On the Performance of a Real-Time Electron Radiation Belt Specification Model

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Abstract

Maintaining accurate real-time hindcast and forecast specification of the radiation environment is essential for operators to monitor and mitigate the effects of hazardous radiation on satellite components. The Radiation Belt Forecasting Model and Framework (RBFMF) provides real-time forecasts and hindcasts of the electron radiation belt environment, which are used as inputs for the Satellite Charging Assessment Tool (SatCAT). We evaluated the long-term statistical error and bias of the RBFMF by comparing the 10-hour hindcast of electron phase space densities (PSD) to a multi-mission dataset of PSD observations. We found that, between the years 2016-2018, the RBFMF reproduced the radiation belt environment to within a factor of 1.5. While the error and bias of assimilated observations were found to influence the error and bias of the hindcast, data assimilation resulted in more accurate specification of the radiation belt state than real-time Van Allen Probe observations alone. Furthermore, when real time Van Allen Probe observations were no longer available, the hindcast errors increased by an order of magnitude. This highlights two needs; (i) the development of physics-based modelling incorporated into this framework, and (ii) the need for real-time observations which span the entire outer radiation belt.

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3	
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8	
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10	Key Points
11	• Real-time data-assimilative hindcasts of the outer electron radiation belt were accurate
12	to within a factor of 1.5.Data assimilation substantially improved the error and bias of
13	radiation belt specification but strongly influenced hindcast error and bias.
14	Improved physics-based modeling and continuous real-time observations through the
15	outer radiation belt are needed for accurate hindcasts.

16 Abstract

17 Maintaining accurate real-time hindcast and forecast specification of the radiation environment 18 is essential for operators to monitor and mitigate the effects of hazardous radiation on satellite 19 components. The Radiation Belt Forecasting Model and Framework (RBFMF) provides real-time 20 forecasts and hindcasts of the electron radiation belt environment, which are used as inputs for 21 the Satellite Charging Assessment Tool (SatCAT). We evaluated the long-term statistical error 22 and bias of the RBFMF by comparing the 10-hour hindcast of electron phase space densities 23 (PSD) to a multi-mission dataset of PSD observations. We found that, between the years 2016-24 2018, the RBFMF reproduced the radiation belt environment to within a factor of 1.5. While the error and bias of assimilated observations were found to influence the error and bias of the 25 26 hindcast, data assimilation resulted in more accurate specification of the radiation belt state than real-time Van Allen Probe observations alone. Furthermore, when real time Van Allen Probe 27 28 observations were no longer available, the hindcast errors increased by an order of magnitude. 29 This highlights two needs; (i) the development of physics-based modelling incorporated into this 30 framework, and (ii) the need for real-time observations which span the entire outer radiation 31 belt.

32 Plain Language Summary

33 It is important to accurately predict and monitor the radiation levels in space to safeguard

- 34 satellites from potential damage. This paper introduces a model called the Radiation Belt
- 35 Forecasting Model and Framework (RBFMF), which provides real-time forecasts and historical
- 36 data (hindcasts) of radiation levels. To test the model's accuracy, we compared its predictions to
- 37 actual observations from satellites between 2016 and 2018. We found that generally, the
- 38 model's predictions of the outer radiation belt were within 1.5 times of the actual
- 39 measurements. Additionally, we discovered that incorporating both real-time satellite
- 40 observations and physics-based simulation improved prediction accuracy compared to relying
- 41 solely on either method. However, we noticed a significant increase in prediction errors when
- 42 real-time observations through the heart of the Van Allen radiation belt were unavailable. This
- 43 underscores the importance of enhancing the model with physics-based modeling and ensuring
- 44 continuous real-time observations of radiation levels in space.

45 1 Introduction

46 The variability of the near-Earth radiation environment poses a serious hazard to 47 telecommunications, navigational, and defense satellites which orbit through these regions. A 48 key effect of spacecraft exposure to radiation is internal charging, where high energy electrons 49 penetrate the surface shielding of a satellite and deposit charge into dielectric materials such as 50 circuit boards or cable insulators, and on ungrounded material such as spot shields or connector 51 contacts (e.g., Fennell et al., 2001; Lohmeyer et al., 2015). The accumulated charging eventually 52 results in electrostatic discharges, which is one of the known causes of "satellite anomalies". 53 Anomalies range in effect from more frequent temporary errors in non-critical systems to rare 54 but catastrophic hardware damage and complete mission failure (Galvan et al., 2014) and can be 55 instigated by a number of issues, such as command errors, manufacture flaws, and 56 environmental exposures. Of all space environment effects on satellites, electrostatic discharges 57 from internal charging have been reported to cause the most anomalies (Green et al., 2017; Koons et al., 1999). 58

