

1                   **On the semiannual formation of large scale**  
2                   **three-dimensional vortices at the stratopause**

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6                   **Key Points:**

- 7                   • EOF analysis of the second matrix invariant of the velocity gradient tensor is ap-  
8                   plied to the shear zones about the tropical stratosphere.
- 9                   • We identify large scale vortices near the tropical stratopause as reconstructed in  
10                  the NASA MERRA-2 atmospheric reanalysis.
- 11                  • The vortices form following the vernal and autumnal equinoxes at times when the  
12                  westerly jet is maximal.

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## Abstract

An examination of the dynamics of the middle atmosphere as reconstructed in the NASA Modern-Era Retrospective analysis for Research and Applications, Version 2 (MERRA-2) reveals the formation of large scale three dimensional vortices in the tropical stratosphere following both the vernal and autumnal equinoxes at times when the jet associated with the westerly phase of the semiannual oscillation (SAO) is maximal and extratropical influences from planetary waves are weakest. An empirical orthogonal function (EOF) analysis of the second matrix invariant of the velocity gradient tensor applied to the shear zones about the SAO reveals statistically stationary wave-5 vortex structures that span more than 3200km in length and up to 40km in the vertical. Eliassen-Palm fluxes suggests the vortices are maintained by a combination of local (shear zones) and remote (vertically propagating tropical) sources of momentum. These large scale coherent features appear to be unique to the stratopause.

## Plain Language Summary

Application of methods commonly employed in engineering fluid mechanics to visualise vortices are used to examine a recent state of the art reconstruction of the middle atmosphere. This analysis reveals huge vortical structures present during the equinoctial seasons in the region of the tropical stratopause. These semiannual coherent features appear to be unique to the middle atmosphere spanning up to 30° longitude at  $\pm 15^\circ$  latitude corresponding to around 3200km in length and between 10 hPa and 0.1 hPa encompassing up to 40km in the vertical.

## 1 Introduction

The tropical middle atmosphere semiannual oscillation (SAO), observed in temperature and the zonal wind variations, was first discovered in radiosonde and rocketsonde measurements in the early 1960's (R. J. Reed, 1962). The SAO is evident from the upper levels of the stratosphere (stratopause) and throughout the mesosphere with very clear phase-locking to the annual cycle. The SAO dominates the variability about the stratopause ( $\approx 1$  hPa) where easterly extreme wind speeds are typically reached following the December and June solstices and the westerly extreme winds after the equinoxes around April and October (Müller et al., 1997). The mean annual evolution of the stratopause SAO has been characterised using 20 years of rocketsonde observations at Ascension Is-

44 land ( $8^{\circ}\text{S}$ ,  $14^{\circ}\text{W}$ ) and Kwajalein ( $8^{\circ}\text{N}$ ,  $167^{\circ}\text{E}$ ) as a Hovmöller time-height diagram of  
45 the zonal wind between  $20\text{km}$  and  $60\text{km}$  in which the westerlies form in the lower meso-  
46 sphere shortly after the solstices propagating downward with an average speed of  $6\text{--}7\text{km}$   
47  $\text{month}^{-1}$  and reaching maximum average values in excess of  $25\text{ms}^{-1}$  ( $20\text{ms}^{-1}$ ) after the  
48 equinoxes in April (October) (Baldwin et al., 2001; Smith et al., 2017, 2020; Kawatani  
49 et al., 2020). The observed downward progression of the westerly acceleration phase of  
50 the SAO suggests a strong role for westerly Kelvin waves as being the source of the req-  
51 uisite momentum flux (R. Reed, 1965), and supported on theoretical grounds in terms  
52 of the interaction of a vertically-propagating Kelvin wave with the mean background flow  
53 (Dunkerton, 1979).

54 Hopkins (1975) first suggested a close coupling between the easterly phase of the  
55 SAO and planetary wave activity in the winter hemisphere arguing that, consistent with  
56 the theoretical work of Dickinson (1968), the stationary planetary waves of the winter  
57 hemisphere stratosphere would be absorbed about the critical line i.e., where the mean  
58 zonal wind is  $0\text{ms}^{-1}$ , near the equator producing an easterly zonal acceleration with lit-  
59 tle tendency for downward propagation. Hopkins (1975) further suggested that the stronger  
60 planetary wave activity in the Northern Hemisphere winter was the cause for the stronger  
61 variance in the monthly mean easterly tropical zonal winds after the January solstice ( $\approx$   
62  $40\text{ms}^{-1}$ ) in contrast to the June solstice ( $\approx 20\text{ms}^{-1}$ ). On the basis of the Hopkins (1975)  
63 study, Holton (1975) proposed that the SAO results from the combined effects of a steady  
64 background source of westerly momentum due to Kelvin waves excited in the tropical  
65 troposphere as the cause of the westerly phase of the SAO where its downward propa-  
66 gation is indicative of dissipation of vertically propagating waves near critical layers. Us-  
67 ing a two-dimensional atmospheric model for zonal mean temperature, winds and chem-  
68 ical constituent mixing ratios developed by Harwood and Pyle (1975), Gray and Pyle  
69 (1986) examined the additional westerly momentum required to successfully simulate the  
70 SAO double peak observed in low latitude satellite tracer distributions ( $\text{N}_2\text{O}$  and  $\text{CH}_4$ ).  
71 In contrast, the easterly phase was hypothesised to arise from the annual cycle of east-  
72 erly momentum due to vertically and equatorward propagating planetary waves of the  
73 winter hemisphere stratosphere being absorbed near the critical line in the tropics. As  
74 such, the stratospheric easterly phase arises due to mean advection of easterly momen-  
75 tum by the seasonally dependent meridional circulation, thus setting the semiannual pe-  
76 riod of the SAO.

77 Subsequent observational studies added further weight to the mechanism proposed  
78 by Holton (1975), showing that the transition from westerlies to easterlies occurs rather  
79 suddenly throughout a deep layer due to the easterly phase of the SAO being forced by  
80 the dissipation of horizontally traveling planetary waves (Hirota, 1980) and cross-equatorial  
81 advection of easterly winds by the residual mean meridional circulation (R. J. Reed, 1966;  
82 Meyer, 1970; Holton & Wehrbein, 1980; Dickinson, 1968; Meyer, 1970; van Loon et al.,  
83 1972; Belmont et al., 1974a, 1974b; Hopkins, 1975; Müller et al., 1997; Garcia et al., 1997;  
84 Garcia & Sassi, 1999; Hirota, 1978, 1980; Li et al., 2012). Additional observational stud-  
85 ies of temperature and trace constituent data (Hirota, 1978, 1979; Bergman & Salby, 1994),  
86 combined with analysis based on the vertical component of the Eliassen-Palm (E-P) flux  
87 (Andrews et al., 1983), revealed short-period, equatorially trapped Kelvin waves with  
88 periods less than 2 days propagating vertically into the stratosphere are the most likely  
89 sources of the majority of the momentum required to generate both the quasi-biennial  
90 oscillation (QBO) and SAO (see also Sato and Dunkerton (1997)). Bergman and Salby  
91 (1994) used high resolution imagery of the global convective pattern to show that these  
92 short period waves are generated in geographical locations over the Indian Ocean to the  
93 western tropical Pacific and to a lesser extent over the African, and American continents.  
94 Theoretical and modeling studies, such as the one by Dunkerton (1979), showed that a  
95 Kelvin wave with sufficiently fast phase speed could propagate through the stratosphere  
96 with only modest attenuation and then be strongly absorbed in the region of very fast  
97 radiative damping near the stratopause.

