Spatial and Seasonal Controls on Eddy Subduction in the Southern Ocean

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May 06, 2024

Abstract

Carbon export driven by submesoscale, eddy-associated vertical velocities ("eddy subduction") remains understudied, leaving a gap in our understanding of ocean carbon sequestration. Here, we assess mechanisms controlling eddy subduction's spatial and seasonal patterns using 15 years of observations from BGC-Argo floats in the Southern Ocean. We identify signatures of eddy subduction as subsurface anomalies in temperature-salinity and oxygen. The anomalies' spatial distribution is concentrated near weakly stratified areas and strong lateral buoyancy gradients diagnosed from satellite altimetry, particularly in the Antarctic Circumpolar Current's standing meander regions. Meanwhile, vertical stratification drives seasonal variability. Bio-optical proxies associated with subsurface anomalies (such as the Chlorophyll a to particulate backscatter ratio: Chl/bbp), indicate that eddy subduction is most active in the spring and early summer, with freshly exported material associated with seasonally weak vertical stratification. Climate change is increasing ocean stratification globally, which may weaken eddy subduction's carbon export potential.

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1 2	Spatial and Seasonal Controls on Eddy Subduction in the Southern Ocean
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6	
7	Key Points:
8 9 10 11 12 13 14	 Eddy subduction in the Southern Ocean is observed as subsurface anomalies in spice and oxygen measured by autonomous profiling floats Spatial distribution is controlled by weak stratification and strong lateral buoyancy gradients, diagnosed using satellite altimetry Bio-optical proxies suggest that eddy subduction is most active in spring/early summer, driven by weak vertical stratification

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17 remains understudied, leaving a gap in our understanding of ocean carbon sequestration. Here,

18 we assess mechanisms controlling eddy subduction's spatial and seasonal patterns using 15 years

of observations from BGC-Argo floats in the Southern Ocean. We identify signatures of eddy

subduction as subsurface anomalies in temperature-salinity and oxygen. The anomalies' spatial distribution is concentrated near weakly stratified areas and regions with strong lateral buoyancy

22 gradients diagnosed from satellite altimetry, particularly in the Antarctic Circumpolar Current's

standing meanders. Meanwhile, vertical stratification drives seasonal variability. Bio-optical

proxies associated with subsurface anomalies (such as the Chlorophyll *a* to particulate

²⁵ backscatter ratio: Chl/b_b), indicate that eddy subduction is most active in the spring and early

summer, with freshly exported material associated with seasonally weak vertical stratification.

27 Climate change is increasing ocean stratification globally, which may weaken eddy subduction's

28 carbon export potential.

29

30 Plain Language Summary

31 Oceans play an important role in global climate by soaking up and sequestering atmospheric

32 carbon dioxide. Photosynthetic activity at the surface turns carbon dioxide into organic carbon,

and if this carbon leaves the surface to the deep ocean, it can be locked away from the

34 atmosphere. One way this occurs is through the physical circulation associated with swirling

35 eddies, which can rapidly transport carbon-rich surface waters and "inject" them into deep

36 waters. However, we still don't fully understand the seasonal timing of this process, or what

drives its spatial distribution. We investigated this in the Southern Ocean, which is very

important to global climate, using data collected by drifting robots. We find that this process is

the most active in regions where eddies drive strong surface stirring, and during the spring, when

40 weak stratification allows injections to penetrate deep into the ocean. Because this process is

41 poorly represented in climate models, these findings will improve our understanding of how the

42 ocean absorbs carbon.

