

Soil infiltration characteristics and pore distribution under freezing-thawing conditions

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Key Points:

- The hydraulic properties of frozen soil were measured with a tension infiltrometer and ethylene glycol.
- Verify the feasibility of aqueous ethylene glycol solution as an infiltration medium.
- Discuss the effect of freeze-thaw action on soil pore distribution and infiltration.

Abstract

Frozen soil infiltration widely occurs in hydrological processes such as seasonal soil freezing and thawing, snowmelt infiltration, and runoff. Accurate measurement and simulation of parameters related to frozen soil infiltration processes are highly important for agricultural water management, environmental issues and engineering problems in cold regions. Temperature changes cause soil pore size distribution variations and consequently dynamic infiltration capacity changes during different freeze-thaw periods. To better understand these complex processes and to reveal the freeze-thaw action effects on soil pore distribution and infiltration capacity, selected black and meadow soils and chernozem, which account for the largest arable land area in Heilongjiang Province, China. Laboratory tests of soils at different temperatures were conducted using a tension infiltrometer and ethylene glycol aqueous solution. The stable infiltration rate, hydraulic conductivity were measured, and the soil pore distribution was calculated. The results indicated that for the different soil types, macropores, which constituted approximately 0.1% to 0.2% of the soil volume under unfrozen conditions, contributed approximately 50% of the saturated flow, and after soil freezing, the soil macropore proportion decreased to 0.05% to 0.1%, while their saturated flow proportion decreased to approximately 30%. Soil moisture froze into ice crystals inside relatively large pores, resulting in numerous smaller-sized pores, which reduced the number of macropores while increasing the number of smaller-sized mesopores, so that the frozen soil infiltration capacity was no longer solely dependent on the macropores. After the ice crystals had melted, more pores were formed within the soil, enhancing the soil permeability.

Key words: Freezing-thawing soil; Hydraulic conductivity; Pore distribution; Macropores; Infiltration characteristics

1. Introduction

Over the last few decades, the temperature changes caused by global warming have altered the

freezing state of near-surface soils, and in China, changes in characteristic values such as the mean annual area extent of seasonal soil freeze/thaw state and maximum freezing depth indicate the degradation of frozen soil, especially at high latitudes (Peng et al., 2016; X. Wang et al., 2019). Under the effect of temperature, most frozen regions experience the seasonal freezing and thawing of soil, accompanied by coupled soil water and heat movement and frost heave processes, thus making the soil structure and function more variable (Fu et al., 2019; Oztas & Fayetorbay, 2003). Parameters such as the soil infiltration rate and hydraulic conductivity are key factors in the study of soil water movement, groundwater recharge, and solute and contaminant transport simulation (Angulo-Jaramillo et al., 2000). In regard to unfrozen soils, the temperature has been shown to change the soil structure and kinematic viscosity of soil water, thereby affecting the unsaturated hydraulic conductivity of soils (Gao & Shao, 2015). In terms of frozen soils, the water infiltration characteristics and pore size distribution are highly variable and difficult to observe (Watanabe et al., 2013); moreover, the water movement in freezing-thawing soils is complicated by the migration of water and heat and the associated water phase change (Nicholas Jarvis et al., 2016). The accurate measurement of water movement parameters and soil pore distribution under freeze-thaw conditions is a necessary prerequisite for the quantitative description of the water movement in frozen soil, and the mechanism and degree of influence of the temperature on the infiltration rate, hydraulic conductivity, porosity and other parameters in the different stages of freeze-thaw periods require further research.

Currently, the studies related to the quantitative characterization of freezing-thawing soil infiltration can be mainly divided into experimental and model studies. Field experiments have been performed less often because under natural conditions, the infiltration water establishes a preferential flow into the deep soil, and the alternating freeze-thaw effect forms ice crystals to block the flow path through large pores,

subsequently limiting water infiltration (Daniel et al., 1997), while the melting effect of the infiltration water on ice makes it difficult to reach a steady infiltration state. Controlled laboratory experiments provide new opportunities for the simulation of frozen soil infiltration processes and the measurement of infiltration parameters. P. Williams and Burt (1974) conducted early direct measurements in the laboratory, resolved the water freezing problem by adding lactose and applied dialysis membranes on both sides of soil columns, and they determined the water conductivity of saturated specimens in the horizontal direction (Burt & Williams, 1976). Andersland et al. (1996) measured the hydraulic conductivity of frozen granular soils at different saturations using a conventional drop permeameter with decane as the permeant and concluded that the hydraulic conductivity was the same as that of unfrozen soils with water as the infiltration solution. McCauley et al. (2002) determined and compared the differences in hydraulic conductivity, permeability and infiltration rate between frozen and unfrozen soils using diesel mixtures as permeants, and their results indicated that the ice content determines whether soil is sufficiently impermeable. Zhao et al. (2013) quantified the unsaturated hydraulic conductivity of frozen soil using antifreeze instead of water, adopted a multistage outflow method under controlled pressures and introduced the pore impedance coefficient. However, most of these studies did not consider the differences in kinematic viscosity and surface tension between soil water and other solutions, which often results in hydraulic conductivity estimation, and the homemade devices in the laboratory are often inconvenient for generalization in the field. Due to the dynamic changes in the temperature and moisture phase, direct measurement is difficult, and hydraulic conductivity empirical equations and models of frozen soil have been developed. First, the frozen soil hydraulic conductivity was simply considered to follow a power exponential relationship with the temperature (Nixon, 1991; Smith, 1985), while others considered the hydraulic conductivity of frozen soil to be equal to that of unfrozen soil at the same water content and

assumed that the hydraulic conductivity of frozen soil was a function of the moisture content of unfrozen soil (Flerchinger & Saxton, 1989; Harlan, 1973; Lundin, 1990). On the basis of Campbell's model (Campbell, 1985), Tarnawski and Wagner (1996) proposed a frozen soil hydraulic conductivity model based on the soil particle size distribution and porosity. Watanabe and Wake (2008) viewed soil pores as cylindrical capillaries and suggested that ice formation occurs at the center of these capillaries and established a model to describe the movement of thin film water and capillary water in frozen soil based on the theory of capillaries and surface absorption (Watanabe & Flury, 2008). The similarity between freezing and soil moisture profiles has been demonstrated (Spaans, 1994; Spaans & Baker, 1996), and subsequently, freezing profiles have been applied to estimate the unsaturated hydraulic conductivity of frozen soils (Azmatch et al., 2012), which has been combined with field tests and inversion models to achieve a high accuracy (Cheng et al., 2019).

