

1           **The Jovian Ionospheric Alfvén Resonator and Auroral Particle Acceleration**

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8           **Key Points:**

- 9           • Broadband acceleration of auroral particles, which is more prevalent at Jupiter than at  
10           Earth, can be achieved by Alfvén waves propagating in the ionospheric Alfvén resonator,  
11           a region formed by the rapid increase in the Alfvén speed above the ionosphere.
- 12           • Modeling of the Jovian ionospheric Alfvén resonator indicate that electrons could be  
13           accelerated to the 10-100 keV range for observed levels of Alfvén wave activity.
- 14           • In addition to the ionospheric resonator, there is also an Alfvén resonator in the high-Alfvén  
15           speed velocity region between the ionosphere and the dense plasma sheet.

16

17 **Abstract**

18 The ionospheric Alfvén resonator (IAR) is a structure formed by the rapid decrease in the plasma  
19 density above a planetary ionosphere. This results in a corresponding increase in the Alfvén  
20 speed that can provide partial reflection of Alfvén waves. At Earth, the IAR on auroral field  
21 lines is associated with the broadband acceleration of auroral particles, sometimes termed the  
22 Alfvénic aurora. This arises since phase mixing in the IAR reduces the perpendicular  
23 wavelength of the Alfvén waves, which enhances the parallel electric field due to electron  
24 inertia. This parallel electric field fluctuates at frequencies of 0.1-20.0 Hz, comparable to the  
25 electron transit time through the region, leading to the broadband acceleration. The prevalence  
26 of such broadband acceleration at Jupiter suggests that a similar process can occur in the Jovian  
27 IAR. A numerical model of Alfvén wave propagation in the Jovian IAR has been developed to  
28 investigate these interactions. This model describes the evolution of the electric and magnetic  
29 fields in the low-altitude region close to Jupiter that is sampled during Juno’s perijove passes. In  
30 particular, the model relates measurement of magnetic fields below the ion cyclotron frequency  
31 from the MAG and Waves instruments on Juno and electric fields from Waves to the associated  
32 parallel electric fields that can accelerate auroral particles.

33 **Plain Language Summary:**

34 Just like at Earth, the polar regions of the planet Jupiter are circled by a luminous aurora (northern  
35 and southern lights) that can be seen from telescopes like the Hubble Space Telescope near Earth.  
36 The aurora on both planets is produced by electrons impacting the upper atmosphere, causing the  
37 atoms and molecules in this region to emit light. At Earth, these electrons are mainly produced by  
38 large voltages that cause all the electrons to be accelerated to nearly the same energy. However,  
39 recent observations from the Juno satellite at Jupiter shows that these electrons are mainly  
40 accelerated over a broad range of energies. This suggests that the voltages accelerating these  
41 electrons are fluctuating rapidly in time. Such fluctuations can be caused by the strong increase in  
42 the effective wave speed due to a rapid decrease in the number of electrons as the altitude is  
43 increased. We have developed a computer model to help understand these interactions.

44 **Index terms:** 2752 MHD Waves and Instabilities, 2756 Planetary Magnetospheres, 2704 Auroral  
45 Phenomena, 2753 Numerical Modeling, 2736 Magnetosphere/Ionosphere interactions

46 **Key Words:** Jupiter, kinetic Alfvén waves, aurora, magnetosphere-ionosphere coupling.

47

## 48 **1. Introduction**

49 The aurora at Jupiter is presently being investigated by the NASA Juno satellite, which went into  
50 a polar orbit around Jupiter on July 4, 2016 (e.g., Bagenal et al., 2017). Observations of auroral  
51 particles at Earth show that the most common form of auroral acceleration is a monoenergetic  
52 beam thought to be caused by a parallel potential drop (e.g., Gurnett & Frank, 1973; Mozer et al.,  
53 1980). However, in other cases, the aurora is associated with electrons having a broadband  
54 distribution in energy (e.g., Chaston et al., 2002; Semeter & Blixt, 2006). However, the  
55 measurements from Juno indicate that the aurora at Jupiter is commonly associated with broadband  
56 electrons, in contrast to the situation at Earth (e.g., Allegrini et al., 2020; Mauk et al., 2017).  
57 Monoenergetic beams of electrons are also present at Jupiter, but are less common.

58 The electrons that produce the discrete aurora are generally thought to be associated with the  
59 acceleration of these electrons by electric fields parallel to the background magnetic field. The  
60 monoenergetic electrons are produced by a quasi-static parallel electric field that accelerates all  
61 the electrons to the same energy (e.g., Karlsson, 2012). A broadband acceleration of these  
62 electrons would require that the parallel electric field would vary over the time it takes for the  
63 electrons to pass through the acceleration region. One possibility would be through the excitation  
64 of whistler-mode waves (Elliott et al., 2018); however, the excitation of these waves requires a  
65 pre-existing beam of electrons. The other possibility, and one that is more widely accepted in the  
66 case of Earth, is the production of kinetic Alfvén waves in the so-called ionospheric Alfvén  
67 resonator that carry a parallel electric field that fluctuates on a time scale of a few seconds,  
68 sufficient to accelerate these particles (e.g., Lysak, 1991, 1993; Watt & Rankin, 2009). It is the  
69 purpose of this paper to examine the effects of Alfvén waves in the ionospheric Alfvén resonator  
70 (IAR) in the context of the Jovian magnetosphere.

71 The ionospheric Alfvén resonator, first recognized in spectral signals associated with ionospheric  
72 heating experiments (Polyakov & Rapaport, 1981), is a structure formed by the rapid decrease of  
73 the mass density of the plasma with altitude above the ionosphere. This structure leads to a rapid  
74 increase in the Alfvén speed, which gives the propagation velocity of Alfvén waves, waves

75 analogous to waves on a string that propagate along magnetic field lines in a plasma. The Alfvén  
76 speed is given by  $V_A = B / \sqrt{\mu_0 \rho}$  in cases where this speed is much less than the speed of light.  
77 However, at Jupiter, and even to some extent at Earth, this speed can approach the speed of light,  
78 in which case it is modified, with the modified speed denoted by  $c_A$ :

$$79 \quad c_A = \frac{V_A}{\sqrt{1 + V_A^2 / c^2}} \quad (1)$$

80 Over the auroral zone at Jupiter, the Alfvén speed will approach the speed of light at altitudes less  
81 than 1 Jovian radius ( $1 R_J = 71492 \text{ km}$ ) over the surface of Jupiter, which is taken to be at the 1  
82 bar level (e.g., Weiss, 2004). The rapid increase in the Alfvén speed causes the partial reflection  
83 of Alfvén waves so that they can be quasi-trapped in the resonator. At both Earth and Jupiter, the  
84 resonant frequencies of the IAR are in the 0.1-20.0 Hz range (Lysak, 1991; Su et al., 2006). At  
85 small wavelengths perpendicular to the field, the effect of finite electron inertia becomes  
86 significant and leads to a parallel electric field that will fluctuate at the IAR resonant frequency.  
87 As a reference point, an electron traveling at one planetary radius per second has an energy of  
88 about 100 eV at Earth and 15 keV at Jupiter.

89 This paper will consider a numerical model of the IAR at Jupiter based on measurements from  
90 Juno. The Waves instrument on Juno (Kurth et al., 2017) can make estimates of the electron  
91 density by observing resonances and cutoffs in the wave emissions (Elliott et al., 2021) that can  
92 serve as an input to the model. In some cases these measurements can be confirmed by direct  
93 particle measurements from the Jovian Auroral Distributions Experiment (JADE; Allegrini et al.,  
94 2020; McComas et al., 2013). In addition, the MAG magnetometer experiment (Connerney et al.,  
95 2017) has made direct measurements of the magnetic fields of the Alfvén waves near perijove  
96 (Gershmann et al., 2019). Alfvén waves at frequencies above 50 Hz have also been observed by  
97 Waves (Sulaiman et al., 2020). These measurements can be used to constrain the amplitudes of  
98 the Alfvén waves excited in our model.

99 The remainder of this paper will be organized as follows. First, the theory of the ionospheric  
100 Alfvén resonator will be considered in general terms. Then we will discuss the numerical model  
101 and its application to the Jovian magnetosphere. This will be followed by a discussion of the

102 formation of parallel electric fields and comparison with the potentials needed to accelerate the  
103 Jovian electrons. We will conclude with a discussion of the results and plans for future work.

## 104 **2. Theory of the Ionospheric Alfvén Resonator**

105 The ionospheric Alfvén resonator (IAR) is formed by the rapid decrease in the plasma density with  
106 altitude above the ionospheric peak, leading to a rapid increase in the Alfvén speed. The IAR has  
107 been frequently invoked in the Earth’s auroral zone and associated with the acceleration of auroral  
108 electrons (e.g., Cohen et al., 2013; Hebden et al., 2005; Hirano et al., 2005; Lynch et al., 2015;  
109 Lysak, 1991, 1993; Lysak & Song, 2008; Lysak et al., 2013; Miles et al., 2018; Pakhotin et al.,  
110 2018; Polyakov & Rapaport, 1981; Sydorenko et al., 2008; Trakhtengertz & Feldstein, 1984;  
111 Woodroffe & Lysak, 2012). It has also been suggested to have an effect on auroral radio emissions  
112 at Jupiter (Ergun et al., 2006; Su et al., 2006). Perhaps the best measurements of ionospheric  
113 densities in the Jovian ionosphere have been made from radio occultation measurements from  
114 Galileo (Hinson et al., 1997) and Voyager 2 (Hinson et al., 1998), which saw peak densities of the  
115 order of  $10^5 \text{ cm}^{-3}$  while more recent radio occultation measurements from Juno suggest densities  
116 could be as high as  $10^9 \text{ cm}^{-3}$  (Hodges et al., 2020). At higher altitudes, electron densities  
117 determined from wave cutoffs and resonances indicate densities below  $2 R_J$  of less than  $100 \text{ cm}^{-3}$   
118 and sometimes as low as  $1 \text{ cm}^{-3}$  (Elliott et al., 2021). Thus, the conditions for the existence of an  
119 ionospheric Alfvén resonator are clearly present on auroral field lines at Jupiter.

