

1 **Simulation of Spring Discharge Using Deep Learning, Considering the**
2 **Spatiotemporal Variability of Precipitation**

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15 **Key Points:**

16 A generative variational autoencoder is applied to augment precipitation data to improve a
17 LSTM network for spring discharge prediction.

18 Augmenting precipitation data improves learning generalization and predictive capability of
19 various deep learning models.

20 The generative variation autoencoder offers a novel solution to address data scarcity issue across
21 diverse research domains.

22 **Abstract**

23 Precipitation data collected from sparse monitoring stations in numerous karst catchment pose a
24 challenge for hydrologic models to accurately capture spatial and temporal correlation between
25 precipitation and karst spring discharge, hindering the development of robust simulation models.
26 To address this data scarcity issue, this study employs a coupled deep learning model that
27 integrates a variation autoencoder (VAE) for augmenting precipitation data and a long short-term
28 memory (LSTM) network for karst spring discharge prediction. The VAE contributes by
29 generating synthetic precipitation data through an encoding-decoding process. This process
30 generalizes the observed precipitation data by deriving joint latent distributions with improved
31 preservation of temporal and spatial correlations in the data. The combined VAE-generated
32 precipitation and observation data are used to train and test the LSTM for predicting the spring
33 discharge. Applied to Niangziguan spring catchment in northern China, our coupled VAE/LSTM
34 model demonstrated significantly higher predictive accuracy compared to a LSTM model using
35 only field observations. We also explored temporal and spatial correlations in the observed data
36 and the impact of different ratios of VAE-generated precipitation data to actual data on model
37 performances. Additionally, our study evaluated the effectiveness of VAE-augmented data on
38 various deep learning models and compared VAE with other data augmentation techniques. Our
39 study demonstrates that the VAE offers a novel approach to address data scarcity and uncertainty,
40 improving learning generalization and predictive capability of various hydrological models.

41

42 **Plain Language Summary**

43 Millions of people around the world use spring as their water sources. To protect these precious
44 springs, water resources managers need to have a good understanding on how spring discharges
45 change in the future under the stress of climate change and human activities. A common tool to
46 help improve this understanding is a computer model. A trustworthy computer model requires
47 plenty of quality data, which are unfortunately not available for many springs. To address this
48 data scarcity issue, we applied a computer-based learning technique, called variation autoencoder
49 (VAE), that learned the patterns of real-world data and generated data that complied with the
50 learned pattern. We then combined the generated data and real-world data to train a computer-
51 based learning model, called long short-term memory (LSTM) network, that is excellent in
52 simulating spring discharges. We tested our method using Niangziguan spring in the northern
53 China, demonstrating that adding VAE-generated data significantly improved the LSTM model.
54 In addition, we investigated the effectiveness of the VAE in improving other common models.
55 The study shows that our model is accurate in predicting spring discharges and VAE is a very
56 helpful tool in improving our model.

57

58 **1 Introduction**

59 Continuous and discontinuous carbonate rocks cover 15.2% of the global land surfaces
60 (Goldscheider et al.,2020). The karst aquifers formed by carbonate rock formations provide fresh
61 water for approximately 678 million or 9.2% of the world's population (Stevanović,2019).
62 Carbonate rocks cover 3.44 million km² of China territory (He et al.,2019). Many large karst
63 groundwater catchments feed big karst springs in northern China (Han et al., 2006). Over the
64 past decades, human activities and environmental problems have led to declining groundwater
65 levels or karst spring dry-ups in many regional karst groundwater catchments (Hao et al., 2009).
66 Therefore, accurate simulation and prediction of karst spring discharge is essential for the
67 sustainable management of water resources in the region.

68 To gain comprehension and accurate predictive capacity regarding these intricate
69 hydrological processes, Labat et al. (2000) developed a rainfall-runoff model that integrates
70 linear and steady-state rainfall-runoff models to identify and simulate the processes. Similarly,
71 Juki et al. (2009) introduced a conceptual rainfall-runoff model to estimate the components of
72 groundwater balance, including the dynamic catchment boundaries and the subsurface flow
73 influences within the catchment area. Notwithstanding the significant advancements achieved by
74 conventional hydrological models, limitations persist when confronted with spatiotemporal
75 nonlinearity and nonstationarity (Wunsch et al., 2022; Çallı et al., 2022).

76 The recent development of deep learning (DL) methods has made significant strides in
77 modeling the spatiotemporal behavior of rainfall-discharge processes. For example, Artificial
78 Neural Networks (ANNs) have been employed in investigating karst hydrological processes
79 (Yaseen et al., 2015) and have emerged as a prominent tool in hydrology. Wunsch et al. (2022)
80 utilized Convolutional Neural Networks (CNNs) to simulate the flow within three karst spring

81 catchment areas in the Alps and the Mediterranean region. Nevertheless, exploring time series
82 data, a vital component in hydrological research, has remained somewhat limited (Yin et al.,
83 2022). To address this gap, Song et al. (2022), Yin et al. (2022), and Zhou et al. (2022) have
84 implemented Long Short-Term Memory (LSTM) networks to simulate karst spring flow and
85 effectively manage time series data. Additionally, Cheng et al. (2021) conducted a comparative
86 evaluation of three machine learning methods (Multi-Layer Perceptron (MLP), LSTM, and
87 Support Vector Machine (SVM) to enhance our understanding of the mechanisms behind the
88 fluctuations in spring discharge in the Longzici spring's karst area and its relationship with
89 precipitation. Their research underscores that artificial neural networks are the preferred
90 approach for simulating and predicting karst spring discharge (Zhou et al., 2022; Gai et al.,
91 2023).

92 However, deep learning models often demand substantial training data for robust
93 performance (Shorten et al., 2021; Tang et al., 2022). In the context of hydrological process
94 studies, the high costs associated with data collection and the inherent spatial and temporal
95 randomness or stochasticity of the natural phenomena present formidable challenges (Dugdale et
96 al., 2022). In remote areas, data collection tasks can become even more arduous, thus
97 constraining a comprehensive grasp of hydrological processes (Mengistu et al., 2022). Nowhere
98 is this challenge more pronounced than in karst regions, where highly spatially variable
99 groundwater flow and the intricate dynamics of groundwater flow and spring discharge
100 complicate sampling and monitoring efforts (Hartmann et al., 2014). Consequently, the sparsely
101 sampled data brings significant challenges to apply deep learning in spring discharge simulation.

102 Some traditional methods have already been employed to deal with data sparsity in
103 hydrology. For example, Yeh et al. (2015) and Yeh et al. (2023) have summarized many

104 advances over the past decades in applying the Bayesian statistic concept to characterize aquifer
105 heterogeneity and to predict groundwater flow and solute transport processes in spatially variable
106 geologic media with sparse data. In particular, they promoted collecting more spatially non-
107 redundant data cost-effectively using hydraulic tomography to reduce uncertainty in predictions
108 (Yeh and Liu, 2000; Zhu and Yeh, 2005). Varouchakis et al. (2013) and Smith et al. (2021)
109 proposed interpolation techniques to enhance model performance with sparse data. Bruckmann et
110 al. (2020) employed sequential Gaussian simulation for the statistical modeling of groundwater
111 flow, enabling the quantification of overall uncertainty in sparsely sampled hard rock aquifers.
112 Sun et al. (2020) also applied it to meteorological observations or regions with limited or no data
113 on the Qinghai-Tibet Plateau by inversely evaluating the reconstructed precipitation with a
114 glacier-hydrology model. This approach contributes to catchment hydrological modeling and
115 forecasting research. Similarly, Grundmann et al. (2019) introduced an inverse surface
116 hydrologic modeling approach to reconstruct spatial-temporal rainfall patterns stochastically and
117 applied it to areas with data scarcity and poor catchment measurements. These methods,
118 however, typically rely on complex mathematical models governed by partial differential
119 equations and algorithms. Moreover, their limited adaptability to diverse hydrological data
120 domains and types hampers their cross-domain applicability and restricts flexibility and
121 scalability, posing challenges in addressing evolving hydrological research needs.

122 While the methods above have improved prediction accuracy in hydrology under sparse
123 sampling conditions, they often struggle to handle the large-scale datasets required by deep
124 learning models (Ghorbanidehno et al., 2020; Addor et al., 2020). Among the diverse branches
125 of deep learning, generative models such as the Variational Autoencoder (VAE), presented in
126 this study, can be precious when confronted with challenges like data scarcity, inadequate

127 sampling (Lin et al., 2023), and the intricacies of hydrological process modeling (Chen et al.,
128 2022). Specifically, this study addresses predicting spring discharge time series from spatially
129 limited observed precipitation time series over a large-scale karst catchment, where unknown
130 spatial and temporal variability of precipitations and hydrologic processes exist. In particular, a
131 deep-learning model that integrates a VAE and a Long short-term memory (LSTM)
132 network developed based on the spatiotemporal statistics of precipitation and discharge to predict
133 the most likely spring discharges and address their uncertainty in a karst catchment. This paper is
134 organized as follows.

