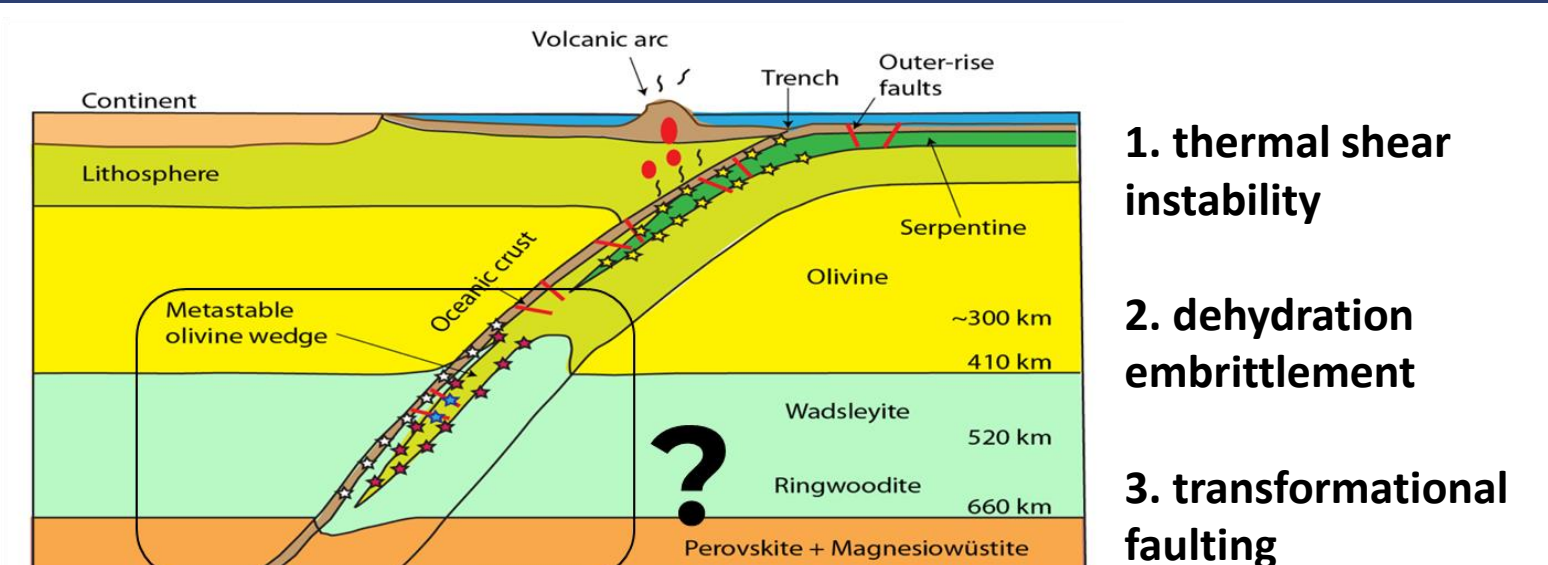


# Nature of Deep Earthquakes in the Pacific Plate from Unsupervised Machine Learning

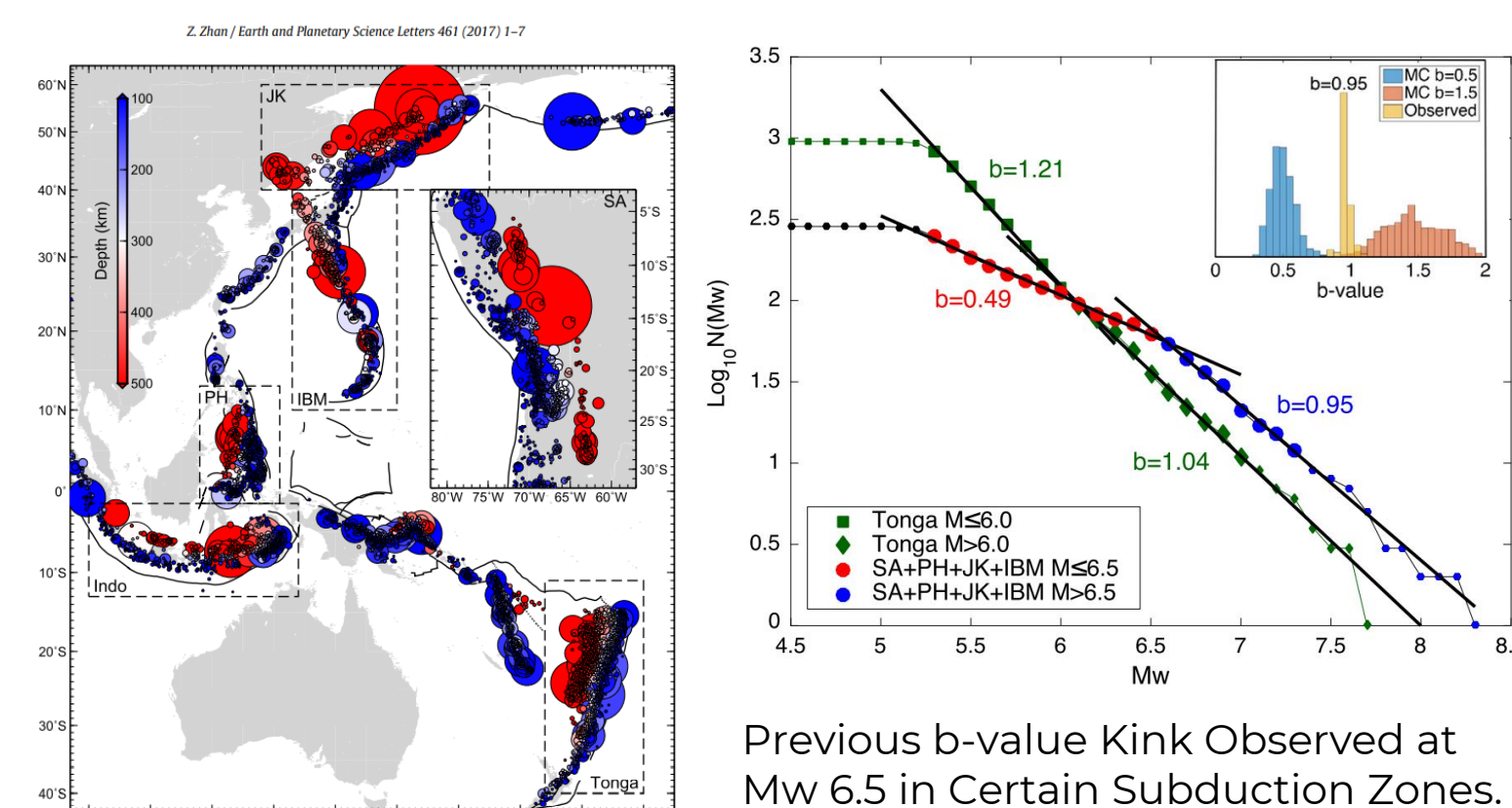