43 **1 Introduction**

44 Oceans play a critical role in regulating global climate by sequestering carbon from the

45 atmosphere (Gruber et al., 2009). A key driver of this is the biological pump, a suite of processes

that exports carbon from the ocean's surface to the interior, where it can be sequestered for years

47 to centuries. Recent modeling suggests that the biological pump keeps 1,300 Pg C sequestered

48 from the atmosphere (Nowicki et al., 2022). The best understood mechanism is the biological

49 gravitational pump, or the sinking of large particles and aggregates out of the euphotic zone,

50 which is estimated to comprise about 70% of global carbon export (Boyd et al., 2019; Nowicki et

al., 2022). However, contributions by other mechanisms of carbon export are increasingly being

52 recognized (Boyd et al., 2019). These include biological mechanisms such as transport by 53 vertically migrating mesopelagic organisms (Bianchi et al., 2013), and physical processes such

as carbon detrainment from shoaling mixed layers (the "mixed-layer pump"; Dall'Olmo et al.,

55 2016; Lacour et al., 2019), large-scale water mass subduction (the "subduction pump"; Levy et

- al., 2013), and submesoscale vertical velocities associated with frontal boundaries and eddies
- 57 (the "eddy subduction pump", or "ESP"; Omand et al., 2015; Resplandy et al., 2019).

58 Among these, eddy subduction (henceforth, also "subduction") remains understudied and under-59 observed due to the challenges of observing these submesoscale processes. In recent decades,

- submesoscale physics has emerged as a key driver of vertical biogeochemical transport.
- 61 Advances in high-resolution numerical modeling have revealed a dynamic eddy field at
- horizontal scales of O(1-10) m, associated with strong, ageostrophic vertical velocities reaching
- 63 up to 100 m day⁻¹. These evolve on timescales of O(1) days with a vertical extension of O(100)
- m, and strongly contribute to vertical tracer variability in models (Balwada et al., 2018; Capet et
- al., 2008; Klein & Lapeyre, 2009; Lapeyre & Klein, 2006; Lévy et al., 2012; Mahadevan &
- Tandon, 2006; Rosso et al., 2014). Mechanisms energizing these submesoscale flows include
- 67 surface frontogenesis associated with dynamic strain fields (Held et al., 1995; Lapeyre & Klein,
- ⁶⁸ 2006; Rosso et al., 2015), as well as baroclinic instabilities within the mixed layer ("mixed layer
- 69 instabilities"), which extract potential energy stored in lateral buoyancy gradients and deep
- mixed layers (Boccaletti et al., 2007; Callies et al., 2015, 2016; Erickson & Thompson, 2018);
 observations of seasonality in some regions have shown peak velocities associated with deep
- winter mixed layers (Buckingham et al., 2016; Callies et al., 2015; Thompson et al., 2016).

73 If downward vertical motions coincide with the presence of particulate carbon in the surface

- 74 ocean, carbon export can occur. During phytoplankton blooms, models and observations show
- that filaments of carbon-rich surface waters can be injected to depth along eddy peripheries.
- 76 Once subducted, these parcels of water retain tracer signatures of their surface origins, including
- elevated oxygen and surface-like temperature-salinity (Davies et al., 2019; Omand et al., 2015).
- Recently, Llort et al. (2018) developed an algorithm to detect eddy subduction events in BGC-
- Argo float profiles by identifying subsurface anomalies in apparent oxygen utilization (AOU)
- and spice (a temperature-salinity variable that reflects isopycnal water-mass contrasts;
- 81 McDougall & Krzysik, 2015), often co-located with elevated particulate organic carbon (POC).
- 82 This approach has been applied to identify eddy subduction in energetic regions such as the
- 83 Southern Ocean (Lacour et al., 2023; Llort et al., 2018), the North Atlantic (Johnson & Omand,
- 84 2021) and the Kuroshio Extension (Chen et al., 2021). Estimates of the eddy subduction pump's
- overall contribution to carbon export vary widely, ranging from being responsible for up to 50%
- of exported POC during spring blooms, to as little as <5% (Davies et al., 2019; Llort et al., 2018;
- Omand et al., 2015; Resplandy et al., 2019; Stukel & Ducklow, 2017).
- 88 Eddy subduction's seasonal variability and the mechanisms responsible remain unresolved,
- representing a major gap in carbon export estimates (Nowicki et al., 2022). Previous
- 90 observational studies have largely addressed seasonality through the timing of detecting
- subsurface anomalies, with mixed findings (Chen et al., 2021; A. R. Johnson & Omand, 2021;
- ⁹² Lacour et al., 2023; Llort et al., 2018). However, the timing of these observations don't
- necessarily reflect the timing of subduction itself, as the anomalies used for detection may have
- persisted at depth for months after subduction actually occurred (Johnson & Omand, 2021).
- 95 Here, we provide observational evidence from BGC-Argo floats in the Southern Ocean and
- ⁹⁶ integrate bio-optical proxies to assess eddy subduction's seasonality and spatial distribution, and
- 97 link it to physical drivers. We identify a seasonal cycle peaking in the austral spring, associated
- with weak vertical stratification. Integrating satellite altimetry, we find that strong lateral

