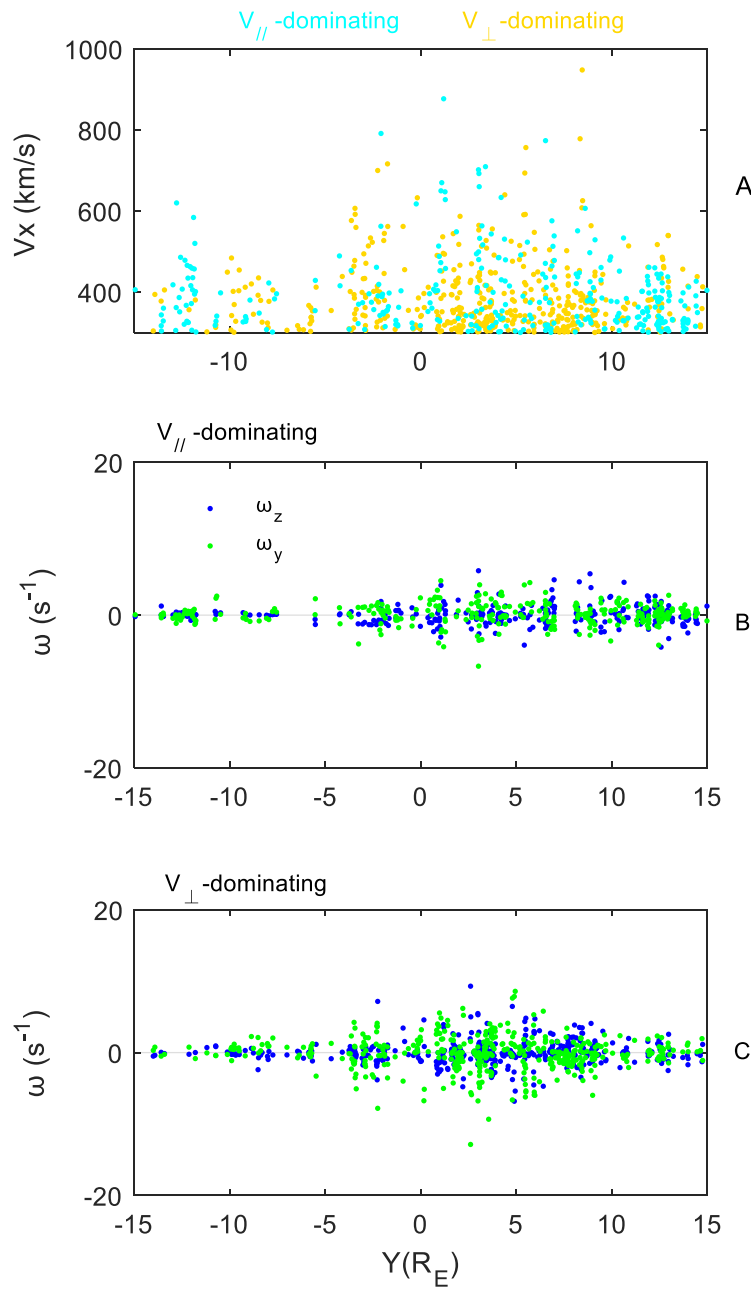
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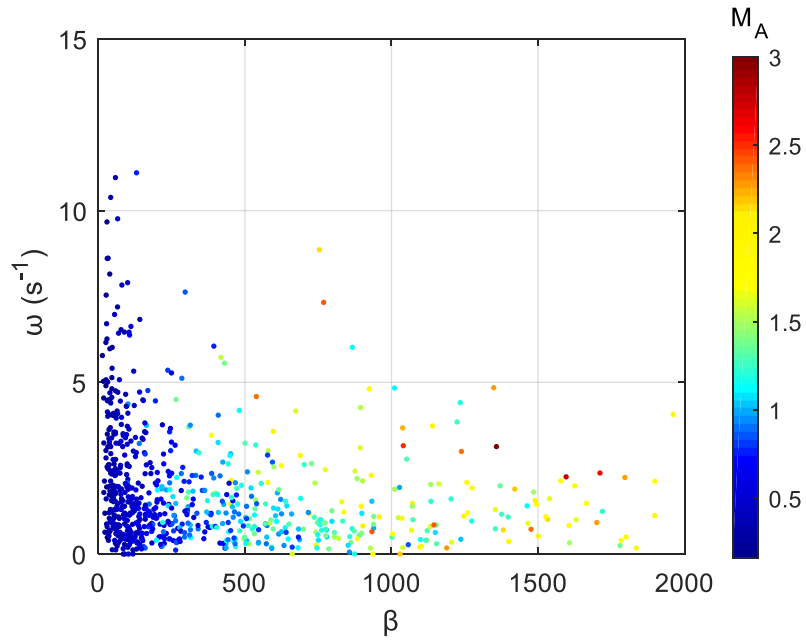