Understanding the distribution characteristics of the soil pore system is essential for the evaluation of the water and heat movement processes in soil. The soil macroporosity has been shown to impose a major impact on water cycle processes such as infiltration, nutrient movement and surface runoff. (Demand et al., 2019; NJ Jarvis, 2007). The macroporosity is widespread in a variety of soils and produces preferential flow in both frozen and unfrozen soils (Beven & Germann, 2013; Mohammed et al., 2018), and the prefreeze moisture conditions affect the amount and state of ice in the macropores of frozen soils, resulting in a notable variability in the infiltration capacity of thawed soils (Granger et al., 1984; Hayashi et al., 2003). Field experiments on frozen soil have also demonstrated that macropores accelerate the infiltration rate (Kamp et al., 2003; Stähli et al., 2004), the number and size of macropores affect the freezing and infiltration capacity of soil layers to different extents, and low temperatures cause infiltration water to refreeze inside macropores (Stadler et al., 2000; Watanabe & Kugisaki, 2017). Research on the frozen soil

macroporosity has largely focused on the qualitative analysis of its impact on the soil structure and infiltration capacity, and with the development of experimental techniques, certain new methods and techniques, such as computed tomography (CT) and X-ray scanning, have been applied to measure the number and distribution of macropores (Bodhinayake et al., 2004; Grevers et al., 1989; Taina et al., 2013), but the lack of sampling techniques targeting frozen soil still restricts related research.

Many limitations and deficiencies remain in the direct measurement of frozen soil infiltration characteristics and pore distribution, and the relevant models also require a large amount of measured data to meet the accuracy and applicability requirements. In this paper, the stable infiltration rate and hydraulic conductivity of three types of soils at different temperatures were measured by precise control of the soil and ambient temperatures, and the macropore and mesopore size distribution was calculated by using a tension infiltrometer and a glycol aqueous solution as the infiltration medium. The conclusions provide a basis and reference for the numerical simulation of the coupled water-heat migration process of freezing-thawing soil and related parameterization studies.

2. Materials and methods

2.1 Test plan

Referring to arable land area data of various regions of Heilongjiang Province, the three types of soils that dominate the cultivated land area in Heilongjiang Province are black and meadow soils and chernozem (Bureau, 1992). Harbin, Zhaoyuan and Zhaozhou were selected as typical soil areas for sampling. A 5-cm surface layer of floating soil and leaves was removed, and topsoil samples were collected at depths ranging from 0-20 cm. After natural air drying and artificial crushing, the soil was sieved, and particles larger than 2 mm in diameter were removed. The remainder was used to prepare soil columns. The basic physical and chemical parameters of the test soils, such as the bulk density, organic content and mechanical parameters,

are listed in Table 1.

Table 1

Basic physical and chemical properties of three kind of soils

| Soil types | Bulk density (g/cm ³) | Organic content (g/kg) | Electrical conductivity (s/m) | Particle size (sand-silt-clay) (%) | Soil texture |
|----------------|--------------------------------------|---------------------------|----------------------------------|--|-----------------|
| Black soil | 1.31 | 28.32 | 0.02 | 12.64-70.82- 16.54 | |
| Meadow soil | 1.22 | 16.51 | 0.01 | 9.52-73.00-17.48 | silt loam |
| Chernozem | 1.15 | 26.52 | 0.01 | 38.99-50.30- 10.71 | |

An artificial climate chamber was applied to control the temperature of the soil column and infiltration solution, and four temperature treatments were established with three replications for each treatment: 15°C, unfrozen soil, representing the soil before freezing, which was recorded as 15°C (BF); -5°C, stable freezing; -10°C, stable freezing; and freezing at -10°C followed by thawing at 15°C, representing the soil after melting, which was recorded as 15°C (AM). The freezing and thawing times were both 48 h. When the soil temperature was consistent with the set temperature in the climate chamber, the samples were considered to be completely frozen, and the effect of the number of freezing and thawing cycles was not considered in this test. According to the basic information of the original soil, the volumetric moisture content of the sieved soil was 30%, with a dry bulk density of 1.2 g/cm³. To ensure a homogeneous column, the soil was loaded into a polyvinyl chloride (PVC) cylinder at 5-cm depth intervals, and petroleum jelly was applied to the sides to reduce the sidewall flow (Lewis & Sjöström,

2010). The PVC cylinder was 26 cm in diameter and 30 cm in height, with a perforated plate at the bottom. To prevent lateral seepage, the barrel occurred 5 cm above the soil surface, and the thickness of the soil layer was 20 cm. A HYDRA-PROBE II sensor (STEVENS Water Monitoring Systems, Inc., Portland, Oregon, USA) was inserted in the middle of the pail to observe the potential soil temperature and liquid water content change to determine whether ice melting occurred. A 5-cm thick layer of sand and gravel was emplaced below the soil column, and a 5-cm thick layer of black polypropylene insulation cotton was wrapped around the outer layer and bottom of the soil column. The stable infiltration rate under tension levels of -3, -5, -7, -9, -11, and -13 cm was measured with a tension infiltrometer, and the infiltration time and cumulative infiltration were recorded. The detailed layout of the test apparatus is shown in Fig. 1.

The addition of a certain amount of lactose, antifreeze or other substances to water greatly reduces the freezing point of water (P. Williams & Burt, 1974; Zhao et al., 2013) so that the soil macropores are not quickly filled with ice with decreasing temperature, thereby maintaining better conditions for water flow. To further verify the feasibility of the use of deionized water to prepare an aqueous solution of ethylene glycol at a mass concentration of 40% as the infiltration medium for the frozen soil measurements, the surface tension of the aqueous glycol solution at -5°C and -10°C and its relationship with the temperature were measured with a contact angle measuring instrument (OCA20, DataPhysics Instruments, Germany) and a surface tension measuring instrument (DCAT-21, DataPhysics Instruments, Germany), respectively. As an example, the contact angle measurement process of the black soil at -10°C with the aqueous ethylene glycol solution is shown in Fig. 2, and it is observed that the contact angle decreases to 0° within a few seconds after the liquid droplet is placed on the soil, and the liquid droplet completely dissolves in the frozen soil, which implies that the addition of glycol to water does not alter the wetting ability of the soil particles (Lu & Likos, 2004). The relevant physicochemical properties of the aqueous ethylene glycol

solution and water are compared in Table 2.