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## INTRODUCTION

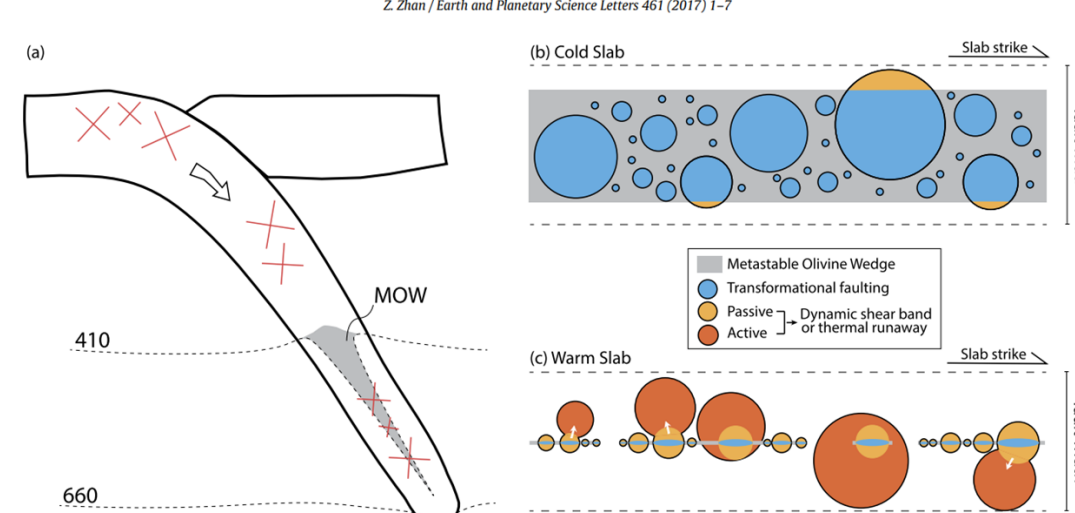


1. thermal shear instability
2. dehydration embrittlement
3. transformational faulting

