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Temporal Evolution of Flux Tube Entanglement at the Magnetopause as Observed by the MMS Satellites

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Key Points:

- 14 • 17 entanglement events are identified.
- 15 • Entanglement occurs more often under By-dominated IMF.
- 16 • Entanglement evolves in three distinguishable stages

17

18 **Abstract**

19 Flux transfer events (FTEs), as flux ropes (FRs), are considered key agents for solar wind
20 energy to enter the terrestrial magnetosphere. Recent observations identify entangled flux tubes
21 that collide and pull against each other. Reconnection occurs to disentangle and produce a new
22 pair of flux ropes with different connectivity. In this paper, we examine how such an
23 entanglement process evolve in time by comparing 17 entanglements observed by the
24 Magnetospheric Multiscale (MMS) mission. The B_y -dominated interplanetary magnetic field
25 (IMF) distribution of the entangled tubes agrees with previous findings. We have identified three
26 evolutionary stages characterized by the magnetic field and pressure enhancement. Our study
27 confirms the flux rope nature of these events and explains how a disparate pair of ropes is
28 formed from two entangled flux tubes, each initially connected to a different hemisphere of the
29 magnetosphere.
30

31 **Plain Language Summary**

32 The Earth's intrinsic magnetic field deflects the solar wind flow at a boundary called the
33 magnetopause. Near this boundary, twisted flux tubes are found when the external field in the
34 solar wind is southward. Such tubes may become entangled if they move towards each other, say
35 from the southern and northern hemispheres. This study analyzes 17 events like this and
36 identifies three evolutionary stages as the entanglement proceeds. The results improve our
37 understanding of not only the complex coupling between solar wind and the Earth's magnetic
38 field, but other similar processes in space plasma.
39

40 **1 Introduction**

41 Flux transfer events (FTEs) were first observed by the ISEE 1 and 2 spacecraft and were
42 interpreted as generated by patchy and impulsive reconnection near the sub-solar point (Russell
43 & Elphic, 1979). Following the first discovery, other generation models were raised, including
44 the multiple X-line model by Lee & Fu (1985), and a single X-line model with a time-varying
45 reconnection rate (Scholer, 1988; Southwood et al., 1988). The different generation mechanisms
46 may be associated with different upstream conditions and could result in different magnetic field
47 topology and connectivity within/around the FTE (Dorelli & Bhattacharjee, 2009; Hesse et al.,
48 1990; Hwang et al., 2020; Pu et al., 2013). Despite differences in detail, all models agree that
49 reconnection plays an essential role in transferring magnetic flux. The most notable yet simple
50 feature of an FTE common to the various models is enhanced magnetic field strength, with a
51 bipolar B_N component in boundary normal coordinates, indicating that the magnetic field is
52 twisted like a rope.

53 Reconnection can happen at multiple locations simultaneously at the magnetopause; Thus
54 the motion of the flux tubes leaving reconnection sites may become intricate, especially when the
55 interplanetary magnetic field (IMF) has a large B_y component (Fargette et al., 2020; Kan, 1988;
56 Nishida, 1989; Otto, 1991; Zhao, 2019). Two flux tubes, with one end connected to the northern/
57 southern hemisphere of the Earth and the other end connected to the magnetosheath, that flow
58 away from their original reconnection sites may collide and become entangled. The magnetic
59 field becomes highly compressed around the interface of these two entangled flux tubes.

60 Secondary reconnection can occur within the flux pile-up region and alter the field line
61 connectivity. Previous three-dimensional MHD simulations (Fedder et al., 2002; Lee et al.,
62 1993), global hybrid simulations (Tan et al., 2011) and observations (Bogdanova et al., 2008; Lv
63 et al., 2016; Pu et al., 2013) have examined how reconnection enables the field topology
64 changes, and have shown four resulting magnetic field bundle topologies: one end connected to
65 the magnetosheath and the other end to the Earth's northern/southern hemisphere; both ends
66 connected to the magnetosphere; and both ends connected to the magnetosheath.

67 Recently, with the improvement of spatial and temporal resolution of instruments, direct
68 observations of flux tube entanglement/interlinked flux tubes (Fargette et al., 2020; Hwang,
69 Dokgo et al., 2020; Kacem et al., 2018; Kieokaew & Foullon, 2019; Øieroset et al., 2019) were
70 reported. These studies pointed out the differences between a classic flux rope and two
71 entangled/interlinked flux tubes: a significant pressure enhancement which violates the force-
72 balanced flux rope model (Russell et al., 2017); a sharp rotation of magnetic field at the field
73 strength peak region instead of a smooth bipolar variation in the transverse direction; and
74 disparate plasma on two sides of this thin current indicating the lack of magnetic connectivity. In
75 these studies, reconnection characteristics have been carefully identified at the entanglement
76 interface. As it proceeds, reconnection is expected to resolve the entanglement and generate a
77 new pair of flux ropes. In contrast to the initial pair which has one end connected to Earth and
78 the other to the sheath, now one rope has both ends connected in the magnetosheath while the
79 other one has both ends connected in the magnetosphere (Russell & Qi, 2020).

