

Statistical Downscaling of Coastal Directional Wave Spectra Using Deep Learning

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March 12, 2024

Abstract

The modelling of coastal Directional Wave Spectra (DWSs) often requires downscaling techniques integrating DWSs from open ocean boundaries. Dynamic downscaling methods reliant on numerical wave models are often computationally expensive. In coastal areas, wave dynamics are strongly influenced by the topography, implying that once the DWSs at the open ocean boundary are known, the DWSs at various locations along the coast are almost determined. This property can be utilized for statistical downscaling of coastal DWSs. This study presents a deep learning approach that can compute coastal DWSs from open ocean DWSs. The performance of the proposed downscaling model was evaluated using both numerical wave model data and buoy data in the Southern California Bight. The results show that the deep learning approach can effectively and efficiently downscale coastal DWSs without relying on any predefined spectral shapes, thereby holding promise for coastal wave climate studies.

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12
13 **Key Points:**

- 14 • A deep learning-based method to downscale open ocean directional wave spectra to
15 coastal regions
16 • The method gives reliable coastal directional wave spectra with low computational costs
17 and is useful for wave climate studies

18

19 **Abstract**

20 The modelling of coastal Directional Wave Spectra (DWSs) often requires downscaling
21 techniques integrating DWSs from open ocean boundaries. Dynamic downscaling methods
22 reliant on numerical wave models are often computationally expensive. In coastal areas, wave
23 dynamics are strongly influenced by the topography, implying that once the DWSs at the open
24 ocean boundary are known, the DWSs at various locations along the coast are almost
25 determined. This property can be utilized for statistical downscaling of coastal DWSs. This study
26 presents a deep learning approach that can compute coastal DWSs from open ocean DWSs. The
27 performance of the proposed downscaling model was evaluated using both numerical wave
28 model data and buoy data in the Southern California Bight. The results show that the deep
29 learning approach can effectively and efficiently downscale coastal DWSs without relying on
30 any predefined spectral shapes, thereby holding promise for coastal wave climate studies.

31

32 **Plain Language Summary**

33 The directional Wave Spectrum (DWS) describes the distribution of wave energy among
34 different frequencies and directions. It is important for many practical applications such as the
35 design of coastal structures and hazard assessment. Modelling of coastal DWSs often involves
36 running a regional numerical wave model, which is very computationally intensive. This study
37 introduces a deep learning method to accurately predict coastal DWSs using open ocean wave
38 data, reducing computational costs. By leveraging the influence of topography on wave
39 dynamics, the model downscales DWSs along the coast. Tested by a case study in the Southern
40 California Bight, the approach proves effective. This advancement offers a promising tool for
41 studying coastal wave climates in future climate scenarios.

42

43 **1 Introduction**

44 Wind-generated surface gravity waves (hereafter, waves) are the most ubiquitous
45 phenomenon observable on the sea surface. Directional Wave Spectra (DWSs), as a fundamental
46 tool for studying and describing waves, have been widely used in studies of waves and related
47 ocean/coast engineering. In contrast to the conventional usage of Integral Wave Parameters
48 (IWPs) such as Significant Wave Height (SWH), Mean Wave Direction (MWD), and Mean
49 Wave Period (MWP), which provide only a limited description of the wave field and can be
50 misleading in sea states with multiple wave components, DWSs can depict the distribution of
51 wave energy across different frequencies and directions. They have the capability to differentiate
52 waves from different origins, making them a detailed and comprehensive tool for describing
53 waves (e.g., Holthuijsen 2007). Therefore, the effective acquisition of wave spectra is of
54 significant importance for both scientific research and human activity.

55 DWSs in coastal areas can provide vital information for the protection of coastal
56 infrastructure, the study of beach morphology evolution, and wave climate research. Hence,
57 employing downscaling methods to obtain local DWSs using data from offshore waves holds
58 paramount importance for both coastal engineering and wave climate studies. Compared to the
59 DWS in coastal regions, the DWS in the open ocean is relatively easy to obtain through
60 numerical modelling (e.g., Alday et al. 2021), statistical modelling (e.g., Song and Jiang 2023),
61 or remote sensing (e.g., Jiang et al. 2022). Once DWSs in the open ocean boundary are obtained,

62 coastal DWSs can then be modelled using a higher-resolution numerical wave model (NWM),
63 which is often termed dynamic downscaling. However, the dynamic downscaling approach is
64 subject to computational resource constraints, limiting its scope of application and efficiency.
65 Therefore, several statistical downscaling methods with low computational costs were presented
66 as a more efficient and economical alternative (e.g., Hegermiller 2017a, James et al. 2018,
67 Ricondo et al. 2023).

68 Topographic modulation, including land shadowing, shoaling, refraction, bottom
69 friction, depth-induced breaking, plays the most important role in the evolution and variability of
70 nearshore DWSs. Given that topography is a relatively stable factor, a strong correspondence can
71 be established between the nearshore DWSs and the open ocean DWSs once the topography is
72 determined. When the DWS at the ocean boundary is ascertained, the corresponding nearshore
73 DWS can also be essentially determined. This can be regarded as the theoretical basis for
74 statistical downscaling. However, such an implicit mapping relationship from the open ocean
75 boundary to the nearshore DWSs might entail a certain level of nonlinearity and complexity.

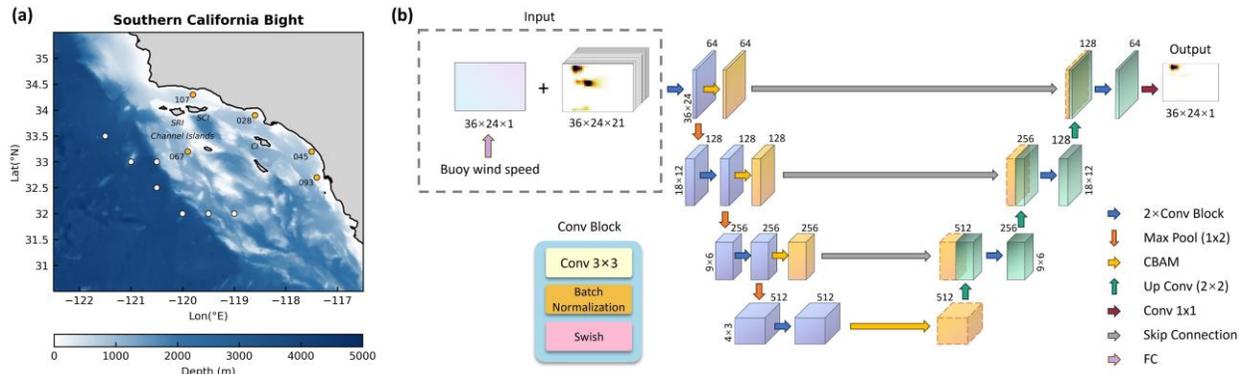
76 In recent years, machine learning technologies, especially the fast-developing deep
77 learning (DL), have opened new avenues for such problems. The DL methods can “learn” the
78 features and correlations between inputs and outputs from a large amount of data by supervised
79 training. They are well suited for the problem that there are quantitative relationship inputs and
80 outputs but the relationship is complex in its explicit form. Due to its powerful ability in
81 nonlinear regression, DL has been widely used in many aspects of oceanography (e.g., Ham et al.
82 2019, Jiang 2022), including modelling ocean waves (e.g., James et al. 2018, Song and Jiang
83 2023). Regarding DL-based downscaling, James et al. (2018) showed that DL is able to
84 statistically downscale the bulk wave parameters very efficiently in a semi-closed basin, which
85 can serve as a surrogate to NWMs. Song and Jiang (2023) show that DL has the capability to
86 predict single-point DWSs in open oceans with (both local current and remote historical) wind
87 forcing with low computational costs. When abstracting the problem of statistical downscaling of
88 DWSs at a given point, we find that deep learning seems to be a good tool for digging such
89 complex quantitative relationships between input (DWSs in the open ocean boundary) and output
90 (DWSs at a given coastal location).

91 In this paper, we establish a statistical model to downscale DWSs from the open ocean
92 boundary to a coastal location based on a UNet architecture. The model can capture the
93 topographic modulations on DWSs all at once from the data, resulting in accurate results while
94 significantly reducing computational costs compared to traditional dynamic downscaling
95 methods. It is noted that the aim of all such statistical models is not to replace physics-based
96 NWMs, but rather to serve as a faster data-driven surrogate that is applicable for time-sensitive
97 applications and computational resource-limited applications. Through this study, we aim to
98 showcase the potential of DL in the application of DWS downscaling, providing insightful
99 perspectives and inspiration for future research. The structure of this paper is as follows: Section
100 2 introduces the study area, the dataset employed, and the UNet model architecture. Section 3
101 presents and analyzes the experimental results. Section 4 discusses and summarizes the findings.

102 2 Study Area, Data, and Methods

103 2.1 Study Area

104 The study area selected for this study is the Southern California Bight (SCB, Figure 1a),
 105 located along the western coast of the United States, spanning from Point Conception to the
 106 Mexican border. The SCB is characterized by complex and dynamic wave conditions, making it
 107 a focal area for wave research. The wave climate in this region is predominantly influenced by
 108 swells originating from Westerlies of both North and South Pacific, as well as local wind seas
 109 (Jiang 2020). These wave systems all exhibit temporal variability across various scales, including
 110 seasonal, inter-annual, and long-term trends (Jiang and Mu 2019). Moreover, the wave
 111 conditions here are significantly modulated (including wave refraction, diffraction, and
 112 sheltering) by the highly irregular shelf topography and many geographical features such as
 113 Santa Rosa Island (SRI), Santa Cruz Island (SCI), and Santa Catalina Island (CI), leading to
 114 substantial small-scale coastal variations in nearshore wave energy (e.g., Hegermiller et al.
 115 2017b). This area can be regarded as an ideal location for the study of DWS downscaling
 116 techniques, given the extensive transformation of the coastal DWSs. By statistically downscaling
 117 DWSs in the SCB, we aim to enhance our ability to predict nearshore wave conditions and to
 118 provide robust tools for DWS downscaling in similar complex coastal environments worldwide.



119 **Figure 1.** The study area and the architecture of the UNet model used in this study. (a) The
 120 bathymetry of the Southern California Bight (Bathymetric data are from ETOPO 2022, NOAA
 121 NCEI 2022, which is available at: <https://www.ncei.noaa.gov/products/etopo-global-relief-model>
 122). The five orange circles represent the locations of five CDIP buoys where directional wave
 123 spectra are available from both the IOWAGA dataset and CDIP dataset (see Section 2.2). The
 124 seven white points denotes the locations of open ocean directional wave spectra that are used as
 125 model input in this study. (b) An illustration of the UNet architecture used in this study. The
 126 input data comprise 21 directional wave spectra from 7 different boundary locations and three
 127 time points (zero, three, and six hours before the current time), plus the wind vector from buoy
 128 points. Each directional wave spectrum is represented in a format with a width of 24 (directions)
 129 and a height of 36 (frequencies), corresponding to outputs for the IOWAGA dataset. The
 130 dimensional attributes of the wind data obtained from buoy points are transformed through a
 131 fully connected neural network layer to ensure alignment with the dimensional structure of the
 132 wave spectrum. Each colored cube symbolizes a feature map, with the numbers on the left and
 133 right sides indicating the width \times height dimensions, and the numbers at the top representing the
 134 number of channels. The blue arrows denote two Conv-Blocks, with each Conv-Block
 135 comprising a 3×3 convolution, batch normalization, and Swish activation function, as depicted in
 136

137 the lower left module. The orange arrows represent a 2×2 max pooling operation, while the
138 green arrows indicate an up-convolution operation. The red arrows signify a 1×1 convolution,
139 and the gray arrows represent skip connections, which entail the concatenation of features. The
140 final output of the model is the predicted DWS with also 24 directions and 36 frequencies.