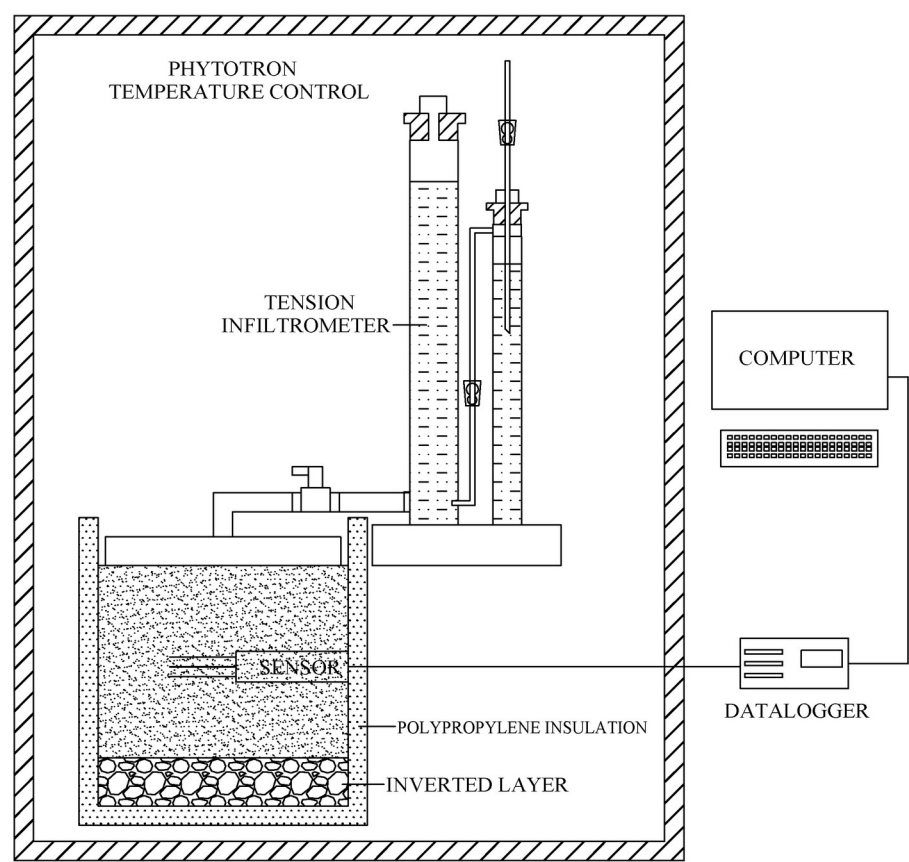


Fig. 1. Diagram of the test equipment.



Fig. 2. Process of the contact angle measurement between the aqueous ethylene glycol solution and black soil at -10°C.

Table 2
Comparison of the physicochemical properties of the 40% ethylene glycol aqueous solution and water

| Infiltration solution | Temperature | Density (g/ | Dynamic | Surface tension | Contact |
|-----------------------|-------------|-------------|---------|-----------------|---------|
|-----------------------|-------------|-------------|---------|-----------------|---------|

| | (°C) | cm ³ | viscosity (mPa.s) | (mN/m) | angle (°) |
|------------------|------|-----------------|-------------------|--------|-----------|
| Water | 15 | 0.9991 | 1.14 | 73.56 | 0 |
| Ethylene glycol | -5 | 1.0683 | 7.18 | 48.89 | 0 |
| aqueous solution | -10 | 1.0696 | 9.06 | 49.10 | 0 |

2.2 Measurement of the frozen soil hydraulic conductivity

Gardner (1958) proposed that the unsaturated hydraulic conductivity of soil varies with the matric potential:

$$K(h) = K_{sat} \exp(\alpha h) \quad (1)$$

where K_{sat} is the saturated hydraulic conductivity, cm/hour, and h is the matric potential or tension, cm H₂O. Wooding (1968) considered that the steady-state unconfined infiltration rate into soil from a circular water source of radius R can be calculated with the following equation:

$$Q = \pi R^2 K \left[1 + \frac{4}{\pi R \alpha} \right] \quad (2)$$

where Q is the amount of water entering the soil per unit time, cm³/h; K is the hydraulic conductivity, cm/hour; and α is a constant. Ankeny et al. (1991) proposed that implementing two successively applied pressure heads h_1 and h_2 could yield the unsaturated hydraulic conductivity, and upon replacing K in Eq. (2) with Eq. (1), the following is obtained:

$$Q(h_1) = \pi R^2 K_{sat} \exp(\alpha h_1) \left[1 + \frac{4}{\pi R \alpha} \right] \quad (3)$$

$$Q(h_2) = \pi R^2 K_{sat} \exp(\alpha h_2) \left[1 + \frac{4}{\pi R \alpha} \right] \quad (4)$$

Dividing Eq. (4) by Eq. (3) and solving for α yields:

$$\alpha = \frac{\ln[Q(h_2)/Q(h_1)]}{h_2 - h_1} \quad (5)$$

where $Q(h_1)$ and $Q(h_2)$ can be measured, h_1 and h_2 are the preset tension values, and α can be calculated with Eq. (5). The result can be substituted into Eq. (3) or (4) to calculate K_{sat} . When the number of tension levels is larger than 2, parameter fitting methods can be applied to improve the accuracy of α and K_{sat} (Hussen & Warrick, 1993).

The tension is controlled by the bubble collecting tube of the tension infiltrometer, and different pressure heads h correspond to different pore sizes r . By applying different pressure heads h to the soil surface, water will overcome the surface tension in the corresponding pores and be discharged, and the infiltration volume is recorded after reaching the stable infiltration state.