80 The purpose of this study is to investigate the temporal evolution of flux tube
81 entanglement, and further evaluate the impact of the reconnection between entangled flux tubes.
82 We examined 17 entanglement events. We identify the characteristics of entanglement at
83 different stages using their differences and similarities in the field line geometry, the pressure
84 profile, and electron distributions. Section 2 introduces the instruments and datasets used in this
85 study. In section 3 we use three representative events to outline the three evolutionary stages of
86 flux rope entanglement. Then we revisit a classic entanglement event with additional analysis at
87 the interface and give a full list of the 17 selected events. Then, based on three representative
88 events, the temporal evolution stages are elaborated. Section 4 includes further discussions and a
89 summary of our findings.

90

91 **2 Data and Methodology**

92 All flux tube entanglement events studied here are observed by the Magnetospheric
93 Multiscale (MMS) mission (Burch et al., 2015) during its first two dayside phases (Winter 2015-
94 2016 and Winter 2016-2017) (Fuselier et al., 2016). During these time periods, at the
95 magnetopause, the MMS maintains a tetrahedron formation at apogee with spacecraft separation
96 usually below 100 km, which allows us to analyze spatial gradients close to the electron-kinetic
97 scale. The magnetic field is measured by the fluxgate magnetometer (FGM) (Russell et al., 2014)
98 at its highest sampling rate of 128 Hz. Fast plasma investigation (FPI) instruments (Pollock et al.,
99 2016) provide the electron/ion distribution functions and moments every 30/150 ms at burst
100 mode, covering the energy range from 10 eV to 30 keV. Solar wind conditions are examined for
101 each event using measurements from the OMNI database (King & Papitashvili, 2005).

102

103 3 Observations

104 3.1 Selecting entanglement cases

105 Based on the previous case studies mentioned in the introduction section (Fargette et al.,
 106 2020; Hwang, Dokgo, et al., 2020; Kacem et al., 2018; Kieokaew & Foullon, 2019; Øieroset et
 107 al., 2019), we used the following criteria to identify the flux tube entanglement:

- 108 • A significant increase in both magnetic field strength and total pressure (the sum of
 109 plasma thermal nkT pressure and magnetic pressure $B^2/(2\mu_0)$)
- 110 • A sharp rotation of the magnetic field (i.e., a thin current sheet) around the maximum
 111 pressure location
- 112 • A sudden change in the electron pitch-angle distribution across the central current sheet

