Online calculation of O$_2$ clumped-isotope variations in an atmospheric chemistry model reveals an important contribution from ozone isotopologue chemistry

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Abstract

Tropospheric $^{18}O^{18}O$ is an emerging proxy for past tropospheric ozone and free-tropospheric temperatures. The basis of these applications is the idea that isotope-exchange reactions in the atmosphere drive $^{18}O^{18}O$ abundances toward isotopic equilibrium. However, previous work used an offline box-model framework to explain the $^{18}O^{18}O$ budget, approximating the interplay of atmospheric chemistry and transport. This approach, while convenient, has poorly characterized uncertainties. To investigate these uncertainties, and to broaden the applicability of the $^{18}O^{18}O$ proxy, we developed a scheme to simulate atmospheric $^{18}O^{18}O$ abundances (quantified as Δ_{36} values) online within the GEOS-Chem chemical transport model. These results are compared to both new and previously published atmospheric observations from the surface to 33 km. Simulations using a simplified O$_2$ isotopic equilibration scheme within GEOS-Chem show quantitative agreement with measurements only in the middle stratosphere; modeled Δ_{36} values are too high elsewhere. Investigations using a comprehensive model of the O-O$_2$-O$_3$ isotopic photochemical system and proof-of-principle experiments suggest that the simple equilibration scheme omits an important pressure dependence to Δ_{36} values: the anomalously efficient titration of $^{18}O^{18}O$ to form ozone. Incorporating these effects into the online Δ_{36} calculation scheme in GEOS-Chem yields quantitative agreement for all available observations. While this previously unidentified bias affects the atmospheric budget of $^{18}O^{18}O$ in O$_2$, the modeled change in the mean tropospheric Δ_{36} value since 1850 C.E. is only slightly altered; it is still quantitatively consistent with the ice-core Δ_{36} record, implying that the tropospheric ozone burden likely increased less than ~40% over the twentieth century.

9589 Words (main text)

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10 Figures

2 Tables

Plain Language Summary

Oxygen in the air is constantly being broken apart and remade. Its constituent atoms are shuffled around by light-induced chemical reactions, which cause changes in the number of heavy oxygen atoms that are bound together. The number of these heavy-atom "clumps" is sensitive to air temperatures and the presence of air pollution; hence, their variations are being used to understand past high-altitude temperatures and atmospheric chemistry. This study incorporates oxygen clumping into an atmospheric chemistry model and compares the results to measurements of oxygen clumping in the atmosphere. We find that the model can explain all the modern-day measurements (from the surface to 33 km altitude), but only if the broader fates of oxygen atoms—i.e., their incorporation into other molecules beyond O_2—are considered. Simulations of the preindustrial atmosphere are also generally consistent with snapshots of the ancient atmosphere obtained from O_2 trapped in ice cores. The developments described herein will thus enable models to simulate heavy oxygen-atom clumping in past cold and warm climates and enable simulated high-altitude atmospheric changes to be evaluated directly against ice-core snapshots of the ancient atmosphere.

1. Introduction

Odd oxygen [O(^3P), O(^1D), and O$_3$] is a key component of the modern atmosphere's oxidizing capacity. As such, tracing its evolution over time may provide better constraints on lifetimes of greenhouse gases, stratosphere-troposphere coupling, biosphere-atmosphere interactions, and radiative forcing in different climates. Moreover, elevated odd-oxygen concentrations in the upper troposphere and stratosphere mean that a globally integrated record of odd oxygen could provide a unique window on the high-altitude atmosphere of the past, both in terms of chemistry and climate [*Thompson et al.*, 1998; *Tripati et al.*, 2014; *Yeung et al.*, 2016; *Loomis et al.*, 2017]. Observational constraints on temperatures of the ancient high-altitude atmosphere, for example, would bring new insights on how Earth's energy balance changes with climate.

The short lifetime of odd-oxygen species, however, precludes their direct preservation in traditional atmospheric archives. Interrogating past variability of atmospheric odd oxygen thus requires the use of proxies and models [*Alexander et al.*, 2003; *Murray et al.*, 2014; *Alexander and Mickley*, 2015; *Geng et al.*, 2017; *Yeung et al.*, 2019]. For example, hydrogen peroxide is a stable product of odd-oxygen chemistry (via HO$_2$ self-reaction) that is preserved in ice cores, but its sensitivity to post-depositional alteration reduces the number of scenarios under which its variations reflect atmospheric odd-oxygen changes [*Frey et al.*, 2006]. Another proxy is the ^{15}N/^{14}N ratio of snow-bound nitrate, which is sensitive to local ultraviolet flux and thus also the local atmospheric column density of O$_3$, provided the local accumulation rate and optical depth in the snow are known [*Frey et al.*, 2009; *Ming et al.*, 2020; *Winton et al.*, 2020]. However, anthropogenic changes to nitrogen cycling can overprint the odd-oxygen signals [*Hastings et al.*, 2009; *Geng et al.*, 2014]. Proxies based on the transfer of O$_3$-derived ^{17}O enrichments, primarily to nitrate and sulfate species, exploit an isotopic signature unique to O$_3$ chemistry, but at best they provide constraints on the relative importance of O$_3$, OH, and HO$_2$ oxidation pathways [*Alexander et al.*, 2009; *Kunasek et al.*, 2010; *Sofen et al.*, 2011; *Sofen et al.*, 2014; *Geng et al.*, 2017]. Common among all these approaches is a sensitivity to local odd-oxygen variability; global trends are not accessible.

Recently, *Yeung et al.* [2019] applied a new proxy for odd-oxygen chemistry preserved in the ice-core record that offers a globally integrated view. It is based on proportional changes in the ^{18}O^{18}O abundance of O$_2$ in the troposphere, a signal that is integrated globally on annual timescales. Isotope-exchange reactions between O(^3P) and O$_2$ drive these changes [*Yeung et al.*, 2014] and provide the crucial link between short-lived atmospheric odd oxygen concentrations and the longer-lived isotopic composition of O$_2$. Tropospheric odd-oxygen chemistry is distinguished from stratospheric odd-oxygen chemistry by the difference in characteristic temperatures: the distribution of isotope-exchange products depends on temperature, with colder temperatures generally yielding larger ^{18}O^{18}O enrichments in O$_2$. Tropospheric ^{18}O^{18}O enrichments (quantified as Δ_{36} values; see Methods) are believed to primarily reflect

89 odd-oxygen chemistry in the free troposphere, with a smaller but important contribution from

90 downwelling stratospheric air [*Yeung et al.*, 2016]. The subtle decrease in tropospheric Δ_{36} value over the

91 twentieth century was interpreted to reflect an increase in the tropospheric ozone burden of less than 40%,

92 corroborating recent model estimates [*Yeung et al.*, 2019].

93 Yet, important details of the global $^{18}O^{18}O$ budget remain uncertain. Previous quantitative

94 estimates of atmospheric $^{18}O^{18}O$ variations were facilitated by global 3-D chemical-transport model

95 simulations of $O(^3P)$ concentrations, but the Δ_{36} calculations were still performed offline, i.e., without

96 direct coupling of atmospheric chemistry, mixing, and transport [*Yeung et al.*, 2016; *Yeung et al.*, 2019].

97 The expense of isotopologue-specific chemistry—e.g., the $O-O_2-O_3$ photochemical system itself requires

98 >300 additional, highly-stiff reactions to represent—renders explicit online calculation of $^{18}O^{18}O$

99 variations impractical.

100 A simplified treatment of the relevant O_2 isotopologue photochemistry is possible because

101 laboratory studies indicate that the approach of Δ_{36} values toward photochemical steady state can be

102 described by pseudo-first-order kinetics [*Yeung et al.*, 2014]. Isotope-exchange reactions between $O(^3P)$

103 and O_2 at low pressures (e.g., $1-2$ mbar) drive isotopologue abundances toward isotopic equilibrium, but

104 the uncertainty in their kinetics is large, particularly at the low temperatures relevant for the upper

105 troposphere and stratosphere (Fig. 1, left). Moreover, isotope effects in O_3 formation could be

106 important—particularly the anomalous enrichments in $^{18}O^{18}O$-containing isotopologues that also vary

107 with temperature and pressure (Fig. 1, right) [*Mauersberger*, 1981; *Heidenreich and Thiemens*, 1983;

108 *Thiemens and Heidenreich*, 1983; *Guenther et al.*, 1999; *Mauersberger et al.*, 1999; *Gao and Marcus*,

109 2001; *Janssen et al.*, 2003]. While imperfect, parameterization of these effects may offer a practical

110 balance between accuracy and computational cost that allows Δ_{36} variations to be simulated online for

111 different climates.

112 In this manuscript, we use new high-precision Δ_{36} measurements from the modern atmosphere

113 spanning a range of latitudes in the Northern Hemisphere to assess two different online Δ_{36} calculation

114 schemes within the GEOS-Chem chemical-transport model. The first scheme considers only O_2 isotopic

115 equilibration at *in situ* temperatures, using rates determined by local $O(^3P)$ concentrations and $O(^3P) + O_2$

116 isotope-exchange rate coefficients, while the second scheme includes a temperature- and pressure-

117 dependent parameterization for the effects of O_3 formation. Furthermore, we compare the results of online

118 and offline Δ_{36} calculation schemes to improve our understanding of the $^{18}O^{18}O$ budget and interpretations

119 of Δ_{36} changes in the recent atmospheric record.

120

121 **2. Methods**

122 **2.1 Measurements of new upper-tropospheric and lower-stratospheric samples**

123   Twenty-three whole-air samples were collected from the NASA ER-2 aircraft during the Studies

124   of Emissions, Atmospheric Composition, Clouds and Climate Coupling by Regional Surveys (SEAC[4]RS)

125   campaign [*Lueb et al.*, 1975; *Toon et al.*, 2016] and selected for O_2 isotopologue composition

126   measurements in duplicate. Flights associated with the campaign took place over the continental United

127   States in August and September of 2013. Samples were selected from five individual flights between

128   23.7°N and 42.6°N latitude and between 87.3°N and 99.5°E longitude, with potential temperatures

129   ranging from $\theta = 328$ K to $\theta = 498$ K.

130   Isotopologue ratios of O_2 were measured on a high-resolution Nu Instruments *Perspective IS*

131   isotope ratio mass spectrometer after gas-chromatographic separation from Ar, N_2, and other trace

132   components of air [*Yeung et al.*, 2016; *Yeung et al.*, 2018; *Ash et al.*, 2020]. These ratios are converted to

133   isotopic "delta" notation according to the following definitions:

134

$$\delta^{18}O = \left(\frac{^{18}R_{sample}}{^{18}R_{air}} - 1\right) \qquad \delta^{17}O = \left(\frac{^{17}R_{sample}}{^{17}R_{air}} - 1\right) \tag{1}$$

136

$$\Delta_{35} = \left(\frac{^{35}R_{sample}}{^{35}R_{stochastic}} - 1\right) \qquad \Delta_{36} = \left(\frac{^{36}R_{sample}}{^{36}R_{stochastic}} - 1\right) \tag{2}$$

138

139   Here, ^{18}R and ^{17}R are the bulk $^{18}O/^{16}O$ and $^{17}O/^{16}O$ ratios in O_2, whereas ^{36}R is the $^{18}O^{18}O/^{16}O^{16}O$

140   isotopologue ratio. The "stochastic" subscript refers to the random distribution of isotopes within O_2, i.e.,

141   $^{35}R_{stochastic} = 2{}^{17}R_{sample}{}^{18}R_{sample}$ and $^{36}R_{stochastic} = ({}^{18}R_{sample})^2$. Air sampled from an external staircase on the

142   third floor of the Keith-Wiess Geology building at Rice University was used as the bulk-isotope standard

143   against which $\delta^{18}O$ values are reported. Reported Δ_{36} values are calibrated against photochemical and

144   heated-gas standards generated at known temperatures according to established techniques [*Yeung et al.*,

145   2014]. The photochemical standards are generated by submerging a 1 L bulb filled with $1 - 2$ mbar of

146   pure O_2 into a constant-temperature bath held at 22ºC, –25ºC, or –78ºC, allowing the bulb to reach

147   thermal equilibrium, and then photolyzing it with a mercury lamp through an N_2-flushed internal quartz

148   finger for 40 minutes. The effective photolysis temperature reflects the radiative equilibrium between the

149   bath and the finger, which is warmed slightly due to the presence of the lamp and N_2 gas flush (i.e.,

150   yielding effective temperatures of 25ºC, –19ºC, or –65ºC for each calibration standard, respectively).

151   High-temperature standards are generated by heating barium peroxide in an evacuated quartz breakseal at

152   800ºC for $1.5 - 3$h, after which the breakseal is quenched by submerging it in room-temperature water.

153   Samples were analyzed between 2017 and 2019, but only one sample showed a bulk isotopic

154   composition more than 0.1‰ different from air O_2, indicating good isotopic fidelity despite several years'

155   storage. The mean $\delta^{18}O$ deviations from air across the whole dataset were 0.019 ± 0.063‰ (1σ, $n = 46$

156   analyses). While omitting the high-$\delta^{18}O$ sample improves the precision across the whole dataset (i.e., $\delta^{18}O$

157   mean of 0.007 ± 0.036‰), such small positive $\delta^{18}O$ deviations—likely arising from diffusive gas loss

158   rather than a contaminant—are unlikely to affect Δ_{36} values significantly. Therefore, all the SEAC^{4}RS

159   measurements were used. The pooled standard deviation of replicates was ±0.026‰, ±0.071‰ and

160   ±0.045‰ in $\delta^{18}O$, Δ_{35}, and Δ_{36} values, respectively.