Under the assumption that the frozen soil pore ice pressure is equal to the atmospheric pressure and that solutes are negligible, the Clausius-Clapeyron equation can be adopted to achieve the interconversion between the soil temperature and suction (Konrad & Morgenstern, 1980; Watanabe et al., 2013), which can be simplified as follows:

$$\psi = -L\rho_w \frac{T}{273.15} \quad (6)$$

where ψ is the soil suction, kPa; L is the latent heat of fusion of water, 3.34×10^5 J/kg; ρ_w is the density of water, 1 g/cm^3 ; and T is the subfreezing temperature, °C. After the unit conversion of the soil suction into h (cm H_2O), the unsaturated hydraulic conductivity of frozen soil at different negative temperatures can be obtained via substitution into Eq. (2).

2.3 Measurement of the pore size distribution in frozen soil

As a nonuniform medium, soil consists of pores of various pore sizes, and the equation for the soil pore radius r can be obtained from the capillary model (Watson & Luxmoore, 1986):

$$r = \frac{2\sigma \cos \beta}{\rho gh} \quad (7)$$

where σ is the surface tension of the solution, g/s²; β is the contact angle between the solution and pore wall; ρ is the density of the solution, g/cm³; g is the acceleration of gravity, m/s²; and h is the corresponding tension of the tension infiltrometer, cm H₂O.

The effective macroporosity θ_m can be calculated for various soil particle sizes based on the Poiseuille equation (Wilson & Luxmoore, 1988):

$$\theta_m = 8\mu K_m / \rho g r^2 \quad (8)$$

where μ is the dynamic viscosity of the fluid, g/(cm*s); K_m is the macropore hydraulic conductivity and is defined as the difference between $K(h)$ at various tension gradients, cm/h; and r is the corresponding equivalent pore size. The effective porosity is equal to the number of pores per unit area multiplied by the area of the corresponding pore size. For different pore sizes, the maximum number of effective macropores per unit area N can be calculated with the following equation:

$$N = \theta_m / \pi r^2 \quad (9)$$

where N is the number of effective macropores per unit area, and Eq. (7) calculates the minimum value of the pore radius, while the result obtained with Eq. (9) is actually the maximum number of effective macropores per unit area and the maximum porosity.

Considering the differences in surface tension and density between the aqueous ethylene glycol solution and water, when calculating the frozen soil pore size distribution, it is necessary to convert the tension into the equivalent pore radius according to Eq. (7), which is classified and subdivided into large and medium pores according to the common classification method (Luxmoore, 1981), the details of which are listed in Table 3, while the corresponding tension values in Table 3 are substituted into the fitting curve

equation to calculate the corresponding stable infiltration rate q and unsaturated hydraulic conductivity K .

Table 3

Tension and equivalent pore radius conversions

| Pore types | Pore radius (mm) | Tension conversion (cm) | | |
|-------------|------------------|-------------------------|--|---|
| | | Water (15°C) | Ethylene glycol aqueous solution (- 5°C) | Ethylene glycol aqueous solution (- 10°C) |
| Macroporous | >0.5 | 0~3 | 0~1.86 | 0~1.87 |
| | 0.3-0.5 | 3~5 | 1.86 ~3.11 | 1.86 ~3.12 |
| | 0.15-0.3 | 5~10 | 3.11~6.22 | 3.12~6.23 |
| Mesoporous | 0.1-0.15 | 10~15 | 6.22~9.32 | 6.23~9.35 |
| | 0.05-0.1 | 15~30 | 9.32~18.65 | 9.35~18.70 |

3. Results

3.1 Infiltration characteristics of freezing-thawing soils

According to the recorded cumulative infiltration and duration, curves of the cumulative infiltration and infiltration rate were plotted over time, as shown in Figs. 3 and 4, respectively. The constant α and saturated hydraulic conductivity K_{sat} were calculated under different tensions h and corresponding steady-state infiltration rates q , and the unsaturated hydraulic conductivity under different tensions was calculated with Eq. (1). The stable infiltration rate and unsaturated hydraulic conductivity at different temperatures are shown in Fig. 5, and the details of α and K_{sat} are listed in Table 4.