- 99 buoyancy gradients, along with weak stratification, shape eddy subduction's spatial distribution,
- but not its seasonality. This work provides an important step towards understanding physical
- 101 contributions to carbon export in the Southern Ocean, a globally important region in ocean
- 102 carbon cycling.

103 2 Data and Methods

104 **2.1 Float Data**

- BGC-Argo float data are from the Southern Ocean Carbon and Climate Observations and
- 106 Modeling (SOCCOM) program. Floats conduct 2000 m vertical profiles every 10 days, and drift
- at a parking depth of 1000 m. Vertical sampling frequency varies between the two float types in
- this dataset: Navis floats sample every 2 m in the upper 1000 m, while APEX floats sample less frequently, with resolution decreasing with depth. Sampling schemes are described in Johnson et
- al. (2017), as well as processing of bio-optical parameters, including optical backscatter at 700
- (b_{bp}) , which is used to derive POC, and chlorophyll *a* fluorescence, which is used to derive
- 111 (b_{bp}) , which is used to derive POC, and chlorophyli *a* hubrescence, which is used to derive 112 chlorophyll *a* concentrations (Chl). Quality control procedures for all other variables are
- described in Maurer et al. (2021). Only data flagged as "good" were used.
- 114 Variables such as conservative temperature (CT) and absolute salinity (S_A) were derived using
- 115 the <u>Thermodynamic Equation of Seawater 2010</u> (TEOS-10; McDougall & Barker, 2011), and
- spice was calculated as a function of CT and SA, following McDougall & Krzysik, 2015. AOU
- 117 was calculated as (AOU= $O_2^{\text{sat}} O_2^{\text{obs}}$), where O_2^{sat} is the oxygen saturation concentration
- calculated using the coefficients of Garcia & Gordon (1992, 1993), and O_2^{obs} is the observed
- dissolved oxygen concentration. Mixed layer depth was defined using a density difference
- threshold of 0.05 kg m⁻³ from the surface, and buoyancy frequency squared (N^2) was calculated
- using TEOS-10.

122 **2.2 Eddy Subduction Anomaly Detection**

- 123 We identified eddy subduction anomalies in float profiles using an algorithm adapted from Chen
- 124 et al. (2021) and Llort et al. (2018). An example is shown in Figure 1, detected on the periphery
- of a mesoscale eddy (Figure 1a). We considered profiles between 30°S and 65°S, and discarded
- profiles with surface salinity > 35 psu, following Llort et al. (2018). We also only considered
- 127 profiles where the median spice value in the mixed layer was lower than that at 600 m, as
- increasing spice with depth in the upper 1000m is characteristic of Southern Ocean waters
- 129 (Tailleux, 2021). Navis floats were down-sampled by selecting data at APEX sampling depths,
- allowing for comparable vertical resolution. Profiles were then vertically smoothed with a 3-bin
- rolling median. The total dataset contained 9,354 profiles collected from February 2008 through
- 132 August 2023.
- 133 For each smoothed profile, we identified co-occurring peaks in spice and AOU between the
- MLD and 600 m depth (defined as relative minima found within 30 meters of each other, at
- 135 depths h_{spice} and h_{AOU} ; Figure 1b,c). We then defined reference profiles to simulate
- 136 "background", ambient values in the absence of subduction (orange lines, Figure 1b,c). An initial
- 137 guess for the reference profile is defined as the straight line in between the maximum values
- above and below each peak (within 100 m in either direction), following Chen et al., 2021. If the