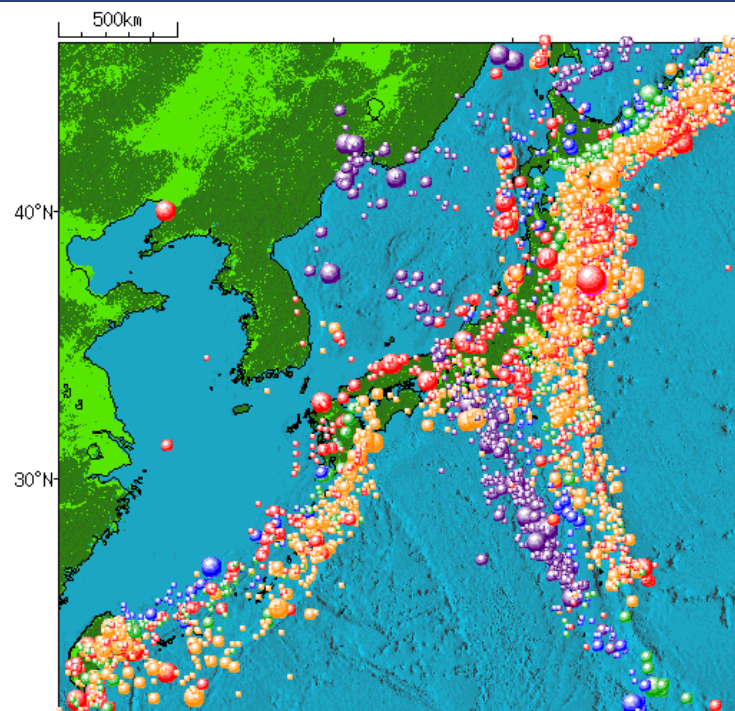


Previous b-value Kink Observed at Mw 6.5 in Certain Subduction Zones.

### Dual Mechanism Hypothesis Based on b-value Analysis of CMT Catalog



## Data & Analysis



- More complete earthquake catalog for Japan and its surrounding regions
- JMA magnitude (Mj) has been converted to Mw (Uchide & Imanishi, 2018)
 
$$M_w = aM_j^2 + bM_j + c$$

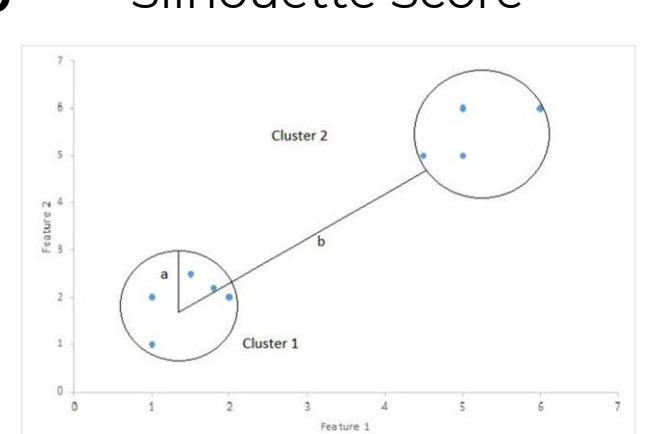
$$a = 0.053 \pm 0.003, b = 0.33 \pm 0.02, \text{ and } c = 1.68 \pm 0.03$$
- JMA Earthquake Magnitude of Completeness (Mc ~ 3.3) much lower than CMT catalog (Mc ~ 5)
- Over two million earthquakes