141 2.2 Data

142 Nowadays, there are several global datasets of DWS with coarse resolution, such as
143 ERA5 wave (Hersbach et al. 2020), CAWCR (Centre for Australian Weather and Climate
144 Research) wave hindcast (Smith et al. 2020), and IOWAGA (Integrated Ocean Waves for
145 Geophysical and other Applications) hindcast (Alday et al. 2021). IOWAGA is a global hindcast
146 wave field dataset generated using the WAVEWATCH III® model (WW3DG 2019). This
147 hindcast is run with the physical parameterization of Ardhuin et al. (2010) forced by the global
148 10-m-wind data from the ERA5 dataset, surface current fields from the CMEMS-Globcurrent,
149 and ice concentration from the IFREMER SSMI-derived daily product. Without assimilating
150 wave observations, the data showed good agreement with both buoy and altimeter
151 measurements. The DWS in this wave model are discretized in 24 directions (15° directional
152 resolution) and 36 frequencies exponentially spaced from 0.034 to 0.95 Hz with a 1.1 increment
153 factor from one frequency to the next. The global model was with a resolution of $0.5^\circ \times 3h$. This
154 dataset contains not only the integrated (and partitioned) wave parameters, but also DWSs at
155 more than 10,000 points all along the world coastline plus the locations of moored buoys
156 (including those in Figure 1) and some additional offshore points. In the study area, a two-way
157 nested grid with a higher resolution of $1/6^\circ$ was used and the wave data were dynamically
158 downscaled. The dataset is available from the website of Laboratoire d'Océanographie Physique
159 et Spatiale (LOPS), IFREMER (<https://www.umr-lops.fr/Donnees/Vagues>) and more details can
160 be found in Alday et al. (2021).

161 The Coastal Data Information Program (CDIP) constitutes an extensive network designed
162 for monitoring wave and beach conditions along the United States coastline. The program has
163 strategically positioned and maintained wave buoys at different locations. These directional wave
164 buoys are capable of measuring waves with periods ranging from 1.6 to 30 seconds. The wave
165 spectrum data of these buoys encompasses 64 frequencies, ranging from 0.025Hz to 0.58Hz. For
166 each of these frequencies, the CDIP provides the first five Fourier coefficients of waves (“First-
167 5”) which are the minimum requirement for reconstructing directional wave spectra. In this
168 study, buoy DWSs were reconstructed using the Maximum Entropy Method from the
169 aforementioned “First-5” (Earle et al., 1999). It is noted that different reconstruction method can
170 result in different DWSs, and these methods have problems such as reducing the directional
171 spread and generating spurious peaks. Also, the buoy-reconstructed DWSs are often noisy with
172 respect to spectral densities at different frequency-direction bins (e.g., Jiang et al., 2022), but
173 they can give a good reference for the spectral shape and the IWPs from buoys, especially
174 SWHs, are reliable. All data and products associated with the CDIP are accessible via the CDIP
175 THREDDS server (<http://thredds.cdip.ucsd.edu/>). More details of this dataset are available in
176 Behrens et al. (2024).

177 We select the data of IOWAGA DWSs at seven open ocean points ($121.5^\circ W, 33.5^\circ N$;
178 $121.0^\circ W, 33.0^\circ N$; $120.5^\circ W, 33.0^\circ N$; $120.5^\circ W, 32.5^\circ N$; $120.0^\circ W, 32.0^\circ N$; $119.5^\circ W, 32.0^\circ N$; and
179 $119.0^\circ W, 32.0^\circ N$) as the input for the DL model. The DWSs at five buoy locations, namely

180 CDIP067, CDIP028, CDIP045, CDIP093, and CDIP107, are used for training and evaluating the
181 DL downscaling model. The locations of these input and output points are shown in Figure 1a.

182 Downscaling process itself is often regarded as a model-to-model (a coarse-resolution
183 one to a fine-resolution one) problem. Therefore, the IOWAGA DWSs at these buoy locations
184 are used as the target output to train and evaluate the DL downscaling model. Meanwhile, we
185 also used the CDIP buoy-reconstructed DWSs directly as the output to show that this DL model
186 can also directly downscale the coarse-resolution modelled DWSs using in-situ observations.

187 2.3 Methods

188 The UNet architecture has emerged as a significant advancement in in medical image
189 segmentation (Ronneberger et al. 2015). In this study, we employ the UNet architecture with
190 modifications aimed at enhancing its performance. Firstly, we incorporate the CBAM
191 (Convolutional Block Attention Module) attention mechanism (Woo et al. 2018) into the encoder
192 section, enabling the network to focus more intently on the important features within the DWSs.
193 Secondly, we substitute the ReLU activation function in each convolutional block with the Swish
194 activation function (Ramachandran et al. 2017) and adopted the Lion optimizer (Chen et al.
195 2023). These enhancements are intended to improve the model's generalization capabilities,
196 enhance prediction accuracy, and expedite the training process.

197 As illustrated in Figure 1b, the UNet architecture in this study comprises a U-shaped
198 encoder-decoder structure. Given the dimensions of the input data, we have employed three
199 encoder-decoder modules in this instance. The input data is of the size $[24, 36, 7 \times 3 + 1]$ denoting
200 24 directions, 36 frequencies, 7 open ocean locations, 3 time points (zero, three, and six hours
201 before the current time, to take the wave propagation time into consideration), plus 1 wind vector
202 record at the target location that is then transformed into a 24×36 matrix through a fully
203 connected neural network. This wind vector is to capture the high-frequency tails that are
204 primarily impacted by local wind at the target location rather than boundary conditions.

205 The foundational module of the UNet network comprises two Conv-Blocks, each
206 comprising a 3×3 two-dimensional convolutional layer, followed by a BatchNorm2d layer and a
207 Swish activation function. The encoder section (left half of Figure 1b) is composed of double
208 convolutional blocks, a CBAM, and max pooling. This arrangement progressively compresses
209 the dimensions of the feature map in terms of both length and width, thereby enhancing higher-
210 order features. The CBAM serves to amplify crucial features while simultaneously suppressing
211 less important features at the respective scale of the image. These features are then fed back to
212 the corresponding up-sampling portion of the network through skip connections, enabling the
213 model to generate output utilizing multiple input scales. Following the encoder, an equivalent
214 number of decoders (right half of Figure 1b) decode the features, including up-sampling to
215 double the size of the feature map and skip connections. This process yields a feature map of the
216 size $[24, 36, 64]$. The final layer of the model consists of a 1×1 convolutional layer which
217 reduces the number of channels to 1, producing the final 24×36 DWS output of the model.

218 For each buoy location, we utilize data spanning 29 years from 1993 to 2021, dividing it
219 into training (1993-2015) and testing (2016-2021) sets. Prior to inputting the DWS data into the
220 network, we randomly shuffle samples within the training set. The value ranges of spectral
221 densities vary significantly for different frequencies and directions bins. Therefore, we apply the
222 Min-Max scaling normalization (normalizing the data in every spectral bin into the range $[0, 1]$)

223 to each spectral bin to mitigate the scale sensitivity and accelerate the convergence of model
224 training.

225 The loss function is the Mean Squared Error (MSE) between the predicted and actual
226 values of the normalized wave spectral densities. The MSE is computed as follows:

$$227 \quad MSE = \frac{1}{m} \sum_{i=1}^m (y_{pre}^i - y_{true}^i)^2 \quad (1)$$

228 where m represents the number of samples, y_{pre}^i denotes the predicted value from the model
229 output for the i -th spectral bin, and y_{true}^i is the reference value of the wave spectrum (IOWAGA-
230 downscaled or buoy-measured) for the i -th spectral bin.

231 The model training process is configured to run a maximum of 100 epochs. To enhance
232 training efficiency and mitigate overfitting, we employ an early stopping strategy, i.e., if no
233 reduction in the loss on the validation set is observed for 10 consecutive epochs, the training is
234 halted. Moreover, to further optimize the performance of the model, we employ a dynamic
235 learning rate adjustment strategy. The initial learning rate is set to 10^{-4} , and if the loss on the
236 training set does not decrease for 4 epochs, we reduce the learning rate to one-tenth of its
237 previous value. To prevent the learning rate from becoming excessively small, potentially halt
238 training, we set a lower limit for the learning rate at 10^{-7} . All training experiments converged
239 before reaching the preset maximum of 100 epochs, meeting the early stopping criteria.

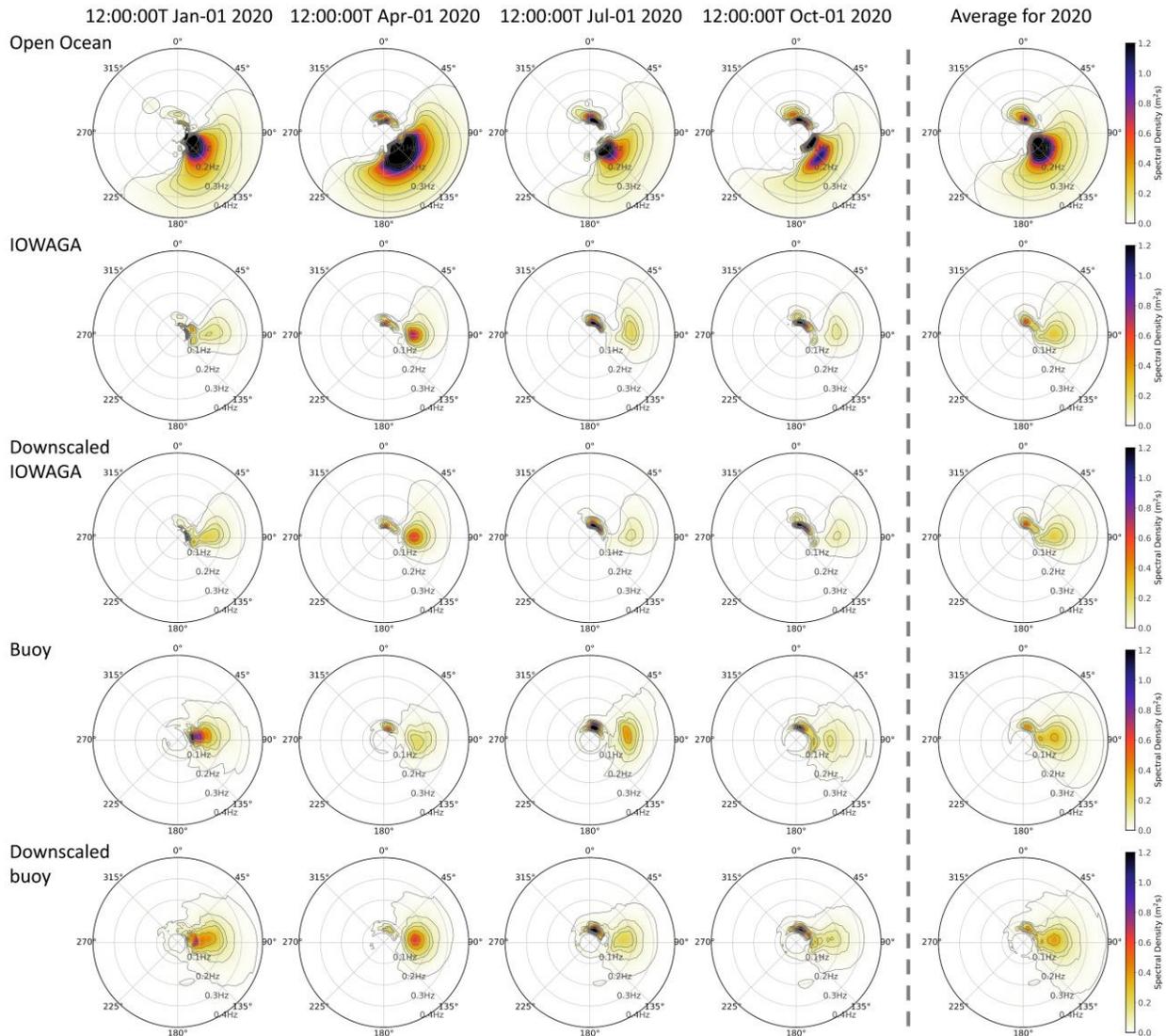
240 The training was conducted separately on five buoy points within the IOWAGA and
241 CDIP datasets, resulting in a total of ten models. All models were trained from scratch, and the
242 model training was conducted on a single NVIDIA 3080Ti graphics card, with Ubuntu 22.04
243 LTS serving as the operating system. The code of UNet is implemented using Python 3.10. The
244 training duration for each buoy point model is within one hour, and it takes only several seconds
245 to downscale 6-year data at each location using the trained model.

246 **3 Results**

247 First, we use the IOWAGA DWSs at the buoy locations to assess whether the DL
248 downscaling model can reproduce the dynamic downscaling in the NWM within acceptable error
249 margins. Taking the CDIP028 buoy location as an example, the five rows in Figure 2 are: the
250 DWSs from its nearest open boundary point (120.5°W , 33.0°N) before downscaling,
251 dynamically downscaled IOWAGA DWSs, DL-downscaled DWSs using IOWAGA DWSs as
252 training targets, buoy-reconstructed DWSs, and DL-downscaled DWSs using buoy DWSs as
253 training targets, respectively. For each row, the four columns to the left of the dashed line are the
254 corresponding DWSs at four arbitrarily selected time points (12:00:00T on the 1st of Jan, April,
255 July, and October, 2020), followed by the corresponding Annual Mean DWS (AMDWS) in 2020
256 to the right of the dashed line.