- line intersects with the observed profile, the top and bottom boundaries of this initial guess are
- 140 iteratively adjusted inwards (towards the peak) until the profiles no longer intersect (Supporting
- 141 Information Figure S1). We then calculated the difference between the observed value and the
- 142 calculated reference value at h_{spice} and h_{AOU}, yielding Δ_{spice} and Δ_{AOU} , respectively (Figure 1b,c). 143 Peaks were classified as eddy subduction pump anomalies ("ESP anomalies") if $\Delta_{spice} < -0.05$
- Peaks were classified as eddy subduction pump anomalies ("ESP anomalies") if $\Delta_{\text{spice}} < -0.05$ kg/m³ and $\Delta_{\text{AOU}} < -8 \,\mu\text{mol/kg}$, following Llort et al. (2018). The anomaly depth was defined at
- h_{AOU} , and the vertical extent of the anomaly (H) was defined as the extent of the reference profile
- for AOU. We discarded anomalies found within 100 m of the MLD in order to avoid
- 147 misidentifying detrainment from shoaling mixed layers (Lacour et al., 2019).
- 148 In order to quantify subduction-driven values associated with an anomaly (e.g. POC and
- 149 Chl/ b_{bp}), we first integrated the observed quantities over the span of H (e.g. POC_{ESP_total} and
- 150 $\text{Chl/}b_{bp_total}$). We then estimated the ambient values (i.e. in the absence of subduction) by
- 151 integrating through reference profiles, defined as the straight line between the observed values at
- the top and bottom of H (e.g. POC_{ambient} and $Chl/b_{bp_ambient}$:_hatched regions in Figure 1d,e). We
- subtracted ambient values from total values, yielding "subduction-driven" integrated values (e.g.
- 154 POC_{ESP} and Chl/ b_{bp} _ESP: green shaded regions in Figure 1d,e). Finally, we normalized these by H
- to yield depth-averaged, subduction-driven quantities within anomalies (e.g. POC_{ESP_avg} and
- 156 $Chl/b_{bp_ESP_avg}$), which are the principal values discussed hereafter.

157 2.3 Satellite Data

- 158 Finite-size Lyapunov Exponents (FSLEs) were downloaded from AVISO+. FSLEs describe
- 159 stretching and compression by quantifying the exponential rate of separation (λ) of neighboring
- 160 particles advected in a flow field: $\lambda(d_0, d_f) = \frac{1}{t} \log(\frac{d_f}{d_0})$, where d_0 and d_f are the initial and final
- distances between the particles, respectively, and t is the time it takes for the particles to reach d_f
- 162 (d'Ovidio et al., 2004). The AVISO+ product uses daily, altimetry-derived geostrophic velocity
- 163 fields to advect particles backward-in-time, so FSLEs are negative, with stronger negative values
- 164 indicating stronger stretching; these FSLE ridges indicate transport barriers and are preferentially
- located between eddy cores (Siegelman et al., 2020a; also demonstrated here in Figure 1a).

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Figure 1. Example of an eddy subduction anomaly detected in a float profile. (a) Map depicting 168 float track and profile location (red circle). Inset shows the same-day surface FSLE field. Red 169 circle = profile location. Shaded red box = the $1^{\circ}x1^{\circ}$ area used to retrieve the strongest FSLE in 170 the profile's vicinity. The float's vertical profiles are shown in (**b-d**), with the MLD indicated by 171 a purple line. Blue lines depict smoothed profiles. The shaded orange band indicates H, the 172 vertical extent of the subduction anomaly. (b) Spice profile. Dotted orange line shows Δ_{spice} at 173 depth h_{spice} , or the difference between the observed value and the calculated reference value 174 (orange circles). The reference profile is shown by the orange line. (c) AOU profile, with 175 reference profile and Δ_{AOU} , similar to the spice profile. (d) POC profile. Shaded green region: 176 POC_{ESP}, the integrated quantity of subduction-driven POC. Hatched region: POC_{ambient}, the 177 subtracted, integrated quantity of ambient POC. (e) Chl/bbp ratio profile. Shaded green area: 178 Chl/bbp_ESP, similar to POC. Hatched region: Chl/bbp_ambient, not visible because values are 179 roughly 0. 180