98 Sassi and Garcia (1997) used spatial and temporal distributions of equatorial heat-  
99 ing based on Bergman and Salby (1994) to successfully model a realistic SAO in the mid-  
100 dle atmosphere. More generally, the stratopause SAO has been successfully simulated  
101 in a number of GCMs (Hamilton & Mahlman, 1988; Sassi et al., 1993; Jackson & Gray,  
102 1994; Müller et al., 1997; Zülicke & Becker, 2017). This has allowed the mechanisms in-  
103 volved in driving the SAO to be examined in detail (at least within the context of the  
104 GCMs). That said, there is much to understand regarding the dynamics of the SAO and  
105 in particular the respective roles of planetary and gravity waves (Hamilton, 1998). Smith  
106 (2012) reviews the literature on the SAO in the broader context of the dynamics of the  
107 middle atmosphere - lower thermosphere (MLT) and in particular the variability and changes  
108 in direction of the zonal winds due to interactions with gravity waves. They make the  
109 point that, above 50km the details of the mean meridional circulation are difficult to mea-

110 sure (Smith et al., 2017) and that numerical models must be relied upon for the large  
111 scale wave driven motions of the middle atmosphere. Coherent temperature or "pancake"  
112 anomalies have been identified in the lower equatorial mesosphere (Hitchman et al., 1987)  
113 resulting from inertial instabilities (Harvey & Knox, 2019) and strong forcing of the sub-  
114 tropical mesosphere by large scale Rossby waves. For a recent detailed analysis of the  
115 momentum budget in the stratosphere, mesosphere, and lower thermosphere see the re-  
116 cent studies undertaken by Sato et al. (2018) and Yasui et al. (2018).

117 In the absence of direct observations of winds between 10 hPa (35km) and 0.01 hPa  
118 (80km), Smith et al. (2017) derived monthly zonally averaged tropical zonal winds in the  
119 middle atmosphere using the balance wind relationship from satellite geopotential height  
120 retrievals. They found easterly maxima near the solstices at 1.0 hPa, westerly maxima  
121 near the equinoxes at 0.1 hPa and easterly maxima near the equinoxes 0.01 hPa with  
122 the maxima significantly stronger during the first cycle, and importantly for this study,  
123 strongest near March at 0.1 and 0.01 hPa. While global climate model simulations of  
124 the zonal mean zonal winds near the stratopause generally reproduce the observed am-  
125 plitudes and phases of the SAO there is some tendency for the models to be more west-  
126 ward than observations might indicate (Smith et al., 2020). Recent intercomparisons of  
127 reanalyses temperatures and winds through the SPARC reanalysis intercomparison project  
128 (S-RIP) (Long et al., 2017) reveal reasonable agreement amongst the more recent reanal-  
129 yses (CFSR, MERRA, MERRA-2, JRA-55 and ERA-Interim) and for the zonal winds  
130 in the upper stratosphere. A detailed comparison of the zonal winds and temperature  
131 in the equatorial stratosphere and lower mesosphere in a number of reanalysed products  
132 to recent satellite SABER and MLS observations has been published by Kawatani et al.  
133 (2020). They find some significant differences in the variation and displacement of the  
134 equatorial zonal wind SAO amplitude maximum between the various reanalyses for heights  
135 above 1 hPa.

136 The structure of descending alternating easterly and westerly jets comprising the  
137 SAO and their associated shear zones suggests the possibility that large scale coherent  
138 structures might at times be present when the shear zones between the vertical easterly  
139 - westerly - easterly jet structure are sufficiently strong that vortical filaments are man-  
140 ifest within the confines of the westerly jet which acts as a waveguide. The main meth-  
141 ods for the identification of three dimensional vortices are based on pointwise analysis  
142 of the velocity gradient tensor (Chakraborty et al., 2005). The characteristic shapes of

143 vortical structures in turbulent flows, including regions of vorticity in the form of fila-  
144 ments, sheets, and blobs are a question of long-standing and intense interest. Vortex  
145 filaments are known to play an important role in the overall turbulence dynamics where  
146 local or point-wise methods of vortex identification typically are used to define a func-  
147 tion that can be evaluated point-by-point and then classify each point as being inside  
148 or outside a vortex according to a criterion based on the point values (Hunt et al., 1988;  
149 Chong et al., 1990; Soria et al., 1994; Kitsios et al., 2011). Most local vortex identifica-  
150 tion criteria are based on the kinematics implied by the velocity gradient tensor, thereby  
151 making them Galilean invariant i.e. invariant to uniform rotations and translations. One  
152 of the most popularly used local criteria is the second matrix invariant of the velocity  
153 gradient tensor  $Q$  (Hunt et al., 1988). In order to isolate regions that might contain co-  
154 herent vortical structures, we first calculate the velocity gradient tensor from the MERRA-  
155 2 reanalysis (Gelaro & Co-authors, 2017), then, following Soria et al. (1994), we calcu-  
156 late  $Q$  between 100 hPa and 0.01 hPa. Empirical orthogonal function (EOF) analysis  
157 is then applied to isolate regions of high  $Q$  variance and the corresponding vortical (pos-  
158 itive  $Q$ ) isosurface structures.

159 This paper is structured as follows. The MERRA-2 reanalysis is briefly described  
160 in section 2. We next characterise the SAO as represented in MERRA-2 in section 3 fol-  
161 lowed by the calculation of the velocity gradient tensor and the second invariant  $Q$  (sec-  
162 tion 4.1), and the EOFs of  $Q$  (section 4.2) and a case study of the observed vortical struc-  
163 tures evident on April 1984 (section 4.3). A final summary is presented in section 5.