257 The comparison between the 1st and 2nd rows shows that the shapes of the DWSs in the
258 coastal region can be largely different from the DWSs in the open ocean due to the coastal
259 processes, even if the two locations are not far away (~ 250 km) from each other. For the DWSs
260 at the open ocean point, they often contain narrow peaks at $-20^{\circ}\sim 20^{\circ}$ corresponding to the swells
261 coming from the westerlies of the South Pacific, which appears as only one peak in the
262 AMDWS. Another more prominent feature in DWSs in the open ocean location is the
263 southeastward peaks, which partly correspond to swells coming from the North Pacific

264 westerlies and partly correspond to wind-seas generated locally by California low-level coastal
 265 jets. These two systems also appear as only one peak in the AMDWS. Besides, low-energy
 266 southward low-frequency partitions can also be observed in some cases but not in the AMDWS
 267 because their energy is smoothed and overwhelmed by wave systems with larger spectral
 268 densities.



269
 270 **Figure 2.** The comparison of directional wave spectra (DWSs) from different data sources at the
 271 location of buoy CDIP028. The 1st row is the DWSs at the open boundary point (120.5°W,
 272 33.0°N) before downscaling. The 2nd row shows the corresponding DWSs from IOWAGA at the
 273 buoy location, and the 3rd row shows the results from the DL downscaling model using
 274 IOWAGA DWSs as the training target. The 4th row is the corresponding buoy reconstructed
 275 DWSs, and the 5th row is the results from the DL downscaling model using buoy DWSs as the
 276 training target. The four columns to the left of the dashed line in each row are the corresponding
 277 DWSs at four arbitrarily selected time points. The five DWSs to the right of the dashed line in
 278 each row are the corresponding annual mean DWSs in 2020.

279 As waves in the open ocean propagate to the coastal regions (2nd row), energy
 280 attenuation and refraction occur. At the CDIP028 location, positions of peaks corresponding to
 281 northward swells experience only small changes, and their corresponding peak in the AMDWS
 282 remain largely unchanged, albeit with substantially reduced spectral densities. Meanwhile, the
 283 southeastward waves, both wind-seas and swells, are refracted significantly to eastward ones,
 284 accompanied by considerable energy reduction. Moreover, low-energy southward partitions in
 285 the open ocean point disappear in the coastal location due to the impact of local topography.

286 Comparing the 2nd and the 3rd rows in Figure 2, it can be seen that the DL downscaling
 287 model can well capture the features of spectral evolution. For both individual instantaneous
 288 DWSs and AMDWS, the DL-downscaled DWSs have a good visual agreement with those
 289 derived from dynamic downscaling with respect to both spectral shape and energy level.
 290 Particularly, spectral bins with relatively high energy densities are accurately modeled, with
 291 well-captured spectral peaks. To save space, the results at the rest four locations are only shown
 292 in Figures S1-S5 in the Supporting Information (SI). These figures also show that the coastal
 293 DWSs obtained by the DL model have a good agreement with those from dynamic downscaling.

294 To further evaluate the performance of the DL downscaling model from a statistical point
 295 of view, three IWPs, including the SWH, MWP, and MWD, are computed from the dynamic
 296 downscaling method and the DL downscaling model, and are then compared. As mentioned in
 297 Section 1, these IWPs provide only a limited description of the wave and can be sometimes
 298 misleading in sea states with multiple wave components. Also, two spectra with different shapes
 299 can sometimes have the same IWP. However, Figure 2 and Figures S1-S5 have shown that the
 300 spectral shapes derived from the two methods have a good agreement in general. This
 301 consistency in spectral shape guarantees the comparison of IWPs to be a reasonable way to
 302 evaluate the performance of the DL downscaling model. These IWPs, especially SWH, are also
 303 widely used in the verification of NWMs because high-quality SWH measurements are available
 304 from space-borne altimeters (e.g., Alday et al. 2021; Liu et al. 2021). For a more detailed
 305 quantitative assessment, the bias, Root-Mean-Square Error (RMSE), and Correlation Coefficient
 306 (CC) are used as the error metrics to evaluate the performance of the DL downscaling model:

$$307 \quad Bias = \frac{1}{n} \sum_{i=1}^n (y_i - x_i) \quad (2)$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - x_i)^2} \quad (3)$$

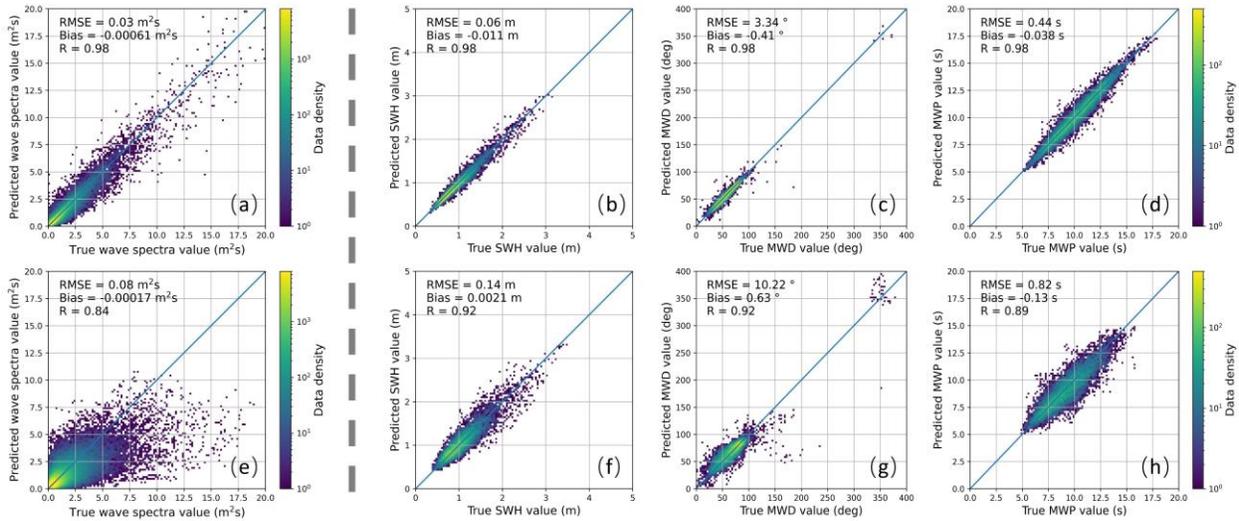
$$CC = \frac{\sum_{i=1}^n (y_i - \bar{y})(x_i - \bar{x})}{\sqrt{\sum_{i=1}^n (y_i - \bar{y})^2} \sqrt{\sum_{i=1}^n (x_i - \bar{x})^2}} \quad (4)$$

308 where x and y denote the IWPs or spectral density from the reference data and the DL models,
 309 respectively, and the bars over them denote their mean values.

310 Figure 3a shows the scatter plot between DL-downscaled and dynamically downscaled
 311 spectral densities at all spectral bins at the location of buoy CDIP028 (all data are from the test
 312 set). Although such a direct comparison between spectral densities is not typically recommended
 313 for evaluating the agreement between two DWSs due to the so-called “double penalty effect” (a
 314 small difference in the location of narrow swell spectral peaks can lead to a large difference in
 315 spectral density), it still provides a quantitative reference on the performance of the DL
 316 downscaling model. The CC between the spectral densities from dynamic downscaling and DL
 317 downscaling is ~ 0.98 , which seems to be a good agreement compared to the CC of spectral

318 densities between two smoothed buoy-reconstructed DWSs (Jiang et al. 2022) and the CC of
 319 spectral densities in Song and Jiang (2023).

320 Figures 3b-3d show the corresponding scatter plots for SWH, MWD, and MWP,
 321 respectively, between the two downscaling methods. Again, the overall results of the three IWPs
 322 all exhibit high overall accuracy: The CCs for SWH, MWD, and MWP all reached 0.98; the
 323 biases for SWH, MWD, and MWP are ~ 0.01 m, $\sim 0.4^\circ$, and ~ 0.04 s, respectively; and the
 324 corresponding RMSEs are ~ 0.06 m, $\sim 3.3^\circ$, and ~ 0.44 s, respectively. Nearly all data points lie
 325 perfectly along the $y = x$ line except for several outliers in the MWD scatter plot. These outliers
 326 correspond to the condition that the overall wave energy is low, in which a small energy error
 327 from the model can have a large impact on the estimation of MWD. The results at the rest four
 328 locations are shown in Figures S6-S10 in the SI where the error metrics of the results from the
 329 DL models are similar to those in Figures 3a-3d. The CCs of the three IWPs in the four points
 330 vary from 0.97 to 1.00, again affirming the consistency of results between the DL downscaling
 331 method and dynamic downscaling.



332
 333 **Figure 3.** Scatter plots between DL downscaling results and their corresponding reference data at
 334 the location of buoy CDIP028. The 1st row is the comparison between DL-downscaled results
 335 (using IOWAGA DWS as training targets) and dynamic-downscaled results, and the 2nd row is
 336 the comparison between DL-downscaled results (using buoy DWS as training targets) and buoy
 337 data. The four columns are the comparison for (a & e) spectral densities, (b & f) SWH, (c & g)
 338 MWD, and (d & h) MWP, respectively.

339 According to the rationale of the DL downscaling method, the downscaling model can
 340 also be trained directly using in-situ observations as targets. Some cases of buoy-reconstructed
 341 and corresponding DL-downscaled DWSs (using buoy DWSs as training targets) for buoy
 342 CDIP028 are shown in the 4th and 5th rows of Figure 2, respectively. The results for the other
 343 buoys are shown in Figures S11-S14. Compared to the DWSs from IOWAGA, the energy ratio
 344 of the wind wave system is slightly higher in the downscaling results of the model, and the swell
 345 is wider due to scattering effects (Jiang et al. 2016, Smit et al. 2018). Besides, the buoy-
 346 reconstructed DWSs themselves are much noisier than modelled DWSs. The noises in DWSs
 347 lead to a strong “double penalty effect” which then results in a CC of only 0.84 between DL-
 348 downscaled and buoy-reconstructed spectral densities (Figure 3e), which is much lower than the
 349 value of 0.98 derived from the “model-to-model” downscaling in Figure 3a. However, the DL

350 downscaling method can still well capture the main shapes and the energy levels of the buoy-
351 reconstructed DWSs for both wind-sea and swell systems. Also, the SWH, MWD, and MWP are
352 in good agreement with the buoy-measured ones: The CCs/RMSEs for SWH, MWD, and MWP
353 are $\sim 0.92/0.14$ m, $0.92/10.22^\circ$, and $0.89/0.82$ s, respectively. Although the agreement is not as
354 good as the comparison between DL and dynamic downscaling, this accuracy is not bad for a
355 model-against-observation comparison. Similar accuracy is observed in the comparisons of IWPs
356 for other buoys, as depicted in Figures S7-S10 in the SI.

357 **4 Discussions**

358 As mentioned in Section 1, the rationale of the DL downscaling method presented in this
359 study is clear: There is an implicit and complex but nearly fixed mapping relationship between
360 the DWSs along open ocean boundaries and the DWS at a coastal location, given the topography
361 is unchanged. This relationship can be fitted by the strong power of deep learning. This is why
362 the DL downscaling can effectively and efficiently downscale open ocean DWSs into nearshore
363 ones without relying on any predefined spectral shapes. However, it is also found that the
364 agreement is better between the DL-downscaled and dynamic-downscaled results is significantly
365 better than that between DL-downscaled and buoy-reconstructed results. This is because when
366 the DL model is trained to downscale the IOWAGA DWSs from the open boundary to coasts,
367 the inputs and the target outputs are more consistent. After all, they are the corresponding inputs
368 and outputs of the NWM for downscaling. However, significant inconsistency exists between
369 modelled open ocean DWSs and buoy DWSs. Although DL models can correct part of the
370 inconsistency through extensive data, there remain inconsistencies that cannot be learned by DL.
371 For instance, buoy DWSs have large random errors (Jiang et al. 2022) that can hardly be
372 replicated by any model. In addition, except for the impact of wind and topography, the
373 evolution of DWSs in the coastal regions is also modulated by wave-current-tide interactions.
374 The information on currents and tides is not used as the input in our DL model (tides and tidal
375 currents are also absent in the IOWAGA hindcast), while these impacts and modulations might
376 be evident in buoy DWSs. It is anticipated that the accuracy of (both dynamic and DL)
377 downscaling can be further improved if the information on currents and tides is available.