161

162   **2.2 Atmospheric chemical transport modeling**

163   Model simulations using GEOS-Chem (version 12.9.2; http://www.geos-chem.org) and the

164   unified (UCX) chemical mechanism [*Eastham et al.*, 2014] were performed using default global

165   emissions for present-day (PD) simulations of June 1998 – June 2000 and calendar year 2015 [*McDuffie*

166   *et al.*, 2020]. The UCX mechanism treats stratospheric and tropospheric chemistry under a common

167   scheme and includes explicit accounting of atomic oxygen species, which is necessary for online

168   calculation of Δ_{36} values. The model used meteorology from the Modern Era Retrospective Reanalysis-2

169   (MERRA2) [*Gelaro et al.*, 2017] with 72 vertical levels (~38 in the troposphere), degraded to a spatial

170   resolution of $4° \times 5°$ (latitude $\times$ longitude). Preindustrial era (PI) simulations were also performed using

171   2015 meteorology with natural (non-anthropogenic) emissions set to those for 1850 C.E. In those

172   simulations, methane, nitrous oxide, and carbonyl sulfide were prescribed using surface mixing ratio

173   boundary conditions that yielded atmospheric concentrations consistent with ice-core constraints [*Murray*

174   *et al.*, 2014]. Anthropogenic halocarbon concentrations were also prescribed (set to zero) using surface

175   boundary conditions. Biomass burning emissions for the PI are uncertain, with estimates of PI-to-PD

176   changes varying in both sign and magnitude [*McConnell et al.*, 2007; *Marlon et al.*, 2008; *Lamarque et*

177   *al.*, 2010; *Wang et al.*, 2010; *Bisiaux et al.*, 2012; *Daniau et al.*, 2012; *Pfeiffer et al.*, 2013; *Nicewonger et*

178   *al.*, 2018; *Dyonisius et al.*, 2020]; recent constraints on PI methane, ethane, and acetylene emissions from

179   biomass burning suggest that they were comparable to those of the PD, or perhaps slightly higher [*Pfeiffer*

180   *et al.*, 2013; *Nicewonger et al.*, 2018; *Dyonisius et al.*, 2020; *Nicewonger et al.*, 2020]. Consequently,

181   biomass burning emissions were held constant for PI simulations.

182   Two online calculation schemes for Δ_{36} values were implemented in GEOS-Chem. Both were

183   simplified schemes designed to minimize the computational burden needed to represent $O(^3P) + O_2$

184   isotope-exchange chemistry. In the first scheme ("O_2 only"), Δ_{36} values decay toward isotopic equilibrium

185   according to simple first-order kinetics, which are dependent on temperature but independent of O_3

186   isotopologue chemistry. In the second scheme ("pressure-dependent"), Δ_{36} values decay toward an

187   isotopic steady state rather than isotopic equilibrium. The steady state is determined by local temperature

188   and pressure due to changes in the rates of both isotope-exchange and O_3 isotopologue formation

189   reactions. In both schemes, the temperature and the atomic oxygen concentration ($[O(^3P)]$) in each grid

190   box determine the local instantaneous rates of isotope exchange. The nominal first-order rate coefficient

191   for the Δ_{36} system was approximated by the temperature-dependent $^{16}O + {}^{18}O^{18}O$ isotope-exchange rate

192   coefficient reported by *Fleurat-Lessard et al.* [2003], i.e., $k_{exch}(T)$, which is more precise than that

193   originally reported in *Wiegell et al.* [1997]. At each time-step, the concentration of the Δ_{36} tracer is

194   relaxed toward its local equilibrium or steady-state value according to the isotope-exchange lifetime and

195   the length of the time-step. After the chemistry operation, the Δ_{36} tracer is allowed to advect.

196   In the O_2-only scheme, the local Δ_{36} value relaxes toward its isotopic equilibrium value, $\Delta_{36,equil}$

197   [*Wang et al.*, 2004], between time t_0 and $t_0 + \Delta t$ according to the equation:

198

199    $$\Delta_{36,t_0+\Delta t} = \Delta_{36,t_0} + \left(\Delta_{36,equil} - \Delta_{36,t_0}\right) \times \left(1 - e^{-\Delta t/\tau_{exch}}\right) \tag{3}$$

200

201   Here, $\tau_{exch} = 1/(k_{exch}(T)[O(^3P)])$ represents the local Δ_{36} lifetime with respect to isotope exchange. In the

202   pressure-dependent scheme, the local Δ_{36} value relaxes toward $\Delta_{36,ss}$ instead of $\Delta_{36,equil}$, with the other

203   quantities remaining the same. The particular value of $\Delta_{36,ss}$ was determined by polynomial fits to the

204   results of an isotope-enabled photochemical model (i.e., a photochemical kinetics model that includes all

205   isotopologue-specific rate coefficients and species; see Section 2.3).

206   The online Δ_{36} outputs included full O_2-only and pressure-dependent outputs (herein Δ_{36} and Δ_{36P},

207   respectively), as well as diagnostic Δ_{36} values for isotope exchange occurring only within the troposphere

208   (Δ_{36t} and Δ_{36Pt}) or only within the stratosphere (Δ_{36s} and Δ_{36Ps}). These latter diagnostics were calculated by

209   turning off the operation in eq. 3 if a grid box is above or below the local tropopause, respectively, during

210   a time-step.

211

212   **2.3 Isotope-enabled photochemical model to determine $\Delta_{36,ss}$ values**

213   The 321-reaction KINTECUS photochemical model for the O-O_2-O_3 system from *Yeung et al.*

214   [2014] was updated to include temperature- and pressure-dependent isotope effects for O_3 formation in

215   the atmosphere [*Ianni*, 2003]. Dinitrogen (N_2) was added as a separate species to yield near-atmospheric

216   mixing ratios of N_2 and O_2 (i.e., 79% N_2 and 21% O_2); argon was not included for simplicity and because

217   isotope effects in O_3 formation in argon appear to be similar to those of N_2 and O_2 [*Morton et al.*, 1990;

218   *Thiemens and Jackson*, 1990; *Feilberg et al.*, 2013]. The temperature dependencies of ^{18}O-containing O_3

219   formation rate coefficients were obtained from *Janssen et al.* [2003], while the pressure dependencies for

220   the relative rate coefficients of the $^{16}O + {}^{16}O^{18}O + M \rightarrow {}^{16}O^{16}O^{18}O + M$ and $^{16}O + {}^{18}O^{18}O + M \rightarrow$

221    $^{16}O^{18}O^{18}O + M$ reactions were obtained from *Guenther et al.* [1999]. The temperature and pressure

222   dependencies of these relative rate coefficients were combined using the following expression from

223   *Guenther et al.* [1999] for O_3 isotopologue enrichments:

7

224

$$E_{O_3}(T, P) = \frac{E_{O_3}(T)}{1 + P/P_{1/2}} \tag{4}$$

226

227   where $E_{O3}(T)$ is the temperature-dependent enrichment of an O_3 isotopologue relative to $^{16}O_3$ at 300K/200

228   Torr obtained from *Janssen et al.* [2003] [e.g., $E_{O3}(T) = 0.47 + (T - 300\ K) \times 0.00015$ for $^{16}O + {}^{18}O^{18}O$],

229   and $P_{1/2}$ is the pressure at which the enrichment is halved, obtained from *Guenther et al.* [1999] (e.g., $P_{1/2}$

230    $= 4100$ Torr or 5466 mbar for $^{16}O + {}^{18}O^{18}O$). The ratio of rate coefficients for the formation of $^{16}O^{16}O^{18}O$

231   and $^{16}O^{18}O^{18}O$, relative to $^{16}O_3$, is thus $1 + E_{O3}(T,P)$. While the 300K/200 Torr anchor point yields zero-

232   pressure E_{O3} values that differ slightly from those used in *Guenther et al.* [1999], they agree within

233   several percent; the method used here yields slightly better agreement with the measurements reported in

234   *Janssen et al.* [2003]. The ratio of rate coefficients for the $^{18}O + {}^{16}O^{16}O + M \to {}^{16}O^{16}O^{18}O + M$ and $^{18}O +$

235    $^{18}O^{18}O + M \to {}^{18}O^{18}O^{18}O + M$ reactions has a negligible dependence of pressure [*Guenther et al.*, 1999],

236   so the 300K/200 Torr relative rate coefficients were used and kept constant [*Mauersberger et al.*, 1999].

237   The 300K/200 Torr isotopologue-specific relative rate coefficients measured by *Mauersberger et al.*

238   [1999] were also used and held constant wherever temperature- and pressure-dependent data were not

239   available (e.g., for ^{17}O-containing O_3 isotopologues). Because of these missing inputs, Δ_{35} values

240   simulated by this model at elevated pressures are unlikely to be accurate; those results are not reported.

241   Where possible, the relative rate coefficients for $O(^3P) + O_2$ isotope exchange reactions were

242   determined assuming microscopic reversibility at isotopic equilibrium for each temperature [*Hathorn and*

243   *Marcus*, 2000; *Wang et al.*, 2004; *Yeung et al.*, 2014], with their absolute rates ultimately tied to the

244    $^{16}O(^3P) + {}^{18}O^{18}O$ isotope-exchange rate constant determined by *Fleurat-Lessard et al.* [2003], i.e., $k_{exch}(T)$

245    $= 2.7 \pm 0.4 \times 10^{-12}$ $(T/300)^{-0.9 \pm 0.5}$ cm^3 s^{-1} (2σ). Seven ^{17}O-containing reactions of the 18 total isotope-

246   exchange reactions were assigned nominal 300 K rate coefficients (i.e., $k_{exch} = 1.5 \times 10^{-12}$ cm^3 s^{-1} per

247   product channel) because their rate coefficients are not known. Previous work has shown that factor-of-

248   two variations in these rate coefficients have a negligible effect on steady-state Δ_{36} values [*Yeung et al.*,

249   2014].

250   Isotope effects in other reactions (e.g., during O_3 photolysis or chemical destruction) may also be

251   important, but their cumulative effects on $^{16}O^{18}O$ and $^{18}O^{18}O$-containing species in the atmosphere are

252   poorly known. Owing to the uncertainties in these quantities [*Liang et al.*, 2006; *Früchtl et al.*, 2015a;

253   *Früchtl et al.*, 2015b; *Huang et al.*, 2019], this model only explores the relationship between the isotope

254   effects for $O(^3P) + O_2$ isotope exchange and O_3 formation. We acknowledge that the results obtained are

255   necessarily incomplete, although they are still informative and relevant to the global atmosphere.

256   Photochemical simulations were performed to generate an array of steady-state solutions between

257   175 K and 325 K and 0.3 mbar and 4000 mbar total pressure. The relative rates of O_2 and O_3 photolysis

258   were adjusted to yield ~50 ppb O_3 at tropospheric pressures. Each model was run using the mean and 2σ

259   uncertainty bounds for $k_{exch}(T)$. At low temperatures, the uncertainty in $k_{exch}(T)$ is nearly a factor of two

260   (Fig. 1, left), which dominates the overall uncertainty in steady-state Δ_{36} values.

261

262   **3.   Results**

263   **3.1 Atmospheric observations of Δ_{36} of O_2**

264   Figure 2 shows the new Δ_{36} measurements on the SEAC[4]RS samples, which were collected by the

265   NASA ER-2 aircraft, along with previous high-precision measurements made at Rice University on

266   samples from the SOLVE mission (NASA ER-2), the DC3 mission (NASA DC-8), and high-altitude

267   balloon flights over Fort Sumner, NM [*Yeung et al.*, 2016]. The Δ_{36} values from SEAC[4]RS samples

268   decrease from ~2.7‰ at $\theta = 500K$ toward the tropospheric value of 1.99‰, which is reached at $\theta = 360K$

269   and below (Fig. 2). A maximum value of 2.77‰ was observed in the lower stratosphere at 24°N ($\theta = $

270   444K). The new data show remarkable consistency with previously reported observations from the

271   midlatitude upper troposphere and stratosphere when plotted against potential temperature [*Yeung et al.*,

272   2016]. All the SEAC[4]RS samples below $\theta = 475$ K were analytically more than 2σ different from isotopic

273   equilibrium, with deviations as large as –1.06‰ relative to $\Delta_{36,equil}$ values implied by *in situ* sampling

274   temperatures (Fig. 2 and Supporting Information). The largest disequilibria were observed in the

275   tropopause region (e.g., $\theta = 360K$), and were larger at 24°N than at 40°N. Notably, in the midlatitudes

276   between $\theta = 400K$ and 500K, measured Δ_{36} values decrease just 0.1‰ with decreasing θ, whereas $\Delta_{36,equil}$

277   values increase by as much as 0.4‰. The Δ_{36} disequilbrium there thus primarily reflects an increase in

278    $\Delta_{36,equil}$ values. By contrast, the Δ_{36} disequilbrium in the lowermost stratosphere largely reflects the

279   gradient in measured Δ_{36} values rather than the more weakly varying $\Delta_{36,equil}$ values.

280   Plots of Δ_{36} values versus trace-gas mixing ratios in the same samples show correlations in certain

281   mixing ratio ranges but a limited dependence on latitude in the lower stratosphere (Fig. 2). In particular,

282   Δ_{36} values and O_3 concentrations are positively correlated consistently across multiple field campaigns

283   below 500 ppb O_3. Δ_{36} values and CO concentrations are inversely correlated, whereas Δ_{36} values and

284   CH_4 concentrations are positively correlated below 1700 ppb CH_4 and negatively correlated above. These

285   observations are consistent with high-Δ_{36} stratospheric air mixing with low-Δ_{36} tropospheric air in the

286   lower stratosphere [*Yeung et al.*, 2016]. The change in the relationship between Δ_{36} values and trace gases

287   where $O_3 > 500$ ppb and $CH_4 < 1700$ ppb reflects a weak or negligible mixing signal for Δ_{36} values in that

288   region of the stratosphere arising from more rapid photochemical isotope reordering of O_2 [*Yeung et al.*,

289   2014].

290   Near 150 ppb O_3—the mixing-ratio-defined tropopause used in some atmospheric chemistry

291   modeling studies (e.g., *Young et al.* [2013])—the SEAC⁴RS data imply a Δ_{36} value of 2.21 ± 0.04‰ (1σ),

292   which is slightly lower than, but consistent with the previously reported value of 2.32 ± 0.08‰ (1σ) from

293   samples taken from the DC3 campaign [*Barth et al.*, 2015; *Yeung et al.*, 2016]. However, the SEAC⁴RS

294   data show higher precision and cover both subtropical and extratropical latitudes in the Northern

295   hemisphere. At θ = 380K—the lower bound of the stratospheric "overworld", where isentropic transport

296   does not cross the tropopause, and thus a common isentropic reference surface for computing

297   stratosphere-to-troposphere mass fluxes [*Holton et al.*, 1995; *Appenzeller et al.*, 1996; *Schoeberl*,

298   2004]—the SEAC⁴RS data imply a mean Δ_{36} value of 2.29 ± 0.04‰ (1σ) based on a linear regression of

299   the data between θ = 358 and θ = 406 K (R^2 = 0.96).