113

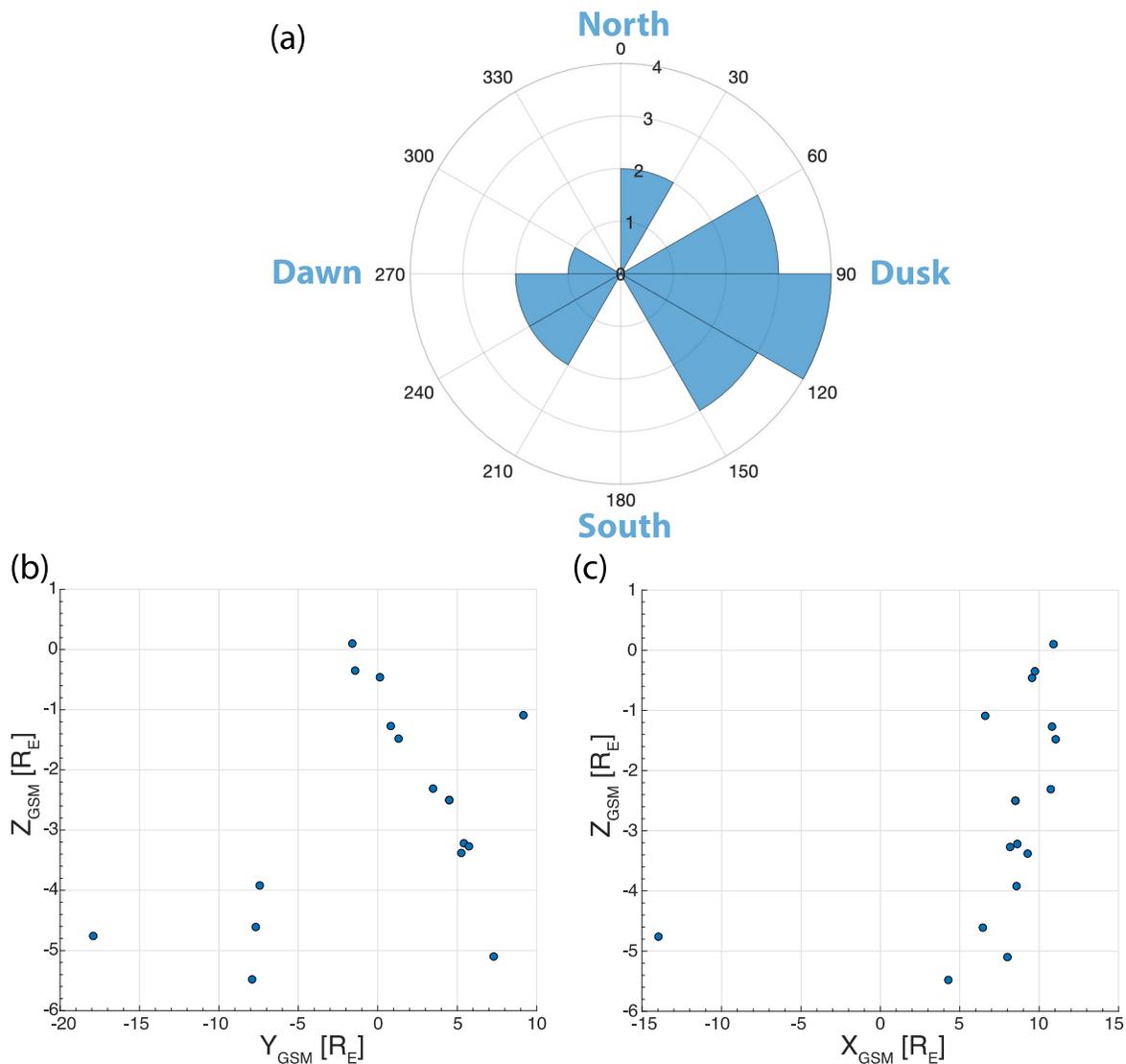
No.	Date	Start time	End time	Location (GSM) [RE]	Delta P [%]	Notes
1	2016-12-10	04:52:59	04:54:04	[9.55, 0.14, -0.46]	59	1
2	2015-10-31	07:17:44	07:19:06	[10.73, 3.48, -2.31]	73	1
3	2015-11-07	14:16:22	14:16:55	[8.62, 5.42, -3.22]	160	1
4*	2017-05-05	20:06:42	20:06:57	[-13.97, -17.91, -4.76]	139	2
5	2015-11-05	14:47:06	14:47:34	[8.17, 5.74, -3.27]	83	3
6	2015-11-21	01:55:59	01:57:38	[9.73, -1.42, -0.35]	112	3
7	2016-02-10	02:47:23	02:48:14	[6.45, -7.68, -4.61]	28	3
8	2016-12-28	04:59:12	04:59:46	[10.9, -1.6, 0.1]	94	3
9	2015-12-08	10:27:41	10:28:07	[10.81, 0.82, -1.27]	46	3
10	2016-02-26	01:48:54	01:49:11	[4.28, -7.91, -5.48]	99	3
11	2016-11-12	17:50:27	17:51:25	[6.6, 9.17, -1.09]	121	3
12	2015-11-06	13:23:31	13:24:24	[9.27, 5.26, -3.38]	212	4
13	2015-12-03	10:24:08	10:25:13	[11.04, 1.31, -1.48]	60	4
14	2016-01-18	01:22:46	01:23:11	[8.57, -7.43, -3.92]	49	4
15	2015-10-11	12:48:52	12:49:31	[8.01, 7.35, -5.06]	69	4
16	2015-11-17	14:20:56	14:21:05	[8.48, 4.48, -2.52]	97	4
17	2015-11-17	14:21:45	14:21:59	[8.48, 4.48, -2.52]	83	4

114 **Table 1.** The time and location of the identified flux tube entanglement events. As labeled in the
 115 notes column, some events have been reported in recent publications: 1. (Øieroset et al., 2019);
 116 2. (Hwang, Dokgo, et al., 2020); 3. (Fargette et al., 2020); 4. This paper. Event 4 has been
 117 studied as entanglement between flux tubes generated within a Kelvin-Helmholtz vortex, but is
 118 not detected at the dayside magnetopause.

119

120 Table 1 lists all the events with their times and locations in the Geocentric Solar
 121 Magnetospheric (GSM) coordinate system. Event location is slightly biased towards the dusk
 122 side, with 10 of 17 events located in positive Y GSM (Fig. 1b). Events also tend to appear below
 123 the equator in a limited Z_{GSM} range ($< 6 R_E$), which may be caused by the longer dwell time of
 124 the MMS in the southern hemisphere and the limited latitude coverage of the orbits. In general,
 125 the entanglement events are ubiquitous and suggesting that flux tube entanglement happens
 126 frequently at the magnetopause. Figure 1a shows the solar wind clock angle of these events. In
 127 contrast with the finding that reconnection is favored by antiparallel fields, FTEs generated by

128 these twisted flux tubes and their entanglement are favored by a By-dominated IMF condition.
 129 This agrees with earlier findings of Fargette et al. (2020) and Russell & Qi (2020).
 130



