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Wavelet methods for the analysis of GPS recordings of slow earthquakes

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Slow slip events

- Duration: Several days to several years.
- Generate much weaker seismic waves than ordinary earthquakes.
- Observed in many subduction zones, such as Cascadia, Nankai, Alaska, Costa Rica, Mexico, and New Zealand (Beroza and Ide, 2011 [3]; Audet and Kim, 2016 [2]).

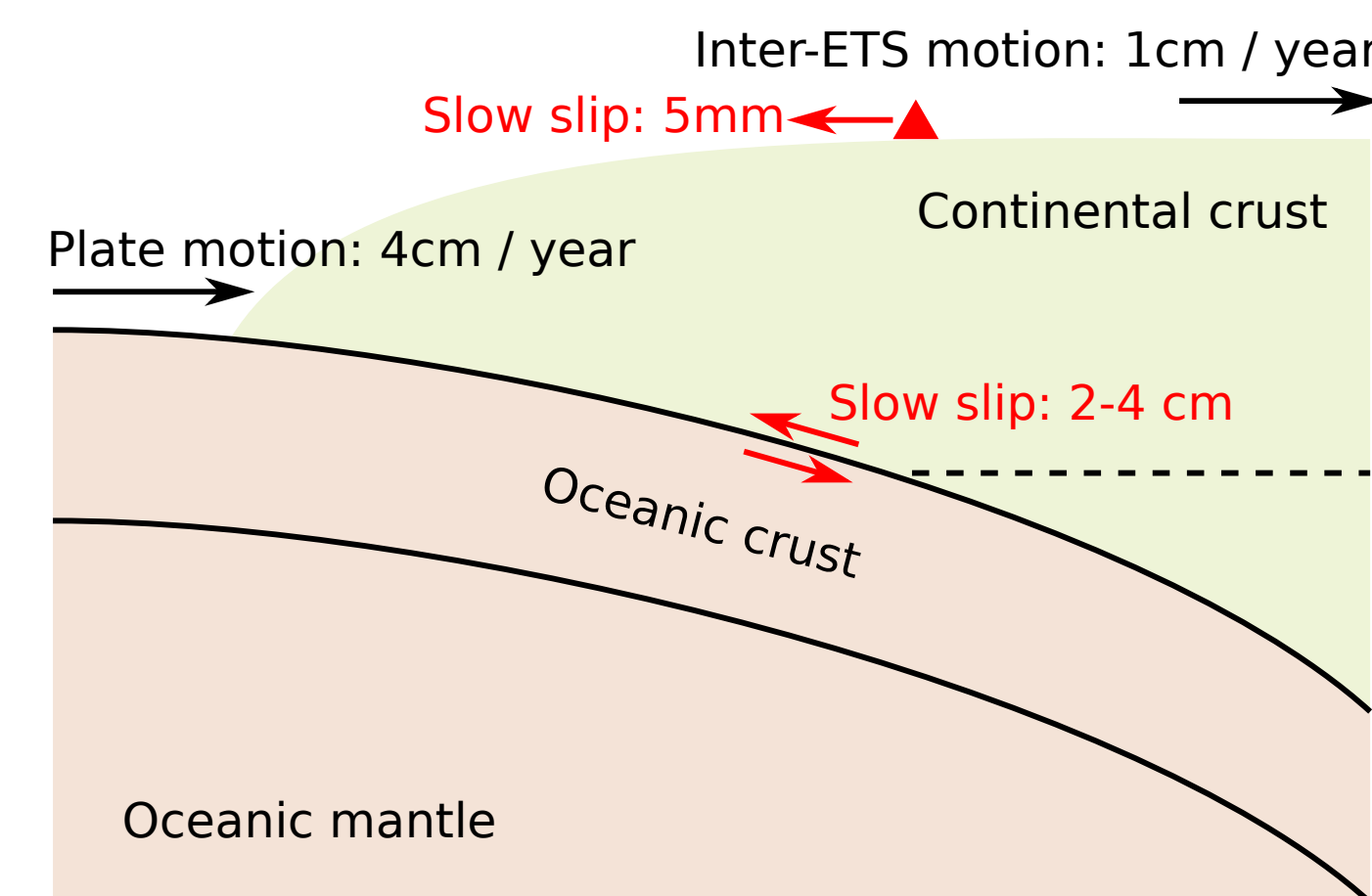


Figure 1: Slow slip event in northern Cascadia.