59 Improved on-orbit anomaly detection tools have been cited by satellite operators as an 60 industrial need for operators to easily and quickly attribute anomalies to space weather effects 61 (Green et al., 2017). To attribute satellite anomalies to internal charging of equipment requires 62 forensic reconstruction of the radiation environment and modelling of charge accumulation on 63 component hardware, such as satellite shielding materials, for defined orbits (LEO, MEO, GEO). 64 The Satellite Charging Assessment Tool (SatCAT) is one such tool which allows users to monitor 65 the real time and long-term effects of internal charging due to fluence of radiation belt 66 electrons. This paper will evaluate the Radiation Belt Forecasting Model and Framework (RBFMF) 67 which SatCAT uses to specify the radiation environment both retrospectively and in real-time. Several models have been developed to model the near-Earth radiation environment based 68

69 upon the Van Allen radiation belt response to solar wind parameters and/or geomagnetic

indices. These models usually fall within three categories; empirically based analytical

- descriptions (e.g., X. Li, 2004; Nagai, 1988; Roeder et al., 2005; Turner & Li, 2011), physics-based
- 72 models (e.g., Horne et al., 2013; Subbotin & Shprits, 2009), and machine learning models (e.g.,

73 Boyd et al., 2023; Chen et al., 2019; Wei et al., 2018). Statistical approaches to modelling the 74 radiation belt have shown success at identifying the key variables which influence radiation belt 75 flux on different timescales. However, statistical approaches do not capture some extreme 76 events, and could be flawed if they cannot reflect the non-linear relationship between input 77 variables are output electron fluxes. While physics-based modelling allows the study of relative 78 contributions of complex acceleration and loss mechanisms in the outer radiation belt, the 79 computational power required to accurately model the interconnected magnetospheric system 80 on an hourly basis provides a significant challenge. Machine learning models have predicted 81 ultra-relativistic electron fluxes with high efficacy but show less accuracy at predicting lower 82 energy fluxes (Camporeale, 2019; Shin et al., 2016) but, similarly to statistical modelling, could have limited capabilities for extreme event which are out of sample to training data. 83

84 By combining physics-based modelling with data assimilative techniques, RBFMF provides a 85 lightweight and robust tool for real time radiation belt forecasting. This framework uses 1D 86 Kalman filtering technique which has previously been shown through event-based studies to be 87 a successful tool for reproducing the radiation belts (e.g., Coleman et al., 2018; Daae et al., 2011; 88 Kellerman et al., 2014). This work will investigate the performance of this forecasting 89 methodology by completing a detailed statistical evaluation of RBFMF over archived multi-year dataset of hindcasts. We aim to assess how data assimilation affects the error and bias of 90 91 radiation belt forecasts, and the influence of variable geomagnetic conditions. In this way, we 92 will identify how the RBFMF may be adapted in the future for improved hindcast reliability.

93 2 Radiation Belt Forecasting Model and Framework

94 The radiation belt forecast framework (RBFMF) is designed to combine physics-based modelling 95 with data assimilative techniques to provide forecasts, nowcasts, and hindcasts of the radiation 96 environment in real-time. This framework is based upon an existing data assimilative models 97 developed by Kellerman et al. (2014) and Shprits et al. (2013), and has been further developed to 98 provide a more robust forecasting infrastructure which provides data products which are 99 integrated into the SatCAT tool. The implementation of this framework is summarized in Figure 100 1.

Radiation Belt Forecasting Model and Framework

Each hour these steps are iterated to provide an updated hindcast, nowcast, and forecast.



101

102 Figure 1 Flow chart summarizing the steps completed each hour in the RBFMF.

103 Diffusive Modelling

104 Radiation belt diffusion is modelled through implementation of the 3-D Fokker-Plank diffusion

105 equation for radiation, Equation 1, (Roederer, 1970; Schulz & Lanzerotti, 1974; Walt, 1994).

