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Abstract

Understanding the coupling between rock permeability, pore pressure, and fluid flow is crucial, as fluids play an important role in the Earth's crustal dynamics. We measured the distribution of fluid pressure during fluid-flow experiments on two typical crustal lithologies, granite and basalt. Our results demonstrate that the pore-pressure distribution transitions from a linear to a non-linear profile as the imposed pore-pressure gradient is increased (from 2.5 MPa to 60 MPa) across the specimen. This nonlinearity results from the effective pressure dependence of permeability, for which two analytical formulations were considered: an empirical exponential and a new micromechanics-based model. In both cases, the non-linearity of pore pressure distribution is well predicted. However, using a compilation of permeability vs. effective pressure data for granites and basalts, we show that our micromechanics-based model, which combines the rough crack asperity model and cubic law theories, outperforms the exponential formulation at low effective pressures.

Pressure dependence of permeability in cracked rocks: experimental 1 evidence of non-linear pore-pressure gradients from local measurements 2 Gang Lin¹, Samuel Chapman¹, Dmitry Garagash², Jérôme Fortin¹ and Alexandre Schubnel¹ 3 4 1. Laboratoire de Géologie, Ecole Normale Supérieure/CNRS UMR 8538, PSL Research 5 University, Paris, France. 6 2. Department of Civil and Resource Engineering, Dalhousie University, Halifax, Nova Scotia, 7 Canada 8 Corresponding author: Gang Lin (gang@geologie.ens.fr) 9 **Key points:** 10 11 Pore pressure was measured locally in rocks exhibiting pressure-dependent permeability.

- We observed a transition from linear to nonlinear pore pressure distribution with increasing
 fluid pressure gradients.
- A new, micromechanics-based, analytical model was developed for the pressure
 dependence of permeability in microcracked rocks.
- 16

17 Abstract:

18 Understanding the coupling between rock permeability, pore pressure, and fluid flow is crucial, as 19 fluids play an important role in the Earth's crustal dynamics. We measured the distribution of 20 fluid pressure during fluid-flow experiments on two typical crustal lithologies, granite and basalt. 21 Our results demonstrate that the pore-pressure distribution transitions from a linear to a non-22 linear profile as the imposed pore-pressure gradient is increased (from 2.5 MPa to 60 MPa) 23 across the specimen. This non-linearity results from the effective pressure dependence of 24 permeability, for which two analytical formulations were considered: an empirical exponential 25 and a new micromechanics-based model. In both cases, the non-linearity of pore pressure 26 distribution is well predicted. However, using a compilation of permeability vs. effective 27 pressure data for granites and basalts, we show that our micromechanics-based model, which 28 combines the rough crack asperity model and cubic law theories, outperforms the exponential 29 formulation at low effective pressures.

30

31 Plain Language Summary:

Fluids and fluid migrations play an important role in the Earth's crustal dynamics and how fluids migrate through a rock will depend primarily on permeability. However, the permeability of crustal rocks may exhibit important pressure dependence, because cracks and fractures will increasingly close with increasing tectonic pressure. In this experimental study, we show that the couplings between increasing pressure, crack closure, and permeability reduction may result in non-linear pore pressure distributions on a rock specimen at the laboratory scale, which confirms for the first time pioneering theoretical and experimental works. Two simple analytical expressions of the pressure dependence of permeability predict this non-linearity. One empirical expression, most commonly used in the literature, takes the form of an exponential. The second one, a new model, based on crack micromechanics, was developed within this work and shown to outperform the exponential formulation at low effective pressure.