378 In some cases, only the information on one point or fewer points in the open ocean
379 boundary is available, and the wind information at the target location might be unavailable. A
380 sensitivity test is conducted to test the performance of the DL model when less input information
381 is used. We try to reduce the number of input locations or the number of input time points to one,
382 or eliminate the wind information as input. For each location, four sets of sensitivity tests are
383 conducted and the corresponding results of DWSs and IWPs are shown in Figures S1-S5 and S6-
384 S10, respectively. Although a slight decrease in model accuracy is observed with the input
385 information reduced, the model can still have an acceptable accuracy even when only one DWS
386 at one time point is used as input without wind information: The spectral shapes are well
387 downscaled and the CCs/RMSEs for SWH, MWD, and MWP are $\sim 0.95/0.10$ m, $0.95/5.1^\circ$, and
388 $0.93/0.75$ s, respectively, at the location of CDIP028 (similar performance for the rest four
389 points).

390 Compared to dynamic downscaling, the DL downscaling method for DWSs presented in
391 this study can significantly reduce computational costs while maintaining high accuracy. It can
392 be used as a surrogate for an NWM in many time-sensitive or computational resource-limited
393 applications. One potential application of this method is in wave climate studies. Nowadays,

394 more and more attentions are drawn to spectral wave climate (e.g., Espejo et al. 2014, Jiang and
395 Mu 2019, Echevarria et al. 2019, Lobeto et al. 2022), but running ensemble high-resolution
396 NWMs to output some coastal DWSs under many different climate scenarios for long-term
397 projections is challenging. This DL downscaling method can rapidly process tens of thousands of
398 sample data in seconds, allowing fast prediction of DWSs under different future scenarios.
399 Future work can be further optimizing the DL model structure using advances in AI and
400 including more physically related input information (such as currents and water level), which
401 might further improve the performance of the model.

402 **Acknowledgments**

403 This work is jointly supported by the National Key Research and Development Program
404 of China (2023YFC3008203), the National Natural Science Foundation of China (42376172),
405 and the Guangdong Basic and Applied Basic Research Foundation (2022A1515240069). We
406 would like to thank IFREMER and CDIP for sharing the data.

407 **Availability Statement**

408 All the data used in this study is available online: IOWAGA data is from Alday et al.
409 (2021), and can be downloaded from the official website of LOPS, IFREMER
410 (<https://www.umn-lops.fr/Donnees/Vagues>). CDIP data is from Behrens et al. (2024), can be
411 download from its official website <https://cdip.ucsd.edu/>. The deep learning models are realized
412 using PyTorch (<https://pytorch.org/>).

413 **References**

- 414 Alday, M., Accensi, M., Ardhuin, F., Dodet, G., (2021). A global wave parameter database for geophysical
415 applications. Part 3: improved forcing and spectral resolution. *Ocean Modelling* 166, 101848.
416 <https://doi.org/10.1016/j.ocemod.2021.101848>
- 417 Ardhuin, F., Rogers, E., Babanin, A.V., Filipot, J., Magne, R., Roland, A., van der Westhuysen, A., Queffelec, P.,
418 Lefevre, J., Aouf, L., Collard, F. (2010). Semiempirical Dissipation Source Functions for Ocean Waves. Part I:
419 Definition, Calibration, and Validation. *Journal of Physical Oceanography*. 40 (9), 1917–1941.
420 <https://doi.org/10.1175/2010JPO4324.1>
- 421 Behrens, J., Olfe, C., Cameron, G., Bucciarelli, R., Timmerman, R., Wright, D., Lodise, J., Merrifield, S., & Terrill,
422 E. (2024). Coastal Data Information Program: advances in measuring and modeling wave activity, climate, and
423 extremes. *Coastal Engineering Journal*. <https://doi.org/10.1080/21664250.2024.2308021>
- 424 Chen, X., Liang, C., Huang, D., Real, E., Wang, K., Pham, H., Dong, X., Luong, T., Hsieh, C.-J., Lu, Y., & Le, Q.
425 V. (2024). Symbolic discovery of optimization algorithms. *Advances in Neural Information Processing*
426 *Systems*, 36.
- 427 Earle, M.D., Steele, K.E., Wang, D.W.C. (1999). Use of advanced directional wave spectra analysis methods. *Ocean*
428 *Eng.* 26 (12), 1421-1434. [https://doi.org/10.1016/S0029-8018\(99\)00010-4](https://doi.org/10.1016/S0029-8018(99)00010-4)
- 429 Echevarria, E. R., Hemer, M. A., & Holbrook, N. J. (2019). Seasonal variability of the global spectral wind wave
430 climate. *Journal of Geophysical Research: Oceans*, 124, 2924–2939. <https://doi.org/10.1029/2018JC014620>
- 431 Espejo, A., Camus, P., Losada, I.J., Méndez, F.J. (2014). Spectral ocean wave climate variability based on
432 atmospheric circulation patterns. *Journal of Physical Oceanography*. 44 (8), 2139-2152.
433 <https://doi.org/10.1175/JPO-D-13-0276.1>
- 434 Ham, Y., Kim, J., Luo, J. (2019). Deep learning for multi-year ENSO forecasts. *Nature* 573 (7775), 568-572.
435 <https://doi.org/10.1038/s41586-019-1559-7>
- 436 Hegermiller, C.A., Rueda, A., Erikson, L.H., Barnard, P.L., Antolinez, J.A.A., Mendez, F.J. (2017a). Controls of
437 multimodal wave conditions in a complex coastal setting. *Geophysical Research Letters*, 44 (24), 312-315,

- 438 323. <https://doi.org/https://doi.org/10.1002/2017GL075272>
- 439 Hegermiller, C.A., Antolinez, J.A.A., Rueda, A., Camus, P., Perez., J., Erikson, L.H., Barnard, P. L., Mendez, F.J.
440 (2017b). A Multimodal Wave Spectrum–Based Approach for Statistical Downscaling of Local Wave Climate.
441 *Journal of Physical Oceanography*, 47 (2), 375–386. <https://doi.org/10.1175/JPO-D-16-0191.1>
- 442 Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz-Sabater, J., Nicolas, J., Peubey, C., Radu,
443 R., Schepers, D., Simmons, A., Soci, C., Abdalla, S., Abellan, X., Balsamo, G., Bechtold, P., Biavati, G.,
444 Bidlot, J., Bonavita, M., De Chiara, G., Dahlgren, P., Dee, D., Diamantakis, M., Dragani, R., Flemming, J.,
445 Forbes, R., Fuentes, M., Geer, A., Haimberger, L., Healy, S., Hogan, R.J., Hólm, E., Janisková, M., Keeley, S.,
446 Lalouaux, P., Lopez, P., Lupu, C., Radnoti, G., de Rosnay, P., Rozum, I., Vamborg, F., Villaume, S., Thépaut,
447 J. (2020). The era5 global reanalysis. *Quarterly Journal of the Royal Meteorological Society*, 146 (730), 1999-
448 2049. <https://doi.org/https://doi.org/10.1002/qj.3803>
- 449 Holthuijsen, L. H. (2007). *Waves in Oceanic and Coastal Waters*. Cambridge University Press, 387pp.
- 450 James, S.C., Zhang, Y., O'Donncha, F. (2018). A machine learning framework to forecast wave conditions. *Coastal*
451 *Engineering*, 137, 1-10. <https://doi.org/https://doi.org/10.1016/j.coastaleng.2018.03.004>
- 452 Jiang, H.Y., Mu, L. (2019). Wave climate from spectra and its connections with local and remote wind climate.
453 *Journal of Physical Oceanography*, 49 (2), 543-559. <https://doi.org/10.1175/JPO-D-18-0149.1>
- 454 Jiang, H., Babanin, A.V., Chen, G. (2016). Event-based validation of swell arrival time. *Journal of Physical*
455 *Oceanography*, 46 (12), 3563-3569. <https://doi.org/10.1175/JPO-D-16-0208.1>
- 456 Jiang, H., Mironov, A., Ren, L., Babanin, A.V., Wang, J., Mu, L. (2022). Validation of wave spectral partitions from
457 swim instrument on-board cfosat against in situ data. *IEEE Trans. Geosci. Remote.*, 60, 1-13.
458 <https://doi.org/10.1109/TGRS.2021.3110952>
- 459 Jiang, H. (2020). Wave Climate Patterns from Spatial Tracking of Global Long-Term Ocean Wave Spectra. *Journal*
460 *of Climate*, 33 (8), 3381–3393, <https://doi.org/10.1175/JCLI-D-19-0729.1>
- 461 Jiang, H. (2022). Wind speed and direction estimation from wave spectra using deep learning. *Atmospheric*
462 *Measurement Techniques*, 15, 1–9, <https://doi.org/10.5194/amt-15-1-2022>
- 463 Liu, Q., Babanin, A.V., Rogers, W.E., Zieger, S., Young, I.R., Bidlot, J., Durrant, T., Ewans, K., Guan, C., Kirezci,
464 C., Lemos, G., Machutchon, K., Moon, I., Rapizo, H., Ribal, A., Semedo, A., Wang, J. (2021). Global wave
465 hindcasts using the observation-based source terms: description and validation. *Journal of Advances in*
466 *Modeling Earth Systems*, 13 (8), e2021M-e2493M. <https://doi.org/10.1029/2021MS002493>.
- 467 Lobeto, H., Menendez, M., Losada, I.J., Hemer, M. (2022). The effect of climate change on wind-wave directional
468 spectra. *Global and Planetary Change*, 213, 103820. <https://doi.org/10.1016/j.gloplacha.2022.103820>.
- 469 Ramachandran, P., Zoph, B., & Le, Q. V. (2017). Searching for activation functions. arXiv preprint
470 arXiv:1710.05941.
- 471 Ricondo, A., Cagigal, L., Rueda, A., Hoeke, R., Storlazzi, C.D., Méndez, F.J. (2023). HyWaves: Hybrid
472 downscaling of multimodal wave spectra to nearshore areas. *Ocean Modelling*, 184, 102210.
473 <https://doi.org/10.1016/j.ocemod.2023.102210>.
- 474 Ronneberger, O., Fischer, P., & Brox, T. (2015). U-net: Convolutional networks for biomedical image segmentation.
475 In *Medical Image Computing and Computer-Assisted Intervention–MICCAI 2015: 18th International*
476 *Conference, Munich, Germany, October 5-9, 2015, Proceedings, Part III* (pp. 234-241). Springer International
477 Publishing. https://doi.org/10.1007/978-3-319-24574-4_28
- 478 Smit, P.B., & Janssen, T.T. (2019). Swell Propagation through Submesoscale Turbulence. *Journal of Physical*
479 *Oceanography*, 49, 2615–2630. <https://doi.org/10.1175/JPO-D-18-0250.1>.
- 480 Smith, G. A., Hemer, M., Greenslade, D., Trenham, C., Zieger, S., & Durrant, T. (2021). Global wave hindcast with
481 Australian and Pacific Island Focus: From past to present. *Geoscience Data Journal*, 8, 24–33.
482 <https://doi.org/10.1002/gdj3.104>
- 483 Song, Y., & Jiang, H. (2023). A Deep Learning–Based Approach for Empirical Modeling of Single-Point Wave
484 Spectra in Open Oceans. *Journal of Physical Oceanography*, 53, 2089–2103. <https://doi.org/10.1175/JPO-D-22-0198.1>.
- 485
- 486 Woo, S., Park, J., Lee, J. Y., & Kweon, I.S. (2018). CBAM: Convolutional block attention module. In *Proceedings*
487 *of the European Conference on Computer Vision (ECCV)* (pp. 3-19).
- 488 The WAVEWATCH III® Development Group (WW3DG). (2019). User manual and system documentation of
489 WAVEWATCH III® version 6.07. Tech. Note 333, NOAA/NWS/NCEP/MMAB, College Park, MD, USA,
490 326 pp. + Appendices.

[Geophysical Research Letters]

Supporting Information for

Statistical Downscaling of Coastal Directional Wave Spectra Using Deep Learning

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Contents of this file

Figures S1 to S15

Introduction

The supporting information shows the results of all downscaling experiments for all five buoy locations used in this study. It contains the following information:

1. Figures S1-S5: The comparison of directional wave spectra (DWSs) between the results from dynamic downscaling and those from Deep Learning (DL) downscaling with different input parameters.
2. Figure S6-S10: The comparison of Integral Wave Parameters (IWPs) between the results from dynamic downscaling and those from DL downscaling with different input parameters, as well as between those from buoy observations and those from DL downscaling.
3. Figure S11-S15: The comparison of DWSs between the results from buoy reconstruction and from DL downscaling using buoy data as training targets.