120 A simple theoretical model of the IAR was presented by Lysak (1991), based on an Alfvén speed  
121 profile first introduced by Trakhtengertz and Feldstein (1984):

$$122 \quad V_A^2(z) = \frac{V_{AI}^2}{\varepsilon^2 + e^{-z/h}} \quad (2)$$

123 Here  $V_{AI}$  is the Alfvén speed in the ionosphere,  $\varepsilon = V_{AI}/V_{AM}$  where  $V_{AM}$  is the magnetospheric  
124 Alfvén speed and  $h$  is the density scale height. This profile is plotted in Figure 1. Inserting this  
125 profile in the wave equation for shear Alfvén waves at a frequency  $\omega$  gives

$$126 \quad \frac{d^2\Phi}{dz^2} + \frac{\omega^2}{V_{AI}^2} (\varepsilon^2 + e^{-z/h}) \Phi = 0 \quad (3)$$

127 Solutions to this equation can be found by using the substitution  $x = x_0 e^{-z/2h}$ , where  $x_0 = 2h\omega/V_A$ .  
128 This transforms equation (3) into a form of Bessel's equation with the general solutions:

$$129 \quad \Phi = A_{inc} J_{ix_0\varepsilon}(x) + A_{ref} J_{-ix_0\varepsilon}(x) \quad (4)$$

130 Here  $A_{inc}$  and  $A_{ref}$  are the amplitudes of the incident and reflected Alfvén waves, respectively. In  
131 the limit of  $\alpha = \mu_0 V_{AI} \Sigma_P \gg 1$ , which is often the case, the eigenfrequencies of these modes (i.e.,  
132 the frequencies that admit a pure incident or reflected wave) are given by  $\omega_n = \xi_n V_{AI}/2h$ , where  $\xi_n$   
133 is the  $n^{\text{th}}$  zero of the zeroth order Bessel function, 2.4, 5.5, 8.6, ... For the profile of Figure 1, the  
134 lowest eigenfrequency is 0.8 Hz.

135 Figure 2 illustrates the structure of these modes as a function of frequency and altitude. This figure  
136 plots the logarithm of the total wave field normalized to the amplitude of the incident wave as a  
137 function of frequency and the distance along the field line. The enhancement of the wave  
138 amplitude at lower altitudes at  $2h\omega/V_A = 2.4, 5.5, 8.6$  can be clearly seen in the Figure. For  
139 comparison with the model to be discussed in the next section, this plot assumes  $\alpha = 18.5$  and  $\varepsilon =$   
140  $0.05$ . The typical crossing of the auroral zone during the early perijoves of the Juno mission at an  
141 altitude of  $0.7 R_J$  corresponds to  $z/h = 18.5$  on this plot.

### 142 **3. Numerical model for the IAR at Jupiter**

143 Next we would like to apply the theory of the IAR to conditions in the main auroral region of  
144 Jupiter. We have developed a numerical model similar to the one used in Lysak and Song (2020)  
145 based on the Connerney et al. (2020) current sheet model and the Bagenal and Delamere (2011)  
146 plasma model. We will concentrate on the region around a co-latitude of  $17^\circ$ , which for this model  
147 corresponds to  $M = 23$  (here  $M$  refers to the equatorial crossing distance of the field line in units  
148 of Jovian radii). As in Lysak and Song (2020), we use magnetic coordinates where the flux  
149 function  $v$  (equal to the vector potential times the distance from the magnetic axis) labels each field  
150 line, and the parallel coordinate  $\mu$  is taken to be the magnetic scalar potential. Here the  $v$  coordinate  
151 is directed southward (at the ionosphere) and the  $\mu$  coordinate increases upward. The usual  
152 eastward azimuthal coordinate  $\varphi$  completes the set. Explicit forms of these coordinates are  
153 described in Lysak and Song (2020). However, in contrast to the previous model, we will focus  
154 on the lower parts of the field line to emphasize the dynamics in the IAR and model only one  
155 hemisphere, which will be the northern hemisphere in the results presented here. Figure 3 shows

156 the simulation volume, with representative field lines and lines at constant scalar potential  
 157 indicated.

158 Figure 4 shows a typical profile of the Alfvén speed (solid line) and density (dashed line) profiles.  
 159 It can be seen that this profile closely follows equation (2) until it reaches about 4 R<sub>J</sub> where it  
 160 begins to decrease because of the decrease in the magnetic field. The Alfvén speed is plotted in  
 161 Figure 5 overlaid on the grid shown in Figure 3. The inset in this figure shows the region of the  
 162 ionospheric Alfvén resonator. These plots are for an ionospheric density of  $2 \times 10^5 \text{ cm}^{-3}$  and a scale  
 163 height of 5000 km.

164 The simulated equations are Maxwell’s equations with a dielectric constant representing the  
 165 Alfvén wave, supplemented by the cold electron equation of motion along the field line, written in  
 166 terms of the field-aligned current. We consider only the toroidal Alfvén wave and assume there is  
 167 no azimuthal variation, so that the wave fields are  $E_v, B_\phi, E_\mu$  and  $J_\mu$ . Then the model equations for  
 168 an ideal MHD Alfvén wave become

$$169 \quad \frac{\partial E_v}{\partial t} = -\frac{1}{\epsilon_\perp \mu_0} \frac{1}{h_\phi h_\mu} \frac{\partial (h_\phi B_\phi)}{\partial \mu} \quad \frac{\partial B_\phi}{\partial t} = -\frac{1}{h_v h_\mu} \left[ \frac{\partial (h_v E_v)}{\partial \mu} - \frac{\partial (h_\mu E_\mu)}{\partial v} \right] \quad (5)$$

170 Here  $\epsilon_\perp = \epsilon_0 (1 + c^2/V_A^2)$ , and the scale factors are  $h_\phi = r \sin \theta$ ,  $h_\mu = R_J B_{\text{eq}}/B$  where  $B_{\text{eq}}$  is the magnetic  
 171 field strength at 1 R<sub>J</sub> on the magnetic equator, and  $h_v = R_J h_\mu / h_\phi$ .

172 The ideal MHD approximation is violated when the perpendicular wavelength becomes  
 173 comparable to the electron inertial length,  $\lambda_e = \sqrt{m_e / \mu_0 n e^2}$ , or the ion acoustic gyroradius,  
 174  $\rho_s = \sqrt{T_e m_i} / eB$ , which despite its common name, depends on the electron pressure, not the  
 175 gyromotion of any ion (e.g., Goertz & Boswell, 1979; Lysak, 1991). The electron inertial length  
 176 is the larger of the two scales when the electron thermal speed is less than the Alfvén speed;  
 177 therefore, the electron inertial length is the most relevant on Jovian field lines in the region less  
 178 than 30 R<sub>J</sub> on field lines threading the main auroral emission (Saur et al., 2018). In this situation,  
 179 equation (5) is supplemented by Ampere’s Law, including the displacement current, and the cold  
 180 electron equation of motion:

181 
$$\varepsilon_{\parallel} \frac{\partial E_{\mu}}{\partial t} = \frac{1}{\mu_0} \frac{1}{h_{\nu} h_{\phi}} \frac{\partial(h_{\phi} B_{\phi})}{\partial \nu} - J_{\mu} \quad \frac{\partial J_{\mu}}{\partial t} = \frac{ne^2}{m_e} E_{\mu} \quad (6)$$

182 The parallel permittivity  $\varepsilon_{\parallel}$  is increased from  $\varepsilon_0$  to improve the stability of the numerical scheme  
 183 (Lysak and Song, 2001).

184 The numerical model can be driven either from the magnetospheric side or the ionospheric side.  
 185 At the ionosphere, we adopt a simplified current sheet model including only Pedersen currents,  
 186 since Hall currents tend to be much smaller in the Jovian ionosphere (e.g., Millward et al., 2002).  
 187 In that case, Ohm's Law integrated over the current sheet can be written as

188 
$$B_{\phi} = \mu_0 \Sigma_P (E_{\nu} \pm V_n B_0) \quad (7)$$

189 where  $\Sigma_P$  is the ionospheric conductance,  $B_0$  is the background magnetic field and  $V_n$  is the  
 190 azimuthal velocity of the neutral atmosphere in the corotating frame. The top sign is appropriate  
 191 for the northern hemisphere while the bottom sign is for the south, due to the way we defined the  
 192 coordinate system. (All the runs shown here are in the northern hemisphere.) The neutral velocity  
 193 term represents a source for the Alfvén waves, which we take to be fluctuations or turbulence in  
 194 the neutral atmosphere. It should also be noted that although the code is three-dimensional, for  
 195 the runs presented in this work the perturbations have been assumed to be uniform in the azimuthal  
 196 direction, so that the magnetic local time (MLT) label on the plots is not relevant.

197 We can use this numerical model to examine the theory of the IAR at Jupiter. First, we will  
 198 consider the ideal MHD case, in which case only the equations (5) are simulated. For this run,  
 199 the density at the ionosphere was set to  $2 \times 10^6 \text{ cm}^{-3}$  and it then decreases exponentially with a scale  
 200 height of 2500 km (0.035  $R_J$ ). However, because of the decrease in the magnetic field strength,  
 201 which is not included in the analytic model described above, the effective scale height for the  
 202 Alfvén speed is about 3500 km. From the theory of the IAR, this would lead to a fundamental  
 203 resonance frequency of 0.8 Hz with the next harmonic at 1.8 Hz.