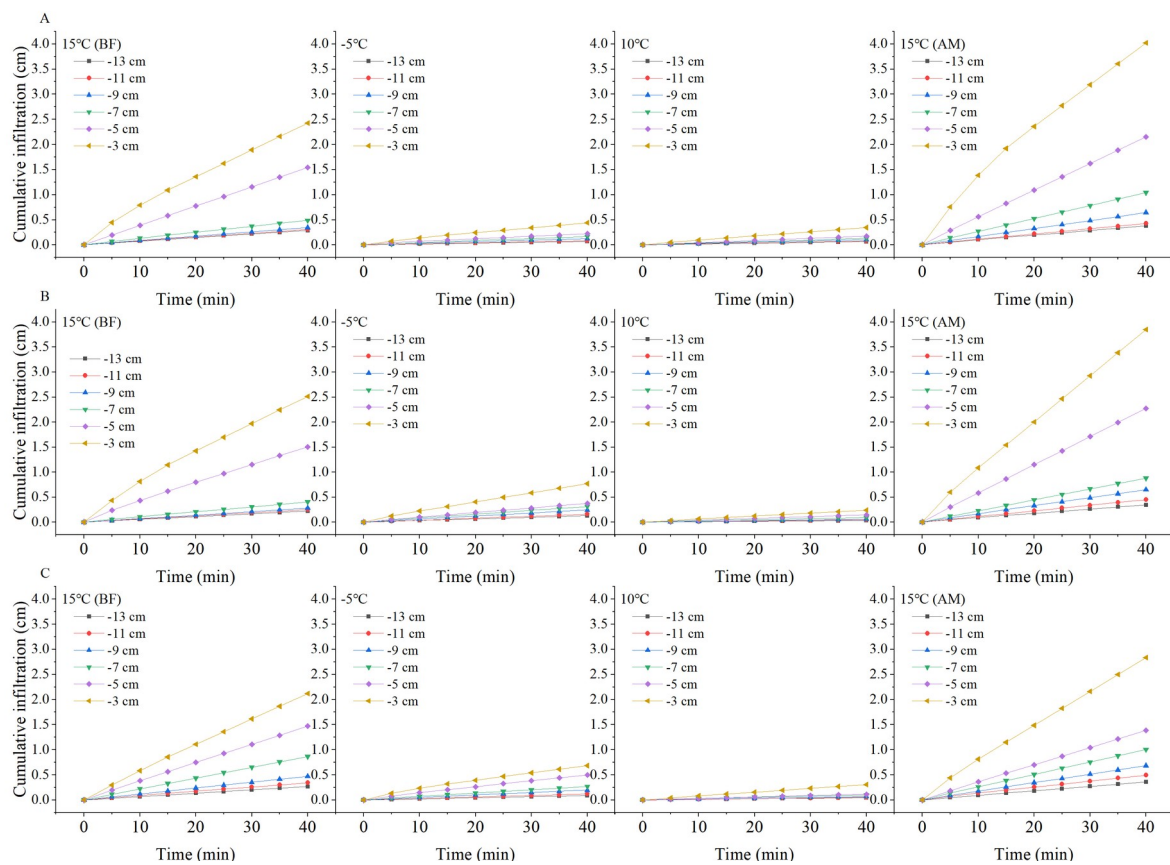


Fig. 3. Cumulative infiltration over time under the different treatments.

Note: A Black Soil; B Meadow Soil; C Chernozem.

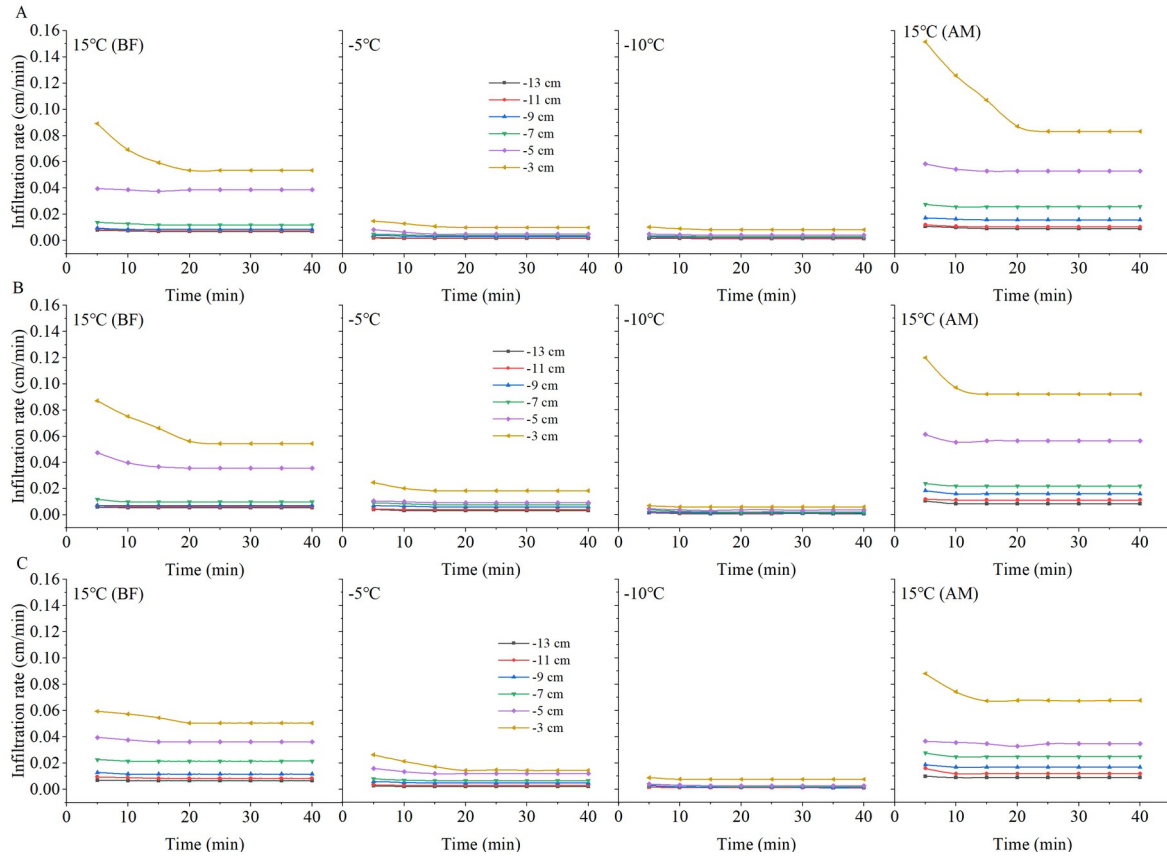


Fig. 4. Infiltration rate over time under the different treatments.

Note: A Black Soil; B Meadow Soil; C Chernozem.

As shown in Figs. 4 and 5, under the different tension conditions, the infiltration capacity of the unfrozen soil is basically consistent with the findings of field experiments and is highly influenced by the tension value (D. Wang et al., 1998). Compared to the room-temperature soil, the cumulative infiltration of frozen soil slowly increases, and the infiltration rate always remains low, while under the same negative temperature treatment, the influence of the tension value is also greatly reduced. When the temperature was reduced to -10°C , few major tension differences were observed except for the maximum tension of -3 cm. From the change in the slope of the two curves, we find that the time for the unfrozen soil to reach the stable infiltration rate usually ranges from 15~20 min, while the time for the frozen soil to reach the stable infiltration rate is usually 10 min under higher tensions of -3 and -5 cm and 5 min under lower tensions.

Comparing the infiltration process before and after the freezing and thawing of the soil, overall, the cumulative infiltration and infiltration rate exhibited varying degrees of increase with increasing tension value, and the increase amplitude expanded. Moreover, the difference in the cumulative infiltration and infiltration rate between the low tension levels ranging from -9 to -13 cm after soil thawing was larger than that before soil freezing, which also indirectly demonstrated that freezing and thawing could further stabilize the soil pore distribution by affecting the homogeneity, which will be detailed in subsequent sections.

