

History and future of the Martian dynamo and implications of a hypothetical solid inner core

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Key Points:

- We develop a new internal structure and thermal evolution model to study dynamo regimes on rocky planets, using Mars as a first example.
- An early, thermally-driven Martian dynamo could be followed by a later, compositionally-driven dynamo, either in the past or the future.
- Detection of a solid inner core on Mars could imply that the Martian dynamo will reactivate at some point in the future.

Abstract

Although Mars does not possess a magnetic field today, parts of its crust are strongly magnetized, suggesting a limited early dynamo, likely powered by rapid heat flow from the core. If the core is undergoing crystallization, the associated compositional changes would provide an additional mechanism for driving convection—possibly the dominant driver for the Earth’s dynamo today. This raises the question: does the lack of a global dynamo field on Mars suggest the absence of a partially crystallized core? More generally, what is the range of possibilities for the history and future of the Martian dynamo and which scenarios would be ruled out by the presence or absence of a solid inner core? Here we develop a new internal structure, thermal evolution, and buoyancy flux model to investigate the conditions under which the Martian core could experience compositionally-driven convection, either in the past or the future. We show that the presence of a partially crystallized core is compatible with the lack of a dynamo today but that such a scenario implies the Martian dynamo could reactivate at some point in the future. We find that convection driven by top down core crystallization (iron snow) can occur only when light elements do not partition strongly into the liquid versus the solid phase. Our model identifies the key variables for determining which dynamo regimes are possible, can help in assessing implications of future observations relating to the Martian core, and forms the basis for further comparative study across rocky planets.

Plain Language Summary

Although Mars does not possess a magnetic field today, parts of its crust are strongly magnetized, suggesting an early field, likely powered by rapid heat flow from the core. For Earth, an additional, and possibly dominant, mechanism for powering the magnetic field arises from core crystallization. Does the lack of a magnetic field on Mars therefore imply its core is entirely liquid and not undergoing freezing? More generally, what is the range of possibilities for the history and future of the Martian magnetic field and which scenarios would be ruled out by confirming the presence or absence of a solid inner core? Here we develop a new model to investigate the conditions under which the Martian magnetic field could be driven by core freezing, either in the past or the future. We show that the presence of a partially crystallized core is compatible with the lack of a magnetic field today but that this would imply the Martian magnetic field could reactivate in the future. Our model identifies the key variables determining which scenarios are possible, can help in assessing the implications of observations relating to the Martian core, and forms the basis for comparative study across rocky planets.

1 Introduction

Planetary magnetism is a fundamental but imperfectly understood phenomenon that has the power to inform our understanding of the deep interiors and thermal histories of planetary bodies of all kinds (e.g., Stevenson et al. (1983); Stevenson (2003); Connerney (2015)). For terrestrial planets, convective motions in the electrically conductive liquid metallic core can drive a global scale self-sustaining magnetic field (dynamo) that shields the planet’s atmosphere and surface from the impinging solar wind and imparts thermoremanent magnetization in rocks as they form and cool at or near the planet’s surface, preserving a record of how the dynamo field may have changed over time (e.g., Purucker and Whaler (2015); Weiss and Tikoo (2014)). Paleomagnetic evidence has established that the Earth’s dynamo field has been active for at least the last ~ 3.5 Gyrs, and possibly longer (e.g., Tarduno et al. (2010, 2015)). By contrast, the case of Mars is interesting because it has no global dynamo field operating today and yet magnetometer and electron reflectometer data from the Mars Global Surveyor and MAVEN missions have established that large portions of the crust—particularly the ancient southern highlands—are extremely strongly magnetized (Acuña, 1999; Stevenson, 2001; Con-

nerney et al., 2005; Langlais et al., 2019), suggesting that a dynamo may have been active early in Mars’ history, but has since shut down.

The lack of magnetization in large impact basins like Hellas, Argyre, and Isidis, whose formation should have produced significant local heating and melt, is generally interpreted as evidence that the early Martian dynamo had shut down by the time these basins formed, roughly 500 Myrs after the formation of Mars (Lillis et al., 2008, 2013; Vervelidou et al., 2017), or even that the formation of the basins themselves could have initiated the shut down (Roberts et al., 2009). Several authors have previously studied the thermal evolution of Mars (e.g., Schubert et al. (1992); Zuber et al. (2000); Hauck and Phillips (2002)), with some studies focusing on the evolution of the Martian dynamo and what controls its timing (e.g., Stevenson et al. (1983); Nimmo and Stevenson (2000); J.-P. Williams and Nimmo (2004); Ke and Solomatov (2009); Landeau and Aubert (2011); Dietrich and Wicht (2013); Hori and Wicht (2013); O’Rourke and Shim (2019)). J.-P. Williams and Nimmo (2004), for example, showed that if the initial core-mantle temperature difference was sufficiently large, strong heat flow across the core mantle boundary (CMB) could have driven thermal convection in the liquid core for a limited period before the core became thermally stably stratified, naturally shutting down convection and the dynamo. However, it has also been suggested that a weak dynamo persisted or reactivated after the formation of the large basins (Schubert et al., 2000; Mittelholz et al., 2020), raising the question of what mechanisms and what conditions could permit such different dynamo histories.

The primary mechanisms for driving core convection are generally thought to be thermal (i.e., due to rapid core-mantle heat flow) and compositional (i.e., arising from compositional changes associated with core crystallization), though other mechanisms could be important as well. If the core is initially much hotter than the mantle, thermal convection will be effective at early times, but its effectiveness diminishes over time as the core and mantle cool. Compositional convection becomes more important later when parts of the core begin to drop below the melting temperature. The Earth’s core is believed to have been entirely liquid for an extended period until its central temperature fell below the high pressure melting curve for iron, which may have occurred as recently as ~ 1 Gyr ago (Labrosse et al., 2001; Gomi et al., 2013; Driscoll & Bercovici, 2014; Davies et al., 2015). Since then, a solid inner core has been growing, currently having a radius about 35% of the core’s total radius. As the core crystallizes, the tendency for lighter elements to partition preferentially into the liquid rather than being incorporated into the solid inner core means that light element rejection introduces a source of buoyancy at the inner core boundary which, for the present-day Earth, is likely an important, if not the dominant, source of buoyancy driving convection in the liquid outer core. At Mars, geodetic observations and interior modeling suggest that the core remains at least partially liquid today (Van Hoolst et al., 2003; Yoder et al., 2003; Rivoldini et al., 2011), but it is not known whether any portion of the Martian core is solid. The In-Sight lander, now operating on the Martian surface, includes a seismometer (SEIS; Banerdt et al. (2020)) and a radio science experiment (RISE; Folkner et al. (2018)) designed to study the deep interior, offering the possibility of confirming the presence or absence of a solid inner core within Mars’ otherwise liquid core. Anticipation of such results is one of the primary motivations for the present study.

This mechanism of compositionally-driven convection, which is thought to be so effective for Earth, thus raises the question of whether or not a solid inner core on Mars is compatible with the absence of a dynamo field at present—a key question in this study. In other words, under what conditions, if any, is it possible to have a crystallizing core without driving convection? If it becomes possible to detect a solid inner core and estimate its radius, what would this tell us about the history and future of the Martian dynamo? Even if compositionally-driven convection is not operating today, is it possible or likely that it has operated at any point in the past or that it will operate at some

point in the future, and what determines which of these scenarios is most likely? It has also been suggested that, owing to the much lower pressures in the Martian core, crystallization may occur from the top down rather than the bottom up—two regimes that could have very different effects on convection and dynamo generation (Hauck et al., 2006; Stewart et al., 2007; Breuer et al., 2015; Davies & Pommier, 2018). What factors determine the crystallization regime and when various types of convection could operate? How different would the results be with a different internal structure, or on a body that is larger or smaller than Mars?

To answer these questions, we have developed a new internal structure and thermal evolution model that tracks core and mantle heating and cooling resulting from radiogenic heating, heat flow across the core mantle boundary, conductive and eruptive heat loss to the surface, and the effects of gravitational energy and latent heat flow associated with core crystallization. We assume a well mixed core with an adiabatic temperature profile and we track the relationship between this core adiabat and the composition-dependent melting curve to determine when parts of the core may crystallize, whether from the bottom up (i.e., Earth-like solid inner core growth), or from the top down (i.e., as “iron snow”). We use an iterative procedure involving equations of state to compute a simplified, but physically reasonable radial density structure. Though not the focus of this first study, this will allow us to investigate the effects of varying the body’s size and internal structure. Finally, we compute both thermal and compositional buoyancy fluxes to determine how each may contribute to driving convection within the liquid part of the core. Apart from the specifics of approximating the iron-sulfur melting curve appropriate for Mars core conditions, the model we describe in section 2 is not specific to Mars. We aim for a planet-independent model in part because we intend to use it in future work to study other bodies like the Moon, Mercury, Venus, or terrestrial-like exoplanets, but also because this allows us to benchmark our model by verifying that it produces reasonable results for the case of the Earth. In section 3, we illustrate a series of possible Martian thermal evolution scenarios and undertake a systematic exploration of the large parameter space, identifying what types of convection could drive a dynamo, under what conditions, and when. In section 4, we summarize the various possible dynamo regimes, the factors that control their timing, and what can be concluded from future observations such as confirming the presence or absence of a solid inner core. Finally, we offer brief concluding remarks in section 5.

2 Methods

This section details the various components of our model. Because we use thermal and compositional buoyancy flux as a proxy for whether or not convection is possible, we begin in 2.1 with a discussion of buoyancy flux and how it is calculated. We show how the compositional buoyancy flux depends on the density anomalies arising from unequal partitioning of light elements into the liquid and solid phases upon freezing, and we describe how those density anomalies are calculated. Section 2.2 describes our method for using a Vinet equation of state and an iterative procedure to obtain a self-consistent internal structure describing the radial profiles of density, pressure, bulk modulus, compression, and thermal expansivity. We use this method to build interior models for both Earth and Mars, demonstrating that the model can be used for an arbitrary planet, with a minimum of body-specific parameters, permitting future comparative study of internal structure on convection and dynamo regimes. Section 2.3 describes the internal temperature structure and our approach for approximating the adiabatic core temperature profile (2.3.1) and its relationship to the melting curve, which depends on the core’s sulfur content (2.3.2), to identify when and where parts of the core may begin to crystallize. Core cooling is largely controlled by CMB heat flow, which is a function of the mantle temperature structure, described in 2.3.3. Section 2.3.3 includes our procedure for obtaining an internally consistent mantle temperature profile, consisting of a convect-

ing region between two conductive thermal boundary layers, whose thicknesses are functions of the temperature-dependent mantle viscosity. Finally, section 2.4 details the energy budget calculations, which include radiogenic heating, CMB heat flow, gravitational and latent heat terms associated with core crystallization (2.4.1), conductive heat flow across the thermal boundary layers at the base and top of the mantle and possible eruptive heat loss to the surface (2.4.2), and how this energy budget is used to compute the body's thermal evolution (2.4.3).

2.1 Buoyancy Flux

Dynamo generation depends on movement in the electrically conductive liquid portion of the core, which we take to arise from some combination of thermal and compositional convection (for this study, we neglect other possible sources, such as mechanical stirring, e.g., Dwyer et al. (2011); Le Bars et al. (2011)). We quantify the introduction of convection-inducing thermal or compositional density perturbations in terms of the buoyancy flux, defined as (e.g., Olson et al. (2017))

$$F = \frac{\rho'}{\rho_c} (\mathbf{g} \cdot \mathbf{u}) \quad (1)$$

where \mathbf{g} is the local gravitational acceleration, \mathbf{u} is the advective velocity (i.e., carrying the density perturbation), ρ_c is the core fluid's background density, and where the density perturbation is, in general, given by

$$\rho' = -\rho_c (\alpha T' + \beta \chi') \quad (2)$$

where α is the thermal expansivity and β is the compositional expansivity (T' represents a temperature perturbation and χ' represents a perturbation in chemical composition). Buoyancy flux describes the rate at which buoyancy is being introduced into the liquid portion of the core (in terms of force per unit mass times a volume flux, yielding units of m^2/s^3). As shown by Lister (2003), although quite different in form and emphasizing different terms, this buoyancy flux approach is fundamentally equivalent to the approach of tracking entropy production, at least as it relates to thermal and compositional convection. Rather than relating the dynamo strength to the total ohmic dissipation in the core, however, we evaluate whether or not thermal and/or compositional density anomalies introduce sufficient buoyancy to drive convection.

Thermal convection occurs when heat is removed from the core more rapidly than it can be conducted along an adiabatic temperature profile (i.e., when the temperature profile is superadiabatic), leading parcels of core fluid near the core mantle boundary (CMB) to cool, become dense, and sink. We express this effect in terms of the thermal buoyancy flux, obtained by requiring the thermal energy advection ($\int_V \rho_c c_c (\nabla \cdot (T' \mathbf{u})) dV$) to equal the superadiabatic heat flow, yielding (e.g., Driscoll and Bercovici (2014), eq. 36)

$$F_T = \frac{\alpha_c g_{\text{cmb}}}{\rho_c c_c} q_T \quad (3)$$

where α_c and ρ_c are the thermal expansivity and mean density of the fluid outer core, c_c is the core's specific heat capacity, g_{cmb} is the gravity at the CMB, and where q_T is the superadiabatic heat flux, given by

$$q_T = q_{\text{cmb}} - q_{\text{ad}} \quad (4)$$

where q_{cmb} is the heat flux across the CMB and q_{ad} is the adiabatic heat flux, given by

$$q_{\text{ad}} = -k_c \left(\frac{dT}{dr} \right)_{\text{ad}} \quad (5)$$

where k_c is the core thermal conductivity and the adiabatic temperature gradient is given by (e.g., Stacey (1992). p.304)

$$\left(\frac{dT}{dr} \right)_{\text{ad}} = -\frac{\alpha_c g_{\text{cmb}}}{c_c} T_{\text{cmb}} \quad (6)$$

where T_{cmb} is the temperature at the CMB. The CMB temperature and heat flux are functions of time and are obtained by considering the energy budget as described in section 2.4.

A positive thermal buoyancy flux indicates that heat is being removed across the CMB sufficiently quickly (i.e., superadiabatically) to introduce a source of density anomalies that can drive convection. A negative thermal buoyancy flux indicates that the CMB heat flux is small enough that the core can cool conductively and will therefore remain thermally stratified (i.e., the temperature profile remains subadiabatic and there is no thermal convection).

If the (primarily iron) liquid core is cool enough that parts of it begin to crystallize, the tendency for the lighter elements to partition preferentially into the liquid phase becomes a source of compositional buoyancy. If the inner core is growing from the bottom up, preferentially crystallizing iron, the rejection of some of the remaining lighter elements introduces a source of buoyant (light element-enriched) liquid at the inner core boundary. In this case, the density perturbation in (1) is the density contrast between the outer core (ρ_c) and the rejected light element-enriched liquid (ρ_χ), which we write as $\Delta\rho_\chi = \rho_c - \rho_\chi$. As the solid iron inner core grows, the density of the remaining liquid outer core decreases as it is gradually enriched in lighter elements. The decrease in ρ_c is initially extremely gradual, however, and remains less than 1% for the first few billion years of inner core growth (e.g., for Mars, assuming 10% sulfur in the core, the decrease in ρ_c remains less than 7% even when the inner core radius approaches 57% of the total core radius after ~ 5 Gyrs of inner core growth), and so we neglect this decrease in our model and assume that ρ_c and $\Delta\rho_\chi$ are constant. If the mass fraction of light elements in the core is χ_S , the core's bulk density (neglecting compression, which is discussed in section 2.2) is given by

$$\frac{1}{\rho_c} = \frac{1 - \chi_S}{\rho_{\text{Fe}}} + \frac{\chi_S}{\rho_S} \quad (7)$$

where we use the subscript S because we assume sulfur to be the principal light element species in the Martian core; ρ_{Fe} and ρ_S are the densities of the major and minor species (assumed to be iron and sulfur), respectively. Neglecting the small density differences between the solid and liquid forms of both the major and minor species (i.e., assuming $\rho_{\text{Fe,sol}} = \rho_{\text{Fe,liq}} = 6980 \text{ kg/m}^3$ and $\rho_{\text{S,sol}} = \rho_{\text{S,liq}} = 1819 \text{ kg/m}^3$), we can approximate the light element-enriched liquid density using

$$\frac{1}{\rho_\chi} = \frac{1 - \chi_{S,\text{liq}}}{\rho_{\text{Fe}}} + \frac{\chi_{S,\text{liq}}}{\rho_S} \quad (8)$$

where, assuming small control volumes partition into equal parts solid and liquid by mass, it can be shown that

$$\chi_{S,\text{liq}} = \frac{2}{1 + D_S} \chi_S \quad (9)$$

is the mass fraction of light elements in the residual liquid, where D_S is the solid-liquid phase partitioning coefficient for the light elements (i.e., the mole fraction of light elements that partition into the solid phase versus the liquid phase) (Zhang et al., 2020). Note that if sulfur partitions into the solid and liquid phases in equal proportions (i.e., if $D_S = 1$), then ρ_χ remains the same as the bulk core density and $\Delta\rho_\chi = 0$; if sulfur partitions preferentially into the liquid, then $D_S < 1$ and $\rho_\chi < \rho_c$ so the residual liquid is positively buoyant.