204 The simulation is driven by a pulse in the neutral velocity lasting 0.25 seconds with an amplitude  
 205 of 1.25 km/s, leading to a 1 V/m electric field in the 8 G field at this latitude, simulating a flow  
 206 burst in the neutral atmosphere (e.g., Yates et al., 2014, 2020). Figure 6 shows the time history of  
 207 the electric and magnetic fields as measured at 1.7  $R_J$ , a typical distance for the auroral crossings

208 in the early Juno perijoves. It can be seen that the fields are not simply an image of the input pulse;  
 209 rather there is structure in the pulses and they repeat due to reflections due to the gradient in the  
 210 Alfvén speed. Figure 7 shows the Fourier transform of the electric field, indicating the peaks are  
 211 at 0.8 and 1.8 Hz, consistent with the theory.

212 Another way of considering the importance of the IAR is the response to a monochromatic driving.  
 213 Figure 8 shows the magnetic field observed at 1.7 R<sub>J</sub> due to a driving at 0.8 Hz (Figure 8a) and 0.4  
 214 Hz (Figure 8b) with the same amplitude as in the previous figures. It can be seen that the resonant  
 215 case (0.8 Hz) reaches an amplitude of about 10 nT while the off-resonant (0.4 Hz) case only  
 216 yields about 2 nT. This illustrates the trapping and reflection of waves that are resonant with the  
 217 IAR cavity.

#### 218 **4. Development of Parallel Electric Fields**

219 As discussed above, the Alfvén wave develops a parallel electric field when the perpendicular  
 220 wavelength becomes comparable to the electron inertial length. The electron inertial effect can be  
 221 implemented by including the two equations of equation (6). For a plane wave in a uniform  
 222 plasma, the parallel electric field due to electron inertia can be written as (e.g., Stasiewicz et al.,  
 223 2000):

$$224 \quad E_{\parallel} = \frac{k_{\parallel} k_{\perp} \lambda_e^2}{1 + k_{\perp}^2 \lambda_e^2} E_{\perp} \quad (8)$$

225 To model the development of parallel electric fields in the IAR, we have done simulations using  
 226 the full set of equations (5) and (6). We use the model shown in Figures 4 and 5, with an  
 227 ionospheric density of  $2 \times 10^5 \text{ cm}^{-3}$  and a scale height of 5000 km. This profile gives a density at  
 228 1.7 R<sub>J</sub> of about  $10 \text{ cm}^{-3}$ , consistent with the density measured at times when Juno crossed the main  
 229 auroral emissions (Elliott et al., 2021). The run is driven by an oscillation at 1.0 Hz in the  
 230 ionospheric electric field, which corresponds to the IAR resonance for this density profile. Figure  
 231 9 shows the magnetic perturbation at 1.74 R<sub>J</sub> for this run. It can be seen that the magnetic field  
 232 oscillates with a peak amplitude of about 12 nT, a value somewhat lower than Juno observations  
 233 with a mean value of 20 nT during PJ1 (Gershman et al., 2019). Figure 10 gives the maximum  
 234 integrated electric field along a model field line during this run. To make this plot, the parallel  
 235 electric field is integrated along each field line, and the maximum value on any field line is plotted.

236 This field increases in a stepwise fashion every 15-20 seconds, reaching values of almost 30 kV  
237 by the end of the run. This suggests that significant particle acceleration could be achieved in this  
238 wave. It should be emphasized that the parallel electric field here is not a potential field, and so  
239 this integrated parallel electric field is not a true potential drop. Nevertheless it does give an  
240 indication of the energies that could be achieved by a particle traversing this region.

241 Figures 9 and 10 raise the question of why the potential drop increases while the magnetic  
242 perturbation doesn't grow appreciably. This is due to the reflections of the Alfvén wave at the  
243 boundary of the plasma sheet. The Alfvén speed profile for this run was shown in Figures 4 and  
244 5. The Alfvén speed shows a sharp gradient between 9 and 10  $R_J$  where the density starts to  
245 increase. A calculation of the Alfvén travel time from the ionosphere indicates that it takes an  
246 Alfvén wave about 6-10 seconds to reach this point from the ionosphere. This causes a reflection  
247 that reinforces the wave field with a 12-20 second period, indicating the presence of a larger  
248 resonant cavity in the high-speed region between the ionosphere and the plasma sheet. Figure 11  
249 shows the field-aligned Poynting flux mapped to the ionosphere at 10, 40, 80, and 120 seconds  
250 into this run. Here green, yellow, and red colors indicate an upward Poynting flux, while blue and  
251 purple are downward fluxes. An animation of the evolution of the Poynting flux can be found in  
252 the supplementary material, Movie S1. A number of features can be seen from this figure and  
253 from the movie. First, at 10 seconds, the wave launched from the ionosphere is traveling up the  
254 field line and has not yet reached the reflection point. By 40 seconds, the wave has hit the Alfvén  
255 speed gradient and has started to reflect, as can be seen in the downward Poynting flux beginning  
256 to appear. The Poynting flux doesn't penetrate beyond 10  $R_J$ , indicating a reflection of the Alfvén  
257 wave. Secondly, the wave becomes more structured with each successive time frame. This is the  
258 result of phase mixing (e.g., Mann et al., 1995; Lysak and Song, 2011), due to the weak plasma  
259 density gradients perpendicular to the main field. This occurs since the resonant frequency of this  
260 high-Alfvén speed cavity is slightly different on each field line, leading to a structuring of the  
261 wave. Because of the decreasing perpendicular scales, the field-aligned current density (not  
262 shown) and the parallel electric field shown in Figure 10 increase with each bounce even though  
263 the magnetic perturbation remains roughly constant.

264 As has been known in the case of the Earth's magnetosphere (e.g., Chaston et al., 2006; Persoon  
265 et al., 1988; Song and Lysak, 2006), the formation of parallel electric fields is favored by low

266 plasma densities. Our runs indicate that this is also the case at Jupiter. A run similar to the run  
267 shown in Figures 9-11 but with the scale height decreased to 4100 km (giving a density of  $1 \text{ cm}^{-3}$   
268 at  $1.7 R_J$ ) is shown in Figure 12. In this case, the magnetic perturbation and the parallel potential  
269 rise in a stepwise fashion to values over 20 nT and up to almost 100 kV. These increases are again  
270 due to reflections between the ionosphere and the Alfvén speed gradient at large radial distance.  
271 Furthermore, another run where the minimum density in the lobes was set to  $10 \text{ cm}^{-3}$  produced  
272 potentials of less than 50 V. This confirms that strong parallel electric fields are favored by low  
273 density, as at Earth.

## 274 **5. Discussion and Conclusions**

275 This work has shown that the structure of the Alfvén speed with altitude on auroral field lines is  
276 critical in the evolution of field-aligned currents and parallel electric fields. Alfvén waves are  
277 reflected when the gradient scale length in the Alfvén speed is comparable with the wavelength of  
278 the wave, so that the WKB approximation is violated. This leads to the formation of resonant  
279 cavities in which Alfvén waves can be trapped. It should be noted that these are leaky cavities  
280 since the shear Alfvén wave equation (3) does not have a classical turning point, so that wave  
281 energy can leak out of the cavity. Nevertheless, the approximate trapping of Alfvén waves in these  
282 gradients can lead to an enhancement of the wave amplitude, which in turn leads to enhanced  
283 parallel electric fields that can accelerate auroral particles.

284 At both Earth (e.g., Cummings et al., 1969; Mann et al., 1995; Singer et al., 1981) and Jupiter  
285 (Lysak & Song, 2020; Manners et al., 2018; Manners & Masters, 2019), reflections from the  
286 conjugate ionospheres can give rise to field line resonances, with periods of a few minutes at Earth  
287 and tens of minutes at Jupiter. In addition, the sharp gradients in the Alfvén speed above the  
288 ionosphere lead to the formation of an ionospheric Alfvén resonator as described here with periods  
289 of seconds. However, the presence of the dense plasma torus due to Io and the resulting plasma  
290 disk of high-density plasma at Jupiter can give rise to other resonant cavities. In this work, we  
291 have seen the presence of the high Alfvén speed region between the ionosphere and plasma disk  
292 can constitute another resonator with periods of tens of seconds. This resonator is unique to  
293 Jupiter, and no analog of this exists at Earth. It is worth noting that the reflection point at this  
294 gradient is itself a function of the wave frequency since lower frequencies have longer  
295 wavelengths. A run like the one in Figures 9-11 except with a lower driving frequency of 0.1 Hz

296 did not reflect before passing out of the simulation volume. Although we have not considered it  
297 here, it is also likely that similar resonant cavities can exist in the plasma torus itself (Manners and  
298 Masters, 2020).

299 For these Alfvén waves to give rise to parallel electric fields, two conditions must be met. First,  
300 the plasma density must be low. This not only increases the electron inertial length, but also limits  
301 the ability of the plasma to carry strong field-aligned currents. In kinetic steady-state models of  
302 currents and parallel electric fields, low densities can lead to a “current choke” condition where  
303 the current required to balance the curl of  $\mathbf{B}$  becomes greater than a critical current that is the order  
304 of  $j_{cirt} \sim nev_{th}$ , where  $v_{th}$  is the electron thermal speed (Ray et al., 2009). When this condition is  
305 violated, the displacement current term in the parallel Ampere’s Law (i.e., the first term on the  
306 right-hand side of the first equation of (6)) becomes important and leads to parallel electric fields  
307 (Song & Lysak, 2006). However, we have not included this choke condition in the results  
308 presented here. This condition will be included in future work.