131
 132 **Figure 1.** IMF conditions and locations of 17 events. **(a)** Solar wind clock angle measured by the
 133 MMS during the 17 events. Starting from 0°, each bin is 30° wide. The bar length in units of
 134 radius is the number of events in that clock angle bin. **(b), (c)** The locations of 17 events in the
 135 GSM Y-Z and X-Z planes. Event 4 has been studied as entanglement between flux tubes
 136 generated within a Kelvin-Helmholtz vortex, but is not detected at the dayside magnetopause
 137

138 3.2 Three stages of entanglement

139 Before introducing the temporal evolutionary features in the MMS data, we qualitatively
 140 describe the entanglement process and the expected characteristics of its different temporal
 141 evolutionart stages. As shown in the sketch of Russell & Qi, 2020, two flux tubes generated at

142 different primary reconnection sites moves towards each other. These tubes have one end
143 connected to the Earth, and the other end connected to the magnetosheath. When the two flux
144 tubes encounter each other, there is no way for them to pass. Instead they become entangled and
145 stretched, with significantly enhanced compression at the interface. How do they eventually
146 disentangle? We have identified three typical cases to examine this evolution process.

147 Figure 2 compares three typical events to show the temporal evolution of flux tube
148 entanglement: event no. 13 (left), event no. 3 (middle), and event no. 1 (right) in Table 1. We
149 rotate the data into an LMN coordinate system, i.e., for event 3 in the middle panels, N is the
150 current sheet normal direction determined by four-spacecraft timing, M' is the averaged current
151 direction (current interval is marked by blue vertical lines in figure 2), L direction is
152 perpendicular to the plane containing both N and M', and finally $N \times L$ gives the M. For each
153 event, we show the four-spacecraft-averaged magnetic field, the current density, the pressure,
154 and the ion and electron energy spectrogram observed by MMS1 in a wider time range to
155 demonstrate the full entanglement (pressure enhancement) region as marked by the black vertical
156 lines. The magnetic field curvature projected in the current sheet moving (normal) direction is
157 plotted in a narrower time interval marked by the blue vertical lines and centered around the
158 current sheet. The red vertical line marks the maximum current density location within the
159 current sheet.

160 In the top panels which correspond to the early stage (event no. 13), the curvature normal
161 component varies around zero, showing no systematic pattern at the central current sheet. The
162 total pressure enhancement is only about 60% of its ambient value, indicating a not-yet-grown
163 compression as the two flux tubes just start to interact. Throughout the entire pressure enhanced
164 region in event no.13, the MMS does not observe a significant electron population at energies
165 above 1keV. This is consistent with an early stage of entanglement, when neither of the two
166 entangled flux tube are “closed” in the magnetosphere. Thus it is difficult for them to trap the hot
167 magnetospheric electrons.

168 As the entanglement proceeds, the field lines bend more toward the current sheet, keep
169 adding magnetic tension force, leading to further increased compression. The most outstanding
170 difference between event no. 3 (middle panels) and the other two is the curvature normal
171 component. The clear negative-to-positive bipolar signature of the curvature normal in event no.
172 3 indicates that the magnetic field lines are curving towards the central current sheet on both
173 sides. Magnetic flux piles up around the central current sheet, knocking the total pressure off
174 balance (middle pressure panel of Figure 2, or enlarged plot in Figure 3d), and preparing for a
175 secondary reconnection to release the energy (Øieroset et al., 2019). The total pressure
176 enhancement is about 190% of the ambient value. These features are consistent with this being
177 the stage when the two flux tubes are actively pulling against each other, and the magnetic field
178 wraps around the interface tightly. Noting the strong pressure build-up and the negative-to-
179 positive bipolar curvature N component, we label event no. 3 as the middle stage of the
180 entanglement process.

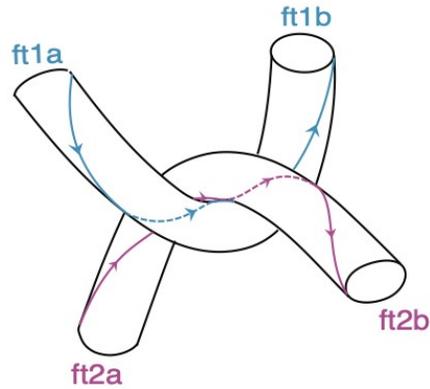
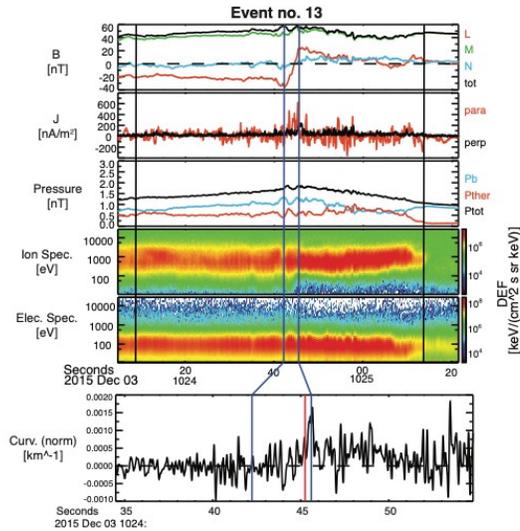
181 Eventually, a new pair of ropes are about to be born, as shown in the bottom panels
182 (event no. 1). In contrast with the initial pair, one rope has both ends connected to the ionosphere
183 (“closed” in the magnetosphere) while the other rope has two ends connected to the
184 magnetosheath (“interplanetary”). The “closed” flux rope is capable of trapping energetic
185 magnetospheric electrons. The “interplanetary” flux rope will lose its energetic electrons quickly.
186 Comparable to the early stage event no. 13, the curvature normal component remains
187 insignificant except in the current sheet region in event no. 1. The total pressure enhancement is