## 164 **2 Data**

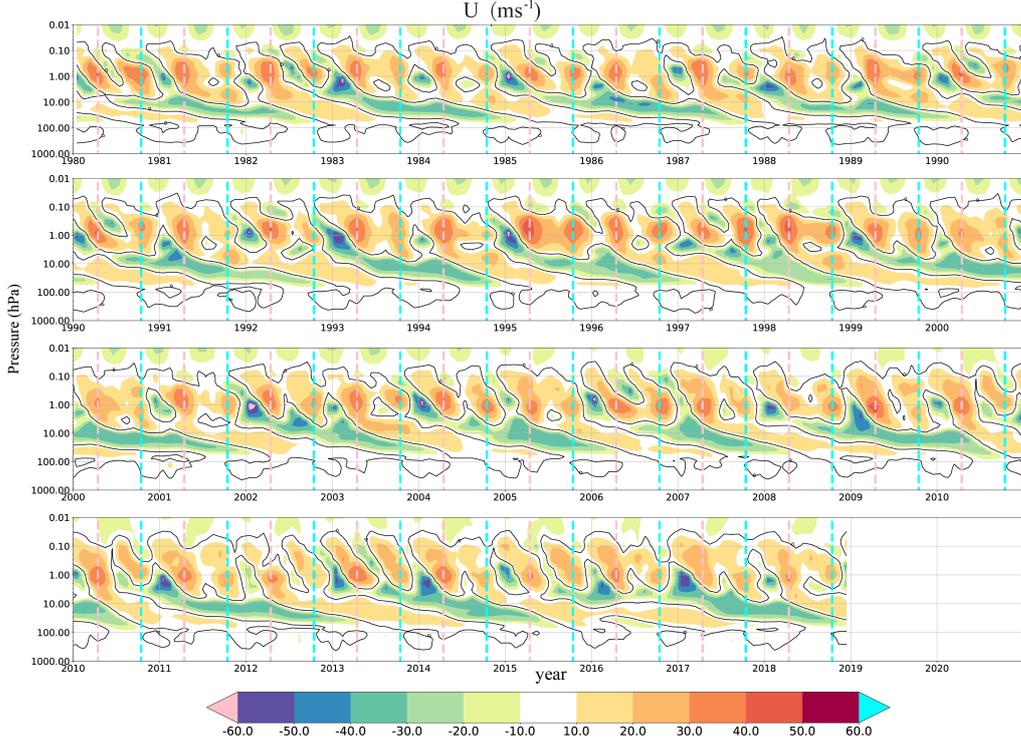
165 We analyse the middle atmosphere using MERRA-2 data. MERRA-2 is an atmo-  
166 spheric reanalysis of the modern satellite era produced by the NASA Global Modeling  
167 and Assimilation Office (GMAO) (Gelaro & Co-authors, 2017). The processed daily and  
168 monthly averages used in this study are based on 3-hourly time averaged three-dimensional  
169 collections consisting of 361 latitudes, 576 longitudes and 72 levels. The height - pres-  
170 sure relationship to model level is displayed in (supplemental Figure 1). All analyses are  
171 performed on the full horizontal grid with calculations of the vortex structures restricted  
172 to the 38 levels above 100 hPa. MERRA-2 provides a multidecadal reanalysis whereby  
173 aerosol and meteorological (satellite radiances, microwave temperature, ATOVs etc) ob-  
174 servations are jointly assimilated within a global data assimilation system. In addition

175 to improved representations of cryospheric processes, MERRA-2 also includes several im-  
176 provements to the representation of the stratosphere including ozone (total column, pro-  
177 files from EOS Aura OMI). Importantly for the middle atmosphere, the gravity wave pa-  
178 rameterization has been retuned to produce a model generated QBO rather than rely-  
179 ing on one imposed through reanalysis tendencies to the wind and temperature fields.  
180 For a complete list of observations assimilated see table 1 of Gelaro and Co-authors (2017).  
181 Of relevance to our study, in the stratosphere at 10 hPa MERRA-2 has a negative bias  
182 of 20.3 Kelvin ( $K^\circ$ ) prior to the assimilation of AIRS radiances in 2002. These biases trend  
183 upward becoming positive in 2005. After 2005, assimilation of both MLS temperature  
184 retrievals (above 5 hPa) and GPSRO bending angle observations (up to approximately  
185 10 hPa) begins in MERRA-2 such that after 2006, the biases have an average value of  
186 0.2-0.3 K. Importantly for this study MERRA-2, resolves most of the middle atmosphere  
187 up to just below the mesopause at 0.01 hPa.

188 The detailed comparison of the representation of the equatorial stratopause SAO  
189 in the major reanalysis products that resolve the stratosphere to SABER and MLS ob-  
190 servations by Kawatani et al. (2020) reveals MERRA and MERRA-2 to have very re-  
191 alistic zonal mean zonal wind amplitude and phase variations (their Figure 1) and cli-  
192 matological annual cycle for the zonal wind at around 1 hPa over the equator (their Fig-  
193 ure 9) relative to other available reanalysis products which uniformly exhibit much weaker  
194 westerly equinoctal winds. It is on this basis we choose MERRA-2 as a valid represen-  
195 tative data set for stratopause zonal wind variations. We will not discuss MERRA-2 fur-  
196 ther simply referring the reader to the relevant citation (Gelaro & Co-authors, 2017).  
197 MERRA-2 products are accessible online through the NASA Goddard Earth Sciences  
198 Data Information Services Center (GES DISC).

### 199 **3 Characterising the semiannual oscillation in MERRA-2**

200 In the following we summarise the general mechanism of the SAO easterly and west-  
201 erly phases, as present in MERRA-2, in terms of the propagation of zonal winds over time  
202 and via the transfer of momentum. Figure 1 shows monthly averages of the U zonal winds  
203 averaged between  $0^\circ$ - $360^\circ$  longitude and  $5^\circ$ N- $5^\circ$ S latitude. The black contour shows zero  
204 average of winds. April and October are indicated by the pink and cyan vertical lines  
205 respectively. The downward propagation of the alternating easterly and westerly jets is  
206 evident as are their relative strengths.



**Figure 1.** Monthly averages of the U zonal winds averaged between  $0^{\circ}$ - $360^{\circ}$  longitude and  $5^{\circ}\text{N}$ - $5^{\circ}\text{S}$  latitude. Black contour shows the critical line. April and October are indicated by the pink and cyan vertical lines respectively.

207 Eliassen-Palm (E-P) fluxes are calculated to examine the transfer of momentum  
 208 from sources in the extratropics via the winter hemisphere and also tropical sources due  
 209 to Kelvin and inertial gravity waves. The E-P flux provides a useful tool to describe wave  
 210 propagation in mean zonal shear flows (Andrews et al., 1983). The E-P flux is defined  
 211 as

$$212 \quad \mathbf{F} = \{F_{\phi}, F_p\} = \left\{ -a \cos \phi \overline{U'V'}, fa \cos \phi \frac{\overline{V'\theta'}}{\theta_p} \right\} \quad (1)$$

213 where  $a$  is the Earth's radius,  $f$  is the Coriolis force,  $\phi$  is the latitude,  $\theta$  the potential  
 214 temperature, the zonal and meridional velocities ( $U, V$ ). Eddy flux terms are computed  
 215 from the daily zonal anomalies and the product is zonally and then time averaged over  
 216 the period 1980-2018.  $\theta_p = \frac{\partial \theta}{\partial p}$  is calculated as the time-mean, zonal mean value of  $\theta$ .  
 217 When the E-P flux vector points upward, the meridional heat flux dominates; when the  
 218 vector points in the meridional direction, the meridional flux of zonal momentum dom-  
 219 inates. The divergence of the E-P flux is proportional to the eddy potential vorticity flux  
 220 and when zero i.e.  $\nabla \cdot \mathbf{F} = 0$ , thermal wind balance is maintained (Edmon et al., 1980).

221 Climatological E-P fluxes were calculated using daily U, V and  $\theta$  data over the pe-  
222 riod 1980-2018 . In Figure 2 shading is the flux divergence with negative values (red) in-  
223 dicated absorption and positive (blue) shading indicative of the production of momen-  
224 tum. See supplementary Figure 2 for all other months. Black contours are the climato-  
225 logical winds whereas the critical line corresponds to the magenta contour line. Follow-  
226 ing Coy et al. (2017), all quantities (E-P fluxes and U zonal winds) have been divided  
227 (normalised) by the associated 1980-2018 standard deviation at each latitude and level.  
228 This has the two-fold benefit of 1) not requiring the usual adhoc scaling of quantities in  
229 the vertical, for example due to the magnitude differences of E-P flux vector components  
230 (Taguchi & Hartmann, 2006) and 2) highlighting exceptional values e.g. individual months  
231 or years as discussed in the following sections. In addition, the vectors below 100 hPa have  
232 been appropriately thinned for display purposes.