135 (1) It first introduces the problems of predicting spring discharge at the Niangziguan
136 Springs karst catchment in China with sparse precipitation observation stations. (2) It then
137 investigates the spatial and temporal statistics of seven spatially sparse precipitation time series
138 to demonstrate that Bayesian statistics can generate many possible precipitation time series in the
139 latent space. These generated time series would represent those not observed at other parts of the
140 catchment and have the same spatiotemporal statistics as those observed. Besides, the study
141 examines the statistical relationship of the observed precipitation time series with the spring
142 discharge time series. Afterward, it uses their spatiotemporal relationships to analyze the most
143 likely discharge time series and address the uncertainty as the stochastic predictive and inverse
144 models in subsurface hydrology discussed in Yeh et al. (2015) and Yeh et al. (2023). (3) This
145 study proposes a deep-learning network (VAE/LSTM) model to avoid complex classical
146 governing surface and subsurface flow partial differential equations and characterization of the
147 hydraulic properties of the karst aquifer. (4) This study presents the results of the model's
148 application to the Niangziguan Karst catchment. It demonstrates the model's validity:
149 argumentation of more synthetic precipitation time series, capturing the precipitation's spatial

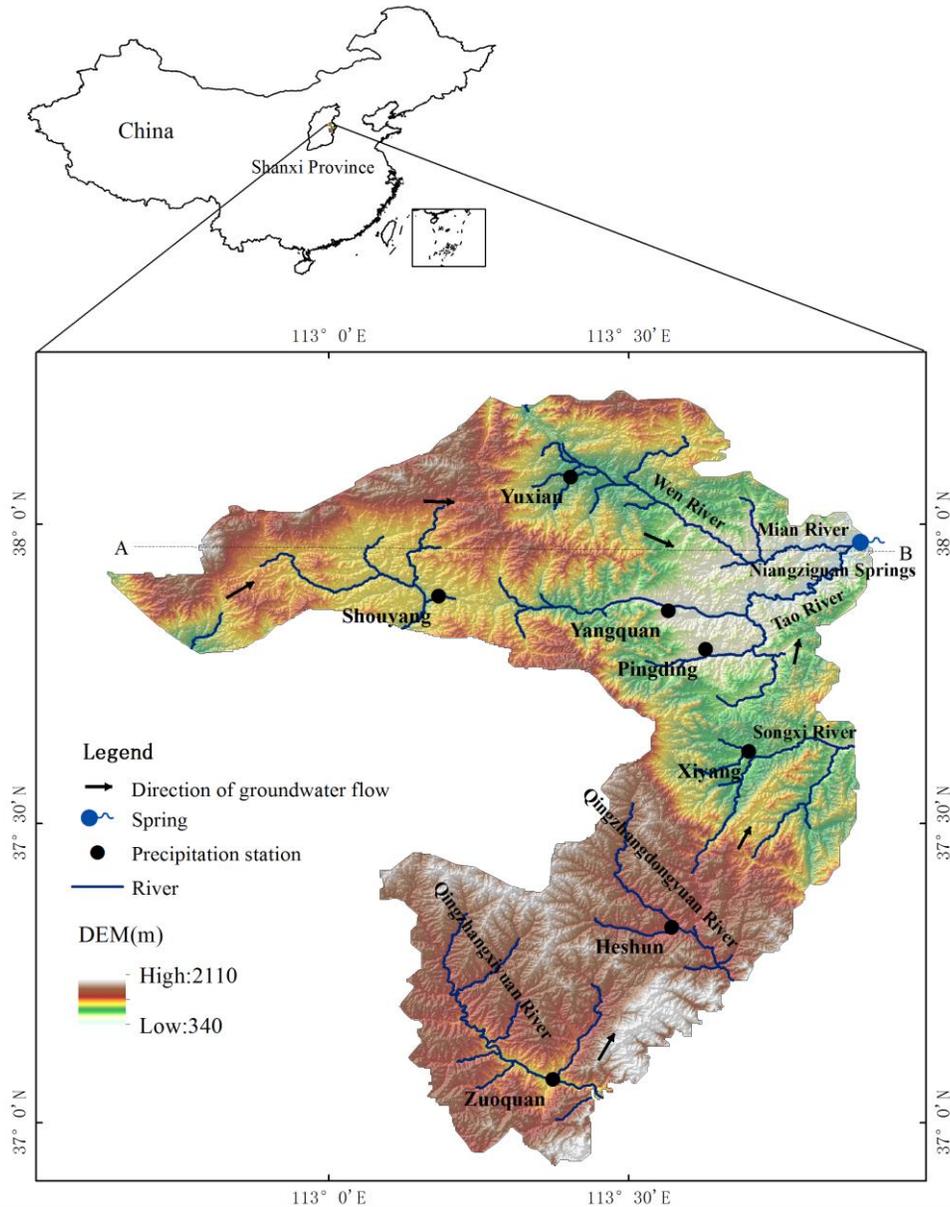
150 variability, improves the spring discharge prediction. (5) At last, this study discusses its scientific
151 insights.

152 **2 Statement of Problems**

153 The Niangziguan Springs composite, one of the largest karst springs in northern China, is
154 located in east Shanxi Province, China, with an annual average spring discharge of 9.35 m³/s
155 from 1959 to 2019. The Karst aquifer is an Ordovician carbonate aquifer, sandwiched by
156 Quaternary loess deposits, Permian shale, Carboniferous argillaceous limestone with coal seams
157 on top, and Cambrian dolomite on the bottom (Gai et al., 2023). The karst groundwater flows
158 eastward, and when groundwater meets with the low-permeable dolomite strata of the Cambrian
159 at the Mian River valley, it perches on the surface, and Niangziguan Springs occurs (Figure 1).

160 The landforms of the Niangziguan Springs catchment are rough hilly terrains and gentle
161 sloping river terraces, where the elevation ranges from 2149m to 362m above mean sea level
162 (MSL). Precipitation is the primary aquifer recharge source, with an annual average precipitation
163 of 534.6 mm from 1959 to 2019 (Gai et al., 2023).

164 Before 1971, the Niangziguan Springs catchment was a remote rural mountainous area
165 with a well-developed river water system. Residents mainly used river and spring water for their
166 water supply. Karst groundwater was not developed and remained in natural condition during
167 that time. Although the residents utilized water from the rivers and streams connected to the
168 subsurface groundwater, widespread pumping development of the karst aquifer did not occur.
169 That is, the impacts of human activities on groundwater were negligible (Hao et al., 2016; Song
170 et al., 2022).



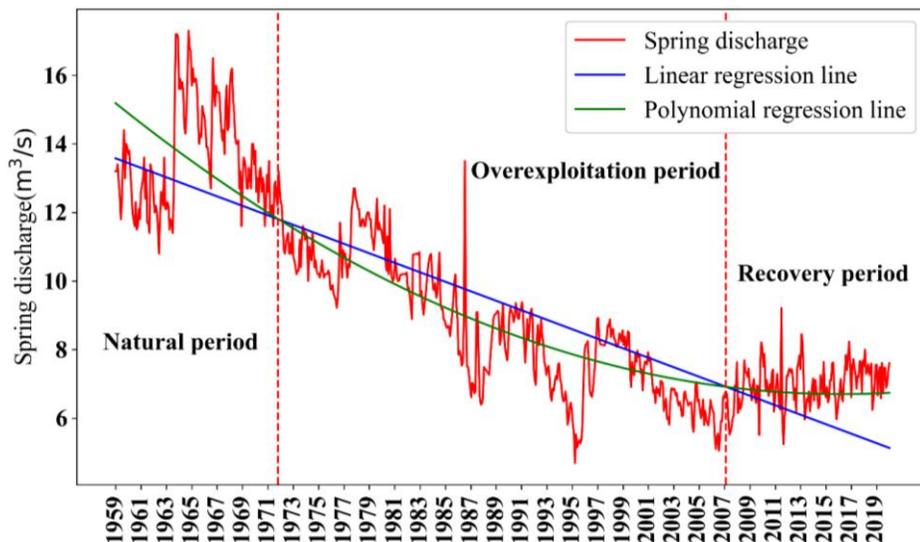
171
 172 **Figure 1.** Niangziguan Springs catchment, China.

173 With China's reforming and opening up from the beginning of the 1970s, regional
 174 economic development and population growth increased. The Niangziguan Springs catchment
 175 has become one of the national heavy industrial zones for coal mining, power generation, and
 176 metallurgy. Specifically, after the early 1970s, groundwater of the catchment began to be
 177 developed for industrial, municipal, and irrigation uses. The regional economic and social

178 development largely influenced karst groundwater in the Niangziguan Springs catchment and the
 179 Niangziguan Spring discharge accordingly.

180 Figure 2 displays the monthly spring discharges measured at the Niangziguan Springs
 181 gauging station in Mian River (point B in Figure 1) from 1959 to 2019. The discharge records
 182 exhibit a two-scale variability, a large-scale declining trends from 1959 to 2019, depicted by the
 183 polynomial and linear regression lines, and local-scale variability at the monthly level. As
 184 illustrated in the figure, the points of intersection between the linear regression line and the
 185 polynomial regression line occur at two distinct time points, namely 1971.10 and 2006.12. Based
 186 on the two intersecting points, we divide the discharge records into the nature period (1959.1-
 187 1970.12), the overexploitation period (1971.1-2006.12), and the recovery period (2007.1-
 188 2019.12). This segmentation method comprehensively analyzes and compares spring discharge
 189 characteristics in these distinct phases while exploring potential patterns and trends in karst
 190 spring spatiotemporal variation.

191



192

193 **Figure 2.** Spring discharge data partition of Niangziguan spring from 1959 to 2019.

194

195 From 1971 through 2006 (the overexploitation period), the region underwent rapid
 196 development due to China's economic reform and open-door policy. Due to a substantial demand
 197 for groundwater, spring discharge exhibited a significant declining trend (An et al., 2020; He et
 198 al., 2019).

199 Post-2006, influenced by China's sustainable development strategy, local authorities
 200 actively promoted industrial transformation (Liu et al., 2020). As a result, natural resource
 201 consumption and groundwater exploitation decreased, leading to a gradual recovery in spring
 202 discharge, and we call this period the recovery period.

203 Precipitation over the catchment is the primary source of the spring discharge. Figure 3
 204 illustrates the monthly precipitations as a function of time (from 1959 to 2019) recorded at seven
 205 meteorological stations located at Yuxian, Shouyang, Pingding, Xiyang, Heshun, and Zuoquan
 206 counties, and Yangquan city (i.e., the black dots in Figure 1) (Gai et al., 2023). These figures
 207 exhibit the variability of the monthly precipitation values, which do not exhibit the trend in the
 208 discharge in Figure 2. Absence of the trend confirms our interpretation of groundwater usage's
 209 influence on the spring discharge due to the catchment development.

210 The mean values and standard deviations of the precipitation corresponding to Figure 3
 211 are also listed in Table 1.

212
 213 **Table 1.** The means and standard deviations of the monthly precipitation time series (1959-2019)
 214 at the seven stations.