Wavelet decomposition

Maximal Overlap Discrete Wavelet Transform (MODWT):

X_t (length N) $\rightarrow J$ wavelet vectors W_j ($j = 1, \dots, J$) of length $N \rightarrow J$ details D_j ($j = 1, \dots, J$) of length N and one smooth S_J of length N .
 J = Level of the wavelet decomposition (Percival and Walden, 2000 [6]).
Detail D_j associated with changes on scale $\tau_j = dt2^{j-1}$, smooth S_J associated with averages in scale $\lambda_J = dt2^J$.

Multiresolution analysis (MRA): $X = \sum_{j=1}^J D_j + S_J$.

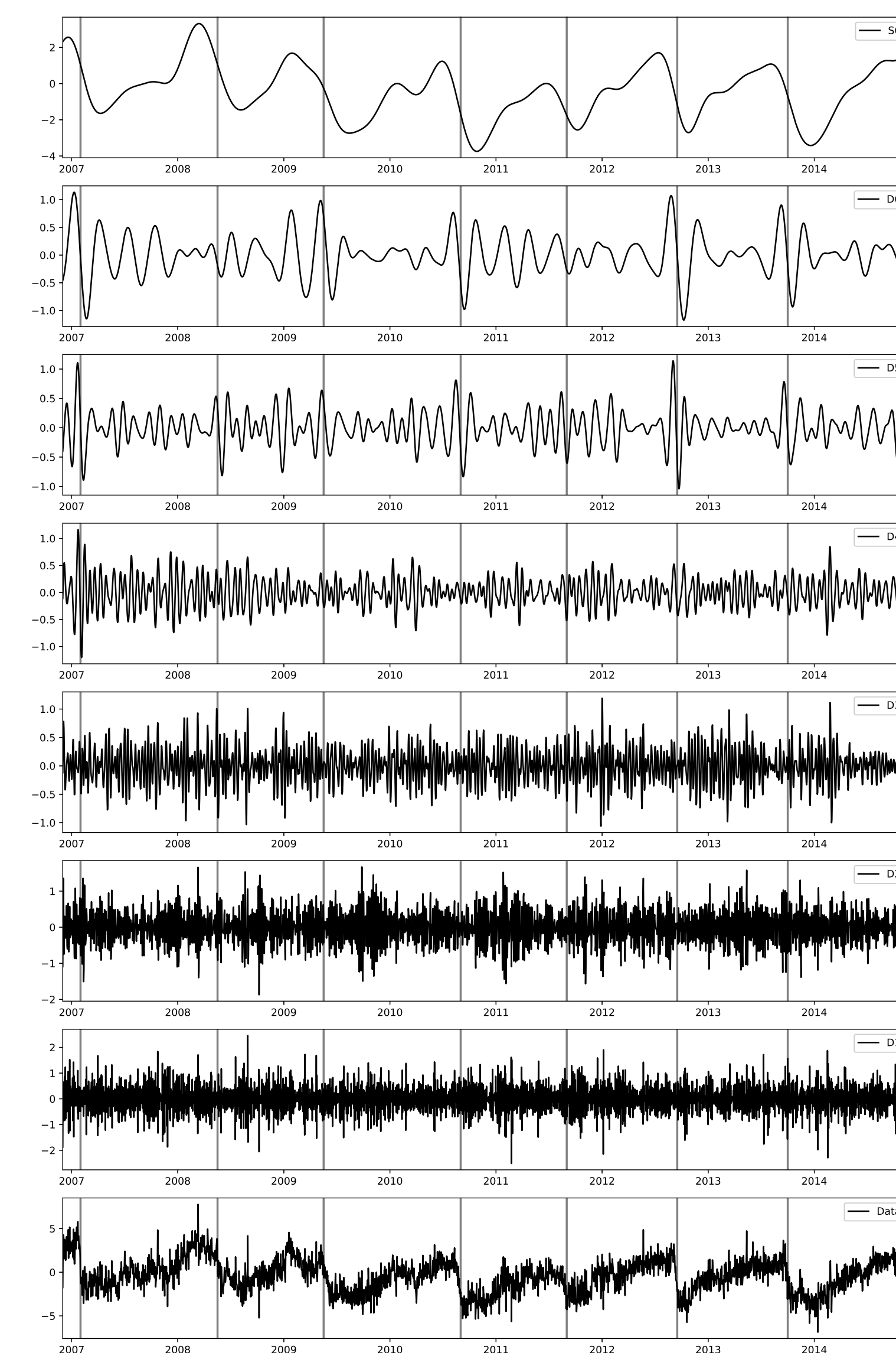


Figure 2: Example of wavelet decomposition. The bottom panel is the longitudinal component of the displacement recorded at GPS station PGC5, located on southern Vancouver Island, Canada. The data has been linearly detrended, and steps due to earthquakes or hardware upgrades, and annual and semi-annual sinusoids signals simultaneously have been estimated and removed following Szeliga *et al.* (2004 [8]). The middle six panels show the details of the decomposition at level 1 to 6 (corresponding to a time scale of 2, 4, 8, 16, 32, and 64 days). The top panel shows the 6th level smooth. Peaks corresponding to the August 2010, September 2012 and September 2013 Episodic Tremor and Slip (ETS) events can clearly be seen in both the 5th and the 6th level details.