300

301   **3.2 O_2-only online Δ_{36} modeling in GEOS-Chem**

302   Modeled Δ_{36} values from the O_2-only online calculation agree with measurements for θ > 500 K,

303   but are 0.1‰ – 0.4‰ higher than the measurements below that potential temperature (Fig. 2). At the

304   surface, these simulations yield a global-mean Δ_{36} value of 2.37‰, whereas measurements consistently

305   yield values that are 0.4‰ lower [*Yeung et al.*, 2014; *Yeung et al.*, 2016; *Li et al.*, 2019; *Yeung et al.*,

306   2019]. Yet, the qualitative trends seen in the observational dataset are reproduced, with latitude-dependent

307   isotopic disequilibria that are greatest at low latitudes.

308   The measurement-model disagreement persisted upon variation of many model parameters. For

309   example, altering the rate coefficient for $O(^3P) + O_2$ isotope exchange within the 2σ uncertainty range of

310   laboratory measurements yielded perturbations to the mean surface Δ_{36} value of <0.01‰. Turning off

311   advective and convective transport changed the surface Δ_{36} value by less than 0.14‰. Resetting Δ_{36}

312   values of all air parcels that cross the tropopause to a fixed value (values between 1.1‰ and 2.3‰ were

313   evaluated) yielded tropospheric Δ_{36} values that are within 0.13‰ of that prescribed value.

314   The diagnostic Δ_{36t} and Δ_{36s} values—calculated Δ_{36} values for isotope exchange occurring in the

315   troposphere and stratosphere only—are 2.27‰ and 2.71‰, respectively. The Δ_{36t} value corresponds to an

316   effective equilibration temperature of –33°C characteristic of the upper free troposphere. The Δ_{36s} value is

317   within 0.1‰ of the simulated Δ_{36} values near the θ = 380K isentrope. Absolute isotope-exchange rates

318   increased by four orders of magnitude from the surface to θ = 900 K, yielding O_2 chemical lifetimes of

319   0.1 – 1000 days with respect to isotope exchange (Fig. 2).

320

321   **3.3. Isotope-enabled photochemical modeling**

322   Incorporation of isotope-specific rate coefficients for O_3 formation into a photochemical model of

323   the O-O_2-O_3-N_2 system, including their pressure- and temperature dependence, revealed deviations from

324   isotopic equilibrium when the system is at photochemical steady state. As pressure increases from 0 to

325   1500 mbar between 175 K and 325 K, steady-state Δ_{36} values (i.e., $\Delta_{36,ss}$) show deficits relative to $\Delta_{36,equil}$

326   values (Fig. 3). The deficits are largest at high pressures, with low-temperature deficits exceeding those at

327   higher temperatures. While the equilibrium Δ_{36}-temperature relationship is approached in the low-

328   pressure limit, modeled $\Delta_{36,ss}$ values remain $0.01 - 0.04$‰ below equilibrium values even at 0.1 mbar.

329   Varying the isotope-exchange rate coefficient $k_{exch}(T)$ about its 2σ uncertainty range changes the

330   magnitude of the $\Delta_{36,ss}$ pressure dependence, with the upper end of the range (i.e., faster rates) yielding

331   smaller steady-state $^{18}O^{18}O$ deficits and vice versa. The resulting uncertainty bounds for $\Delta_{36,ss}$ values at

332   atmospherically relevant conditions are largest at low temperatures and high pressures. For example, at

333   175 K, the uncertainty in $k_{exch}(T)$ led to an effective 2σ range of 2.3‰ at 1000 mbar ($+0.9$‰ and -1.4‰

334   about the mean) but a smaller 2σ range of 0.26‰ at 100 mbar ($+0.10$‰ and -0.16‰ about the mean).

335   The assumed relative rate of O_3 and O_2 photolysis also affects the magnitude $^{18}O^{18}O$ deficit, but the effect

336   is $O(0.01$‰$)$. The overall pressure-dependent trends are fit well by a third-order polynomial at a given

337   temperature ($R^2 > 0.999$; Fig. 3).

338   Nulling out the relative rate coefficient enhancements in the $O + O_2 + M \rightarrow O_3 + M$ reactions that

339   form heavy O_3 isotopologues—which are as large as 50% compared to the rate of the $^{16}O_3$-forming

340   reaction—eliminates the pressure-dependent deficits in $^{18}O^{18}O$ relative to isotopic equilibrium when the

341   system is at isotopic steady state. This deviation of $\Delta_{36,ss}$ from $\Delta_{36,equil}$ values is most sensitive to the

342   enhancements in the relative rate coefficients for the $^{16}O + {}^{18}O^{18}O$ and $^{16}O + {}^{16}O^{18}O$ reactions that form

343   O_3. For example, at 1000 mbar and 200 K, the isotope-exchange pathway for $^{16}O + {}^{18}O^{18}O$ collisions

344   outpaces the O_3 production pathway by a factor of ~50. Moreover, a $^{16}O + {}^{18}O^{18}O$ collision produces O_3

345   ~20% faster than a $^{16}O + {}^{16}O^{18}O$ collision under these conditions [*Guenther et al.*, 1999; *Janssen et al.*,

346   2003]. This unusually fast transfer of $^{18}O^{18}O$ into O_3, especially compared to $^{16}O^{18}O$, lowers the Δ_{36} value

347   of the remaining O_2 pool. Ozone formation via $^{16}O + {}^{18}O^{18}O$ collisions therefore causes a roughly $1/50 \times$

348      $0.2 \times \frac{1}{2} = 2$‰ decrease in Δ_{36} value, comparable to the 1.8‰ difference between $\Delta_{36,equil}$ and $\Delta_{36,ss}$ values

349   obtained from the full photochemical model (note that the factor of $\frac{1}{2}$ arises from the presence of both

350      $^{16}O^{18}O$ and $^{18}O^{16}O$ isotopomers, which halves the effect of the $^{16}O + {}^{18}O^{18}O$ rate enhancement for O_3

351   formation). A similar calculation at 1000 mbar and 300 K yields an estimated 0.7‰ deficit in $\Delta_{36,ss}$

352   compared to $\Delta_{36,equil}$, close to the 0.5‰ deficit calculated by the full model. At low pressures, the

353   sequestration of $^{18}O^{18}O$ isotopologues into O_3 is small: $^{16}O + {}^{18}O^{18}O$ isotope exchange is favored by a

354   factor of 10^5 over O_3 formation at 1 mbar and 300 K, resulting in deficits of $O(0.01$‰$)$. These results

355   suggest that the steady-state deficits in $\Delta_{36,ss}$ compared to $\Delta_{36,equil}$ values arise largely from an efficient

356   titration of $^{18}O^{18}O$ by ^{16}O to make excess $^{16}O^{18}O^{18}O$.

11

357   We note that the $\Delta_{36,ss}$ values at pressures > 1100 mbar may be most sensitive to uncertainties in

358 the relative temperature- and pressure-dependence of O_3 isotopologue formation rate coefficients; because

359 these pressures are higher than atmospheric pressures, the corresponding $\Delta_{36,ss}$ values are not critical for

360 modeling atmospheric Δ_{36} values, and we do not evaluate them further.

361   Our preliminary mercury-lamp photolysis experiments, in which air is irradiated for 40 minutes at

362 elevated pressures (500 – 1000 mbar), show large Δ_{36} deficits relative to isotopic equilibrium. An

363 experiment at 25°C and 887 mbar pressure showed a 0.16‰ deficit, while an experiment at –65°C and

364 540 mbar showed a 0.9‰ deficit relative to the $\Delta_{36,equil}$ value. These experiments confirm the presence of

365 a pressure-dependent photochemical steady state for Δ_{36} values, but the precise Δ_{36} deficits are not yet in

366 quantitative agreement with those predicted by the photochemical model (0.55‰ and 0.95‰,

367 respectively). This disparity may be related to photolytic isotope fractionations for O_3 and O_2 at 254 nm

368 and 185 nm, respectively (i.e., the emission wavelengths of the mercury lamp), which are uncertain for

369 $\delta^{18}O$ and $\delta^{17}O$ and unknown for Δ_{36}. Nevertheless, these experiments are a proof of principle of the

370 $^{18}O^{18}O$ "titration effect," with excellent measurement-model agreement at low temperatures. A thorough

371 laboratory investigation is appropriate for future work.

372

3.4 Parameterizing the pressure dependence of Δ_{36} values at photochemical steady state

374   A parameterization of the pressure-dependent $^{18}O^{18}O$ titration effect on $\Delta_{36,ss}$ described in Section

375 3.3 was implemented as an online Δ_{36} calculation in GEOS-Chem using two polynomial fits. First, the

376 coefficients of the $\Delta_{36,ss}$ vs. pressure polynomial fits (i.e., a to d in $\Delta_{36,ss} = a\mathrm{P}^3 + b\mathrm{P}^2 + c\mathrm{P} + d$) were

377 plotted as a function of temperature. Fifth-order polynomial fits for each coefficient as a function of

378 temperature [e.g., a(T), b(T), etc.] were obtained and used to calculate a, b, c, and d as a function of both

379 temperature and pressure; the results are shown in Table 1. The $\Delta_{36,ss}$ value obtained from this two-

380 component scheme was then substituted for $\Delta_{36,equil}$ in eq. 3 to represent the local pressure-dependent Δ_{36}

381 endmember for isotope exchange. This scheme, while simplified, reproduced the $\Delta_{36,ss}$ values in the

382 photochemical model to within 0.01‰ (Fig. 3). It offers a great reduction in cost compared to

383 representing isotopologue-specific reactions in GEOS-Chem explicitly.

384   The combined effects of atmospheric pressure and temperature covariations on $\Delta_{36,ss}$ values

385 predicted by the pressure-dependent scheme are shown in Fig. 4. Near the surface, the $\Delta_{36,ss}$ value is 0.6‰

386 to 0.8‰ lower than the $\Delta_{36,equil}$ value and somewhat insensitive to temperature; the pressure dependence

387 largely determines $\Delta_{36,ss}$ values. In the mid- to upper stratosphere, however, $\Delta_{36,ss}$ values are close to

388 $\Delta_{36,equil}$ values, with temperature exerting the dominant control. In between (i.e., the free troposphere up

389 through the lower stratosphere), $\Delta_{36,ss}$ values are consistently lower than $\Delta_{36,equil}$ values, although

390 temperature and pressure are of comparable importance for determining local $\Delta_{36,ss}$ values. These results

391   imply that using $\Delta_{36,ss}$ instead of $\Delta_{36,equil}$ values in atmospheric chemistry simulations will lead to a more

392   pronounced contrast between tropospheric and stratospheric air, and detectable Δ_{36} offsets extending into

393   the lower stratosphere.

394   The results of GEOS-Chem simulations utilizing local $\Delta_{36,ss}$ values are compared to the Δ_{36}

395   observations in Fig. 5. The model for year 2015 shows excellent agreement with the SEAC^{4}RS, DC3, and

396   Ft. Sumner measurements at all altitudes in midlatitudes, with discrepancies smaller than those incurred

397   by the 2σ uncertainty range in the rate coefficient for $O(^3P) + O_2$ isotope exchange. The high-latitude

398   SOLVE samples were obtained in January 2000 from in the polar vortex [*Yeung et al.*, 2009; *Wiegel et*

399   *al.*, 2013], which can be heterogeneous in space and time; consequently, the 2015 meteorology may not

400   be applicable. The simulations for January 2000, by contrast, explain the SOLVE samples well (Fig. 5,

401   dashed line). At the surface, the pressure-dependent online Δ_{36} calculation scheme yields a global-mean

402   Δ_{36P} value of 1.97‰ in 2015 with diagnostic Δ_{36Pt} and Δ_{36Ps} values of 1.83‰ and 2.43‰ for troposphere-

403   only and stratosphere-only isotope exchange, respectively (Table 2). The calculated surface Δ_{36P} value is

404   in quantitative agreement with the long-term mean of surface Δ_{36} measurements made at Rice University

405   (1.99 ± 0.02‰; 95% confidence interval), while the Δ_{36Ps} value is ~0.14‰ higher than the Δ_{36} value at the

406    $\theta = 380$ K isentrope implied by the current set of atmospheric observations.

407

408   **3.5 Modeled spatial and temporal variability in Δ_{36} values**

409   Figure 6 shows modeled seasonal variations in modern-day surface Δ_{36P} values at various sites in

410   the Northern and Southern Hemispheres. Mean Δ_{36P} values are 0.02‰ lower in the Northern Hemisphere,

411   while the seasonal ranges are 0.03‰ and 0.02‰ in the Northern and Southern Hemispheres, respectively.

412   In the O_2-only calculation scheme, the seasonal ranges are slightly smaller (0.02‰ and 0.01‰,

413   respectively). None of these subtle hemispheric differences in Δ_{36} values are currently analytically

414   resolvable.

415   The preindustrial (PI) simulations yielded a global-mean surface Δ_{36} value that is 0.06‰ higher

416   than the present day (PD) in the pressure-dependent model scheme, whereas they it is 0.05‰ higher than

417   the PD in the O_2-only model scheme (Table 2). Moreover, the spread in PI-to-PD Δ_{36} change derived

418   from the 2σ uncertainty range in $\underline{k}_{exch}(T)$ is ≤0.004‰ in both schemes. Both model schemes therefore

419   yield results that are generally consistent with the tropospheric Δ_{36} change measured in ice cores (0.03 ±

420   0.02; 95% confidence interval) [*Yeung et al.*, 2019], despite measurement-model disagreements in

421   absolute Δ_{36} values. We note that these Δ_{36} differences correspond to the same modeled change in the

422   tropospheric O_3 burden, which is 34% higher in the PD compared to the PI (i.e., 296 Tg O_3 vs. 221 Tg

423   O_3).

424

4. Discussion

4.1 Assessing the accuracy of the $\Delta_{36,ss}$ pressure dependence

A pressure dependence to $\Delta_{36,ss}$ could have significant implications for interpretating Δ_{36} variations in nature. First, however, one must evaluate whether the pressure-dependent online calculation scheme is accurate by evaluating other potential sources of error. The evidence for an important pressure-dependent effect on atmospheric Δ_{36} values includes: (*i*) observation-model agreement in atmospheric Δ_{36} values above $\theta = 500$ K, but Δ_{36} disagreements in the below in the O_2-only calculation scheme, (*ii*) demonstrated isotopic disequilibrium caused by nonstatistical removal of O_2 isotopologues during O_3 formation, and (*iii*) excellent observation-model agreement when $\Delta_{36,ss}$ values are used in place of $\Delta_{36,equil}$ values in GEOS-Chem/MERRA2.