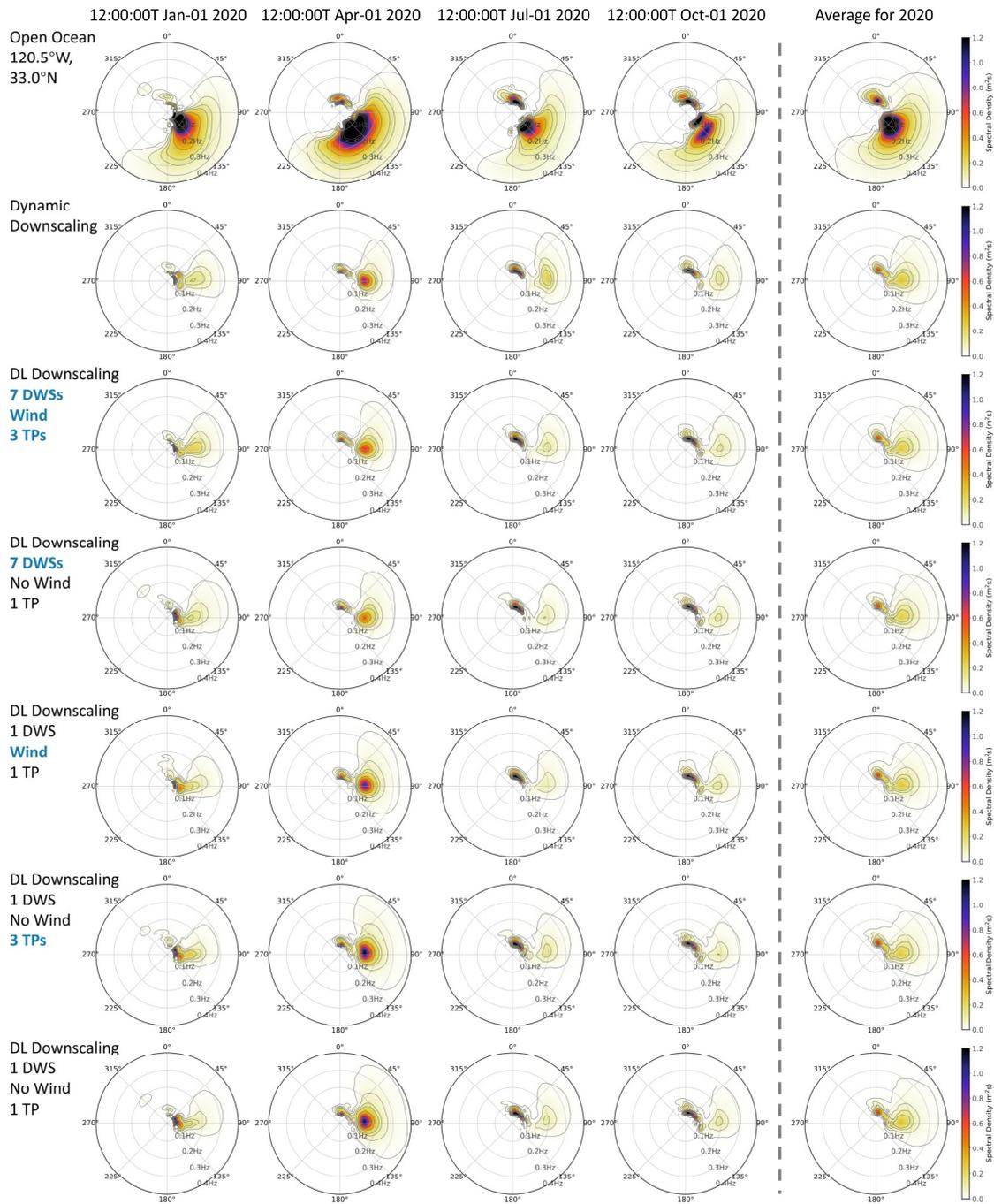


Figure S1. The comparison of directional wave spectra (DWS) between the results from dynamic downscaling and those from Deep Learning (DL) downscaling with different input parameters at the location of buoy CDIP028. The 1st row is the DWSs at the open boundary point (120.5°W, 33.0°N) before downscaling. The 2nd row shows the corresponding dynamic-downscaled DWSs from IOWAGA at the buoy location. The 3rd-7th rows show the results from the DL downscaling model using IOWAGA DWSs as the training target, but with different input parameters. The input parameters for the 3rd row include open boundary DWSs at seven locations and at three time points, and the wind vector at the buoy location (the results shown in Figure 2 in the main text). Those for the 4th row include open boundary DWSs at seven locations but only at one time point, without the

wind vector input. Those for the 5th row include the open boundary DWS at only one location and at only one time point, but with the wind vector input. Those for the 6th row include the open boundary DWSs at only one location but at three time points, without the wind vector input. Those for the 7th row include only the open boundary DWS at only one location and at only one time point, without the wind vector input. The four columns to the left of the dashed line in each row are the corresponding DWSs at four arbitrarily selected time points. The seven DWSs to the right of the dashed line in each row are the corresponding annual mean DWSs in 2020.

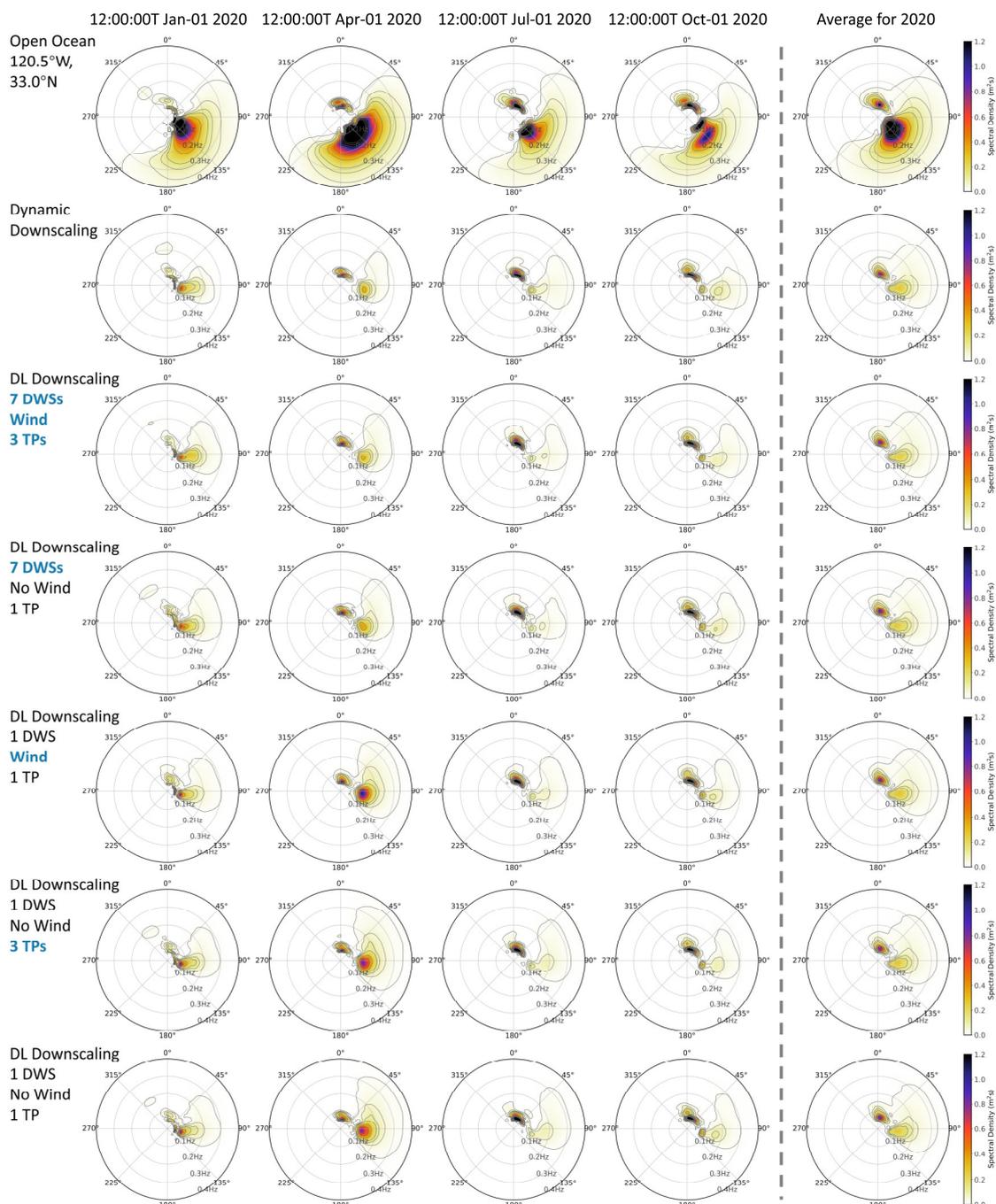


Figure S2. The same as Figure S1, but for buoy CDIP045.

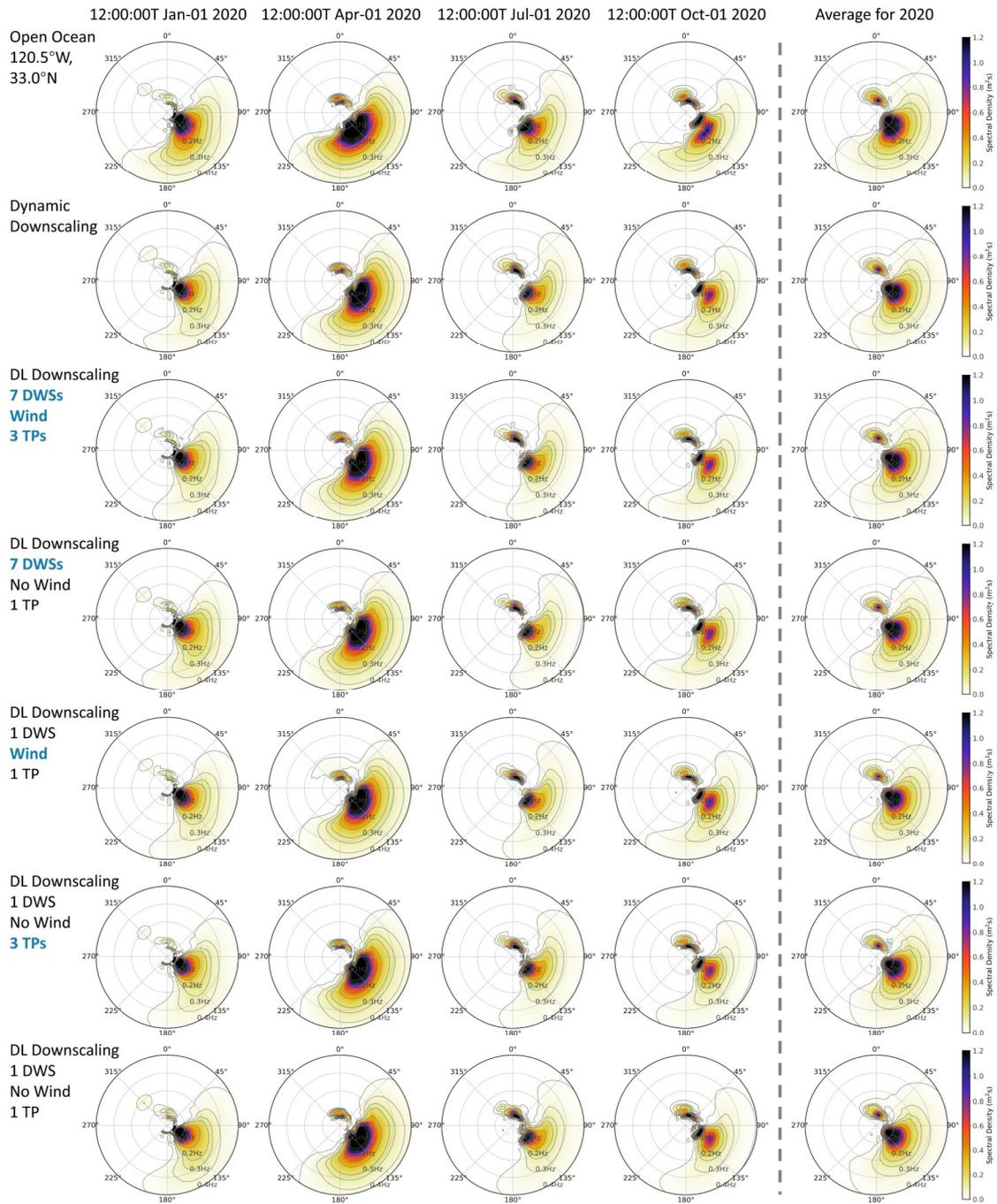


Figure S3. The same as Figure S1, but for buoy CDIP067.