309 The second required condition is that the perpendicular wavelength of the Alfvén waves must  
310 become comparable to the electron inertial length or ion acoustic gyroradius. This can be  
311 accomplished in a number of ways. First, plasma turbulence can lead to a cascade of energy from  
312 large scales to small scales, a process that has been invoked in both Earth (e.g., Chaston et al.,  
313 2008) and at Jupiter (Saur et al., 2003, 2018). A second possibility is that shown here, that phase  
314 mixing due to perpendicular gradients in the Alfvén speed can lead to smaller wavelengths. This  
315 process occurs because the resonant period in the Alfvén resonant cavities is slightly different on  
316 adjacent field lines, so that these waves get out of phase with each other. This is demonstrated in  
317 Figure 11 showing how the waves trapped in the high-speed resonator develop perpendicular  
318 structure. A third possibility is ionospheric feedback. The precipitation of electrons into the  
319 ionosphere leads to a localized ionization enhancement, and additional currents will flow at those  
320 conductance gradients (e.g., Lysak, 1991; Miura & Sato, 1980). This process will be considered  
321 in future work.

322 Another issue is how these low-density cavities can develop. Measurements from Juno indicate  
323 that electron densities below about  $2 R_J$  are around  $100 \text{ cm}^{-3}$  (Elliott et al., 2021). As we have  
324 seen, these densities are too high for significant parallel electric fields to develop. This would  
325 suggest that the density cavities form as a result of the magnetosphere-ionosphere interaction. Juno

326 observations indicate that there is a strong proton upflow on auroral field lines (Szalay et al., 2021)  
327 as well as on the Io flux tube (Szalay et al., 2018). These upflowing ions may leave behind a  
328 density depletion at lower altitudes. One possibility is that these upflowing ions are accelerated  
329 by the ponderomotive force of the Alfvén waves (e.g, Rankin et al., 1995; Sydorenko et al., 2008).  
330 Another possibility is that they are accelerated by the parallel electric fields themselves, leading to  
331 a different type of positive feedback, in which the density cavity is produced by the parallel electric  
332 fields, and in turn the parallel electric fields are enhanced by the low plasma densities.

333 Although the present work has focused on the main auroral emission region, Alfvén waves have  
334 long been associated with the coupling of the moon Io with the ionosphere of Jupiter (e.g., Acuña  
335 et al., 1981; Bagenal, 1983; Belcher et al., 1981; Chust et al., 2005; Crary, 1997; Goertz, 1980;  
336 Gurnett & Goertz, 1981; Hinton et al., 2019; Neubauer, 1980). This process will be the focus of  
337 future work; however, it is quite likely that similar magnetosphere-ionosphere coupling processes  
338 should be associated with this interaction. It is also likely that the high-speed resonator described  
339 here is present on the Io flux tube and may be responsible for the structure observed in the footprint  
340 tail of Io and other moons (Moirano et al., 2021; Mura et al., 2018).

341 In summary, we have presented the theory and modeling of the ionospheric Alfvén resonator as  
342 well as the resonator formed by the high-Alfvén-speed region between the ionosphere and the  
343 plasma sheet. These resonant structures can lead to large-amplitude Alfvén waves that can lead to  
344 structuring of the field-aligned currents due to phase mixing. In low-density regions of the  
345 magnetosphere, parallel electric fields can develop due to the effect of electron inertia that can lead  
346 to potentials up to 100 kV on auroral field lines. While the overall evolution of the auroral  
347 acceleration at Jupiter is a complicated problem, this work has shown that the dynamics of Alfvén  
348 waves propagation in the inhomogeneous plasma at Jupiter is a major ingredient in understanding  
349 auroral acceleration at Jupiter.

### 350 **Acknowledgments and Data Availability.**

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356 numerical simulations and data files associated with the results presented in this paper are  
357 available at the Data Repository for the University of Minnesota (DRUM).

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## Figure Captions

561 **Figure 1.** Profiles of the Alfvén speed (solid curve) and density (dashed curve) for the idealized  
562 ionospheric Alfvén speed profile of equation (2).

563 **Figure 2.** Amplitude of the electric field, normalized to the incident wave amplitude for the IAR  
564 profile of Figure 1. Enhancements of the wave field at normalized frequencies of 2.4, 5.5 and  
565 8.6 are evident.

566 **Figure 3.** Plot of the simulation volume, with some representative field lines plotted along with  
567 the curves at constant scalar potential that gives the coordinate parallel to the magnetic field.

568 **Figure 4.** Alfvén speed (solid) and density (dashed) profiles for the runs shown

569 **Figure 5.** Plot of the log of the Alfvén speed overlaid on the grid of Figure 3. Inset: blowup of  
570 ionospheric Alfvén resonator region.

571 **Figure 6.** Profiles of the (a) electric field and (b) magnetic field for a run in which a 0.25 second  
572 pulse was input from the ionospheric end of the simulation region.

573 **Figure 7.** Fourier transform of the electric field of Figure 5a, showing resonant frequencies at  
574 0.8 and 1.8 Hz.

575 **Figure 8.** Response of the magnetic field to a driver at the (a) resonant frequency of 0.8 Hz; and  
576 (b) at a non-resonant frequency of 0.4 Hz. The response is about 5 times greater at the resonant  
577 frequency.

578 **Figure 9.** Time history of the magnetic field at  $17^\circ$  co-latitude for a run including the parallel  
579 electric field. The modulation of the field is due to the reflections from the boundary of the  
580 plasma sheet.

581 **Figure 10.** Integrated parallel electric field for the run of Figure 8. Reflections from the plasma  
582 sheet lead to the enhancement of the parallel potential drop on a 15-second time scale.

583 **Figure 11.** Contours of Poynting flux mapped to ionospheric heights at times of (a) 10 seconds;  
584 (b) 40 seconds; (c) 80 seconds; and (d) 120 seconds into the run. Green/red colors indicate  
585 upward Poynting flux and blue downward. After 10 seconds, the wave is moving upward from  
586 the ionosphere. By 40 seconds wave has reflected from the Alfvén speed gradient at about  $10 R_J$

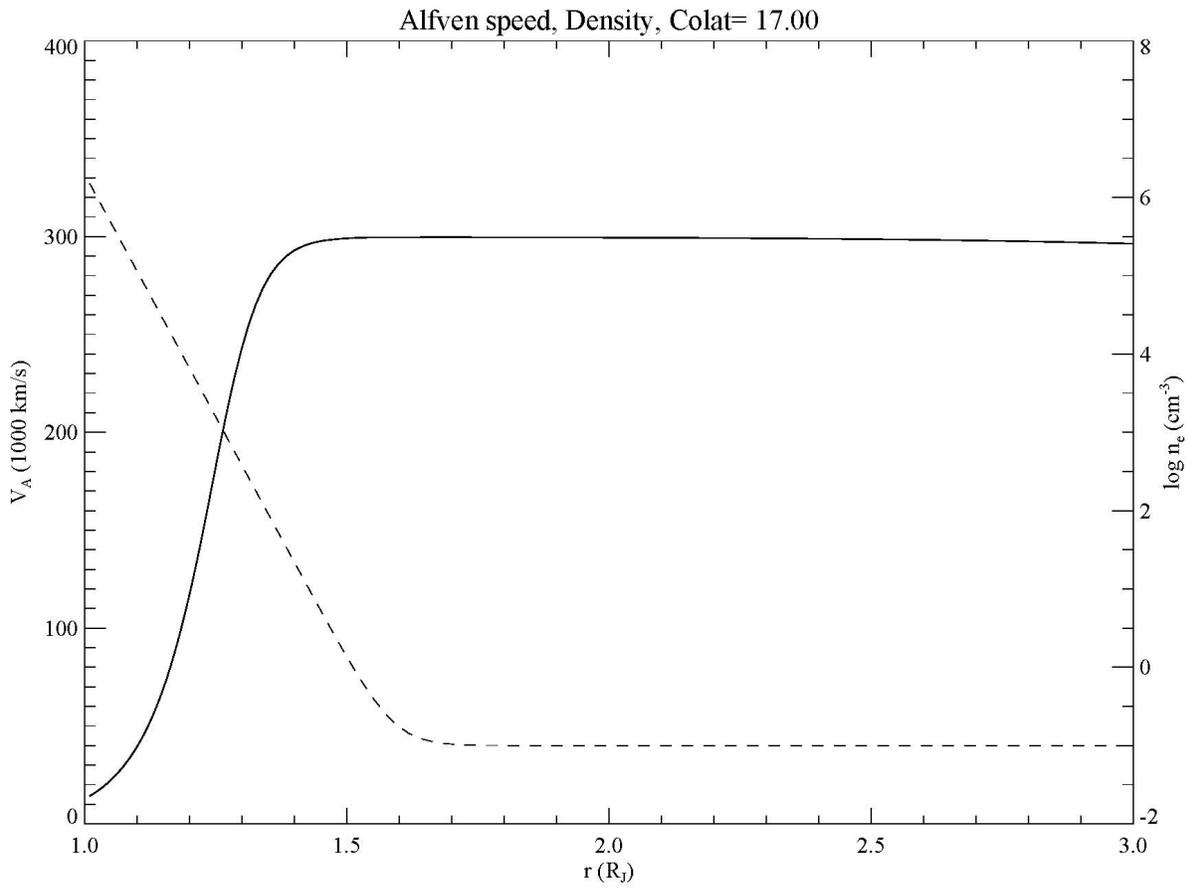
587 and is returning to the ionosphere. At later times, the Poynting flux is alternative in sign,  
588 indicative of a standing wave. As the run progresses, there is increased structure in the  
589 perpendicular direction due to phase mixing.

590 **Figure 12.** Maximum potential for a run in which the ionospheric scale height is decreased to  
591 4100 km, leading to a density of about  $1 \text{ cm}^{-3}$  at  $1.7 R_J$ .