### Clustering Analysis with Unsupervised Machine Learning:

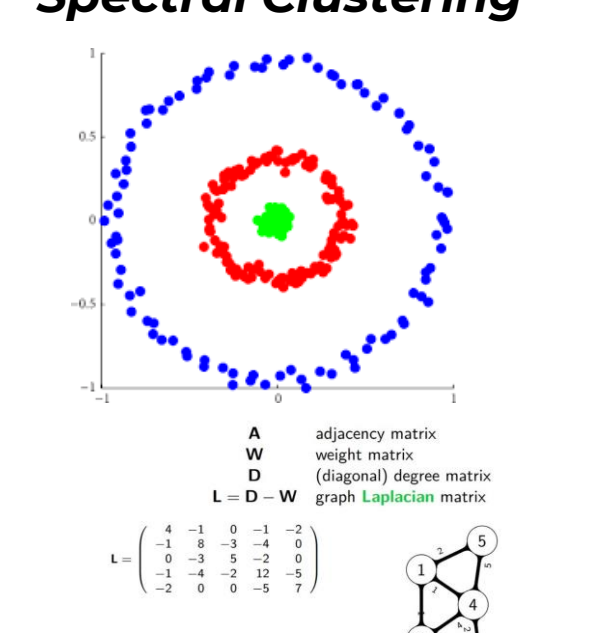
#### K-means Clustering

1. Initialize k random centroids
2. Create clusters
3. Recalculate the centroids
4. Repeat until convergence.

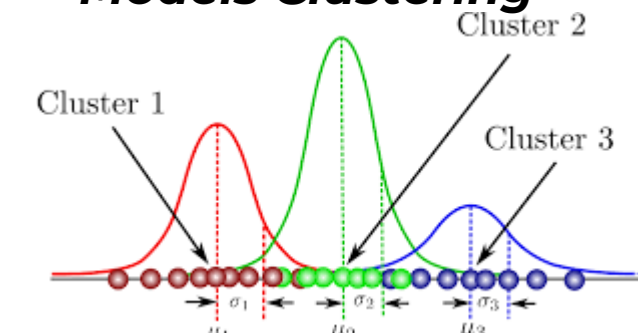
#### Silhouette Score



#### Spectral Clustering



#### Gaussian Mixture Models Clustering



### b-value analysis and its error analysis:

$$b_0 = \frac{1}{\ln(10) * (\mu - M_c)}$$

$$b_1 = \frac{1}{\ln(10) * (\mu - (M_c - \Delta M / 2))}$$

$$b_2 = \frac{1}{\ln(10) * \Delta M * \ln(1 + \frac{\Delta M}{\mu - M_c})}$$

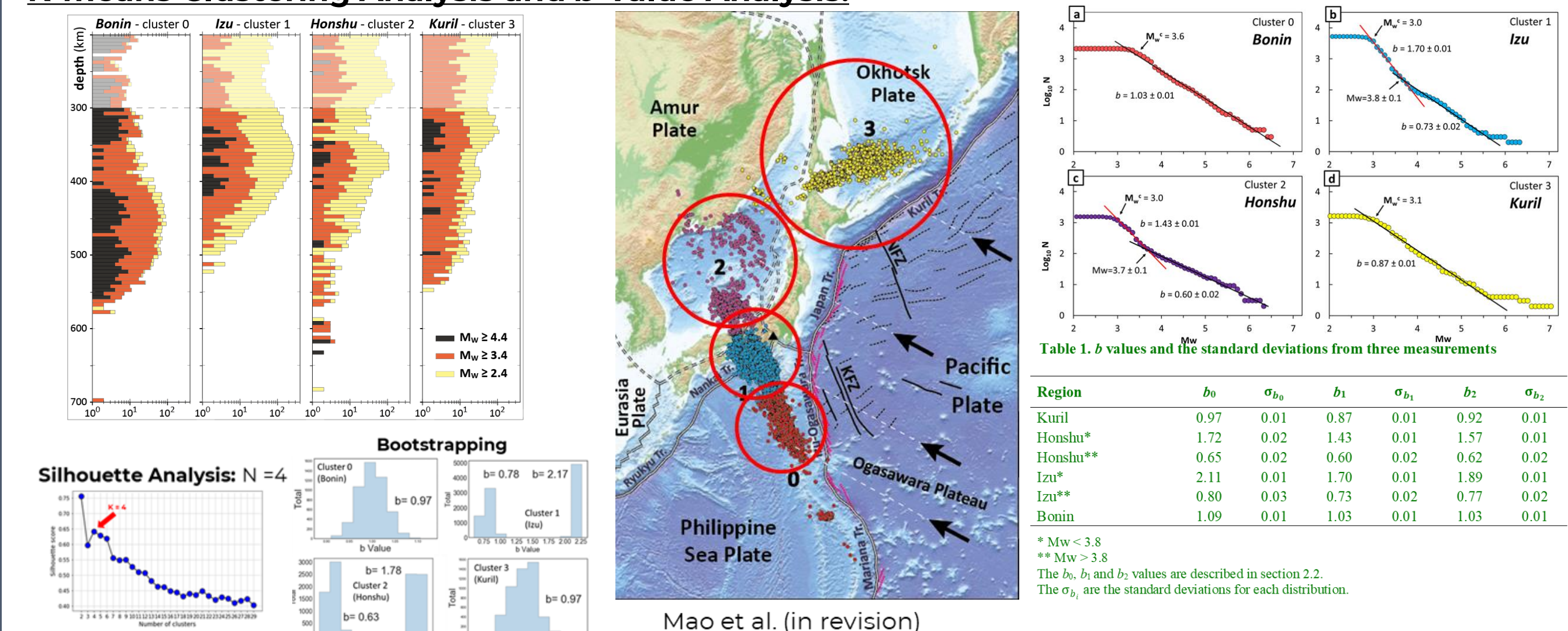
$$\sigma_{b_0} = 2.3 b_0^2 \sqrt{\frac{\sum_{i=1}^N (M_i - \mu)^2}{N(N-1)}}$$

$$\sigma_{b_1} = 2.3 b_1^2 \sqrt{\frac{\sum_{i=1}^N (M_i - \mu)^2}{N(N-1)}}$$

$$\sigma_{b_2} = \frac{\Delta M}{\ln(10) * \Delta M * \sqrt{N * (1 + \frac{\Delta M}{\mu - M_c})}}$$