43

44 **1. Introduction**

45 Fluid migration and pore pressure distribution in the crust are important parts of the Earth's system and have an impact on most geological activities, such as groundwater circulation 46 (Corbet & Bethke, 1992; Thomas et al., 2023), mineral resources formation (Li et al., 2022; Tivey, 47 48 2007), magmatic fluid pressurizations (Fazio et al., 2017; Gueugneau et al., 2017; Manga & 49 Brodsky, 2006), and induced earthquakes (Keranen et al., 2014; Kim et al., 2018). Indeed, recent 50 tomographic studies on the Changning earthquake in China (Lei et al., 2019; Li et al., 2021) and 51 the Pohang earthquake in South Korea (Kim et al. 2018; Yeo et al. 2020) have emphasized the 52 crucial importance of pore pressure excess in triggering earthquakes (Ellsworth, 2013; Guglielmi et al., 2015). In the Earth's crust, the mechanisms that may lead to pore pressure excess involve 53 54 complex couplings between stress (in the fluid and matrix), temperature, and rock physical 55 properties (e.g. porosity and permeability) (Rice, 1992; Rice, 2006) or even, at greater depth, 56 mineral dehydration (Brantut et al., 2010; Wong et al., 1997). However, in-situ measurements of 57 pore pressure in the field are difficult outside of local measurements around boreholes.

58 It was generally considered during fluid injection into the subsurface that the front of micro-59 seismicity follows closely the pore pressure diffusion front (Shapiro & Dinske, 2009). In the last 60 years, some publications have supported the view that the micro-seismicity front is more likely 61 to be related to the propagation of a slow slip front, while the pore pressure diffusion front lags 62 behind (Bhattacharya & Viesca, 2019; Danré et al., 2024; Eyre et al., 2019; Garagash et al., 63 2017; Guglielmi et al., 2015). To mitigate potential geological hazards associated with fluid 64 pressure, a better understanding of the pore pressure diffusion and distribution laws in crystalline 65 and/or low porosity/tight rocks is important.

The permeability of rocks has been studied experimentally for decades and was shown to exhibit important pressure dependence, mainly because of elastic crack-closure as (effective) confining pressure increases (Brace et al., 1968). Many empirical models were used to describe the permeability changes with effective stress, which can generally be divided into two classes of models: exponential or power law pressure dependence. David et al. (1994) used an exponential law to describe the permeability dependence of five kinds of sandstones. They also adopted such an exponential pressure dependence for the permeability of a natural Grimsel

73 granodiorite (David et al., 2018), and finally concluded that this relationship was suitable for 74 relatively high effective stress ranges. The exponential law model was also widely used in 75 describing the pressure dependence of permeability in faults (Evans et al., 1997; Ji et al., 2023). 76 A significant limitation of the exponential law model is its inability to provide accurate fits at a 77 low effective pressure range. The power law is another method to characterize permeability 78 pressure dependence (Ghabezloo et al., 2009; Morrow et al., 1984; Su et al., 2022). However, it 79 cannot be regarded as a general constitutive relation due to its divergence at zero effective 80 pressure (Jia et al., 2017; Zheng et al., 2015).

81 The pressure dependence of rock permeability has been used by David et al. (1994) and 82 Rice (1992) to argue for the presence of non-linear pressure gradients across faults and within 83 the crust. Another important question is the occurrence of non-linear pore pressure diffusion and 84 distribution during laboratory experiments. While experimental inferences have been reported using strain gages (Garagash et al., 2017), new measurement techniques have recently been 85 developed to measure the fluid pressure locally on samples in the laboratory. For instance, 86 87 Dautriat et al. (2009) were able to measure the radial and axial permeability of cylindrical rock samples by injecting fluid and monitoring pore pressure along the sides of the specimens. 88 Nicolas et al. (2020) monitored the diffusion of pore pressure pulses in intact andesite rock using 89 90 fiber optic sensors and modeled this process by solving the diffusion equation. Brantut and Aben 91 (2021) introduced newly developed strain-gauge based pore pressure transducers and used them 92 on sandstone and granite. Proctor et al. (2020) pre-embedded sensors in a granite sample 93 adjacent to a saw-cut plane to detect the variations in pore pressure during rupture nucleation 94 and concluded that the effect of fluid pressure changes can exceed that of frictional variations. 95 A similar experiment was conducted by Brantut (2020), who focused on fluid pressure drop 96 induced by dilatancy and reported the occurrence of partial vaporization or degassing of fluid 97 during rupture.