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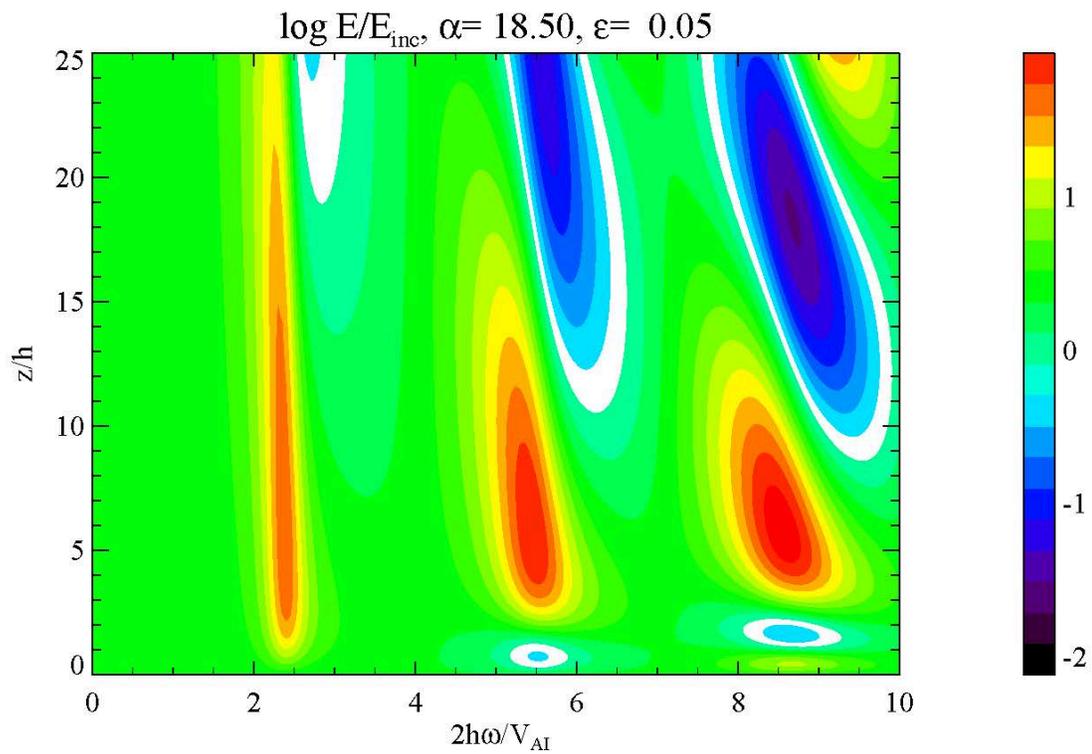
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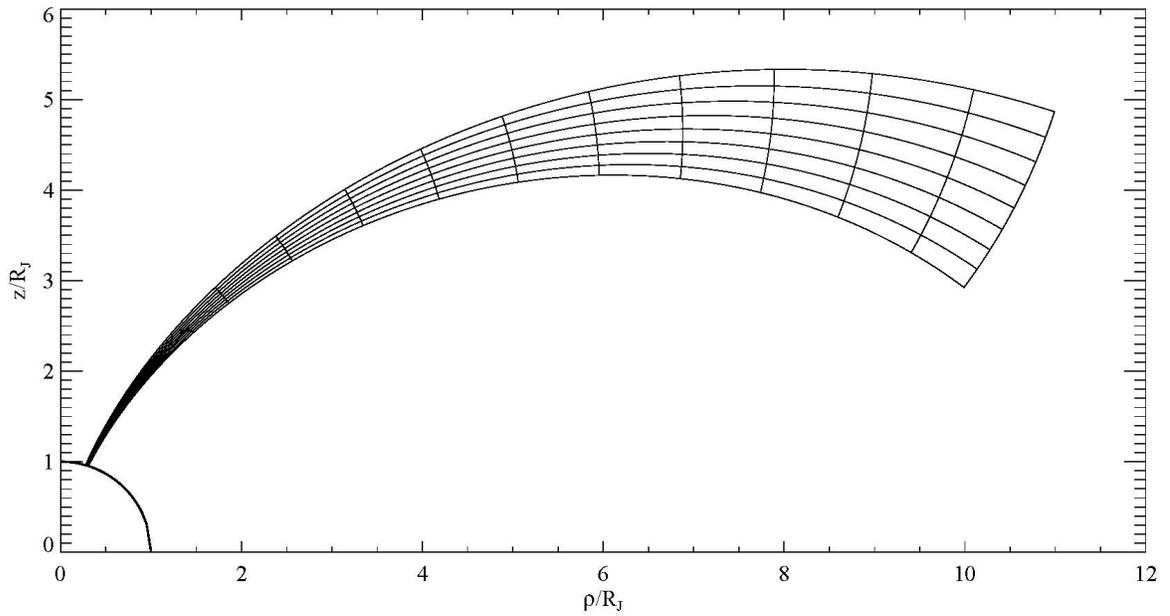
599 **Figure 1.** Profiles of the Alfvén speed (solid curve) and density (dashed curve) for the idealized  
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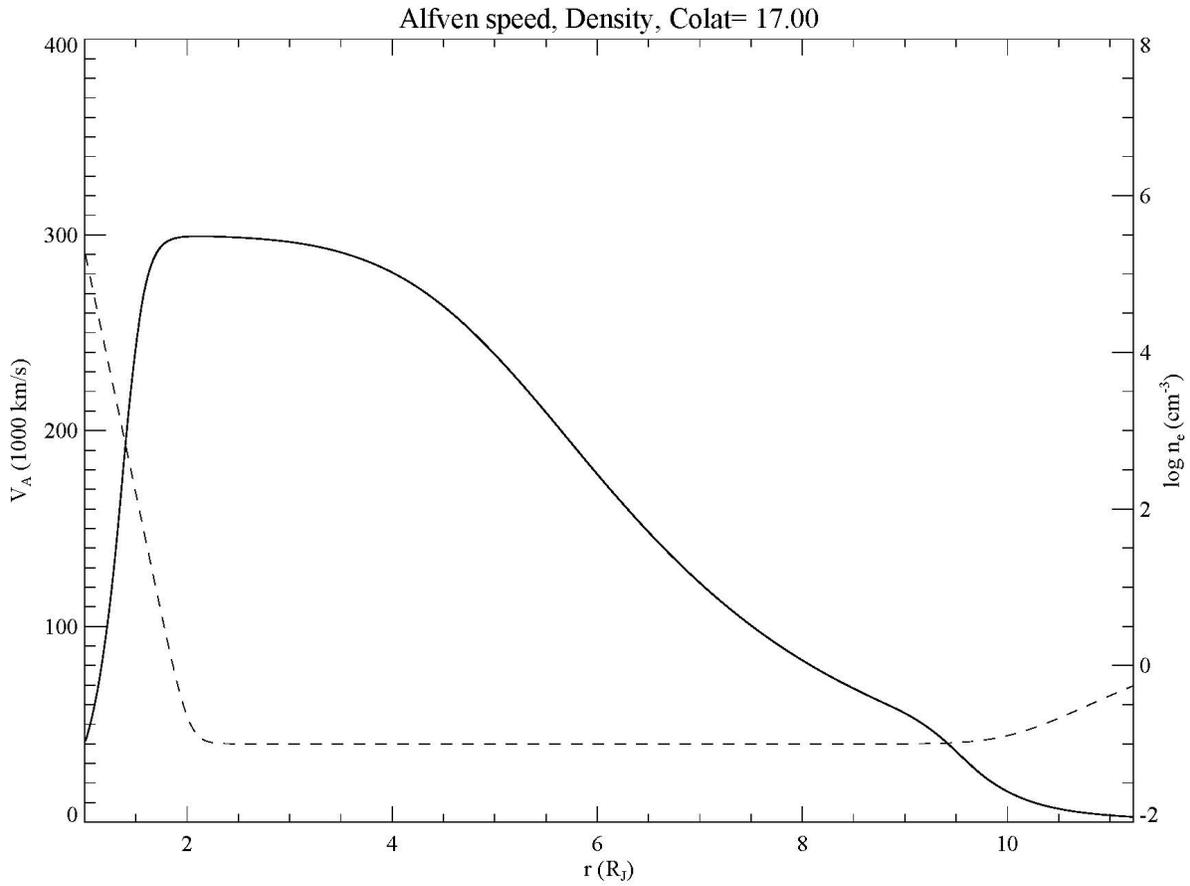
602 **Figure 2.** Amplitude of the electric field, normalized to the incident wave amplitude for the IAR  
 603 profile of Figure 1. Enhancements of the wave field at normalized frequencies of 2.4, 5.5 and  
 604 8.6 are evident.

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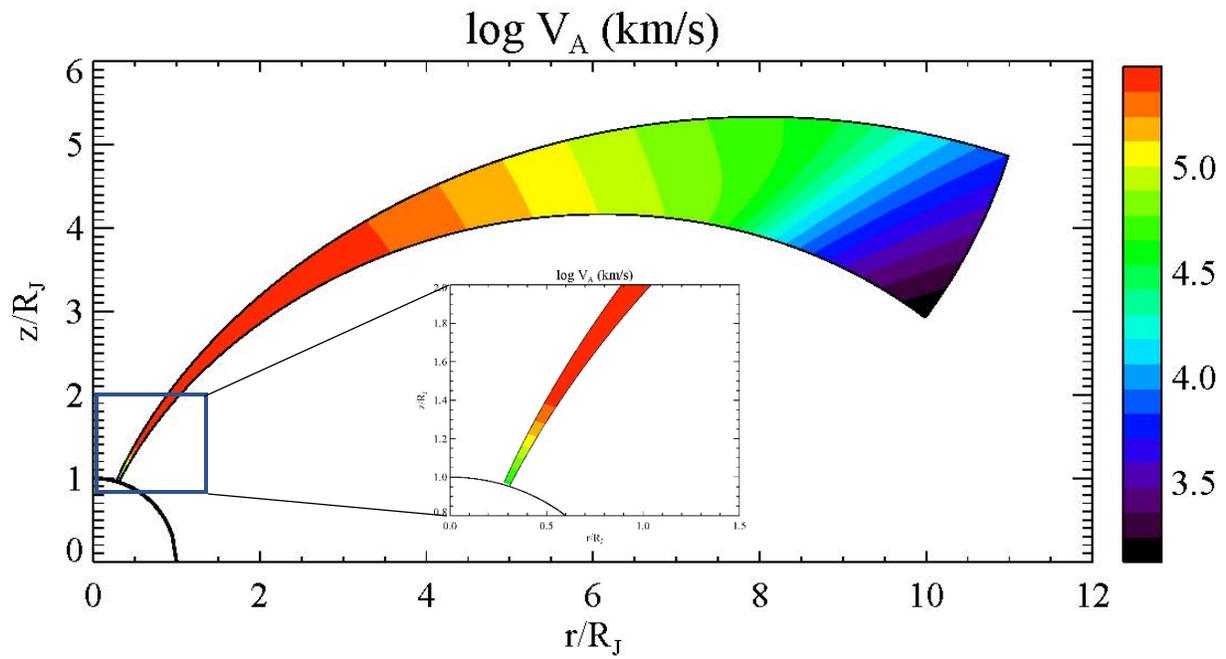
606 **Figure 3.** Plot of the simulation volume, with some representative field lines plotted along with  
 607 the curves at constant scalar potential that gives the coordinate parallel to the magnetic field.  
 608 The bracket indicates the region of the ionospheric Alfvén resonator where the main acceleration  
 609 will take place.