188 70% in event no. 1, similar to that of the entanglement in its early stage. At this late stage, the
189 compression has been canceled when reconnection has almost released the entanglement and the
190 new ropes are about to form. The key difference between event no. 13 and event no. 1 is in the
191 electron distributions. In event no. 1, the right half of the pressure enhanced region shows
192 increased flux between 1k – 10 keV, which is absent in the left half. This is consistent with a
193 later stage of entanglement when reconnection has almost finished making two new ropes one of
194 which (like the right half in event no. 13) has the majority of its field lines connected to the
195 southern and northern hemisphere of the Earth and is capable of trapping the hot electrons
196 originating from the plasma sheet.

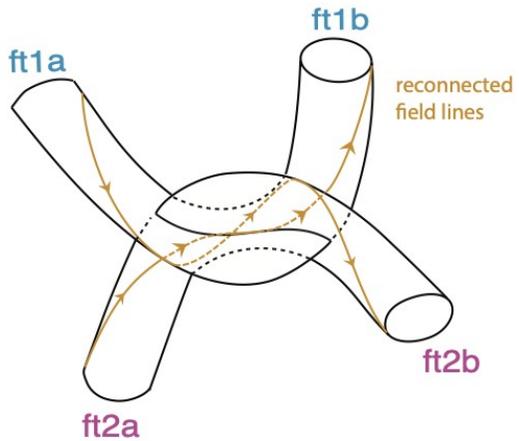
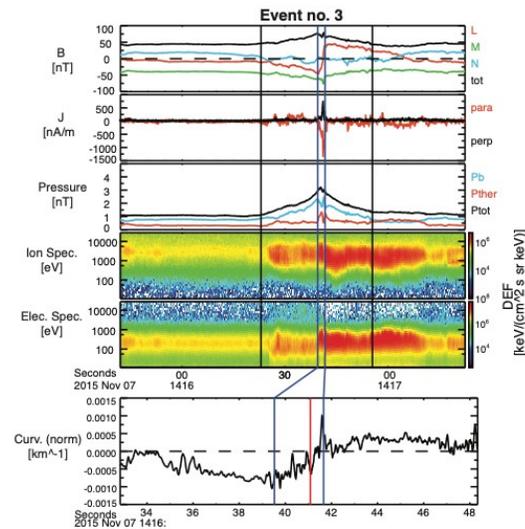
197 As sketched on right of each event in Figure 2, based the events we identified (in Table
198 2), we summarize the temporal evolution characteristics of flux tube entanglement as follows:

- 199 • The three most diagnostic parameters to examine are: 1) the total pressure; 2) the
200 curvature component along the current sheet normal; and 3) the hot electron flux.
- 201 • An early-stage entanglement does not have the bipolar variation in curvature and has less
202 significant pressure enhancement ($< 100\%$), indicating the two flux tubes are loosely
203 compressed. There are no clear energetic magnetospheric electron flux increases on either
204 side because the flux tubes have not been sufficiently “closed” in the magnetosphere, thus
205 it is harder for them to trap hot electrons.
- 206 • A mid-stage entanglement exhibits a clear bipolar curvature normal component, and a
207 fairly strong total pressure increase ($> 100\%$), indicating the significant compression
208 between two tubes. A hot electron population may or may not be present due to the co-
209 existence of magnetic field lines with different connectivity.
- 210 • A late-stage entanglement does not have the bipolar variation in curvature and has less
211 significant pressure enhancement ($< 100\%$), as the compression has mostly resolved by
212 reconnection. Energetic magnetospheric electrons appear either before or after the current
213 sheet crossing, indicating that the field lines on this side are almost “closed” (i.e., have
214 two ends on the Earth), and a new pair of flux ropes is about to be born.