98 Here, we use a similar sensor design to that of Brantut and Aben (2021) to monitor the local 99 pore pressure distribution in micro-cracked rocks under small (2.5 MPa) to large fluid pressure 100 gradients (60 MPa). First, we measured the specimen's permeability as a function of effective 101 pressure by applying a small pore pressure gradient (1 MPa). We then applied large pore 102 pressure gradients and measured the pore pressure distribution along the length of the two 103 samples. We discuss the observed variations of permeability and pore pressure distribution as a 104 function of effective stress by comparing them to a new micromechanics-based model and 105 an exponential model. Solving the diffusion equation for these two models, we compare our 106 experimental measurements to theoretical predictions and compare our micromechanics-107 based model to an extensive set of experimental data found in the literature.

109 2. Experimental Methods

110 Here, compressive stress and compressive strain are positive, and confining pressure and 111 pore pressure are denoted by Pc and p, respectively. The simple effective pressure is Pc-p and is denoted by P_{eff} (Terzaghi, 1925). The samples are crystalline rocks widely used in previous 112 research (Brace et al., 1968; Fortin et al., 2011; Heap et al., 2018; Wang et al. 2013): Westerly 113 granite and Etna basalt. Two cylindrical samples of 40 mm in diameter and 90 mm in length 114 115 were prepared. The granite sample was heat-treated in three steps: i) the sample was heated up to 650 °C at a rate of 5 °C/min, ii) it was kept at the target temperature for 2 h, iii) then, the 116 117 sample was left to cool down to ambient temperature. The initial porosity is 4.9% for the basalt 118 and 3.7% for the heat-treated granite. Porosity was measured using the triple weight technique.

119 Experiments were performed using a hydraulic triaxial cell installed at the Laboratoire de 120 Géologie of École Normale Supérieure in Paris (Borgomano et al., 2020). Two pumps (Quizix 6000-Series) were connected to the top and bottom of the sample to control the pore pressure. 121 122 Confining and pore pressure were measured with an accuracy of approximately 10⁻² MPa. Samples were jacketed with neoprene sleeves to isolate them from confining oil, and water was 123 used as pore fluid. Internal pore pressure sensors were used to measure the pore pressure at 124 125 different locations along the sample (Brantut & Aben, 2021). The accuracy of these internal 126 pore pressure sensors is +/- 1 MPa. Details and calibration of these sensors are given in Text S1 of supporting information. In the case of the Westerly granite sample, 6 pore pressure sensors 127 were installed along a double-line arrangement (Figure S1), and the measured pore pressure 128 129 value is the average of that performed by 2 sensors at the same height. In the case of the basalt sample, 7 pore pressure sensors were used in a spiral arrangement (Figure 1a). Note that during 130 this experiment, we will set the pore pressure measured by the first top sensor as the boundary 131 132 pressure (see Figures 3a and 3b).

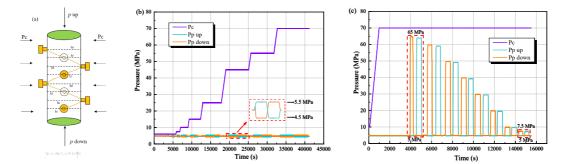


Figure 1. Experimental procedure. (a) Schematic diagram of a sample equipped with 8 internal pore pressure (p) sensors in a spiral arrangement (Etna basalt specimen). (b) Pressure loading path for permeability measurements with increasing confining pressures Pc, from 6 to 70 MPa, p being kept at 5 MPa. Permeability was measured using the constant flow method, with a pore pressure gradient kept at 1 MPa. (c) Pressure loading path for p distribution

measurements, for decreasing p gradients. p was measured locally using the internal p sensors, under constant confining pressure (70 MPa), and for p gradients ranging from 2.5 to 60 MPa.

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135 As a first step, dry samples underwent two confining pressure cycles up to 70 MPa, to 136 guarantee that the samples behaved purely elastically in the following steps. We then injected 137 water into the samples until the pore pressure reached 5 MPa while maintaining a confining 138 pressure of 10 MPa. Two experimental procedures were followed: i) classical permeability measurement under pressure (Figure 1b) and ii) pore pressure gradient experiment (Figure 1c). 139 140 During the first procedure, permeability was measured using the steady-state method (e.g. Fortin 141 et al. 2011; Ougier-Simonin et al., 2011) following the loading path in Figure 1b. At a given 142 confining pressure, a 1 MPa pore pressure gradient was fixed (p = 5.5 MPa on one end and 4.5 143 MPa on the other end of the rock specimen), the fluid flow through the sample was measured, and permeability was inferred using Darcy's law. Permeability was measured twice at each 144 145 effective pressure step by switching the flow direction, and a mean value was calculated.