## Results & Conclusion

### K-means Clustering Analysis and b-value Analysis:



### Spectral and GMM Clustering Analysis:

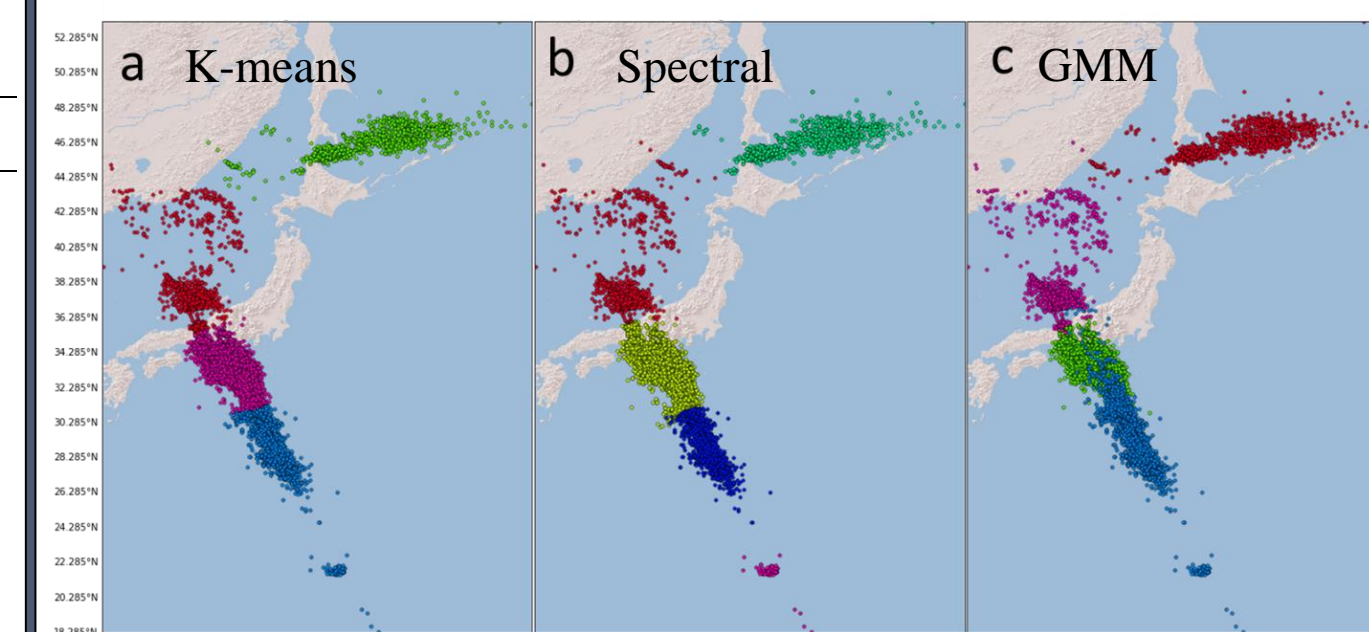
Table 2. b values and their errors from three measurements (Spectral Clustering, N=5)

Region	$b_0$	$\sigma_{b_0}$	$b_1$	$\sigma_{b_1}$	$b_2$	$\sigma_{b_2}$
Kuril	0.97	0.01	0.87	0.01	1.00	0.01
Honshu*	1.70	0.02	1.42	0.01	1.43	0.01
Honshu**	0.66	0.02	0.61	0.02	0.61	0.02
Izu*	2.10	0.01	1.69	0.01	1.71	0.01
Izu**	0.79	0.02	0.72	0.02	0.73	0.02
Bonin	0.93	0.01	0.84	0.01	0.95	0.01

Table 3. b values and their errors (Gaussian Mixture Models Clustering, N=4)

