

# Revisiting impact of MJO on soil moisture: a causality perspective

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## Introduction

- **Madden-Julian Oscillation (MJO) and El Niño Southern Oscillation (ENSO) impact extreme dry/wet conditions over tropical continental land [1-2]**
- **Granger Causality (GC) is widely used in geosciences**
  - **Useful and interpretable**
  - **Strong assumptions made: linearity and stationarity**
- **Our cross-kernel Granger causality (XKGC) [3]**
  - **Nonlinear relations**
  - **Kernel function for nonstationary processes**
- **We use XKGC to uncover the effect of the MJO and ENSO on global SM anomalies**

## Cross-information Kernel Granger Causality (XKGC)

### ● Granger Causality (GC):

#### Unrestricted Regression

$$y_{t+1} = \sum_{k=0}^p a_k y_{t-k} + \varepsilon_t^y$$

#### Causality Index

$$\delta_{x \rightarrow y} = \log(\mathbb{V}[\varepsilon_t^y]^2 / \mathbb{V}[\varepsilon_t^{y|x}]^2)$$

#### Restricted Regression

$$y_{t+1} = \sum_{k=1}^p a_k y_{t-k} + \sum_{l=1}^q b_l x_{t-l} + \varepsilon_t^{y|x}$$

- **Kernel Granger Causality (KGC)  $\mathbf{z}_t = [\mathbf{y}_t, \mathbf{x}_t] \in \mathbb{R}^{p+q}$** 
  - **Concatenate  $[X, Y]$  data in the restricted regression**
  - **Standard kernelization**

$$\begin{aligned} y_{t+1} &= \mathbf{a}_H^T \phi(\mathbf{y}_t) + \varepsilon_t^y \\ y_{t+1} &= \mathbf{b}_H^T \psi(\mathbf{z}_t) + \varepsilon_t^{y|x} \end{aligned} \quad \Rightarrow \quad \begin{aligned} y_{t+1} &= \boldsymbol{\alpha}^T \mathbf{k}_t + \varepsilon_t^y \\ y_{t+1} &= \boldsymbol{\beta}^T \boldsymbol{\ell}_t + \varepsilon_t^{y|x} \end{aligned}$$

- **Simple & neat**
- **One kernel param. to fit all & no cross-relation**
- **Cross-Kernel Granger Causality (XKGC):**
  - **Define a new feature map to generalize KGC**

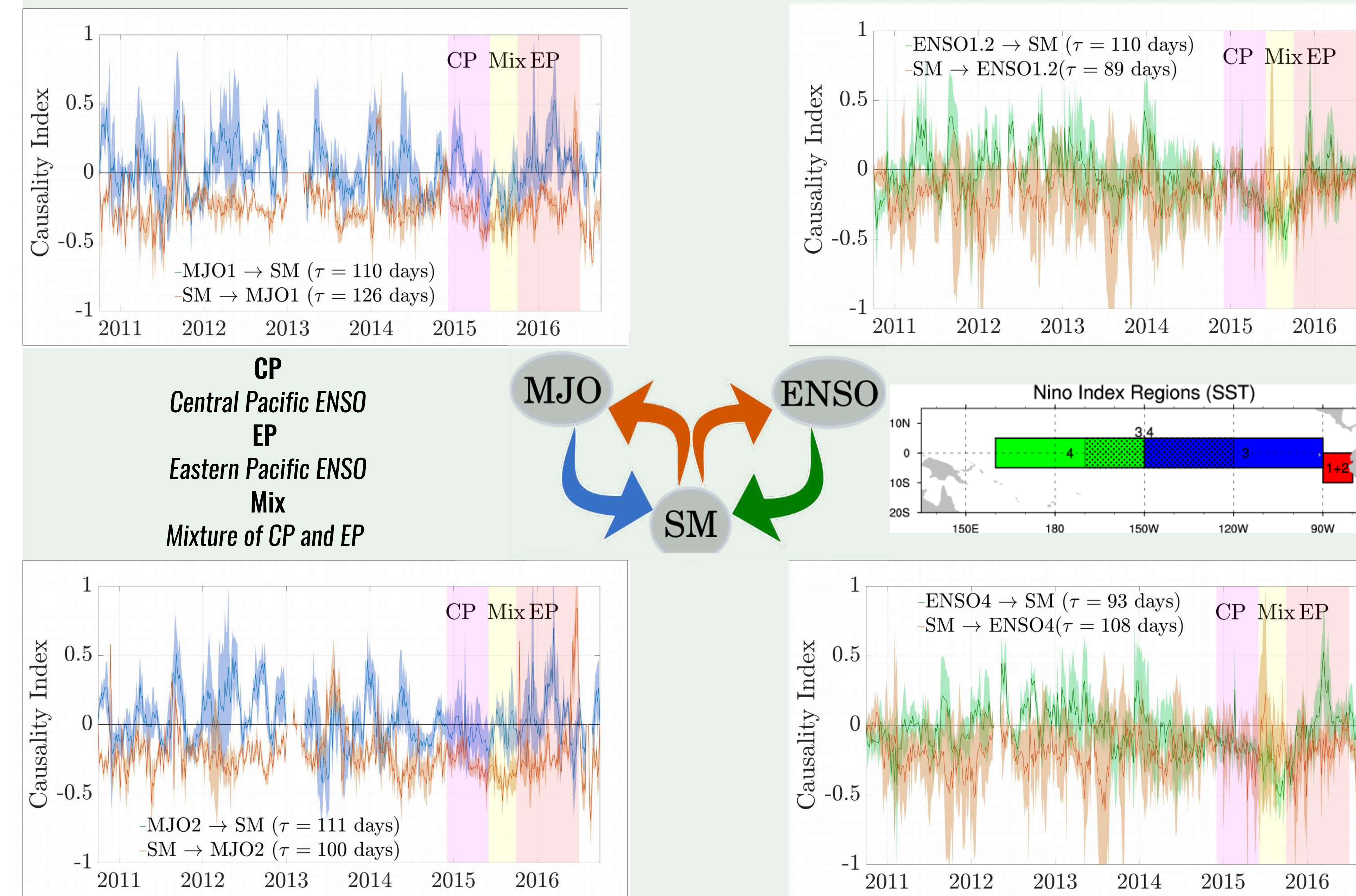
$$\psi(\mathbf{x}_t, \mathbf{y}_t) = [\phi_1(\mathbf{y}_t), \phi_2(\mathbf{x}_t), \phi_3(\mathbf{y}_t) + \phi_3(\mathbf{x}_t)] \quad \Rightarrow \quad \mathbf{K} = \psi^T \psi$$