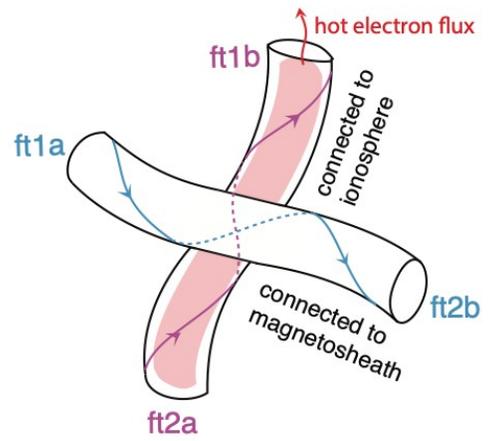
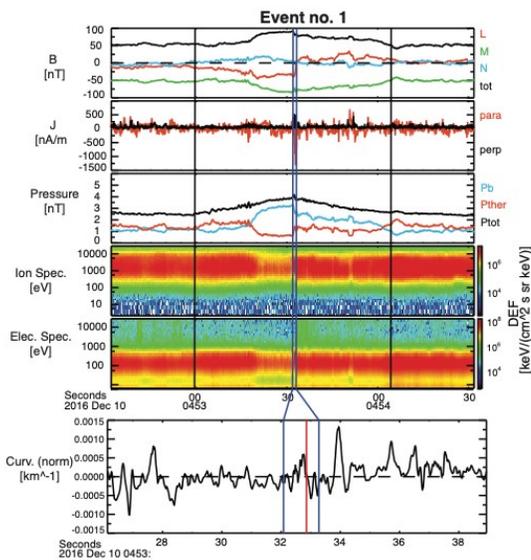
Early stage