While the modern-day atmospheric observations can be explained within the pressure-dependent framework, other factors are still relevant to consider. In particular, measurement errors, errors in stratosphere-to-troposphere transport (STT) in the model, and errors in the rates of oxygen-isotope exchange could be important. We explore each of these possibilities below.

4.1.1 Potential errors in measurements

The agreement between measurements and the GEOS-Chem/MERRA2 model in the middle stratosphere (i.e., 500 K $< \theta < 950$ K), argues against significant measurement errors. The high $O(^3P)$ concentrations in the middle stratosphere—reflected in both the model and *in situ* measurements (e.g., $\sim 10^8$ cm^{-3} at 30 km in boreal autumn; [*Anderson*, 1975])—rapidly reorder isotopes in O_2, resulting in O_2 isotope-exchange lifetimes of day or less [*Yeung et al.*, 2012; *Yeung et al.*, 2014]. Thus, Δ_{36} values are expected to be near local isotopic equilibrium in the middle stratosphere, where $\Delta_{36,ss}$ and $\Delta_{36,equil}$ values are within 0.03‰. The measurements made at Rice University are consistent with this expectation. Mass-spectrometric scale distortions in Δ_{36} measurements are accounted for by low-pressure (<2 mbar) photochemical and high-temperature calibration experiments performed during every analytical session [*Yeung et al.*, 2014; *Yeung et al.*, 2018]. The associated uncertainties are an order of magnitude smaller than the observation-model disagreements. Measured differences in Δ_{36} values between photochemical calibration standards are typically within 0.03‰ of those predicted by theory; these deviations are quantitatively attributable to a combination of isotopic reordering during sample handling [*Yeung et al.*, 2012] and possibly a subtle pressure-dependent effect that is not currently resolvable. Moreover, recent work demonstrating reasonable agreement between first-principles theory and respiratory fractionation of Δ_{36} values [*Ash et al.*, 2020] offers ancillary evidence arguing against large analytical errors (i.e., $>0.05‰$) in the measurements made at Rice University.

Finally, all Δ_{36} and Δ_{35} values measured at Rice to date covary along a mass-dependent fractionation trend (Fig. 7, which shows the slope of 1.92 for isotopic equilibrium [*Wang et al.*, 2004]).

459   While the exact pressure-dependent relationship between $\Delta_{36,ss}$ and $\Delta_{35,ss}$ values is not independently

460   known, the O_3 formation reactions most relevant to $\Delta_{35,ss}$ values (e.g., $^{16}O + {}^{17}O^{18}O$ and $^{16}O + {}^{16}O^{17}O$) are

461   predicted to have rate coefficients similar to those most relevant to $\Delta_{36,ss}$ values [*Hathorn and Marcus*,

462   2000]. However, the relative rate coefficients for $O(^3P) + O_2$ isotope exchange are mass-dependent, so the

463   net titration of $^{17}O^{18}O$ isotopologues is expected to occur in proportion to their steady-state abundances;

464   ozone formation should not strongly alter the relationship between Δ_{36} and Δ_{35} values. Consequently, the

465   measured mass-dependent covariation in Δ_{36} and Δ_{35} values argues against analytical biases in Δ_{36}

466   measurements, but this inference remains to be verified by measurements of isotopologue-specific rate

467   coefficients.

468   One other laboratory has reported Δ_{36} measurements on air samples from the midlatitude upper

469   troposphere and lower stratosphere. The Δ_{36} values reported in *Laskar et al.* [2019] are all 0.3 – 0.4‰

470   higher than the Ft. Sumner and SEAC[4]RS data (samples from September 2004 and 2013, respectively),

471   despite the common latitude range and season (34°N – 42°N, 10 – 20 km, sampled September 2016).

472   Reported Δ_{36} values for surface air from Utrecht, The Netherlands are also higher than the values reported

473   for surface air in earlier papers [*Yeung et al.*, 2012; *Yeung et al.*, 2014; *Yeung*, 2016; *Li et al.*, 2019]. No

474   data from the middle stratosphere were reported. At face value, the uniformly higher tropospheric and

475   lower-stratospheric Δ_{36} values in *Laskar et al.* [2019] might favor the O_2-only photochemical scheme;

476   however, such a result would imply a profound inaccuracy in the Rice data. Importantly, a large offset in

477   the Rice data would imply that the midlatitude middle stratosphere is far from isotopic equilibrium,

478   contrary to expectations based on high local $O(^3P)$ concentrations [*Anderson*, 1975]. Rapid advection of

479   high-Δ_{36} air from the tropical stratosphere to the midlatitudes could cause a Δ_{36} excess of 0.3 – 0.4‰ in

480   the midlatitude stratosphere (i.e., reflecting air that is 12 – 16°C cooler at equilibrium); however, that air

481   would need to travel at an average speed of ~30 m s^{-1} during the traverse—ten times faster than

482   meridional wind speeds in the MERRA2 reanalysis in the middle stratosphere—without mixing with the

483   surrounding air. We note that the average meridional wind speeds in MERRA2 [$O(1 \text{ m s}^{-1})$] are consistent

484   with transport timescales from the tropics to the midlatitudes implied by chemical tracer studies [*Boering*

485   *et al.*, 1996; *Andrews et al.*, 1999]. Furthermore, the narrow spread in measured Δ_{36} values along surfaces

486   of constant potential temperature suggests that dispersive mixing is pervasive and mutes any variability

487   arising from meridional temperature gradients. Consequently, the Δ_{36} values reported in *Laskar et al.*

488   [2019] are incompatible with their atmospheric context. The origin of the interlaboratory disagreement

489   remains unknown, but could plausibly be related to differences in calibration protocols such as the

490   pressures of photolysis of photochemical standards.

491   **4.1.2 Potential errors in stratosphere-troposphere exchange fluxes**

492   Inaccurate STT fluxes could have varied effects on lower-stratospheric Δ_{36} values because O_2

493   there is not at photochemical steady state with respect to its isotopologues. Weak STT fluxes in the model

494   would cause excessive lower-stratospheric residence times, driving Δ_{36} values in the model closer to local

495    $\Delta_{36,equil}$ or $\Delta_{36,ss}$ values than in the observations. STT fluxes that are too strong would have a variety of

496   effects depending on whether the transport is diabatic (e.g., from excessive vertical velocities in the

497   residual circulation) or isentropic (e.g., an excessive diffusive flux). Stronger downward diabatic flow

498   might increase lower-stratospheric Δ_{36} values due to the influx of high-Δ_{36} air from above. This particular

499   case is difficult to distinguish from the weak-STT case, but both scenarios would underestimate the

500   fraction of tropospheric air in the lower stratosphere (i.e., air that has not been photochemically reordered

501   since crossing the tropopause). By contrast, excessive isentropic mixing would increase the fraction of

502   tropospheric air in the lowermost stratosphere, rendering modeled Δ_{36} values there too low.

503   We therefore used the fraction of tropospheric air as a metric to evaluate the accuracy of STT in

504   the model. A two-component mass balance between tropospheric O_2 and stratospherically reordered O_2 in

505   air for each sample can be constructed to approximate the lower-stratospheric budget:

506

507    $$\Delta_{36,observed} = f_{trop}\Delta_{36,trop} + (1 - f_{trop})\Delta_{36,ss \text{ or } equil} \tag{5}$$

508

509   Here, stratospheric O_2 is defined as O_2 that was recently reset to its local $\Delta_{36,ss}$ or $\Delta_{36,equil}$ value. An

510   estimate of the fraction of tropospheric air, f_{trop}, can thus be derived from an observed Δ_{36} value and the

511   calculated local $\Delta_{36,ss}$ endmember of the sampling location. While the assumption that only local

512   reordering and mixing alters Δ_{36} values leads to some uncertainties in this estimate for f_{trop}, the results

513   should be sufficient to test for gross errors in STT because the lapse rate is small in the lower

514   stratosphere, resulting in smaller variations in $\Delta_{36,ss}$ or $\Delta_{36,equil}$. We used $\Delta_{36,trop} = 1.99‰$ for the

515   measurements [*Yeung et al.*, 2019] and $\Delta_{36,trop} = 1.97‰$ (pressure-dependent scheme) or $2.37‰$ (O_2-only

516   scheme) for the model to maintain internal consistency.

517   To facilitate comparison with other studies of STT, the modeled isotope-exchange timescale from

518   GEOS-Chem, τ_{exch}, was used to derive an effective mean residence time ($\tau_{residence}$) from the equation

519

520    $$f_{trop} = e^{-\tau_{residence}/\tau_{exch}} \tag{6}$$

521

522   This effective mean residence time can be directly compared to mean residence times for the lowermost

523   stratosphere reported in observational studies. A disagreement between the $\tau_{residence}$ values obtained via Δ_{36}

524   measurements, the model, and other observational studies would indicate shortcomings in the calculation

525   of the $\Delta_{36,ss}$ endmembers, τ_{exch}, or the two-endmember approach.

526   Figure 8 shows the values of f_{trop} and $\tau_{residence}$ derived from this analysis. In both schemes, the

527   tropospheric fraction is less than 5% above $\theta = 450$ K and increases below, with excellent observation-

528   model agreement. The data also support a subtle meridional trend in modeled f_{trop} values, in which

529   subtropical f_{trop} values are 10 – 15% higher than midlatitude values at the same potential temperature.

530   Calculated residence times range between 20 and 60 days in the lowermost stratosphere (i.e., $\theta < 380$ K),

531   consistent with observationally constrained estimates of 20 – 80 days in the tropical tropopause layer

532   documented during boreal winter [*Andrews et al.*, 1999; *Krüger et al.*, 2009]. STT mass fluxes in the

533   MERRA2 reanalysis therefore appear reasonably accurate, at least for the purposes of this measurement-

534   model comparison.

535   **4.1.3 Potential errors in O(^3P) + O$_2$ isotope-exchange rates**

536   The measurement-model agreement in the "O$_2$-only" calculation scheme could potentially be

537   improved if lower-stratospheric O(^3P) + O$_2$ isotope-exchange rates are overestimated and/or tropospheric

538   isotope-exchange rates are underestimated. Because the uncertainty in laboratory measurements of

539   k_{exch}(T) has only a weak effect on the O$_2$-only online Δ_{36} results (cf. Fig. 2), the changes in isotope-

540   exchange rates would need to be driven by changes in O(^3P) concentrations. GEOS-Chem's chemical

541   mechanism does omit O$_2$($^1\Sigma$) chemistry, which can lead to an underestimate of O(^3P) concentrations

542   particularly in the stratosphere [*Yeung et al.*, 2014], but the accuracy of stratospheric O$_3$ concentrations

543   calculated by the UCX mechanism [*Eastham et al.*, 2014] disfavors this scenario: an additional odd-

544   oxygen source in the stratosphere would increase O$_3$ concentrations and drive lower-stratospheric Δ_{36}

545   values closer to isotopic equilibrium, exacerbating existing disagreements. Similarly, the high accuracy of

546   tropospheric O$_3$ concentrations in GEOS-Chem argues against a major (e.g., factor-of-two or more)

547   deficit in tropospheric O(^3P) concentrations at the global scale [*Hu et al.*, 2017].

548   A preponderance of evidence therefore supports a pervasive titration of ^{18}O^{18}O into O$_3$ in the

549   atmosphere, which results in lower atmospheric Δ_{36} values than isotopic equilibration would predict.

550   Thus, an error in the Rice laboratory measurements does not need to be invoked; the GEOS-

551   Chem/MERRA2 model represents STT and photochemical isotope exchange reasonably well; and

552   uncertainties in the isotope-exchange rates cannot account for the magnitude of the Δ_{36} offsets between

553   measurements and the O$_2$-only photochemical scheme. Given this evidence, we can now explore the

554   implications this new pressure-dependent isotope chemistry has for our understanding of the global Δ_{36}

555   budget.

556

557   **4.2 Revisiting the global Δ_{36} budget: reconciling online and box-model approaches**

558   Tropospheric Δ_{36} values are determined largely by the balance of two processes: O(^3P) + O$_2$

559   reactions and stratosphere-troposphere mass exchange. Model predictions using pressure-dependent $\Delta_{36,ss}$

560   values affect the implied importance of each process, but not the overall form of the budget. Therefore, in

561   steady state, and omitting biological oxygen cycling (which has a negligible contribution to the global Δ_{36}

562   budget [*Yeung et al.*, 2015]), one can describe the tropospheric budget as a two-endmember mixture:

563

564    $$\Delta_{36,\text{trop}} \approx \left(\frac{E_{trop}}{F_{ST}+E_{trop}}\right)\Delta_{36,\text{Pequil}} + \left(\frac{F_{ST}}{F_{ST}+E_{trop}}\right)\Delta_{36,\text{strat}} \qquad (7)$$

565

566   Here, E_{trop} (mol yr^{-1}) is the effective integrated isotope-exchange flux in the troposphere, F_{ST} (mol yr^{-1}) is

567   the STT flux of O_2, $\Delta_{36,\text{Pequil}}$ is the global effective-mean $\Delta_{36,ss}$ value for the troposphere, and $\Delta_{36,\text{strat}}$

568   is the global effective-mean Δ_{36} value of air descending from the stratosphere into the troposphere. Note

569   that the Δ_{36Pt} and Δ_{36Ps} values calculated online in the simulations correspond to $\Delta_{36,\text{Pequil}}$ and $\Delta_{36,\text{strat}}$

570   values, respectively.

571   Previously, the quantities in eq. 7 were determined using a chemical tropopause (150 ppb O_3), an

572   empirical $\Delta_{36,\text{strat}}$ value, and model-derived E_{trop} and $\Delta_{36,\text{Pequil}}$ values because online calculations were not

573   yet available [*Yeung et al.*, 2016; *Yeung et al.*, 2019]. The resulting balance yielded $\Delta_{36,\text{trop}}$ values similar

574   to observations. However, the modeling results reported herein suggest that the previous approach was

575   not internally consistent. For example, using the offline scheme described in *Yeung et al.* [2016], one

576   would derive a $\Delta_{36,\text{Pequil}}$ value of 1.45‰ and a $\Delta_{36,\text{trop}}$ value of 1.64‰ for the present day, both of which

577   are much lower than the corresponding quantities obtained from the online calculation ($\Delta_{36,\text{Pt}} = 1.83$‰

578   and $\Delta_{36,\text{trop}} = 1.97$‰). Thus, it is useful to examine how the online and offline calculations might be

579   reconciled, both to correct any conceptual disparities that may exist and to improve our understanding of

580   the online model results.