Application: Denoising of GPS time series

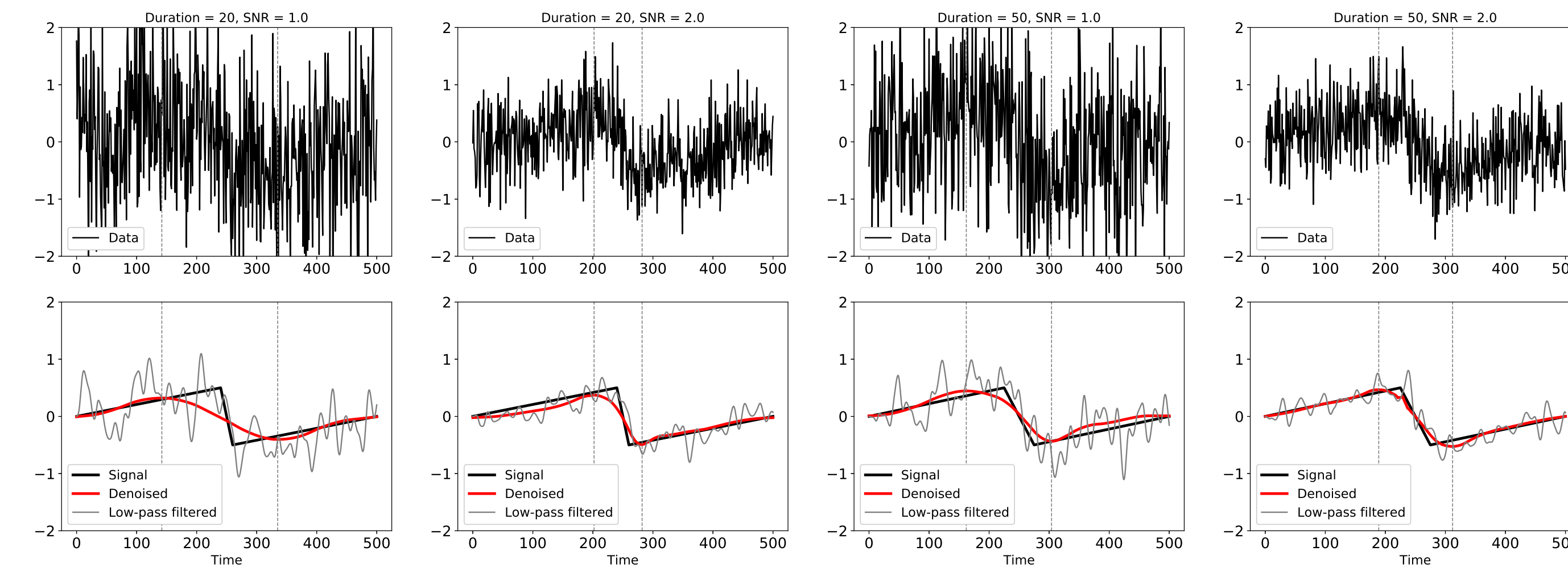


Figure 3: Denoising of synthetic time series using wavelets for two durations of the slow slip and two signal-to-noise ratios. The black line on the bottom panels is the signal. The black line on the top panels is the signal to which a Gaussian noise has been added. The red line on the bottom panels is the denoised signal obtained using thresholding of the wavelet vectors. The two vertical dashed lines show the time of the maxima and minima of the denoised signal. The grey line on the bottom panels is the signal obtained with a low-pass filter.

- **Application of MODWT:** Estimation of a signal hidden by noise within an observed time series.

- Main idea:
 - Compute wavelet coefficients W_j .
 - Thresholding, scaling, or shrinkage of the W_j \rightarrow New wavelet coefficients W_0 (Percival and Walden, 2000 [6]).
 - Inverse wavelet transform of $W_0 \rightarrow$ Denoised signal.

- Example with synthetics (top figure).

- Example with GPS data (bottom figure).