181 **3 Results and Discussion**

182 **3.1 Spatial Distribution of Eddy Subduction**

183 The BGC-Argo dataset provides full, basin-wide spatial coverage of the Southern Ocean over 15

184 years. We find eddy subduction anomalies in 4.4% of profiles, defined as coherent, negative

185 mesopelagic anomalies in spice and AOU (Figure 1b,c), frequently associated with positive

anomalies in bio-optical parameters (Figure 1d,e). These anomalies are spatially concentrated

around the Polar Front and Antarctic Circumpolar Current (ACC), consistent with Llort et al.

188 (2018) (Figure 2a). However, their circumpolar distribution is uneven, with most detected in the

189 ACC's standing meander regions: the Eastern Pacific Rise, the Kerguelen, Crozet, and Campbell

190 Plateaus, and the Drake Passage. These regions are known for enhanced eddy kinetic energy

191 (EKE) and vertical exchange (Dove et al., 2022), as the vigorous flow of the ACC is diverted by

underwater topography, generating mesoscale eddies that strain surface density fields and create

strong lateral buoyancy gradients. This frontogenesis can subsequently energize vigorous

194 submesoscale motions (Rosso et al., 2015).

195 To better assess spatial distribution, we use altimetry-derived FSLEs, a powerful Lagrangian

diagnostic of submesoscale activity. FSLEs are elevated within the ACC's standing meanders

197 (Dove et al., 2022), and strong FSLEs have been shown to be co-located with strong, deep-198 reaching submesoscale lateral buoyancy gradients and the intense vertical velocities associated

with them (Siegelman, et al., 2020a,b). Thus, to assess whether a given float profile was in the

vicinity of submesoscale fronts, we matched each profile with its same-day satellite FSLE field

and identified the strongest FSLE within the surrounding 1°x1° area (e.g. within the red square in

Figure 1a). These matchups are displayed in Figure 2b and clearly show the ACC's standing

203 meanders as hotspots of submesoscale activity (i.e. strong FSLEs), largely congruent with the

204 distribution of eddy subduction anomalies.

However, some groups of anomalies are detected in comparatively quiescent regions in between

the standing meanders, such as 60-120°W and 150-180°W (Figure 2a,b). Vertical stratification

207 strength is another mechanism known to influence submesoscale activity, with weak

stratification allowing deeper penetration of vertical velocities (Callies et al., 2016; Erickson &

209 Thompson, 2018). Although stratification shows a less dramatic spatial pattern than FSLEs,

210 many float profiles in these regions have notably weak stratification (yellow colors in Figure 2c),

suggesting that this could also influence eddy subduction's spatial distribution. These

mechanistic relationships will be further explored statistically in Section 3.3.

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214

- Figure 2. Maps of the float dataset. Colored lines indicate front locations as defined by mean 215 dynamic topography from satellite altimetry (Park & Durand, 2019): purple=Subantarctic Front 216 (SAF); green=Polar Front (PF); blue=Southern ACC Front (SACCF). (a) Locations of eddy 217 218 subduction anomalies across the Southern Ocean. Gray circles indicate all float profiles considered in the analysis. Purple-scale colored circles indicate detected ESP anomalies, colored 219 by the magnitude of Δ_{AOU} . (b) Spatial distribution of FSLE magnitudes, a proxy for the strength 220 of lateral buoyancy gradients. Each point is a satellite matchup to a float profile, showing the 221 strongest FSLE within $1^{\circ}x1^{\circ}$ of each profile. (c) Spatial distribution of vertical stratification in 222 each float profile, measured as maximum N², and displayed on a log-scale. The colorscale 223 maximum is limited to 10^{-4} (roughly the median of the maximum N² distribution; see Figure 4d) 224
- to emphasize variation in the lower half of the distribution.