610



611 **Figure 4.** Profiles of the Alfvén speed (solid) and density (dashed) for the runs shown

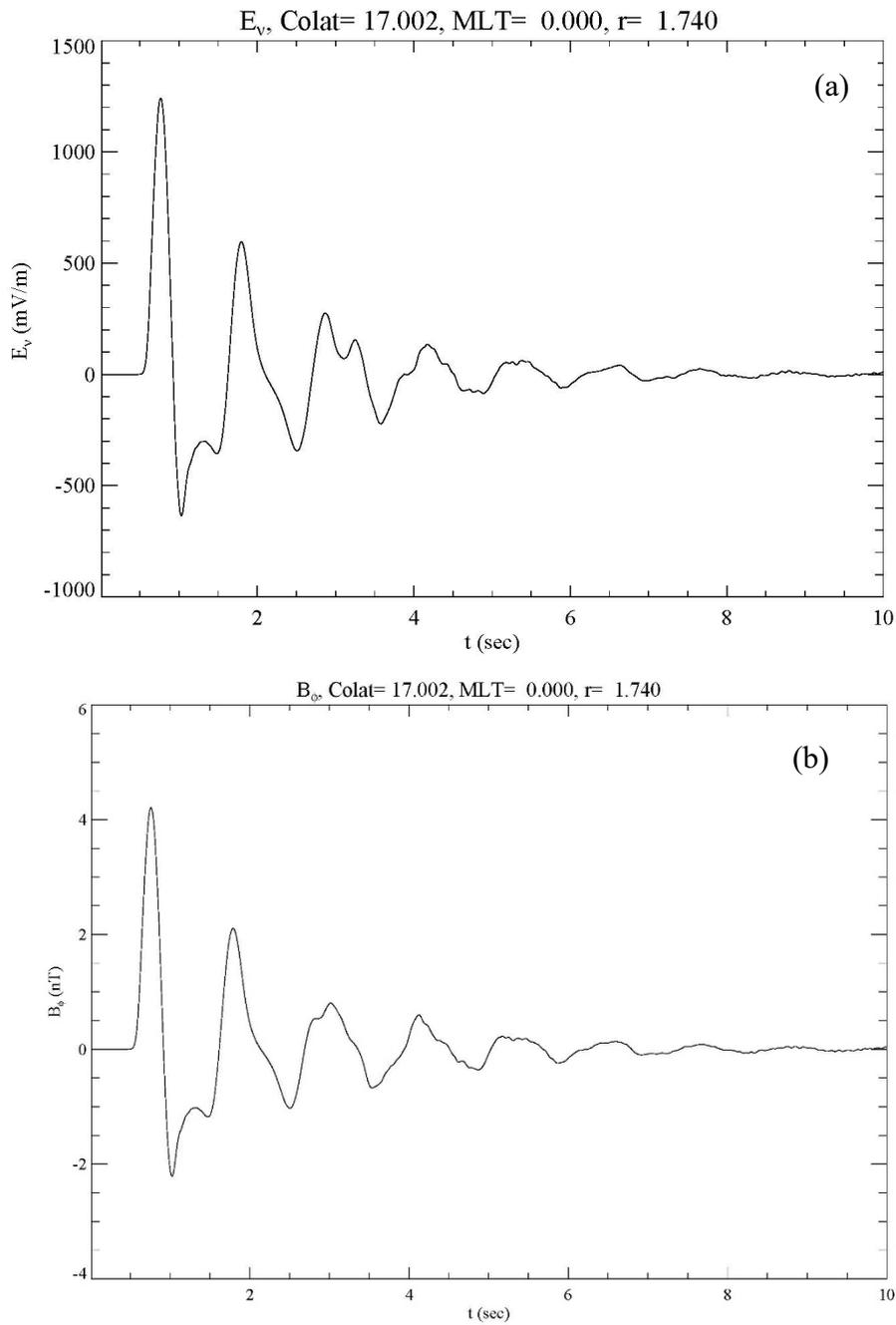
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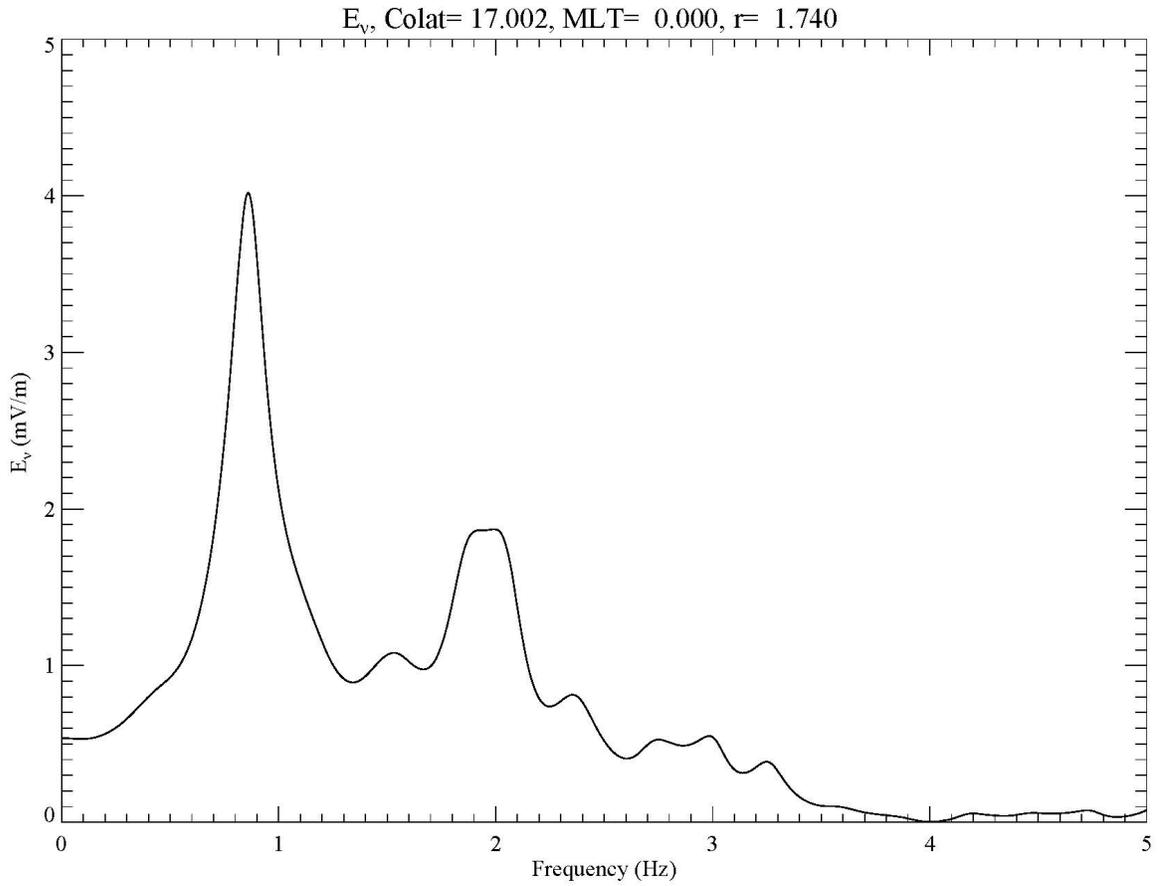
614 **Figure 5.** Plot of the log of the Alfvén speed overlaid on the grid of Figure 3. Inset: blowup of  
 615 ionospheric Alfvén resonator region.