In the second procedure, the pore pressure distribution was measured along the length of the 146 sample under pore pressure gradients. First, the confining pressure was fixed to 70 MPa and the 147 148 pore pressure to 5 MPa, as shown in Figure 1c. Then, the pore pressure on one end was increased 149 to generate a pore pressure gradient along the sample's length. Pore pressure was measured 150 locally, in the steady-state regime, by the internal pore pressure sensors. In total, 8 pore pressure gradients were investigated, starting from a large pore pressure gradient of 60 MPa (65 MPa on 151 one side and 5 MPa on the other) to a small pore pressure gradient of 2.5 MPa (7.5 MPa on one 152 153 side and 5 MPa on the other).

154

155 **3. Experimental results**

156 **3.1 Pressure dependence of permeability**

157 The permeability evolution of heat-treated Westerly granite and Etna basalt is shown in 158 Figure 2a as a function of effective pressure. As reported by previous studies, the permeability of both rocks decreases with increasing effective pressure. Permeability of Etna Basalt decreases 159 almost 20-fold, from about 3×10^{-17} m² at an effective pressure of 1 MPa to about 2×10^{-18} m² at 160 65 MPa. The permeability of Westerly granite exhibits an even greater pressure dependence. 161 from about $6x10^{-18}$ m² to $2x10^{-19}$ m² within the same differential pressure range. Most of the 162 163 decrease in permeability (80% for Etna Basalt and 90% for Westerly granite) occurs before 20 164 MPa effective pressure.

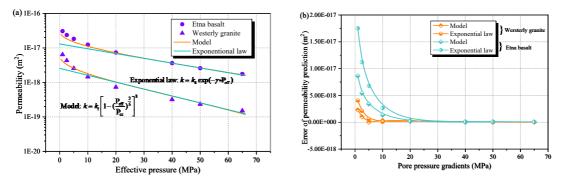


Figure 2. Permeability evolution and error analyses in heat-treated Westerly granite and Etna basalt. (a) Permeability evolution: the experimental data for permeability of heat-treated Westerly granite and Etna basalt are expressed by triangles and circles, respectively. Orange and blue solid lines are best fits using the new micromechanics-based model model and exponential law respectively. (b) Error analyses: Orange and blue solid lines are differential permeability between experimental data and theoretical predictions for heat-treated Westerly granite and Etna basalt. The points of hexagonal and quadrilateral correspond to the prediction error expressed using the exponential law and the new micromechanics-based model and exponential law models converge at high effective pressure, but that the new micromechanics-based model and exponential law models converge at low effective pressure.

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167 **3.2 Pore pressure distribution under large pore-pressure gradient**

168 Using the local pore pressure sensors, the distribution of pore pressure could be monitored 169 both in Westerly granite and Etna basalt, under low to high pore pressure gradients for gradients 170 across the specimen ranging from 2.5 to 60 MPa (Figure 3). As expected from Darcy's law for 171 a constant (pressure independent) permeability, pore pressure varies linearly as a function of 172 sample length for low to moderate pore-pressure gradients (2.5, 5, and 15 MPa). However, as the pore pressure gradient is increased (from 25 MPa and above and up to 60 MPa), the 173 distribution of pore pressure becomes non-linear within the rock specimen. The same 174 175 phenomenon was observed for both rocks (see Figure 3a and 3b) and is therefore not affected by the magnitude of permeability, but rather by its pressure dependence, i.e. the permeability 176 177 not being constant along the sample's length. Interestingly, one should note that this corresponds to a situation of pore-pressure excess when compared to what would be a linear distribution of 178 179 pore pressure, i.e. pore pressure is higher than what it would be for linear-gradient (and a 180 constant permeability).