106

$$\frac{\partial f}{\partial t} = \sum_{i,j} \frac{\partial}{\partial J_i} \left(D_{J_i J_j} \frac{\partial f}{\partial J_j} \right) - Losses$$
Equation 1

107 Where *f* is the phase averaged electron phase space density (PSD), J_i , J_j , represent the first, 108 second, and third adiabatic invariants of adiabatic motion (μ , J, ϕ respectively), and diffusion

- 109 coefficients $D_{J_iJ_j} = \langle \Delta J_i \Delta J_j \rangle / (2\Delta t)$ which denote the scattering rates $(D_{\mu\mu}, D_{JJ}, D_{\Phi\Phi})$. In this paper
- 110 we will use $K (\propto J \text{ assuming } \mu \text{ is conserved})$ as the second adiabatic invariant and $L^* (\propto 1/\Phi)$ as
- 111 the third adiabatic invariant (noting that $L^* = L$ in a dipolar magnetic field). The Versatile Electron
- 112 Radiation Belt (VERB) code (Subbotin & Shprits, 2009) is used to implement a solution to this
- 113 equation using precomputed diffusion coefficients.

114 Diffusion Coefficients

- By precomputing diffusion matrices, the diffusion equation can be solved quickly at each time
- step by selecting diffusion coefficients for the prevailing *Kp* level. Mixed local diffusion terms are
- 117 excluded, which enables larger grid steps. Three types of waves were used to derive the
- 118 diffusion coefficient matrices; ULF waves (Brautigam & Albert, 2000), lower-band chorus (W. Li et
- al., 2007; Shprits et al., 2007) and plasmaspheric hiss (Spasojevic et al., 2015). The plasma density
- 120 was obtained from (Sheeley et al., 2001) for diffusion coefficient computation. The diffusion
- 121 coefficients were computed using the Full Diffusion Code at UCLA.

122 Initial and Boundary Conditions

123 Diffusion is solved for a dipolar magnetic field with a grid covering L-shells 1 to 7, energies 10 keV to 10 MeV, and pitch angles 0.3 ° - 89.7°. The upper boundary condition in energy is a 124 Dirichlet boundary with constant f = 0, the lower-boundary condition is also Dirichlet for each 125 126 time step, although updated by assimilation. The lower boundary condition in pitch angle is a 127 Neumann boundary $\partial f / \partial \alpha = 0$, to allow for both weak and strong diffusion effects to be 128 simulated. The upper boundary condition in L utilizes both Dirichlet and Neumann boundaries, 129 depending on the last closed drift shell (LCDS) derived from Tsyganenko (1989) with a centered 130 dipole (see Kellerman, 2018). The lower boundary in L is a Dirichlet boundary, with f = 0 at L_{min} , 131 representing loss to the atmosphere.

The model was initialized through the average PSD observed by spacecraft from the previous month. For each additional forecast going forward through several years, the initial condition of each time step is set to the nowcast simulated for the previous hour.

135 Data Assimilation

136 Data assimilation uses filtering algorithms to estimate the state of a system using joint 137 probability distributions from a simulated system and sparsely observed data. The Kalman Filter 138 (Kalman, 1960) is a widely used data assimilation algorithm which estimates the system state by 139 minimizing the mean square errors of the simulated state variables and observed state variables. 140 Readers are referred to past works for detailed descriptions the Kalman filter to radiation belt 141 analysis (e.g., Kondrashov et al., 2007; Naehr & Toffoletto, 2005; Ni et al., 2009; Shprits et al., 142 2007). Because the computational requirements of a 3D Kalman filter are very large, making it 143 impractical for real time applications, the RBFMF instead employs a one-dimensional splitoperator Kalman filter. This methodology has been validated in a synthetic-forecast analysis over 144 145 multiple years (Kellerman, 2018). Due to several unknown errors in the model and real-time 146 observational datasets, the errors were set equal for data and model.

147 2.1 Observations

148 Figure 2 shows how the modelled radiation belt PSD compares to the multi-mission PSD 149 observations (described further in Section 3). The nowcast time is indicated in Figure 2 by the 150 white line, with the preceding eight days showing hindcast PSD, and the following two days 151 show the PSD forecast. By comparing the modelled PSD in Figure 2a to the measured PSD in Figure 2b, we can see that the RBFMF is highly successful at reproducing the structure and 152 153 dynamical evolution of the radiation belt in this example. The magnitude of the radiation belt flux is well captured overall, although when the observed PSD became enhanced up to $\sim 15 \text{ x}$ 154 10^{-5} (c/cm/MeV)³ at 5 < L* < 6 between 6-9th August, the hindcast PSD appeared to be slightly 155 156 underestimated. Figure 2c shows that the percentage error was < 100% for most of the interval 157 (i.e., PSD was estimated within a factor of 1 during the interval), but became largest (> 200%) near the outer boundary ($L^* > 6$) as electrons were lost on 3rd August, and along the inner edge 158 of the radiation belt (4 < L^* < 5) during the enhancement between 4th to 7th August. 159 160 While the interval in Figure 2 appears to show that the RBFMF is a good representation of the