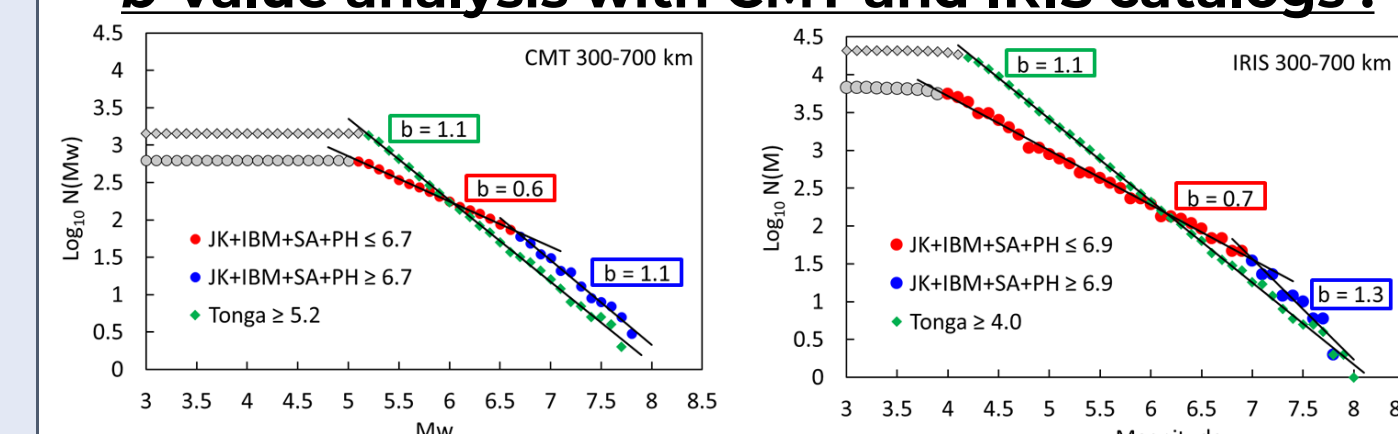
Region	$b_0$	$\sigma_{b_0}$	$b_1$	$\sigma_{b_1}$	$b_2$	$\sigma_{b_2}$
Kuril	0.97	0.01	0.87	0.01	0.88	0.01
Honshu*	1.70	0.02	1.42	0.01	1.43	0.02
Honshu**	0.65	0.02	0.61	0.02	0.61	0.02
Izu*	2.17	0.01	1.74	0.01	1.76	0.01
Izu**	0.83	0.03	0.76	0.02	0.76	0.03
Bonin	1.09	0.01	0.97	0.01	0.97	0.01

### Comparison of Three Clustering Methods:



Three clustering methods generated similar clustering maps. The b-value analysis results are also similar. The clustering analysis of the JMA catalog is robust.

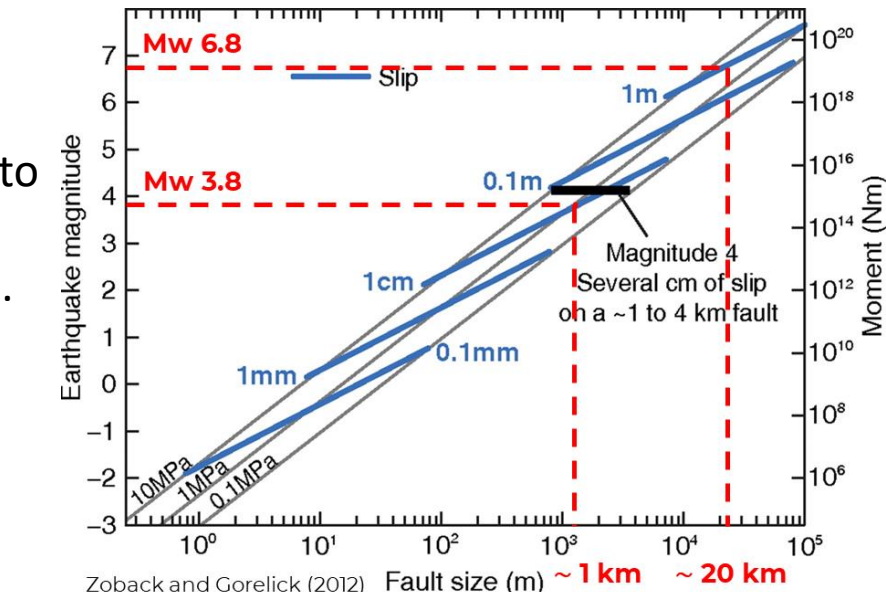
### b-value analysis with CMT and IRIS catalogs:



- IRIS and CMT catalogs show similar earthquake distributions
- Warm subduction zones show a change of b-values at Mw~6.8
- Cold Tonga subduction zone has a constant b-value of ~1.1

In JMA catalog, a new kink at Mw 3.8 was observed, in addition to the kink at Mw 6.5 in CMT and IRIS catalogs.