Excess in pore pressure increases with increasing gradients, and at the highest gradients, the pore pressure remains close to that of the high-end pore pressure for close to 50% of the sample's length. This effect is more pronounced in Westerly granite than in Etna basalt, which results from the difference in the pressure dependence of permeability of both rocks. To be clearer, the 185 more pronounced the pressure sensitivity, the more pronounced the pore pressure excess and 186 the more abrupt (spatially) the pore pressure shutdown at the low (pore pressure) end of the 187 specimen.

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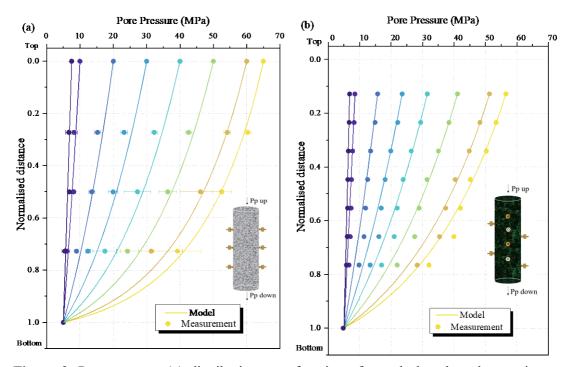


Figure 3. Pore pressure (p) distribution as a function of sample length under varying p gradients of (a) heat-treated Westerly granite and (b) Etna basalt. Low p gradients correspond to cold (blue) colors; large gradients to warm (yellow) colors; circles correspond to local p measurements performed by the internal p sensors; solid lines to theoretical predictions using the new micromechanics-based model (equations 1 and 3) for p distribution.

189

190 4. Discussion

191 4.1 Pore pressure distribution with pressure dependent permeability

192 In our experiments, the pore pressure *p* was only measured at the steady state. Hence the 193 pore pressure distribution should follow the diffusion equation under the steady state:

194
$$\frac{d}{dz} \left[-\frac{k}{\eta} \frac{dp}{dz} \right] = 0 \quad (1)$$

195 where k is permeability; η is the fluid viscosity. The pressure distribution, i.e. the relationship 196 between pore pressure p and the location along the z-axis in equation (1) will therefore depend 197 on the functional form of the pressure dependence of permeability k. Following our 198 measurements, two functional forms may be used to express the permeability effective pressure 199 dependence: an exponential form or a micromechanics-based model.

200 The exponential law is generally expressed as (David et al., 1994):

$$k = k_0 e^{-\gamma (P_{\text{eff}})}$$
(2)

where k_0 is the initial permeability at zero pressure; γ is a coefficient called stress sensitivity factor (1/Pa), inherent to the rock sample. The micromechanics-based model used in this study is:

205
$$k = k_0 \left[1 - \left(\frac{P_{eff}}{P_{cc}}\right)^{\frac{2}{5}} \right]^3$$
 (3)

with $P_{eff} \leq P_{cc}$ and where k_0 is the initial permeability at zero pressure and P_{cc} is the crack closing 206 207 pressure, an inherent parameter of the rock sample and characteristic pressure above which all 208 the cracks in the specimen can be considered as closed. P_{cc} is therefore related to the 209 consolidation stress (maximum previously experienced pressure) of rock. Details on the 210 derivation are presented in Text S2 of the supporting information. One should note here that: i) 211 although empirical, this new model is physics-based, as the exponent 2/5 arises from rough 212 crack asperity model (Brown & Scholz, 1985; Gavrilenko & Gueguen, 1989; Johnson, 1982; Walsh, 213 1981), while the exponent 3 arises from the well-established cubic-law for permeability 214 (Zimmerman & Bodvarsson, 1996); ii) it replaces the complex microstructure of a cracked rock 215 by that of an idealized single rough crack, with a roughness distribution equiprobable at all 216 heights below that of the initial aperture. Such an asperity distribution was proven to best fit experimental permeability data (Gavrilenko & Gueguen, 1989). In essence, the law describes the 217 218 permeability evolution (cubic law) of a rough crack under external pressure/normal stress.