581   First, we will examine how $\Delta_{36,\text{Pequil}}$ and $\Delta_{36,\text{Pt}}$ values can be reconciled. By comparing the $\Delta_{36,\text{Pequil}}$

582   and $\Delta_{36,\text{Pt}}$ values obtained for present-day and preindustrial simulations, we find that online Δ_{36Pt} values

583   are most closely reproduced by the weighting scheme below:

584

585    $$E_{trop} = \frac{\sum_{trop\ grid\ boxes} k_{exch}(T)[O(^3P)][O_2]m_{box}\rho_{box}^n}{\sum_{trop\ grid\ boxes} m_{box}\rho_{box}^n} \times V_{trop} \qquad (8)$$

586

587    $$\Delta_{36,Pequil} = \frac{\sum_{trop\ grid\ boxes} k_{exch}(T)[O(^3P)][O_2]m_{box}\rho_{box}^n\Delta_{36,Pequil,box}}{\sum_{trop\ grid\ boxes} k_{exch}(T)[O(^3P)][O_2]m_{box}\rho_{box}^n} \qquad (9)$$

588

589   Each equation represents the annual tropospheric mean obtained by weighting contributions from

590   different processes within each tropospheric grid box. The first term in the numerators of both equations,

591    $k_{\text{exch}}(T)[O(^3P)][O_2]$, is the local rate of isotope exchange in units of concentration per unit time; m_{box} is the

592   mass of air used to normalize for the variable size of grid boxes, and V_{trop} is the volume of the troposphere

593   determined using the "FracOfTimeInTrop" field in GEOS-Chem (which uses the local World

594   Meteorological Organization lapse-rate tropopause to determine the average mass fraction of each grid

595   cell residing in the troposphere over each time-step).

596   The $\rho_{box}{}^{n}$ term represents the balance between two factors: the efficiency of isotope reordering

597   and the cumulative residence time within each grid box. These two factors influence how much isotope

598   exchange will drive the Δ_{36} value toward $\Delta_{36,ss}$ in each box. The isotope-reordering efficiency varies

599   inversely with the number density ρ_{box} (i.e., $n = -1$) because isotopic steady state is reached more quickly

600   when fewer O_2 molecules are present—fewer exchange events are required. The cumulative residence

601   time was previously argued to vary directly with the number density ρ_{box} (i.e., $n = 1$) [*Yeung et al.*, 2016].

602   Assuming ergodicity in a well-stirred troposphere—i.e., the ensemble mean being equal to the temporal

603   mean—higher number densities imply longer residence times for air molecules in those boxes.

604   The value of n that reproduces the Δ_{36Pt} value for 2015 is –0.8, indicating that the isotope-

605   exchange efficiency in each grid box is much more important than the relative air parcel residence time

606   for determining tropospheric Δ_{36} values. For example, in the upper troposphere, GEOS-Chem predicts

607   molar isotope-exchange rates that are roughly ten times faster than at the surface ($\tau_{exch} \sim 10^2$ vs. 10^3 days;

608   see Fig. 5). Number densities are also about tenfold lower in the upper troposphere. Together, these two

609   properties make isotope exchange ~100 times faster in the upper troposphere than at the surface.

610   Atmospheric mixing counteracts the effects of residence-time differences between the lower and upper

611   troposphere, further amplifying the importance of isotope exchange in the upper troposphere. Isotope

612   exchange in the upper troposphere thus appears to be the dominant contribution to the $\Delta_{36,Pequil}$ value. The

613   optimal value of n, however, depends on the balance of chemistry and transport, and thus may be model-

614   and climate-dependent: faster rates of isotope exchange decrease the importance of residence-time

615   differences (e.g., $n = -1$ was optimal for the $+2\sigma$ simulation) while slower rates of isotope exchange

616   increase their importance (e.g., $n = -0.3$ for the -2σ simulation). Yet, calculated PI-PD differences in

617     $\Delta_{36,Pequil}$ changed <0.002‰ upon varying the value of n between –1 and –0.3.

618   Using eq. 8 above, one can also evaluate the relative importance of different regions to the

619   present-day $\Delta_{36,Pequil}$ value. The results show that the major contribution to the annual-mean $\Delta_{36,Pequil}$ value

620   comes from the low- and mid-latitude free troposphere in GEOS-Chem/MERRA2 (Fig. 9). Peaks in

621   boreal spring and summer in the extratropics were identified, indicating that both STT of O_3 and

622   anthropogenic emissions influence the seasonal $\Delta_{36,Pequil}$ value by accelerating $O(^3P) + O_2$ isotope

623   exchange reactions locally. Integrated annually and globally, the mean effective altitude for tropospheric

624   photochemistry is 10.1 km, with a broad 1σ-equivalent width of approximately ±4.5 km about the mean.

625   This effective mean altitude is higher than that previously reported (~5 km; [*Yeung et al.*, 2016]) and

626 reflects the greater importance of upper-tropospheric photochemical reordering uncovered in this study.

627 The zonal distribution is similar to that of Earth's surface area, with a maximum in isotope-exchange flux

628 in the relatively cloud-free subtropics (Fig. 9). The tropospheric contribution to the Δ_{36} budget is therefore

629 sensitive to photolysis, chemistry, and temperature of the free troposphere on the global scale.

630 Next, we compare the modeled $\Delta_{36,Ps}$ value with the empirically determined $\Delta_{36,strat}$ value. The

631 latter depends strongly on how the tropopause is defined, and its accuracy is limited by the number and

632 spatiotemporal coverage of available observations. Our Northern-Hemisphere observations currently

633 suggest that the $\Delta_{36,strat}$ value is between 2.2 and 2.3‰ when using $\theta = 380$ K or 150 ppb O_3 as the

634 effective Δ_{36} tropopause (Fig. 5). The modeled $\Delta_{36,Ps}$ value of 2.43‰ therefore appears to be $0.1 - 0.2$‰

635 higher than the observed $\Delta_{36,strat}$ value (Table 2). Seasonality may be responsible for this apparent

636 disagreement. Within the model, the annual-mean $\Delta_{36,Ps}$ value is closest to Δ_{36} values at $\theta = 380$ K during

637 boreal spring, when net STT fluxes are strongest [*Holton et al.*, 1995; *Appenzeller et al.*, 1996]. However,

638 the majority of lower-stratospheric measurements to date were sampled during boreal autumn, when net

639 mass transport moves mass in the opposite direction, i.e., from the troposphere into the stratosphere. One

640 therefore expects the boreal autumn-biased $\Delta_{36,strat}$ values to be lower than the annual-mean Δ_{36Ps} value

641 because the fraction of unaltered tropospheric air (e.g., f_{trop}) is larger in boreal autumn than in spring. The

642 current set of observations therefore provides an incomplete constraint on Δ_{36Ps}. Nevertheless, the

643 observed seasonal bias is consistent with that expected from the seasonality of stratosphere-troposphere

644 exchange; no inconsistencies are evident.

645 The preceding discussion thus provides a way to obtain the tropospheric terms of eq. 7: when

646 $\Delta_{36Pt} = \Delta_{36,Pequil}$, the online and offline descriptions are equivalent, and yields $E_{trop} = 1.4 \times 10^{19}$ mol O_2 yr^{-1}.

647 The Δ_{36Ps} value (2.43‰) and online $\Delta_{36,trop}$ value (1.97‰) then allow one to solve for F_{ST}, which is

648 inferred to be 4.3×10^{18} mol O_2 yr^{-1}. This F_{ST} value is similar to the net STT flux derived from seasonal

649 diabatic transport across the $\theta = 380$ K surface in the extratropics used in our previous studies (i.e., $4.6 \times$

650 10^{18} mol O_2 yr^{-1}; [*Appenzeller et al.*, 1996; *Schoeberl*, 2004]) and is consistent with the 1-2 month mean

651 residence time of air in the extratropical lowermost stratosphere (cf., Fig. 8). The present-day Δ_{36} value at

652 the surface is thus comprised of 77% tropospherically reordered air and 23% stratospherically reordered

653 air in steady state.

654 We note that the MERRA2 STT flux reported in *Boothe and Homeyer* [2017], i.e., $F_{ST,BH} = 1.2 \times$

655 10^{19} mol O_2 yr^{-1}, is threefold larger than the estimate above and would result in an inconsistency of

656 ~0.1‰ in $\Delta_{36,trop}$ values, with the box model yielding $\Delta_{36,trop} = 2.11$‰. This inconsistency arises because

657 the residence-time threshold used for determining "irreversible" STT trajectories in *Boothe and Homeyer*

658 [2017] is much shorter than typical isotope-exchange lifetimes in the lowermost stratosphere (e.g., 4 days

659 vs. 1-2 months). Consequently, the STT mass flux from the analysis of *Boothe and Homeyer* [2017]

660   includes many tropopause-crossing transients that leave Δ_{36} values largely unaltered in an air parcel; the

661   value of F_{ST} relevant for the global Δ_{36} budget should be smaller. *Škerlak et al.* [2014] found that STT

662   fluxes based on trajectory studies scale inversely with the square root of the STT residence-time

663   threshold. That scaling relationship predicts that high-Δ_{36} stratospheric air becomes irreversibly mixed

664   into the troposphere about a month after descending below $\theta = 380K$, i.e., $F_{ST}/F_{ST,BH} \sim (4\ \text{days} / 30$

665   days$)^{1/2}$, consistent with the expected isotope-exchange lifetime at those altitudes.

666   In summary, the two-box framework for the atmospheric Δ_{36} budget can be reconciled with the

667   online simulations after a more accurate accounting of photochemical reordering in the upper troposphere

668   and the STT flux relevant for Δ_{36}. This new analysis reveals that the effective mean altitude interrogated

669   by the tropospheric Δ_{36} tracer is 10 km rather than ~5 km, which was previously suggested [*Yeung et al.*,

670   2016]. The previous approach had underweighted isotope exchange in the upper troposphere because it

671   did not consider the faster approach to isotopic steady state at low number densities. Importantly, the

672   consistency between the online and offline approaches allows one to rapidly evaluate the importance of

673   perturbations (e.g., temperature changes) on past tropospheric Δ_{36} values without requiring additional

674   online simulations.

675

676   **4.3 Changes in the Δ_{36} budget and O_3 since the preindustrial era**

677   Previous work documented a tropospheric Δ_{36} decrease over the twentieth century associated with

678   an increased tropospheric O_3 burden [*Yeung et al.*, 2019]. Online Δ_{36} calculations and diagnostics allow us

679   to analyze the GEOS-Chem/MERRA2 results here in more detail and estimate the magnitude of known

680   systematic uncertainties, facilitating a more quantitative comparison with the atmospheric record. The PI

681   and PD simulation results can be summarized as follows: the increase in tropospheric O_3 since 1850 CE

682   yields a predicted $\Delta_{36,\text{trop}}$ decrease of 0.06‰. The magnitude of the $\Delta_{36,\text{trop}}$ decrease is caused by (*i*) the

683   locus of $O(^3P) + O_2$ isotope exchange shifting toward the Northern Hemisphere and lower altitudes (Fig.

684   10), resulting in the $\Delta_{36,\text{Pequil}}$ value decreasing by 0.04‰ (Table 2), and (*ii*) the effective integrated

685   isotope-exchange flux in the troposphere (E_{trop}) increasing by ~30%. We note that the uncertainty bounds

686   derived from online simulations run at the $\pm 2\sigma$ limits for $k_{\text{exch}}(T)$ are <0.005‰ for the PI-to-PD shift in

687   Δ_{36P}.

688   We will now estimate the known systematic uncertainties. First, the modeled changes reflect

689   present-day meteorology and thus omit the ~1°C global warming since 1850 C.E. This warming has two

690   potentially opposing effects on the mean tropospheric Δ_{36} value: to decrease $\Delta_{36,\text{Pequil}}$ further and to

691   increase F_{ST}. The two-box framework suggests that a 1°C tropospheric warming would cause an

692   additional 0.01‰ decrease in $\Delta_{36,\text{Pequil}}$, if all else is kept unchanged (Fig. 11). However, anthropogenic

693   warming is believed to have also accelerated the lower branch of the Brewer-Dobson circulation by

694   ~10%, which would increase F_{ST} [*Lin and Fu*, 2013]. Using the effective present-day F_{ST} of 4.3×10^{18}

695   mol O_2 yr^{-1} across the tropopause and the model-derived quantities $E_{trop} = 1.1 \times 10^{19}$ mol O_2 yr^{-1}, $\Delta_{36,strat} =$

696   2.43‰, and $\Delta_{36,Pequil} = 1.87$‰ for the PI, we calculate that a 10% smaller STT flux during the PI results in

697   a 0.01‰ smaller PI-PD shift in global-mean tropospheric Δ_{36} value. Consequently, the two opposing

698   effects of the 1°C warming since the preindustrial cancel within the tropospheric Δ_{36} budget.

699   Second, interannual variability in meteorology can affect both the magnitude of F_{ST} and the

700   effective chemistry/transport balance (i.e., the exponent *n* in eqs. 8 and 9). Our explorations of these

701   effects suggest that interannual variability about long-term means contributes ~0.01‰ uncertainty to the

702   global-mean $\Delta_{36,trop}$ value for a given emissions scenario and climate state. For example, the mean Δ_{36P},

703   Δ_{36Pt}, and Δ_{36Ps} values for GEOS-Chem/MERRA2 simulations from June 1998 – June 2000 were all

704   0.01‰ higher than in 2015 despite comparable global pollutant emissions [*McDuffie et al.*, 2020].

705   Third, the biomass burning emissions of nitrogen oxides (NO_x) and carbon monoxide (CO) are

706   still uncertain in the preindustrial atmosphere. Recent studies suggest that preindustrial biomass burning

707   emissions were higher than they are in the present, by as much as 40% for CO and 20% for NO_x

708   [*Rowlinson et al.*, 2020], perhaps due to land-use change [*Pfeiffer et al.*, 2013; *Andela et al.*, 2017;

709   *Hamilton et al.*, 2018]. Such "high-fire" NO_x and CO emissions from biomass during the PI would reduce

710   the PI-to-PD increase in tropospheric O_3 burden from 34% to 15% [*Murray et al.*, 2014]) and thus also

711   mute the change in tropospheric Δ_{36} value. Taking the change in tropospheric O_3 burden as a proxy for

712   E_{trop}, the "high-fire" scenario would reduce the PI-to-PD change in tropospheric Δ_{36} value by 0.01‰.

713   Finally, the modeled tropospheric Δ_{36} change over the GISP2 (Summit, Greenland) ice coring site

714   is 0.01‰ larger than over the WAIS-D (West Antarctica) ice coring site in both calculation schemes,

715   reflecting a larger O_3 reduction in the Northern hemisphere. However, this small difference would not be

716   detectable by current analytical methods. Nevertheless, averaging measurements from the Northern and

717   Southern hemispheres provides a more robust estimate of the global tropospheric Δ_{36} value and its

718   changes through time.