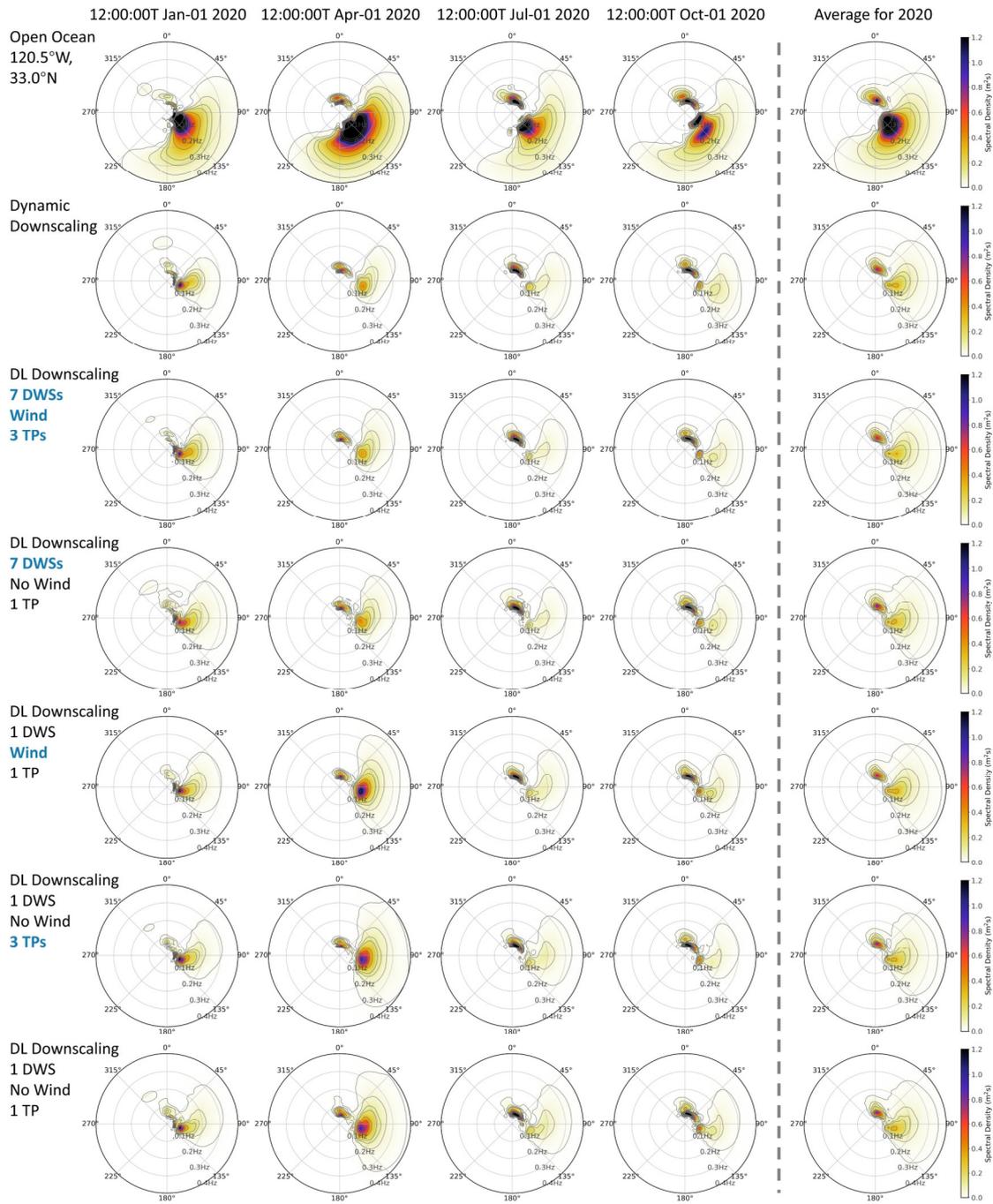


Figure S4. The same as Figure S1, but for buoy CDIP093.

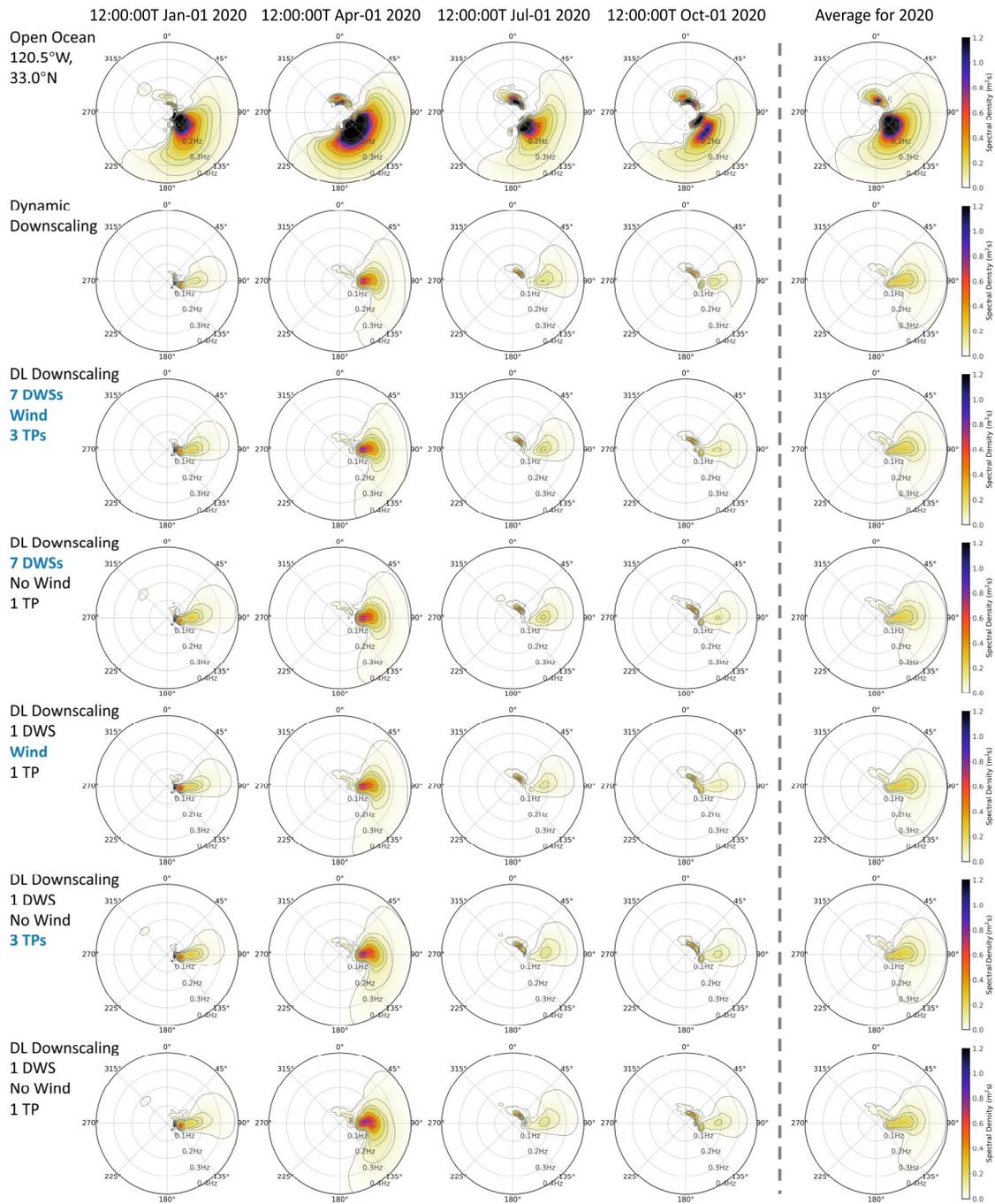


Figure S5. The same as Figure S1, but for buoy CDIP107.

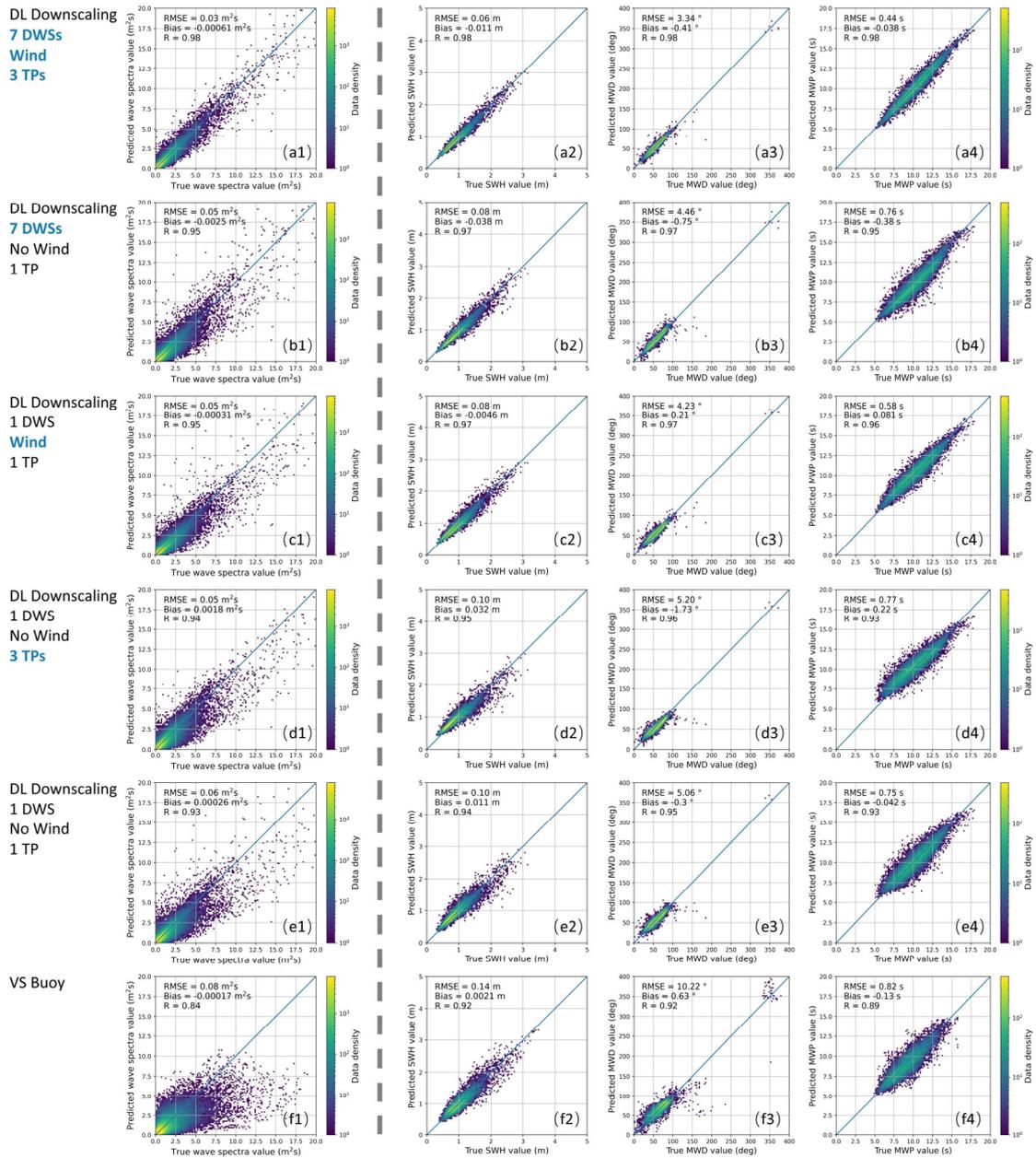


Figure S6. Scatter plots between Deep Learning (DL) downscaling results and their corresponding reference data with different input parameters and training targets at the location of buoy CDIP028. The 1st-5th rows show the comparison between the DL-downscaled results using IOWAGA directional wave spectra (DWSs) as training targets and the dynamic-downscaled results, but with different input parameters. The input parameters for the 1st row include open boundary DWSs at seven locations and at three time points, and the wind vector at the buoy location (the results shown in Figures 3a-3d in the main text). Those for the 2nd row include open boundary DWSs at seven locations but only at one time point, without the wind vector input. Those for the 3rd row include the open boundary DWS at only one location and at only one time point, but with the wind vector input. Those for the 4th row include the open boundary DWSs at only one location but at three time points, without the wind vector input. Those for the 5th row include only the open boundary DWS at only one location and at only one time point, without the wind vector input. The 6th row is the

comparison between DL-downscaled results (using buoy DWS as training targets) and buoy data (the results shown in Figures 3e-3h in the main text). The four columns are the comparison for (the 1st column) spectral densities, (the 2nd column) SWH, (the 3rd column) MWD, and (the 4th column) MWP, respectively.