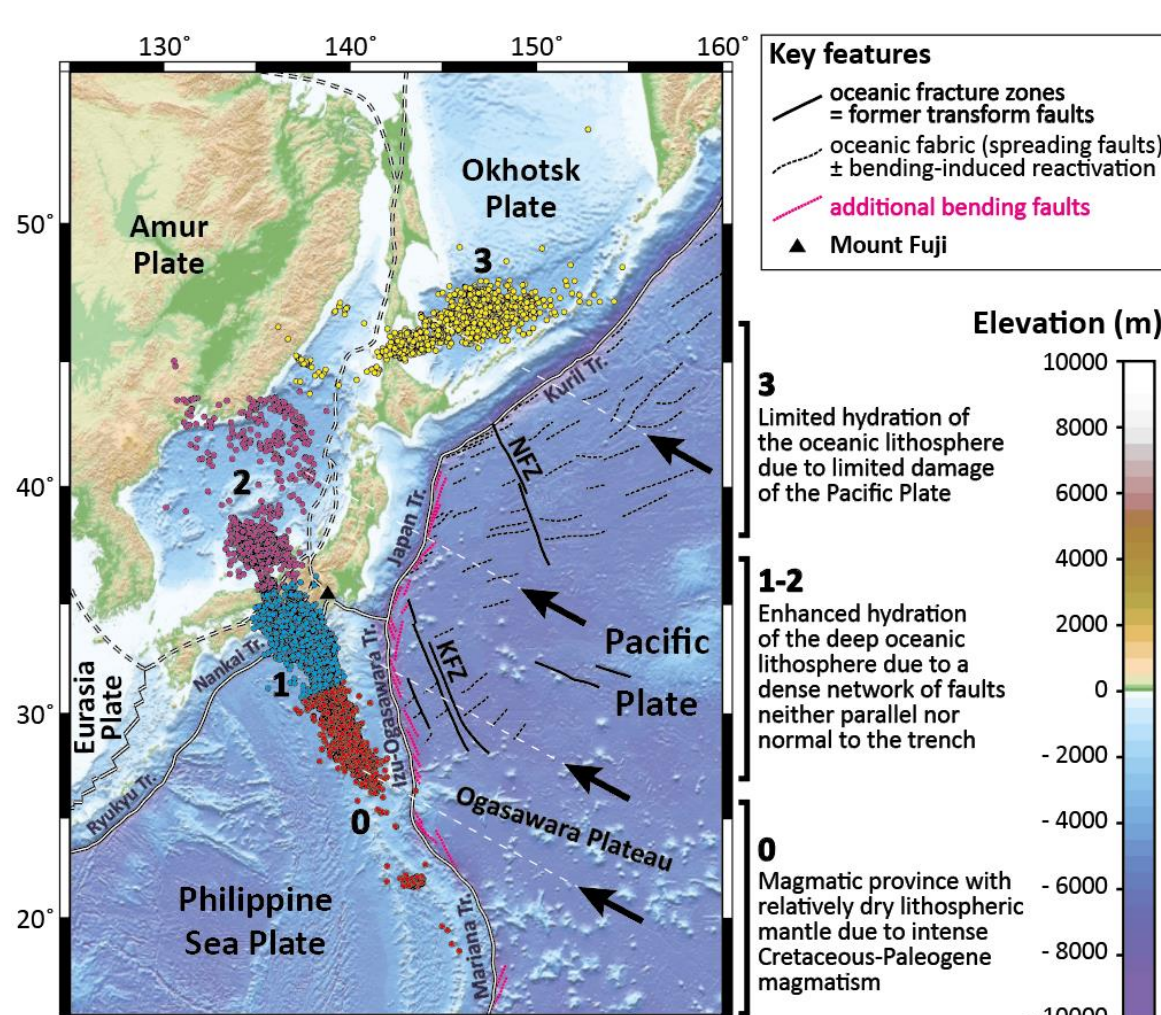
Two b-value Kinks indicate two different rupture dimension thresholds.