161 outer radiation belt, we must quantitively evaluate the performance of the model to determine if 162 it is accurate over long time periods, and identify when the simulation is inaccurate so that it can be improved. We will test the RBFMF against the observed state of the electron radiation belt for
two time periods between 2016 - 2018 and between 2019 - 2020. The key difference between
these years is than between 2016-2018 both GOES and Van Allen Probe data were assimilated
into the hindcast in real time, whereas from 2019 onwards, only GOES data was assimilated in
real time.



168



displayed in panel (a) as a function of L* over time, for μ = 700 MeV/G and K = 0.1 G^{0.5}R_E.

171 Panel (b) shows corresponding PSD observations, f_{obs}, taken by multiple missions. Panel

172 (c) shows the absolute percentage error of the simulated PSD: $|f_{obs} - f_{sim}/f_{sim}| \times 100$.

173 3 Validation Method

In this analysis, the RBFMF will be validated against a multi-mission dataset of radiation belt
observations (described in Section 3.1), which serves as the 'true' state of the radiation belt. The
error and bias of the radiation belt hindcast of electron phase space density (PSD) is analyzed in

adiabatic coordinates. To do this, the observed PSD (described in Sections 3.1) is converted onto the same resolution coordinate grid as the simulated PSD by interpolating across the first and second adiabatic invariants, μ and K, then averaging PSD into L^* bins on an hourly basis. The quotient ($Q_i = f_{sim}/f_{obs}$) of each simulation data point can then be determined if there is a corresponding PSD observation.

182 The statistical error and bias of the 10-hour hindcast is calculated between January 2016 -183 October 2019 and between March 2019 – December 2020. Special focus is given to the 10-hour 184 hindcast (dashed line, Figure 2a) because this is the most frequently used by satellite operators 185 for anomaly attribution. Error and bias are quantified using symmetric metrics described by 186 Morley et al. (2018), which account for variable electron PSD magnitudes. The median symmetric 187 accuracy (MSA) is described in Equation 2 and the symmetric signed percentage bias (SSPB) is 188 described in Equation 3, where M() symbolizes the median calculation. In this scheme, the MSA 189 is small if simulation errors are low, SSPB < 0 if the hindcast is biased towards underprediction 190 of PSD, and SSPB > 0 if the hindcast is biased towards overprediction of PSD.

$$MSA = 100 \left(\exp \left(M(|\log_e(Q_i)|) - 1 \right) \right)$$
 Equation 2

191

$$SSPB = 100 \operatorname{sgn}(M(\log_e(Q_i)))(\exp(M(|\log_e(Q_i)|) - 1))$$
 Equation 3

192 3.1 Multi-Mission PSD Observations

PSD observations are taken from 32 individual satellites which are part of 5 different scientific
missions and hosted payloads (see Staples et al., 2022; Staples et al., 2023 for usage of this
dataset):

Van Allen Probe Magnetic Electron Ion Spectrometer (MagEIS) and Relativistic Electron Proton Telescope (REPT) instruments (Baker et al., 2014; Blake et al., 2014).

- GOES 13 and15 (Geostationary Operational Environmental Satellite) Magnetospheric
 Electron Detector (MAGED) Energetic Proton, Electron, and Alpha Detector (EPEAD)
 (Rodriguez, 2014a, 2014b; Sillanpää et al., 2017).
- GPS (Global Positioning System) Navstar Combined X-ray dosimeter (CXD) (Morley et al.,
 2017; Tuszewski et al., 2004).
- THEMIS (Time History of Events and Macroscale Interactions during Substorms)
 Electrostatic Analyzer (ESA) and Solid-State Telescope (SST) (Angelopoulos, 2008;
 Angelopoulos et al., 2008; McFadden et al., 2008).
- MMS (Magnetospheric Multiscale) Fly's Eye Electron Proton Spectrometer (FEEPS) (Blake
 et al., 2016; Burch et al., 2016).