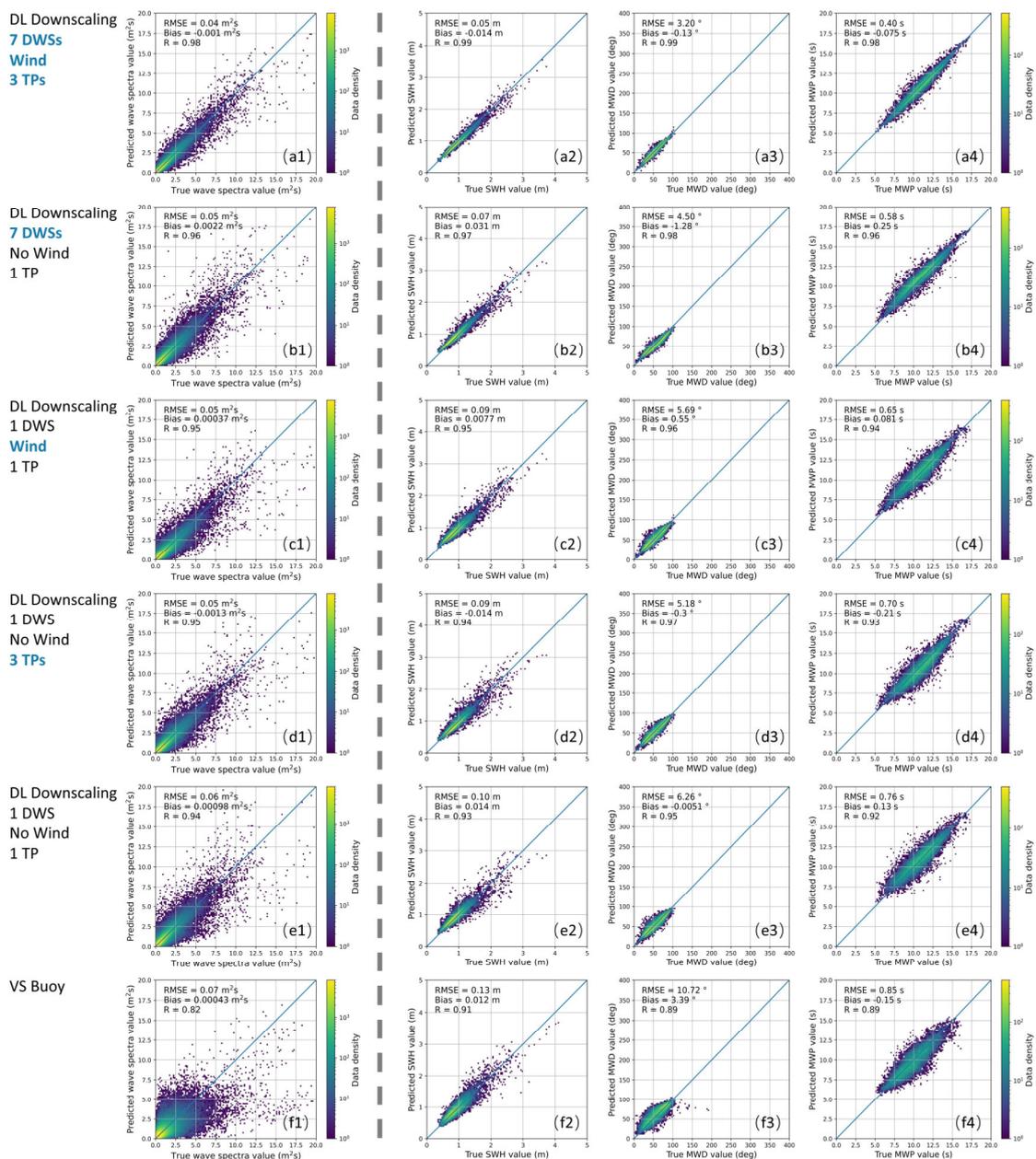


Figure S7. The same as Figure S6, but for buoy CDIP045.

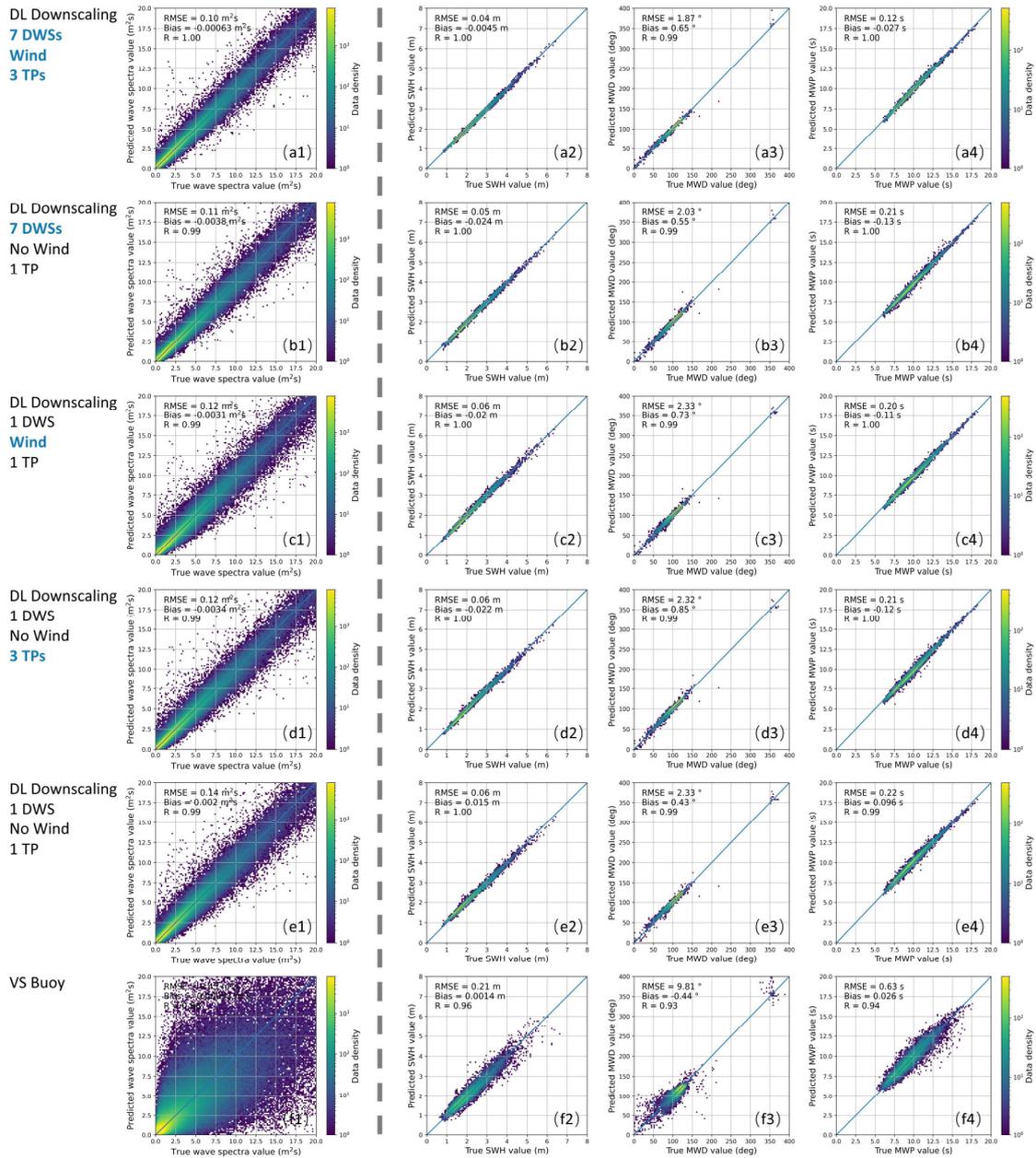


Figure S8. The same as Figure S6, but for buoy CDIP067.

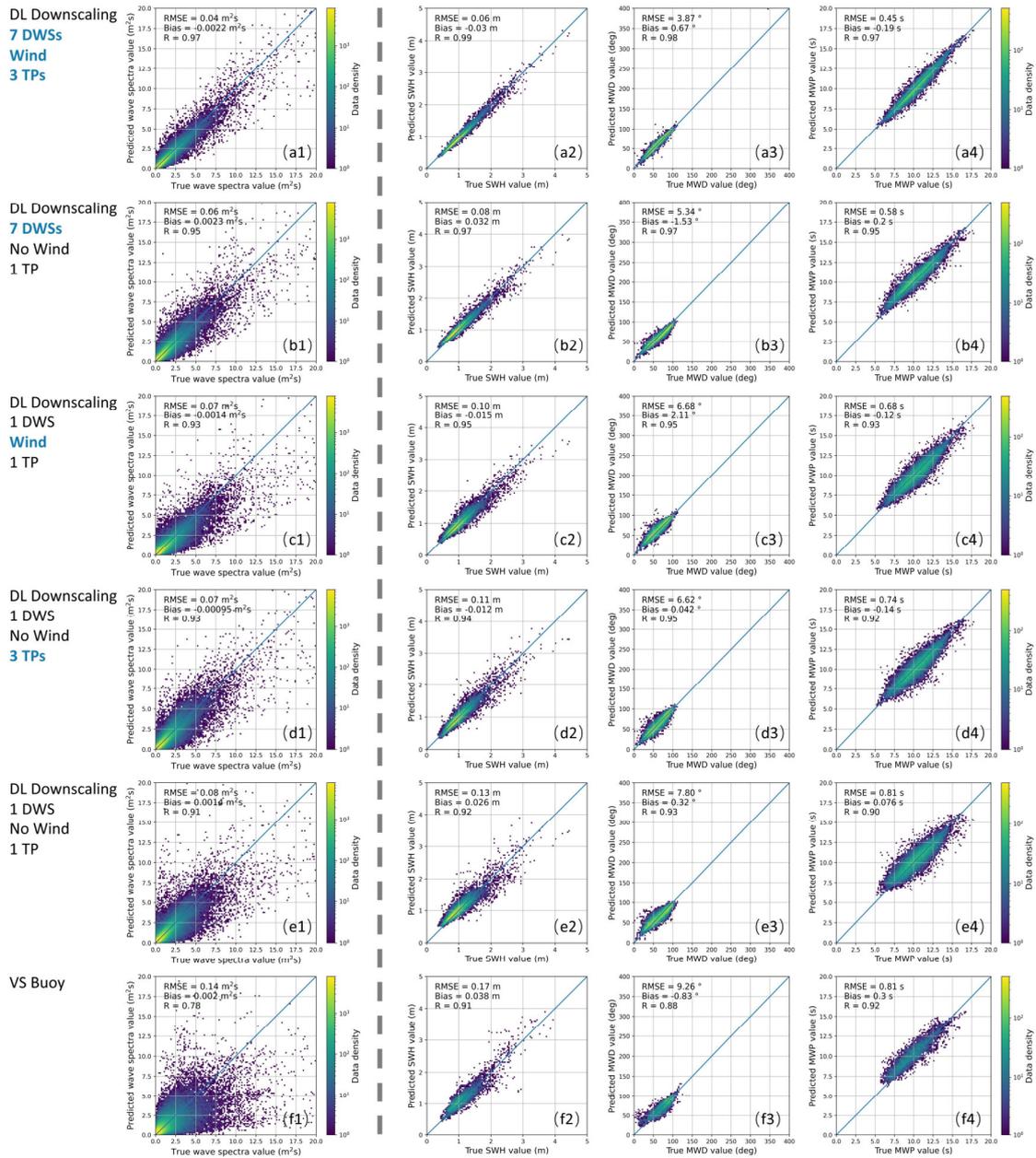


Figure S9. The same as Figure S6, but for buoy CDIP093.