219 As shown in Figure 2a, the evolution of permeability k with effective stress P_{eff} for both 220 samples, is well described by the exponential law and the micromechanics-based model. Fitting parameters (k_0, γ , and P_{cc}) are given in Table S1 of supporting information. k_0 values 221 obtained for the exponential law are lower than those obtained for the micromechanics-based 222 223 model which can readily be explained by the fact the micromechanics-based model provides a 224 better fitting at low effective pressure, in a range of pressure where the exponential law underestimates the permeability. Not surprisingly, the inverse pressure sensitivity parameter 225 226 $1/\gamma$ of the exponential law is approximately one order of magnitude lower than the crack closure pressure P_{cc} of our micromechanics-based model. Nevertheless, both formulations 227 converge at high effective pressure. Figure 2b quantifies the fitting of the error of both laws. 228 229 As seen in Figure 2b, our micromechanics-based model captures the evolution of permeability 230 under low effective pressure conditions better. Importantly the micromechanics-based model 231 does not have the low-pressure limitations of the exponential law. However, distinguishing the 232 fitting effects becomes challenging when the effective pressure exceeds 20 MPa.

233 Substituting the exponential law (equation 2) into the diffusion equation (equation 1), we 234 get the following solution (modified from Rice 1992 or David et al. 1994):

235
$$p(z) = \frac{\ln}{\alpha} \left[\left(e^{\gamma P_{\text{down}}} - e^{\gamma P_{\text{up}}} \right) \frac{z}{L} + e^{\gamma P_{\text{up}}} \right]$$
(4)

where P_{down} and P_{up} are the pore pressure boundary conditions set at the top and bottom of the specimen. From equation (4), the pore pressure p can be predicted at any position z by determining the stress sensitivity factor γ with given boundary conditions. As presented in Table S1 of the supporting information, the stress sensitivity factors γ for Westerly granite and Etna Basalt are 0.046 and 0.032 respectively, and the solutions for pore pressure distribution in our specimen are shown as solid lines in Figures S2a and S2b. These theoretically predicted trends are indeed consistent with those of the experimental data points (Figure S2).

243 Similarly, another solution can be obtained by substituting the micromechanics-based model244 (equation 3) into the diffusion equation (equation 1):

245
$$p^*\left(1 - \frac{15}{7}p^{*\frac{2}{5}} + \frac{5}{3}p^{*\frac{4}{5}} - \frac{5}{11}p^{*\frac{6}{5}}\right) = Cz - D \quad (5)$$

Here $p^* = \frac{Peff}{P_{res}}$, and C and D are constants which detailed expressions are given in Text S3 246 of supporting information. The functional form of equation (5) is interesting, as a linear pore 247 pressure gradient is readily retrieved at small p^* (i.e. disregarding the 1st, 2nd, and 3rd order 248 terms in $p^{*^{2/5}}$). Equation (5) can thus be interpreted as a Taylor series expansion in $p^{*^{2/5}}$ with 249 250 respect to the reference linear case. The analytical solution of $p^{*}(z)$ is non-trivial because of the 251 polynomial nature of equation (5). But a solution can be retrieved by looking for the pore 252 pressure value p (ranging between P_{down} and P_{up}) that minimizes the difference between the left hand-side and right hand-side of equation (5) at a given position z. These best-fit solutions are 253 254 shown as solid lines in Figures 3a and 3b, which shows that equation (5) indeed predicts the 255 trend observed in experimental data. In particular, our micromechanics-based model predicts a 256 transition from linear to non-linear pore pressure gradients when increasing pore pressure 257 difference is imposed at the two ends of the rock specimen.