For this inner core growth-driven compositional buoyancy flux, the rate at which the inner core radius is growing, \dot{R}_{ic} , is the rate at which the density anomalies are being introduced in (1). Hence, this compositional buoyancy flux, scaled up to the CMB ($r = R_c$) to enable direct comparison with (3), is given by (e.g., Driscoll and Bercovici (2014), eq. 37)

$$F_\chi = g_{\text{icb}} \frac{\Delta\rho_\chi}{\rho_c} \left(\frac{R_{\text{ic}}}{R_c} \right)^2 \dot{R}_{\text{ic}} \quad (10)$$

where the gravity is taken to be linear across the core such that

$$g_{\text{icb}} = g_{\text{cmb}} \frac{R_{\text{ic}}}{R_{\text{c}}} \quad (11)$$

where the radius and growth rate of the inner core, R_{ic} and \dot{R}_{ic} , given by (39) and (40), are functions of the time varying temperature structure of the core and its relationship to the melting curve, as described in section 2.3.2.

As we discuss further in section 2.3, it is also possible for the core to crystallize from the top down rather than from the bottom up, in what is known as the iron snow regime (e.g., Hauck et al. (2006); Breuer et al. (2015)). This occurs when the core temperature profile is steeper than the melting curve such that the central part of the core remains above the melting curve even as crystallization begins to occur in the region above the radius at which the two curves meet, R_{snow} , which we call the base of the snow zone. In this case, as the core cools, iron-rich crystals forming above R_{snow} are negatively buoyant compared to the surrounding liquid (since the lighter elements partition preferentially into the liquid), and therefore sink as iron snow. If the falling crystals are warmed enough to remelt, they mix into the liquid layer below, introducing positive density anomalies and driving convection from above (e.g., Olson et al. (2017))—a process analogous to the buoyancy generated by exsolution of a minor species, leaving behind a negatively buoyant iron-rich residual liquid (e.g., Du et al. (2017); Mittal et al. (2020)). The crystals will remelt at a particular radius, R_{remelt} , where their temperature (assumed to follow the adiabat) reaches the melting curve for the iron-rich crystals. In general, because the crystals are relatively depleted in light elements, the relevant melting curve is elevated compared with that of the initial bulk liquid core. If the difference between the two melting curves is neglected (e.g., Breuer et al. (2015); Rückriemen et al. (2015)), then $R_{\text{remelt}} = R_{\text{snow}}$, meaning the crystals remelt immediately below the base of the zone in which they are forming. We instead compute a separate melting curve (see 2.3.2) for the crystals and find its intersection with the adiabat to obtain R_{remelt} , which, in general, is smaller than R_{snow} and may in fact be zero if the crystals never warm enough to remelt. Although the crystals may generate small eddies as they fall, they are not expected to contribute to large-scale convection unless they can remelt and mix into the underlying fluid (e.g., Olson et al. (2017)).

If the falling crystals do remelt, they introduce density anomalies at R_{remelt} at the rate at which the snow zone is growing, $-\dot{R}_{\text{snow}}$. The snow-driven buoyancy flux, once again scaled up to the CMB to enable direct comparison with (3) and (10), is thus

$$F_{\text{s}} = g_{\text{remelt}} \frac{\Delta\rho_{\text{snow}}}{\rho_{\text{c}}} \left(\frac{R_{\text{remelt}}}{R_{\text{c}}} \right)^2 (-\dot{R}_{\text{snow}}) \quad (12)$$

where

$$g_{\text{remelt}} = g_{\text{cmb}} \frac{R_{\text{remelt}}}{R_{\text{c}}} \quad (13)$$

and where $\Delta\rho_{\text{snow}} = \rho_{\text{snow}} - \rho_{\text{c}}$ is the excess density of the iron snow compared with the surrounding liquid, where we approximate the snow density using

$$\frac{1}{\rho_{\text{snow}}} = \frac{1 - \chi_{\text{S,sol}}}{\rho_{\text{Fe}}} + \frac{\chi_{\text{S,sol}}}{\rho_{\text{S}}}, \quad (14)$$

the solid component counterpart to (8), where

$$\chi_{\text{S,sol}} = \frac{2}{1 + D_{\text{S}}^{-1}} \chi_{\text{S}}. \quad (15)$$

As with bottom up inner core growth, the base of the snow zone and its rate of change are given by (39) and (40) and are functions of time as described in section 2.3.2. Likewise, the location of remelting, R_{remelt} , is given by (39) but using a melting curve that

corresponds to the iron-rich snow rather than to the bulk liquid core. If the crystals do not remelt, then $F_s = 0$, and a solid inner core grows by accumulation of the falling solids at the center of the core.

Even if the CMB heat flux is subadiabatic, such that the upper region of the core is thermally stably stratified, any ongoing core crystallization could continue to act as a source of buoyancy that could drive convection. However, the greater the thermal stratification at the top of the core, the smaller the compositionally convecting region will be, and the more difficult it will be to sustain a dynamo. Hence, as a simplification, and following Driscoll and Bercovici (2014), we will consider convection and dynamo action to be possible only when the net buoyancy flux, resolved at the CMB, is positive. That is, whenever

$$F_c = F_T + F_\chi + F_s > 0 \quad (16)$$

and not otherwise. We emphasize that this is a simplification and that even a positive net buoyancy flux ($F_c > 0$) may not be a sufficient condition for dynamo generation. We also do not attempt to calculate the expected field strength in the case of $F_c > 0$. Instead, we are concerned mainly with how the timing of the rising and falling of F_c , and thus the timing of the onset and cessation of convection and dynamo action, is controlled by parameters such as the initial temperature structure, radiogenic heating, mantle viscosity, thermal conductivity, light element partitioning, and core composition.

2.2 Density Structure

We model the planet's interior as a series of spherically symmetric concentric shells. The models consist of an outer rocky mantle and an inner primarily iron core, which may be further partitioned into solid and liquid phases. Owing to compression at high pressures, we allow for radially variable density within each layer according to the Adams-Williamson equation

$$\frac{d\rho}{dr} = \frac{-\rho^2(r) g(r)}{K_s(r)} \quad (17)$$

where K_s is the isentropic bulk modulus, given by

$$K_s(r) = K_T(1 + \alpha(x)\gamma(x)T(r)) \quad (18)$$

where K_T is the isothermal bulk modulus, T is the temperature, α is the thermal expansivity, and γ is the Grneisen parameter. K_T is in turn related to the density by the third order Vinet equation of state (Vinet et al., 1989; Oganov, 2007)

$$K_T = K_0 \left(1 + \left(1 + \theta x^{1/3} \right) \left(1 - x^{1/3} \right) \right) \exp \left(\theta \left(1 - x^{1/3} \right) \right) x^{-2/3} \quad (19)$$

where the compression is represented by

$$x = \frac{\rho_0}{\rho} \quad (20)$$

(equivalently, $x = V/V_0$, as it is expressed by Vinet et al. (1989); Oganov (2007)) and where

$$\theta = \frac{3}{2} (K'_0 - 1) \quad (21)$$

where K_0 is the zero pressure bulk modulus and K'_0 is its derivative with respect to pressure. The thermal expansivity and the Grneisen parameter are functions of the compression according to the parameterizations

$$\alpha(x) = \alpha_0 x^{\delta_T} \quad (22)$$

and

$$\gamma(x) = \gamma_0 x^{\gamma_1} \quad (23)$$

based on high pressure experiments (Chopelas & Boehler, 1992; Merkel et al., 2000). These parameterizations were previously used by Driscoll and Olson (2011) but the sign on the exponents in our (22) and (23) are reversed from those in their eq. 8 due to a typo in the text after their eq. 6 in which their x is inverted from the one previously defined by Oganov (2007) and in our (20) (see also Boujibar et al. (2020)). Whereas Driscoll and Olson (2011) and Boujibar et al. (2020) assumed the exponent in (22) to be $\delta_T = 3$, we allow it to vary for different materials. The reference values, ρ_0 , K_0 , α_0 , and γ_0 , and the exponents, δ_T and γ_1 , are material and temperature dependent; the values given in Table 2 have been selected to approximately satisfy experimental data for the expected temperatures and compositions of the cores and mantles of Earth and Mars (e.g., Boehler et al. (1990); Chopelas and Boehler (1992); Stacey and Davis (2004); Vočadlo (2015)).

The temperature required by (18) is estimated by integrating

$$\frac{dT}{dr} = -\frac{\rho(r)g(r)\gamma(r)}{K_s(r)}T(r) \quad (24)$$

subject to the boundary condition of an assumed temperature at the top of the mantle and the density and gravity profiles obtained as discussed immediately below. For purposes of modeling the planet’s energy budget and thermal evolution, however, we will define a distinct temperature structure as described in sections 2.3 and 2.4. Although the temperature profile obtained by integration of (24) differs from the temperature profile that emerges from the thermal evolution calculation (in part because the latter includes a steep temperature change across the thermal boundary layers), by substituting an evolved temperature profile into (18) instead of using (24), we verified that the effect on the computed radial density structure is negligible (densities are everywhere within $< 1\%$). Hence, integration of (24) is sufficient for estimating the temperature profile for purposes of computing the radial density structure prior to considering the planet’s thermal evolution, avoiding the computationally expensive process of having to continually update the density structure as the temperature profile evolves.

At a given radius, r , the enclosed mass, $M(r)$, and the hydrostatic pressure, $P(r)$, are given by integration of

$$\frac{dM}{dr} = \rho(r)4\pi r^2, \quad (25)$$

and

$$\frac{dP}{dr} = -\rho(r)g(r) \quad (26)$$

where the gravitational acceleration is

$$g(r) = \frac{GM(r)}{r^2}. \quad (27)$$

Although it follows that

$$\frac{dg}{dr} = 4\pi G\rho(r) - \frac{2GM(r)}{r^3}, \quad (28)$$

it is more straightforward to compute $g(r)$ directly from (27) since $M(r)$ is determined at every step of the integration.

We obtain the interior structure by integrating equations (17), (24), (25), and (26) inward from the outer edge of the body, in 5-meter steps, subject to the boundary conditions of the known total mass and an assumed density and temperature at the top of the mantle (e.g., Driscoll and Olson (2011); Boujibar et al. (2020)). At the transition between the mantle and the core, there is a discontinuity in density and elastic properties, which we estimate by requiring continuity in the pressure profile. Specifically, given the

known value of K_s on the mantle side of the boundary, we find the value of K_s for the core side that yields equal pressures on either side of the boundary, where the pressure is approximated as

$$P = (K_S - K_0) / K'_0, \quad (29)$$

and then we solve (18)–(20) to obtain the density at the top of the core before resuming the inward integration.

In general, when the integration terminates at $r = 0$, the enclosed mass does not go precisely to zero, as is required for a self-consistent physical solution. To ensure that $M(0) = 0$, we carry out the above procedure iteratively, making small changes to the assumed density at the top of the mantle until $M(0) \approx 0$ to within a factor of 10^{-5} . Finally, we force the density to be constant over the innermost 2% of the body’s radius and then recompute the mass, pressure, and gravity profiles by integrating outward from $r = 0$, thereby ensuring that $M(0)$ and $g(0)$ are precisely zero. As a result, the enclosed mass at $r = R$ differs slightly from the true total mass, but only by a factor of $\sim 10^{-5}$.

As an example, Figure 1 shows the simplified radial density structures we obtained for Earth and Mars when we adopt the parameters given in Tables 1 and 2. The Martian core radius is uncertain but we adopt the middle of the wide range obtained by Brennan et al. (2020)—although we note that at least one recent InSight-based study suggests the core may be larger (Deng & Levander, 2020). In principle, the Martian core radius should be a function of its sulfur content because greater sulfur content implies a lower density core, which in turn requires a slightly larger core radius in order to satisfy the mass and moment of inertia constraints (e.g., Brennan et al. (2020)). Such changes in the radial density structure do have some effects on relevant model parameters, but they are small compared with uncertainties in the reference values for those parameters. For example, we determined that higher sulfur content lowers the reference core density as well as lowering core pressures such that compression, x , and therefore thermal expansivity, α , are largely unaffected by changes in core sulfur content: adjusting wt%S in the range 7 ± 7 affects α at the $\sim 10\%$ level, an effect that is overwhelmed by uncertainty in the reference value, α_0 .

Table 1. Coarse internal structure of Earth and Mars.

Parameter	Symbol	Earth	Mars
Full radius	R	6371 km	3389.5 km
Core radius	R_c	3480 km	1745 km
Bulk density	$\bar{\rho}$	5513.6 kg/m ³	3934.1 kg/m ³

2.3 Temperature Structure

The model planet’s temperature structure can be divided into four regions: a well-mixed core, a conductive lower mantle thermal boundary layer, a well-mixed (convecting) region of the mantle, and a conductive upper mantle thermal boundary layer. An example model temperature profile is illustrated in Figure 2a for a case approximating the present-day Earth, and a few hypothetical Martian temperature profiles are illustrated in Figure 2b–d.

2.3.1 Core Temperature Structure

The adiabatic temperature profile across the core can be written (e.g., Labrosse et al. (2001))

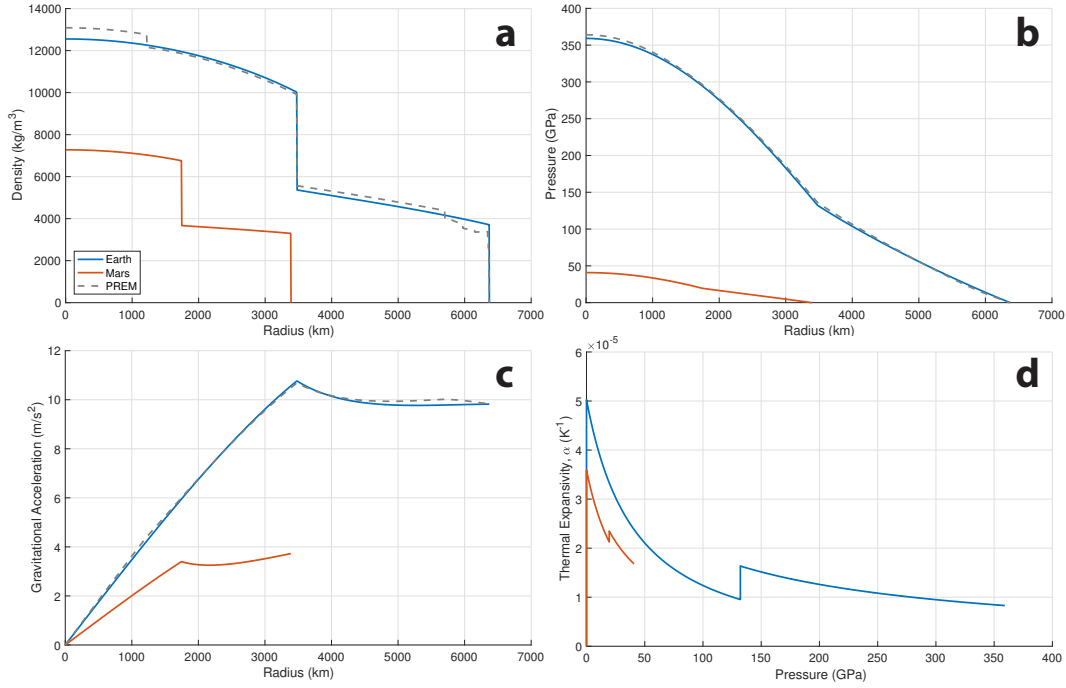


Figure 1. Radial density structures (a), pressure profiles (b), gravity profiles (c), and thermal expansivity profiles (d) for Earth (blue) and Mars (red) obtained as described in section 2.2.