616



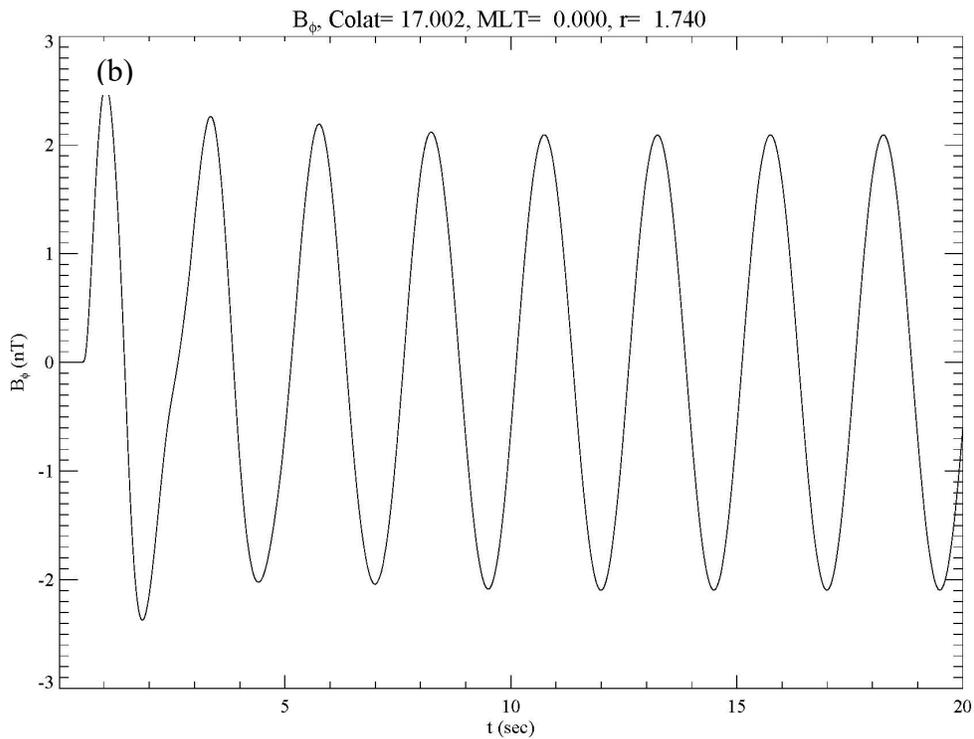
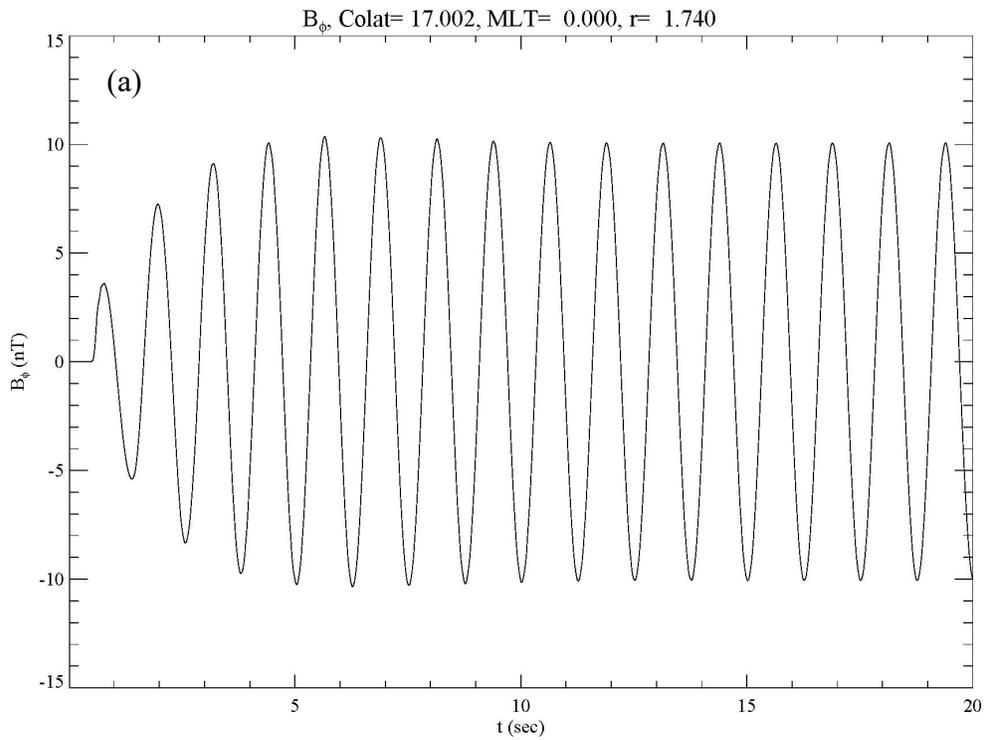
617 **Figure 6.** Profiles of the (a) electric field and (b) magnetic field for a run in which a 0.25 second  
 618 pulse was input from the ionospheric end of the simulation region.

619



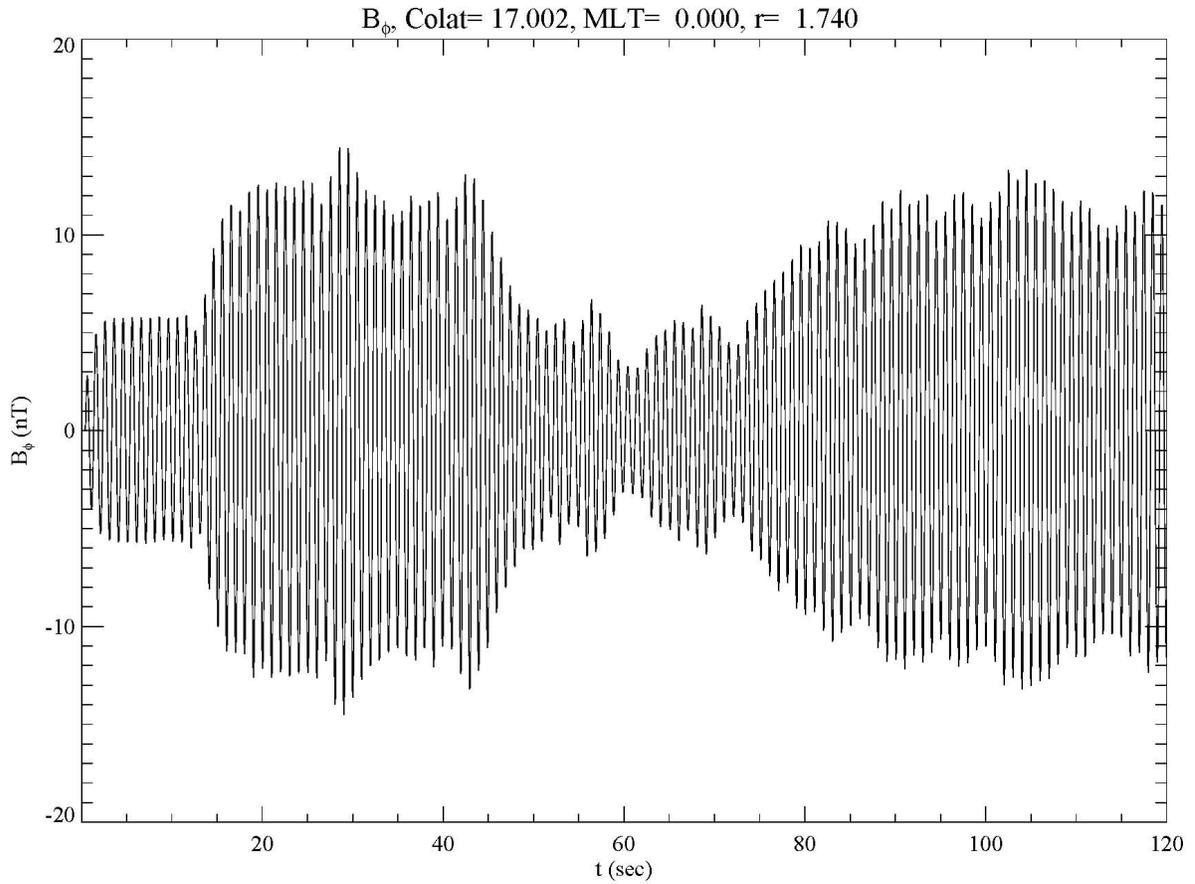
620 **Figure 7.** Fourier transform of the electric field of Figure 5a, showing resonant frequencies at  
621 0.8 and 1.8 Hz.

622



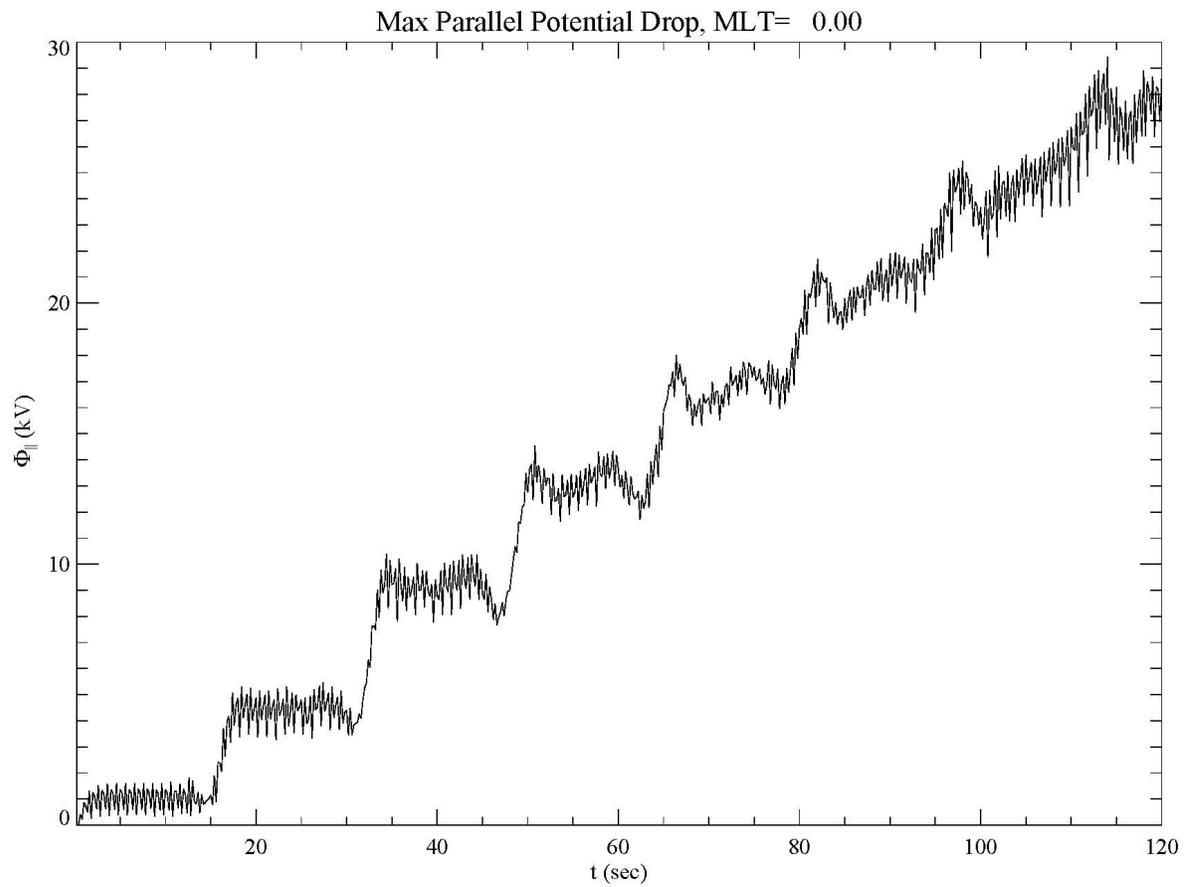
623 **Figure 8.** Response of the magnetic field to a driver at the (a) resonant frequency of 0.8 Hz; and  
 624 (b) at a non-resonant frequency of 0.4 Hz. The response is about 5 times greater at the resonant  
 625 frequency.