	Yangquan	Pingding	Yuxian	Shouyang	Xiyang	Heshun	Zuoquan
Mean(mm)	45.2	44.8	46.0	41.0	45.5	45.6	43.7
Variance	3493.9	3426.7	3388.1	2521.2	3626.4	3273.3	2888.4

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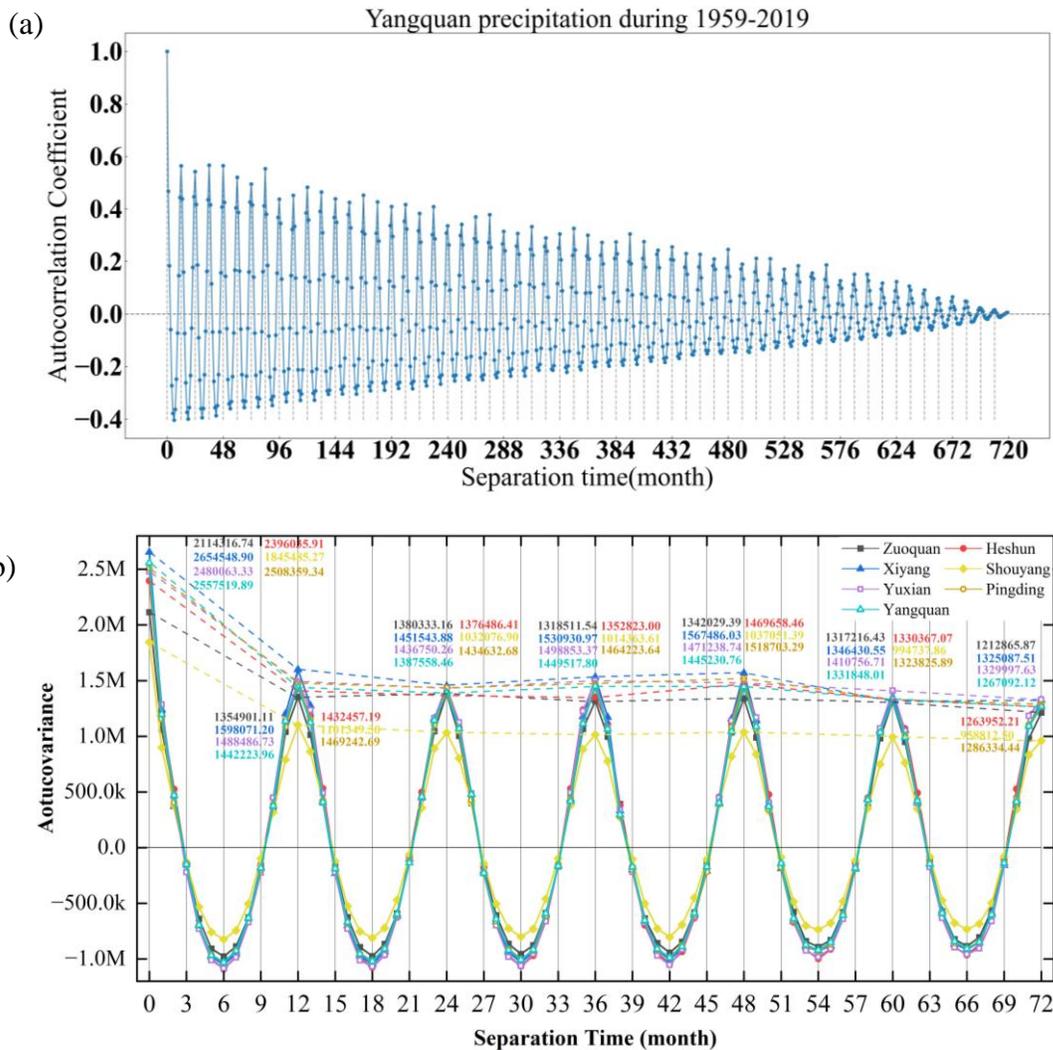


217
 218 **Figure 3.** The monthly precipitations as a function of time (from 1959 to 2019) recorded at
 219 seven meteorological stations.

220
 221 As indicated in Table 1, the mean values of the monthly precipitations (1959-2019) at the
 222 seven stations are almost the same. Their standard deviations are close, indicating a slight spatial
 223 variation in the monthly precipitation. However, the precipitation records manifest a periodic
 224 behavior: heavy rainfalls in the middle of every year (the temporal variability).

225 Figure 4a illustrates the temporal autocorrelation of the recorded precipitation time series
 226 (from 1959 to 2019) at Yangquan station. The maximum or minimum autocorrelation values
 227 decrease as the lag (separation) time increases. The autocorrelation behaviors of the precipitation
 228 time series at the other six stations have similar patterns, showing the same 12-month periodicity

229 (Figure 4b). This periodicity implies that if this month's precipitation is higher than the mean, the
 230 precipitation 12 months later will likely be higher than the mean or vice versa. The negative
 231 covariances indicate that if a given month's precipitation value is higher than the mean, the
 232 precipitation separated by a time lag between 3 to 9 months will be below the mean value of the
 233 entire record (Table 1). Such a periodic autocorrelation suggests that the precipitations over the
 234 catchment lasted less than a month. As a result, the monthly accumulated precipitations at
 235 different locations over the catchment do not exhibit significant deviations.

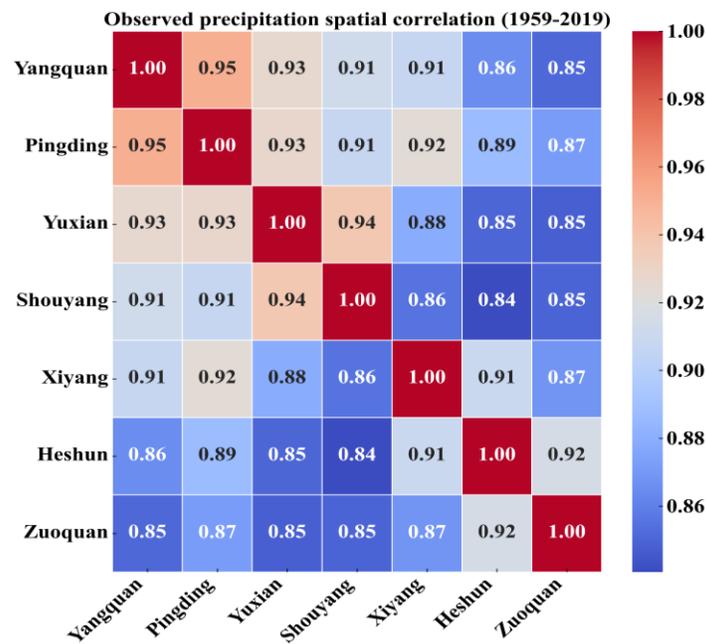


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239 **Figure 4.** (a) illustrates the autocorrelation of the precipitation from 1959 to 2019 at Yangquan
 240 station. (b) shows the autocovariance of the monthly precipitation perturbations as a function of
 241 time recorded at seven meteorological stations (1959 to 1964).

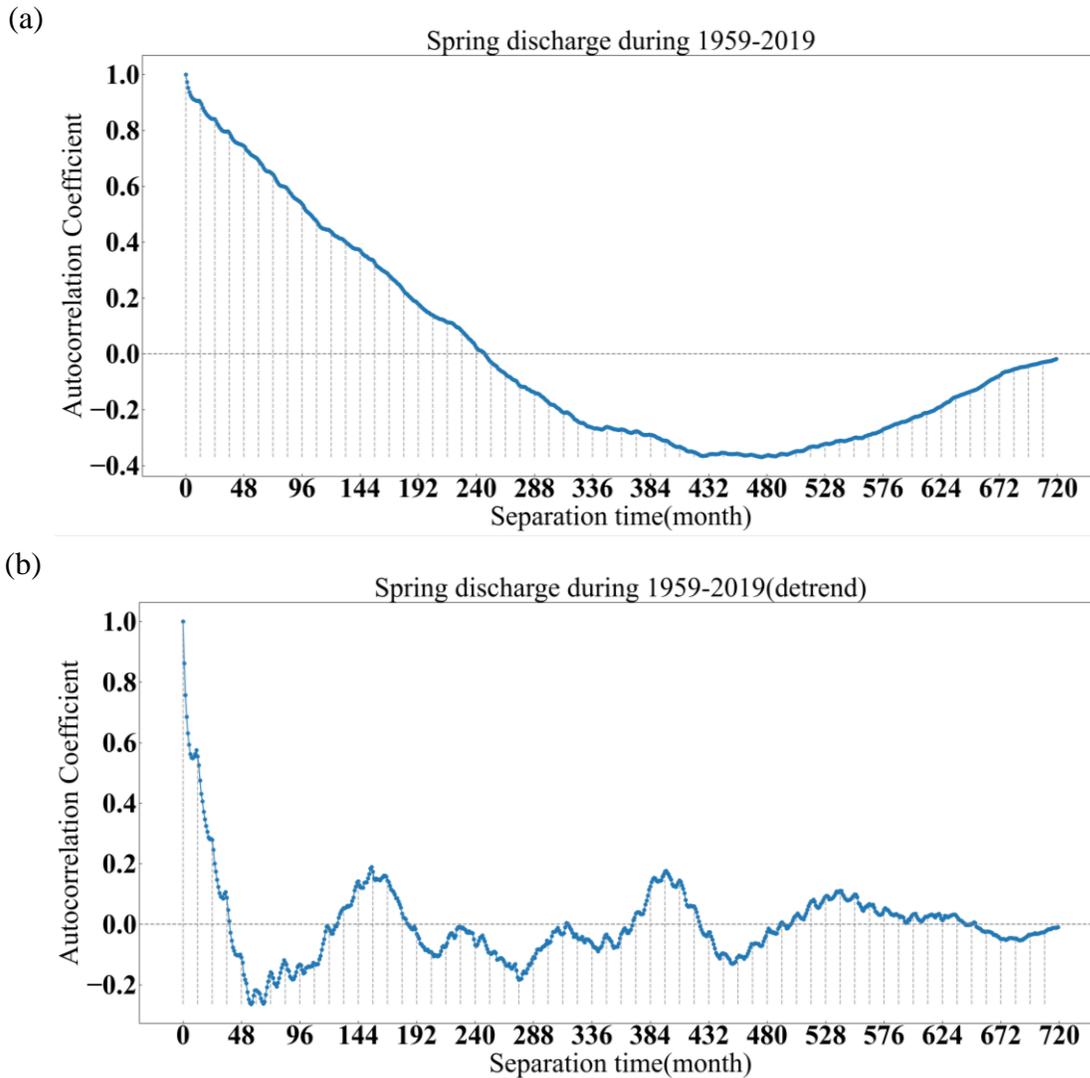
242 Figure. 4b shows that the time series at the seven stations behave similarly. The similarity
 243 is expected since the time series are monthly precipitations, which integrate the spatial variation
 244 of the precipitation over the time intervals of less than a month. However, they are slightly
 245 different, unveiling spatial variations in the precipitation over the entire catchment. This spatial
 246 variation is also confirmed by Figure 5, which plots the correlation values of the recorded
 247 precipitation among the seven stations, revealing that the precipitations are correlated well
 248 between adjacent stations and less with far away stations.