233 For the solstices, the mean temperature gradient between the summer and winter  
234 poles is a maximum at the stratopause resulting in a single thermal cell characterised  
235 by rising (sinking) motion in the summer (winter) hemisphere, a compensating flow from  
236 the summer to winter hemisphere, where a strong zonal asymmetry arises due to the in-  
237 jection of momentum from the winter hemisphere. Thus for the solstices momentum flux  
238 into the equatorial stratopause is not balanced by equal contributions from both hemi-  
239 spheres required to drive the equatorial westerly jet which is necessary to generate the  
240 required shear and to act as a waveguide for the formation of coherent vortex structures.  
241 Hence the easterly phase of the SAO is structurally unable to support the existence of  
242 large scale coherent vortices.

243 For the easterly SAO phase, the Hovemoller plot of the MERRA-2 zonal winds  $U$   
244 in the middle atmosphere reveals the relative strengths of the easterly SAO maxima fol-  
245 lowing the respective solstices (Figure 1). Specifically, the maximum zonal winds are in  
246 excess of  $30ms^{-1}$  and occur in January and August at  $\approx 1$  hPa following the Decem-  
247 ber and June solstices. In January, the easterly jet is at a maximum then decays over  
248 the first half of the year before re-establishing with typically significantly weaker max-  
249 imum values after the June solstice. Climatological E-P flux vectors during the solstices  
250 (see December and June climatologies in supplemental Figure 2) reveal extratropical plan-  
251 etary waves propagating into the tropics from the winter hemisphere whereas E-P flux  
252 divergences show deposition of (easterly) momentum due to the dissipation of the afore-  
253 mentioned planetary waves driving wave forcing and mean advection. This is consistent

254 with the general mechanism for the easterly phase of the SAO first proposed by Holton  
255 (1975). As the SAO easterly phase relies on planetary wave forcing and mean momen-  
256 tum advection, it is strongly coupled to the annual cycle and specifically to the winter  
257 hemisphere.

258 Due to the seasonal reversal of the mean zonal and meridional winds the equinoc-  
259 tal and solstitial seasons differ substantially. Specifically, the radiatively driven mean merid-  
260 ional circulation in the equinoctial season is characterised by upward motion at the equa-  
261 tor and corresponding subsidence near the poles with the Coriolis torque generating mean  
262 westerlies in both hemispheres (see Figure 2). The associated momentum flux due to the  
263 observed mean meridional overturning circulation (Figure 2) closely matches that de-  
264 scribed by Gray and Pyle (1986) with a horizontal flux of momentum into the equato-  
265 rial westerly jet at the stratopause ( $\approx 1$  hPa - 50 km). The westerly SAO phase (Fig-  
266 ure 1) is characterised by a pronounced zonal symmetry about the equator and strong  
267 mean westerly jets in excess of  $35\text{ms}^{-1}$ . For the months of April and October immedi-  
268 ately after the equinoxes, the westerly SAO jet, centered near 1 hPa, is maximal with  
269 zonally symmetric momentum fluxes and divergence (Figure 2). The equinoctial E-P flux  
270 vectors are consistent with the induced meridional overturning circulation from satel-  
271 lite observations of tracer distributions described in Figure 3 of Gray and Pyle (1986).  
272 E-P flux divergence indicates westerly momentum sources (positive) where the equato-  
273 rial jet forms acting to maintain and enhance the jet. The E-P fluxes indicate the equa-  
274 torial stratopause regions are the primary source of momentum driving the westerly equa-  
275 torial stratopause jet, with little evidence of systematic inter-hemispheric momentum flux  
276 due to extratropical planetary waves. Tropical sources due to Kelvin and inertial grav-  
277 ity waves are clearly evident during the westerly phase. These sources of momentum are  
278 associated with tropical convection and are thought to be responsible for generating the  
279 westerly phase via interaction of the mean flow with vertically propagating internal grav-  
280 ity waves and large-scale equatorial waves generated in the lower atmosphere. The cli-  
281 matological westerly jet has a generally downward propagation from 0.1 hPa to about  
282 1 hPa and is strongest in April with a secondary maxima in October. Our results are  
283 generally supportive of the hypothesis of Holton (1975) that high frequency Kelvin waves,  
284 with periods from 2 to 4 days, originating in the troposphere propagate unhindered into  
285 the middle atmosphere where they are absorbed about the critical line as the major source  
286 of momentum during the westerly phase.

## 4 Stratopause vortex structures

An examination of the middle atmosphere  $Q$  in all months (not shown) revealed vortical structures are only evident in the stratopause SAO westerly phase and are most coherent after the equinoxes. These structures are highly dependent on the westerly jet being sufficiently strong, requiring velocities in excess of  $35\text{ms}^{-1}$ , and where sufficient shear is present in the gradients at the upper and lower boundaries of the SAO. We shall show that preferential conditions for these vortex structures to occur are where there is a well developed easterly jet present in the vicinity of 0.1 hPa above the westerly SAO jet and when the QBO is strongly easterly.

### 4.1 Calculation of $Q$

Following (Chong et al., 1990; Soria et al., 1994; Chakraborty et al., 2005) we define the velocity gradient tensor  $A_{ij}$  in terms of symmetric  $S_{ij} = S_{ji}$  and anti-symmetric  $W_{ij} = -W_{ji}$  parts where,

$$A_{ij} = \partial U_i / \partial x_j = S_{ij} + W_{ij} \quad (2a)$$

and

$$S_{ij} = (\partial U_i / \partial x_j + \partial U_j / \partial x_i) / 2 \quad (2b)$$

$$W_{ij} = (\partial U_i / \partial x_j - \partial U_j / \partial x_i) / 2 \quad (2c)$$

are the rate of strain and the rate of rotation tensors respectively. The  $U_{i=1,2,3}$  indices are the zonal and meridional velocities ( $U, V$ ) in meters per second ( $\text{ms}^{-1}$ ) and  $\omega$  the Lagrangian rate of change of pressure with time in units of pascals per second ( $\text{Pa s}^{-1}$ ). The  $x_{i=1,2,3}$  indices are latitude and longitude ( $\phi, \lambda$ ) in meters ( $m$ ) and isobaric pressure level  $p$  in Pa respectively. The eigenvalues  $\gamma$  of  $A_{ij}$  satisfy the characteristic equation

$$\gamma^3 + P\gamma^2 + Q\gamma + R = 0, \quad (2d)$$

where the matrix invariants are

$$P = -\text{Tr}[A] = -S_{ii} \quad (2e)$$

$$Q = \frac{1}{2}(P^2 - \text{Tr}[A^2]) = \frac{1}{2}(P^2 - S_{ij}S_{ji} - W_{ij}W_{ji})$$

$$= \begin{vmatrix} \frac{\partial U}{\partial \phi} & \frac{\partial U}{\partial \lambda} \\ \frac{\partial V}{\partial \phi} & \frac{\partial V}{\partial \lambda} \end{vmatrix} + \begin{vmatrix} \frac{\partial U}{\partial \phi} & \frac{\partial U}{\partial p} \\ \frac{\partial \omega}{\partial \phi} & \frac{\partial \omega}{\partial p} \end{vmatrix} + \begin{vmatrix} \frac{\partial V}{\partial \lambda} & \frac{\partial V}{\partial p} \\ \frac{\partial \omega}{\partial \lambda} & \frac{\partial \omega}{\partial p} \end{vmatrix} \quad (2f)$$

316 Tr is the trace,  $Q$  has units of  $s^{-2}$ , and

$$317 \quad R = - \left| A \right| \quad (2g)$$

318 where  $||$  defines the determinant.