The dashed lines in (a-c) show PREM (Dziewonski & Anderson, 1981) as a point of comparison for our simplified model Earth. The density, pressure, and gravity profiles (a-c) are shown as a function of radius but the thermal expansivity profile (d) is shown as a function of pressure to enable more direct comparison with experimental results (e.g., Boehler et al. (1990); Chopelas and Boehler (1992); Vočadlo (2015)).

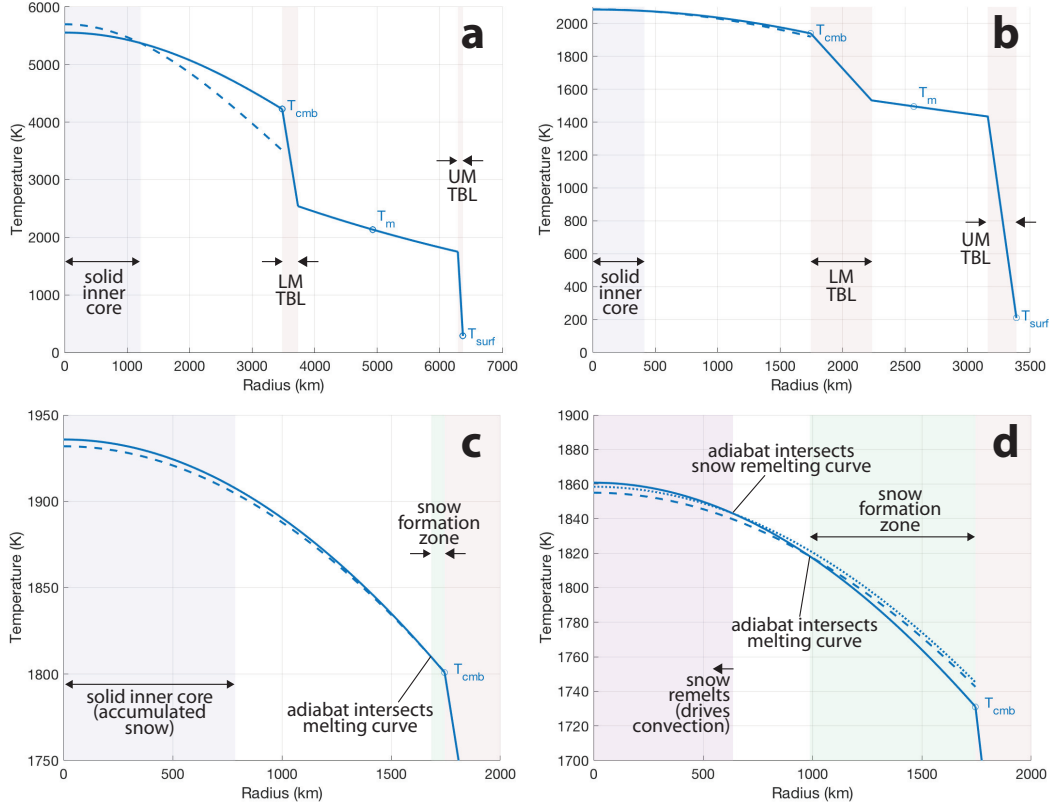


Figure 2. Example internal temperature structures for Earth (a) and Mars (b-d); the Martian core is emphasized in (c-d). Open circles and labels indicate the CMB temperature (T_{cmb}), the mid-mantle temperature (T_m), and the surface temperature (T_{surf}). Pale red shading highlights the two conductive thermal boundary layers (TBLs) at the top and bottom of the mantle (UM, LM, respectively). Solid lines represent the temperature as a function of radius; dashed lines represent the melting temperature across the core; dotted line represents the remelting temperature for falling iron snow (visible only in d—a case in which D_S is close to unity). Pale blue shading at the left in (a-c) indicates the presence of a solid inner core where the core temperature, (33), falls below the melting curve, (36) (a,b) or where falling iron snow does not remelt and accumulates at the center (c). Whereas the melting curve is steeper than the core adiabat in (a) and (b), such that the core crystallizes from the bottom up, it is shallower in (c) and (d) such that crystallization occurs in the “snow zone” (pale green shading) above the intersection of the melting curve and the core adiabat. In (d), the melting curve for the falling iron snow (dotted line) is very close to the bulk core melting curve such that the core adiabat is able to cross both melting curves: the intersection with the bulk core melting curve defines the base of the snow zone (pale green shading) and the intersection with the snow remelting curve defines the radius at which the snow remelts, and below which snow driven convection may take place (pale purple shading). The snow remelting curve was also calculated for (c) but is not visible because it is far above the temperature range shown.

Table 2. Equation-of-state parameters used in radial structure computation, assuming a perovskite-like mantle and liquid iron core for Earth, and a peridotite-like mantle and liquid iron-sulfur core for Mars. Values are similar to those of Driscoll and Olson (2011) and correspond approximately with various experimental results (Boehler et al., 1990; Chopelas & Boehler, 1992; Stacey & Davis, 2004; Vočadlo, 2015).

Parameter	Symbol	Earth’s mantle	Earth’s core	Martian mantle	Martian core
Zero pressure density	ρ_0	3900 kg/m ³	6900 kg/m ³	3226 kg/m ³	6000 kg/m ³
Zero pressure bulk modulus	K_0	200 GPa	125 GPa	128 GPa	125 GPa
Bulk modulus gradient	K'_0	4.0	5.5	4.2	5.5
Reference Grneisen parameter	γ_0	1.0	1.6	0.99	1.6
Grneisen parameter exponent	γ_1	1.4	0.92	2.1	0.92
Reference thermal expansivity	α_0	$4 \times 10^{-5} \text{ K}^{-1}$	$5 \times 10^{-5} \text{ K}^{-1}$	$4 \times 10^{-5} \text{ K}^{-1}$	$4 \times 10^{-5} \text{ K}^{-1}$
Thermal expansivity exponent	δ_T	4.5	3.0	4.9	4.5

$$T_{\text{core}}(r) = T_{\text{cen}} \exp\left(-\frac{r^2}{D_N^2}\right) \quad (30)$$

where T_{cen} is the temperature at zero radius and D_N is a length scale given by

$$D_N = \sqrt{\frac{3c_c}{2\pi\alpha_c\rho_c G}} \quad (31)$$

where c_c is the specific heat capacity, G is the gravitational constant, ρ_c is the mean core density, and α_c is the mass-averaged thermal expansivity of the core, given by

$$\alpha_c = \frac{1}{M_c} \int_0^{R_c} \alpha(x) dM \quad (32)$$

where M_c is the total core mass and dM is the mass of each infinitesimally thin shell, and where $\alpha(x)$ is given by (22) with x being a function of radius emerging from the density profile via (20). It can be shown that the radial gradient of (30) at $r = R_c$ is equivalent to (6). Note that Labrosse et al. (2001) use the zero-radius density, ρ_{cen} , in (31), which gives a similar result, provided the density does not vary too greatly across the core. However, when ρ_{cen} is used in place of ρ_c , the equivalence with (6) is not strictly preserved.

Because we often prefer to reference the CMB temperature, we can also write (30) as

$$T_{\text{core}}(r) = T_{\text{cmb}} \exp\left(\frac{R_c^2 - r^2}{D_N^2}\right). \quad (33)$$

The mass-averaged core temperature is given by

$$T_c = \frac{1}{M_c} \int_0^{R_c} T_{\text{core}}(r) dM(r). \quad (34)$$

Substituting from (33), we can write

$$\frac{T_c}{T_{\text{cmb}}} = \exp\left(\frac{R_c^2}{D_N^2}\right) \frac{1}{M_c} \int_0^{R_c} \exp\left(-\frac{r^2}{D_N^2}\right) dM(r) \quad (35)$$

which we integrate numerically to obtain the relationship between T_c and T_{cmb} , which is time invariant as we neglect the small change in the core density profile that occurs during inner core growth. For the models defined by Tables 1 and 2 and illustrated in Figure 2, $\frac{T_c}{T_{\text{cmb}}}$ is ~ 1.12 for Earth and ~ 1.03 for Mars.

2.3.2 Melting Curve and Core Crystallization

Parts of the core will crystallize if part of the core temperature profile falls below the melting curve (Figure 2). The melting curve may be expressed in a number of ways (e.g., Labrosse (2003); J.-P. Williams and Nimmo (2004); Rivoldini et al. (2011)).

For the sake of computational efficiency, we prefer to use a form that, when equated with (33), yields a closed form analytical expression for the radius at which the two curves intersect. In particular, we will express the melting curve as

$$T_{\text{melt}}(r) = T_{\text{melt, cen}} \exp\left(-\frac{r^2}{D_{\text{m}}^2}\right) \quad (36)$$

where $T_{\text{melt, cen}}$ is the melting temperature at the center of the planet and where D_{m} is a length scale that, like D_N , depends on the planet's density structure and the material properties of its core. For Earth, we choose $T_{\text{melt, cen}} = 5700$ K and $D_{\text{m}} = 5000$ km (Table 5) in order to obtain good agreement between the melting curve given by (36) and those based on laboratory experiments and *ab initio* calculations (e.g., Fei et al. (2000); Boehler et al. (1990); Anzellini et al. (2013); Vočadlo (2015)) as shown in Figure 3, where we have plotted T_{melt} against the pressure profile obtained by integration of (26).

For Mars, we assume an Fe-FeS core for which the melting curve depends sensitively on the amount of sulfur in the core. We compute the Martian $T_{\text{melt, cen}}$ and D_{m} according to the polynomials

$$T_{\text{melt, cen}} = t_0 + t_1 \chi_{\text{S}} \quad (37)$$

and

$$D_{\text{m}} = d_0 + d_1 \chi_{\text{S}} + d_2 \chi_{\text{S}}^2 + d_3 \chi_{\text{S}}^3 \quad (38)$$

where χ_{S} is the sulfur mass fraction of the core and where the constants (Table 3) were obtained by fitting, in a least squares sense, to the results of several laboratory experiments (Boehler et al., 1990; Fei et al., 2000; Stewart et al., 2007; Morard et al., 2008) as summarized by Rivoldini et al. (2011). In particular, we fit to the melting curves described by eq. 2 by Rivoldini et al. (2011), noting the following corrections: in their Table 3, the constants a_1 and a_2 are reversed and the constant c_1 should be positive; in their Table 4, the reference temperature for ≥ 21 GPa should be 1355 K not 1255 K. The resulting Martian core melting curves are shown in Figure 3 for several different assumed sulfur mass fractions. The melting curves become increasingly flat with increasing sulfur content. If the sulfur content is sufficiently high (approaching the eutectic from the pure iron side), the melting curve may be shallower (i.e., increasing more gradually with depth) than the core temperature profile, given by (30), whose steepness is largely controlled by the core material's thermal expansivity via (31). In such a case, the core will not solidify from the bottom up, but will instead solidify first near the CMB in what may be called the iron snow regime (e.g., Hauck et al. (2006); Stewart et al. (2007); Q. Williams (2009); Breuer et al. (2015); Davies and Pommier (2018); Gilfoy and Li (2020)) (Figure 4a).

Table 3. Constants required for equations (37) and (38) for Martian core melting curve.

Constant	Value
t_0	2547 K
t_1	−7689 K
d_0	5.243×10^6 m
d_1	1.689×10^7 m
d_2	-2.183×10^8 m
d_3	2.725×10^9 m

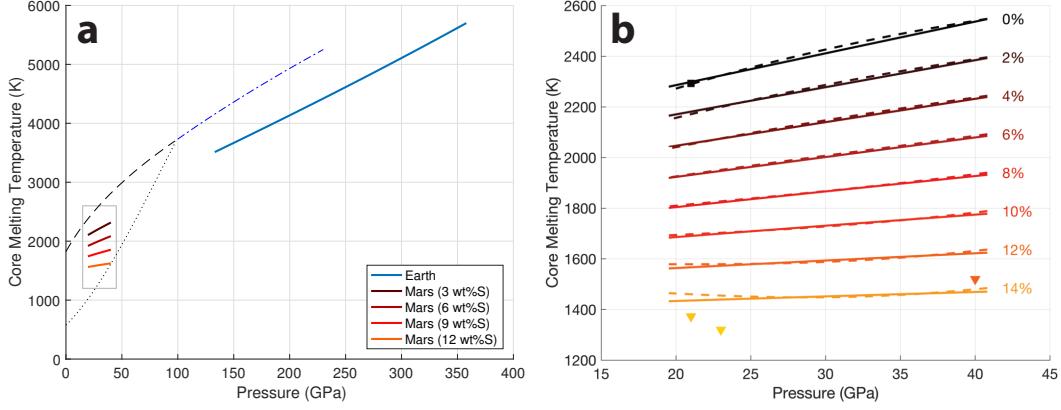


Figure 3. Melting curves for iron-rich cores as a function of pressure. The dashed and dash-dotted lines in (a) represent the melting curves for pure iron obtained by Anzellini et al. (2013). The solid lines represent melting curves described by (36) and corresponding approximately to the cores of Earth and Mars. The solid blue line, which we take to be representative for the Earth’s core, is obtained from (36) by assuming that $T_{\text{melt, cen}} = 5700$ K and $D_{\text{m}} = 5000$ km. The red and orange lines represent melting curves for the Martian core assuming different amounts of sulfur. The thin rectangle in (a) highlights the region relevant to the Martian core, which is shown in more detail in (b). Additional Martian core melting curves, computed from (36), are shown as solid lines in (b) and are compared with the Rivoldini et al. (2011) model (dashed lines) and the results from pure iron experiments (Boehler et al. (1990); Fei et al. (2000); squares) and Fe-FeS eutectic experiments (Stewart et al. (2007); Morard et al. (2008); triangles). Lines and symbols are color-coded by sulfur content (darkest red = 0 wt%S; brightest orange = 14 wt%S).

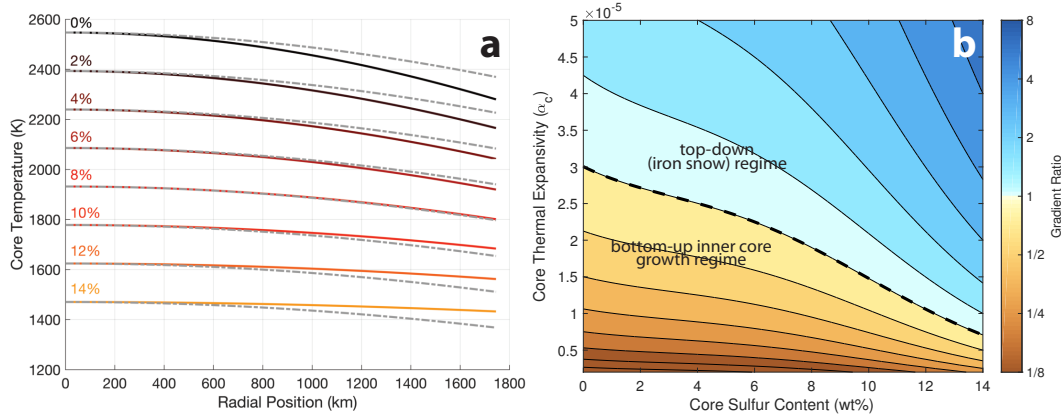


Figure 4. (a) Martian core melting curves as a function of radius (solid lines, color coded by wt%S as in Figure 3) compared with adiabatic temperature profiles across the core (dash-dotted lines), where we have set $T_{\text{cen}} = T_{\text{melt, cen}}$ and where $\alpha_c = 2 \times 10^{-5} \text{ K}^{-1}$. Core temperature profiles are shallower than the melting curve when sulfur content is $\lesssim 8\%$, but steeper otherwise. (b) Ratio between core temperature profile and melting curve gradients at $r=0$ as a function of core thermal expansivity and sulfur content. Depending on sulfur content and thermal expansivity, core crystallization occurs either from the bottom up (orange shaded region below the dashed black line) or as iron snow precipitating from near the CMB (blue shaded region above the dashed black line).