249 **Figure 5.** The correlations between the precipitation data recorded at the seven stations illustrate
 250 their spatial similarity and variation.
 251

252 We also carried out the autocorrelation analysis for the spring discharge time series in
 253 Figure 2. The autocorrelation of the spring discharge without detrending is shown in Figure 6a.
 254 and that of the discharge after removing the polynomial trend (Figure 2) is illustrated in Figure
 255 6b, which exhibits some periodicities at large and small scale. The small-scale variations have
 256 one year's periodicity, corresponding to the above mentioned precipitations. It suggests that an
 257 appropriate cross-correlation analysis of the precipitation and spring discharge data must use the

258 detrended spring discharge data. Table 2 lists the means and standard deviations of the spring
 259 discharge time series (1959-2019) before and after detrending. Figures 6a and 6b and Table 2
 260 indicate that human activity heavily influences spring discharge time series during the over-
 261 exploration period.



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265 **Figure 6.** Auto-correlation of spring discharge. (a) non-detrended. (b) detrended data.

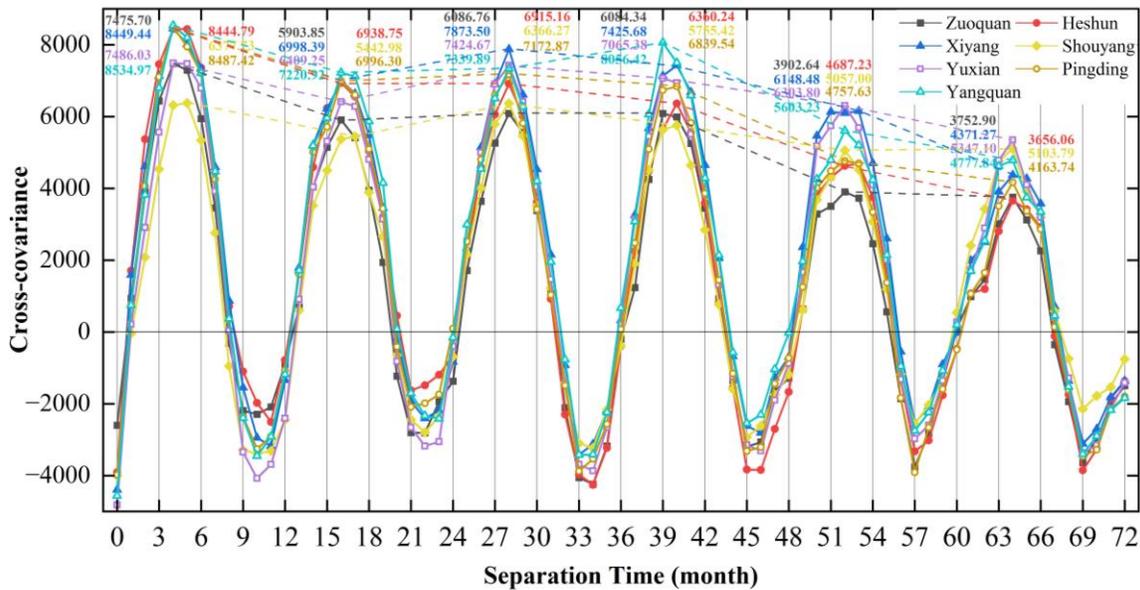
266 **Table 2.** Means and variances of non-detrended and detrended spring discharge data.

Spring discharge	Non-detrended	Detrended
Mean (mm)	9.35	0
Variance (mm ²)	7.99	1.49

267 The analyses in Figures 3, 4, 5, and 6 suggest that the precipitation over the catchment
 268 and the spring discharge time series can be conceptualized as spatiotemporal stochastic processes
 269 (Preciley, 1979) or latent processes (AI jargon): they are random but correlated in space and
 270 time.

271 Since the precipitation is the primary source of the spring discharge, relationships
 272 between the precipitation and discharge data must exist. As such, we instigated the cross-
 273 covariance between the discharge and the precipitation at each of the seven stations as a function
 274 of separation time in Figure 7. The discharge time series (1959-2019) were detrended, and the
 275 residuals were then analyzed.

276



277 **Figure 7.** The cross-correlation between the discharge (detrended) and the precipitation at each
 278 of the seven stations as a function of separation time (month).
 279

280 The cross-covariance in Figure 7 shows a periodicity of almost 12 months as the
 281 autocorrelation of the precipitation time series (after human impacts were removed), suggesting
 282 that the precipitations closely control the spring discharge. Notice that the maximum cross-
 283 correlation occurs four or five months after the precipitation perturbation greater than the mean

284 value. These four or five months may present the average travel time for the precipitation to
285 reach the spring discharge location.

286 The above discussion and Figure 1 demonstrate that the catchment covers an area with
287 significant topographic variations, implying precipitations likely vary in time and space, not
288 captured by the monthly cumulative precipitation data from the seven stations. The problems of
289 sparse measurement and spatiotemporal variability processes are not new. Many scientists have
290 employed stochastic approaches to deal with this issue in hydrology. For instance, Yeh et al.
291 (2015) and Yeh et al. (2023) introduced the approach that conceptualizes the spatial variation of
292 hydraulic properties in geologic media as a spatial stochastic process. Given some observed
293 values, the process is exemplified by a joint posterior distribution with the mean, variance, and
294 autocorrelation function as a function of correlation scales.

295 Within this probability distribution, many possible heterogeneous aquifer parameters
296 exist and can be used to simulate the statistically most likely flow and transport processes and to
297 derive the associated uncertainty due to the effects of unknown heterogeneity missed by
298 sampling. This approach is called Monte Carlo (MC) simulation in hydrology. This approach,
299 however, requires solving 3-D partial differential equations governing the surface and subsurface
300 flow with many parameters, boundaries, and initial conditions. Such an approach is a complex
301 numerical simulation task.

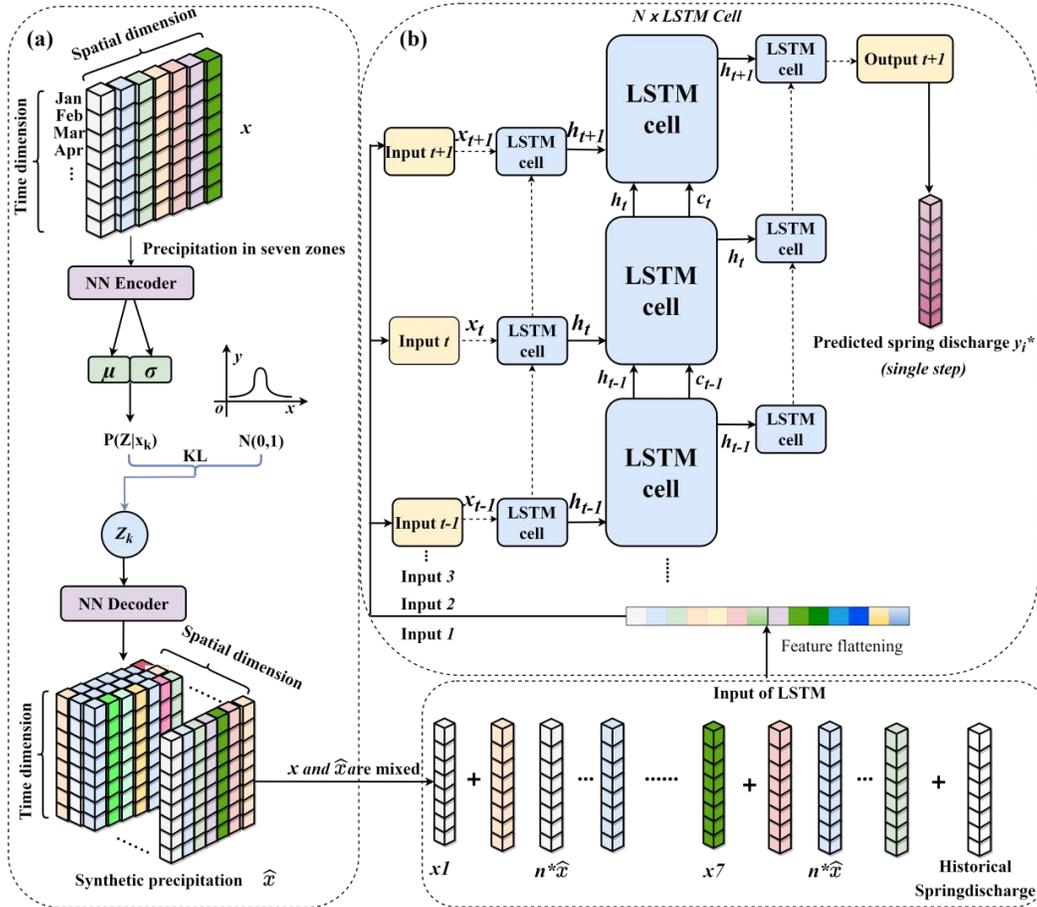
302 Of course, this study could have followed the stochastic MC simulation approach, but it
303 faces many difficulties. An alternative is to use a deep-learning machine approach, skipping
304 solving 3-D partial differential equations. However, it needs to deal with sparsely distributed
305 temporal varying precipitation information.

306 For this reason, this study proposes a new deep-learning network model combining VAE
307 and LSTM to predict precipitation-driven spring discharge. Figure 8 displays the architecture of
308 the proposed network. VAE is a data generation model that can generate new data of similar
309 spatiotemporal statistics (mean, covariance, and probability distribution) from the input data via
310 the encoding and decoding mechanism in VAE. On the other hand, LSTM is a model that
311 exploits spatiotemporal cross-correlation statistics between precipitation and spring discharge
312 data to predict spring discharge at different times.