Table 4

Infiltration parameters of the different temperature treatments of the three soil types

| Soil types | Temperature (°C) | α (cm/h) | K_{sat} (cm/h) |
|-------------|------------------|-----------------|------------------|
| Black soil | 15 (BF) | 0.2742 | 5.1480 |
| | -5 | 0.1993 | 0.5960 |
| | -10 | 0.2028 | 0.5221 |
| | 15 (AM) | 0.2629 | 7.4658 |
| Meadow soil | 15 (BF) | 0.3071 | 5.9232 |
| | -5 | 0.1996 | 1.1385 |
| | -10 | 0.2477 | 0.4903 |
| | 15 (AM) | 0.2934 | 9.3757 |
| Chernozem | 15 (BF) | 0.2166 | 3.7185 |
| | -5 | 0.1907 | 0.9739 |
| | -10 | 0.2508 | 0.6077 |
| | 15 (AM) | 0.2182 | 5.1283 |

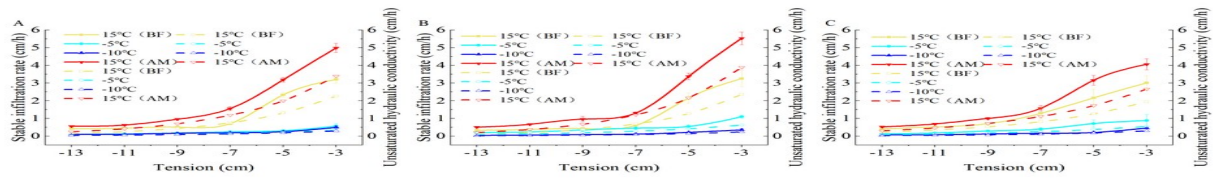


Fig. 5. Variation curves of the unsaturated hydraulic conductivity and stable infiltration rate with the tension for the different treatments of the three soils.

Note: A Black soil; B meadow soil; C chernozem. The solid lines represent the stable infiltration rate, and the dashed lines represent the unsaturated hydraulic conductivity.

Combining Fig. 5 and Table 4, we observe that the three types of soils exhibit a high infiltration capacity under normal temperature conditions. With increasing set tension value, the suction force of the soil matrix gradually weakens, the constraint and maintenance capacity of the matric potential to the soil water decreases, the number of pores involved in the soil water infiltration process increases, and the unsaturated hydraulic conductivity and stable infiltration rate of the three types of soils all reveal different degrees of increase. When the temperature was lowered from 15°C to -5°C and the soil reached the stable frozen state, the saturated water conductivity of the black soil, meadow soil and chernozem soil decreased by 88.42%, 80.78% and 73.8%, respectively. With decreasing soil temperature to -10 °C, due to the presence of liquid water in the pores, the saturated water conductivity still exhibited a certain decrease over the prefreeze conditions and continued to decrease by 1.43%, 10.94% and 9.85%, respectively. At negative temperatures, the unsaturated hydraulic conductivity decreased considerably and fluctuated within a small range, mainly because the unfrozen and saturated water contents were low after soil freezing. Comparing the two treatments of -5°C and -10°C, the unsaturated hydraulic conductivity (ANOVA, $P=0.72$, $F=0.14$)

and stable infiltration rate (ANOVA, $P=0.71$, $F=0.15$) of the black soil revealed almost no significant change, indicating that most of its pores were filled with ice crystals at -5°C and were no longer involved in water infiltration. The unsaturated water conductivity of the meadow and chernozem soils still exhibited a more significant reduction when the freezing temperature was further reduced to -10°C . When the temperature was raised again to 15°C and the soil was completely thawed, the steady infiltration rate and saturated hydraulic conductivity increased with increasing temperature, and the values were higher than those of the soil at the same temperature before freezing. The saturated hydraulic conductivity of the black soil, meadow soil and chernozem increased by 45.02%, 58.63% and 37.91%, respectively, over the 15°C (BF) treatment values.

3.2 Pore distribution characteristics of the freezing-thawing soil

Considering the differences in the physical and chemical properties between the infiltration solutions, infiltration parameters such as the hydraulic conductivity and stable infiltration rate alone do not fully reflect the infiltration characteristics and internal pore size of frozen soils. According to Eqs. (7)-(9), the maximum number per unit area N , effective porosity θ_m and percentage of pore flow to saturated flow P corresponding to the different soil pore sizes of the three soils under the different temperature treatments are calculated, as shown in Figs. 6 and 7.