Mid stage



Late stage

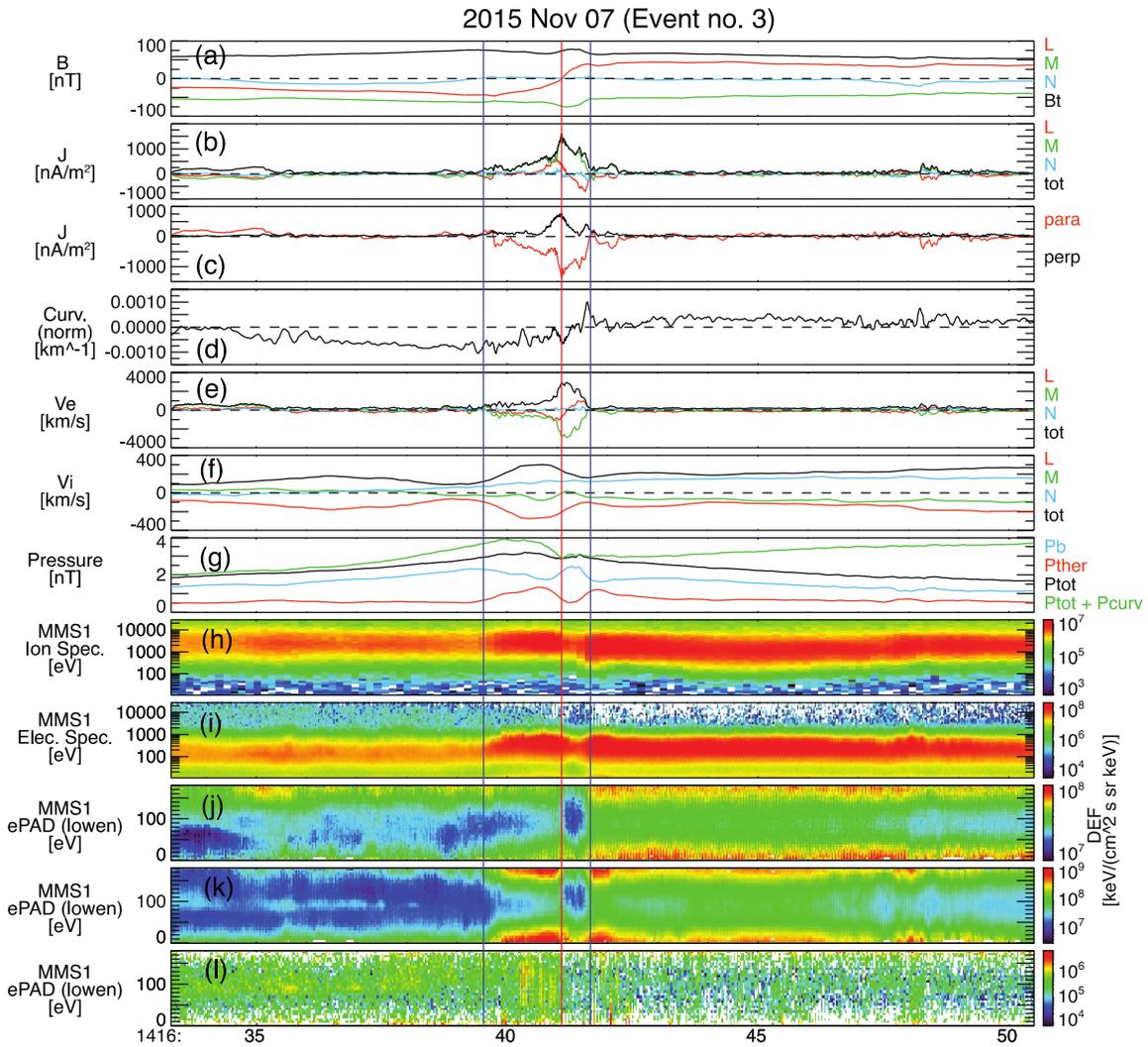


216 **Figure 2.** Context plot for three representative events and schematic sketches showing
 217 characteristics of early, mid and late stages of the entanglement. We show the four-spacecraft-
 218 averaged magnetic field, the current density, the pressure, the ion and electron energy
 219 spectrogram in a wider time range to demonstrate the full entanglement (pressure enhanced)
 220 region as marked by the black vertical lines. The magnetic field curvature projected in the
 221 direction of the current sheet normal is plotted in a narrower time interval around the sheet
 222 marked by the blue vertical lines. The red vertical line marks the maximum current density
 223 location within the current sheet. The LMN rotation matrix for event no. 3 has been mentioned in
 224 the text. The LMN directions in GSM for event no. 13 are L: [0.50, -0.86, -0.06], M: [0.42, 0.18,
 225 0.89], N: [0.75, 0.47, -0.46], for event no.3 are L: [-0.08, -0.92, 0.39], M: [-0.78, -0.19, -0.59],
 226 N: [-0.62, 0.36, 0.70], and for event no. 1 are L: [0.66, -0.58, -0.48], M: [-0.34, 0.34, -0.88], N: [-
 227 0.67, -0.74, -0.03].
 228

229 We use the mid stage event, event no.3 (November 7, 2015) as an example for further
 230 analysis of the highly compressed interface between two entangled flux tubes. The sharp rotation
 231 of the magnetic field is clearly seen as the B_L reversal from 14:16:39.527 to 14:16:41.660. B_N is
 232 close to zero. B_M remains strong and enhanced at the current density peak time (indicated by the
 233 red vertical line). The current density dramatically increased around the maximum magnetic flux
 234 pile-up region. The dominant component of current is anti-parallel to the magnetic field and the
 235 magnitude reaches over 1000 nA/m². The normal speed of this current sheet is about 90 km/s.
 236 With a timespan of 2.1 seconds (between the blue vertical lines), the current sheet thickness is
 237 ~190 km. Electron bulk flow velocity increases significantly in the current sheet and deviates
 238 from the ion bulk flow velocity, especially in the M direction, suggesting that the current is
 239 mainly carried by the electrons. The electron flow accelerates and reverses in the L direction
 240 (Fig. 2e). Meanwhile, the ion flow increases in the -L direction (Fig. 2f), consistent with the
 241 current sheet actively reconnecting. Fig. 2h-l manifests the abrupt change in the energy spectra
 242 (Fig. 2h, i), as well as the electron pitch-angle distribution (Fig. 2j-l). Last, in panel (d), the
 243 curvature of magnetic field increased around the current sheet, plus a clear bipolar signature: it is
 244 negative before the MMS encounters the current sheet and reverses to positive after crossing the
 245 current sheet, indicating that the field lines bend towards the current sheet on both sides. This is
 246 consistent with the compression of the magnetic field, providing magnetic tension force to
 247 balance the pressure. Also consistently, in Fig. 2g, the green line is the estimated total pressure
 248 including the curvature force in the normal direction integrated along the path away from the
 249 current sheet center/maximum current density location (

$$250 \quad P_{curv} = \int \frac{B^2}{\mu_0} |Curv_N| dx = \int \frac{B^2}{\mu_0} (\overrightarrow{curv} \cdot \overrightarrow{V_{i,perp}}) dt, \text{ where } B \text{ is the magnetic field strength, } \mu_0 \text{ is the}$$

251 vacuum permeability, $Curv_N$ is the curvature normal component, $\overrightarrow{V_{i,perp}}$ is the ion bulk flow
 252 velocity perpendicular to the magnetic field). This modified total pressure (green line in Fig. 2g)
 253 on the right appears stable, but on the left, there still remains an apparent slope, suggesting
 254 pressure balance has not yet been reached during such a dynamic process.