Whereas the melting curves given by Stewart et al. (2007) (their Figure 2) would imply that melting temperature always decreases with depth in the Martian core, even when sulfur content is as low as 10.6 wt%, the Rivoldini et al. (2011) phase curve model, which incorporates the Stewart et al. (2007) experimental results along with those of several other studies (Boehler et al., 1990; Fei et al., 2000; Morard et al., 2008), produces curves in which the melting temperature generally increases with depth—though the curves do flatten as sulfur content approaches roughly 13wt%. Davies and Pommier (2018) favor the iron snow regime because they adapted the J.-P. Williams and Nimmo (2004) melting curve to fit the Stewart et al. (2007) curves (see liquidus curve parameters in Table 1 by Davies and Pommier (2018)); when the original parameters of J.-P. Williams and Nimmo (2004) are retained (their Table 1), the melting curve closely resembles ours. Furthermore, the Davies and Pommier (2018) core temperature profile (which they describe as $T = T_0 (1 + 0.02P)$, with pressure in units of GPa) implies a $\sim 22\%$ drop in temperature across the Martian core, whereas our adiabatic core temperature profiles, given by (30), are significantly flatter, with temperature drops closer to $\sim 7\%$, due in part to differences in assumptions about thermal expansivity. Both of these effects mean that, while the iron snow regime may occur in our model, it is not guaranteed, and there remains the possibility of core crystallization from the bottom up, depending on the relative slopes of the core adiabat and the melting curve.

It can be shown that, whenever $D_N > D_m$, the core temperature profile is shallower than the melting curve such that, if the core is initially entirely liquid, crystallization will occur first at the center. Conversely, whenever $D_N < D_m$, the core temperature profile is steeper than the melting curve and crystallization will occur first at the CMB. The transition between bottom up inner core growth and the iron snow regime is thus determined mainly by the thermal expansivity and sulfur content of the core since these determine D_N and D_m , respectively (Figure 4b). The length scale D_N is equally sensitive to the core’s specific heat capacity, but we focus on thermal expansivity in Figure 4b because it is not as well determined and because a wide range of values have been adopted in previous studies. As we discussed in section 2.2, we have simplified our model by neglecting the effect of sulfur content on the radial density structure—in principle, increased sulfur content in the core should alter the density structure in a way that leads to slightly larger core thermal expansivity, but the effect is small compared to uncertainty in the reference thermal expansivity.

We obtain the intersection of the adiabatic core temperature profile and the melting curve by equating (33) and (36) and solving for r to get

$$R_{\text{int}} = \left(\frac{\ln(T_{\text{melt,cen}}/T_{\text{cmb}}) - (R_c/D_N)^2}{D_m^{-2} - D_N^{-2}} \right)^{1/2}. \quad (39)$$

Differentiating with respect to time yields

$$\dot{R}_{\text{int}} = -\frac{1}{2R_{\text{ic}}} \left(\frac{1}{D_m^{-2} - D_N^{-2}} \right) \frac{\dot{T}_{\text{cmb}}}{T_{\text{cmb}}}. \quad (40)$$

In the case of bottom up core crystallization, these define the radius and growth rate of the solid inner core, R_{ic} and \dot{R}_{ic} . These expressions are similar to but differ slightly from eqs. 29 and 30 by Driscoll and Bercovici (2014) because we have expressed the melting curve using our (36) instead of their eq. 28. Though we do not use an equivalent equation, we note also that their eq. 32 contains a typo: the first R_c on the right hand side should be R_{ic} . In the iron snow regime, the intersection of the core adiabat and the melting curve instead defines the base of the snow zone, above which iron crystals are forming. Note, however, that the signs are different: when the melting curve is steeper than the temperature profile, $D_N > D_m$, the term in parentheses in (40) is positive, meaning that the inner core growth rate is positive if the core is cooling; when the melting

curve is shallower than the temperature profile, $D_N < D_m$, the term in parentheses is negative, meaning that the radius of the base of the snow zone decreases as the core cools (i.e., the snow zone grows downward from the top of the core).

As we discussed in 2.1, we also require the radius at which the snow crystals remelt, R_{remelt} , which is once again obtained by equating (33) and (36) but with the melting curve for the crystals corresponding to their reduced sulfur content, given by (15). For very small partitioning coefficients ($D_S \ll 1$), the snow is almost pure iron, with a correspondingly higher melting temperature, and will therefore not remelt unless the adiabat is very steep. If the crystals do not remelt, a solid inner core grows as the falling solids accumulate at the center of the core. We assume the solids accumulate without porosity and therefore that an inner core built in this way follows the density profile obtained as described in section 2.2, just as in the case of crystallization from the bottom up.

2.3.3 Mantle Temperature Structure

We assume the mantle consists of conductive thermal boundary layers at the top and bottom, separated by a convecting region in which the temperature profile is described by

$$T_{\text{mantle}}(r) = T_m \exp\left(\frac{\alpha_m g_m}{c_m}(R_m - r)\right) \quad (41)$$

where T_m is a representative mid-mantle temperature (i.e., the temperature at radius $R_m = \frac{R_c + R}{2}$), α_m is the mid-mantle thermal expansivity, c_m is the mantle's specific heat capacity, and g_m is the gravity at R_m . We assume linear temperature profiles across the thermal boundary layers with the temperature drops being

$$\Delta T_{\text{LM}} = T_{\text{cmb}} - T_{\text{LM}} \quad (42)$$

and

$$\Delta T_{\text{UM}} = T_{\text{UM}} - T_{\text{surf}} \quad (43)$$

where T_{surf} is a prescribed fixed value for each planet and where T_{LM} and T_{UM} are computed by extrapolating, via (41), the mantle temperature profile to the base and top of the convecting part of the mantle, respectively. Because the thermal boundary layer thicknesses are not yet known at this point in the calculation, we initially assume their thicknesses to be zero (this results in two small discontinuities in the mantle temperature profile) and then we iterate to obtain a self-consistent solution, as described at the end of this section.

The boundary layer thicknesses δ_{LM} and δ_{UM} are given by (e.g., Driscoll and Bercovici (2014))

$$\delta_{\text{LM}} = \left(\frac{Ra_{\text{crit}} \kappa_{\text{LM}} \nu_{\text{LM}}}{\alpha_m g_{\text{cmb}} \Delta T_{\text{LM}}}\right)^{1/3} \quad (44)$$

and

$$\delta_{\text{UM}} = \left(\frac{Ra_{\text{crit}} \kappa_{\text{UM}} \nu_{\text{UM}}}{\alpha_m g_{\text{surf}} \Delta T_{\text{UM}}}\right)^{1/3} \quad (45)$$

where $Ra_{\text{crit}} = 660$ is an assumed critical Rayleigh number. The thermal diffusivities, κ_{LM} and κ_{UM} are computed from the thermal conductivities as $\kappa = \frac{k}{\rho c_m}$, where the pressure- and therefore depth-dependent thermal conductivities are given by (Van den Berg et al., 2002; Driscoll & Olson, 2011)

$$k = k_0 \left(1 + P(r) \frac{K'_0}{K_0}\right) \quad (46)$$

where the reference conductivity is $k_0 = 3.3 \text{ W/m/K}$, $P(r)$ is the radially dependent pressure (section 2.2), K_0 is the zero-pressure bulk modulus of the mantle, and K'_0 is its derivative with respect to pressure (Table 2).

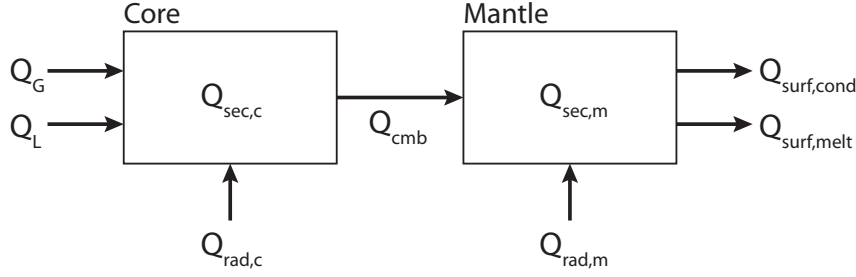


Figure 5. Schematic illustration of the global energy budget. $Q_{\text{sec},c}$ and $Q_{\text{sec},m}$ represent the secular warming (if positive) or cooling (if negative) terms for the core and mantle, respectively. The heat flows into and out of the core and mantle are detailed in sections 2.4.1 and 2.4.2 and include: gravitational potential energy (Q_G), latent heat (Q_L), radiogenic heating ($Q_{\text{rad},c}$, $Q_{\text{rad},m}$), and surface heat flows from the mantle ($Q_{\text{surf},\text{cond}}$, $Q_{\text{surf},\text{melt}}$). The crust is not included in our model.

We compute the temperature dependent viscosity for the thermal boundary layer at the top of the mantle as

$$\nu_{\text{UM}} = \nu_{\text{ref}} \exp \left(\frac{A_v}{R_g} \left(\frac{1}{T_{\text{UM}}} - \frac{1}{T_{\text{ref}}} \right) \right) \quad (47)$$

where ν_{ref} is a prescribed reference viscosity corresponding to a reference temperature T_{ref} , A_v is the activation energy, and R_g is the ideal gas constant. As a means of accounting for the increase in viscosity with pressure, we then compute the lower mantle viscosity as

$$\nu_{\text{LM}} = f \nu_{\text{UM}} \quad (48)$$

where f is a free parameter of order 10.

Finally, having determined the boundary layer thicknesses, we update our estimates of T_{LM} and T_{UM} by extrapolating, via (41), the mantle temperature profile to the base and top of the convecting part of the mantle, respectively, and then we recalculate the temperature drops and boundary layer thicknesses via (42)-(48). This process can be carried out iteratively until the two discontinuities in the temperature profile are eliminated. In practice, two iterations are sufficient to make the discontinuities negligibly small (~ 2 K).

2.4 Energy Budget

2.4.1 Core Energy Budget

The temperature evolution of the core is controlled by the balance of internal radiogenic heating, heat flow from the core to the mantle (i.e., across the CMB), and the latent heat and gravitational potential energy associated with core crystallization (or melting) (Figure 5). Specifically (e.g., Nimmo (2015)),

$$Q_{\text{sec},c} = Q_{\text{rad},c} - Q_{\text{cmb}} + Q_L + Q_G \quad (49)$$

where $Q_{\text{sec},c}$ is the secular warming (or cooling, if negative) of the core, and where the first term on the right hand side is the heat released by the decay of radioactive isotopes, which we compute as

$$Q_{\text{rad},c}(t) = Q_{\text{rad},c,\text{init}} \exp(-t/\tau_c) \quad (50)$$

where τ_c is the decay timescale for the relevant radioactive materials in the core, which we assume to be primarily ^{40}K , and $Q_{\text{rad,c,init}}$ is a prescribed radiogenic heat flow at time zero. The second term on the right is the heat flow across the CMB (i.e., across the lower mantle thermal boundary layer) and is obtained via (59), as described in section 2.4.2. The third and fourth terms on the right hand side of (49) are non-zero only while parts of the core are freezing or melting. Q_L is the latent heat related to the phase change

$$Q_L = \dot{M}_{\text{c,sol}} L_{\text{Fe}} \quad (51)$$

where L_{Fe} is the latent heat of fusion for iron. Similarly, Q_G is related to the gravitational energy associated with the separation of the crystallizing iron from the melt containing lighter elements, and is approximated as

$$Q_G = \dot{M}_{\text{c,sol}} E_G. \quad (52)$$

Both of these terms require the rate of mass change of the solid portion of the core, $\dot{M}_{\text{c,sol}}$. In the bottom up crystallization regime (i.e., when $D_N > D_m$), this is effectively the mass flow rate across the phase boundary (the inner core boundary) and is obtained by multiplying the rate of change of the inner core radius, \dot{R}_{ic} , with the surface area at that radius, R_{ic} , and the local density, ρ_{icb} , obtained from the radial density structure (section 2.2). Noting that it can be verified that $\frac{\dot{T}_c}{T_c} = \frac{\dot{T}_{\text{cmb}}}{T_{\text{cmb}}}$, the result is

$$\dot{M}_{\text{c,sol}} = -\frac{2\pi R_{\text{ic}} \rho_{\text{icb}}}{(D_m^{-2} - D_N^{-2})} \frac{\dot{T}_c}{T_c}. \quad (53)$$

Notice that if the core adiabat and the melting curve intersect at a steep angle (i.e., if the length scales D_N and D_m are very different), then a given increment of cooling leads to a small increase in the mass of the solid portion of the core, $M_{\text{c,sol}}$. However, if D_N and D_m are very similar, the core adiabat and melting curves become nearly co-linear such that even a small increment of cooling corresponds to a large increase in $M_{\text{c,sol}}$.

In the iron snow regime ($D_N < D_m$), if the falling snow remelts, it can drive convection in the underlying fluid as described in section 2.3.2, but the net production of solids is zero ($\dot{M}_{\text{c,sol}} = 0$), and therefore there is no contribution to the energy budget. $\dot{M}_{\text{c,sol}}$ is non-zero only during bottom-up growth of a solid inner core or when iron snow crystals form in the snow zone and sink to the center without remelting. In the latter case, $\dot{M}_{\text{c,sol}}$ is a function of the snow zone's volume and the rate of crystallization per unit volume in the snow zone, which depends on the rate at which the core temperature is decreasing. We do not, however, attempt to model this scenario in detail because the falling, but not remelting, snow does not drive convection, and is therefore not relevant to the problem of identifying different modes of dynamo generation.

Finally, the secular warming/cooling term relates to the core's heat capacity and rate of temperature change as

$$Q_{\text{sec,c}} = M_c c_c \dot{T}_c \quad (54)$$

allowing us to solve equation (49) for the rate of temperature change in the core, obtaining

$$\dot{T}_c = \frac{Q_{\text{rad,c}} - Q_{\text{cmb}}}{M_c c_c + \left[\frac{2\pi R_{\text{int}} \rho_{\text{int}} (L_{\text{Fe}} + E_G)}{(D_m^{-2} - D_N^{-2}) T_c} \right]} \quad (55)$$

where the term in square brackets is zero when there is no net freezing or melting in the core. If the core is experiencing net freezing or melting, then the rate of its temperature change will be reduced because some fraction of the energy flow goes into the phase change part of the budget (latent heat and gravitational energy) rather than to the warming or

cooling of the core. This effect is especially pronounced when the phase boundary is at a large fraction of the core's radius, as in early times in the iron snow regime or later times in the bottom-up crystallization regime. Notably, if freezing or melting is occurring and D_N and D_m are very similar (i.e., the core adiabat and melting curves are nearly co-linear), then the rate of temperature change in the core will become extremely slow as the energy budget becomes dominated by freezing or melting.

2.4.2 Mantle Energy Budget

The temperature evolution of the mantle is controlled by the balance of the heat flow across the CMB, the internal radiogenic heating, and the surface heat flows (Figure 5). Specifically (e.g., Driscoll and Bercovici (2014))

$$Q_{\text{sec,m}} = (Q_{\text{cmb}} + Q_{\text{rad,m}}) - (Q_{\text{surf,cond}} + Q_{\text{surf,melt}}) \quad (56)$$

where $Q_{\text{sec,m}}$ is the secular warming (or cooling, if negative) of the mantle, $Q_{\text{rad,m}}$ is the radiogenic heating in the mantle, Q_{cmb} is the heat flow from the core into the mantle (i.e., across the lower mantle thermal boundary layer), and $Q_{\text{surf,cond}}$ and $Q_{\text{surf,melt}}$ represent the heat lost out the top of the mantle (i.e., to the surface via conduction and erupting melt, respectively). There is no latent heat term in (56) because we assume the mantle cooled quickly from the magma ocean phase and is already entirely solid by the beginning of our simulations.

The radiogenic heating is given by

$$Q_{\text{rad,m}}(t) = Q_{\text{rad,m,init}} \exp(-t/\tau_m) \quad (57)$$

where τ_m is an effective decay timescale for the relevant radioactive materials in the mantle (primarily ^{238}U , ^{235}U , ^{232}Th , and ^{40}K), and $Q_{\text{rad,m,init}}$ is a prescribed radiogenic heat flow at time zero.