**Figure 1. Evolutions of the vorticity field in the course of the reconnection jet on 26 July, 2017**  
MMS1 locates at  $(-23.4 R_E, 6.4 R_E, 4.4 R_E)$  (GSM). The BBF starts at 17:22 UT (solid vertical line),  
and ends at 17:37 UT (the last dashed line). Panel A is the ion energy flux spectrogram. Panel B plots  
the three components of the measured ion velocity. Panel C shows  $V_{\parallel}$  and  $V_{\perp}$ . Panels D and E are the  
measured  $B_x$ ,  $B_y$ ,  $B_z$ , and total  $B$  ( $B_T$ ). Panels F to H are the all components of measured  $E$  and  
corresponding convective  $E$  (calculated by  $E_c = V \times B$ ). Panels I and J plot  $\omega_x$ ,  $\omega_y$ ,  $\omega_z$ , the total  $\omega$  ( $\omega_T$ ).  
Panel K shows  $\omega_{\parallel}$  and  $\omega_{\perp}$ . Panel K shows the angel between  $V$  and  $B$  ( $\theta_{VB} = \arctan(\frac{V_{\perp}}{V_{\parallel}})$ ) and the  
anisotropic angle of the vorticity ( $\theta_{AA} = \arctan(\frac{\omega_{\perp}}{\omega_{\parallel}})$ ).

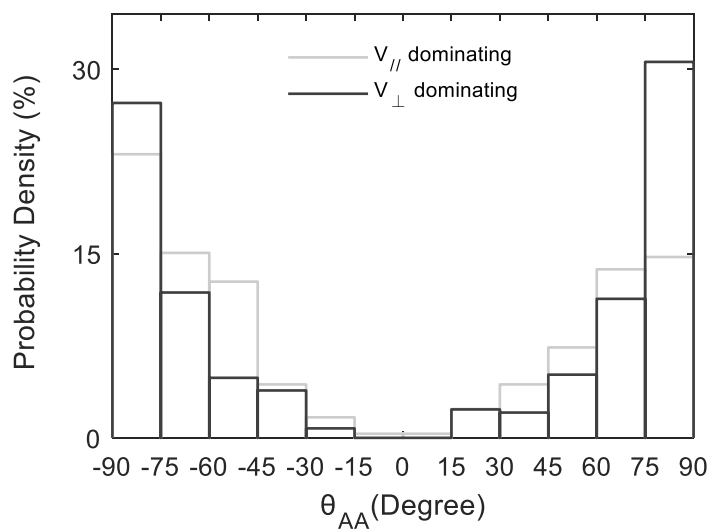


**Figure 3. Scatter plots of the evolution of the vorticity field of the BBF in the dawn-dusk direction**

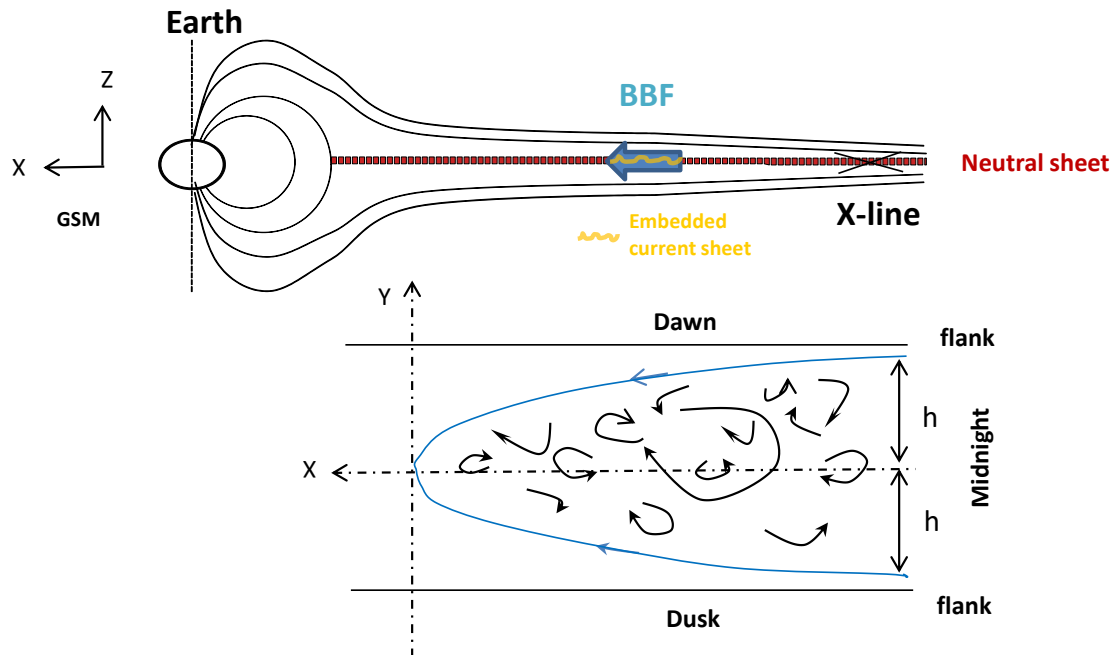
Each point represents a BBF event. Panel A plots the BBF  $V_x$ . Panels B and C are the vorticity field in the  $V_{||}$ -dominating and  $V_{\perp}$ -dominating BBF, respectively.



**Figure 4. Scatter plot of  $\beta$ -dependence vorticity field of the BBF**  
 Color of the point corresponds to the Alfvén Mach number  $M_A = V/V_A$ .



**Figure 2. Probability densities of the  $\theta_{AA}$  for the  $V_{//}$ -dominating and  $V_{\perp}$ -dominating BBF**



**Figure 5. Cartoon of the vorticity field within the earthward traveling BBF embedded unsteady current sheet**

The blue curved line with the arrow is the boundary of the reconnection jet. The vorticity field within the reconnection jet has significant dawn-dusk asymmetry.