313 **3 Variational Autoencoder (VAE) and Long Short-Term Memory (LSTM) network: VAE** 314 **/ LSTM model**

315 3.1 Variational AutoEncoders (VAE)

316 The VAE is a data-generative model that consists of two parts: an encoder and a decoder.
317 The encoder derives latent posterior distributions of input data by neural networks and samples
318 from the distributions to obtain latent samples. The decoder converts the latent samples back to
319 the data that have similar statistical features with input data by neural networks. Different from
320 MC simulation, this process is controlled by the neural network parameters trained by the input
321 data. Details are available in Supporting Information S1 (Figure S1).



322

323 **Figure 8.** The architecture of the VAE/LSTM for precipitation-driven spring discharge
 324 prediction. (a) is the module of the VAE for new precipitation data generation that has similar
 325 spatiotemporal statistics with the observed precipitation. (b) is the module of LSTM for spring
 326 discharge prediction using the observed precipitation, synthetic precipitation and historical
 327 spring discharges.

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The VAE encoder is conditioned on the observed precipitation from the seven stations to
 derive seven latent posterior probability distributions with their means and covariances.
 Specifically, let X_{ik} be the precipitation data set of all the i -th month at the k observation station,
 where $i=1,2,\dots,12$, $k=1,2,\dots,7$ (representing 12 months of the observed precipitation data in seven
 zones of Niangziguan Springs catchment). The encoder maps X_{ik} to a latent state distribution
 $P_{\theta_E}(Z_{ik} | X_{ik})$ with the mean u_{ik} and the variance σ_{ik}^2 , which is the posterior probability distribution

334 of $P(X_{ik})$. θ_e is the parameter matrix of the encoder neural network associated with all zone
 335 precipitation. Thus, the latent distribution is a joint posterior probability distribution of the
 336 observed precipitation data, which can characterize other unknown locations by mean, variance,
 337 and covariance (i.e., spatiotemporal relationship between the precipitations at different locations
 338 in the entire catchment). Let z_{ik} be the sample of $P_{\theta_e}(Z_{ik} | X_{ik})$. Then the VAE decoder converts z_{ik}
 339 to a new precipitation data, \hat{x}_{ik} as $P_{\theta_d}(\hat{x}_{ik} | z_{ik})$, where θ_d is the parameter matrix of the decoder
 340 neural network.

341 The VAE, in essence, conceptualizes the multi-scale spatiotemporal variable precipitation
 342 as stochastic processes, similar to the stochastic conceptualization of multi-scale heterogeneous
 343 geologic media (Chapter 4 in Yeh et al., 2015). Based on this process, the VAE generates many
 344 possible synthetic data, representing those spatiotemporal varying precipitations not observed at
 345 the seven stations (similar to the above MC simulation). This approach is the so-called "data
 346 augmentation" in the machine learning field.

347 3.2 Long Short-Term Memory (LSTM) Network

348 As sufficient spatially varying precipitation data over the catchment becomes available,
 349 next, the deep learning network of LSTM uses 12 consecutive months of the observed
 350 precipitation data in seven zones $[X]_{12 \times 7}$, and their synthetic precipitation $\hat{X}_{12 \times 7 \times M}$ (M is the
 351 number of synthetic data of each zone) as well as the observed spring discharge data Y_{12} from the
 352 past 12 months to exploit their spatiotemporal cross-correlations features to predict the spring
 353 discharge in the following months. Again, this is analogous to the conditional stochastic
 354 approaches of cokriging or SLE (Yeh et al., 2005).

355 LSTM has been widely employed for modeling time series data and proved well-suited
 356 for hydrological data, especially in Karst regions, for predictive tasks (Song et al., 2022). The
 357 core innovation of LSTM incorporates memory cells and gate mechanisms. Memory cells enable
 358 the network to store and retrieve long-term memory information, while gate mechanisms oversee
 359 and control the data read and write operations of these memory cells. These mechanisms are
 360 similar to stochastic hydrology's spatial and temporal correlation concepts (i.e., data are
 361 correlated over short or long temporal or spatial distances, depicted by the auto or cross-
 362 correlation, Yeh et al., 2015; Yeh et al., 2023). The LSTM process, controlled by its network
 363 parameters θ_{LSTM} of all the gates, acquires high-dimensional positively or negatively correlated
 364 spatiotemporal features of spring discharges for all data as $F_{\theta_{LSTM}}$. Finally, a nonlinear calculation
 365 of $F_{\theta_{LSTM}}$ by a fully connected neural network outputs the spring discharge for the following month
 366 or months denoted as Y^* , which can be given as

$$367 \quad Y^* = C_{\theta_{FC}}(F_{\theta_{LSTM}}), \quad (1)$$

368 where θ_{FC} is the parameter matrix of the fully connected neural network. Details are available in
 369 Supporting Information S2 (Figure S2).

370 In our model, the VAE and LSTM are coupled. The output of VAE, the observed
 371 precipitation, and spring discharges are fed to the LSTM to predict the spring discharge. The
 372 initial parameters of θ_E , θ_D , $F_{\theta_{LSTM}}$ and θ_{FC} are zero and are iteratively updated by the coupled
 373 model training until some criteria about the agreement between the observed and synthetic
 374 precipitation and the observed and simulation spring discharge are met. Afterward, the algorithm
 375 and the optimal parameters were verified through the testing (verification) phase, where the
 376 observed discharge time series were not used in the training.

377 Unlike traditional statistical methods, our approach exploits the results of synthetic
 378 precipitation and spring discharge prediction work together to update the model's parameters.
 379 This update enables LSTM to explore spatiotemporal variation cross-correlation features
 380 between precipitation and spring discharge while enabling VAE to generate more realistic spatial
 381 variation precipitation. That is, it can leverage the cross-correlation between spring discharge and
 382 precipitation to generate more reasonable data instead of relying solely on the statistical process
 383 of the precipitation itself. The detailed algorithm of VAE and LSTM can be seen in the
 384 Supporting Information S1 and S2 (Figures S1 and S2).

385 3.3 Evaluation Metrics

386 To assess the predictive accuracy of the model, we employed the following evaluation
 387 metrics: root mean square error (RMSE), mean absolute error (MAE), mean absolute percentage
 388 error (MAPE), and Nash-Sutcliffe efficiency coefficient (NSE). They are defined below:

$$389 \quad RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - y_i^*)^2} \quad (2)$$

$$390 \quad MAE = \frac{1}{N} \sum_{i=1}^N |y_i - y_i^*| \quad (3)$$

$$391 \quad MAPE = \frac{1}{N} \sum_{i=1}^N |(y_i - y_i^*) / y_i| \times 100\% \quad (4)$$

$$392 \quad NSE = 1 - \frac{\sum_{i=1}^N (y_i - y_i^*)^2}{\sum_{i=1}^N (y_i - \bar{y})^2} \quad (5)$$

393 The y_i in the above equations represents the observed spring discharge value, \bar{y} is the
 394 mean of the observed discharges, the y_i^* is the predicted, and N is the number of values used.

395 **4 Results**

396 4.1 Model Implementation

397 This study employs the proposed coupled model of VAE/LSTM to predict spring
398 discharge. Since the parameters of the neural network model control its performance, parts of the
399 observed data are used for the model training to obtain the optimal parameters, and the remaining
400 is used for model testing (verification).

401 In this paper, the ratio of the training data to the testing data is 2:1 for each divided period
402 (i.e., nature, overexploitation and recovery periods in Figure 2) as shown in Figure 2.
403 Specifically, during the nature period, the training phase used the time series from 1959.1 to
404 1966.12, and the testing phase employed data from 1967.1 to 1970.12. During the
405 overexploitation period, 1971.1- 1994.12 is the training phase, 1995.1-2006.12 is the testing
406 phase. For the recovery period, 2007.1-2014.12 is the training phase, 2015.1-2019.12 is the
407 testing phase.

408 In addition, the LSTM time step used in this paper is 12 months (Song et al., 2022),
409 which is consistent with 12 month periodicity in the autocorrelation of precipitation data (Figure
410 4) and the cross-correlation between the precipitation and spring discharge (Figure 7). In other
411 words, the model continuously employs cross-covariance of the past 12 months of precipitation
412 and spring flow to predict the next month's spring discharge.

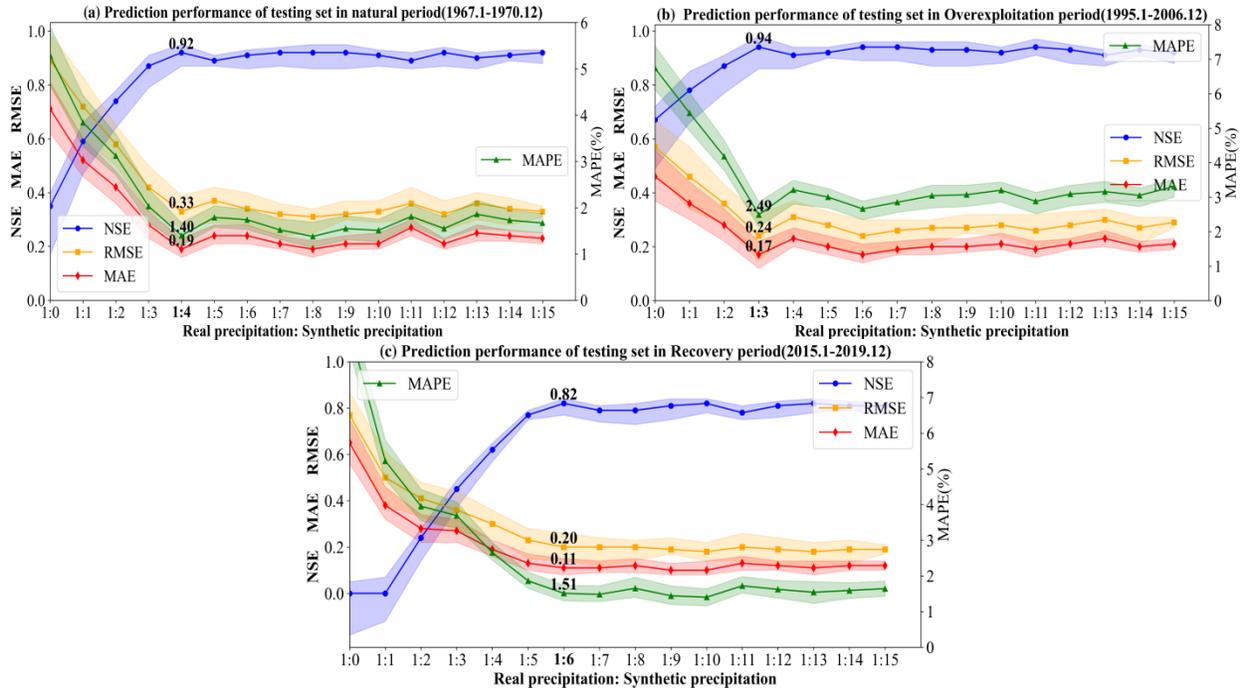
413 More synthetic precipitation data reduces the uncertainty of spatial precipitation
414 distribution, which can improve the ability of the LSTM to capture the cross-correlation features
415 between precipitation and spring discharge. However, this will lead to higher data dimension
416 calculations and reduce the generalization ability of the LSTM to diverse data during the testing
417 phase. Therefore, it systematically increases the proportion of synthetic data during the training

418 process to determine the optimal numbers of the synthetic data in each period. This incremental
419 approach enables the model to grasp precipitations' spatiotemporal characteristics over the
420 watershed progressively.