$$\mathbf{K}(\mathbf{x}_t, \mathbf{y}_t) = \mathbf{K}_{xx} + \mathbf{K}_{yy} + \mathbf{K}_{xy} + \mathbf{K}_{yx}$$
  - **Generalizes KGC for more complex X-Y relations**
  - **Separates kernel parameters for each relation**
  - **Can find different scales on the non-linear relations**

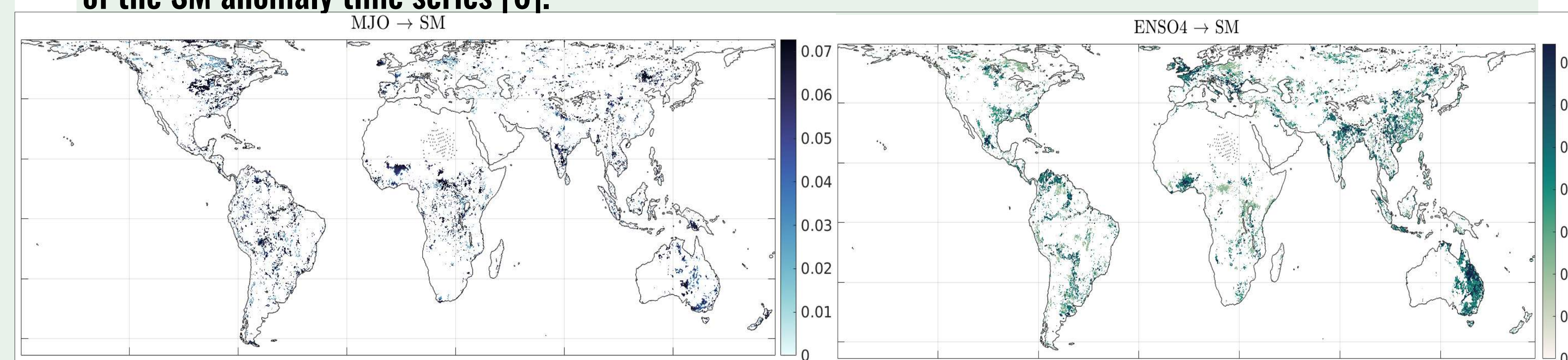
## MJO impact on soil moisture anomalies: An ENSO disruption

**Figure 1: ENSO atmospheric disruption, MJO and SM anomalies.** Estimation of causality indices using XKGC with a (half year) moving window. Mean and deviation of each index come from a sensitivity analysis of the autoregressive models [4], where values  $> 0$  indicate causality. Three regimes are identified [5]:

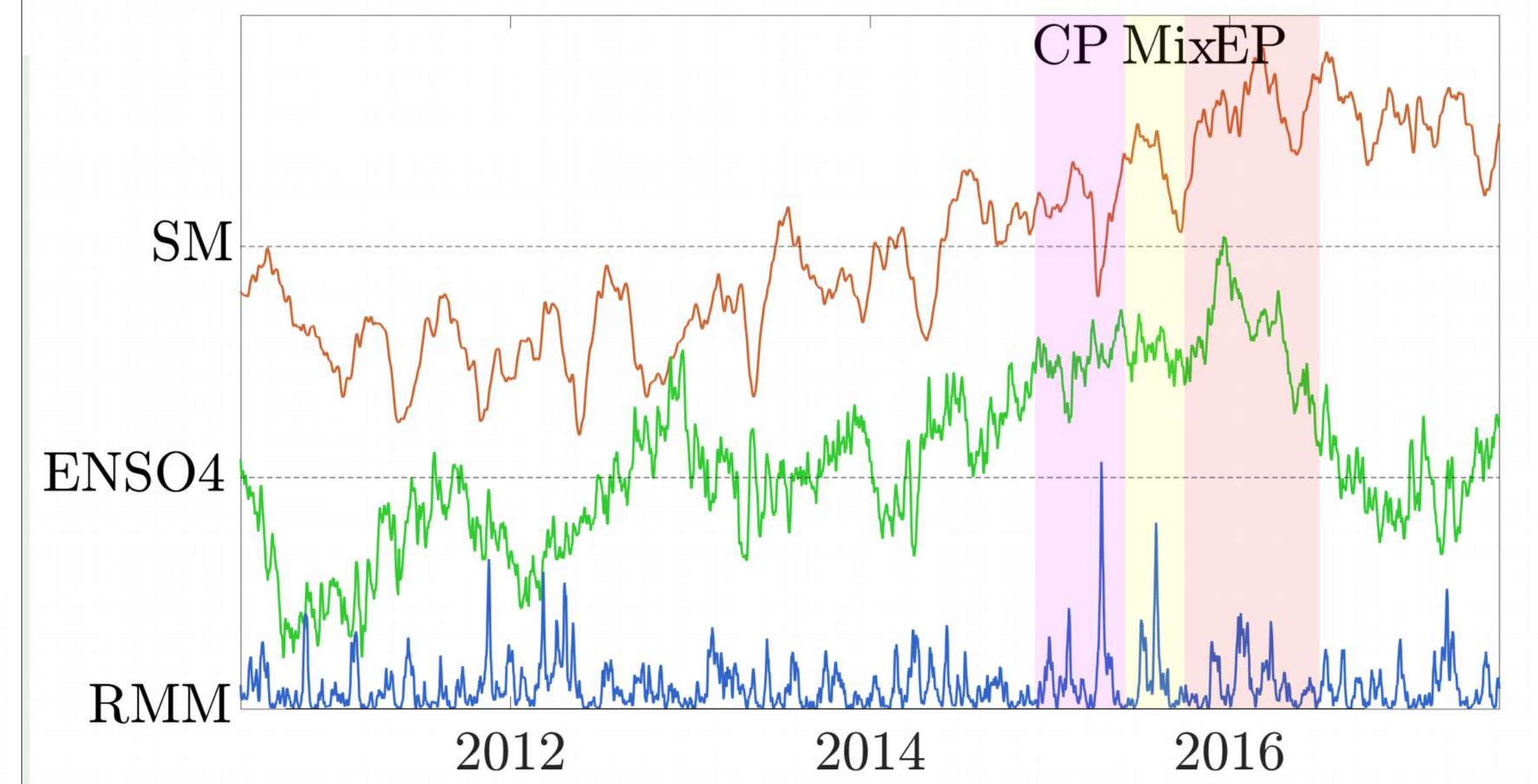
1. **Neutral period:** both ENSO and MJO induce variability (Granger Causality) on the SM anomalies till the start of the 2016 ENSO event (El Niño Godzilla).
2. **Disruption:** the link breaks at the CP ENSO phase and remains till the EP ENSO phase.
3. **Transition period:** during the peak of the ENSO event, highest variability induced on SM anomalies



**Figure 2: Spatio-temporal analysis of ENSO and MJO impacts on SM anomalies.** Causality index maps obtained from the neutral period (2010-2015). Spatial distribution extracted from the spatial component of the SM anomaly time series [6].



## Data



**Figure 3: Time series of main variables.**

- **ENSO:** SST anomalies of the equatorial Pacific Ocean.
- **Real-time Multivariate MJO (RMM):** First two EOF of 850 and 200 hPa zonal wind average over the Equator.
- **SM:** data extracted from ESA's SMOS (Soil Moisture Ocean Salinity) mission. Independent and complex valued Spatio-temporal features have been extracted using a nonlinear dimensional reduction method for different time scales [6].

## Conclusions

- **New XKGC method generalizes GC & KGC**
- **Reconstructing the ENSO atmospheric disruption, breaking the causal link between MJO and ENSO and the SM anomalies**
- **Common causal mediators revealed**
- **Causality maps reveal different MJO and ENSO impacts on SM anomalies**

## References

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