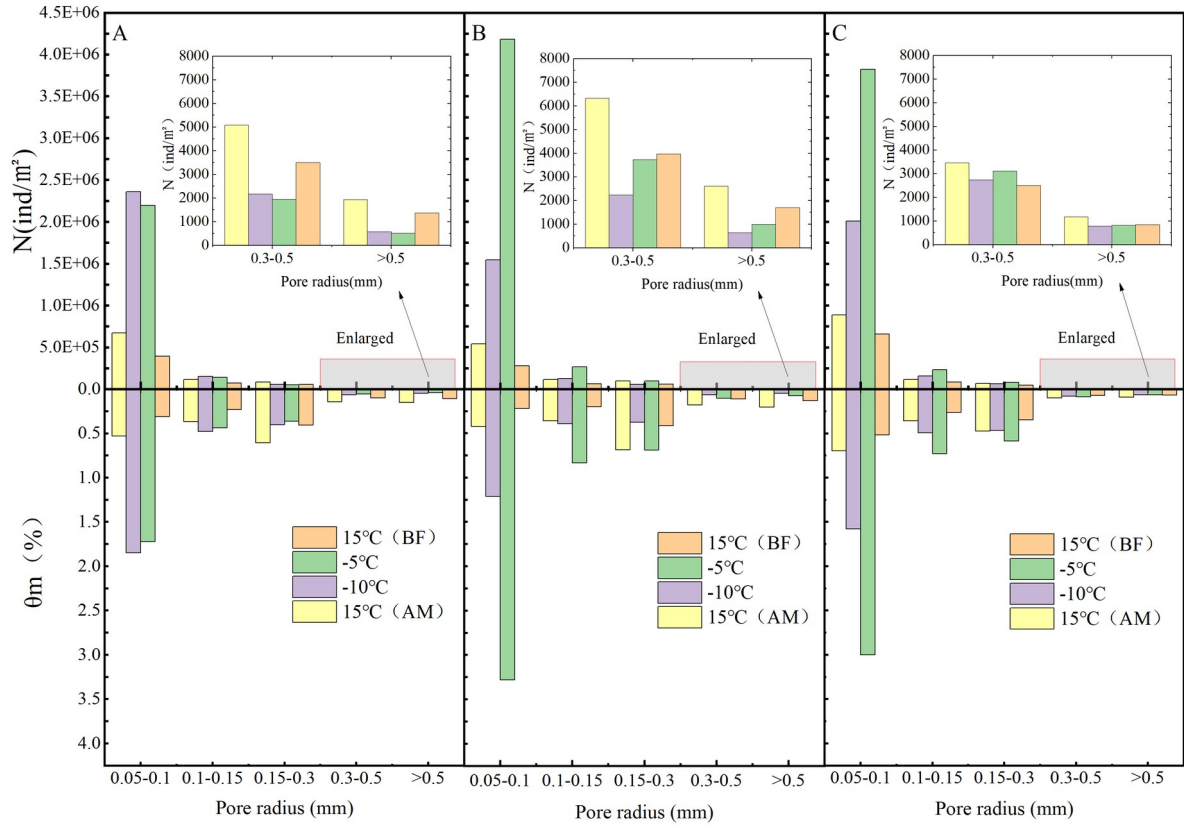


Fig.6. Number of pores and effective porosity of the different equivalent pores.

Note: A Black Soil; B Meadow Soil; C Chernozem.

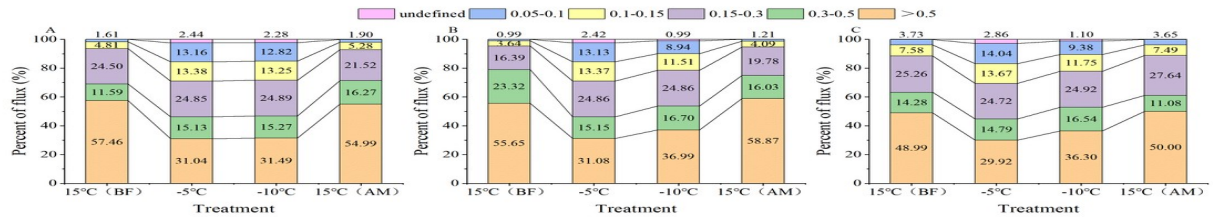


Fig. 7. Percentage of the pore flow in the saturated flow for the different equivalent pore sizes.

Note: A Black Soil; B Meadow Soil; C Chernozem.

Fig. 6 shows that pores of different equivalent radii widely occur in all three soils, and under all four temperature treatments, the largest N value is that for the medium pores with an equivalent radius of 0.05-

0.1 mm, and N gradually decreases with increasing equivalent radius size. Under the two room-temperature treatments at 15°C (BF) and 15°C (AM), the largest number of 0.05- to 0.1-mm medium pores and the smallest number of >0.5-mm macropores differed by two orders of magnitude, and the number of pores of each size exhibited different degrees of increase or decrease over the two treatments at -5°C and -10°C where freezing occurred, with the number of medium pores with an equivalent pore size of 0.05-0.1 mm significantly changing. Increases of more than an order of magnitude were achieved in all three soils, while the macropores with an equivalent pore size of >0.5 mm were generally reduced by an order of magnitude, with the difference in the number of pores of these two sizes reaching four orders of magnitude. This indicates that freezing caused by temperature change significantly alters the soil internal structure, with ice crystals forming in the relatively large pores containing the internal soil moisture, resulting in a large number of smaller pores. Assessing the two treatments at -5°C and -10°C separately, when the temperature was lowered from -5°C to -10°C, the number of pores in each pore size interval of the meadow and chernozem soils exhibited a significant decrease, while the black soil revealed a small increase, which might be related to the high organic matter content of the black soil. Comparing the two treatments at 15°C (BF) and 15°C (AM), the number of pores in all three soils increased to different degrees after thawing, and more pores were formed with the melting of ice crystals after freeze-thaw destruction of the soil particles, which enhanced the soil water conductivity.

Comprehensive analysis of Figs. 6 and 7 reveals that before freezing, the θ_m of the various pore sizes of the black and meadow soils and chernozem with an equivalent radius of >0.5 mm were 0.11%, 0.13% and 0.07%, respectively, while the P value reached 57.46%, 55.65% and 48.99%, respectively, with the values of the thawed soil similar to these values. This indicates that for all five soil pore sizes under unfrozen conditions, although the number of macropores with a pore size >0.5 mm is the smallest and the

effective porosity is the lowest, their contribution to the saturated flow is usually more than half, and the macropores need only represent a small fraction of the pore volume to significantly contribute to the soil water flow. For the frozen soil, the P value of the >0.5-mm macropores was significantly reduced and remained at approximately 30% after the reduction, while the P value of the smaller pore sizes such as 0.15-0.3 mm, 0.1-0.15 mm, and 0.05-0.1 mm, revealed different degrees of increase. Moreover, the smaller the pore size was, the greater the P value increased, and their contribution eventually accounted for more than 10% of the saturated flow. The saturated flow became more evenly distributed across the pores of each size, and the total proportion of medium pores exceeded that of the macropores. This indicates that the freezing action caused obvious changes to the soil structure, pore size and quantity, and although the macropores still played an important role, the infiltration capacity of the frozen soil no longer relied solely on these macropores, and the contribution of certain smaller-sized mesopores to the infiltration capacity of the frozen soil could no longer be neglected. Selecting the black soil as an example, the total effective porosity of the pores of each size under the four treatments was 1.15%, 2.62%, 2.84%, and 1.80%, and the P values were 99.97%, 97.56%, 97.72%, and 99.96%, respectively, which implies that the soil water infiltrated almost entirely via the large and medium pores. The small micropores, even in large numbers, contributed little to the infiltration process.