The conductive heat loss through the top of the mantle is a function of the thermal conductivity and the temperature gradient across the boundary layer at the top of the mantle. Approximating the latter as the temperature jump (ΔT_{UM}) divided by the thickness of the thermal boundary layer (δ_{UM}), we can write

$$Q_{\text{surf,cond}} = 4\pi R^2 k_{\text{UM}} \frac{\Delta T_{\text{UM}}}{\delta_{\text{UM}}} \quad (58)$$

where we are using the planet's full radius to approximate the boundary's surface area. Similarly, the heat flow across the CMB can be written

$$Q_{\text{cmb}} = 4\pi R_{\text{cmb}}^2 q_{\text{cmb}} \quad (59)$$

where we have approximated the boundary's surface area using the CMB radius. The CMB heat flux, also appearing in equation (4), is

$$q_{\text{cmb}} = k_{\text{LM}} \frac{\Delta T_{\text{LM}}}{\delta_{\text{LM}}}. \quad (60)$$

The boundary layer thicknesses, temperature drops, and thermal conductivities in (58) and (60) are obtained as described in section 2.3.3.

Heat is also lost from the mantle in the form of the production of melt, which is then erupted to the surface. The rate of heat loss due to eruptions (i.e., the advective heat loss) may be taken as proportional to the conductive heat loss through the upper mantle boundary layer (i.e., the diffusive heat loss) with the constant of proportionality being effectively a Peclet number for heat transport out the top of the mantle

$$Pe = \frac{Q_{\text{surf,melt}}}{Q_{\text{surf,cond}}} \quad (61)$$

where a large value corresponds to very efficient transport of melt to the surface and where a tectonically/volcanically quiescent planet would have a Peclet number approaching zero. Although one could estimate $Q_{\text{surf,melt}}$ directly by modeling the details of how much melt should be produced based on the temperature structure near the surface and how efficient eruptions might be, given the type of tectonic activity (e.g., Driscoll and Bercovici (2014)), these details will vary so widely between Earth and Mars (and any other planets we may wish to consider using our model) that instead, we will simply treat this effective Peclet number as an additional free parameter in the model and allow for a wide range of values.

Finally, the rate of temperature change of the mantle, \dot{T}_m , is given by

$$Q_{\text{sec,m}} = M_m c_m \dot{T}_m \quad (62)$$

where M_m and c_m are the mantle's mass and specific heat capacity, respectively. Hence,

$$\dot{T}_m = \frac{Q_{\text{cmb}} + Q_{\text{rad,m}} - Q_{\text{surf,cond}} - Q_{\text{surf,melt}}}{M_m c_m}. \quad (63)$$

2.4.3 Thermal Evolution

The thermal history of the interior, including any possible core crystallization, can now be obtained by numerically integrating (55) and (63) through time (we use the first order Euler method, with $dt = 1$ Myrs, which is sufficient because of the small curvature in the temperature histories) subject to some assumed initial values for T_{cmb} , T_m , $Q_{\text{rad,c}}$, and $Q_{\text{rad,m}}$. At each time step, we explicitly solve the coupled set of equations to obtain T_{cmb} , Q_{cmb} , R_{ic} , and \dot{R}_{ic} (or R_{snow} and \dot{R}_{snow}) as functions of time. Finally, we use (3), (10), (12), and (16) to determine when thermally- and/or compositionally-driven dynamos may be active.

3 Results and Analysis

3.1 Thermal Histories

Before applying our model to Mars, we first benchmark its performance against the case of Earth, where we have better constraints. Figure 6 shows one possible thermal history for Earth, computed as described in section 2.4, where we have adopted the fixed properties given in Table 4 and the initial conditions and variable properties given in Table 5. The parameters were chosen to be similar to those adopted in previous work (e.g., Driscoll and Bercovici (2014))—though our mantle viscosity is defined in a way that differs from theirs and should be regarded as an effective viscosity, calibrated to yield a temperature structure and heat flows that are broadly consistent with modern estimates (e.g., Jaupart et al. (2015)). Figure 6c illustrates that the model delivers a present-day inner core radius (open circle in Figure 6c) consistent with the known value (Dziewonski & Anderson, 1981). Prior to inner core nucleation at ~ 3.6 Gyrs, the dynamo is driven entirely by thermal buoyancy (red dashed line in Figure 6d). As the inner core grows, compositional buoyancy (green dash-dotted line) becomes increasingly important. In the relatively near future (at ~ 4.57 Gyrs), the outer core becomes thermally stratified. Convection may persist after this, but must be driven entirely by compositional buoyancy. Figure 8a illustrates a present-day snapshot of the thermal history shown in Figure 6, illustrating the corresponding temperature structure, energy budget, and buoyancy fluxes. Our model neglects heat production within the lithosphere, but our energy budget is otherwise broadly consistent with previously estimated ranges (e.g., Figure 1 by Lay et al. (2008); Table 12 by Jaupart et al. (2015)).

Figure 7 shows one possible thermal history for Mars which follows from the fixed properties in Table 4 and the set of initial conditions and variable properties specified under 'Mars 1' in Table 5. In this example scenario, a thermal dynamo is possible for

Table 4. Fixed parameters adopted for thermal evolution models.

Parameter	Symbol	Value	Reference
Activation energy	A_v	300 kJ/mol	Karato and Wu (1993), Table 1
Critical Rayleigh number	Ra_{crit}	660	Turcotte and Schubert (1982)
Core specific heat capacity	c_c	840 J/kg/K	Stacey (1995); Nimmo (2015)
Mantle specific heat capacity	c_m	1260 J/kg/K	Tsuchiya et al. (2005), Figure 4
Latent heat of fusion for iron	L_{Fe}	750 kJ/kg	Nimmo (2015)
Gravitational energy density	E_G	300 kJ/kg	Driscoll and Bercovici (2014)
Core radioactive material half life	$t_{half,c}$	1.251 Gyrs	Driscoll and Bercovici (2014)
Mantle radioactive material half life	$t_{half,m}$	2.940 Gyrs	Driscoll and Bercovici (2014)

the first 500 Myrs but then the thermal buoyancy flux becomes negative (the outer core becomes thermally stratified), causing convection to shut down. An inner core then nucleates at around 4 Gyrs, introducing compositional buoyancy into the outer core. At this point, the rate of temperature decrease in the core slows dramatically (Figure 7a) because the heat flow out of the core becomes dominated by latent heat and because the similarity in the slopes of the core adiabat and the melting curve (Figure 8b) means that a given increment of cooling must be accompanied by a great deal of crystallization (as we discussed in section 2.4.1). Although a solid inner core is growing after ~ 4 Gyrs, the sum of the thermal and compositional buoyancy fluxes remains negative until ~ 4.76 Gyrs, meaning that outer core convection and a dynamo could reactivate after that time. Figure 8b illustrates a present-day snapshot of the thermal history shown in Figure 7, illustrating the corresponding temperature structure, energy budget, and buoyancy fluxes.

To illustrate the variety of possibilities, Figure 9 shows four additional example thermal histories (buoyancy flux histories only) for Mars, which follow from the Mars 2-5 columns in Table 5. Compared with the Mars 1 scenario shown in Figure 7, Mars 2 represents a case with a reduced mantle viscosity, permitting more rapid cooling at early times such that, by the time the inner core nucleates, the thermal stratification is so strong that compositional convection is not sufficient to reactivate the dynamo. Note that this more rapid cooling scenario also requires higher thermal conductivity and lower light element density contrast (i.e., larger partitioning coefficient, D_S) to ensure that the early thermal dynamo still operates for the first 500 Myrs but without compositional buoyancy being so strong that it would drive convection even today. In the Mars 3 scenario, the lower sulfur content and therefore higher melting temperature means that the inner core nucleates earlier, some ~ 500 Myrs after the demise of the early thermal dynamo, causing a brief period of compositionally-driven convection starting about ~ 1 Gyrs after thermal convection stopped. Because of the rapid cooling and smaller light element density contrast, compositional buoyancy can no longer overcome the thermal stratification after ~ 3.7 Gyrs, and the dynamo shuts down again permanently. In the Mars 4 scenario, the higher sulfur content lowers the melting temperature significantly but the starting temperature is also lower, allowing core crystallization to begin (in the iron snow regime) at ~ 3.2 Gyrs. At this point, because most of the energy coming out of the core is now latent heat, the temperature decline slows dramatically (kink in Figure 9c), but because the snow does not remelt (owing to its much lower sulfur content and therefore much higher melting point), there is no compositionally-driven convection. Finally, in the Mars 5 scenario, core crystallization begins at ~ 2.7 Gyrs and, assuming a partitioning coefficient very close to unity, the falling snow remelts and is able to drive convection for a brief period. As the remelting radius drops quickly, the snow driven convection weakens until convection shuts down again permanently.

Table 5. Variable parameters adopted for thermal evolution models illustrated in Figures 6–9. For Mars, $T_{\text{melt,cen}}$, D_m , and $\Delta\rho_\chi$, are not specified directly, they are computed from χ_S and D_S using (8), (9), (37), and (38) and shown here to the nearest K, km, or kg/m³; reference viscosities are computed as described in section 3.2.2 in order to ensure the early thermal dynamo terminates at 500 Myrs, and are shown here to the nearest power of ten.

Parameter	Symbol	Earth	Mars 1	Mars 2	Mars 3	Mars 4	Mars 5
Initial CMB temperature	T_{cmb}	5900 K	2200 K	2200 K	2200 K	2000 K	2000 K
Initial mid-mantle temperature	T_m	3300 K	1800 K	1800 K	1800 K	1600 K	1600 K
Initial core radiogenic heat	$Q_{\text{rad,c}}$	35 TW	5 TW	5 TW	5 TW	5 TW	5 TW
Initial mantle radiogenic heat	$Q_{\text{rad,m}}$	25 TW	0 TW	0 TW	0 TW	0 TW	0 TW
Core sulfur mass fraction	χ_S	-	6 wt%	6 wt%	4.5 wt%	8 wt%	9 wt%
Light element partitioning coefficient	D_S	-	0.05	0.5	0.5	0.5	0.99
Core melting temperature at $r = 0$	$T_{\text{melt,cen}}$	5700 K	2086 K	2086 K	2201 K	1932 K	1855 K
Melting curve length scale	D_m	5000 km	6059 km	6059 km	5809 km	6592 km	6981 km
Light element density contrast	$\Delta\rho_\chi$	500 kg/m ³	694 kg/m ³	276 kg/m ³	225 kg/m ³	330 kg/m ³	5.7 kg/m ³
Core thermal conductivity	k_c	120 W/m/K	56 W/m/K	89 W/m/K	89 W/m/K	56 W/m/K	89 W/m/K
Mantle reference viscosity at 1500 K	ν_{ref}	10 ¹⁹ m ² /s	10 ¹⁸ m ² /s	10 ¹⁷ m ² /s	10 ¹⁷ m ² /s	10 ¹⁷ m ² /s	10 ¹⁶ m ² /s
LM/UM viscosity ratio	f	15	2	2	2	2	2
Surface heat flow Peclet number	Pe	0.1	0.0	0.0	0.0	0.0	0.0
Surface temperature	T_{surf}	288	210	210	210	210	210
Core crystallization style		bottom-up	bottom-up	bottom-up	bottom-up	iron snow	iron snow
Thermally-driven convection		until ~ 4.57 Gyrs	until 500 Myrs	until 500 Myrs	until 500 Myrs	until 500 Myrs	until 500 Myrs
Compositionally-driven convection		from ~ 3.65 Gyrs	from ~ 4.76 Gyrs	never	~ 1.60 – 3.75 Gyrs	never	~ 2.69 – 2.82 Gyrs

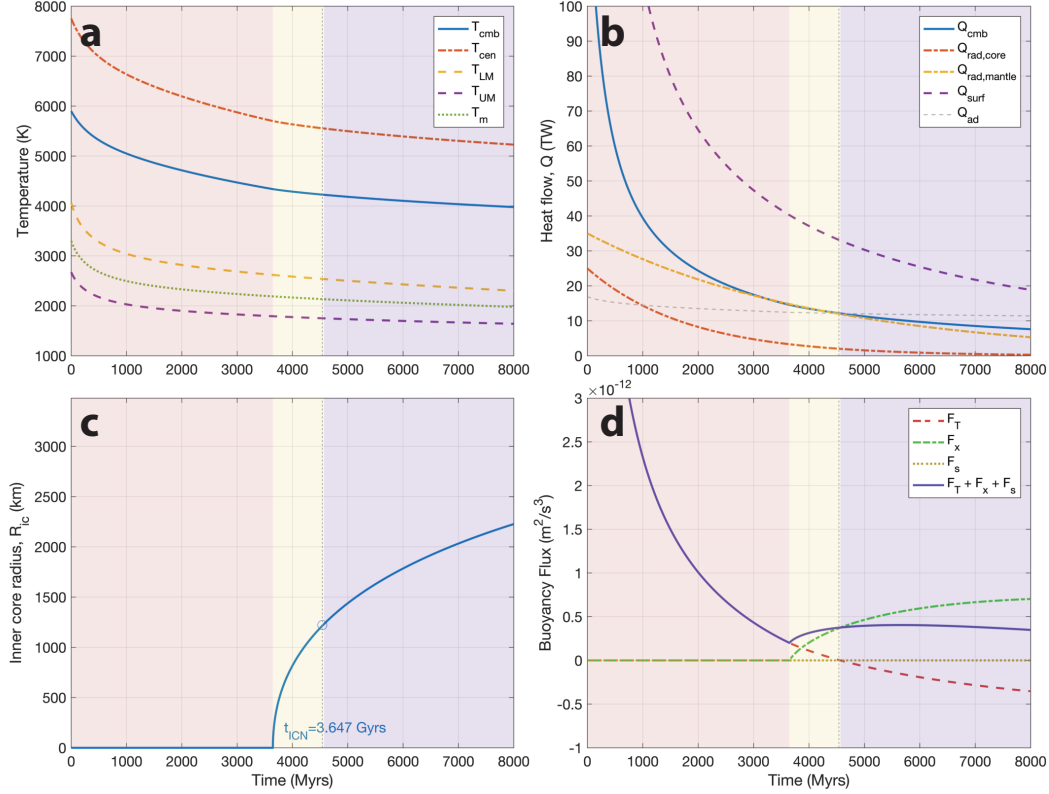


Figure 6. Example time evolution of Earth's (a) temperature structure, (b) heat flows, (c) inner core radius, and (d) buoyancy fluxes, where CMB = core mantle boundary; cen = zero radius; LM = top of lower mantle thermal boundary layer; UM = bottom of upper mantle thermal boundary layer; rad = radiogenic, surf = surface. The open circle in (c) represents the known present-day inner core radius. For the buoyancy fluxes in (d), the red dashed line represents thermal buoyancy flux, the green dash-dotted line represents compositional buoyancy flux, and the solid blue line represents the sum of the two. The red shaded region represents the thermally driven dynamo regime; purple shading represents the compositionally driven dynamo regime; yellow shading represents the period where both thermal and compositional buoyancy contribute to driving convection and the dynamo. A thin dashed line marks the present day at 4.54 Gyrs.