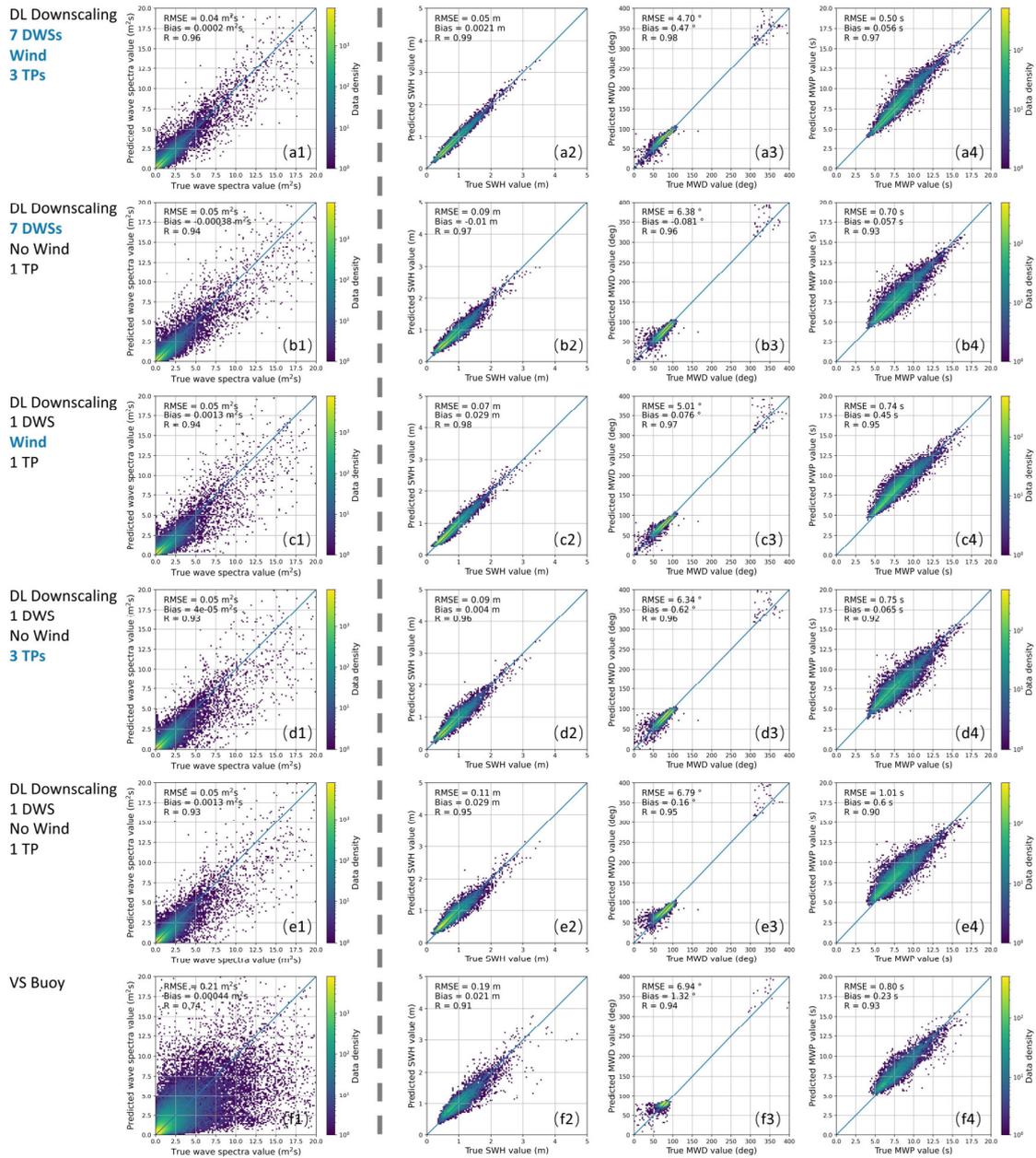


Figure S10. The same as Figure S6, but for buoy CDIP107.

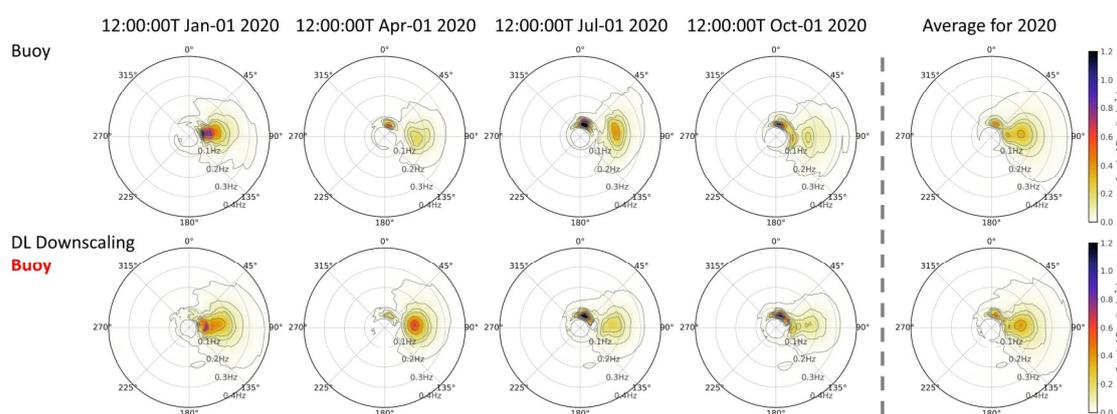


Figure S11. The comparison of directional wave spectra (DWSs) between the results from buoy reconstruction and from Deep Learning (DL) downscaling using buoy data as training targets. The 1st row is the corresponding buoy reconstructed DWSs, and the 2nd row is the results from the DL downscaling model using buoy DWSs as the training target. The four columns to the left of the dashed line in each row are the corresponding DWSs at four arbitrarily selected time points. The two DWSs to the right of the dashed line in each row are the corresponding annual mean DWSs in 2020.

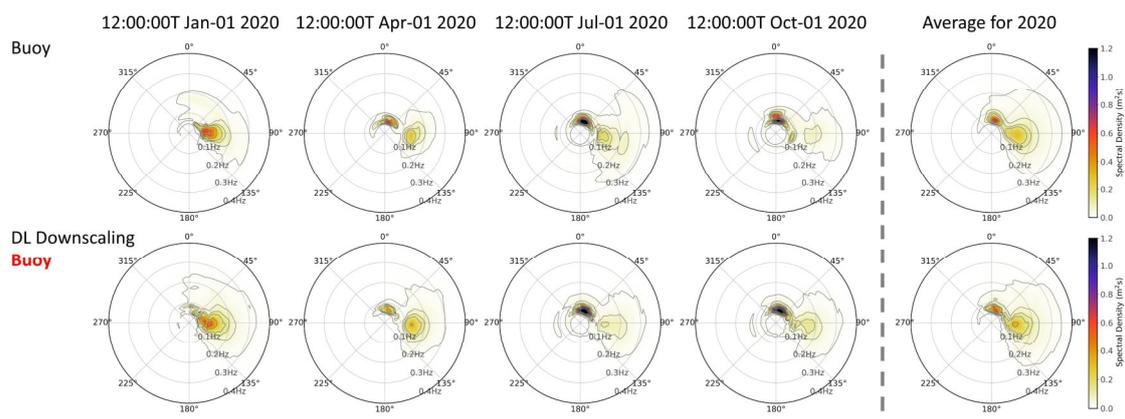


Figure S12. The same as Figure S11, but for buoy CDIP045.

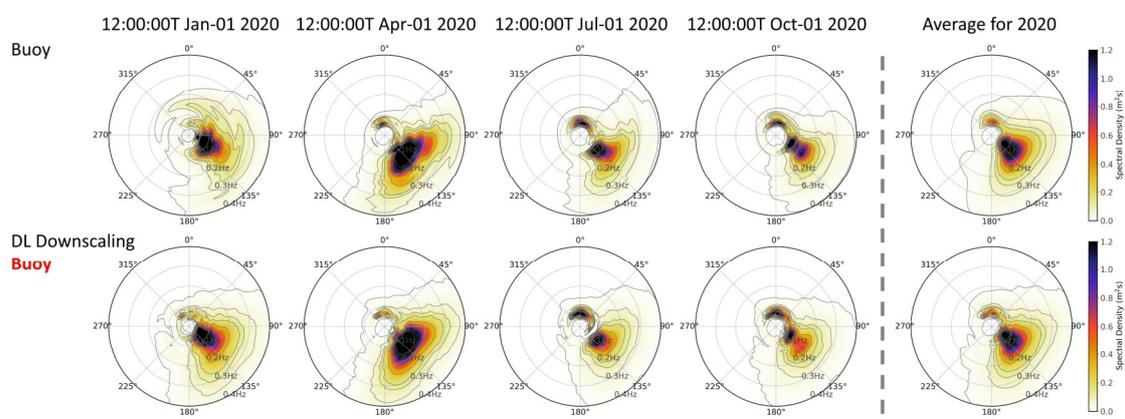


Figure S13. The same as Figure S11, but for buoy CDIP067.

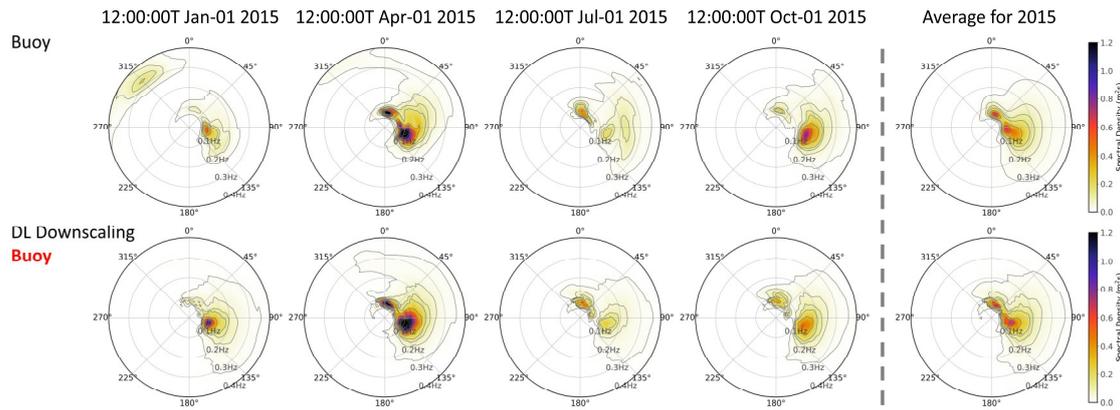


Figure S14. The same as Figure S11, but for buoy CDIP093. Because CDIP093 does not have the data for year 2020, the data of 2015 is used instead (the data is not used in the training process)

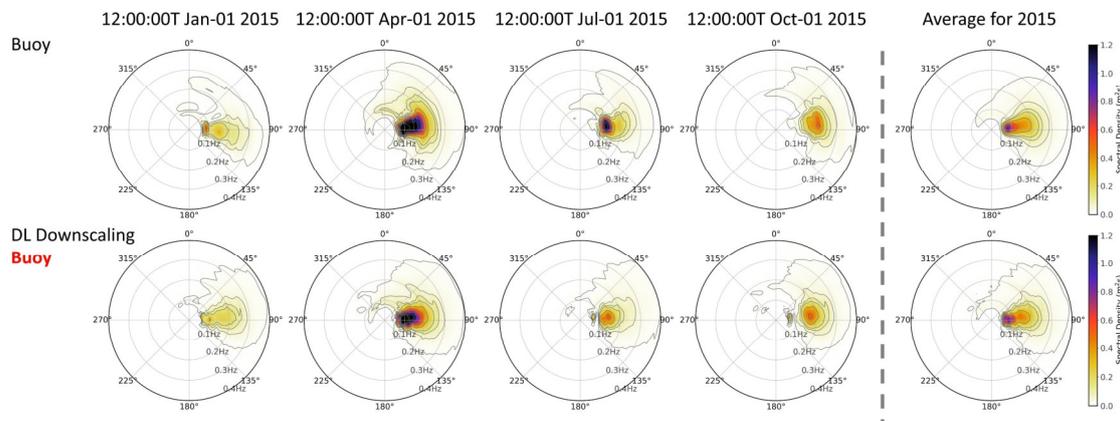


Figure S15. The same as Figure S11, but for buoy CDIP107. Because CDIP107 does not have the data for year 2020, the data of 2015 is used instead (the data is not used in the training process).