719   This explicit quantification of potential systematic uncertainties in the online Δ_{36} calculation

720   suggests that the modeled decrease in tropospheric Δ_{36} since 1850 C.E. is 0.06 ± 0.02‰ (2σ based on

721   uncertainties added in quadrature), consistent with the mean 0.03 ± 0.02‰ decrease (95% confidence

722   interval) observed in the ice-core record [*Yeung et al.*, 2019]. Despite some uncertainty in the modeled

723   absolute Δ_{36} values arising from the isotopic photochemistry of O_3, the associated systematic uncertainties

724   likely do not contribute more than 0.02‰ to modeled changes in tropospheric Δ_{36} value. Preindustrial

725   scenarios invoking higher biomass-burning emissions NO_x and CO [*Rowlinson et al.*, 2020] would likely

726   yield an estimated $\Delta_{36,trop}$ change closer to the centroid of the observed probability density distribution.

727

5. Conclusions

The observational, modeling, and experimental evidence presented in this study all suggest that the titration of $^{18}O^{18}O$ into heavy ozone molecules—an atmospheric sink for $^{18}O^{18}O$ that was previously thought to be negligible—drives Δ_{36} values toward a photochemical steady state that differs from isotopic equilibrium. An online parameterization of this effect within the GEOS-Chem chemical transport model, based on pressure- and temperature-dependent outputs of a detailed isotope-enabled kinetics model, allows GEOS-Chem to reproduce high-precision laboratory measurements on atmospheric samples collected over a range of latitudes, altitudes, seasons, and years. This improved understanding of the factors that affect atmospheric Δ_{36} values, however, results in only minor changes to the predicted evolution in tropospheric Δ_{36} values over the twentieth century in response to the increase in tropospheric O_3; thus, the Δ_{36} tracer remains a constraint on the global preindustrial O_3 burden. Analytical precision in Δ_{36} measurements and uncertainties surrounding preindustrial biomass burning emissions currently dominate the uncertainty in the measurement-model comparison of PI and PD Δ_{36} values, with the PI-PD change in Δ_{36} values consistent with no more than a 30-40% increase in the tropospheric O_3 burden since 1850 C.E.

Furthermore, the online Δ_{36} calculation scheme described herein allows variations in odd-oxygen chemistry and free-troposphere temperatures—manifesting as changes tropospheric Δ_{36} values—to be investigated for past climates within chemical-transport and chemistry-climate models. While O_3 photochemistry and climate are linked through biogeochemistry and atmospheric dynamics [*Alexander et al.*, 2003; *Rind et al.*, 2009; *Murray et al.*, 2014; *Geng et al.*, 2017; *Wang et al.*, 2020], Δ_{36} may nevertheless offer a valuable constraint on the long-term coevolution of atmospheric chemistry and climate.

Data Availability

761   The measured data and model outputs used to support the conclusions can be accessed at Zenodo
762   link to be posted prior to publication.
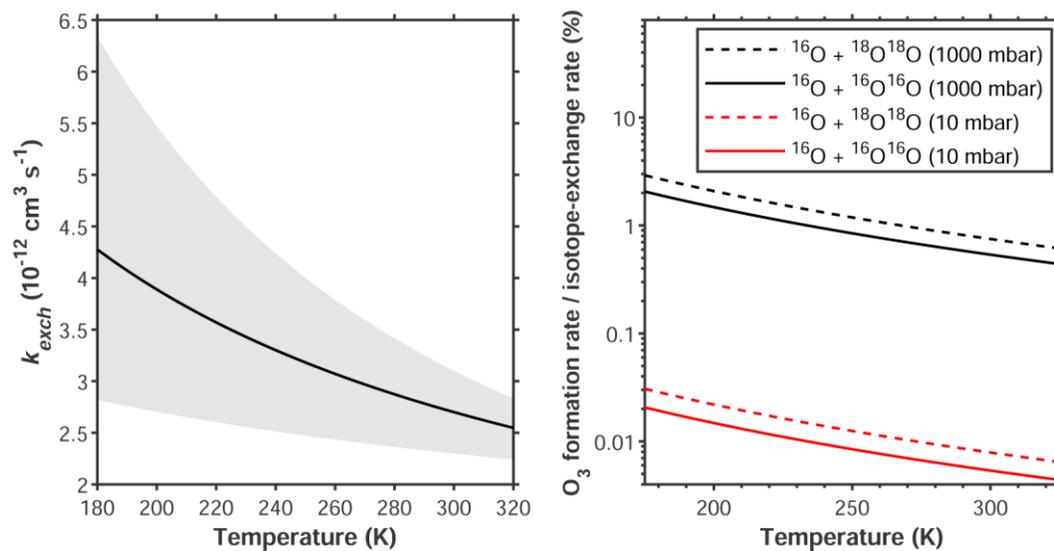
Figure 1. (Left) Temperature dependence of the bimolecular rate coefficient for the $^{16}O + {}^{18}O^{18}O$ isotope-exchange reaction obtained from the combined laboratory/theory study of *Fleurat-Lessard et al.* [2003]. Shaded area represents experimental 2σ uncertainty range. (Right) The ratios of O_3-formation and isotope-exchange rates for $^{16}O + {}^{16}O^{16}O$ and $^{16}O + {}^{18}O^{18}O$ collisions at different pressures, which shows relative rates of O_3 formation that are markedly faster for $^{16}O + {}^{18}O^{18}O$ collisions at high pressures and low temperatures.
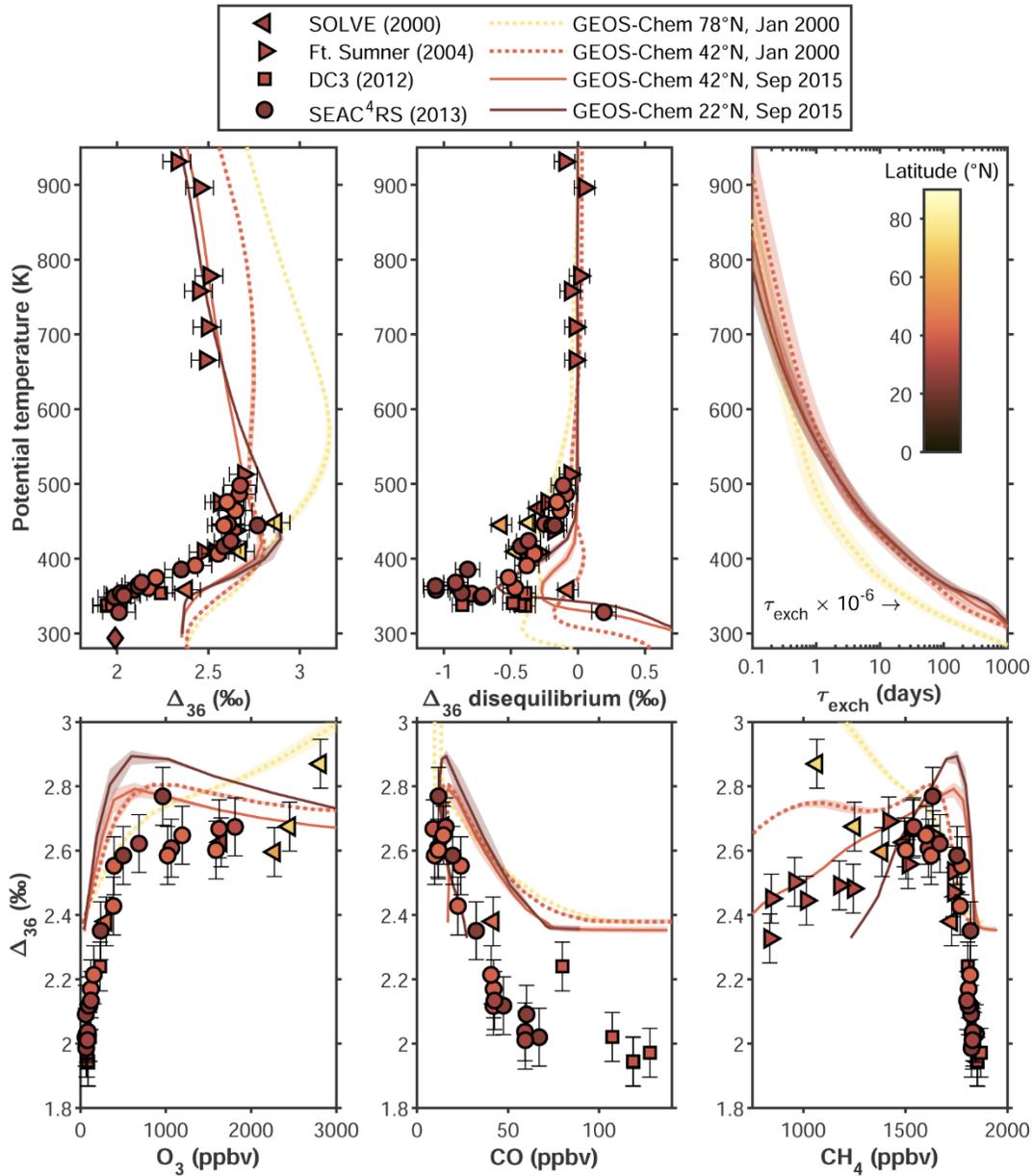
Figure 2. Measurement-model comparison for the O₂-only online Δ₃₆ calculation scheme in GEOS-Chem. Error bars on the data points represent the 1σ pooled standard deviation of duplicates. Modeled monthly means from January 2000 and September 2015 are plotted for comparison. Shaded areas represent pseudo-2σ uncertainty bounds obtained by running identical simulations at the experimental ±2σ bounds for k_{exch}(T). Note that the isotope-exchange lifetime for the 78°N, January 2000 profile is scaled by 10^{-6} for clarity.
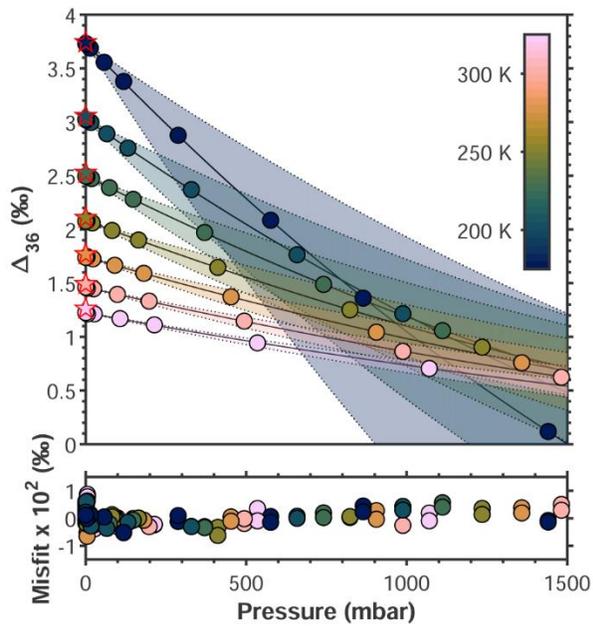
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Figure 3. $\Delta_{36,ss}$ vs. pressure from the isotope-enabled photochemical kinetics model for a range of temperatures (filled circles) compared to polynomial fits of the trends (curves). For reference, Δ_{36} values for isotopic equilibrium (i.e., $\Delta_{36,equil}$) are shown as stars on the left axis. Deviations of $\Delta_{36,ss}$ from $\Delta_{36,equil}$ values at 0.1 mbar range from –0.01‰ at 175K to –0.04‰ at 300K. The lower plot shows the misfit between the modeled $\Delta_{36,ss}$ compositions and polynomial fits to those values.