All spacecraft data is calibrated to Van Allen Probe B and bias-corrected GOES 15 data, which are chosen as the "gold standards" for the calibration. The GPS pitch angle distributions are

assumed using the Zhao et al. (2018) model. For each spacecraft instrument, the adiabatic

211 invariants μ , K, and L^* are computed using a model magnetospheric field, represented by the

212 International Geomagnetic Reference Field model (IGRF; Thébault et al., 2015) and Tsyganenko

213 (1989) external magnetic field model (T89). The final PSD dataset is interpolated across

214 dimensions of μ and K, but not across L^* or time.

215 4 Validation Results

216 4.1 Original Forecast Framework (2016-2018)

Figure 3 shows the MSA, SSPB, and number of samples, N, calculated for the 10-hour hindcast of radiation belt PSD as a function of the first and second adiabatic invariants, μ and K at three sampled *L**. The *L** values shown in Figure 3 are selected to represent trends in error and bias observed in the slot region (~ $L^* = 2.44$), the core of the outer radiation belt, and the outer

radiation belt near medium earth orbit (~ $L^* = 4.12$) and at geostationary orbit (~ $L^* = 6.04$).



222

Figure 3 Left column shows the statistical error (MSA) of the 10-hour hindcast between 224 2016-2018, shown by color as a function of μ and K for a sample of simulated $L^* = 2.44$, 225 4.12, and 6.04. The middle column shows statistical bias (SSPB) in the same format, and 226 right column shows the number of samples N used in the computation of MSA and SSPB.

We observe a large variance in the MSA and SSBP across the different L^* regions. At $L^* = 2.44$ the maximum percentage error was 350%, and the maximum bias was 250%. At $L^* = 2.44$, electrons are generally located inside the overlapping plasmasphere and slot region, so the large positive bias indicates that the model systematically overestimated the PSD in the slot region. It is because electron PSD is generally very low at $L^* < 4$, that comparatively small absolute differences in PSD create large errors and bias relative to the measured PSD. In the outer radiation belt region (L* > 4) the error and bias were much smaller than the slot region, reaching a maximum of 150% percentage error and -150% bias. This indicates that statistically the hindcast accurately predicted the outer radiation belt PSD to within a factor of 1.5. Moreover, the hindcast error and bias was highly dependent upon μ and *K*.

At $L^* = 4.12$ the greatest errors were found to reach 150% corresponding to the highest

238 measured μ values depending on *K* (i.e., highest energies, ~ multi-MeV) and was

correspondingly biased toward underestimation of PSD by ~120%. At lower μ values (which

correspond to the bulk of the radiation belt plasma population) the hindcast showed a statistical

overestimation of PSD by 70% or less, showing that the hindcast predicted the core outer belt

PSD to within a factor of 0.7. The hindcast error and bias showed similar trends at $L^* = 6.04$: The

highest errors were observed at the highest measured μ (highest energies) with a negative bias

244 > -100%, and at lower μ the hindcast overestimated PSD by up to 70%. In addition to these

error and bias relationships, at $L^* = 6.04$ there was a strong error of 150% and bias of -150%

observed at μ < 100 MeV/G. This population corresponds to lower energy < 300 keV electron

populations. To ensure that error and bias is not dependent upon hindcast hour, the same
analysis was completed for different hindcast hour, and no appreciable differences were

observed.

The following analysis discusses the source of the statistical hindcast error and bias and evaluates the accuracy of the hindcast under different geomagnetic conditions.

252 4.1.1 Assimilated Data Bias

253 One potential source of error in the model hindcast is assimilated data bias. Between 2016-2018 254 the assimilated datasets were real time GOES data, and the Van Allen Probe Beacon data. 255 Because the assimilated GOES data is similar to the final science data product, it is not 256 informative to evaluate the bias of this data. The Van Allen Probe beacon data was provided in 257 real time over the Van Allen Probe mission without the same corrections and post-processing as 258 the long-term science data archive, and so is possibly more prone to errors. To assess if the 259 error and bias of assimilated PSD observations influenced the hindcast PSD, we will evaluate the 260 error and bias of the Van Allen Probe Beacon data (Figure 4) and compare the hindcast error

12

- and bias (Figure 3). The error and bias of Van Allen Probe beacon data is quantified by
- calculating the MSA and SSBP respectively using Equation 2 and Equation 3, where the quotient
- is calculated as $Q = PSD_{Beacon}/PSD_{Final}$, and PSD_{Final} is the science data product from the
- same Van Allen Probe. This analysis effectively shows the differences between the real time data
- 265 product and the more highly processed science data as a function of μ , K, and L^* .