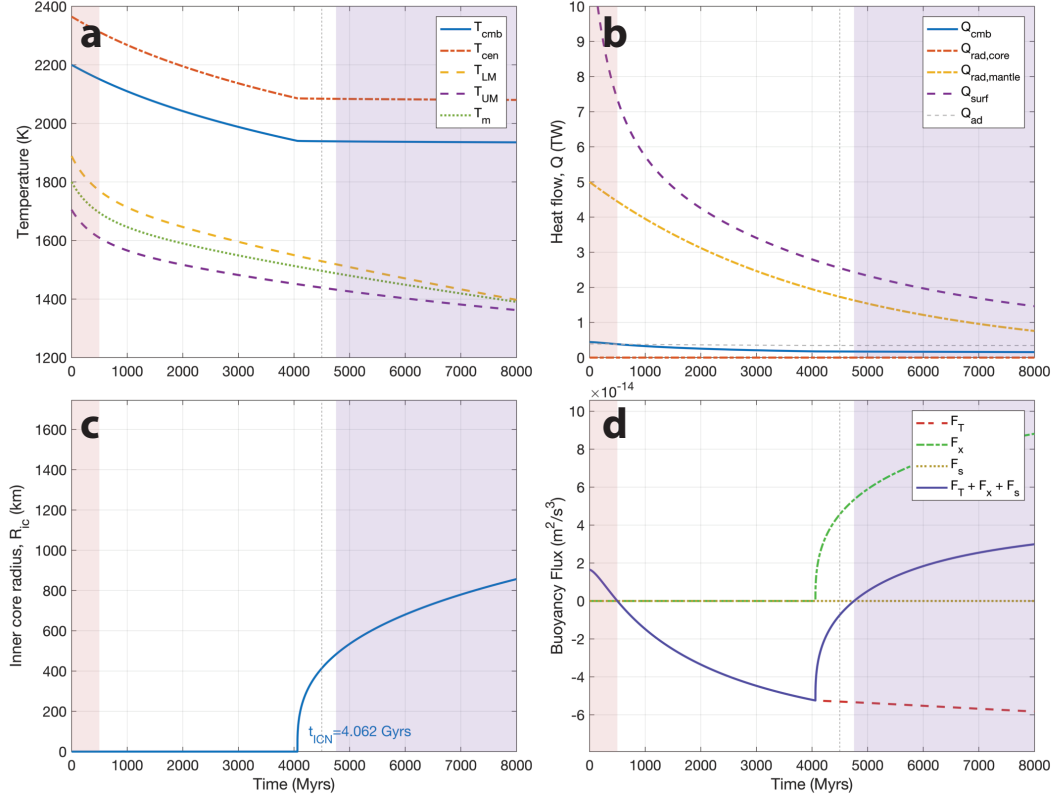


Figure 7. Example time evolution of the Martian (a) temperature structure, (b) heat flows, (c) inner core radius, and (d) buoyancy fluxes, adopting the Mars 1 parameters from Table 5, where CMB = core mantle boundary; cen = zero radius; LM = top of lower mantle thermal boundary layer; UM = bottom of upper mantle thermal boundary layer; rad = radiogenic, surf = surface. For the buoyancy fluxes in (d), the red dashed line represents thermal buoyancy flux, the green dash-dotted line represents compositional buoyancy flux, and the solid blue line represents the sum of the two. The red shaded region represents the thermally driven dynamo regime operating for the first 500 Myrs; purple shading represents the compositionally driven dynamo regime; the absence of shading (white region) represents the period where there is no convection and therefore no dynamo. A thin dashed line marks the present day at 4.5 Gyrs.

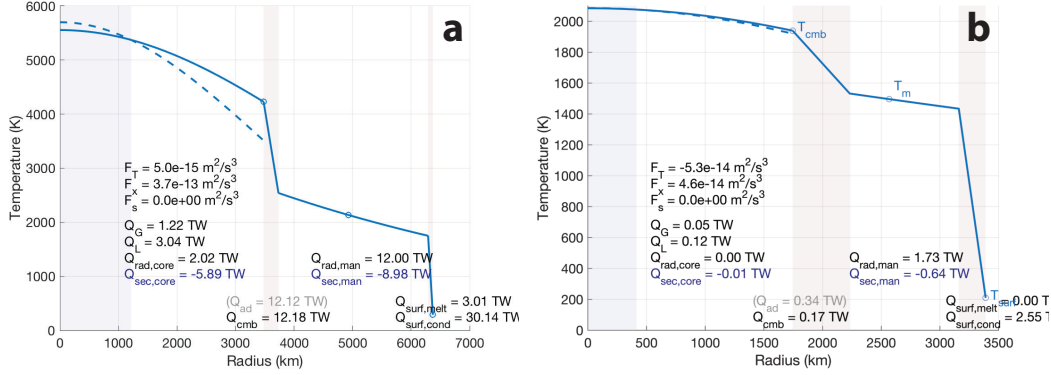


Figure 8. Temperature structure, heat flows, and buoyancy fluxes for Earth (a) and Mars (b). These are present-day snapshots of the thermal histories illustrated in Figures 6 and 7, respectively, and are the same as the cases illustrated in Figure 2a,b but additionally showing heat flows (energy budget) and buoyancy fluxes computed as described in sections 2.4 and 2.1. Pale red shading highlights the two conductive thermal boundary layers at the top and bottom of the mantle. Pale blue shading at the left indicates the presence of a solid inner core. Although a solid inner core is growing in both cases, the net buoyancy flux in (b) is negative, meaning the compositional buoyancy flux is not sufficient to power a dynamo at the present day.

3.2 Parameter Space Exploration

Whereas Figures 7 and 9 illustrate just a few possible thermal histories for Mars, exploring a wide range of parameters will allow us to determine more generally which initial conditions and material properties permit convection during which periods of Mars' history and future. Although the large number of parameters makes the parameter space too large to explore exhaustively, we break the problem down into parts, exploring subsets of the parameter space systematically in a way that yields a series of useful insights. In particular, we will first study the parameters that control the timing of the demise of the early thermal dynamo (3.2.2) and then use the approximately known thermal dynamo end time to constrain the parameter space significantly before examining the parameters affecting the possible subsequent compositional dynamo (3.2.3). Throughout the parameter space exploration, the Mars 1-5 cases defined in Table 5 will serve as points of reference, wherever possible.

3.2.1 Parameter Ranges

First, we note that several of the variable parameter ranges can be bounded to some degree. Assuming the Martian core is at least partly liquid, the CMB temperature must be above the Fe-FeS eutectic, which is around 1600 K at 20 GPa (Boehler, 1996), and so the initial CMB temperature, $T_{\text{cmb,init}}$, must have been at least somewhat larger, perhaps 1700 K. It is more difficult to establish an upper limit for the initial CMB temperature, but we consider values up to 2500 K, which is approximately the mantle solidus at the CMB—because a molten mantle will cool extremely rapidly, we assume the Martian mantle is entirely solid by the beginning of our simulations. In general, we assume the initial mid-mantle temperature was similar to or somewhat smaller than the initial CMB temperature, though we consider a wide range of possibilities, from 1500 K to 2300 K. As a point of reference, the Earth's upper mantle viscosity is estimated to be roughly 10^{20} – 10^{21} Pas ($\sim 10^{17}$ m²/s) at around 1500 K (Mitrovica & Forte, 2004). However, we allow for a wide range of possible reference mantle viscosities, from 10^{14} m²/s to 10^{19} m²/s

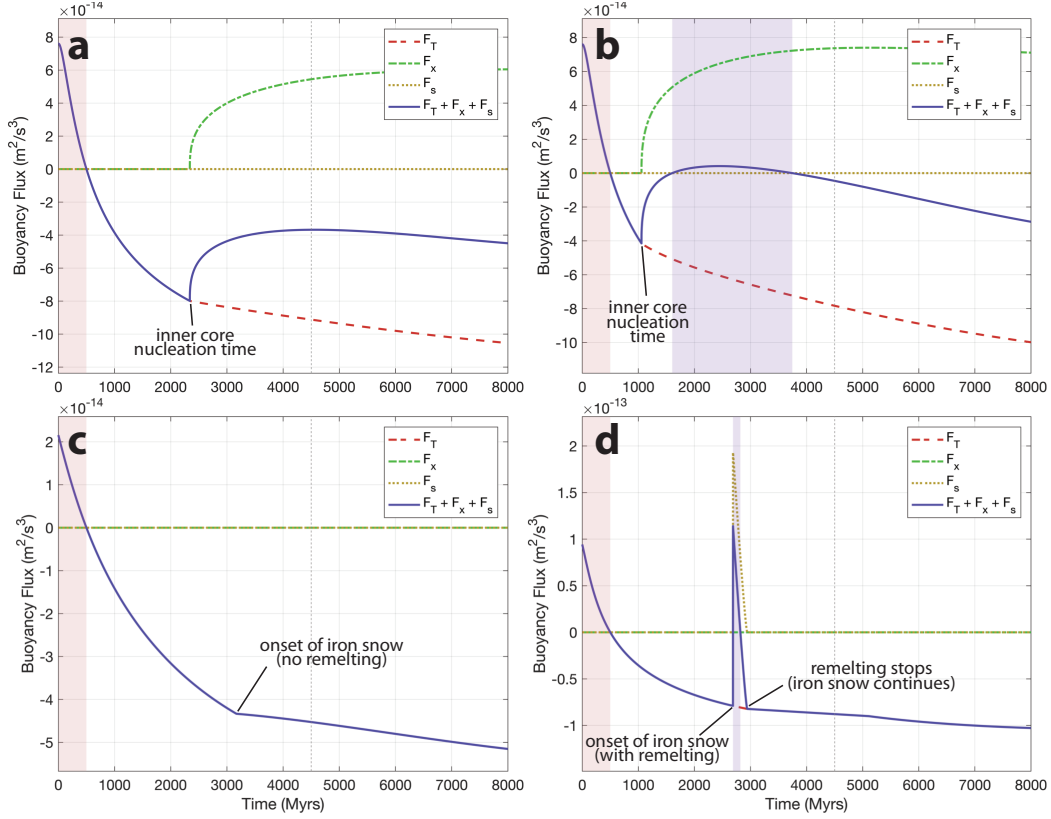


Figure 9. Example time evolution of Martian buoyancy fluxes for the cases labeled in Table 5 as Mars 2 (a), Mars 3 (b), Mars 4 (c), and Mars 5 (d). The red dashed line represents thermal buoyancy flux, the green dash-dotted line represents buoyancy flux arising from inner core growth, the dotted gold line represents the snow-driven buoyancy flux, and the solid blue line represents the sum of the three. The red shaded region at the left represents the early thermally driven dynamo regime operating for the first 500 Myrs; purple shading represents the compositionally driven dynamo regime; the absence of shading (white region) represents the period where there is no convection and therefore no dynamo. A thin dashed line marks the present day at 4.5 Gyrs.

(roughly 10^{17} – 10^{23} Pas), and emphasize that we are concerned more with the effect of varying mantle viscosity than in the absolute numbers. We consider a wide range of thermal conductivities for the Martian core (see e.g., Suehiro et al. (2017); Hsieh et al. (2020)), from as low as 30 W/m/K to as high as 120 W/m/K, allowing for the extreme possibility of nearly pure iron.

3.2.2 Early Dynamo Driven by Thermal Convection

Before discussing the effects of compositional buoyancy arising from a crystallizing core, we focus on an early Martian dynamo driven by thermal convection. We focus on thermal buoyancy flux and the model parameters that control it because we take a positive thermal buoyancy flux to be a proxy for the presence of a dynamo driven by thermal convection. From equation (3), it is clear that a positive thermal buoyancy flux requires that q_T , given by (4), be positive—that is, the CMB heat flux must exceed the adiabatic heat flux. The latter is given by (5) and depends on the CMB temperature and the core thermal conductivity, thermal expansivity, and specific heat capacity. The CMB heat flux is given by (60) and depends on the lower mantle thermal boundary layer thickness and thermal conductivity, and the temperature drop across it. In general, the CMB heat flux is initially superadiabatic (i.e., q_T is initially positive) and decreases over time as the core and mantle temperatures gradually converge, decreasing the temperature jump at the CMB. If the core and mantle temperatures are initially similar, however, q_T (and therefore the thermal buoyancy flux) initially increases before reaching a peak and then decreasing for the rest of the planet’s history (Figure 10). Similarly, although we do not show it here, the presence of radioactive elements in the core would tend to delay the peak in q_T (and thermal buoyancy flux). The timing of the peak is likewise delayed by higher mantle viscosities (Figure 10, Figure 11). Increasing the Peclet number means that relatively more heat escapes through the top of the mantle, which in turn keeps CMB heat flow higher, thus decreasing the rate at which q_T drops. Hence, although we do not illustrate this effect here, if q_T is initially positive, a higher Peclet number would lead q_T to remain positive for slightly longer (e.g., for the cases illustrated in Figures 7 and 9, increasing the Peclet number from 0.0 to 0.5 would delay the end of thermal convection from ~ 500 Myrs to ~ 750 Myrs).

The inference from crustal magnetic anomalies that the Martian dynamo was active early and ceased ~ 500 Myrs after formation thus suggests a relatively large initial core-mantle temperature difference (as previously argued by J.-P. Williams and Nimmo (2004)) and/or a relatively low mantle viscosity. On the other hand, if the mantle viscosity is too low, the top of the core remains superadiabatic (i.e., q_T remains positive) for a much longer period, unless the core thermal conductivity is very high (Figure 10a, Figure 12). Hence, an early dynamo driven by thermal convection and ending ~ 500 Myrs after formation is permitted only under a fairly narrow range of conditions—namely, when ΔT_{init} is sufficiently large (i.e., upper left parts of Figure 11) and for certain combinations of reference mantle viscosity and core thermal conductivity (i.e., along the dashed white lines in Figure 12). Figure 13 shows this early dynamo constraint in terms of the implied reference mantle viscosity as a function of initial CMB and mid-mantle temperatures. This requirement that permissible combinations of initial temperatures imply particular values of reference mantle viscosity and core thermal conductivity, helps to reduce the range of possibilities we will need to explore below when discussing compositionally-driven convection.

3.2.3 Compositionally-Driven Convection

Up to this point, we have focused on the early thermal dynamo, whose timing is independent of core composition—provided the core does not begin to crystallize before the thermal dynamo shuts down. The purpose of section 3.2.2 was mainly to constrain the relationship between several of the model parameters in order to make the rest of

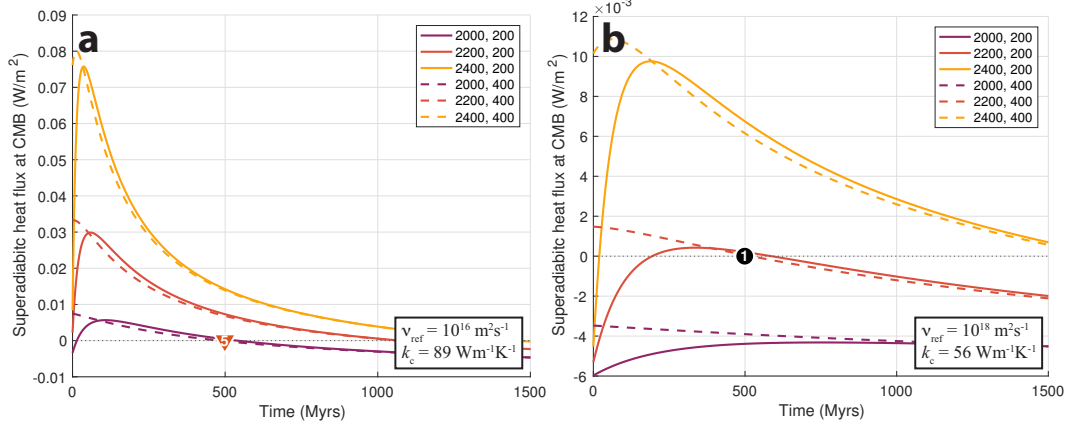


Figure 10. Superadiabatic heat flux, q_T , given by (4), for the first 1.5 Gyrs after the formation of Mars assuming various initial CMB and mid-mantle temperatures and either rapid cooling (with reference mantle viscosity $\nu_{\text{ref}}=10^{16} \text{ m}^2/\text{s}$, and core thermal conductivity $k_c=89 \text{ W/m/K}$) (a) or slower cooling (with $\nu_{\text{ref}}=10^{18} \text{ m}^2/\text{s}$ and $k_c=56 \text{ W/m/K}$) (b). Initial CMB temperatures are represented by different colors (2000 K, 2200 K, or 2400 K; see inset) and solid and dashed lines represent cases where the CMB to mid-mantle temperature drops are 200 K or 400 K, respectively. Higher values of k_c would shift the curves downward. The Peclet number is assumed to be zero for all curves; higher Peclet numbers would shift the curves slightly to the right. The peak in q_T occurs earlier for lower mantle viscosities, higher initial CMB temperatures, and larger core-mantle temperature differences. The black circle in (b) corresponds to the Mars 1 reference case and the red triangle in (a) corresponds to the Mars 5 reference case (Table 5); in both cases, the superadiabatic heat flux begins at its peak and then declines, reaching zero at 500 Myrs.