226 **3.2 Seasonality of Eddy Subduction**

- 227 We detect subduction anomalies more frequently during summer months (Figure 3a). However,
- the timing of detection does not necessarily indicate the timing of subduction, as the coarse
- spatial and temporal resolution of BGC-Argo floats cannot provide Lagrangian tracking of
- individual subduction events as they evolve. Instead, our method can only identify subsurface

tracer anomalies after subduction occurs, and these anomalies may persist for months at depth 231 afterwards (Johnson & Omand, 2021). 232

To assess the timing of subduction, we look at other proxies. A useful metric is the Chl/b_{bp} ratio, 233 or the ratio of chlorophyll *a* to particulate backscatter. At the surface, this ratio reflects 234 phytoplankton photophysiology and community composition (Barbieux et al., 2018; Cetinić et 235 al., 2015; Rembauville et al., 2017). However, beneath the mixed layer, it can be a proxy for the 236 freshness of exported material; in the days after particulate material leaves the mixed layer, 237 238 Chl/b_{bp} decays by a power law as phytoplankton and their pigments degrade (Lacour et al., 2019). Accordingly, this ratio is high within the mixed layer and over an order of magnitude 239 lower in the mesopelagic (Supporting Information Figure S2). Within subduction anomalies, 240 $Chl/b_{bp_ESP_avg}$ is frequently elevated relative to ambient mesopelagic waters, indicating freshly 241 subducted phytoplankton biomass (Figure 1e). It also has a notable seasonal cycle, with the 242 highest values, indicating the most freshly subducted material, occurring during the spring and 243 early summer (Figure 3b). AOU within subducted anomalies (AOU ESP avg) shows a similar 244 seasonality, with the most negative values occurring during the spring (Figure 3c), indicating less 245

- respiration, or "aging", has occurred. 246
- By comparison, the seasonal cycle of eddy-subducted POC (POC_ESP_avg; Figure 1d) is slightly 247
- delayed, with summer-detected anomalies carrying the highest POC content (Figure 3d). This 248
- suggests that despite high Chl/bbp_ESP_avg values, springtime subduction events may not 249
- necessarily export large amounts of biomass. However, most detected anomalies carry little 250
- excess POC relative to ambient waters, resulting in little seasonality when averaging (Figure 3d). 251
- Importantly, these seasonal cycles are distinct from those of ambient values in the mesopelagic, 252
- which are influenced by other processes such as gravitational sinking of large particles. Ambient 253
- values of both POC and Chl/b_{bp} show strong seasonality beneath the mixed layer, peaking in 254
- mid-late summer (Supporting Information Figure S3). Spike analyses following Briggs et al. 255
- (2011) indicate that this is likely driven by large particle sinking, which is also highest during 256
- mid-late summer (Supporting Information Figure S4). 257
- The metrics here provide a novel, qualitative overview of previously unresolved seasonality in 258
- eddy subduction, suggesting it is most active in the spring and early summer. However, fully 259
- understanding its timing will require high-resolution sampling to dissect the physical and 260
- biogeochemical processes that contribute to the destruction of coherent tracer anomalies over 261
- time; for example, turbulent mixing will affect all variables discussed here, while respiration will 262
- transform biogeochemical tracers such as AOU and POC. The Chl/b_{bp} ratio is additionally 263
- subject to chlorophyll pigment degradation. Notably, anomalies in spice should only be 264
- dissipated by turbulent mixing, and spice ESP avg does not show a seasonal cycle (Figure 3e), 265
- suggesting that the relative roles of physics vs respiration in dissipating subducted features need 266
- to be further untangled. However, the observed seasonality is informative in diagnosing 267
- 268 mechanisms, discussed next.





Figure 3. Seasonal patterns across observed ESP anomalies. X-axis ticks correspond to [June, Sept, Dec, Mar]. (a) Detection rate of ESP anomalies per month, normalized by the total number of profiles per month. Plots (b-e) show seasonality of depth-averaged properties within ESP anomalies, with ambient values subtracted. Line plots depict medians, with shaded regions indicating interquartile ranges. Overlain strip plots show individual data points. (b) POC_ESP_avg, (c) Chl/bbp_ESP_avg, (d) AOU_ESP_avg, (e) spice_ESP_avg. Axis limits in (b) and (d) display 98% of

277 data points.