266

267 Figure 4 Left column shows the statistical error (MSA) and middle column shows the

- statistical bias (SSPB) of the Van Allen Probe B beacon data between 2016-2018,
- compared to the final Van Allen Probe science data. Right column shows the number of
- data samples N used in the computation of MSA and SSPB. Error, bias, and sample size are
- all shown by color as a function of μ and K at sampled bins of $L^* = 2.44$; 4.12; 6.04 which
- were chosen to match the hindcast model grid.
- Figure 4 shows that universally (i.e., all L^* , μ , and K), the error and bias for Van Allen Probe
- beacon data was greater than the hindcast error and bias (Figure 3). For example, at $L^* = 2.44$,

275 both the error and bias of beacon data reached > 800%, whereas the maximum hindcast error 276 and bias were ~ 350% and ~250% respectively. The magnitude difference in error and bias was 277 less significant at $L^* = 4.12$, which reached a maximum of 200% error and -200 % respectively. 278 Despite differences in magnitude, we highlight that the error and bias observed for Van Allen 279 Probe beacon data (Figure 4) was nearly identically distributed across μ , K, and L* compared to 280 the 10-hour hindcast error and bias. For example, at $L^* = 4.12$, the maximum errors were at the 281 highest μ values across all K, and were negatively biased, transitioning to a positive bias at low μ 282 values. This observation shows that the assimilated data significantly influenced the error and 283 bias of the hindcast. Though, because the magnitude of the hindcast error and bias was less 284 than the assimilated data, the simulated hindcast gave a significantly improved estimation of 285 radiation belt PSD than if Van Allen Probe beacon data was used alone.

286 4.1.2 Storm-time Error Analysis

287 Knowing how well the model captures the radiation belt evolution during different geomagnetic 288 conditions is of particular interest because most impacts to satellites are observed during 289 geomagnetically active periods. To analyze how the statistical error and bias varies with geomagnetic conditions, we extract geomagnetic storm intervals between 2016-2018 based 290 291 upon Sym-H index evolution. A storm is identified by time periods where Sym-H decreased 292 below -40 nT. The main storm phase is classified from intervals when Sym-H decreased from a 293 value above 15 nT, to a Sym-H minimum below -40 nT. The recovery storm phase is classified 294 from when the Sym-H increased after the main storm phase, until it reached a value above -15 295 nT. We further select times during geomagnetic storms when the AE index was in the upper 80% 296 percentile of data. High AE index periods are known to be associated with substorm injections of 297 lower energy source electrons from the magnetotail into the inner magnetosphere, and AE index 298 values exceeding 150 nT have previously been used as a proxy for substorm injections (e.g., 299 Meredith et al., 2000). As before, we calculate the statistical error and bias of each storm phase 300 using Equation 2 and Equation 3. Figure 5 and Figure 6 show how the computed error and bias varied under different geomagnetic conditions at $L^* = 4.12$ and $L^* = 6.04$, respectively. To easily 301 302 compare between geomagnetic conditions, the color bars have been saturated to \pm 200%. We

303 do not show the equivalent figure for $L^* = 2.44$ as no substantial differences between storm 304 phases were observed.

305 Firstly, we observe from Figure 5 that the statistical error and bias under geomagnetically quiet 306 conditions were effectively the same as for all data between 2016-2019 shown in Figure 3. This 307 indicates that the overall statistical error and bias for the hindcast at $L^* = 4.12$ was not 308 influenced by increased error or bias during geomagnetic variations. Figure 5 g-h show that high 309 μ values (highest energies \geq MeV) appear least accurate and most biased during the recovery 310 storm phase (and during substorm injections) as MSA increased to 200% at the highest μ values 311 (panel g), and SSPB decreases to -200% (panel h). This indicates that, during the recovery phase, 312 the hindcast underestimated the PSD of MeV electrons, which is understood to become 313 enhanced during this phase (e.g., Jaynes et al., 2015; K. R. Murphy et al., 2018; Sorathia et al., 314 2018). Conversely, PSD of low μ electrons (\leq 700 keV for) is less accurate during the main storm 315 phase (panel d), and during substorm related injections (panel j-k). In both cases the error is 316 observed to reach 200% and the hindcast was biased towards underestimation of PSD down to -317 200%. Figure 5 shows that the hindcast consistently underestimated PSD across all storm 318 conditions at $L^* = 4.12$, for all μ and K.