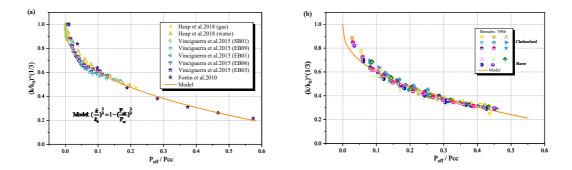
We also compared the error in the prediction of the measured pore pressure profile with 258 theoretical solutions using the exponential law and the micromechanics-based model (Figure 259 260 S3). The error in predicting the pore pressure profiles using the exponential law and the micromechanics-based model is almost the same, especially for low pore pressure gradients, 261 262 which also correspond to relatively high effective pressure, where the permeability predictions 263 are equivalent. Again, the predictive performance of the micromechanics-based model slightly surpasses that of the exponential law as the pore pressure gradients increase. This is particularly 264 265 true when the pore pressure gradient reaches 60 MPa, for which errors in predictions obtained with the micromechanics-based model for Westerly granite and Etna Basalt are 2.7% and 5.4%, 266 respectively, in contrast to 3.3% and 6.0% for the predictions based on the exponential law. 267

This highlights once again the capacity of the micromechanics-based model to better capture permeability and pore evolutions at low effective pressure.

Finally, note that only the Terzaghi effective pressure was used, i.e. Peff = Pc - p, while previous studies have demonstrated that the effective pressure coefficient (Biot coefficient for pressure) was close to, but generally lower than 1 in crystalline rocks (Bernabe. 1986, 1987, 1988). It is foreseeable that our predictions might have been better if an effective pressure coefficient slightly lower than one had been measured and considered. In any case, the large errors observed in Figure S3 are probably due to limitations of our sensor sensitivity, which remains the limiting factor.

4.2 Pressure dependence of permeability for crystalline rocks

The evolution of permeability of porous and cracked rocks with effective pressure has been 278 279 extensively studied (e.g. Bernabe, 1986; Brace et al., 1968; David et al., 1994; Dong et al., 2010; Heller et al., 2014; Davies & Davies, 2001; Gray & Fatt, 1963). In general, either the exponential 280 law $k = k_0 e^{-\gamma (P_{eff})}$ or a power-law of the form $k = k_0 (P_{eff})^{-m}$ have been employed to 281 describe the pressure dependence of permeability. However, neither the exponential law nor 282 283 the power-law, have a clear micromechanical background to support their formalism, and 284 should be considered empirical mathematical approximations. In addition, such power-law 285 formalism for the permeability pressure dependence presents three important caveats: i) a dimensional problem, which one can circumvent by normalization; ii) the arbitrary nature of 286 287 the exponent m, which needs to be fitted on a case-by-case basis; iii) the asymptotic convergence to zero when the effective pressure gets close to zero (Su et al., 2022; Zheng et al., 288 2015). We showed above that the exponential law is indeed efficient in predicting both the 289 290 permeability and pore pressure evolution at high effective pressure. However, problems arise 291 at low effective pressures.



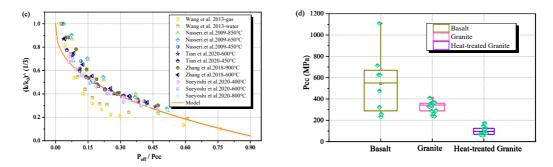


Figure 4. Validation of the new micromechanics-based model. Comparison of published experimental data and the new micromechanics-based model for (a) basalts, (b) natural granites and (c) heated treated granites. The data have been normalized according to the format of the new micromechanics-based model. The orange line is the normalized model $\left(\left(\frac{k}{k_o}\right)^{\frac{1}{3}}=1-\left(\frac{Peff}{Pcc}\right)^{\frac{2}{5}}\right)$. (d) The ranges of closure pressure *Pcc* for basalt (green), granite (pink), and heat-treated granite (blue), with medium *Pcc* being 551, 343, and 96 MPa, respectively.

