

A subgrain-size piezometer calibrated for EBSD

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Key Points

1. We present a new subgrain-size piezometer calibrated for EBSD, with a 1° critical misorientation angle.
2. This subgrain-size piezometer can be applied to multiple minerals and appears to be independent of the deformation geometry.
3. This subgrain-size piezometer should be unaffected by the presence of secondary minerals and thus applicable to polymineralic rocks.

22 **Abstract**

23 We calibrate a subgrain-size piezometer using electron backscatter diffraction (EBSD) data
24 collected from experimentally deformed samples of olivine and quartz. Systematic analyses of angular
25 and spatial resolution test the suitability of each dataset for inclusion in calibration of the subgrain-size
26 piezometer. To identify subgrain boundaries, we consider a range of critical misorientation angles and
27 conclude that a 1° threshold provides the optimal piezometric calibration. The mean line-intercept
28 length, equivalent to the subgrain-size, is found to be inversely proportional to the von Mises equivalent
29 stress for datasets both with and without the Holyoke and Kronenberg (2010) correction. These new
30 piezometers provide stress estimates from EBSD analyses of polymineralic rocks without the need to
31 discriminate between relict and recrystallised grains and therefore greatly increase the range of rocks that
32 may be used to constrain geodynamic models.

33 **Plain Language Summary**

34 Understanding the tectonic stress in the lithospheric plates is key to evaluating a breadth of
35 geological phenomena, such as the evolution of major ductile shear zones. One method of estimating
36 past stress magnitudes is to measure microstructural features that vary systematically with the applied
37 stress, a technique known as ‘piezometry’. Several piezometers have been calibrated based on the size of
38 recrystallised grains in a rock, but they are limited to domains consisting of only a single mineral, as the
39 presence of multiple minerals inhibits grain growth. Subgrains, however, are features inside individual
40 grains and are unaffected by the presence of other minerals. We use electron backscatter diffraction
41 (EBSD), a scanning electron microscopy technique, to quantify the relationship between subgrain size
42 and stress in rocks that have been deformed in a laboratory under controlled conditions, providing the
43 first subgrain-size piezometer calibrated for EBSD. In addition, unlike many piezometers that are
44 calibrated for a single mineral, our piezometer can be applied to each mineral in a rock. This piezometer

45 offers the potential to investigate the macroscopic stress and microscopic stress distributions in a wide
46 range of rock types.

47 **1. Introduction**

48 Quantitative constraints on the stresses associated with past deformation events in the ductile
49 portion of the lithosphere are key to developing and testing geodynamic models. One method of
50 estimating past stress magnitudes is to measure microstructural elements that can be related to stress
51 through experimental calibrations, a technique known as piezometry. Paleopiezometry has provided key
52 estimates of the strength of continental (e.g., Kohlstedt & Weathers, 1980; Stipp et al., 2002; Weathers et
53 al., 1979) and oceanic (e.g., Hansen et al., 2013; Jaroslow et al., 1996; Speckbacher et al. 2011; Warren
54 & Hirth, 2006) fault zones, yielded insight into the mechanisms of localisation in outcrop-scale shear
55 zones (e.g., Austin et al., 2008; Gueydan et al., 2005; Haertel & Herwegh, 2014; Linckens et al., 2011;
56 Skemer et al., 2010; Skemer et al., 2013), and enabled tests of the extrapolation of laboratory-derived
57 rheological laws to geological conditions (e.g., Behr & Platt, 2011; Hansen & Warren, 2015; Hirth et al.,
58 2001; Stipp et al., 2002; Wex et al., 2019). Thus, paleopiezometry is an essential tool for field-based
59 quantitative investigations of the mechanical behaviour of the lithosphere.

60 The most frequently used piezometers are based on the size of dynamically recrystallized grains,
61 herein referred to as grain size (Karato et al., 1980; Rutter, 1995; Schmid et al., 1980; Stipp & Tullis,
62 2003; Twiss, 1986; Van der Wal et al., 1993). However, piezometers based on grain size are only
63 applicable to rocks consisting of a single mineral. Secondary minerals may modify grain size by limiting
64 grain-boundary mobility and thus inhibiting grain growth, an effect known as ‘pinning’ (Evans et al.,
65 2001; Hiraga et al., 2010; Smith, 1948; Tasaka et al., 2017). As most natural rocks contain more than one
66 mineral, pinning severely limits the applicability of grain-size piezometers.

67 Like grain size, subgrain size varies systematically with differential stress during steady-state
68 deformation (Luton & Sellars, 1969; Twiss, 1986). Piezometers based on these intragranular structures

69 are preferable to those based on grain size for two reasons: 1) subgrain sizes are not modified by grain-
70 boundary pinning (Hansen & Warren, 2015; White, 1979), and 2) as subgrains form over relatively small
71 strain intervals ($\leq 10\%$, Biberger & Blum, 1992; Ross et al., 1980) in both relict and recrystallised
72 grains. Therefore, subgrain-size piezometry can be applied to samples subject to small strains and
73 obviates the need to identify grains that formed by dynamic recrystallisation. Subgrain-size piezometry
74 therefore provides a tool to evaluate past stress experienced by broader range of rocks, including
75 polymineralic rocks (e.g., Hansen & Warren, 2015).

76 Relationships between applied stress and subgrain size measured using optical microscopy or
77 transmission electron microscopy (TEM) have been established for quartz (Mercier et al., 1977), olivine
78 (Durham & Goetze, 1977; Goetze, 1975; Karato et al., 1980; Toriumi, 1979), and calcite (Friedman &
79 Higgs, 1981; Platt & De Bresser, 2017). In addition, subgrain-size piezometers applicable to multiple
80 minerals have previously been proposed (Shimizu, 1998; Twiss, 1986). However, different methods for
81 measuring microstructural features have different detection limits, which can lead to systematic offsets
82 between piezometric relationships for the same mineral (Cross et al., 2017; Hansen et al., 2011).
83 Currently, no subgrain-size piezometers have been calibrated for data collected by electron backscatter
84 diffraction (EBSD), despite the relatively simple sample preparation, rapid data acquisition, and
85 precision in misorientation angles of $\pm 0.5^\circ$ (Humphreys, 2004) associated with this technique.

86 Here, we present EBSD measurements of subgrain size in experimentally deformed olivine and
87 quartz samples and derive a single piezometric relationship for both minerals. We explore the sensitivity
88 of the piezometric calibration to the lower cut-off of subgrain-boundary misorientation angles and
89 provide tests for the number of intercept lines, the number of grains, and the step size required to
90 accurately capture the subgrain size. The resulting piezometer greatly extends the range of rocks for
91 which EBSD data can provide quantitative stress estimates.

92 **2. Method**

93 ***2.1 Sample Description***

94 Samples from three sets of experiments conducted on quartz and olivine were analysed. The
95 experimental conditions associated with each sample can be found in the supplementary material (Table
96 S1). Each stress reported in Table S1 is the von Mises equivalent stress (hereafter referred to solely as
97 the equivalent stress, σ) experienced by the sample, which is assumed to be associated with the
98 microstructures observed at the end of the experiment. All samples were deformed in a regime in which
99 deformation is rate-limited by the motion of dislocations.

100 **2.1.1 Quartz Experiments**

101 Quartz samples prepared from Black Hills Quartzite were deformed in two sets of experiments,
102 denoted Qz-1 and Qz-2. Qz-1 samples were deformed in a Griggs apparatus at Brown University, Rhode
103 Island (Stipp & Tullis, 2003). Qz-2 consists of samples deformed in a Griggs apparatus either at Texas
104 A&M University or at Brown University (Holyoke & Kronenberg, 2013; Holyoke & Tullis, 2006). Both
105 sets of experiments were conducted at a confining pressure of 1.50–1.56 GPa and temperatures in the
106 range 800°–1100°C. Samples included in the calibration lay within recrystallisation regimes 2 and 3 as
107 defined by Hirth and Tullis (1992), as the relationship between subgrain size and stress appears to
108 change in regime 1 (cf., Stipp & Tullis, 2003).

109 The Qz-1 samples consisted of cylinders deformed in axial compression at constant
110 displacement rates of 1.8×10^{-6} – 1.7×10^{-3} mm/s. Flow stress, taken as an average of the value between
111 10% strain and the value at the final strain (17–41%) in each experiment, ranged between 34 ± 16 and
112 268 ± 40 MPa (Stipp et al., 2003).