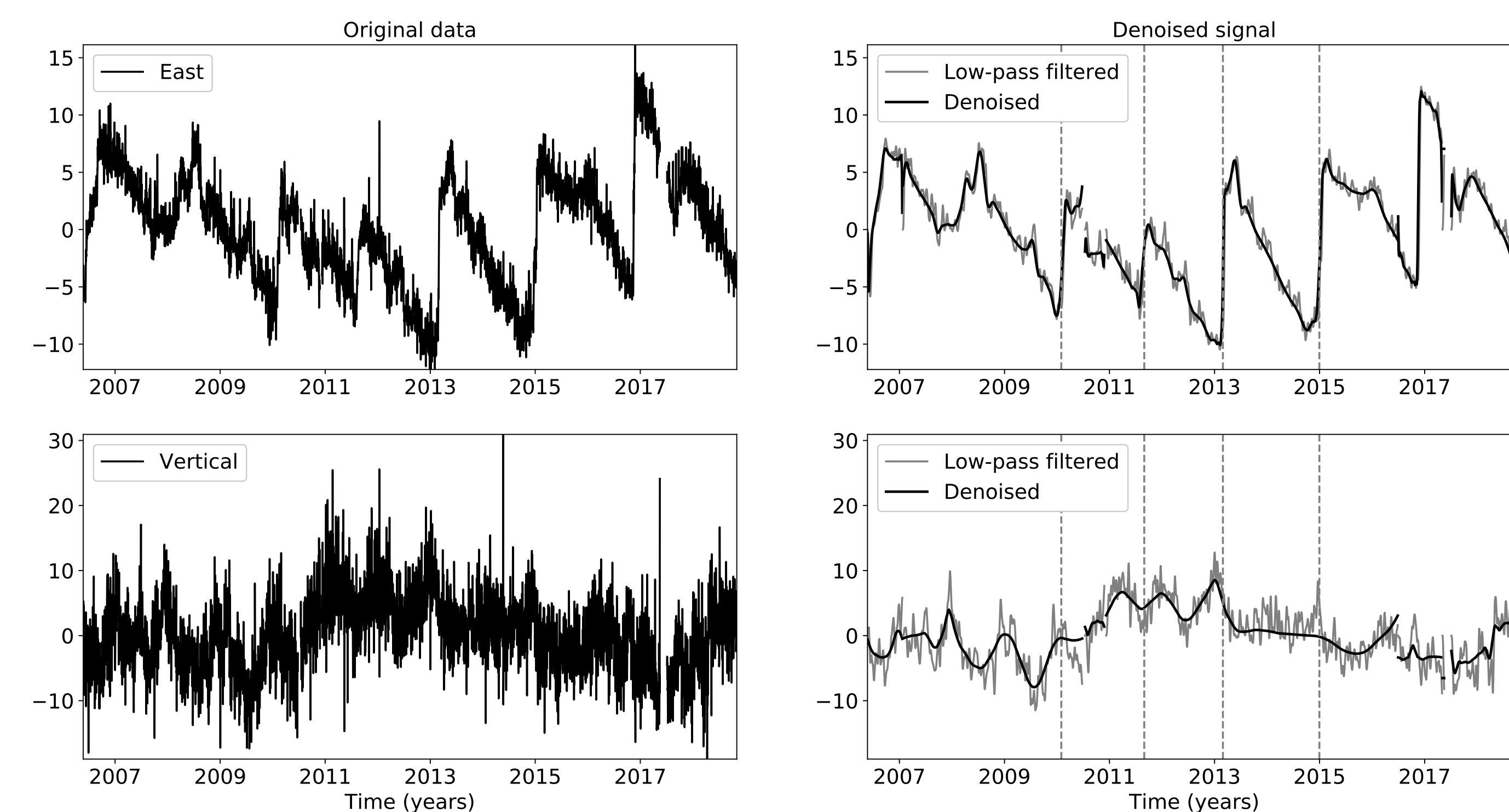


Figure 5: Original (left) and denoised (right) displacement observed at GPS station CKID for the eastern (top) and vertical (bottom) components. The black line on the right panels is the denoised signal obtained using thresholding of the wavelet vectors. The grey line on the right panels is the signal obtained with a low-pass filter. The vertical dashed lines indicate the timing of the slow slip events identified by Todd and Schwartz (2016 [10]).

Application: Detection of small slow slip events

- **Application of MODWT:** Detection of small slow slip events.

- Main idea:
 - Compute details D_j for 10 GPS stations.
 - Apply a time shift $t = s * \text{latitude}$ for different values of the slowness s .
 - Stack over the 10 GPS stations.
 - Plot amplitude of detail in function of time and slowness.

- Stacked 4th level detail.

- Sum of the stacked 4th, 5th and 6th level details.

- Tremor recorded in the vicinity of GPS stations.