319 Similarly, Figure 6 shows that at $L^* = 6.04$, quiet times exhibited the same statistical error and 320 bias as the overall time period (Figure 3), and PSD of high μ (energies \geq MeV) were the least 321 accurate and most biased during the recovery phase of the storm (Figure 6 g-h). However, 322 Figure 6d shows that, irrespective of μ , the largest overall errors were observed at low K (i.e., 323 equatorial electrons) during the main storm phase. Given Figure 6e shows a bias towards 324 overestimation of PSD at these K, and that $L^* = 6.04$ is near geostationary orbit, it is possible 325 that loss to the outer boundary was not well captured by the hindcast. Figure 6j also shows large 326 hindcast errors for μ <500 MeV/G, and bias towards underestimation of PSD by up to -200%. 327 Since this feature was most prominent during storms with the highest AE index, we expect these 328 errors were caused by substorm injections of lower-energy (<500 keV) electrons.

15



329

330 Figure 5 Left column shows the statistical error (MSA) and middle column shows the statistical bias (SSPB) of the 10-hour hindcast between 2016-2018, compared to the final 331 332 multi-mission PSD observations. Right column shows the number of data samples N used 333 in the computation of MSA and SSPB. Error, bias, and sample size are all shown by color 334 as a function of μ and K at sampled bins of $L^* = 4.12$. Each row shows error and bias under different geomagnetic conditions a-c are guiet times, d-f are the main storm phase, g-I 335 336 are the recovery storm phase, and j-l show storm intervals which contain substorm 337 injections.



338

Figure 6 Statistical error and bias under different geomagnetic conditions, sampled at L* = 6.04 is shown in the same format as Figure 5.

341 4.2 Updated Forecast Framework (2019-2020)

Since the end of the Van Allen Probe mission in early 2019, the RBFMF has been operating by assimilating only GOES observations in real time. To assess how this affected the accuracy of the 10 hour hindcast, we repeat the analysis presented in the previous section, comparing the 10 hour hindcast at $L^* = 4.2$ to PSD observations obtained from the GPS constellation between March 2019 – December 2020 (Figure 7). Since the real-time GOES data assimilated into the

hindcast model is similar to the final science data product, it is not meaningful to complete anerror analysis at geostationary orbit using this data.

349 Figure 7 shows that the hindcast error and bias at $L^* = 4.12$ were significantly increased 350 compared to the Van Allen Probe era (Figure 3), reaching maxima of > 2000%, which is a factor 351 of 10 greater than was observed between 2016-2018. The hindcast was strongly biased towards 352 overestimation of PSD at all μ and K values by similar magnitudes to the error, which suggests 353 that the model could be improved by the inclusion of a corrective factor. It is important to note 354 that GPS satellites do not resolve electron flux by pitch angle, so an assumed pitch angle 355 distribution is used to calculate PSD as a function of μ , K, and L^* . It is possible that error and bias 356 determined at $L^* = 4.12$ were affected by the assumed pitch angle distribution used in GPS data 357 processing, rather than actual errors in the hindcast. Another dataset of PSD observations which 358 are pitch angle resolved is needed to test if this is the case (e.g., ARASE). 359 We emphasize that the diffusive simulation driving the hindcast provided a good first 360 approximation of radiation belt dynamics, but is somewhat rudimentary as simplified diffusive 361 modelling was employed. However, we chose not to modify the forecast model until a

362 comprehensive analysis of hindcast performance was conducted. Since less observational data is

363 now available to constrain the hindcast via data assimilation, the diffusion simulation should be

improved by updating the precomputed diffusion coefficients using more modern

methodologies of representing Chorus (e.g., Wong et al., 2024), Hiss (e.g., Agapitov et al., 2020;

Watt et al., 2019), and ULF waves (e.g., Kyle R. Murphy et al., 2023). The diffusive effects of EMIC

367 waves could also be incorporated (e.g., Ross et al., 2020) to improve the representation of

368 electron loss in the inner magnetosphere.



Figure 7 Statistical error (MSA, panel a) and bias (SSPB, panel b) are of the 10-hour

hindcast in 2019-2020 are shown as a function of μ and *K* at *L** = 4.12. The number of data samples, N, is shown in the panel c.