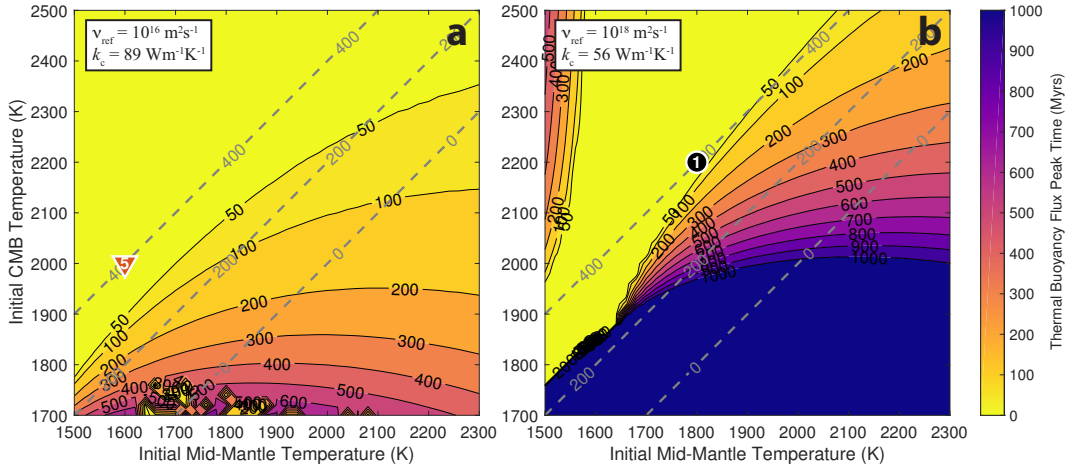


Figure 11. Timing of peak thermal buoyancy flux assuming either rapid cooling (with $\nu_{\text{ref}}=10^{16} \text{ m}^2/\text{s}$ and $k_c=89 \text{ W/m/K}$) (a) or slower cooling (with $\nu_{\text{ref}}=10^{18} \text{ m}^2/\text{s}$ and $k_c=56 \text{ W/m/K}$) (b). Superadiabatic heat flux (Figure 10), and thus thermal buoyancy flux, peaks early (i.e., peak time is $\lesssim 100$ Myrs) only when the initial core-mantle temperature difference ($\Delta T_{\text{init}}=T_{\text{cmb,init}}-T_{\text{m,init}}$) is sufficiently large. Grey dashed lines illustrate contours of constant ΔT_{init} . The black circle in (b) corresponds to the Mars 1 reference case and the red triangle in (a) corresponds to the Mars 5 reference case (Table 5); in both cases, the thermal buoyancy flux begins at its peak and declines steadily thereafter (Figure 10).

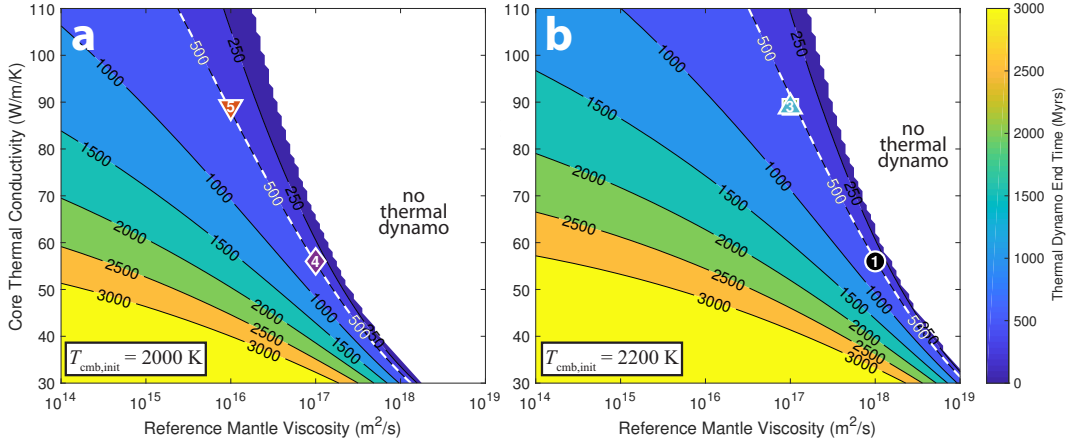


Figure 12. Timing of the end of thermal convection (i.e., when thermal buoyancy flux becomes negative) as a function of core thermal conductivity and reference mantle viscosity, and assuming initial CMB temperatures of either 2000 K (a) or 2200 K (b) and $\Delta T_{\text{init}}=400$ K. The blank white regions represent parts of the parameter space where the mantle viscosity is too high and/or the thermal conductivity is too large for the thermal buoyancy flux to ever be positive (i.e., the core is thermally stratified to begin with and never undergoes thermal convection)—the rough edges are an artifact of the finite grid resolution. The white dashed lines represent the approximate time at which the early Martian dynamo is thought to have shut down. The numbered symbols indicate the Mars 1-5 reference cases defined in Table 5, whose time histories are illustrated in Figures 7 and 9; Mars 2 and Mars 3 occupy the same point in (b).

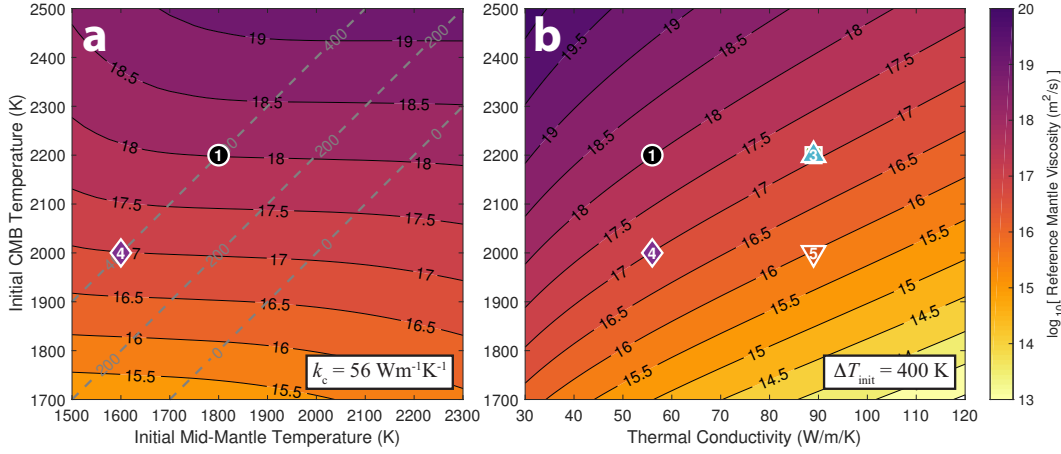


Figure 13. Reference mantle viscosity required to yield an early thermal dynamo that ends 500 Myrs after the formation of Mars. We consider: (a) a range of initial CMB and mid-mantle temperatures and a fixed core thermal conductivity of $k_c=56$ W/m/K; or (b) a range of initial CMB temperatures and core thermal conductivities and a fixed $\Delta T_{\text{init}}=400$ K, ensuring the thermal dynamo initiates early (see Figure 11). Grey dashed lines in (a) illustrate contours of constant ΔT_{init} . The numbered symbols indicate the Mars 1-5 reference cases defined in Table 5 and illustrated in Figures 7 and 9; Mars 2 and Mars 3 occupy the same point in (b).

the parameter space exploration more tractable once we begin to consider the variable of core composition (i.e., sulfur content).

Bottom Up Crystallization Regime

When the sulfur content and thermal expansivity are sufficiently small, the Martian core crystallizes from the bottom up (Figure 4b). A solid inner core nucleates when the central temperature, T_{cen} , drops below the central melting temperature, $T_{\text{melt,cen}}$. The time at which this occurs is a function of the melting curve (which depends on the core composition—i.e., its sulfur content), the initial core temperature, and the rate at which core temperature declines. In the absence of radiogenic heating in the core, the latter is entirely a function of the CMB heat flow and hence depends mainly on the mantle viscosity and the temperature difference between the core and mantle, which in turn has a small dependence on the surface heat flow Peclet number. However, if we again require that the early thermal dynamo ends at 500 Myrs, then any given combination of initial CMB and mid-mantle temperatures constraints the mantle reference viscosity (Figure 13). Hence, the only remaining relevant variable is the sulfur content, χ_{S} , which determines the melting temperature, $T_{\text{melt,cen}}$, which then determines when the inner core nucleates and the implied present-day inner core radius (Figure 14). Although core thermal conductivity has no effect on the timing of inner core nucleation, its influence on the timing of the demise of the thermal dynamo means that core thermal conductivity is relevant to the constraint on mantle viscosity (Figure 13) and is therefore indirectly relevant to inner core growth (Figure 14). Though we do not show it here, the surface heat flow Peclet number has an additional small effect, with larger Peclet numbers likewise corresponding to more rapid cooling and earlier inner core nucleation, and therefore larger present day inner core radii. A present-day solid inner core is possible under a wide range of conditions as long as the melting temperature is sufficiently high (i.e., the sulfur content is sufficiently low) and the initial CMB temperature is sufficiently low (Figure 14).

As the solid inner core is growing, however, compositional convection becomes increasingly important. As a result, not all combinations of parameters in Figure 14 are compatible with net buoyancy flux being negative at present or with the early thermal dynamo shutting down at ~ 500 Myrs. The compositional buoyancy flux, given by (10), and thus the vigor of compositional convection, is a function of the inner core’s mass growth rate (i.e., its surface area and rate of change of its radius) and the density contrast, $\Delta\rho_{\chi}$, between the liquid outer core and the light elements that are being rejected as the inner core grows—an additional parameter that we have not yet discussed because it does not affect any of the results we have seen so far in this section. The density contrast is, however, what accounts for the much stronger compositional buoyancy flux in the Mars 1 case compared to the Mars 2 and 3 cases (compare Figure 7d against Figures 9a,b). Because it is the mass growth rate that matters, compositional buoyancy flux is small at first due to the inner core’s initially negligible surface area, even though the inner core radius may be increasing rapidly. However, if the density contrast is large enough and the inner core begins growing early enough, the net buoyancy flux can eventually become positive again (Mars 1 case, Figure 7d). Inner core nucleation time is a function of the initial core temperature relative to the melting temperature, and the rate at which the core is cooling. The latter is indirectly a function of core thermal conductivity: higher core thermal conductivity (which implies lower mantle viscosity to satisfy the 500 Myr early thermal dynamo requirement) translates to more rapid core cooling and earlier nucleation of the inner core. Higher surface heat flow Peclet numbers likewise drive more rapid cooling and earlier inner core nucleation. The subsequent evolution of net buoyancy flux then depends primarily on the light element density contrast, with higher density contrasts (a consequence of a small light element partitioning coefficient, D_{S}) yielding larger net buoyancy fluxes.

Figures 14, 15, and 16 illustrate the effects of varying the core sulfur content, χ_s , as well as either the initial CMB temperature (Figure 14), the core thermal conductivity, k_c (Figure 15), or the light element partitioning coefficient, D_S (Figure 16). If the sulfur content is too small, the inner core would nucleate early and compositional convection would bolster early thermal convection, precluding dynamo cessation at ~ 500 Myrs (blank white regions). Similarly, even if sulfur content and/or the initial CMB temperature were sufficiently high to permit the early thermal dynamo to shut down at ~ 500 Myrs, large portions of the parameter space must be excluded because they would yield a positive net buoyancy flux today (pale white shading). Conversely, if the sulfur content is relatively higher, depressing the melting temperature, and/or the initial temperatures are too high, the inner core would nucleate late and compositional convection would never be sufficient to reactivate the dynamo (dark shading). Under certain conditions, it is also possible that compositional buoyancy, though not sufficient to drive convection today, was sufficient in the past (pale blue shading) or will be sufficient in the future (pale orange shading). If D_S is small and a solid inner core is present today, convection may well reactivate at some point in the future (e.g., the Mars 1 case). It is also possible that there was a limited period of compositionally-driven convection in the past (e.g., Mars 3), but this may be difficult as it requires D_S to be somewhat large (~ 0.3 or more) in order to maintain a small light element density contrast, and it requires relatively rapid cooling (high thermal conductivity and low mantle viscosity), allowing net buoyancy flux to fall over time after an initial peak driven by compositional buoyancy (Figure 9b).

Top Down Crystallization (Iron Snow) Regime

When the sulfur content is very high, and thus the core melting temperature is very low, core crystallization may still occur if the initial temperatures are sufficiently low, but the iron crystals will form at the top of the core and sink as iron snow. If the falling snow crystals warm enough to remelt, they can drive convection in the underlying fluid. However, this requires the melting curve for the solid iron to be very similar to that of the bulk liquid core, which is the case only if the light element partitioning coefficient, D_S , is close to unity (see Mars 5 at the extreme top right of Figure 16d). Moreover, even if such a large partitioning coefficient is possible, the resulting density contrast between the snow and the bulk liquid core is consequently small (e.g., in the Mars 5 case, with $D_S=0.99$, $\Delta\rho_{\text{snow}} \approx 5.7 \text{ kg/m}^3$). Hence, although large portions of the parameter space permit iron snow, the falling snow generally does not remelt, and therefore is not able to drive convection.

4 Discussion

4.1 Controlling parameters

Our analysis has built upon previous Martian thermal evolution studies by further clarifying the relationships between several of the most important unknown or poorly constrained parameters. We showed that there are multiple ways of ensuring that a thermal dynamo shuts down ~ 500 Myrs after formation, even without a large initial core-mantle temperature difference (e.g., via very low mantle viscosity; Figure 13a), but a large initial core-mantle temperature difference is required to ensure a strong thermal dynamo that is active for a significant period before shutting down (Figure 11; J.-P. Williams and Nimmo (2004)). We showed that fixing the time of the end of thermal convection places a strong constraint on the trade-off between mantle viscosity and core thermal conductivity: lower mantle viscosity corresponds to higher CMB heat flow, and therefore stronger thermal buoyancy flux, which will prolong thermal convection unless the core thermal conductivity is also higher, reducing the superadiabatic heat flow (Figure 12). Although the initial temperatures are not well constrained on their own, they are closely linked to mantle viscosity and core thermal conductivity: lowering the assumed starting tem-

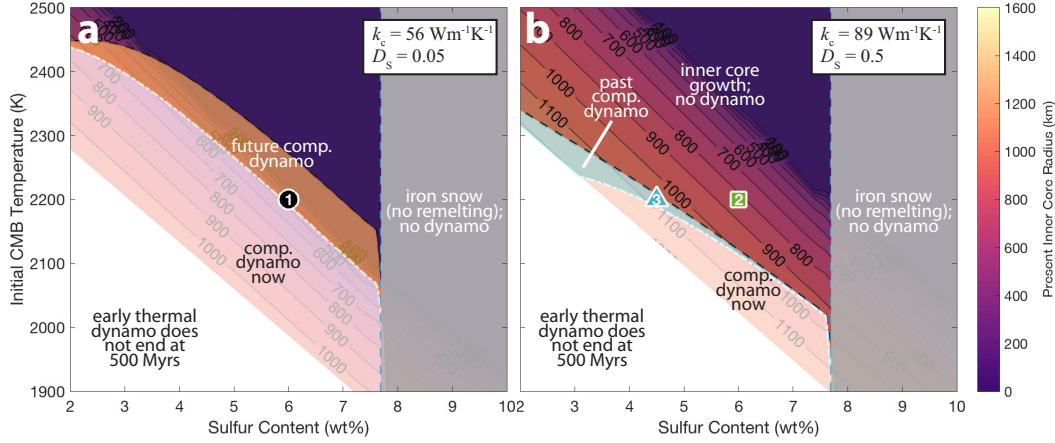


Figure 14. Present day solid inner core radius as a function of initial CMB temperature and sulfur content, assuming $\Delta T_{\text{init}}=400$ K and the reference mantle viscosities shown in Figure 13 (ensuring the early thermal dynamo terminates at ~ 500 Myrs) and either: (a) relatively slow cooling with $k_c=56$ W/m/K; or (b) more rapid cooling with $k_c=89$ W/m/K. The black circle in (a) corresponds to the Mars 1 reference case, in which the present inner core radius is 414 km; the green square and the blue triangle in (b) correspond, respectively, to the Mars 2 and 3 reference cases, in which the present inner core radii are 825 km and 1071 km. The blank white region at the lower left is excluded because the early thermal dynamo does not terminate at 500 Myrs. The pale white shading left of the dash-dotted white line represents the part of parameter space in which the present net buoyancy flux is positive, which we take to be incompatible with the lack of a present-day dynamo. In the dark region to the right of the black dashed line, net buoyancy flux is never positive again after the demise of the early thermal dynamo. In the region between the white and black curves, compositional buoyancy flux is positive either in the future (pale orange shading) or in the past (pale blue shading). The blue dashed line at ~ 7.7 wt%S marks the boundary between bottom-up and top-down (iron snow, grey shading) core crystallization. The numbered symbols indicate the Mars 1-3 reference cases defined in Table 5, whose time histories are illustrated in Figures 7 and 9.