319 For turbulence in three dimensional flows, large scale coherent eddies decay as vor-  
 320 ticity diffuses out in convergence zones defined where there is irrotational straining and  
 321 strong divergence and convergence of streamlines. In other words, the magnitude of the  
 322 straining defined by  $S_{ij}S_{ji}$  is large compared to the magnitude of the rate of rotation,  
 323 with regions of elongation  $S_{ij}S_{jk}S_{ki} > 0$  and flattening  $S_{ij}S_{jk}S_{ki} < 0$  (Hunt et al.,  
 324 1988). For incompressible flows, where the first flow invariant  $P = -S_{ii} = 0$ , it fol-  
 325 lows that the second invariant  $Q = (W_{ij}W_{ij} - S_{ij}S_{ij})/2$ . This means that large nega-  
 326 tive values of  $Q$  are indicative of regions where the strain dominates the rotation whereas  
 327 for large positive values rotation dominates strain. In the results presented here, we have  
 328 defined  $Q$  in terms of the zonal and meridional velocities ( $U, V$ ) and  $\omega = \frac{Dp}{Dt}$  the La-  
 329 grangian rate of change of pressure with time, hence for constant model grid pressure  
 330 levels,  $\omega$  depends only on the vertical wind velocity and the change in pressure with height,  
 331 from which it follows that the interpretation of  $Q$  is exactly as for 3D turbulence.

## 332 4.2 EOFs of $Q$

333 In calculating EOFs of  $Q$ , we first construct daily anomalies w.r.t. the climatolog-  
 334 ical month i.e.  $Q'(\phi, \lambda, p, t) = Q(\phi, \lambda, p, t) - \bar{Q}(\phi, \lambda, p)$ . We then construct spatial anoma-  
 335 lies  $Q''$  from the zonal average  $\check{Q}$  as  $Q''(\phi, \lambda, p, t) = Q'(\phi, \lambda, p, t) - \check{Q}(\phi, p, t)$ . These  
 336 anomalies are then normalized by the spatial and temporal standard deviation  $\sigma$  of  $Q''$   
 337 at each pressure level i.e.  $\hat{Q}(\phi, \lambda, p, t) = Q''(\phi, \lambda, p, t)/\sigma(p)$ . In the current study, vor-  
 338 tex structures will be represented by isosurfaces of EOFs of  $Q$ . Normalizing by the spatio-  
 339 temporal standard deviation allows us to then rescale the EOF patterns before calcu-  
 340 lating the iso-surfaces of interest i.e.  $Q_i^{eof}(\phi, \lambda, p) = \hat{Q}_i^{eof}(\phi, \lambda, p) \times \sigma(p)$ .

341 The 3D structures for the leading EOFs 1 & 2 of  $Q$  for April (Figure 3) and Oc-  
 342 tober (Figure 4) reveal a distinct wave-5 pattern with opposite sign about the equator  
 343 due to the change of sign in the meridional velocity gradient. These EOFs are in quadra-  
 344 ture. The corresponding April 2D EOFs at 0.62 hPa i.e., through the middle of the west-  
 345 erly jet, have explained variances of 2.9% and 2.4% respectively. The structures are less  
 346 coherent between 200°E and 300°E which is the region where the westerly jet of the SAO

347 is consistently weak and where the mean zonal wind velocities, are considerably less than  
 348 the maximum mean values as indicated by the  $35\text{ms}^{-1}$  mean U contour line (yellow) in  
 349 the top-down perspectives. As for April, the leading pair of 3D-EOFs of October  $Q$  are  
 350 confined to a region where the background zonal U wind exceeds  $35\text{ms}^{-1}$ . The struc-  
 351 tures would again appear to be close to a hemispheric wave-5 pattern if the westerly jet  
 352 was strong enough to support it.

353 The April 3D-EOFs 3 & 4 (supplemental Figure 3) form a large scale wave-4 pat-  
 354 tern with individual structures in excess of  $40^\circ$  longitude spanning  $20^\circ\text{N}$  to  $20^\circ\text{S}$ . The  
 355 corresponding 2D-EOFs 3 & 4 explain 2.3% & 2.0% of the  $Q$  variance respectively at  
 356 0.62 hPa. All 4 leading 3D-EOFs for April display noticeable asymmetry being larger  
 357 and more coherent south of the equator. October 3D EOFs 3 & 4 (supplemental Fig-  
 358 ure 4) appear to be wave-6 and do not display the North - South asymmetries present  
 359 for April. October 3D-EOFs 3 & 4 are considerably noisier than for April, a reflection  
 360 of the weaker background flow and reduced shear zones.

### 361 **4.3 April 1984 case study**

362 In order to show that the vortical  $Q$  structures are not simply statistical, we now  
 363 focus exclusively on the westerly phase of the SAO associated and the particular month  
 364 of April 1984. This date was chosen as the vortical structures are particularly evident  
 365 with no filtering required, however, a number of other dates could have been chosen. An  
 366 examination of the mean April 1984 E-P fluxes (Figure 5) shows close similarities to the  
 367 climatological April previously discussed. We see absorption of momentum about the  
 368 critical line associated with the easterly QBO phase and some evidence of flux into the  
 369 tropics as the SH transitions to winter. There is evidence of eddy forcing (positive E-  
 370 P flux divergence) in the shear regions between the easterly QBO and the westerly SAO  
 371 ( $\approx 10$  hPa), and between the westerly SAO and the weak easterly jet near 0.1 hPa. Most  
 372 interesting is to consider the anomalous flux w.r.t. the climatological April. Here we see  
 373 an intense highly localized source of momentum in the shear zone i.e. +ve E-P flux di-  
 374 vergence at 10 hPa, with a closeby corresponding region of absorption into the westerly  
 375 SAO jet on the opposite side of the critical line between  $\pm 20^\circ$  latitude.