278 **3.3 Physical and Biological Mechanisms Controlling Spatial and Seasonal Patterns**

279 Multiple physical and biological processes are required for eddy subduction. Physically, the

strength of submesoscale overturning circulations scales with strong lateral buoyancy gradients

and deep mixed layers (Fox-Kemper et al., 2008). Additionally, weak vertical stratification

allows these velocities to penetrate deeper into the interior (Callies et al., 2016; Erickson &

283 Thompson, 2018). Finally, POC must be available at the ocean's surface for export. Examining

seasonal cycles in these variables, spring/early summer emerges as a period conducive to eddy

subduction across the Southern Ocean, with an overlap of deep mixed layers, weak vertical

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stratification (defined as maximum N²), and increasing POC in the mixed layer (Figure 4a). This
aligns with the seasonality discussed in Section 3.2. Interestingly, altimetry-derived FSLEs, an
indicator of lateral buoyancy gradients (Siegelman et al., 2020a), do not show a seasonal cycle
here (Figure 4b), suggesting that lateral buoyancy gradients in this region may not drive the eddy
subduction's seasonality.

Statistical distributions of float profiles provide further insights into these mechanisms. Profiles 291 with subduction anomalies are shifted towards higher surface POC content (Figure 4c), 292 293 demonstrating that carbon must be available to be exported. Similarly, profiles with subduction anomalies are shifted towards more weakly stratified water columns (Figure 4d). Profiles with 294 anomalies in the top quartile of Chl/b_{bp} ESP avg values, likely the most recently subducted, are 295 even more weakly stratified. Direct comparison of maximum N² to Chl/b_{bp_ESP_avg} suggests that 296 weak stratification is a prerequisite for detecting recent eddy subduction (Supporting Information 297 Figure S5). Interestingly, despite its strong seasonality, mixed layer depth does not show much 298 effect – distributions are similar between profiles with and without subduction anomalies (Figure 299 4e). Conversely, although FSLEs do not show seasonality, profiles with subduction anomalies 300 are strongly shifted towards stronger nearby FSLEs, implying closer proximity to strong lateral 301 302 buoyancy gradients (Figure 4f).

These statistical analyses indicate that in the Southern Ocean, strong lateral buoyancy gradients 303 and weak vertical stratification exert significant physical controls on eddy subduction. The 304 spatial analyses in Section 3.1 suggest that these mechanisms drive eddy subduction's 305 concentration in standing meanders and weakly stratified areas. Meanwhile, the seasonal 306 analyses in Sections 3.2 and 3.3 suggest that vertical stratification is the dominant driver of 307 seasonality, along with the seasonal availability of surface POC. Mixed layer depth appears to 308 exert little influence. Thus, in areas prone to submesoscale motions, weak springtime 309 stratification may act as a seasonal trapdoor that determines whether they can export material 310 beneath the mixed layer. Indeed, this is consistent with Stommel's Demon, which argues that a 311 "demon" selects the properties of late winter water to be injected into the ocean interior 312

313 (Stommel, 1979).



315

Figure 4. Mechanisms driving eddy subduction. (a) Seasonality of water column properties for
all float profiles, showing MLD (blue), maximum N² (red), and depth-averaged POC within the
surface mixed layer (olive). The line plot depicts medians, with shaded regions indicating
interquartile ranges. (b) Seasonality of altimetry-derived FSLE magnitudes. The strip plot shows
satellite matchups to each float profile, showing the strongest FSLE within 1°x1°. Line plot as in
(a). (c-f) Cumulative distribution plots of profiles by various mechanistic variables. Each curve

322 represents the cumulative proportion of observations falling below the corresponding x-axis

- value. Colors indicate all profiles (blue), only profiles with ESP anomalies (orange), and only
- profiles with ESP anomalies with the highest 25% Chl/bbp_ESP_avg values (green) (c) Depth-
- averaged mixed layer POC (\log_{10}) (d) Maximum N² (\log_{10}) . (e) Mixed layer depth. (f) Magnitude
- of the strongest altimetry-derived FSLE within a $1^{\circ}x1^{\circ}$ area.