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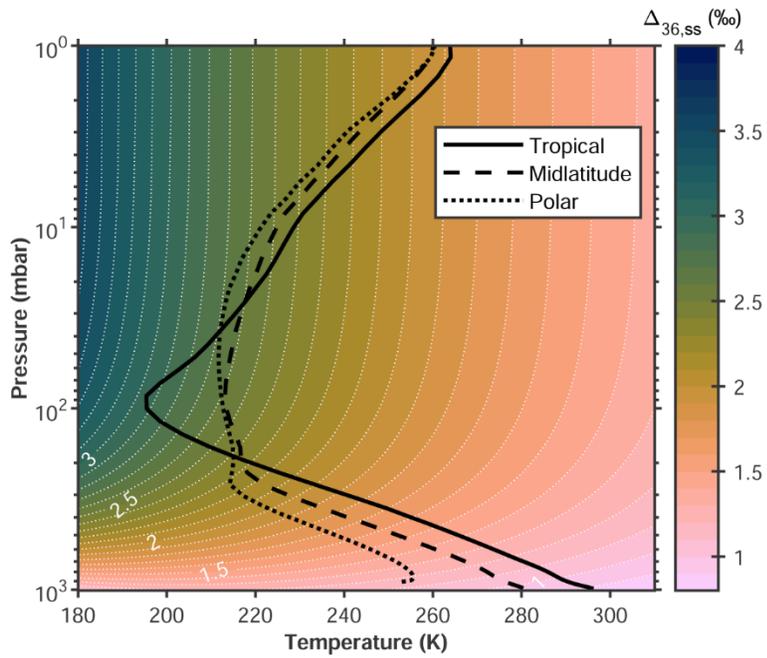
Figure 4. Trends in $\Delta_{36,ss}$ along atmospheric covariations of temperatures and pressures. Modern zonal-mean atmospheric temperature profiles for tropical (30°S – 30°N), midlatitude (30°S – 60°S and 30°N – 60°N), and polar (60°S – 90°S and 60°N – 90°N) latitudes from the MERRA2 reanalysis are overlain.
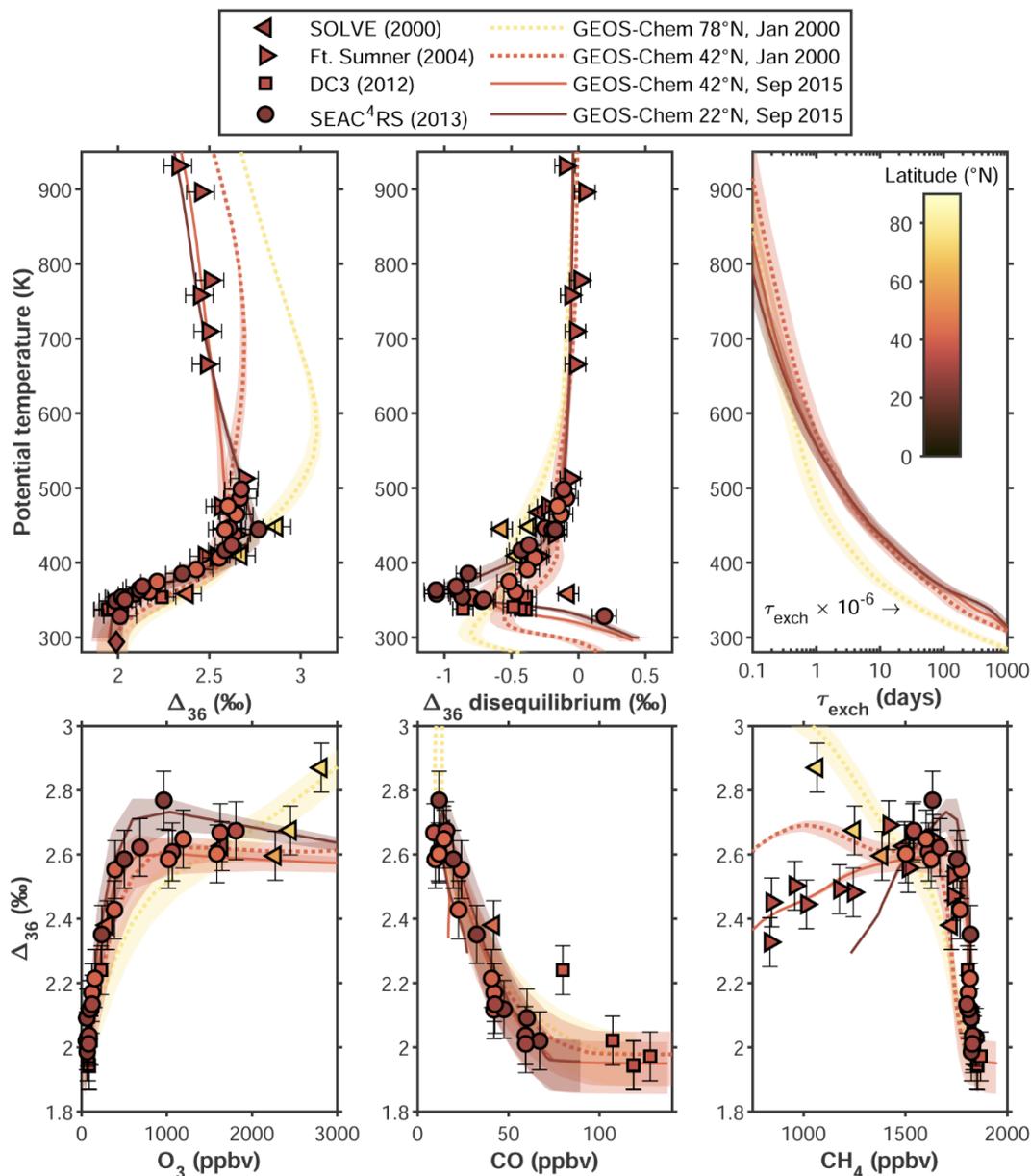
Figure 5. Measurement-model comparison for the pressure-dependent online Δ_{36} calculation scheme in GEOS-Chem. Error bars on the data points represent the 1σ pooled standard deviation of duplicates. Modeled monthly means from January 2000 and September 2015 are plotted for comparison. Shaded areas represent pseudo-2σ uncertainty bounds obtained by running identical simulations at the experimental ±2σ bounds for $k_{exch}(T)$. Note that the isotope-exchange lifetime for the 78°N, January 2000 profile is scaled by 10^{-6} for clarity.
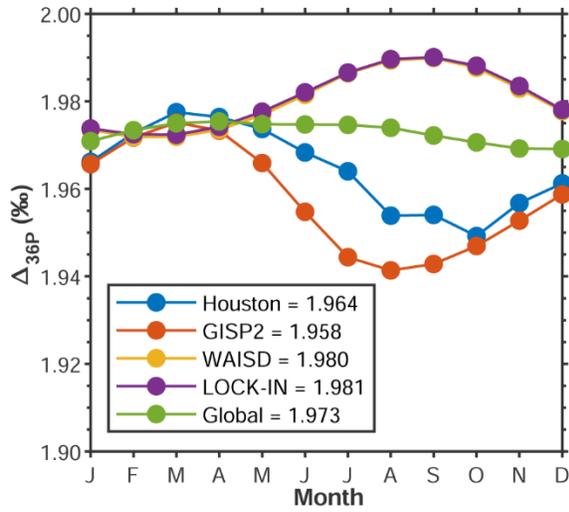
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Figure 6. Modeled seasonal cycle of surface Δ_{36P} values at various sites in 2015. The modeled global-
mean surface Δ_{36P} value is also shown. Ice-coring site locations are Summit, Greenland (GISP2; 72.6ºN,
38.5 ºW), the West Antarctic Ice Sheet Divide (WAISD; 79.5ºS, 112.1ºW) and East Antarctica near
Dome C (LOCK-IN; 74.1ºS, 126.2ºE).
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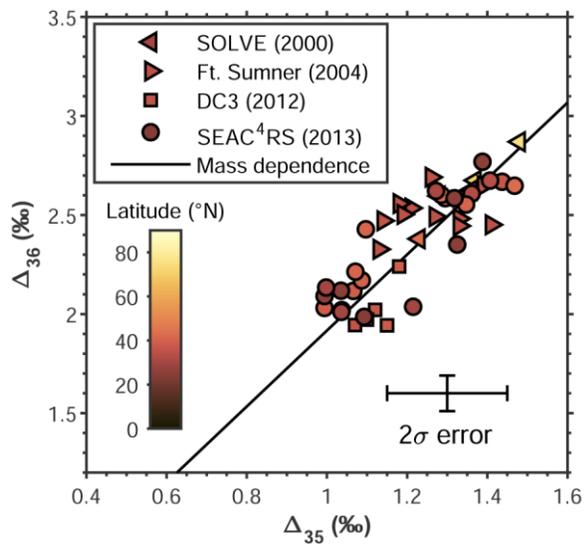
Figure 7. Comparison of Δ_{36} and Δ_{35} values measured on the same samples, which show a mass-dependent trend.
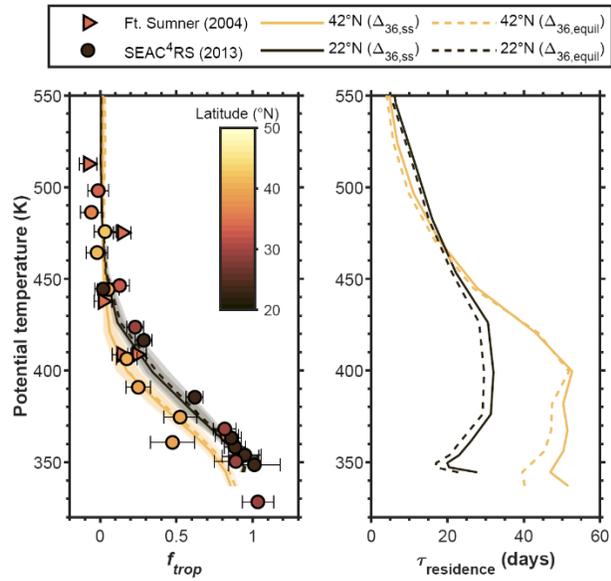
Figure 8. Measurement-model comparison of stratosphere-troposphere mixing fractions (left) and implied lower-stratospheric residence times (right).
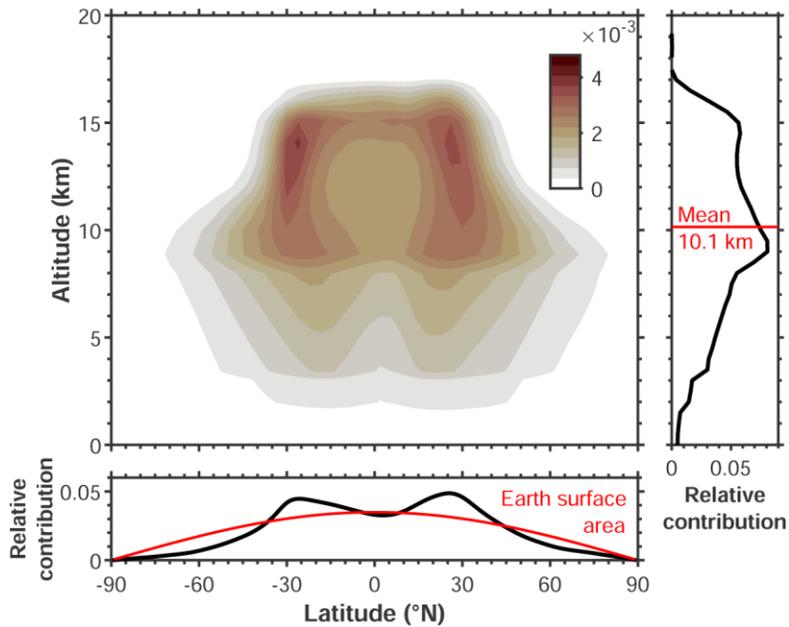
Figure 9. Contour plot depicting where O(^3P) + O$_2$ isotope-exchange chemistry records tropospheric climate (i.e., $\Delta_{36,Pt}$ or $\Delta_{36,Pequil}$; cf. eq. 7) in GEOS-Chem/MERRA2 model year 2015. Also shown are the integrated relative contributions as a function of altitude and latitude (black curves). The mean effective altitude (red line in right panel) and Earth surface area (red curve) are shown for comparison.
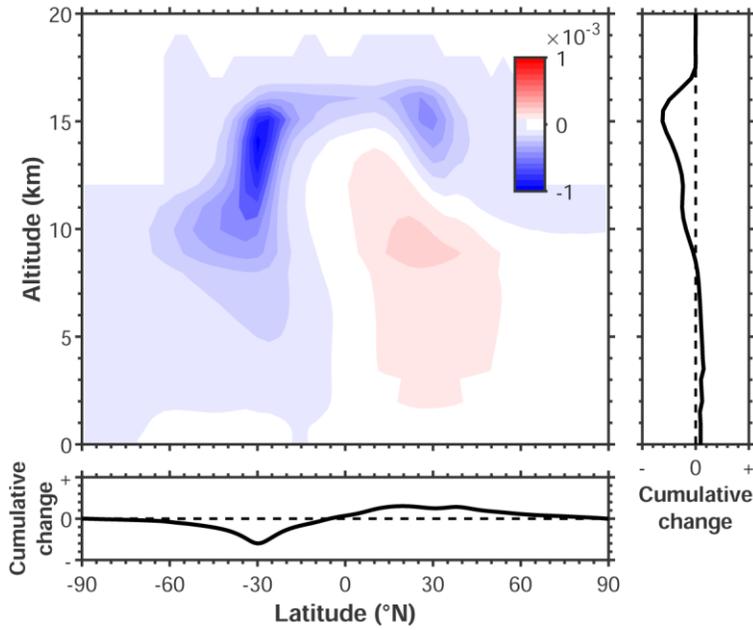
Figure 10. Changes in the distribution of tropospheric isotope-exchange chemistry between the present-day and the preindustrial scenarios in GEOS-Chem/MERRA2. Chemistry in the Northern Hemisphere, particularly at low altitudes, increases in importance relative to the Southern Hemisphere and high altitudes due to an increase in anthropogenic ozone in the troposphere near the surface.

828 **Table 1. Coefficients for $\Delta_{36,ss}$ fits. Each coefficient in $\Delta_{36,ss} = a\mathrm{P}^3 + b\mathrm{P}^2 + c\mathrm{P} + d$ is fit using the**
829 **polynomial $A\mathrm{T}^5 + B\mathrm{T}^4 + C\mathrm{T}^3 + D\mathrm{T}^2 + E\mathrm{T} + F$.**
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	A	B	C	D	E	F
Mean [$k_{16+1818} = 2.7 \times 10^{-12} (300/\mathrm{T})^{0.9}$]						
a	1.67450×10^{-21}	2.34401×10^{-18}	1.29657×10^{-15}	-3.54132×10^{-13}	4.77886×10^{-11}	-2.55820×10^{-9}
b	-7.14103×10^{-17}	1.08435×10^{-14}	-6.49426×10^{-12}	1.92717×10^{-9}	-2.85715×10^{-7}	1.72235×10^{-5}
c	2.62554×10^{-14}	3.94330×10^{-11}	2.37342×10^{-8}	-7.20271×10^{-6}	1.11512×10^{-3}	-7.21957×10^{-2}
d	-6.69867×10^{-12}	1.02273×10^{-8}	-6.32908×10^{-6}	2.01818×10^{-3}	-3.45655×10^{-1}	2.78442×10^{1}
-2σ [$k_{16+1818} = 2.3 \times 10^{-12} (300/\mathrm{T})^{0.4}$]						
a	3.57694×10^{-21}	4.77481×10^{-18}	2.53652×10^{-15}	-6.70701×10^{-13}	8.84132×10^{-11}	-4.66738×10^{-9}
b	-2.64053×10^{-17}	3.60380×10^{-14}	-1.96845×10^{-11}	5.39466×10^{-9}	-7.45832×10^{-7}	4.20735×10^{-5}
c	7.81517×10^{-14}	1.09547×10^{-10}	6.18342×10^{-8}	-1.76614×10^{-5}	2.57586×10^{-3}	-1.56147×10^{-1}
d	-8.20053×10^{-12}	1.21061×10^{-8}	-7.25720×10^{-6}	2.24431×10^{-3}	-3.72815×10^{-1}	2.91308×10^{1}
+2σ [$k_{16+1818} = 3.1 \times 10^{-12} (300/\mathrm{T})^{1.4}$]						
a	2.05428×10^{-21}	2.73672×10^{-18}	1.44666×10^{-15}	-3.79007×10^{-13}	4.91901×10^{-11}	-2.53351×10^{-9}
b	-8.19913×10^{-18}	1.12586×10^{-14}	-6.16633×10^{-12}	1.68755×10^{-9}	-2.32094×10^{-7}	1.30447×10^{-5}
c	1.72122×10^{-14}	2.47728×10^{-11}	1.43647×10^{-8}	-4.22404×10^{-6}	6.38706×10^{-4}	-4.10595×10^{-2}
d	-6.92907×10^{-12}	1.04446×10^{-8}	-6.39831×10^{-6}	2.02497×10^{-3}	-3.45166×10^{-1}	2.77545×10^{1}