376 Having identified the regions of shear between the respective easterly and westerly  
 377 jets as significant sources (and sinks) for momentum, we now examine the aforementioned

378  $Q$  flow invariant. The April 1984 isosurfaces of the monthly mean  $U$  winds and  $Q$  be-  
 379 tween 0.01 hPa and 100 hPa are shown in Figure 6. Here the westerly positive phase of  
 380 the SAO ( $30\text{ms}^{-1}$  green isosurface) is wedged between the easterly mesosphere jet be-  
 381 tween 0.01 hPa and 0.1 hPa and the easterly phase of the QBO between 10 hPa and 60  
 382 hPa ( $5\text{ms}^{-1}$  purple isosurfaces). In the regions of shear between the respective jets,  $Q$   
 383 isosurfaces are largely unorganised and noisy. These are the regions corresponding to large  
 384 amplitude anomalous E-P fluxes (Figure 5). The large scale coherent positive  $Q$  isosur-  
 385 faces i.e. vortices, are, as for the leading April EOFs, entirely contained within the west-  
 386 erly jet centred about 1 hPa and occur only at latitudes where the jet exceeds  $30\text{ms}^{-1}$ .  
 387 In common with the April EOFs 1 & 2, these structures span up to  $30^\circ$  longitude at  $\pm 15^\circ$   
 388 latitude corresponding to around 3200km in length and between 10 hPa and 0.1 hPa en-  
 389 compassing up to 40km in the vertical.

## 390 5 Summary

391 Vortex structures associated with  $Q$  manifest only during the SAO westerly phase  
 392 and only where the westerly jet reaches speeds in excess of  $35\text{ms}^{-1}$ . Similar wind veloc-  
 393 ities are necessary to form the shear zones at the jets upper and lower boundary. As such  
 394 the vortices are most coherent during March-April and less evident during October. The  
 395  $Q$  structures manifest on given dates within the equinoctial month(s) with wave num-  
 396 bers between 4-7 but are typically wave-5, resembling the leading statistically station-  
 397 ary 3D-EOF  $Q$  patterns. Our analysis indicates that the vortices are maintained by a  
 398 combination of local (shear zones) and remote (vertically propagating tropical) sources  
 399 of momentum. Although not directly discussed here, there is evidence that the phase re-  
 400 lationship between the QBO and SAO directly influences the strength of the shear zone  
 401 at the lower boundary of the stratopause SAO during its westerly phase with consequences  
 402 for the resulting  $Q$  vortices.

403 The emergence of the vortex structures during the westerly SAO phase and their  
 404 dependence on the jet strength and shear at the boundaries indicates a rich flow geom-  
 405 etry allowing methods commonly applied to analyse turbulent shear flows to be fruit-  
 406 fully employed. The scale and extent of these vortical structures, structures that appear  
 407 to be unique to the stratopause, is remarkable. While the mechanisms of the SAO have  
 408 been generally understood for quite some time, many of the details remain to be quan-  
 409 tified, particularly the spectrum of Kelvin and inertial gravity waves required to gener-

410 ate sufficient momentum to drive the westerly phase. Despite not explicitly resolving grav-  
411 ity waves due to our reduced temporal resolution, our E-P flux analysis is broadly con-  
412 sistent with the recent detailed analysis of Sato et al. (2018). They emphasise the com-  
413 plicated roles of E-P flux divergences and nonlinear dynamics during the equinoctal sea-  
414 sons, clear motivation for further exploration of the unique coherent structures appear-  
415 ing near the stratopause.

416 Observational evidence for the existence of the vortex structures described here might  
417 in principle be derived from long lived satellite trace gas distributions, such as N<sub>2</sub>O, from  
418 instruments such as the Microwave Limb Sounder (MLS) on the Earth Observing Sys-  
419 tem Aura satellite launched in July 2004. While the scientifically useful range of the Aura/MLS  
420 N<sub>2</sub>O data is from 100 to 1 hPa (Khosrawi et al., 2013) the detection of equinoctal vor-  
421 tices at the stratopause may be difficult but perhaps not impossible due to the size of  
422 the structures in question. Similar limitations on the effective vertical extent of obser-  
423 vations apply to Kelvin wave signatures in stratospheric trace constituents from MLS  
424 however the observational basis for the important role of fast Kelvin waves on the dy-  
425 namics of the stratosphere is well established (Salby et al., 1984; Gray & Pyle, 1986; Mote  
426 et al., 2002; Mote & Dunkerton, 2004; Feng et al., 2007).

427 Finally it remains to verify the existence of equinoctal stratopause vortices in other  
428 reanalyses and if possible observational data and to develop the corresponding linear in-  
429 stability analysis to better understand the mechanisms by which these structures might  
430 manifest.

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436 Datasets for this research are available in these in-text data citation references: (Gelaro  
437 & Co-authors, 2017).