327 **5 Conclusions**

- 328 Our work has several broad implications for our understanding of carbon export and
- 329 submesoscale dynamics, and emphasizes open questions for the community. First, we find
- evidence of a seasonal cycle in eddy subduction, which has remained unresolved in global
- carbon export calculations (Nowicki et al., 2022). Future work should assess global variability in regions beyond the Southern Ocean. Second, we highlight the utility of bio-optical proxies such
- as Chl/b_{bp} ratios beneath the ocean's surface. However, high-resolution sampling is necessary to
- quantify the evolution and aging of tracers over the course of submesoscale processes. Third, we
- emphasize the power of contextualizing subsurface float observations with Lagrangian
- diagnostics from satellites such as FSLEs. Finally, we identify strong lateral buoyancy gradients
- and weak vertical stratification as key spatiotemporal controls on vertical exchange in the
- 338 Southern Ocean. Future investigation should untangle specific physical mechanisms and the
- relative impacts of frontogenesis versus instabilities (Archer et al., 2020; Callies et al., 2015;
- Erickson & Thompson, 2018; Klein & Lapeyre, 2009; Rosso et al., 2015). Finally, climate
- change has been driving increased stratification strength across global oceans (Sallée et al.,
- 342 2021), potentially decreasing eddy subduction's contribution to global carbon export.

343 Acknowledgments

- The authors are grateful for conversations with Joan Llort, Shuangling Chen, Léo Lacour, Laure
- Resplandy, Kathleen Abbott, Lily Dove, Mara Freilich, and Jackie Veatch. Float data were
- collected and made freely available by the SOCCOM Project funded by the National Science
- Foundation, Division of Polar Programs (NSF PLR -1425989 and OPP-1936222), supplemented
- by NASA, and by the International Argo Program and the NOAA programs that contribute to it.
- The Argo Program is part of the Global Ocean Observing System. M.L. Chen acknowledges
- NASA Grant 80NSSC22K1451. O. Schofield acknowledges NASA Grant 80NSSC21K0969.

351 **Open Research**

- Float data were downloaded from the <u>UCSD SOCCOM and GO-BGC data archive</u>. Our analyses
- use the delayed-mode, quality controlled, low-resolution snapshot from <u>2023-08-28</u> (Riser et al.,
- 2023). Altimetry-derived FSLEs were produced by Ssalto/Duacs in collaboration with LOcean
- and CTOH and distributed by AVISO+, with support from CNES
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- 357 <u>exponents.html</u>). Analyses were conducted in Python 3.8.17 using Xarray version 2022.11.0,
- available under the Apache license at <u>https://docs.xarray.dev/</u> (The Xarray Development Team,
- 359 2022); GSW version 3.6.17, available under the GSW License at <u>https://www.TEOS-10.org</u>
- 360 (McDougall & Barker, 2011); and Pandas version 1.5.3, available under the BSD 3-Clause
- ³⁶¹ "New" or "Revised" License at <u>https://pandas.pydata.org</u> (The Pandas Development, 2023).

- 362 Figures were plotted using Matplotlib version 3.7.1, available under the Matplotlib license at
- 363 <u>https://matplotlib.org</u> (The Matplotlib Development Team, 2023); Seaborn version 0.12,
- available under the BSD 3-Clause "New" or "Revised" License at <u>https://seaborn.pydata.org</u>
- 365 (The Seaborn Development Team, 2022); and Cartopy version 0.21.1, available under the BSD-3
- Clause License at <u>https://scitools.org.uk/cartopy/</u>) (The Cartopy Development Team, 2022). The
- 367 software associated with this manuscript for data processing and analysis is licensed under MIT
- and published on GitHub <u>https://github.com/mchen96/southern_ocean_eddy_subduction/</u>, and
- 369 can be run in a zero-install environment on the cloud at
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