255
 256 **Figure 3.** An example of two entangled flux tubes as observed by the MMS on 2015 November
 257 7. **(a)** Four-spacecraft-averaged magnetic field in LMN coordinates and the field strength; **(b),**
 258 **(c)** current density computed by curlometer technique in LMN and field-aligned coordinates; **(d)**
 259 magnetic field curvature projected in the direction of central current sheet normal; **(e), (f)** four-
 260 spacecraft-averaged electron and ion bulk flow velocity; **(g)** four-spacecraft-averaged pressure;
 261 **(h), (i)** ion and electron energy spectrogram at MMS1; **(j)-(l)** electron pitch-angle distribution for
 262 low (10eV-200 eV), mid (200eV-2 keV), and high (2 keV-30 keV) energy range at MMS1. Blue
 263 vertical lines mark the central current sheet between two entangled flux tubes. The red vertical
 264 line marks the location of strongest current density within this current sheet.
 265

266 **4 Discussion and Conclusions**

267 We applied the criteria outlined in the previous section to all 17 events, and we have
268 classified 2 events as early-stage (nos. 9 and 13), 3 events as mid-stage (nos. 3, 6 and 11), and 3
269 events as late-stage (nos. 1, 8 and 13). The other events are ambiguous and cannot easily be
270 classified into any of the three stages, due to the mixture of characteristics. The rest events show
271 fewer diagnostic features. This is to be expected since the entanglement is a continuously
272 developing process, and we do not expect a clear boundary between different stages. For
273 example, in event no. 11 (Figure 1 in supplementary material), the total pressure enhancement is
274 greater than 100% of the ambient plasma, and to the left of the central current sheet, the
275 curvature normal component becomes negative, however, to the right of the central current sheet,
276 there is no clear positive curvature normal component, thus the lack of bipolar signature but a
277 relatively strong compression indicates event no. 11 is in a transition stage either between early
278 and middle, or between middle and late. Another example is event no. 2 (Figure 2 in
279 supplementary material). While there exists the bipolar signature in the curvature, the pressure
280 enhancement is not as strong as other mid-stage events, thus it also seems to be in a transition
281 stage.

282 To further examine if the properties of the current sheet between two entangled flux tubes
283 are able to reveal the temporal evolution, we list additional information about these local current
284 sheets for each of the eight events in Table 1 of the supplementary material. The duration of the
285 entanglement events (the timespan between the event start time and the end time listed in Table
286 1) has a wide range from ~30 seconds to ~100 seconds, suggesting that the spatial scale of
287 entanglement varies. The magnitude of entanglement depends on the sizes of the flux tubes,
288 which is determined by the primary reconnection rate and duration. The velocity of the central
289 current sheet is relatively slow, as to be expected in two tubes tugging in opposite directions.
290 Except in event no. 9, current sheets in the rest of the events move at a speed close to or below
291 100 km/s. The current sheet duration is manually determined as the timespan of the magnetic
292 field rotation region around the pressure peak. The current sheet width is computed by normal
293 speed multiplied by the current sheet duration. There are two events (no. 1 and no. 13) with thin
294 current sheets (close to or smaller than ion inertial length). Other current sheets are thicker, but
295 still thinner than 5 ion inertial lengths. The current sheet ratio, computed as the timespan of the
296 current sheet divided by the timespan of the event duration, is below 7%. This parameter
297 quantitatively describes how “sharp” the field rotation is at the center, and this sharp rotation
298 certainly differs from a smooth variation, as seen in an isolated stable flux rope. None of these
299 parameters are informative about the temporal development sequences. This implies that flux
300 tube entanglement may happen under varying conditions, like varying flux tube sizes, and/or
301 plasma flow speed.

302 The total pressure profile in event no. 3 is very symmetric, as are most events. However,
303 5 out of 17 events are asymmetric (event nos. 7, 10, 11, 12 and 14). This asymmetry may be due
304 to the differences in size and momentum of the two flux tubes. They do not occur as often as
305 symmetric ones. One possible explanation is, if one tube is significantly weaker than another
306 tube, it will easily be overpowered or merged. Under this circumstance, the entanglement process
307 would not last as long, and would be observed less frequently.

308 In this study, we examined a list of 17 flux tube entanglement events from the first two
309 dayside phases of the MMS observations. Their B_y -dominated IMF distribution agrees with
310 previous findings. By comparing their similarities and differences in the magnetic field
311 curvature, total pressure, and existence of hot electrons, we select eight events to showcase the
312 temporal evolutionary features of three stages. They show that mid-stage entanglement events

313 usually have the clearest bipolar signature in the curvature normal component, and a fairly strong
314 total pressure increase ($> 100\%$). Early-stage and late-stage entanglement does not have the
315 bipolar variation in curvature and has less significant pressure enhancement ($<100\%$). In late-
316 stage events, energetic magnetospheric electrons appear either before or after the central current
317 sheet crossing, indicating that one set of field lines is almost closed (having two ends on the
318 Earth), and a new pair of flux ropes is about to be born.
319

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324 spacecraft and instruments and ensure the data are accurate and are provided to the science team
325 in a timely manner. We would also like to thank Dr. San Lu for very beneficial discussions.
326
327

328 **Data Availability Statement**

329 MMS data are available publicly from the mission's Science Data Center
330 (<https://lasp.colorado.edu/mms/sdc/public/>). Solar wind data is available at CDAWeb
331 (<https://cdaweb.sci.gsfc.nasa.gov>).

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333

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