4. Discussion

4.1 Permeability and hydraulic conductivity of the frozen soil

In the field environment, although it is difficult to accurately measure the infiltration rate of frozen soils using traditional instruments and methods such as single-loop infiltrators, the obtained test results still demonstrate that the infiltration capacity decreases by one or more orders of magnitude when the soil is frozen (Stähli et al., 2004). Although the cumulative infiltration and infiltration rate of frozen soil are low,

the presence of unfrozen water allows a certain amount of infiltration flow to be maintained in the soil. When water is applied as the infiltration solution, the low temperature in the frozen soil easily causes the infiltration water to freeze, thus forming a thin layer of ice on the soil particle surface and delaying the subsequent infiltration of water. This phenomenon results in a low infiltration rate after the freezing of soils with a high initial water content and a relatively high infiltration rate after the freezing of dry soils (Watanabe et al., 2013), because the higher the ice content is, the more latent heat needs to be overcome to melt any ice crystals, resulting in a weakened propagation of the melting front, thus limiting the infiltration rate so that it is controlled by the downward movement of the melting leading edge of the ice crystals (Pittman et al., 2020). During the measurements using the tension infiltrator in this study, the sensor temperature always remained consistent with the soil temperature, indicating that the use of an aqueous glycol solution could be a useful way to avoid the problem of freezing of the infiltration solution. In addition, the hydraulic conductivity of frozen soils with different capacities and at various water flow rates was demonstrated not to greatly differ (Watanabe & Osada, 2017).

Whether water or other low-freezing point solutions are applied as infiltration media, the hydraulic conductivity of frozen soil significantly changes only within a limited temperature range above -0.5°C depending on the unfrozen water and ice contents, and at a soil temperature below -0.5°C , the hydraulic conductivity usually decreases to below 10^{-10} m/s (Watanabe & Osada, 2017; P. Williams & Burt, 1974). The unsaturated hydraulic conductivity in our experiments was measured at a set tension level, and according to Eq. (6), the soil substrate potential increases by 125 m for every 1°C decrease in temperature (P. J. Williams & Smith, 1989), while the frozen soil hydraulic conductivity calculated at -5°C and -10°C , which corresponds to the actual matric potential, is much lower than 10^{-10} m/s and can be ignored. This suggests that even under ideal conditions where no heat exchange occurs between the infiltration solution

and the soil and no freezing of the infiltration water takes place to prevent the subsequent infiltration, the unsaturated hydraulic conductivity of the frozen soil is so low that the frozen soil at lower temperatures in its natural state could be considered impermeable, both for water and other solutions.

4.2 Effect of the freeze-thaw cycles on soil pore distribution

In our study, the N value after freezing for the different types of soil was approximately 1000-2000/m² using the tension infiltrator, which agreed well with other studies and remained at a same magnitude (Pittman et al., 2020), indicating that the method is generally reliable. The freeze-thaw effect significantly improves the water conductivity of the different types of soils because it increases the porosity, decreases the soil compactness and dry weight, and thus increases the soil water conductivity (Fouli et al., 2013). On this basis, we also found that the freeze/thaw process significantly alters the size and number of soil pores, especially after freezing, and the number of macropores decreases, while the contribution of macropores to the saturated flow decreases. The proportion of the saturated flow in the mesopores with a pore size of <0.3 mm approaches or even exceeds the proportion in the macropores, indicating that the soil water inside relatively large pores is more likely to freeze, which in turn creates a large number of small pores, whereas the water transfer process in unfrozen soils primarily relies on the macropores, with obvious differences (Watson & Luxmoore, 1986; Wilson & Luxmoore, 1988). The unsaturated water conductivity of the frozen soils measured in this study is quite low, but under human control (Watanabe & Kugisaki, 2017) or natural conditions in the field (Espeby, 1990), water has been shown to infiltrate into frozen soils through macropores as long as the pore size is large enough. Considering that the soil in this experiment is disturbed soil that has been air dried and sieved, although the macropores created by tillage practices (Lipiec et al., 2006) and invertebrate activities (Lavelle et al., 2006) are excluded, due to the inherent heterogeneity of the soil particles, macropores remain in the uniformly filled soil column (Cortis &

Berkowitz, 2004; Oswald et al., 1997), and these macroporous pores still play a role in determining the infiltration water flow.

Studies related to the frozen soil macropore flow and pore distribution are still quite few and more data should be acquired and more models should be developed to better understand the water movement in frozen soil regions. In subsequent studies, we will consider applying the methods used in this paper to field experiments to examine the dynamics of the infiltration capacity and pore distribution in nonhomogeneous soils during whole freeze-thaw periods under real outdoor climatic conditions, such as lower temperatures and more severe freeze-thaw cycles, but the infiltration solution must be carefully selected, as ethylene glycol is toxic, to prevent contamination of agricultural soils and crops, and a certain concentration of lactose could be considered (Burt & Williams, 1976; P. Williams & Burt, 1974). Measurements should focus on frozen soil layers at different depths, especially in the vicinity of freezing peaks, and the spatial variability in the distribution of frozen soil pores should be investigated. This work helps to improve the accuracy of simulations such as those of frozen soil water and heat movement or snowmelt water infiltration processes.

5. Conclusions

In this paper, the infiltration capacity of soil columns under four temperature treatments representing various freeze-thaw stages was measured, and the distribution of the pores of various sizes within the soil was calculated based on the measurements by applying an aqueous ethylene glycol solution with a tension infiltrator in the laboratory. The results revealed that for the three types of soils, i.e., black soil, meadow soil and chernozem, the macropores, which accounted for only approximately 0.1% to 0.2% of the soil volume at room temperature, contributed approximately 50% to the saturated flow, and after freezing, the proportion of macropores decreased to 0.05% to 0.1%, while their share of the saturated flow decreased to

approximately 30%. Coupled with the even smaller mesopores, the large and medium pores, accounting for approximately 1% to 2% of the soil volume, conducted almost all of the soil moisture under saturated conditions. Freezing decreased the number of macropores and increased the number of smaller-sized mesopores, thereby significantly increasing their contribution to the frozen soil infiltration capacity so that the latter was no longer solely dependent on the macropores. The infiltration parameters and pore distribution of the black soil were the least affected by the different negative freezing temperatures under the same moisture content and weight capacity conditions, while those of the meadow soil were the most impacted.

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