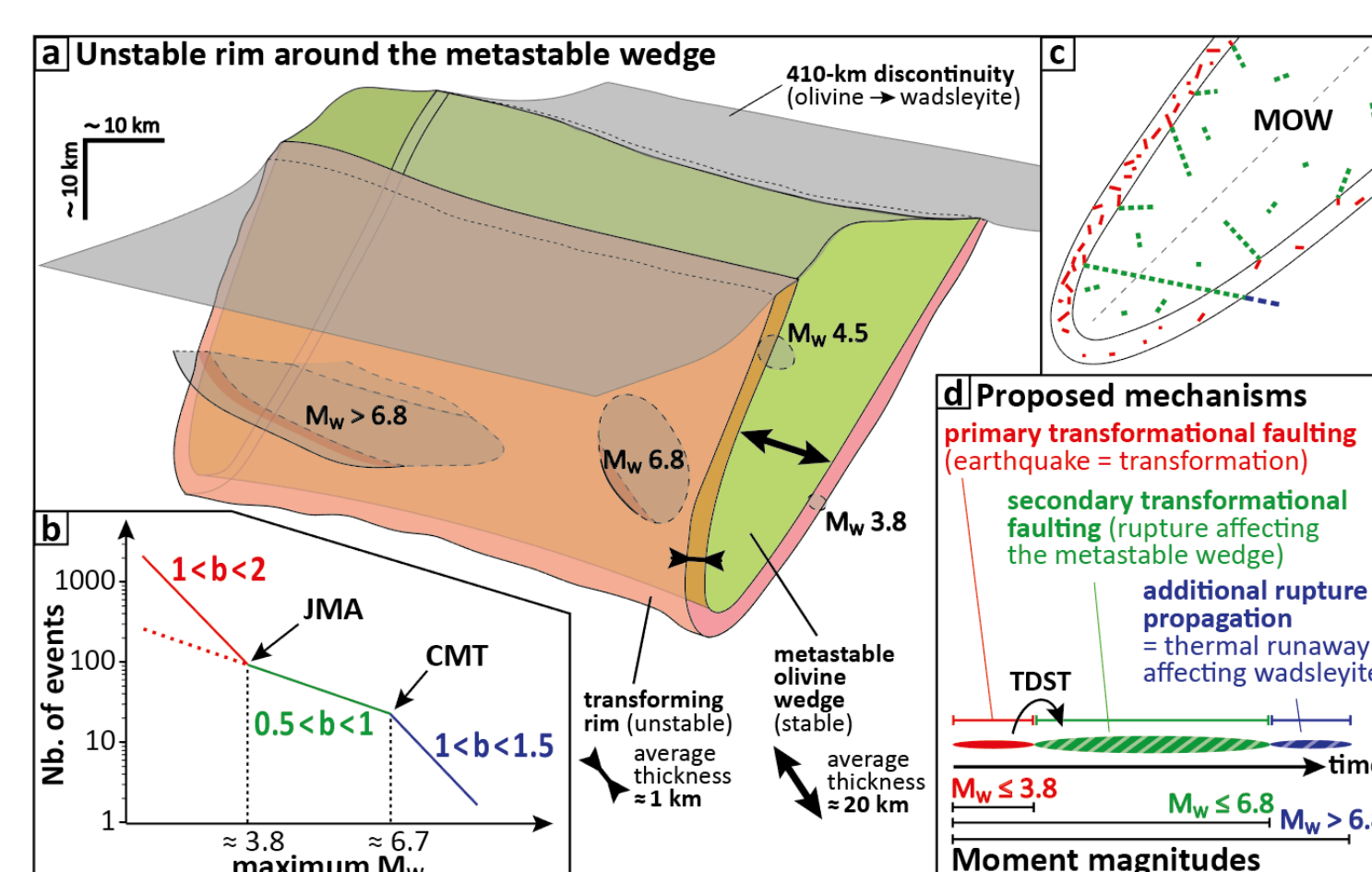
## Conclusion:

- Unsupervised machine learning approaches facilitate the unbiased clustering of deep-focus earthquakes from the JMA catalog.
- The b-value kink at Mw~3.8 provides strong evidence for phase transformational faulting triggering deep-focus earthquakes in an unstable rim of the metastable olivine wedge with a width of ~1 km.
- In the highly reactive halo, water acts as a catalyst for transformational faulting, resulting in higher b-values in the Honshu and Izu slabs for Mw < 3.8.
- We speculate that the b-value kink at Mw~3.8 can be observed in other subduction zones with similar tectonic environments and earthquake catalogs.

## Mechanisms for the b-value Kinks



Pre-Subducting Plate Hydration Affects the Water Abundance in the MOW Halo.



Deep-Focus Earthquakes Triggered in the Unstable Transforming Rim and can Propagate Into and then Outside the MOW. Water Acts as a Catalyst of Small Earthquakes in a Highly Reactive Halo of MOW.

## References

1. Zhan, Z. Gutenberg–Richter law for deep earthquakes revisited: A dual-mechanism hypothesis. *Earth Planet. Sci. Lett.* **461**, 1–7 (2017).
2. Ishii, T. & Ohtani, E. Dry metastable olivine and slab deformation in a wet subducting slab. *Nature Geoscience* **14**, 526–530 (2021).
3. Warner, M. & Sandri, L. A review and new insights on the estimation of the b-value and its uncertainty. *Annals of Geophysics* **46**(6) (2003).
4. Ferrand, T. P. *et al.* Dehydration-driven stress transfer triggers intermediate-depth earthquakes. *Nature Communication* **8**, 1–11 (2017).