373 **5** Summary

374 We have conducted a comprehensive assessment of the accuracy and bias of the Radiation Belt Forecasting Model and Framework, which is used to specify the real-time radiation environment 375 376 in the Satellite Charging Assessment Tool. Historical hindcasts were compared to observations 377 of the radiation belt by computing the statistical errors and bias between the years January 2016 378 - October 2018 while the Van Allen Probes remained in operation, and between March 2019 -379 December 2020 following the end of the Van Allen Probe mission. 380 The hindcast was found to be accurate to within a factor of 1.5 in the outer radiation belt ($4 < L^*$ 381 < 7) during the years when the Van Allen Probe data was assimilated into the model (Figure 382 3d,q). We identified that the statistical hindcast bias was predominantly introduced by the assimilated Van Allen Probe data, which displayed the same dependence of bias upon μ and K 383 384 (Figure 4). Analysis of geomagnetic storms between 2016-2018 also revealed increased hindcast error and bias compared to quiet times at $L^* > 4$. The most energetic electrons (> MeV) were 385 386 more likely to be underestimated by the hindcast during storm recovery phase (Figure 5), error increased for equatorial electrons at $L^* \sim 6$ during the main storm phase (Figure 6d), and the 387 388 hindcast underestimated lower energy electrons (< 500 keV) related to substorm injections 389 (Figure 6j).

We have shown that the hindcast was much more accurate at predicting PSD than if the Van Allen Probe beacon data was used alone (Figure 4). Moreover, we found that the Van Allen Probe beacon data played a crucial role in constraining hindcast simulation between 2016-2019 as the hindcast error and bias increased tenfold when the Van Allen Probe data was no longer available (2018-2020). This highlights that combining coarsely processed data with physicsbased modelling through data assimilation can improve the accuracy of radiation environment specification than either method used alone.

397 6 Future Work

398 Our analysis has emphasized the importance of real-time observations at multiple locations 399 through the outer radiation belt. Even though the beacon Van Allen Probe data contained 400 significant error and bias compared to the final processed data, assimilation of these 401 observations into the RBFMF considerably improved the simulation compared to times where it 402 was not assimilated. Furthermore, we showed that data assimilative techniques displayed 403 reduced error and bias compared to the real time observations which were coarsely processed 404 compared to final processed science data. Since the end of the Van Allen Probe mission, there 405 are no similar observations available as the currently operational observatories (e.g., GPS, 406 ARASE) do not provide publicly available data in real time. We emphasize that any provision of 407 real time observations from existing or new missions enhance the operational impact of data, 408 even if it is sub-optimally processed compared to science quality data. Furthermore, analysis of 409 real-time data errors, analogous to our analysis of beacon Van Allen Probe data, can be used to 410 inform the observational uncertainties used during data assimilation simulations.

In lieu of real-time observations to constrain this stimulation through the heart of the radiation
belt, our analysis has highlighted key areas in which the physics simulation could be improved.
Overestimation of PSD in the plasmasphere could be addressed by evaluating more recent
diffusion coefficients computed for Plasmaspheric Hiss (e.g., Agapitov et al., 2020; Watt et al.,
2019). Improved representation of electron loss at geostationary orbit during the storm main
phase could be incorporated by using a dynamic outer boundary of the simulation (Bloch et al.,
2021; Staples et al., 2020) and evaluating new radial diffusion coefficients (Kyle R. Murphy et al.,

418 2023). Updating the radial diffusion coefficients could also improve hindcast with sparse real-419 time data by accurately propagating the effects of assimilated data across L*. Underestimation 420 of ultra-relativistic electrons during the storm recovery phase could be improved by updating 421 energy diffusion through new parameterizations of Chorus waves (e.g., Wong et al., 2024). 422 Furthermore, substorm injections of lower energy electrons are necessary, and could be 423 incorporated through updates to the simulation boundaries. Continued development of the 424 physics-based simulation is ongoing so that new versions of the RBFMF can be provided with 425 improved hindcast accuracy.

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Open Research

Spacecraft data from GOES and the Van Allen Probes are publicly available via the NASA/GSFC CDAWeb service (https://cdaweb.gsfc.nasa.gov/index.html/). Solar Wind data and geomagnetic indices are publicly available through the NASA/GSFC Space Physics Data Facility OMNIWeb service (https://omniweb.gsfc.nasa.gov/). Due to the size of the specification model output and the electron PSD reference dataset, these cannot be hosted on an online repository platform, but will be made available upon request.

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