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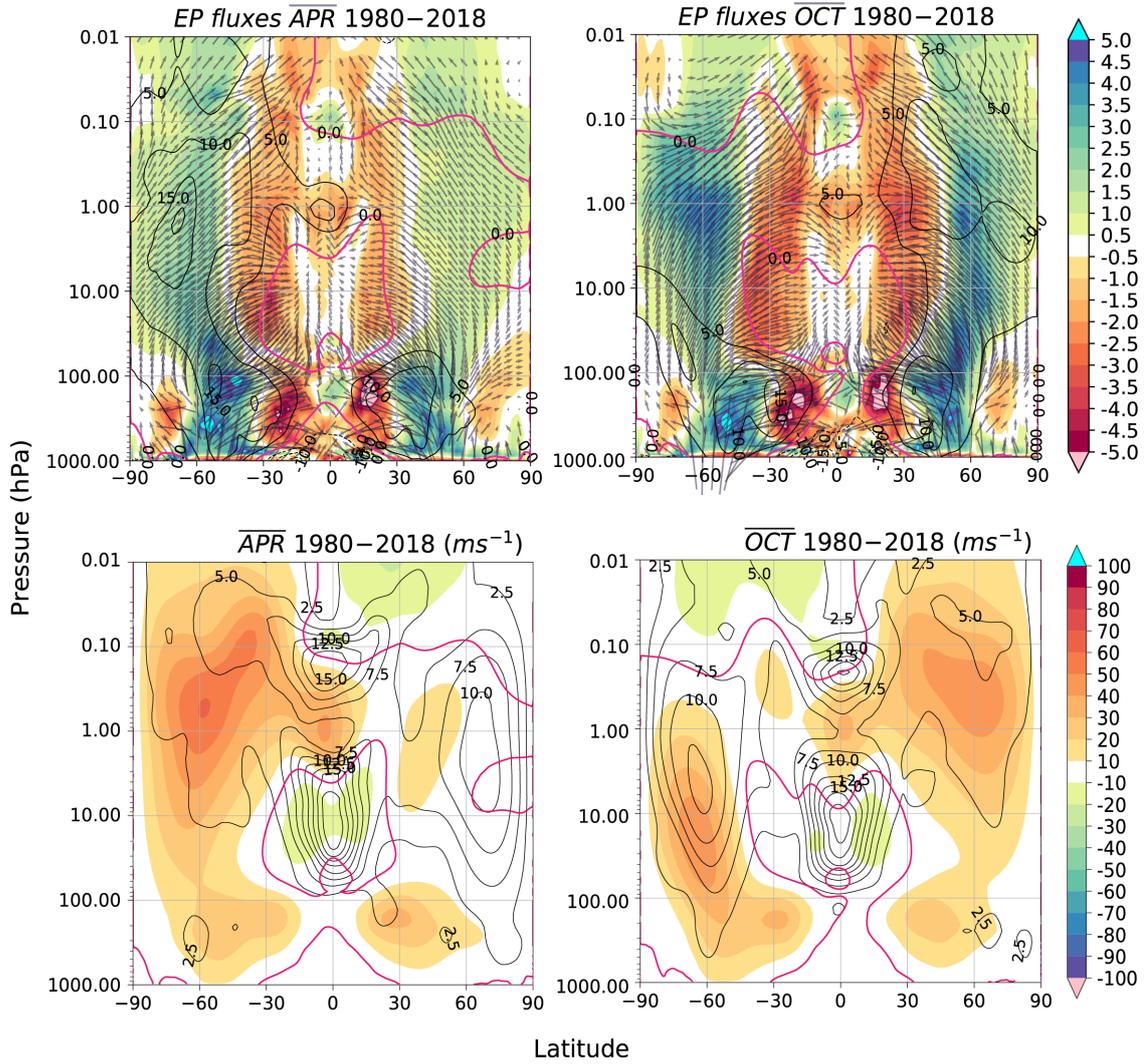
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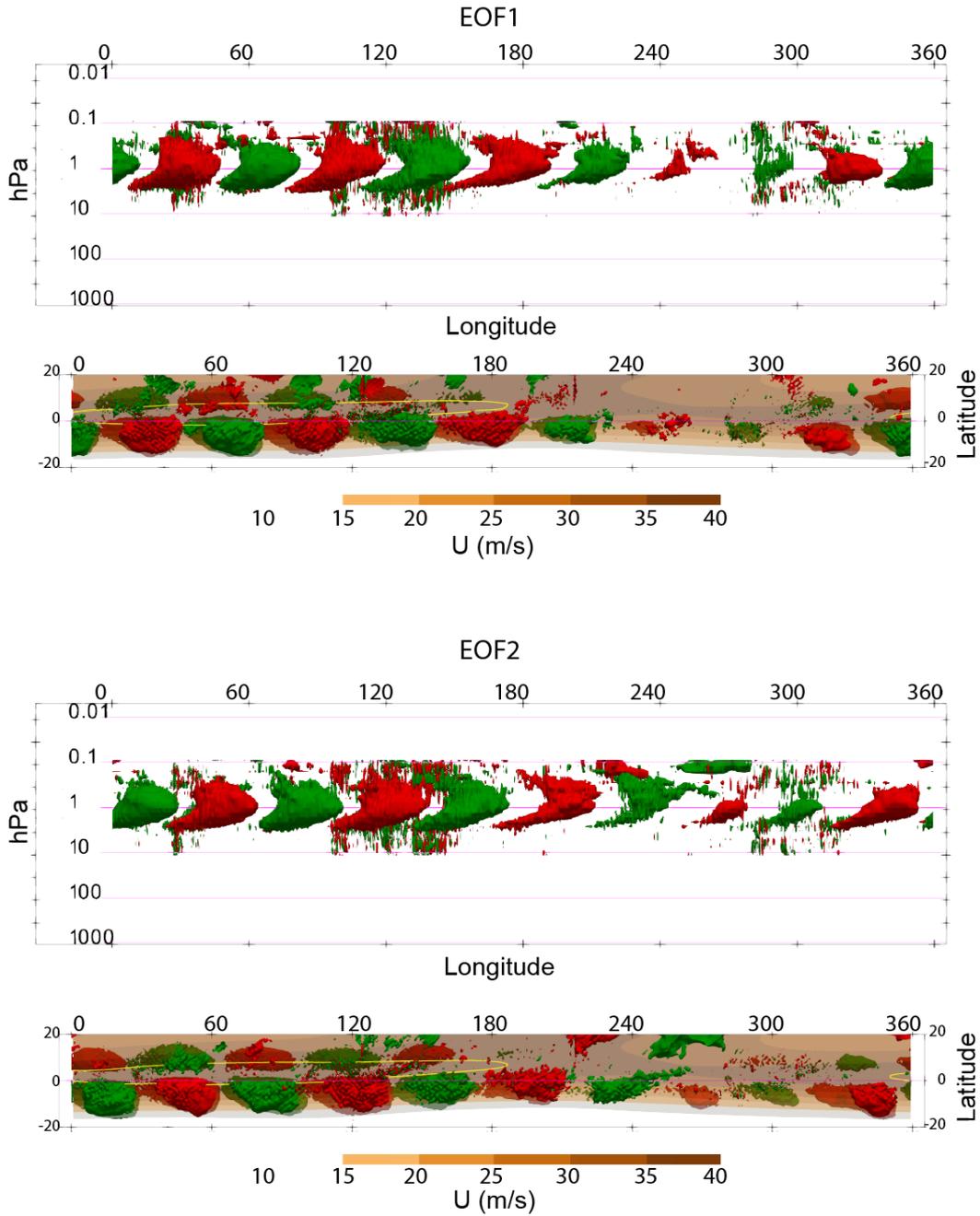
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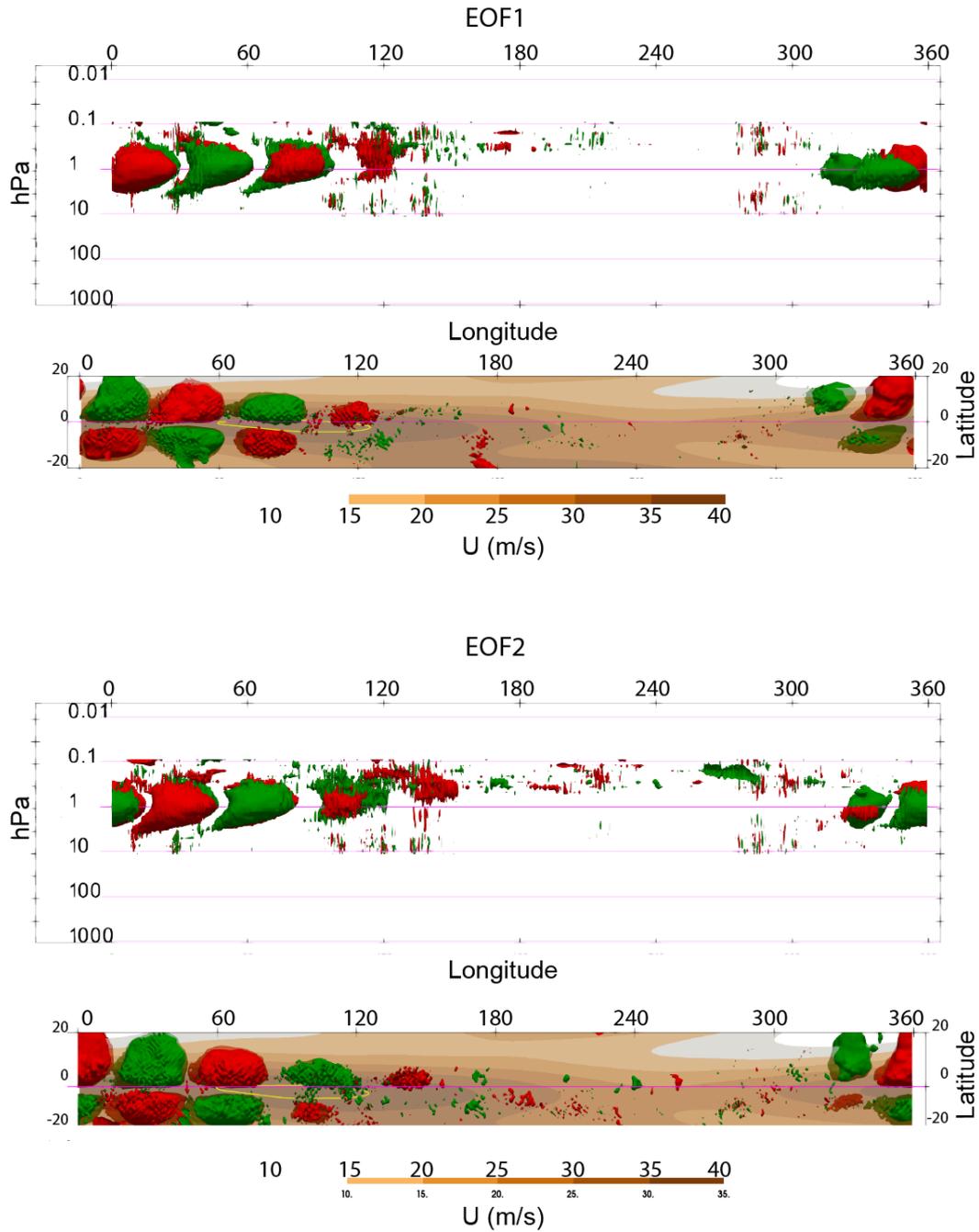
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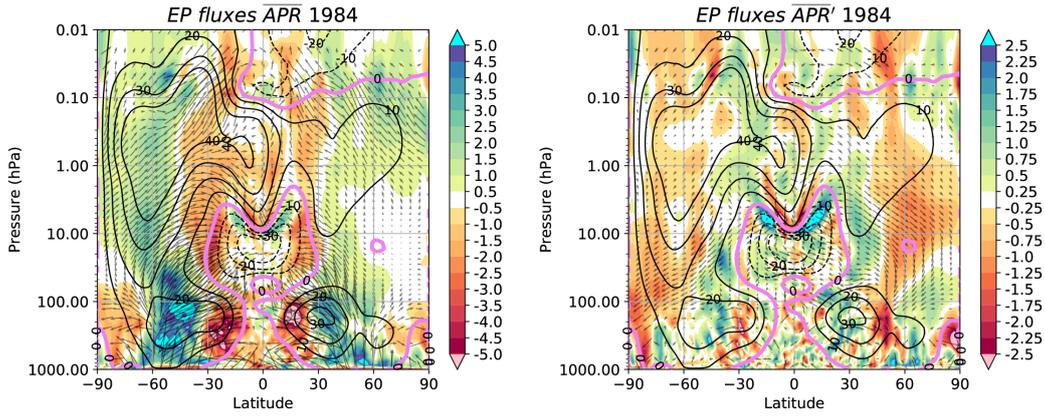
**Figure 2.** Left column: April and right column: October E-P flux calculations. (upper row) Climatological E-P fluxes, calculated using daily U, V and T data over 1980-2018. Shading is the flux divergence with positive (negative) values indicating westerly (easterly) sources of momentum. Black contours the climatological winds. Negative U values are dashed and zero corresponds to the magenta contour. All quantities (E-P fluxes and U zonal winds) have been divided by the 1980-2018 standard deviation. The vectors below 100 hPa have been appropriately thinned for display purposes. (lower row) Shading indicates the monthly climatological (1980-2018) U winds zonally averaged between  $0^{\circ}$ - $360^{\circ}$  longitude. Negative (positive) wind values indicate easterly (westerly) flow. Black contours are the corresponding standard-deviations in  $ms^{-1}$ .