113 For the Qz-2 samples, experienced either general shear or axial compression at constant
114 equivalent strain rates of 1.6×10^{-6} – 1.15×10^{-5} . Final shear strains ranged from 50% to 610%. The only

115 experiment deformed in axial compression in Qz-2, TMQ-7, reached a final axial strain of 15.6%. All
116 Qz-2 samples, excluding W-1105, were deformed to their yield point. The ability of subgrains to keep
117 pace with the stress after very little strain means the lack of steady-state conditions should not influence
118 the piezometric calibration. Therefore the final flow stress, converted into the equivalent stress, was
119 taken as the stress associated with the final microstructures.

120 Correction of the mechanical data in Qz-1 and Qz-2 for the friction on the σ_1 piston, were
121 performed according to the procedures of Gleason and Tullis (1995) / Stipp and Tullis (2003) and
122 Holyoke and Tullis (2006), respectively. We then compare two sets of stresses to subgrain size, either
123 with or without a second friction correction described by Holyoke and Kronenberg (2010, 2013) to
124 account for increased friction due to a Poisson effect on the load column during loading of the sample.

125 *2.1.2 Olivine Experiments*

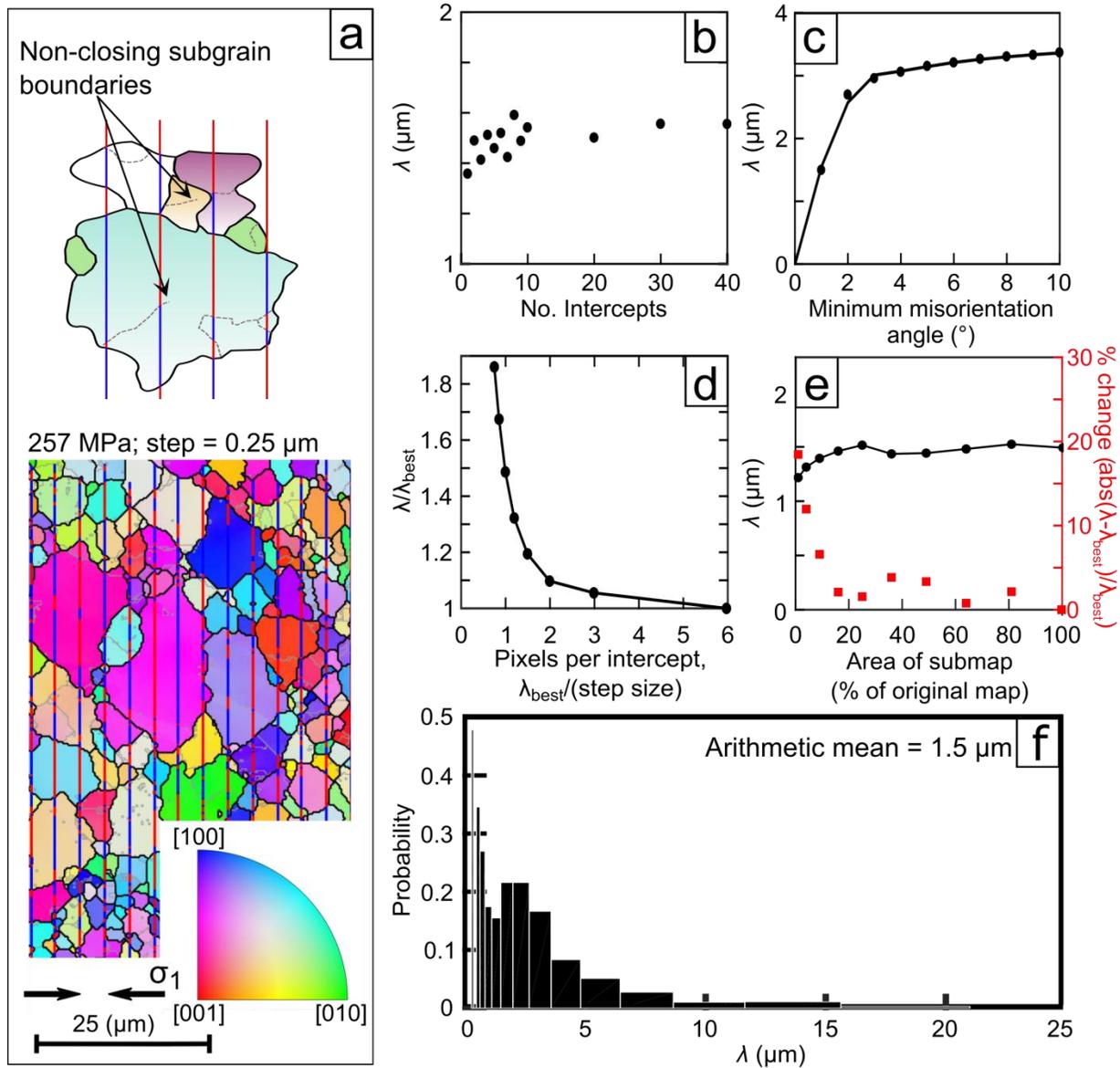
126 Data from olivine samples deformed in a number of different axial compression and torsion
127 experiments were compiled to form the ‘Ol’ dataset (Hansen et al., 2011, 2012; Pommier et al., 2015;
128 Tasaka et al., 2016, 2017) . Polycrystalline Fo₉₀ and Fo₅₀ samples were fabricated from San Carlos
129 olivine (Hansen et al., 2011) or from a combination of oxide powders and San Carlos olivine (Tasaka et
130 al., 2017), respectively. Experiments were conducted in a servo-controlled, internally heated, gas-
131 medium apparatus (Paterson, 1990) at the University of Minnesota, at a confining pressure of 300 MPa
132 and temperatures of 1150°–1250°C. Equivalent strain rates were 9×10^{-6} – 1.48×10^{-3} s⁻¹. Stress was
133 measured with an internal load cell and controlled to ± 1 MPa for axial compression experiments (Hansen
134 et al., 2011) and ± 2 MPa for torsion experiments (Tasaka et al., 2016). Stresses measured during torsion
135 experiments were converted to equivalent stress following Paterson and Olgaard (2000). In axial
136 compression experiments, maximum axial strains reached up to 20%. In torsion experiments, except PT-
137 0966, the strain was recorded as the outer radius shear strain and reached up to 880%. For sample PT-
138 0966 the shear strain, recorded as 500%, was calculated from an originally vertical crease in the jacket
139 formed during the initial pressurisation of the sample.

140 ***2.2 Acquisition of Microstructural Data***

141 For EBSD analyses, samples deformed in axial compression were cut parallel to the cylindrical
142 axis (Hansen et al., 2011; Holyoke & Kronenberg, 2013; Stipp & Tullis, 2003). For samples deformed in
143 torsion, tangential sections were chosen for analysis (Hansen et al., 2012; Tasaka et al., 2016, 2017). In
144 the direct shear geometry, sections parallel to the shear direction and perpendicular to the shear plane
145 were chosen (Holyoke & Tullis, 2006). The sectioned surfaces were prepared by polishing with diamond
146 lapping films or suspensions with decreasing grit sizes from 30 to 0.05 μm and were generally finished
147 by polishing with 0.03 or 0.04 μm colloidal silica.

148 EBSD data were collected with an FEI Quanta 650 FEG E-SEM in the Department of Earth
149 Sciences, University of Oxford, equipped with Oxford Instruments AZtec (Version 3.3) acquisition
150 software and a NordlysNano EBSD camera. Samples, were tilted at 70° and mapped in low vacuum (50–
151 60 Pa, H_2O) at accelerating voltages of 20–30 kV with step sizes of 0.1–1.0 μm . Noise reduction was
152 performed using Oxford Instruments Channel5 software. Non-indexed points with ≥ 6 indexed
153 neighbours within the same grain were assigned the average orientation of their neighbours. In addition,
154 pixels in images of quartz that were systematically misindexed due to pseudosymmetry were corrected
155 by applying a rotation of 60° around [0001] (Trimby et al., 2002).

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Figure 1: Full analysis of PI-1523 (olivine), where λ is the measured mean line-intercept length and λ_{best} is the value of λ associated with the smallest step size and largest map area. (a) Schematic of the line-intercept method on a map of the sample coloured by normal to the section. (b) Mean line-intercept length versus the number of intercept lines taken in both the vertical and the horizontal direction. (c) Mean line-intercept length versus minimum misorientation angle used to define a subgrain boundary. (d) Step-size analysis, see main text for

164 description. (e) Area analysis, see main text for description. (f) Histogram of mean line-intercept lengths with a
165 logarithmic bin width.