626



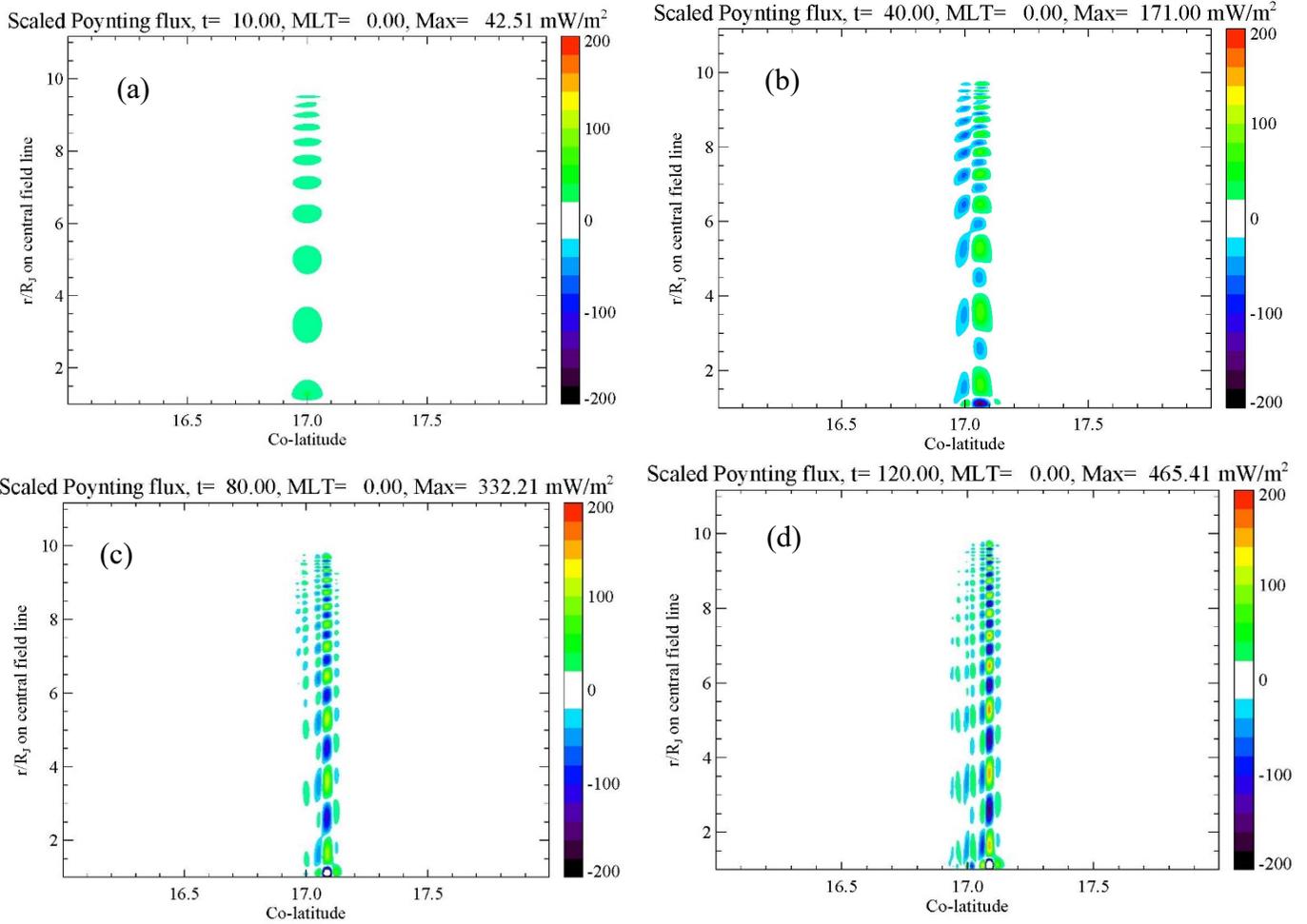
627 **Figure 9.** Time history of the magnetic field at  $17^\circ$  co-latitude for a run including the parallel  
628 electric field. The modulation of the field is due to the reflections from the boundary of the  
629 plasma sheet.

630



631 **Figure 10.** Integrated parallel electric field for the run of Figure 8. Reflections from the plasma  
632 sheet lead to the enhancement of the parallel potential drop on a 15-second time scale.

633

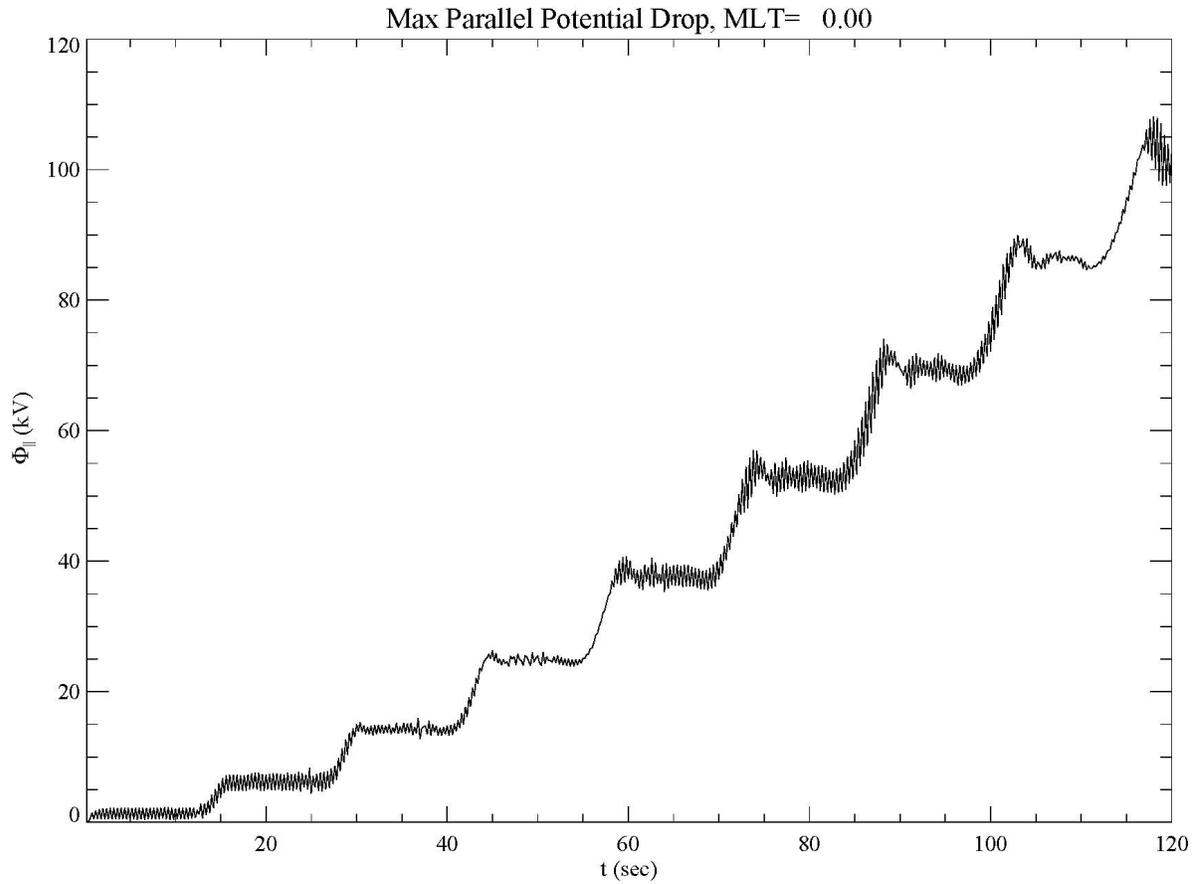


634

635

636 **Figure 11.** Contours of Poynting flux mapped to ionospheric heights at times of (a) 10 seconds;  
 637 (b) 40 seconds; (c) 80 seconds; and (d) 120 seconds into the run. Green/red colors indicate  
 638 upward Poynting flux and blue downward. After 10 seconds, the wave is moving upward from  
 639 the ionosphere. By 40 seconds wave has reflected from the Alfvén speed gradient at about  $10 R_J$   
 640 and is returning to the ionosphere. At later times, the Poynting flux is alternative in sign,  
 641 indicative of a standing wave. As the run progresses, there is increased structure in the  
 642 perpendicular direction due to phase mixing.

643



644 **Figure 12.** Maximum potential for a run in which the ionospheric scale height is decreased to  
645 4100 km, leading to a density of about  $1 \text{ cm}^{-3}$  at  $1.7 R_J$ .

646

647

648

649