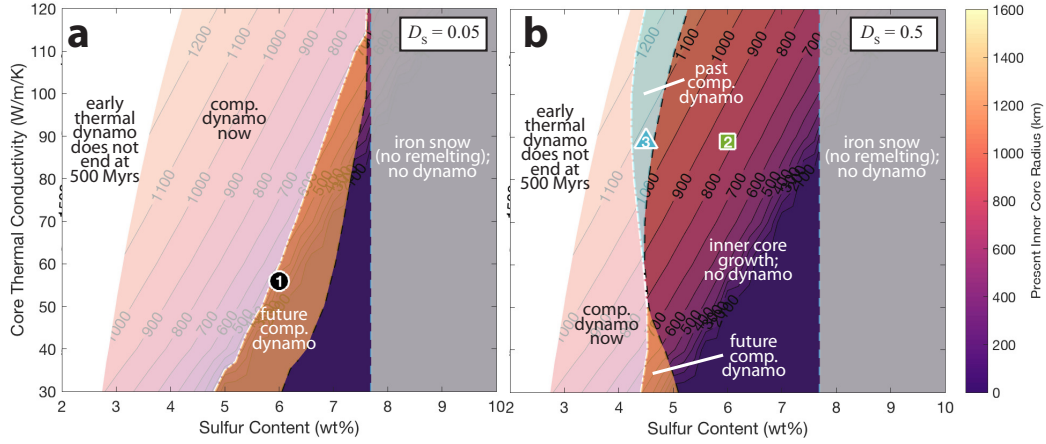


Figure 15. Present inner core radius as a function of core sulfur content and thermal conductivity, assuming $T_{\text{cmb,init}}=2200$ K, $\Delta T_{\text{init}}=400$ K, and partitioning coefficients of either 0.05 (a) or 0.5 (b). The blank white region at the left is excluded because the early thermal dynamo does not terminate at 500 Myrs. The pale white shading left of the dash-dotted white line represents the part of parameter space in which the present net buoyancy flux is positive, which we take to be incompatible with the lack of a present-day dynamo. In the dark region to the right of the black dashed line, net buoyancy flux is never positive again after the demise of the early thermal dynamo. In the region between the white and black curves, compositional buoyancy flux is positive either in the future (pale orange shading) or in the past (pale blue shading). The blue dashed line at ~ 7.7 wt%S marks the boundary between bottom-up and top-down (iron snow, grey shading) core crystallization. The numbered symbols indicate the Mars 1-3 reference cases defined in Table 5, whose time histories are illustrated in Figures 7 and 9.

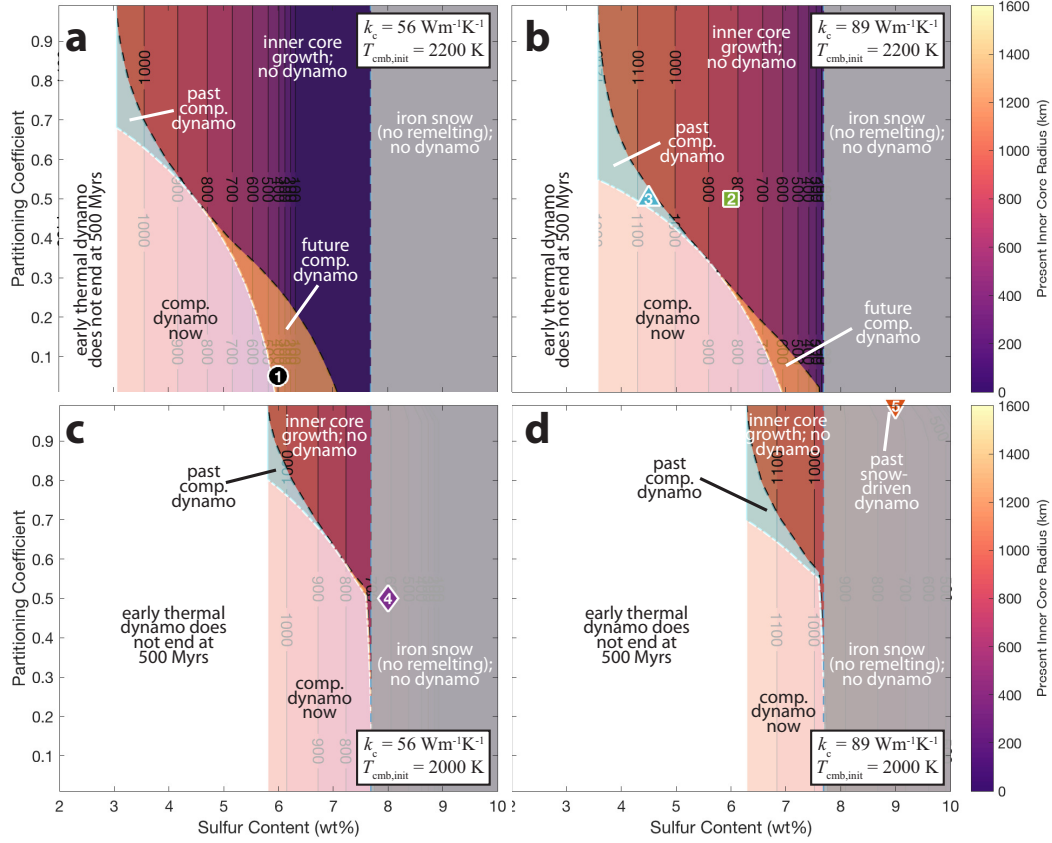


Figure 16. Present inner core radius as a function of core sulfur content and the partitioning coefficient, assuming an initial CMB temperature of either 2200 K (a,b) or 2000 K (c,d) and assuming either $k_c=56$ W/m/K (a,c) or $k_c=89$ W/m/K (b,d). The blank white region at the left is excluded because the early thermal dynamo does not terminate at 500 Myrs. The pale white shading left of the dash-dotted white line represents the part of parameter space in which the present net buoyancy flux is positive, which we take to be incompatible with the lack of a present-day dynamo. In the dark region to the right of the black dashed line, net buoyancy flux is never positive again after the demise of the early thermal dynamo, except in the iron snow regime with remelting (extreme top right of d). In the region between the white and black curves, compositional buoyancy flux is positive either in the future (pale orange shading) or in the past (pale blue shading). The blue dashed line at ~ 7.7 wt%S marks the boundary between bottom-up and top-down (iron snow, grey shading) core crystallization. The numbered symbols indicate the Mars 1-5 reference cases defined in Table 5, whose time histories are illustrated in Figures 7 and 9.

perature by 200 K, for example, requires either lowering the mantle viscosity by an order of magnitude or lowering the core thermal conductivity by roughly 30 W/m/K in order to maintain the same thermal dynamo end time (Figure 13). Hence, any constraints that can be independently placed on mantle viscosity and core thermal conductivity effectively constrain the initial CMB temperature as well. For the bottom-up inner core growth regime, our results also clarified the trade-off between initial CMB temperature and core sulfur content as it relates to the radius of the solid inner core (Figure 14).

4.2 Possible dynamo histories

Our analysis has demonstrated that there is a range of possibilities for the history and future of the Martian dynamo that are compatible with an early thermal dynamo operating until ~ 500 Myr after formation and the lack of a dynamo operating at present. Some, but not all of these scenarios, are also compatible with the presence of a solid inner core today. Below, we summarize the possibilities:

1. **No crystallization:** If the core is sufficiently hot or its sulfur content is sufficiently high (depressing the melting temperature), the core may be entirely liquid and could remain so for billions of years to come. In this scenario, compositionally driven convection never takes place.
2. **Bottom up crystallization:** If the core's sulfur content, thermal expansivity, and temperature are sufficiently low, the core can crystallize from the bottom up in a fashion similar to Earth's ongoing inner core growth. In this bottom-up inner core growth regime, ongoing crystallization and light element rejection may or may not generate sufficient buoyancy to reactivate the dynamo after the demise of the early thermal dynamo. Possibilities include:
 - (a) **Inner core growth, but no dynamo:** If the core cools sufficiently rapidly at early times such that cooling is now slow, buoyancy arising from a crystallizing solid inner core is insufficient to overcome thermal stratification, meaning that no compositionally driven dynamo ever operates.
 - (b) **Inner core growth, future dynamo:** If the light element density contrast ($\Delta\rho_\chi$) is sufficiently large, and the inner core nucleated only recently, compositionally-driven convection may be insufficient to drive a dynamo at present, but could become sufficient to reactivate the dynamo in the future.
 - (c) **Inner core growth, past dynamo:** If the light element density contrast is lower and the core has already cooled a great deal, a compositionally-driven dynamo may have operated for a brief period in the past before shutting down permanently at some point before the present, owing to low core heat flow.
3. **Top down crystallization:** If the core's sulfur content and/or thermal expansivity are sufficiently high (see Figure 4b), but the temperature is sufficiently low, the core can crystallize from the top down in the iron snow regime. In such a top-down crystallization scenario:
 - (a) **Iron snow, brief dynamo:** If the light element partitioning coefficient (D_S) is sufficiently close to unity (i.e., the light elements partition almost as much into the solid as into the liquid), then if crystallization begins (either in the past or the future), the falling iron snow could remelt and mix into the layer below, driving convection from above. Such snow-driven convection would continue until the core is too cool for the snow to remelt, at which point the falling snow would accumulate at the center of the core, shutting down all convection.
 - (b) **Iron snow, but no dynamo:** If no part of the core is ever warm enough for the falling snow to remelt (i.e., if D_S is small), the snow would accumulate at the center of the core and no snow-driven dynamo would ever operate. In this scenario, iron snow may be forming even now, but will never be able to power a dynamo.

4.3 Implications of a solid inner core

In light of the above list of possibilities, confirmation of the presence or absence of a solid inner core could have several implications. For example:

- The detection of a solid inner core today immediately constrains the relationship between the initial core temperature and the sulfur content (with higher sulfur content requiring lower initial temperatures, as illustrated in Figure 14).
- A solid inner core today is compatible with the bottom-up core crystallization regime (if sulfur content is low) with compositionally driven convection occurring either in the past (e.g., Mars 3; requires small $\Delta\rho_\chi$ [large D_S] and rapid cooling), future (e.g., Mars 1; requires recent inner core nucleation and larger $\Delta\rho_\chi$ [small D_S]), or never (e.g., Mars 2; requires rapid cooling but late inner core nucleation, perhaps due to high initial temperatures).
- A solid inner core today is also compatible with a period of snow-driven convection (if sulfur content is high) operating in the past (e.g., Mars 5; requires D_S approaching unity), but not the future.
- Conversely, the absence of a solid inner core today is compatible with a period of compositionally driven convection (in either top-down or bottom-up crystallization regimes) in the future, but not the past.
- The absence of a solid inner core today is, of course, also compatible with the possibility that no part of the Martian core ever crystallizes (if the core is sufficiently hot or its sulfur content is sufficiently high).

Of particular interest is the possibility of compositionally-driven convection operating for a limited period following the demise of the early thermal dynamo but shutting down again before the present (exemplified by the Mars 3 case; pale blue shading in Figures 14–16). This scenario is interesting in that it could help explain observations of magnetized units that apparently post-date the formation of the large impact basins (e.g., Mittelholz et al. (2020)). On the other hand, this scenario requires a relatively large light element partitioning coefficient ($D_S > 0.3$), which is not expected at Mars core pressures (Zhang et al., 2020). A smaller partitioning coefficient would yield a larger light element density contrast, leading to stronger compositional buoyancy, that would remain effective even to the present day. If the partitioning coefficient is small, then the only possibilities for a compositionally-driven dynamo is that it becomes active at some point in the future (pale orange shading in Figures 14–16), or not at all. If the partitioning coefficient is small and a solid inner core is detected, then, for almost any combination of the other parameters, compositionally-driven convection will become active within the next ~ 1 Gyrs. Conversely, if the Martian core is confirmed to be entirely liquid, then it would not be clear whether or not compositionally-driven convection will ever take place.

4.4 Caveats and future work

Our exploration of the large parameter space was made tractable in large part by adopting the assumption that the early thermal dynamo shut down 500 Myrs after the formation of Mars. Relaxing this assumption would affect our subsequent results related to the timing of the possible onset and cessation of compositionally-driven convection. Nevertheless, any early thermal dynamo would shut down eventually unless the mantle viscosity were very low. And if the mantle viscosity were much lower, the resulting rapid cooling would cause a solid inner core to nucleate early, leading to strong compositionally-driven convection that would continue operating even today, unless the sulfur content were high enough for crystallization to occur in the iron snow regime. Another caveat is that our model involves a number of simplifications including: neglecting the changes in sulfur content of the liquid part of the core over time (though, as we argued in section 2.1, this should be small) and the effect on density and thermal conductivity; ne-

glecting the radial variation in core thermal conductivity and expansivity; and defining the threshold for convection and dynamo action based on the simple sum of the individual buoyancy fluxes in (16). The effects of relaxing these assumptions are not necessarily obvious but will be the subject of future work. The addition of a time-variable Peclet number could also be valuable as a means of accounting for changes over time in the level of volcanic activity.

Finally, we intend to use our model to study the Moon, Mercury, Venus, Io, Ganymede, terrestrial-like exoplanets, and super Earths, as well as alternate internal structures for Mars (e.g., Brennan et al. (2020); Deng and Levander (2020)), to characterize how planet scale and core size (see Boujibar et al. (2020)) interact with the various model parameters we have considered here to determine how and when thermally- and/or compositionally-driven dynamos may operate in general. The Moon is a particularly interesting case because, like Mars, it has no dynamo operating today, but parts of its crust are nevertheless strongly magnetized. The combination of age dating and measurement of the magnetic properties of returned lunar samples has permitted some reconstruction of the Moon's magnetic history (e.g., Garrick-Bethell et al. (2009); Weiss and Tikoo (2014); Tikoo et al. (2017)). This has raised questions about how the Moon could have generated a dynamo field strong enough to magnetize not just the collected samples, but also the even more strongly magnetized larger scale crustal magnetic anomalies (e.g., Hood et al. (2001); Halekas et al. (2010); Hemingway and Tikoo (2018)), and how and when the dynamo shut down. Hence, we are motivated to apply our model to the Moon and show how it relates to the results we have discussed here. The case of Mars has been an appropriate starting point, however, as it may be a boundary case for which there is an especially wide range of possibilities. For example, in larger bodies, the much higher core pressures make bottom-up core crystallization more likely whereas the much lower pressures in smaller bodies like Ganymede and Mercury mean that top-down core crystallization is more likely. Our model for driving convection via remelting of the falling iron snow showed that the details determining whether or not, and where, the crystals can remelt are clearly important and worthy of more detailed study. Although we showed that this mechanism may not be efficient for Mars due to the similarity in slopes of the core adiabat and the melting curve, the same mechanism could be more efficient at Ganymede and Mercury, where the much lower core pressures permit much higher thermal expansivity and therefore a much steeper adiabat (see eq. 6). In any case, a comprehensive exploration of the parameter space spanned by this wider range of bodies could further illuminate the range of possibilities for terrestrial-like planet dynamo histories and the factors that control them.

5 Conclusions

Our analysis has demonstrated that there is a range of possibilities for the history and future of the Martian dynamo. Consistent with previous work, we have shown that a large initial core-mantle temperature difference can help to ensure that thermal convection is able to power a dynamo at early times, and that, given an appropriate combination of mantle viscosity and core thermal conductivity, thermal stratification can be made to shut down this early thermal dynamo ~ 500 Myrs after the formation of Mars. We have additionally shown that the presence of a solid inner core inside Mars' otherwise liquid core is compatible with the lack of an active dynamo at present and that its presence could imply that either: (A) a compositionally-driven dynamo will become active at some point in the next ~ 1 Gyrs or, (B) if the light element partitioning is large enough, such a dynamo may have been active for a limited period in the past. We have argued that, if the light elements partition strongly into the liquid phase, it may be difficult to drive convection in the top-down crystallization (iron snow) regime because the falling snow crystals may not warm enough to remelt. Our analysis has clarified the effects of, and illustrated the importance of obtaining better constraints on, many of the

most important parameters, including: core composition (i.e., sulfur content), light element partitioning, mantle viscosity, core thermal conductivity, and core thermal expansivity. Future experimental and modeling efforts to better constrain these parameters could help to more definitively determine which Martian dynamo scenarios are most likely. More generally, expanding our analysis to include a wider array of bodies, ranging from the Moon to super Earths, could help to further clarify the conditions that determine which types of dynamos may operate on which types of bodies, and when.

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