166 For our piezometer, subgrains were measured using the line-intercept method. This method,
167 compares adjacent pixels on evenly spaced lines transecting the sample (Figure 1a). Along each line,
168 misorientations greater than a specified angle, the critical misorientation angle, are detected and the
169 intercept length between misorientations recorded. The number of intercept lines is increased and the
170 mean line-intercept length measured until the latter stabilises ($\pm 2.5\%$), thus ensuring the number of
171 intercepts is sufficient to accurately estimate the mean value.

172 The line-intercept method is preferred over other grain-size measurement techniques because it
173 includes non-closing subgrain boundaries. When analysing subgrain boundaries with small
174 misorientation angles, it is important to include such primitive structures because subgrain boundaries do
175 not always fully enclose an isolated region (e.g., Figure 1a & Figure 2). Additional benefits compared to
176 alternative area-based subgrain-size measurement include lower sensitivity to changes in step size
177 (Mingard et al., 2007; Valcke et al., 2006), faster processing times (Humphreys, 2001), and lower
178 sensitivity to anomalous clusters of data points missed during post-processing (Hansen et al., 2011).

179 To obtain sample averages, we use the arithmetic mean of the line-intercept lengths. This
180 approach provides the mean spacing between all boundaries with misorientations above the chosen
181 critical value. An alternative average, the geometric mean, is more sensitive to misindexed pixels and
182 variations in step-size (Mingard et al., 2007). In previous studies, a stereological correction was
183 commonly applied to convert the mean line-intercept length from a 2-D section to the mean grain
184 diameter in 3-D (Hansen et al., 2011; Hansen & Warren, 2015; Underwood, 1970, pages 80–93; Valcke
185 et al., 2006). As the choice of 3D correction adds an additional layer of uncertainty to the data
186 processing, we avoid any correction and simply use the mean line-intercept length, λ , as the
187 microstructural length scale in our piezometric calibration.

188 *2.3 Sensitivity Tests*

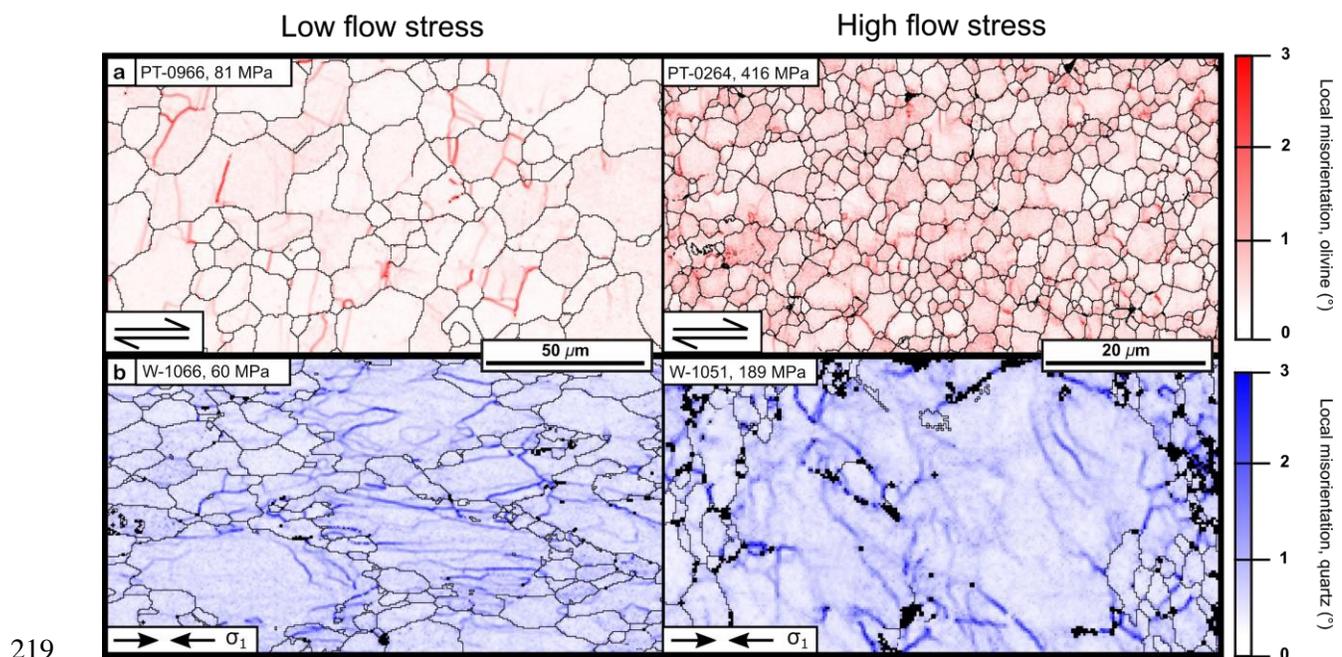
189 As EBSD maps only examine a portion of a deformed material, we devised two tests to assess
190 whether a mapped area is representative of the bulk deformation. These tests examine the effect of the
191 size and spatial resolution of the map on the measured values of mean intercept length. MATLAB[®]
192 scripts to perform these tests are presented in the Supplemental Material (Text S1).

193 As increasing the step size of an EBSD map leads to overestimates of grain size (Cross et al.,
194 2017; Humphreys, 2001), we tested the influence of step size on measured subgrain size. We evaluated
195 the spatial resolution by implementing the same step size analysis test as Cross et al. (2017). In this
196 procedure, the resolution of the map is artificially reduced (i.e., the effective step size increased) by
197 selecting subsets of points in the map on a regular grid. The line-intercept length is then measured and
198 compared to the mean-line intercept length associated with the smallest step size, λ_{best} . We refer to the
199 ratio of λ to λ_{best} as the intercept variation factor. The spatial resolution is deemed sufficient if the
200 measured mean intercept length is not sensitive to the effective step size. For each sample in Figures 1d
201 and S2, decreasing the pixels per intercept length (defined as the λ_{best} divided by the effective step size)
202 had an insignificant effect on the mean line-intercept length. The presence of an asymptote at an
203 intercept variation factor of 1 is evidence that step size is small enough to capture the mean intercept
204 length.