421 4.2 Effectiveness of VAE/LSTM model for Single-Step Spring Discharge Prediction

422 Figures 9a, b, and c show the evaluation performance of single-step spring discharge
423 prediction with various proportions of the synthetic of the three periods in the testing phase.
424 These figures underscore the influence of additional spatiotemporal precipitation data on the
425 model's predictive capabilities. As shown in the figure, VAE/LSTM model yields better-
426 predicted spring discharges as the proportion of synthetic precipitations gradually increases,
427 which reflects that the model is exposed to an expanding pool of spatiotemporal varying
428 precipitation data, enabling it to acquire broader spatiotemporal precipitation attributes.
429 Furthermore, the predicted performance becomes stable when the proportion increases to a
430 certain extent. Although there are differences in the cross-covariance between precipitation and
431 spring discharge in different zones (as shown in Figure 7), when a certain amount of spatial
432 precipitation data is employed, LSTM can capture their relevant features well, implying that the
433 ergodic condition is reached.

434 Figure 9 displays the single-step spring discharge prediction. It shows that the evaluation
435 of NSEs of our model in the three periods can reach 0.92, 0.94 and 0.82, respectively, indicative
436 of the excellent performance of our model. It is worth noting that the ratios of synthetic data that
437 make the prediction optimal are different for different periods: 7:28 in the natural period, 7:21 in
438 the overexploitation period, and 7:42 in the recovery period. Many reasons could contribute to
439 this variation of the three periods. One likely reason is that human intervention has disrupted the
440 natural correlation between precipitation and spring discharge.



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442

443 **Figure 9.** Performance evaluation of LSTM Model with VAE data augmentation at different data
 444 ratios. The ratio means the amount of data by which one precipitation data is enhanced.

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Figure 9 also illustrates that model performance slightly deteriorates when the proportion of synthetic precipitation becomes high. The slight deterioration may be due to insufficient experiments. This result may imply that LSTM becomes overly sensitive to specific details and noise. Theoretically, more synthetic precipitations with corrected spatiotemporal statistics should yield stable predictions.

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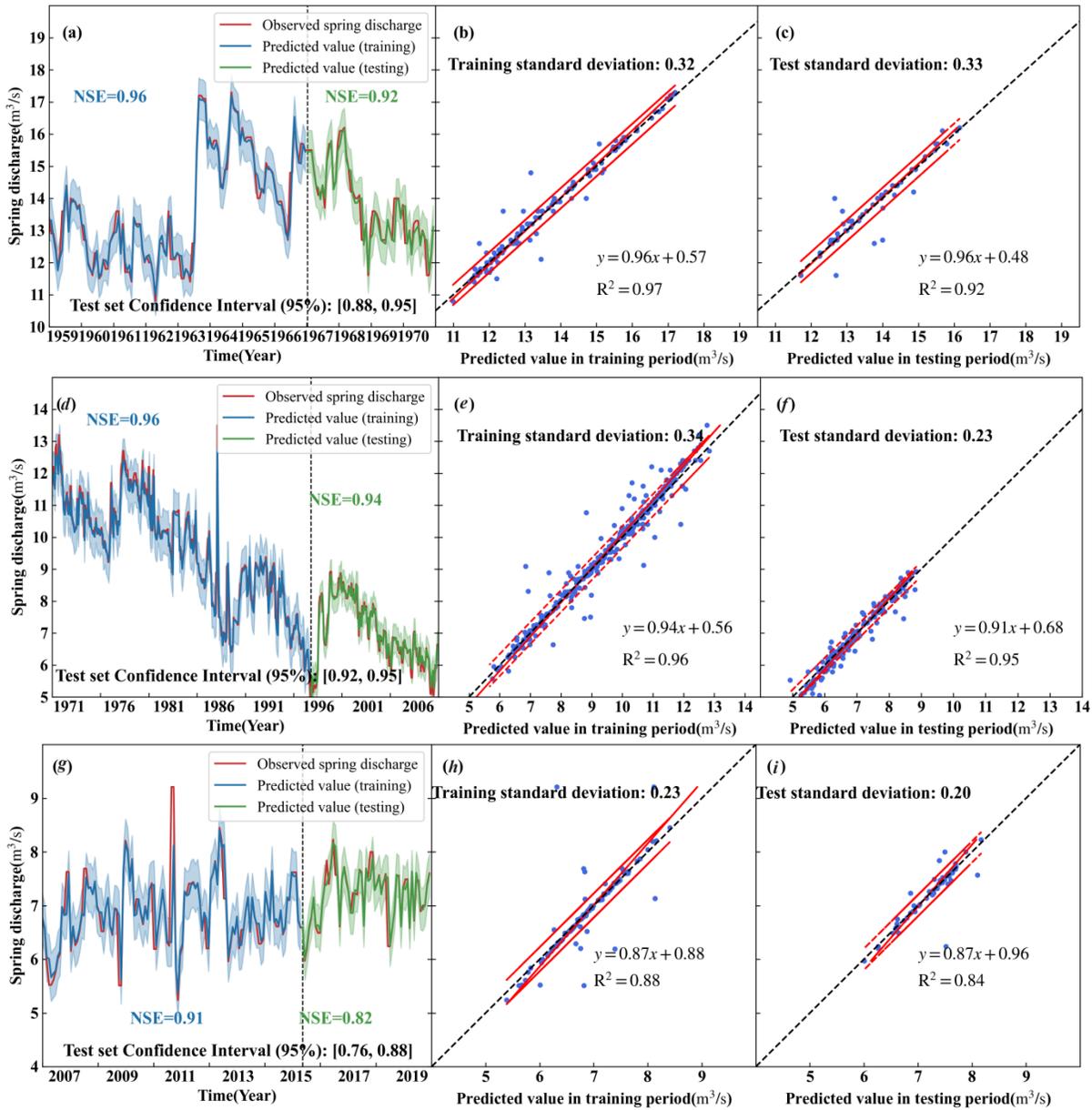
Figure 10 visually compares the observed and the single-step predicted spring discharge in the training and testing phases for the three periods. Figure 10a-c are the results of the natural period (1959.1-1970.12). Figure 10d-f are the results of the overexploitation period (1971.1-2006.12). Figure 10g-i are the results of the recovery period (2007.1-2019.12). In these figures, the red curve is the observed spring discharge, the blue curve denotes the predicted spring discharge during training, and the green curve represents the predicted spring discharge in the testing phase. The scatter plots compare the observed and predicted discharges in the training

457 and testing data set. The shaded area (in Figures 10a, 10d, and 10g) and the area between the red
458 lines in the scatter plots are the predictions where their NSEs are with a 95% confidence interval.
459 That means that when evaluating the model, we can have a 95% confidence level to believe that
460 the real NSE value falls within the calculated confidence interval. This range provides a
461 statistical measure of the model's performance and helps to determine the model's credibility
462 under different conditions.

463 These figures indicate that the NSEs of training for the three periods are all higher than
464 0.9. Further, for the testing phase, the NSEs of the three periods reaches 0.92, 0.94, and 0.82,
465 respectively. The R^2 of the scatter plots comparing predicted and observed spring discharge of
466 the three periods for the training phase are 0.97, 0.96, and 0.88. They are 0.92, 0.95, and 0.84 for
467 the testing phase. These results demonstrate outstanding predictive performance during the
468 testing periods. For the different periods, these results show some differences. Such differences
469 arise because these results depend on LSTM's training, which is influenced by the amount of
470 observed data in each period and the differences in data distribution between the testing and
471 training phases. As shown in Figure 2, the amount of observed data during each period and the
472 distribution also varies.

473 Table 3 presents NSE, RMSE, MAE, and MAPE values for the VAE/LSTM model
474 during the training and testing phases of spring discharge for each of the three periods, using
475 optimal synthetic precipitation ratios. These results underscore the robustness of the proposed
476 model, which is enhanced by precipitation data augmentation (considering spatiotemporal
477 variation) through VAE.

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482 **Figure 10.** Comparison between observed and predicted spring discharge in training and testing
 483 for the three periods.

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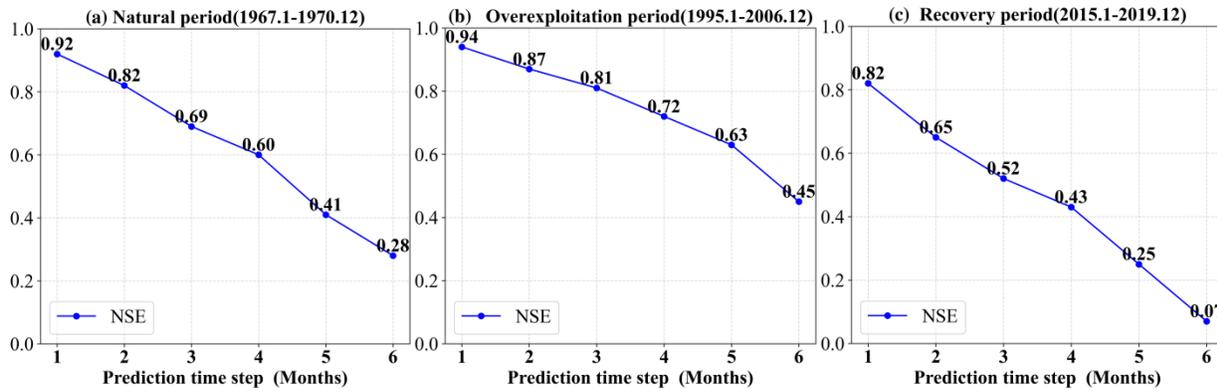
485 **Table 3.** Performance of VAE/LSTM for single-step spring discharge prediction during training
 486 and testing phases of the three periods.