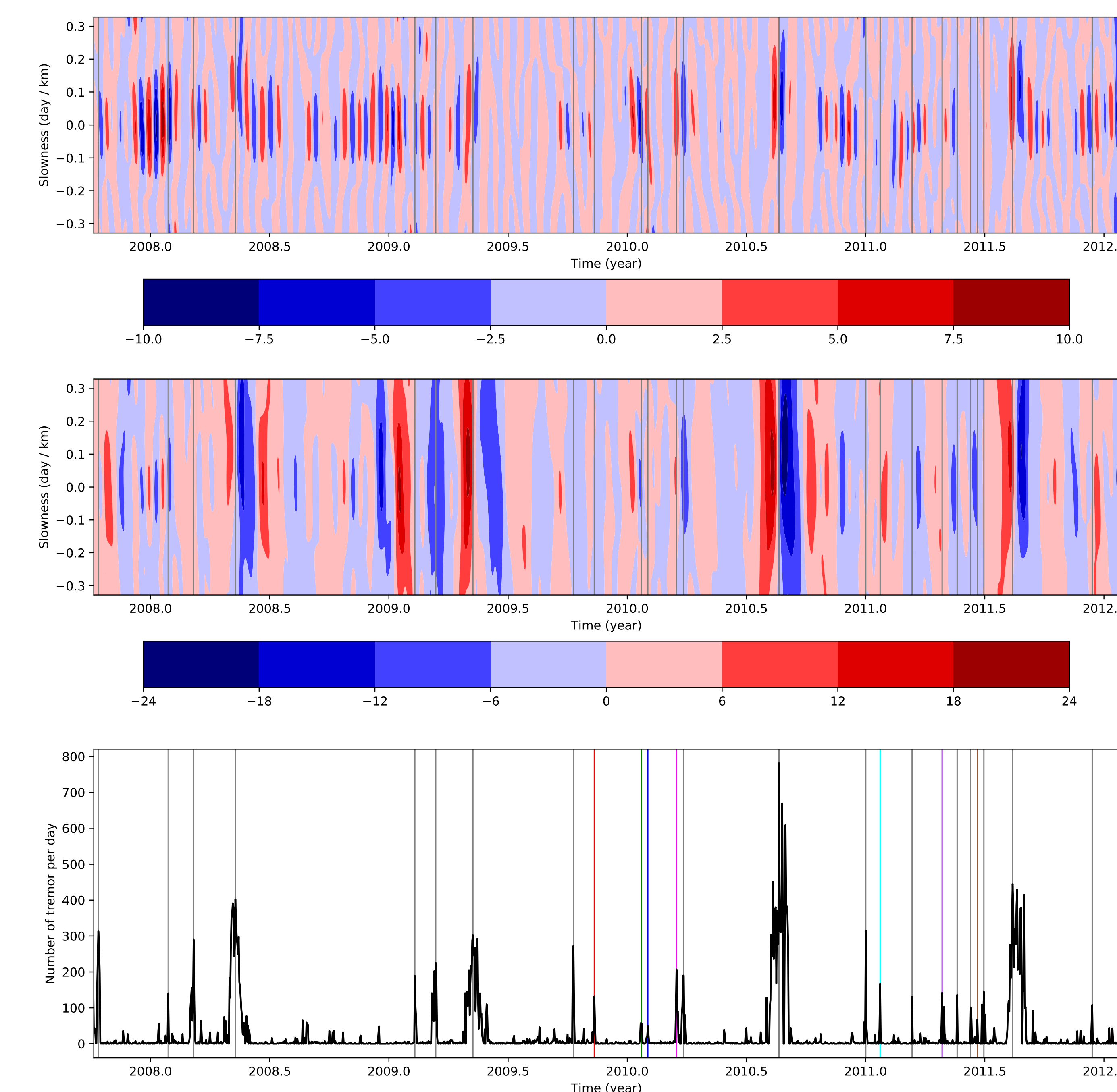


Figure 7: Stacking of the 4th level detail (top) and sum of the stacking of the 4th, 5th, and 6th level details (middle) of the wavelet decomposition of the longitudinal component of the displacement recorded at 10 GPS stations. A time shift corresponding to different values of the slowness of the propagation of the slow slip is applied before the stacking. The bottom panel represents the number of tremor recorded per day in the vicinity of the GPS stations. The colored vertical bars show the timing of the tremor from Figure 6. We can see an increase in amplitude of the 4th level detail corresponding to the tremor episodes recorded in January 21-23 2010, February 1-3 2010, and March 16-21 2010.

Summary

- Slow slip events can last from a few days to several years, and have a relatively short recurrence time (months to years), compared to the recurrence time of regular earthquakes.
- Wavelets methods are mathematical tools for analyzing time series simultaneously in the time and the frequency domain by observing how weighted averages of a time series vary from one averaging period to the next.
- Aim of the project: Use wavelet methods to analyze GPS recordings of slow slip events in New Zealand.
- Detect possible smaller (magnitude 5) slow slip events:
 - Nankai and Cascadia: Tectonic tremor observations spatially and temporally correlated with slow slip observations \rightarrow Episodic Tremor and Slip (Obara, 2002 [5]; Rogers and Dragert, 2003 [7]).
 - Tremor can be used as a proxy to study slow slip events (Aguar *et al.*, 2009 [1]; Frank, 2016 [4]).
 - What can we do when there is no spatial / temporal correlation between tremor and slow slip?
- Determine the vertical displacement of the ground surface during a slow slip event:
 - Vertical component most useful in constraining the up-dip and down-dip extent of slip (Szeliga *et al.*, 2008 [9]).
 - Smaller than the horizontal displacement, and generally hard to resolve.

References

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Acknowledgements

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A.D. would like to thank Pr Donald Percival for introducing her to wavelet methods during his excellent class taught at University of Washington. This work was funded by the grant from the National Science Foundation EAR-1358512.