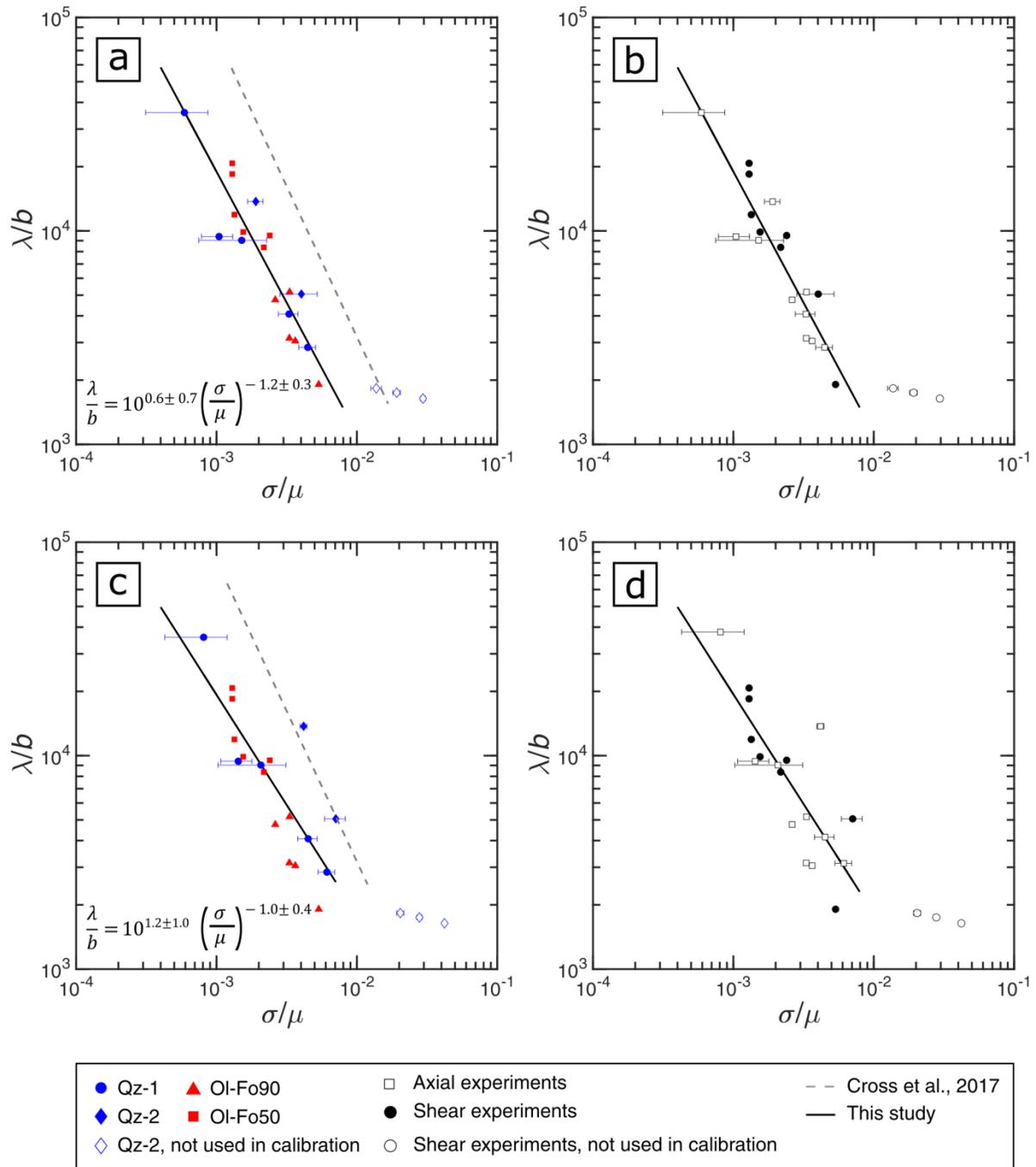
205 In the second test, we evaluated the size of the map relative to the mean intercept length, that is,
206 whether a sufficient number of intercepts were measured for their mean value to be representative of the
207 sample mean. We propose that, rather than being fixed (Humphreys, 2001, 2004; Valcke et al., 2006),
208 the number of required subgrains (or intercept lengths) is likely to depend on the variance of the true
209 subgrain-size distribution. Therefore, for each map, we tested the effect of map area on the mean
210 intercept length by measuring the mean intercept length from a centred sub-area of the original map.
211 Initially, this sub-area was 1% of the size of the original map. We then measured the mean intercept

212 length as the sub-area was progressively increased in size. As the size of the sub-area increases, the mean
 213 intercept length should asymptotically approach the mean for the entire map, indicating the full map area
 214 is sufficiently large. Examples of the area-analysis technique are presented in Figures 1e and S3.
 215 Samples that demonstrated a strong dependence of mean line-intercept length on the size of the sub-area
 216 (e.g., Figure S4) were mapped multiple times. The mean intercept length was then calculated as the
 217 average intercept length across all the maps to ensure representative measurement.

218 3. Results



220 Figure 2: Maps of local misorientation for (a) olivine and (b) quartz samples deformed at low and high flow
 221 stresses. Black lines are grain boundaries (misorientation $\geq 10^\circ$). Unindexed pixels are also plotted in black.
 222 Experiments conducted at high flow stresses have higher densities of subgrain boundaries.



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224 Figure 3: Mean line-intercept length, normalised by the Burgers vector as a function of the equivalent stress,

225 normalised by the shear modulus. In (a) and (b) the correction from Holyoke and Kronenberg (2010) was applied

226 to the quartz data, whereas in (c) and (d) the correction was not applied. (a) and (c) data are coloured by phase,

227 with the recrystallised grain-size piezometer of Cross et al. (2017), also calibrated for EBSD, plotted for

228 comparison. (b) and (d) plot the same data as in (a) and (c), respectively, coloured by deformation geometry. Axial
 229 experiments refer to those conducted in pure shear and shear experiments refer to those conducted in general
 230 shear or simple shear.

231 To identify a general piezometric relationship applicable for both quartz and olivine, the
 232 equivalent stress and the mean intercept length were normalised by the shear modulus μ and the Burgers
 233 vector b respectively. We then explored the effect of the choice of critical misorientation angle on mean
 234 intercept length. We tested angles ranging from 1° to 10° (e.g., Figure 1c). We did not evaluate critical
 235 misorientation angles below 1° , the minimum angle that can be measured repeatedly and accurately with
 236 Hough-based EBSD (Humphreys, 2001, 2004; Wallis et al., 2016). Also we did not evaluate critical
 237 misorientation angles above 10° as we consider misorientations of $>10^\circ$ to be grain boundaries rather
 238 than subgrain boundaries. For all values of the critical misorientation angle, in all three datasets, the
 239 mean intercept length exhibits a power-law relationship with the equivalent stress (Figure S5). The three
 240 datasets coincide best at lower critical misorientation angles. The discrepancy between the quartz
 241 datasets and the olivine dataset increases as a function of increasing critical misorientation angle.
 242 Therefore, we used a critical misorientation angle of 1° in our calibrations.

243 We fit a power-law equation using least squares linear regression on the logarithmic
 244 transformation of mean intercept length against equivalent stress, yielding the following equations:

$$245 \quad \frac{\lambda}{b} = 10^{0.6 \pm 0.7} \left(\frac{\sigma}{\mu} \right)^{-1.2 \pm 0.3} \quad (\text{eq.1})$$

246 and

$$247 \quad \frac{\lambda}{b} = 10^{1.2 \pm 1.0} \left(\frac{\sigma}{\mu} \right)^{-1.0 \pm 0.4} \quad (\text{eq.2}).$$

248 Equations 1 and 2 represent piezometers with and without the calibration of Holyoke and Kronenberg
 249 (2010) discussed above in Section 2.11, respectively. Uncertainties are reported as 95% confidence

250 intervals. Here we use $b = 5.10 \times 10^{-4} \mu\text{m}$ or $5 \times 10^{-4} \mu\text{m}$ and $\mu = 4.2 \times 10^4 \text{ MPa}$ or $7.78/6.26 \times 10^4 \text{ MPa}$ for
251 quartz and olivine ($\text{Fo}_{90}/\text{Fo}_{50}$), respectively (see supplementary Text S2 for discussion).

252 **4. Discussion**

253 The organization of dislocations into subgrain boundaries is driven by the associated reduction
254 in the strain energy of the system (e.g., Raj & Pharr, 1986; Read, 1953, page 226). During deformation,
255 the mean subgrain size varies systematically with the applied stress. Normalising the stress by the shear
256 modulus and the subgrain size by the Burgers vector collapses mineral-specific piezometers into a single
257 relationship (e.g., Twiss, 1986). Our results thus define a subgrain-size piezometer, which can be used on
258 multiple minerals. As our piezometer is calibrated by EBSD, it differs from calibrations obtained by
259 different measurement techniques (Durham & Goetze, 1977; Goetze, 1975; Karato et al., 1980; Mercier
260 et al., 1977; Toriumi, 1979). We also provide a set of tests that assess the suitability of a dataset for
261 analysis by this method based on factors including the number of linear intercepts, the step size, and the
262 map area. The ability to perform these tests routinely in an automated and objective manner provides
263 clear benefits over existing quality control measures (e.g., Humphreys, 2001, 2004; Valcke et al., 2006).

264 Subgrain-size piezometry is beneficial compared to grain-size piezometry in several ways. First,
265 the most significant advantage of subgrain-size piezometry over grain-size piezometry is that the former
266 is insensitive to the presence of secondary minerals and the pinning of grain boundaries (Hansen &
267 Warren, 2015; White, 1979). As most rocks are polymineralic and the presence of secondary phases
268 leads to smaller-than-expected recrystallised grains, the majority of existing stress estimates were
269 derived from spatially restricted monomineralic rocks or domains. In contrast, in polymineralic rocks,
270 subgrain-size piezometry should record the average stress supported by the analysed phase, regardless of
271 the fraction of secondary phases. Thus, the subgrain-size piezometer can be used to analyse the stress
272 supported by each phase deforming by dislocation creep in polymineralic rocks. Consequently, grain-

273 size piezometry based estimates of stresses supported by the lithosphere (e.g., Behr & Platt, 2011;
274 Weathers et al., 1979; White, 1979) can be tested against new data acquired using subgrain-size
275 piezometry on more representative rock types.