Period	Data Ratio	Phase	NSE	RMSE	MAE	MAPE(%)
Natural	1:4	Training	0.96	0.32	0.18	1.31
1959-1970		Testing	0.92	0.33	0.19	1.40
Overexploitation	1:3	Training	0.96	0.37	0.19	1.97
1971-2006		Testing	0.94	0.24	0.17	2.49
Recovery	1:6	Training	0.91	0.20	0.09	1.31
2007-2019		Testing	0.82	0.20	0.11	1.51

487 4.3 Effectiveness of VAE/LSTM Model for Multi-Step Spring Discharge Prediction

488 Next, this paper expands its predictive horizon from forecasting one month of spring
 489 discharge to predicting spring discharge for the next six months. The results for the test data set
 490 of the three periods depicted in Figure 11 show a gradual decrease in the NSE values as the
 491 prediction step extends. When comparing the prediction outcomes across the three periods, it is
 492 evident that the NSE values for one-month and six-month predictions are as follows: 0.92 and
 493 0.28 (Natural period), 0.94 and 0.45 (overexploitation period) and 0.82 and 0.07 (Recovery
 494 period), respectively, which have a reduction of 69.57%, 52.13%, and 91.46%, correspondingly.
 495 This pattern might be linked to the climatic conditions of the Niangziguan spring. Niangziguan
 496 Spring is in northern China and is influenced by the northern monsoon and continental climate
 497 (He et al., 2019). During abundant rainfall, increased surface runoff can diminish the proportion
 498 of spring recharge, thereby impacting spring discharge (Fiorillo et al., 2010). Furthermore,
 499 predicting the next six months encompasses the summer high-temperature season, when rising
 500 temperatures can result in the evaporation of certain springs. Evaporative losses curtail the

501 effective recharge of spring (Mustafa et al., 2015), consequently diminishing the accuracy of
 502 forecasting future spring discharge.



503
 504 **Figure 11.** NSE performance for different forecast horizons in multi-step prediction of spring
 505 discharge for the three periods.

506 In contrast to single-step prediction, multi-step prediction provides longer-term
 507 projections, aiding in exploring the evolving patterns of karst spring discharge. However,
 508 considering long-term climate trends and seasonal variations at Niangziguan Spring, expanding
 509 the prediction horizon may include a greater range of seasons and climate variations. Different
 510 seasons may exhibit significant differences in precipitation patterns, increasing the complexity of
 511 predictions. Hence, choosing an excessively long prediction horizon may result in less accurate
 512 long-term LSTM predictions than shorter ones. Opting for smaller prediction horizons, such as
 513 two and three months, yields better predictive accuracy (Table 4). Smaller prediction timeframes
 514 encompass similar seasons and climatic conditions, aiding in capturing the trends in spring
 515 discharge more effectively. The previous cross-covariance analysis (Figure 7) should also
 516 explain these results.

517

518 **Table 4.** Performance of VAE/LSTM for 2 months and 3 months spring discharge predictions on
 519 the test data set for the three periods using the optimal parameters

Period	Prediction Steps	NSE	RMSE	MAE	MAPE(%)
Natural	2 Months	0.82	0.53	0.43	3.14
1967.1-1970.12	3 Months	0.69	0.64	0.53	3.92
Overexploitation	2 Months	0.87	0.36	0.28	4.01
1995.1-2006.12	3 Months	0.81	0.44	0.34	5.30
Recovery	2 Months	0.65	0.26	0.18	2.46
2015.1-2019.12	3 Months	0.52	0.32	0.21	2.88

520 **5 Discussions**

521 5.1 Comparing VAE-Augmented Deep Learning Models in Spring Discharge Prediction

522 This study also evaluates various deep learning models (RNN, ANN, GCN, and
 523 Transformer) to validate the universality of the data augmentation method proposed and its
 524 potential value in other hydrological applications. The introduction of these approaches are
 525 available in supporting information S3 and Figure S3. The experimental results in Table 5
 526 demonstrate that various deep learning models, following precipitation enhancement, achieve
 527 favorable single-step predictive outcomes. It is crucial to emphasize that the LSTM model yields
 528 the best predictive results (Table 3). This is attributed to its outstanding capability for time series
 529 modeling, its internal state to retain past information, and its proficiency in extracting temporal
 530 features. Therefore, it remains the preferred model for handling hydrological data, especially in
 531 karst terrains.

532

533 **Table 5.** Performance comparison of various models with VAE based data augmentation

Models	Periods	NSE	RMSE	MAE	MAPE(%)
RNN	Original(No Periods)	0.33	0.54	0.38	5.74
	Augmented(natural)	0.92	0.33	0.18	1.34
	Augmented(Overexploitation)	0.95	0.23	0.14	2.06
	Augmented(Recovery)	0.82	0.21	0.11	1.56
	Augmented(Mean)	0.89	0.26	0.14	1.65
ANN	Original(No Periods)	-0.42	0.79	0.64	9.84
	Augmented(natural)	0.77	0.55	0.41	3.02
	Augmented(Overexploitation)	0.81	0.44	0.32	4.90
	Augmented(Recovery)	0.77	0.23	0.13	1.83
	Augmented(Mean)	0.78	0.41	0.29	3.25
GCN	Original(No Periods)	0.05	0.64	0.43	6.41
	Augmented(natural)	0.73	0.59	0.44	3.13
	Augmented(Overexploitation)	0.82	0.43	0.31	4.82
	Augmented(Recovery)	0.60	0.31	0.15	2.11
	Augmented(Mean)	0.71	0.44	0.30	3.35
Transformer	Original(No Periods)	-0.15	0.71	0.57	8.23
	Augmented(natural)	0.90	0.36	0.25	1.89
	Augmented(Overexploitation)	0.87	0.36	0.26	3.97
	Augmented(Recovery)	0.78	0.23	0.15	2.14
	Augmented(Mean)	0.85	0.32	0.22	2.67

534 Specifically, RNN and LSTM excel in handling time series data because they can capture
535 temporal dependencies within hydrological data through internal states. Conversely, ANN is
536 typically designed as a feedforward neural network and lacks internal states for handling
537 temporal dependencies, potentially resulting in inferior performance when dealing with time
538 series data.

539 Furthermore, GCN can be employed in hydrological prediction for spatiotemporal graph
540 data, where nodes represent distinct geographical locations, and edges represent connections
541 between these locations. GCN's strength lies in its capacity to consider the relationships between
542 geographical locations (Gai et al., 2023). However, in this study, the data primarily focuses on
543 time series information, leading to slightly lower predictive performance for GCN than LSTM.

544 Simultaneously, the predictive performance of the Transformer model is not as
545 satisfactory as that of LSTM. This discrepancy may arise because Transformers tend to perform
546 better under conditions of large-scale datasets (Vaswani et al., 2017), whereas the dataset in this
547 research comprises only thousands of records even after augmentation. Therefore, Transformer
548 models may struggle to leverage their advantages when dealing with smaller datasets. In
549 summary, in the context of sparse and uncertain hydrological data, the approach presented in this
550 study significantly improves the performance of various deep-learning models in hydrological
551 prediction.

552 5.2 Performance Comparison of Various Data Augmentation Approaches

553 This study compares the performance of the LSTM model using various data
554 augmentation approaches. The results of performance metrics are shown in Table 6. We initiated
555 experiments for spring discharge prediction using linear regression and ARIMA (AutoRegressive

556 Integrated Moving Average) models. These traditional prediction models yielded unsatisfactory
557 results (as indicated in the first two rows of the table). This outcome is attributed to the fact that,
558 in hydrological forecasting, the relationship between spring discharge and various factors,
559 including meteorological and hydrological variables, is often nonlinear and nonstationary.

560 Furthermore, this involves statistical methods, like augmenting precipitation data to
561 conform to a uniform distribution of its extremes (Fourth row of Table 6). It also includes
562 precipitation augmentation using the tophat kernel function and density estimation (fifth row of
563 Table 6). Linear interpolation is applied by estimating values between known precipitation data
564 points, resulting in new augmented values (sixth and seventh row of Table 6). The methods for
565 data augmentation using deep learning include the LSTM model with direct data augmentation
566 without period division (eighth row of the Table 6) and the LSTM model with a two-period
567 division before and after human activities in 1971 for data augmentation (ninth row of the Table
568 6). The experimental results highlight that the LSTM model enhanced by VAE exhibits lower
569 errors in spring discharge prediction than the baseline LSTM model. Moreover, it demonstrates
570 superior predictive performance compared to traditional data augmentation methods.