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834 **Table 2. Comparison of the predicted PI-PD change in Δ_{36} values and diagnostics.**

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		O$_2$-only			Pressure-dependent		
		$\Delta_{36,surface}$	Δ_{36t}	Δ_{36s}	$\Delta_{36,surface}$	Δ_{36Pt}	Δ_{36Ps}
Mean							
	2015	2.372	2.271	2.712	1.973	1.832	2.430
	1850	2.418	2.302	2.710	2.033	1.871	2.428
	Change	*0.046*	*0.031*	*-0.002*	*0.060*	*0.039*	*-0.002*
-2σ							
	2015	2.379	2.253	2.712	1.874	1.691	2.346
	1850	2.427	2.283	2.710	1.939	1.730	2.344
	Change	*0.048*	*0.030*	*-0.002*	*0.065*	*0.039*	*-0.002*
+2σ							
	2015	2.367	2.286	2.712	2.042	1.934	2.489
	1850	2.411	2.318	2.710	2.100	1.973	2.488
	Change	*0.044*	*0.032*	*-0.002*	*0.058*	*0.039*	*-0.001*

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Figure 1.
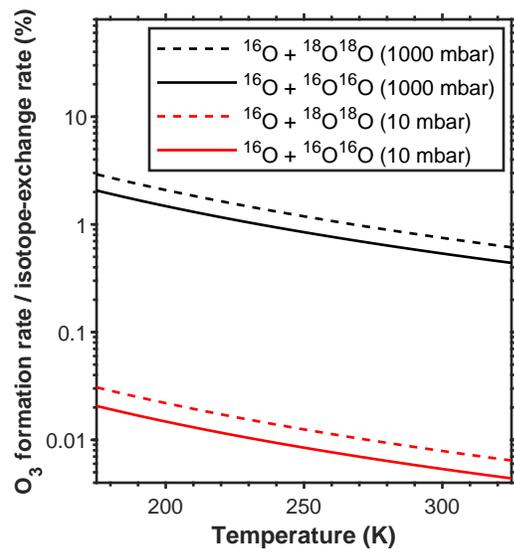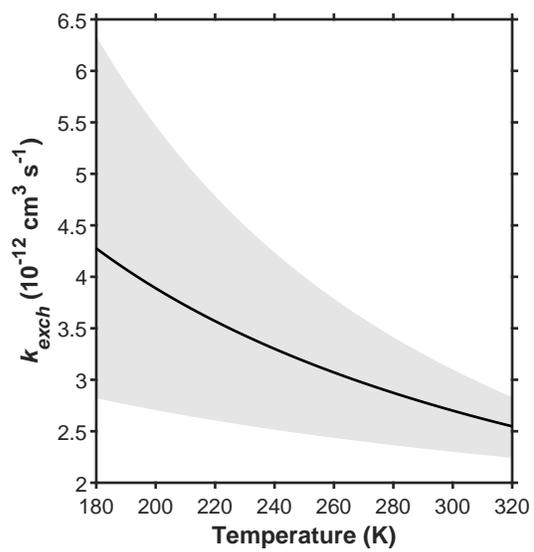
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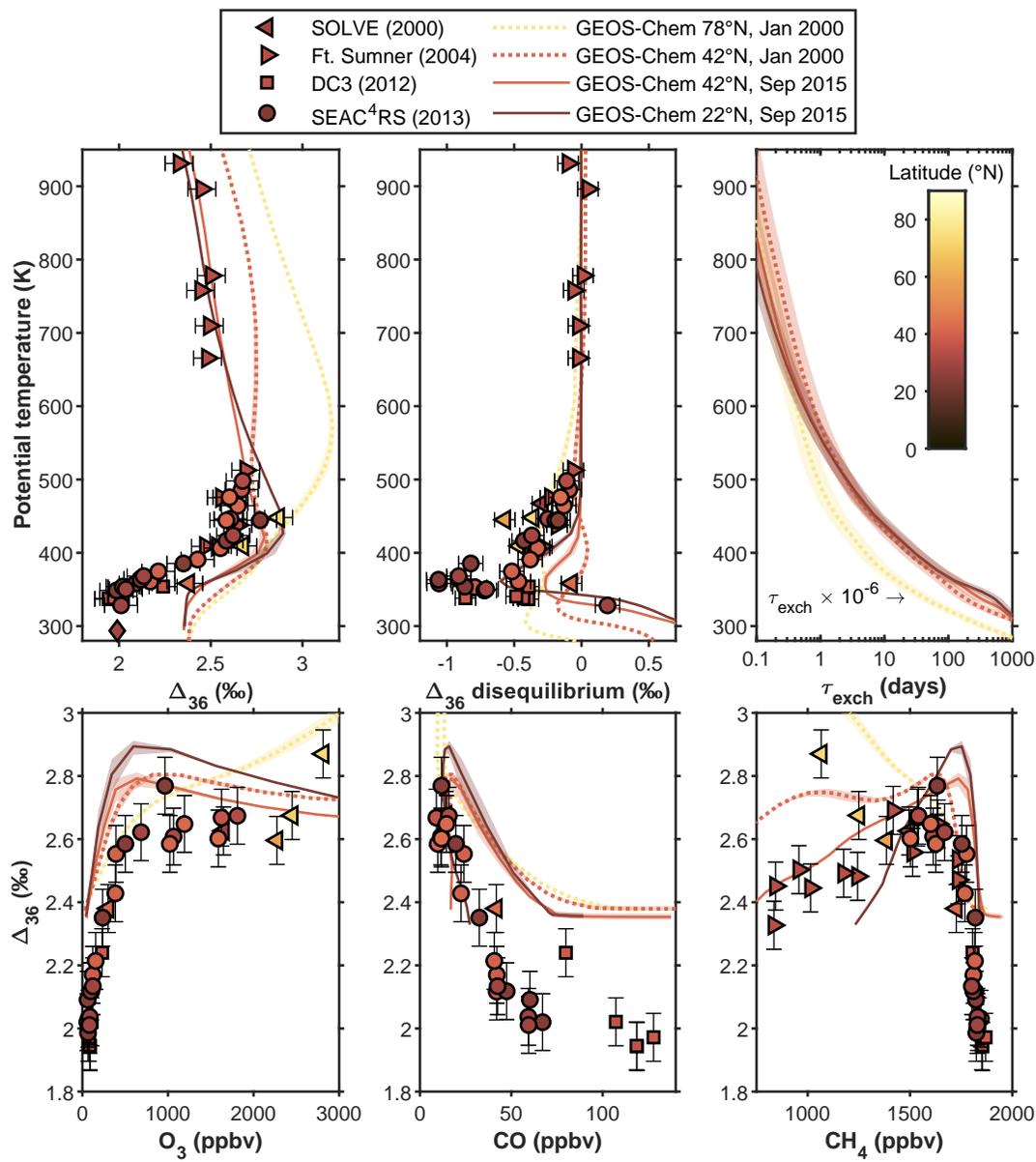
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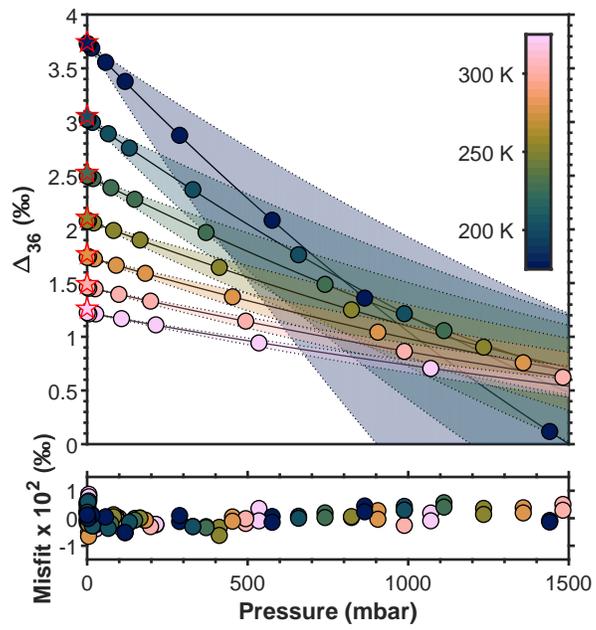
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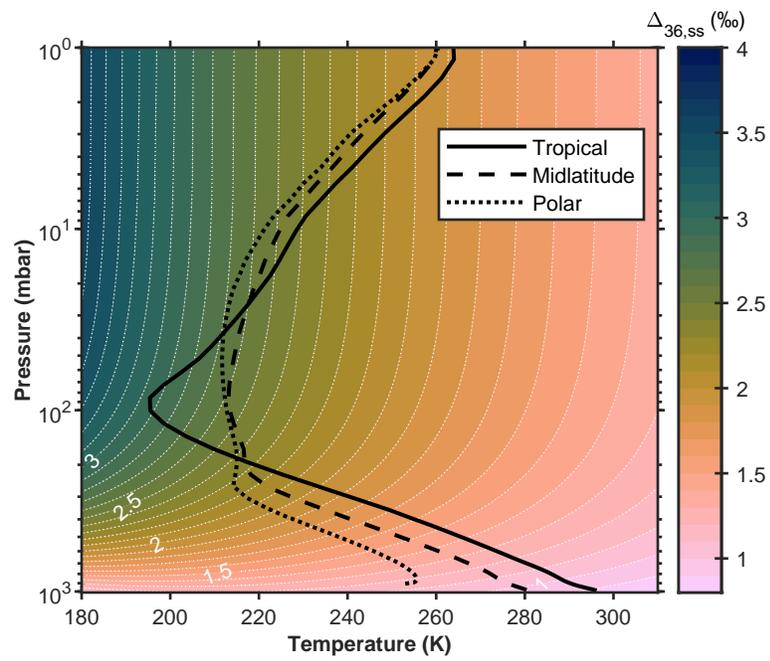
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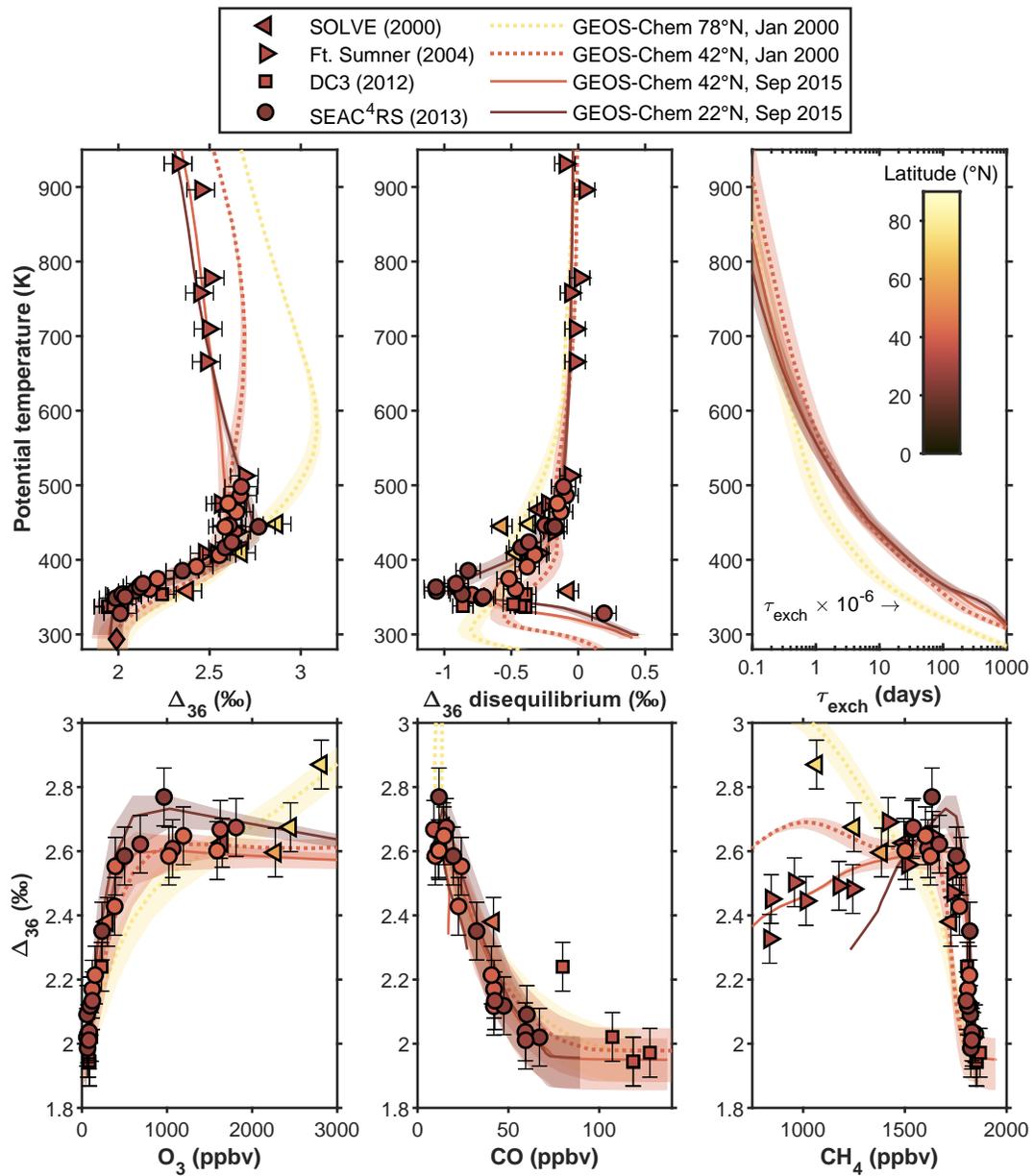
Figure 6.

Figure 7.

Figure 8.

Legend:
▷ Ft. Sumner (2004)   42°N ($\Delta_{36,ss}$) — — 42°N ($\Delta_{36,equil}$)
● SEAC^{4}RS (2013)   22°N ($\Delta_{36,ss}$) — — 22°N ($\Delta_{36,equil}$)

Left panel axes: Potential temperature (K) vs f_{trop}; inset colorbar Latitude (°N).
Right panel axis: $\tau_{residence}$ (days).

Figure 9.

Mean
10.1 km

Relative
contribution

Altitude (km)

Latitude (°N)

Earth surface
area

Relative
contribution

Relative
contribution

$\times 10^{-3}$

Figure 10.