276 Grain-size piezometry also requires the user to distinguish between recrystallised and relict
277 grains, the proportions of which depend on total strain. Previously, the bimodal grain-size distribution of
278 partially recrystallised rocks allowed the characterization of recrystallised and relict grains on the basis
279 of size (e.g., Post & Tullis, 1999; Stipp & Tullis, 2003). This method truncates the grain-size
280 distribution, thereby modifying the mean grain size and the resulting stress calculated from that grain
281 size. More recent work used the degree of intracrystalline lattice distortion within each grain to identify
282 recrystallised grains on the assumption that relict grains have a greater degree of internal distortion than
283 recrystallised grains (Cross et al., 2017). Although this new method provides a working calibration, it
284 adds additional steps and assumptions to the analysis. In deforming materials with active subgrain
285 formation, both recrystallized and relict grains develop subgrain boundaries which fall on a single
286 piezometric relationship (Ross et al., 1980). As our calibration contains subgrains both from relict and
287 recrystallised grains, as long as both sets of grains contain subgrains in the sample to be analysed, no
288 distinction between them is necessary in measuring subgrain size. Instead, we only need to define a
289 critical misorientation angle. The 1° critical misorientation angle fits with previous observations that
290 subgrain boundaries tend to have misorientation angles $< 2^\circ$ at strains of 15% and $< 5^\circ$ at strains of 50%
291 (Pennock et al., 2005) In addition, Trimby et al. (1998), observed subgrains in relict and recrystallized
292 grains were the same size based on a 1° critical misorientation.

293 Finally, subgrain-size piezometry is independent of flow geometry. In contrast, samples
294 deformed in general shear and axial compression may exhibit different grain sizes at the same equivalent
295 stress (Heilbronner & Kilian, 2017). As observed by Heilbronner and Kilian (2017), different kinematics
296 in subdomains of deformed quartzites lead to different crystallographic preferred orientations (CPOs).
297 Different CPOs may reflect differences in the activity of different slip systems, which in turn may affect

298 the mean size of recrystallized grains. Thus, as demonstrated in the compilation of data for quartz
299 presented by Tokle et al. (2019), experiments conducted in simple shear yield a different grain-size
300 piezometer than experiments conducted in axial compression. To explore whether this hypothesis holds
301 true for subgrain sizes, we regrouped the data according to whether the samples were deformed in a pure
302 shear (i.e., axial compression) or general or simple shear, geometry. In Figures 3b and 3d, there is no
303 obvious dependence of the mean intercept length on the deformation geometry. Therefore, we suggest
304 that our single subgrain-size piezometer can be applied to a wide range of rocks, regardless of flow
305 geometry or CPO.

306 It is necessary to highlight two potential limitations of subgrain-size piezometry. First, it appears
307 that the observed relationship between subgrain size and stress is not applicable to deformation at high
308 stresses (Figure 3). The relationship between subgrain size and stress may change at higher stresses as
309 the recrystallization mechanisms changes, similar to the relationships observed for the size of
310 recrystallised grains of quartz (Stipp & Tullis, 2003), which is why the three samples deformed in this
311 high-stress regime were not included in our calibrations. Similarly, differences in the processes of
312 subgrain formation or in the mechanisms of dynamic recrystallisation might require different calibrations
313 at significantly low stresses (e.g., Valcke et al., 2007, 2015; Stipp et al., 2010). Therefore, we
314 recommend that our piezometer should be applied over the normalised subgrain size and stress range
315 over which it was calibrated. This range corresponds to mean line-intercept lengths of 1–9 μm for
316 olivine and 1–18 μm for quartz and a similar range for other silicate minerals. These limits on subgrain
317 size correspond to stress ranges of 60–420 MPa and 20–240 MPa for olivine and quartz, respectively.

318 Second, the potential for modifying subgrain size through static annealing or stress relaxation
319 after deformation remains poorly constrained. Ross et al. (1980) suggested that subgrains record the
320 highest stress in rocks subjected to complex deformation histories. However, we demonstrate a strong
321 correlation between subgrain size and final stress is apparent, even in cases in which the larger stresses
322 were experienced earlier in the deformation history (Hansen et al., 2012; Holyoke & Tullis, 2006).

323 Furthermore, experiments in steel by Qin et al. (2003) revealed that subgrains were only able to coarsen
324 with additional strain while under stress of a reduced magnitude, whereas they did not coarsen during
325 static annealing. These observations suggest that subgrain sizes best reflect the last increments of
326 deformation, although further work is clearly required to fully investigate the mobility of subgrain
327 boundaries in minerals. If the subsequent modification of subgrain size occurs on a different timescale
328 than the modification of other microstructural features such as dislocation density or recrystallized grain
329 size, then combined analysis using multiple piezometers may yield information about complex stress
330 histories (Kohlstedt & Weathers, 1980; White, 1979).

331 **5. Conclusions**

- 332 1. We present a subgrain-size piezometer calibrated for EBSD with a 1° critical
333 misorientation angle. This piezometer, which was derived from data for olivine and
334 quartz should be applicable to other phases.
- 335 2. The size of subgrains calculated based on a critical misorientation angle of 1° appears to
336 be independent of the deformation geometry, that is, whether the specimen is deformed
337 in simple/general shear or pure shear.
- 338 3. It is recommended that our piezometer should be applied over the normalised subgrain
339 size and stress range with which it was calibrated. This corresponds to mean line-
340 intercept lengths of 1 to 9 μm for olivine and 1 to 18 μm for quartz corresponding to
341 stresses of 60 – 420 MPa and 20 – 240 MPa, respectively
- 342 4. MATLAB[®] scripts, provided in the Supplemental Material, can be used to test the
343 suitability of input data for stress estimates specifically in terms of spatial resolution and
344 size of the data set.

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354 **References**

355 Abramson, E. H., Brown, J. M., Slutsky, L. J., & Zaug, J. (1997). The elastic constants of San Carlos
356 olivine to 17 GPa. *Journal of Geophysical Research*, *102*(B6), 12253–12263.

357 <https://doi.org/10.1029/97JB00682>

358 Austin, N., Evans, B., Herwegh, M., & Ebert, A. (2008). Strain localization in the Morcles nappe
359 (Helvetic Alps, Switzerland). *Swiss Journal of Geosciences*, *101*(2), 341–360.

360 <https://doi.org/10.1007/s00015-008-1264-2>

361 Behr, W. M., & Platt, J. P. (2011). A naturally constrained stress profile through the middle crust in an
362 extensional terrane. *Earth and Planetary Science Letters*, *303*(3), 181–192.

363 <https://doi.org/10.1016/j.epsl.2010.11.044>

364 Behr, W. M., & Platt, J. P. (2014). Brittle faults are weak, yet the ductile middle crust is strong:
365 Implications for lithospheric mechanics. *Geophysical Research Letters*, *41*(22), 8067–8075.

366 <https://doi.org/10.1002/2014GL061349>

367 Biberger, M., & Blum, W. (1992). Subgrain boundary migration during creep of lif: I. Recombination of
368 subgrain boundaries. *Philosophical Magazine A*, *65*(3), 757–770.