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294 Figure 4 displays a large compilation of experimental data on the permeability evolution 295 with effective pressure in crystalline rocks. Three cases were considered: granites, basalts, and heat-treated granites, respectively displayed in Figures 4a, 4b, and 4c. For each data set, a best 296 297 fit was performed using our micromechanics-based model. One can see that when plotting $(k/ko)^{1/3}$ as a function of the normalized effective pressure (*Peff/Pcc*), the pressure dependence 298 299 of permeability of all rock types converges with the micromechanics-based model prediction. 300 This is particularly true for basalts and natural granites (Figures 4a and 4b). Note here that the 301 Chelmsford and Barre granites data were cored from three different directions and showed 302 relative homogenous permeability (Bernabe, 1986). However, the predictive performance of our 303 model on heat-treated granites was not as strong as that observed in natural basalts and granites, 304 and the data exhibited increased dispersion along the trendline in this case (see Figure 4c). We 305 suspect that differences in the heat-treatment procedures impact the homogeneity of these data 306 sets, which, in turn, affects the model's predictions for experimental data. Finally, an additional output of these fits is the crack closure pressures Pcc obtained for each of these data sets. One 307 can see that Pcc obtained for natural granites is close to a median value of 340 +/- 3 MPa. This 308 309 is a satisfying result, as larger dispersion was observed by David et al. (1994) for the pressure sensitivity parameter $1/\gamma$ of granite using the exponential law, probably because, when using 310 311 the exponential law, the best-fit parameter will largely depend on the pressure range of fitting, as we have seen how the exponential fails at predicting the low effective pressure permeability 312 313 evolution. The Pcc obtained for basalts is much more dispersed (550 \pm -1 MPa), which 314 probably arises from the inherent variety of basalt permeability, depending on their cooling

conditions when they were emplaced. Basalt, in the rock mechanics community, also refers to the large variety of rocks, sometimes a bit more acidic than basalt per se for the petrology/volcanology community (Heap et al., 2018). The P_{cc} for heat-treated granites is smaller, centered around 95 +/- 1 MPa, but quite dispersed, again probably due to the variety in heat-treatment processes in these studies.

320 Finally, it is important to stress that an important limitation of our micromechanics-based model is that the predicted permeability k becomes negative when effective stress P_{eff} exceeds 321 322 that of the closing pressure P_{cc} . A similar phenomenon is also observed in Walsh's model 323 (equation A-4). However, this cannot occur, as when the applied effective pressure increases, 324 an increasing number of cracks will close, which will require an even higher pressure to fully 325 seal the remaining cracks. P_{cc} is therefore related to the maximum pressure previously 326 experienced by a rock, or the maximum consolidation stress, in such a way that previous 327 experimental loadings or burial depth will contribute to the P_{cc} . In other words, P_{cc} should increase with increasing applied P_{eff} . For the P_{cc} determined above for natural granites and 328 329 basalts, the situation $(P_{eff}/P_{cc} > 1)$ cannot occur within the first 10-20km of the brittle crust, and 330 perhaps even below, as elevated (up to lithostatic) pore pressures are thought to be prevalent at 331 greater depths (David et al., 1994; Miller et al., 2004). At such depth, the Terzaghi effective 332 pressure approximation probably also reaches its limit of applicability, as the Biot coefficient for effective pressure is expected to fall close to zero somewhere within the ductile/plastic 333 334 regime (Hirth & Beeler, 2015).

5. Conclusion

336 Non-linear pore pressure distribution arises due to non-linear changes in permeability k in response to a significant pore-pressure gradient. Our experiments involving different pore 337 338 pressure gradient measurements indeed show that the pore pressure distribution in 339 crystalline/cracked rocks transitions from linear under low pore-pressure gradients to non-linear 340 under high pore-pressure gradients, which results from the pressure dependence of permeability. 341 The pore pressure distribution at elevated pressure gradients can be predicted by solving the 342 diffusion equation, which is achieved by describing the pressure dependence of permeability using either an empirical exponential law or a new micromechanics-based model. This new 343 model, derived from a micromechanical analysis, is based on a combination of i) the aperture 344 345 evolution of a rough crack under applied stress; ii) the cubic law, a well-established law to describe laminar flow within single fractures (Zimmerman & Bodvarsson, 1996). One should 346 347 stress here that this new formalism results from an important simplification of previous analysis 348 performed by Gavrilenko and Gueguen (1989) and has the potential to predict the generation

and maintenance of pore pressure in crystalline rocks, over the entire range of effectivepressures expected within the brittle crust.

351

352 Acknowledgments

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359 Data Availability Statement

360 The experimental data from the present study are available in Figshare, 361 (<u>https://doi.org/10.6084/m9.figshare.25315504</u>).

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