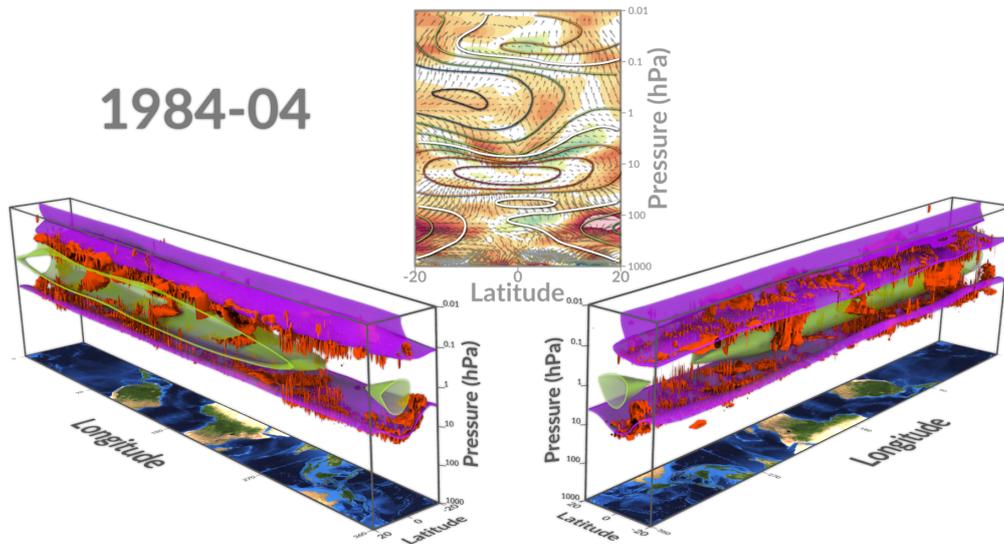
**Figure 3.** The leading 2 3D-EOFs of  $Q$  based on daily anomalies for April w.r.t. the climatological month viewed from the South and top-down. Positive (negative)  $Q$  values are indicated in red (green).  $Q$  isosurfaces correspond to  $\pm 1.5e^{-11}$ . The climatological  $U$  zonal wind velocities are indicated by the shaded background in the top-down view where velocities range from  $15\text{-}40\text{ms}^{-1}$  with colouring in  $5\text{ms}^{-1}$  increments indicated by the colour bar. The yellow contour indicates the boundary between the  $30\text{-}35\text{ms}^{-1}$  &  $35\text{-}40\text{ms}^{-1}$  climatological  $U$  zonal wind velocities. The opacity of the climatological  $U$  zonal wind values has been reduced in order to better see the structure below the  $0.62\text{ hPa}$  level from the top down aspect panels.



**Figure 4.** The leading two 3D-EOFs of  $Q$  based on daily anomalies for October. Velocities greater than  $30 \text{ m/s}^{-1}$  are identified by the yellow contour line. All other parameters are as for Figure 3.



**Figure 5.** April 1984 monthly E-P fluxes (arrows) and flux divergence (shaded). Left panel is the average for April 1984, the right panel is the anomaly relative to long term 1980-2018 mean. Anomalies are normalised by the local standard deviation for the month. Black contours are respective monthly mean U zonal winds, and the zero contour (critical line) is shown in magenta ( $ms^{-1}$ ).



**Figure 6.** Isosurfaces of Q (positive  $1.5e^{-11}$ ) and U (easterly  $5ms^{-1}$  (magenta) and westerly  $30ms^{-1}$  (green)) for April 1984. Q below 100 hPa has been greyed-out. Isosurfaces are identified between 0.01 hPa and 10 hPa. The middle insert panel displays April 1984 monthly E-P fluxes (arrows) and flux divergence (shaded) between  $20^{\circ}S$  and  $20^{\circ}N$  with the critical line shown as the white contour.