369 <https://doi.org/10.1080/01418619208201548>

- 370 Birch, F. (1966). Compressibility; elastic constants. In S.P. Clark (Eds.), *Handbook of Physical*
371 *Constants* (pp. 169). New York, NY: The Geological Society of America.
- 372 Britton, T. B., & Wilkinson, A. J. (2011). Measurement of residual elastic strain and lattice rotations
373 with high resolution electron backscatter diffraction. *Ultramicroscopy*, *111*(8), 1395–1404.
374 <https://doi.org/10.1016/j.ultramic.2011.05.007>
- 375 Britton, T. B., & Wilkinson, A. J. (2012). Stress fields and geometrically necessary dislocation density
376 distributions near the head of a blocked slip band. *Acta Materialia*, *60*(16), 5773–5782.
377 <https://doi.org/10.1016/j.actamat.2012.07.004>
- 378 Cross, A. J., Prior, D. J., Stipp, M., & Kidder, S. (2017). The recrystallized grain size piezometer for
379 quartz: An EBSD-based calibration. *Geophysical Research Letters*, *44*(13), 6667–6674.
380 <https://doi.org/10.1002/2017GL073836>
- 381 Deer, W. A., Howie, R. A., & Zussman, J. (1992). *An introduction to the rock-forming minerals*. 2nd ed.
382 Harlow, Essex, England: New York, NY: Longman Scientific & Technical.
- 383 Durham, W. B., & Goetze, C. (1977). Plastic flow of oriented single crystals of olivine: 1. Mechanical
384 data. *Journal of Geophysical Research*, *82*(36), 5737–5753.
385 <https://doi.org/10.1029/JB082i036p05737>
- 386 Evans, B., Renner, J., & Hirth, G. (2001). A few remarks on the kinetics of static grain growth in rocks.
387 *International Journal of Earth Sciences*, *90*(1), 88–103. <https://doi.org/10.1007/s005310000150>
- 388 Friedman, M., & Higgs, N. G. (1981). Calcite Fabrics in Experimental Shear Zones. In N.L. Carter, M.
389 Friedman, J.M. Logan, D.W. Stearns (Eds.), *Mechanical Behavior of Crustal Rocks: The Handin*
390 *Volume* (pp. 11–27). Washington, DC: American Geophysical Union.
- 391 Gleason, G. C., & Tullis, J. (1995). A flow law for dislocation creep of quartz aggregates determined
392 with the molten salt cell. *Tectonophysics*, *247*(1-4), 1–23. [https://doi.org/10.1016/0040-](https://doi.org/10.1016/0040-1951(95)00011-B)
393 [1951\(95\)00011-B](https://doi.org/10.1016/0040-1951(95)00011-B)
- 394 Goetze, C. (1975). Sheared Iherzolites: From the point of view of rock mechanics. *Geology*, *3*(4), 172–

- 395 173. [https://doi.org/10.1130/0091-7613\(1975\)3<172:SIFTPO>2.0.CO;2](https://doi.org/10.1130/0091-7613(1975)3<172:SIFTPO>2.0.CO;2)
- 396 Gueydan, F., Mehl, C., & Parra, T. (2005). Stress-strain rate history of a midcrustal shear zone and the
397 onset of brittle deformation inferred from quartz recrystallized grain size. In D. Gapais, J.P. Brun &
398 P.R. Cobbold (Eds.), *Deformation Mechanisms, Rheology and Tectonics: from Minerals to the*
399 *lithosphere* (Special Publications 243, p. 127–142) London, UK: *Geological Society*.
400 <https://doi.org/10.1029/GM024p0011>
- 401 Haertel, M., & Herwegh, M. (2014). Microfabric memory of vein quartz for strain localization in
402 detachment faults: A case study on the Simplon fault zone. *Journal of Structural Geology*, 68, 16–
403 32. <https://doi.org/10.1016/j.jsg.2014.08.001>
- 404 Hansen, L. N., & Warren, J. M. (2015). Quantifying the effect of pyroxene on deformation of peridotite
405 in a natural shear zone. *Journal of Geophysical Research, Solid Earth*, 120(4), 2717–2738.
406 <https://doi.org/10.1002/2014JB011584>
- 407 Hansen, L. N., Zimmerman, M. E., & Kohlstedt, D. L. (2011). Grain boundary sliding in San Carlos
408 olivine: Flow law parameters and crystallographic-preferred orientation. *Journal of Geophysical*
409 *Research, Solid Earth*, 116(B8), B08201. <https://doi.org/10.1029/2011JB008220>
- 410 Hansen, L. N., Zimmerman, M. E., & Kohlstedt, D. L. (2012). The influence of microstructure on
411 deformation of olivine in the grain-boundary sliding regime. *Journal of Geophysical Research,*
412 *Solid Earth*, 117(B9), B09201. <https://doi.org/10.1029/2012JB009305>
- 413 Hansen, L. N., Cheadle, M. J., John, B. E., Swapp, S. M., Dick, H. J. B., Tucholke, B. E., & Tivey, M.
414 A. (2013). Mylonitic deformation at the Kane oceanic core complex: Implications for the
415 rheological behavior of oceanic detachment faults. *Geochemistry, Geophysics, Geosystems*, 14(8),
416 3085–3108. <https://doi.org/10.1002/ggge.20184>
- 417 Heilbronner, R., & Kilian, R. (2017). The grain size(s) of Black Hills Quartzite deformed in the
418 dislocation creep regime. *Solid Earth*, 8(6), 1071–1093. <https://doi.org/10.5194/se-8-1071-2017>
- 419 Heilbronner, R., & Tullis, J. (2002). The effect of static annealing on microstructures and

- 420 crystallographic preferred orientations of quartzites experimentally deformed in axial compression
421 and shear. *Geological Society, London, Special Publications*, 200(1), 191–218.
422 <https://doi.org/10.1144/GSL.SP.2001.200.01.12>
- 423 Heilbronner, R., & Tullis, J. (2006). Evolution of c axis pole figures and grain size during dynamic
424 recrystallization: Results from experimentally sheared quartzite. *Journal of Geophysical Research*,
425 111(B10), B10202. <https://doi.org/10.1029/2005JB004194>
- 426 Hiraga, T., Tachibana, C., Ohashi, N., & Sano, S. (2010). Grain growth systematics for forsterite ±
427 enstatite aggregates: Effect of lithology on grain size in the upper mantle. *Earth and Planetary
428 Science Letters*, 291(1-4), 10–20. <https://doi.org/10.1016/j.epsl.2009.12.026>
- 429 Hirth, G., & Tullis, J. (1992). Dislocation creep regimes in quartz aggregates. *Journal of Structural
430 Geology*, 14(2), 145–159. [https://doi.org/10.1016/0191-8141\(92\)90053-Y](https://doi.org/10.1016/0191-8141(92)90053-Y)
- 431 Hirth, G., Teyssier, C., & Dunlap, J. W. (2001). An evaluation of quartzite flow laws based on
432 comparisons between experimentally and naturally deformed rocks. *International Journal of Earth
433 Sciences*, 90, 77–87. <https://doi.org/10.1007/s005310000152>
- 434 Holyoke, C. W., III, & Kronenberg, A. K. (2010). Accurate differential stress measurement using the
435 molten salt cell and solid salt assemblies in the Griggs apparatus with applications to strength,
436 piezometers and rheology. *Tectonophysics*, 494(1-2), 17–31.
437 <https://doi.org/10.1016/j.tecto.2010.08.001>
- 438 Holyoke, C. W., III, & Kronenberg, A. K. (2013). Reversible water weakening of quartz. *Earth and
439 Planetary Science Letters*, 374, 185–190. <https://doi.org/10.1016/j.epsl.2013.05.039>
- 440 Holyoke, C. W., III, & Tullis, J. (2006). Mechanisms of weak phase interconnection and the effects of
441 phase strength contrast on fabric development. *Journal of Structural Geology*, 28(4), 621–640.
442 <https://doi.org/10.1016/j.jsg.2006.01.008>
- 443 Humphreys, F. J. (2001). Grain and subgrain characterisation by electron backscatter diffraction. *Journal
444 of Materials Science*, 36(16), 3833–3854. <https://doi.org/10.1023/A:1017973432592>

- 445 Humphreys, F. J. (2004). Characterisation of fine-scale microstructures by electron backscatter
446 diffraction (EBSD). *Scripta Materialia*, 51(8), 771–776.
447 <https://doi.org/10.1016/j.scriptamat.2004.05.016>
- 448 Jaroslow, G. E., Hirth, G., & Dick, H. J. B. (1996). Abyssal peridotite mylonites: implications for grain-
449 size sensitive flow and strain localization in the oceanic lithosphere. *Tectonophysics*, 256(1), 17–37.
450 [https://doi.org/10.1016/0040-1951\(95\)00163-8](https://doi.org/10.1016/0040-1951(95)00163-8)
- 451 Karato, S.-I. (2012). *Deformation of Earth Materials: An Introduction to the Rheology of Solid Earth*
452 Cambridge UK: Cambridge University Press.
- 453 Karato, S.-I., Toriumi, M., & Fujii, T. (1980). Dynamic recrystallization of olivine single crystals during
454 high temperature creep. *Geophysical Research Letters*, 7(9), 649–652.
455 <https://doi.org/10.1029/GL007i009p00649>
- 456 Kohlstedt, D. L., & Weathers, M. S. (1980). Deformation-Induced Microstructures, Paleopiezometers,
457 and Differential Stresses in Deeply Eroded Fault Zones. *Journal of Geophysical Research*, 85(B11),
458 6269–6285. <https://doi.org/10.1029/JB085iB11p06269>
- 459 Linckens, J., Herwegh, M., Müntener, O., & Mercolli, I. (2011). Evolution of a polymineralic mantle
460 shear zone and the role of second phases in the localization of deformation. *Journal of Geophysical*
461 *Research*, 116(B6), B06210. <https://doi.org/10.1029/2010JB008119>
- 462 Luton, M. J., & Sellars, C. M. (1969). Dynamic recrystallization in nickel and nickel-iron alloys during
463 high temperature deformation. *Acta Metallurgica*, 17(8), 1033–1043. [https://doi.org/10.1016/0001-](https://doi.org/10.1016/0001-6160(69)90049-2)
464 [6160\(69\)90049-2](https://doi.org/10.1016/0001-6160(69)90049-2)
- 465 Mackwell, S. J., & Paterson, M. S. (2002). New Developments in Deformation Studies: High-Strain
466 Deformation. *Reviews in Mineralogy and Geochemistry*, 51(1), 1–19.
467 <https://doi.org/10.2138/gsrng.51.1.1>
- 468 Mao, Z., Fan, D., Lin, J.-F., Yang, J., Tkachev, S.N., Zhuravlev, K., & Prakapenka, V.B. (2015).
469 Elasticity of single-crystal olivine at high pressures and temperatures. *Earth and Planetary Science*