571 Traditional statistical methods often rely on a single distribution estimate, which proves
572 challenging for capturing the intricate spatiotemporal characteristics of precipitation due to its
573 inherent complexity and uncertainty. In contrast, the VAE can derive joint latent distributions to
574 learn the nuanced representation of data by the encoding-decoding process, resulting in improved
575 preservation of temporal and spatial correlations in precipitation. Unlike precipitation
576 interpolation methods, which are limited by local information and may lead to information loss
577 in global spatiotemporal correlations, VAE excels at comprehensively preserving the multimodal
578 nature and global correlations of precipitation data, thereby providing enhanced information for

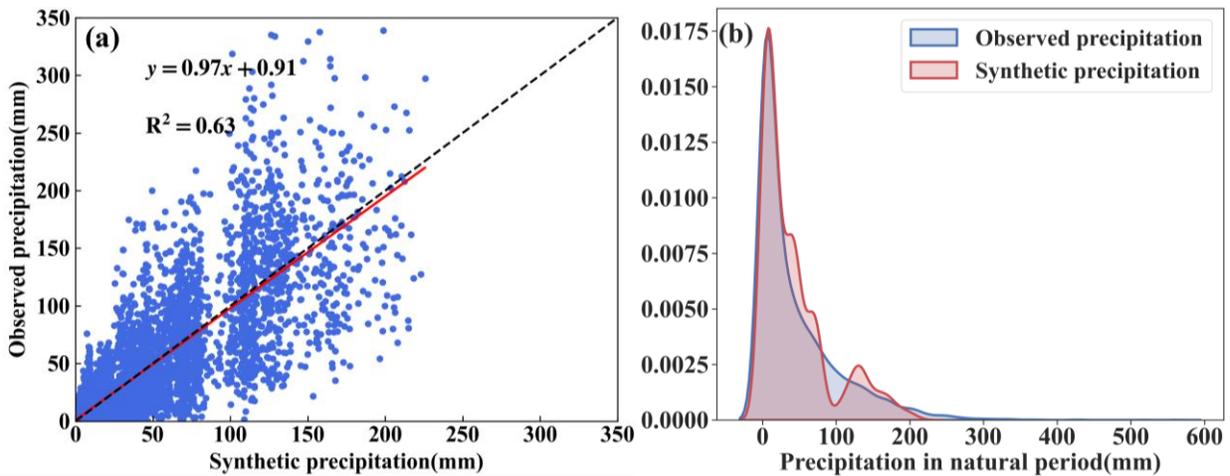
579 the LSTM. In augmenting precipitation with VAE across various periods, the enhanced model
 580 improves the NSE to 0.55 (NSE=0.38 vs. NSE=0.93) and MAE by 0.25 (MAE=0.40 vs.
 581 MAE=0.15). Moreover, the decrease in RMSE (RMSE=0.54 vs. RMSE=0.15) further
 582 substantiates the superior fit between the enhanced model and actual observations. Consequently,
 583 the three-period LSTM model with data augmentation yields enhanced performance in spring
 584 discharge prediction. Additionally, period-wise predictions based on regression analysis
 585 significantly augment the overall predictive capabilities of the model.

586 **Table 6.** LSTM model validation with different data augmentation strategies on validation set.

Data Augmentation Approach	NSE	RMSE	MAE	MAPE(%)
LinearRegression	0.04	1.53	1.26	9.04
ARIMA	-2.84	1.15	1.01	13.93
Only LSTM (Baseline)	0.38	0.54	0.40	6.03
LSTM with precipitation Uniform Distribution	-0.51	4.13	3.36	32.42
LSTM with Kernel Density Estimation (tophat)	0.67	0.65	0.49	3.63
LSTM with Linear Interpolation (No Periods)	0.49	0.87	0.69	5.04
LSTM with Linear Interpolation (Three-Period)	0.80	0.50	0.41	3.02
LSTM with VAE Data Augmentation (No Periods)	0.57	0.39	0.22	3.10
LSTM with VAE Two-Period Data Augmentation	0.72	0.31	0.15	2.11
LSTM with VAE Three- Period Data Augmentation	0.93	0.26	0.15	1.80

587 5.3 Visualization and Quantitative Results of the VAE

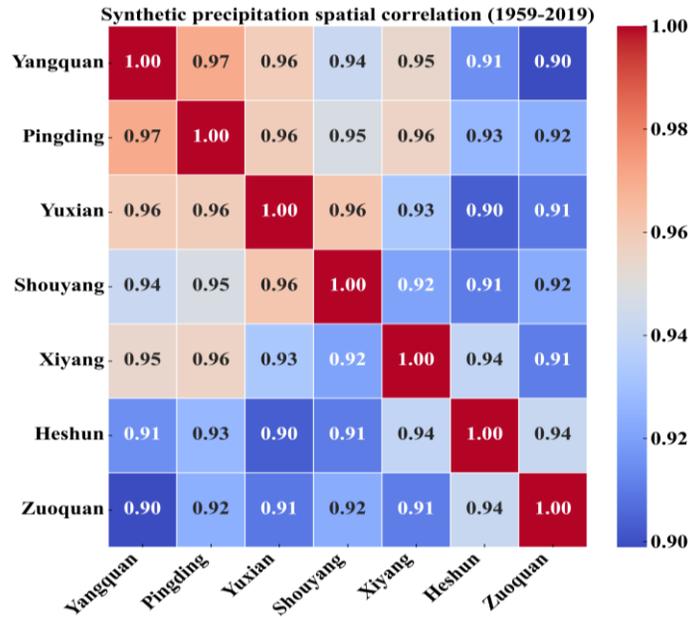
588 Next, we demonstrate that the VAE encoder captures the posterior probability
 589 distribution, mean, and autocovariance functions of observed precipitation data, and then the
 590 decoder generates the synthetic data with the same distribution, mean, and autocovariance
 591 functions. Figure 12a is the scatter plots showing that the synthetic series are unbiased compared
 592 with the observed data for the seven stations from 1959-2019. Figure 12b demonstrates that the
 593 probability distribution of the synthetic time series is consistent with that of the observed.



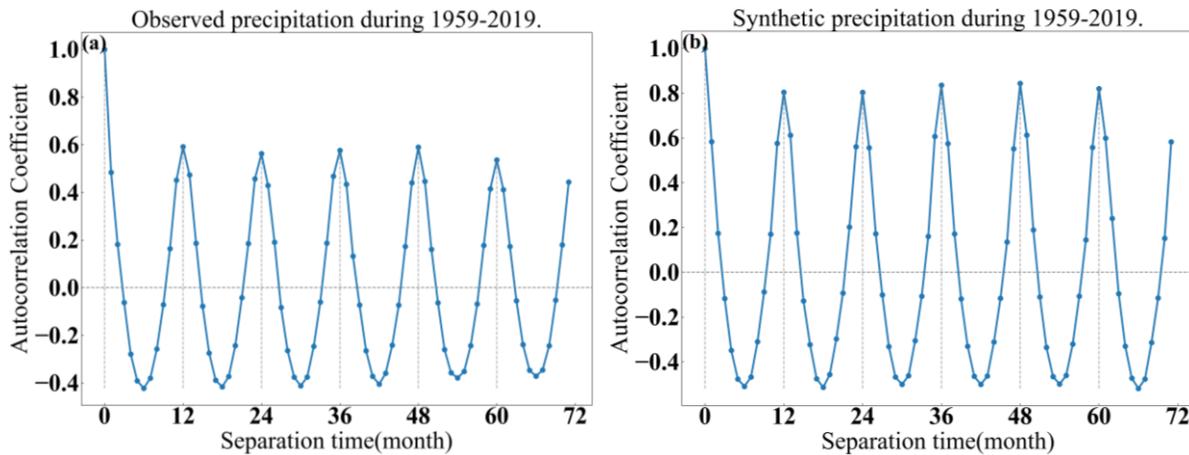
594 **Figure 12.** The observed and synthetic precipitation distribution for the seven stations from
 595 1959-2019.
 596

597 Figure 13 displays the correlations between the augmentation data at seven precipitation
 598 observation stations. Compared with Figure 5, the synthetic data reduce the gap of spatial
 599 precipitation and thus enhance the correlation between the precipitation observation points.
 600 Notice that intuitively, hourly or daily precipitations may vary throughout the region. The
 601 cumulative precipitations over a month likely filter out the spatial variability in precipitation. As
 602 such, the correlation between monthly precipitation data at different locations in the catchment is
 603 similar, indicating that the monthly precipitation spatial pattern over the entire catchment is
 604

605 almost uniform (small spatial variability). This result may suggest that the temporal variability of
 606 precipitation may play a more critical role in predicting the spring discharge than its spatial
 607 variability. Figure 14 shows the temporal auto-correlation of the seven stations' observed and
 608 synthetic precipitation time series (from 1959 to 2019). They illustrate that the VAE also
 609 enhances the temporal correlation of the precipitation.



610
 611 **Figure 13.** The correlations between the augmentation data at 7 precipitation observation
 612 stations



613
 614 **Figure 14.** The temporal auto-correlation of the observed and synthetic precipitation (from 1959
 615 to 2019). (a) is for the observed precipitation. (b) is for the synthetic precipitation.

616 **6 Conclusions**

617 This study utilized a VAE model to generate synthetic precipitation data and applied it to
618 the simulation of spring discharge in data-sparse karst regions. Augmenting the precipitation data
619 improved the learning capabilities and predictive performance of various deep learning models
620 (e.g., LSTM, RNN, ANN, GCN, Transformer, see supplementary section) for spring discharge
621 prediction.

622 We applied the VAE-augmented precipitation to the LSTM model for three periods of
623 Niangziguan Spring in China: a natural period, a subsequent overexploitation period, and finally,
624 a recovery period. The results of the augmented model demonstrated a significant advantage in
625 single-step spring discharge prediction. When validated against actual observations, the
626 augmented model exhibited notably higher predictive accuracy than the baseline LSTM model.

627 In the multi-step prediction of LSTM after data augmentation, which considered spring
628 discharge across three distinct periods, this study had revealed that opting for smaller prediction
629 horizons (e.g., two and three months) led to enhanced predictive accuracy. We concluded that
630 these narrower prediction timeframes encompassed more closely aligned seasons and climatic
631 conditions, thus facilitating the model in capturing the patterns in spring discharge more
632 effectively.

633 Our precipitation data augmentation strategy was further validated through multi-model
634 generalization experiments, demonstrating the versatility and effectiveness of this approach in
635 addressing challenges related to data scarcity in hydrology, particularly in regions with limited
636 data availability. This strategy is not restricted to specific LSTM models but can be extended to a
637 broader range of models depending on various hydrological contexts and research questions.

638 While we applied this strategy to a karst spring, its generality allows it to meet the
639 demands of diverse research inquiries across different domains. It offers researchers a novel
640 solution to address issues related to data scarcity and sampling difficulties, enabling them to
641 select appropriate models for prediction and analysis tailored to their specific requirements. We
642 present a fresh perspective on handling the challenges of data scarcity and uncertainty in
643 hydrological data.

644 **Acknowledgments**

645 The work of Yonghong Hao is partially supported by the National Natural Science
646 Foundation of China 42072277, 41272245, 40972165, 42307088 and 40572150. Chunmei Ma is
647 partially supported by the Scientific Research Project of Tianjin Education Commission under
648 Grant (No.2021KJ186). Yeh is partially supported by US NSF grant 000316729.

649

650 **Open research**

651 **Data Availability Statement**

652 The test data and test codes of our hybrid model are available at:
653 <https://github.com/csmcm/spring-discharge-prediction>.

654

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