- 470 *Letters*, 426, 204–215. <https://doi.org/10.1016/j.epsl.2015.06.045>.
- 471 Mercier, J.-C. C., Anderson, D. A., & Carter, N. L. (1977). Stress in the Lithosphere: Inferences from
472 Steady State Flow of Rocks. In M. Wyss (Eds.), *Stress in the Earth* (pp. 199–226). Birkhäuser,
473 Basel. https://doi.org/10.1007/978-3-0348-5745-1_12
- 474 Mingard, K. P., Roebuck, B., Bennett, E. G., Thomas, M., Wynne, B. P., & Palmiere, E. J. (2007). Grain
475 size measurement by EBSD in complex hot deformed metal alloy microstructures. *Journal of*
476 *Microscopy*, 227(3), 298–308. <https://doi.org/10.1111/j.1365-2818.2007.01814.x>
- 477 Paterson, M. S. (1990), Rock deformation experimentation, In A. G. Duba and W. B. Durham, H. C.
478 Heard, J. W., Handin, H. F., Wang (Eds.), *The Brittle Ductile Transition in Rocks, The Heard*
479 *Volume, Geophysical Monograph Series* (Vol. 56, pp. 187–194). AGU, Washington, D. C.:
480 American Geophysical Union.
- 481 Paterson, M. S., & Olgaard, D. L. (2000). Rock deformation tests to large shear strains in torsion.
482 *Journal of Structural Geology*, 22(9), 1341–1358. [https://doi.org/10.1016/S0191-8141\(00\)00042-0](https://doi.org/10.1016/S0191-8141(00)00042-0)
- 483 Peng, Z., & Redfern, S. A. T. (2013). Mechanical properties of quartz at the α - β phase transition:
484 Implications for tectonic and seismic anomalies. *Geochemistry, Geophysics, Geosystems*, 14(1), 18–
485 28. <https://doi.org/10.1029/2012GC004482>
- 486 Pennock, G. M., Drury, M. R., & Spiers, C. J. (2005). The development of subgrain misorientations with
487 strain in dry synthetic NaCl measured using EBSD. *Journal of Structural Geology*, 27(12), 2159–
488 2170. <https://doi.org/10.1016/j.jsg.2005.06.013>
- 489 Platt, J. P., & De Bresser, J. H. P. (2017). Stress dependence of microstructures in experimentally
490 deformed calcite. *Journal of Structural Geology*, 105, 80–87.
491 <https://doi.org/10.1016/j.jsg.2017.10.012>
- 492 Poirier, J. P., & Nicolas, A. (1975). Deformation-Induced Recrystallization Due to Progressive
493 Misorientation of Subgrains, with Special Reference to Mantle Peridotites. *The Journal of Geology*,
494 83(6), 707–720. <https://doi.org/10.1086/628163>

- 495 Pommier, A., Leinenweber, K., Kohlstedt, D. L., Qi, C., Garnero, E. J., Mackwell, S. J., & Tyburczy, J.
496 A. (2015). Experimental constraints on the electrical anisotropy of the lithosphere–asthenosphere
497 system. *Nature*, *522*, 202. <https://doi.org/10.1038/nature14502>
- 498 Post, A., & Tullis, J. (1999). A recrystallized grain size piezometer for experimentally deformed feldspar
499 aggregates. *Tectonophysics*, *303*(1), 159–173. [https://doi.org/10.1016/S0040-1951\(98\)00260-1](https://doi.org/10.1016/S0040-1951(98)00260-1)
- 500 Qin, Y., Götz, G., & Blum, W. (2003). Subgrain structure during annealing and creep of the cast
501 martensitic Cr-steel G-X12CrMoWVNbN 10-1-1. *Materials Science and Engineering: A*, *341*(1),
502 211–215. [https://doi.org/10.1016/S0921-5093\(02\)00215-0](https://doi.org/10.1016/S0921-5093(02)00215-0)
- 503 Raj, S. V., & Pharr, G. M. (1986). A Compilation and Analysis of Data for the Stress Dependence of the
504 Subgrain size. *Materials Science and Engineering*, *81*, 217–237. [https://doi.org/10.1016/0025-](https://doi.org/10.1016/0025-5416(86)90265-X)
505 [5416\(86\)90265-X](https://doi.org/10.1016/0025-5416(86)90265-X)
- 506 Read, W. T. (1953). *Dislocations in crystals*. New York, NY: McGraw-Hill.
- 507 Ross, J. V., Ave Lallemand, H. G., & Carter, N. L. (1980). Stress dependence of recrystallized-grain and
508 subgrain size in olivine. *Tectonophysics*, *70*(1-2), 39–61. [https://doi.org/10.1016/0040-](https://doi.org/10.1016/0040-1951(80)90020-7)
509 [1951\(80\)90020-7](https://doi.org/10.1016/0040-1951(80)90020-7)
- 510 Rutter, E. H. (1995). Experimental study of the influence of stress, temperature, and strain on the
511 dynamic recrystallization of Carrara marble. *Journal of Geophysical Research, Solid Earth*,
512 *100*(B12), 24651–24663. <https://doi.org/10.1029/95JB02500>
- 513 Schmid, S. M., Paterson, M. S., & Boland, J. N. (1980). High temperature flow and dynamic
514 recrystallization in carrara marble. *Tectonophysics*, *65*(3), 245–280. [https://doi.org/10.1016/0040-](https://doi.org/10.1016/0040-1951(80)90077-3)
515 [1951\(80\)90077-3](https://doi.org/10.1016/0040-1951(80)90077-3)
- 516 Shimizu, I. (1998). Stress and temperature dependence of recrystallized grain size: A subgrain
517 misorientation model. *Geophysical Research Letters*, *25*(22), 4237–4240.
518 <https://doi.org/10.1029/1998GL900136>
- 519 Shimizu, I. (2008). Theories and applicability of grain size piezometers: The role of dynamic

- 520 recrystallization mechanisms. *Journal of Structural Geology*, 30(7), 899–917.
521 <https://doi.org/10.1016/j.jsg.2008.03.004>
- 522 Skemer, P., Warren, J. M., Kelemen, P. B., & Hirth, G. (2010). Microstructural and Rheological
523 Evolution of a Mantle Shear Zone. *Journal of Petrology*, 51(1-2), 43–53.
524 <https://doi.org/10.1093/petrology/egp057>
- 525 Skemer, P., Warren, J. M., Hansen, L. N., Hirth, G., & Kelemen, P. B. (2013). The influence of water
526 and LPO on the initiation and evolution of mantle shear zones. *Earth and Planetary Science Letters*,
527 375, 222–233. <https://doi.org/10.1016/j.epsl.2013.05.034>
- 528 Smith, C. S. (1948). Zener pinning. *Transactions of the Metallurgical Society of AIME*, 175, 15–51. New
529 York, NY: American institute of mining metallurgical and petroleum engineers.
- 530 Speckbacher, R., Behrmann, J. H., Nagel, T. J., Stipp, M., & Devey, C. W. (2011). Splitting a continent:
531 Insights from submarine high-resolution mapping of the Moresby Seamount detachment, offshore
532 Papua New Guinea. *Geology*, 39(7), 651–654. <https://doi.org/10.1130/G31931.1>
- 533 Stipp, M., & Tullis, J. (2003). The recrystallized grain size piezometer for quartz. *Geophysical Research*
534 *Letters*, 30(21), 2088. <https://doi.org/10.1029/2003GL018444>
- 535 Stipp, M., Stünitz, H., Heilbronner, R., & Schmid, M. (2002). Dynamic recrystallization of quartz:
536 correlation between natural and experimental conditions. In: S. De Meer, M.R. Drury, J.H.P. De
537 Bresser & G.M. Pennock, (Eds.): *Deformation Mechanisms, Rheology and Tectonics: Current*
538 *Status and Future Perspectives* (Special Publications 200, pp. 171-190). London, UK: Geological
539 Society of London, . <https://doi.org/10.1144/GSL.SP.2001.200.01.11>
- 540 Stipp, M., Tullis, J., Scherwath, M., & Behrmann, J. H. (2010). A new perspective on paleopiezometry:
541 Dynamically recrystallized grain size distributions indicate mechanism changes. *Geology*, 38(8),
542 759–762. <https://doi.org/10.1130/G31162.1>
- 543 Tasaka, M., Zimmerman, M. E., & Kohlstedt, D. L. (2016). Evolution of the rheological and
544 microstructural properties of olivine aggregates during dislocation creep under hydrous conditions.

- 545 *Journal of Geophysical Research, Solid Earth*, 121(1), 92–113.
546 <https://doi.org/10.1002/2015JB012134>
- 547 Tasaka, M., Zimmerman, M. E., & Kohlstedt, D. L. (2017). Rheological weakening of Olivine +
548 Orthopyroxene aggregates due to phase mixing: 1. Mechanical Behavior. *Journal of Geophysical*
549 *Research, Solid Earth*, 122(10), 7584–7596. <https://doi.org/10.1002/2017JB014333>
- 550 Tasaka, M., Zimmerman, M. E., Kohlstedt, D. L., Stünitz, H., & Heilbronner, R. (2017). Rheological
551 weakening of olivine+ orthopyroxene aggregates due to phase mixing: Part 2. Microstructural
552 development. *Journal of Geophysical Research, Solid Earth*, 122(10), 7597–7612.
553 <https://doi.org/10.1002/2017JB014311>
- 554 Thatcher, W., & Pollitz, F. F. (2008). Temporal evolution of continental lithospheric strength in actively
555 deforming regions. *GSA Today: A Publication of the Geological Society of America*, 18(4/5), 4–11.
556 <https://doi.org/10.1130/GSAT01804-5A>
- 557 Tokle, L., Hirth, G., & Behr, W. M. (2019). Flow laws and fabric transitions in wet quartzite. *Earth and*
558 *Planetary Science Letters*, 505, 152–161. <https://doi.org/10.1016/j.epsl.2018.10.017>
- 559 Toriumi, M. (1979). Relation between dislocation density and subgrain size of naturally deformed
560 olivine in peridotites. *Contributions to Mineralogy and Petrology*, 68(2), 181–186.
561 <https://doi.org/10.1007/BF00371899>
- 562 Trimby, P., Day, A., Mehnert, K., & Schmidt, N.-H. (2002). Is fast mapping good mapping? A review of
563 the benefits of high-speed orientation mapping using electron backscatter diffraction. *Journal of*
564 *Microscopy*, 205(3), 259–269. <https://doi.org/10.1046/j.1365-2818.2002.00995.x>
- 565 Trimby, P. W., Prior, D. J., & Wheeler, J. (1998). Grain boundary hierarchy development in a quartz
566 mylonite. *Journal of Structural Geology*, 20(7), 917–935. [https://doi.org/10.1016/S0191-](https://doi.org/10.1016/S0191-8141(98)00026-1)
567 [8141\(98\)00026-1](https://doi.org/10.1016/S0191-8141(98)00026-1)
- 568 Twiss, R. J. (1986). Variable sensitivity piezometric equations for dislocation density and subgrain
569 diameter and their relevance to olivine and quartz. In B. E. Hobbs & H. C. Heard (Eds.), *Mineral*

- 570 *and Rock deformation: Laboratory studies: The Paterson Volume*. Washington, D.C: American
571 Geophysical Union. <https://doi.org/10.1029/GM036p0247>
- 572 Underwood, E. E. (1970). *Quantitative stereology*. Addison-Wesley Publishing Company.
- 573 Valcke, S. L. A., & De Bresser, J. H. P. (2015). Influence of deformation conditions on the development
574 of heterogeneous recrystallization microstructures in experimentally deformed Carrara marble.
575 *Geological Society*. <http://dx.doi.org/10.1144/SP409.4>
- 576 Valcke, S. L. A., Drury, M. R., de Bresser, J. H. P., & Pennock, G. M. (2007). Quantifying
577 Heterogeneous Microstructures: Core and Mantle Subgrains in Deformed Calcite. *Materials*
578 *Science Forum*. <https://doi.org/10.4028/0-87849-434-0.307>
- 579 Valcke, S. L. A., Pennock, G. M., Drury, M. R., & De Bresser, J. H. P. (2006). Electron backscattered
580 diffraction as a tool to quantify subgrains in deformed calcite. *Journal of Microscopy*, 224(3), 264–
581 276. <https://doi.org/10.1111/j.1365-2818.2006.01698.x>
- 582 Van der Wal, D., Chopra, P., Drury, M., & Gerald, J. F. (1993). Relationships between dynamically
583 recrystallized grain size and deformation conditions in experimentally deformed olivine rocks.
584 *Geophysical Research Letters*, 20(14), 1479–1482. <https://doi.org/10.1029/93GL01382>
- 585 Wallis, D., Hansen, L. N., Britton, T. B., & Wilkinson, A. J. (2016). Geometrically necessary dislocation
586 densities in olivine obtained using high-angular resolution electron backscatter diffraction.
587 *Ultramicroscopy*, 168, 34–45. <https://doi.org/10.1016/j.ultramic.2016.06.002>
- 588 Wallis, D., Parsons, A. J., & Hansen, L. N. (2017). Quantifying geometrically necessary dislocations in
589 quartz using HR-EBSD: Application to chessboard subgrain boundaries. *Journal of Structural*
590 *Geology*. <https://doi.org/10.1016/j.jsg.2017.12.012>
- 591 Warren, J. M., & Hirth, G. (2006). Grain size sensitive deformation mechanisms in naturally deformed
592 peridotites. *Earth and Planetary Science Letters*, 248(1–2), 438–450.
593 <https://doi.org/10.1016/j.epsl.2006.06.006>
- 594 Weathers, M. S., Bird, J. M., Cooper, R. F., & Kohlstedt, D. L. (1979). Differential stress determined

- 595 from deformation-induced microstructures of the Moine Thrust Zone. *Journal of Geophysical*
596 *Research, Solid Earth*, 84(B13), 7495–7509. <https://doi.org/10.1029/JB084iB13p07495>
- 597 Wex, S., Mancktelow, N. S., Camacho, A., & Pennacchioni, G. (2019). Interplay between seismic
598 fracture and aseismic creep in the Woodroffe Thrust, central Australia—Inferences for the rheology
599 of relatively dry continental mid-crustal levels. *Tectonophysics*, 758, 55–72.
600 <https://doi.org/10.1016/j.tecto.2018.10.024>
- 601 White, S. (1979). Grain and sub-grain size variations across a mylonite zone. *Contributions to*
602 *Mineralogy and Petrology*, 70(2), 193–202. <https://doi.org/10.1007/BF00374448>
- 603 Wilkinson, A. J. (1996). Measurement of elastic strains and small lattice rotations using electron back
604 scatter diffraction. *Ultramicroscopy*, 62(4), 237–247. [https://doi.org/10.1016/0304-3991\(95\)00152-](https://doi.org/10.1016/0304-3991(95)00152-2)
605 2
- 606 Wilkinson, A. J., & Randman, D. (2010). Determination of elastic strain fields and geometrically
607 necessary dislocation distributions near nanoindentations using electron back scatter diffraction.
608 *Philosophical Magazine*, 90(9), 1159–1177. <https://doi.org/10.1080/14786430903304145>
- 609 Wilkinson, A. J., Meaden, G., & Dingley, D. J. (2006). High resolution mapping of strains and rotations
610 using electron backscatter diffraction. *Materials Science and Technology*, 22(11), 1271–1278.
611 <https://doi.org/10.1179/174328406X130966>
- 612