PlanetMag: Software for evaluation of outer planet magnetic fields and corresponding excitations at their moons

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Key Points:

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8	• We developed an open-source software package in Matlab called PlanetMag for
9	evaluating planet magnetic field models from the literature
10	• PlanetMag uses ephemeris data and least-squares inversion methods to determine
11	amplitudes and phases of magnetic excitations for moons
12	• Complex excitation moments are determined for all outer planet large moons in
13	support of magnetic sounding investigations

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14 Abstract

Spacecraft magnetic field measurements are able to tell us much about the plan-15 ets' interior dynamics, composition, and evolutionary timeline. Magnetic fields also serve 16 as the source for passive magnetic sounding of moons. Time-varying magnetic fields ex-17 perienced by the moons, due to relative planetary motion, interact electrically with con-18 ductive layers within these bodies (including salty subsurface oceans) to produce induced 19 magnetic fields that are measurable by nearby, magnetometer-equipped spacecraft. Many 20 factors influence the character of the induced field, including the precise amplitude and 21 phase of the time-varying field, known as the excitation or driving field and represented 22 by excitation moments. In this work, we present an open-source Matlab software pack-23 age named PlanetMag that features calculation of planetary magnetic field models avail-24 able in the literature at arbitrary positions and times. The implemented models enable 25 simultaneous inversion of the excitation moments across a range of oscillation frequen-26 cies using linear least-squares methods and ephemeris data with the SPICE toolkit. Here 27 we summarize the available magnetic field models and their associated coordinate sys-28 tems. Precisely-determined excitation moments are a critical input to forward models 29 of global induced fields. Our results serve as a prerequisite to any precise comparison to 30 spacecraft data for magnetic sounding investigation of giant planet moons—connecting 31 the induced magnetic field to a moon's interior requires accurate representation of the 32 oscillating excitation field. We calculate complex excitation moments relative to the J2000 33 epoch and share the results as ASCII tables compatible with related software packages 34 intended for induction response calculations. 35

³⁶ Plain Language Summary

Planetary magnetic fields tell us much about a planet's interior, composition, and 37 history. Magnetic fields are also useful for remotely probing the interior of their moons, 38 especially for finding and characterizing potential subsurface oceans. Liquid-water oceans 39 within the solar system are ideal places to search for habitable environments beyond Earth. 40 Relating spacecraft magnetic measurements to the interior properties of the moons re-41 quires an understanding of various related components, including the manner in which 42 the magnetic field applied to the moon changes with time. We have developed an open-43 source software package called *PlanetMag* that uses published magnetic field models to 44 estimate the magnetic field at any point in time and space. It also has the ability to pre-45

cisely estimate the planetary field oscillations at the location of each large moon in the
solar system, which is needed for prediction of the magnetic field response from the moon.
Calculations of these magnetic oscillations are provided in text files compatible with ex-

⁴⁹ isting software.

50 1 Introduction

The giant planets—Jupiter, Saturn, Uranus, and Neptune—all have strong, inter-51 nally generated magnetic fields (Schubert & Soderlund, 2011). The intrinsic field of each 52 rotates with the planet. For this reason, they are believed to be generated deep in the 53 interior, by the action of a dynamo (Stanley & Glatzmaier, 2010)—fluid motion of elec-54 trically conductive materials in the rotating frame of the planet generate stable magnetic 55 fields. The magnetic fields of the planets demonstrate considerable variability. Proper-56 ties of the dynamo region are expected to be what dictates the structure of the intrin-57 sic field, which is represented by multipole magnetic moments. Multipole moments are 58 spherical harmonic coefficients used to describe the magnetic field outside the body. 59

In the reference frame of each moon orbiting these planets, the ambient magnetic 60 field oscillates with time, owing to non-zero eccentricity and inclination, the rotation of 61 the parent planet to which the magnetic moments are fixed, or both. These relative plan-62 etary motions typically give rise to magnetic field variations at the orbital period of the 63 moon and apparent rotation rate of the planet, respectively, due to positional differences 64 between the two bodies. Time-varying magnetic fields drive electrical currents within 65 conductive layers of the moons, thereby producing an induced magnetic field that is mea-66 surable outside the body. 67

Induced magnetic fields, properly isolated from other magnetic field contributions 68 such as the background planetary field, fields associated with magnetospheric plasma cur-69 rents, and spacecraft contaminate fields, can be used to detect and characterize subsur-70 face saltwater and magma oceans. Magnetic measurements can thus be used to constrain 71 the properties of subsurface oceans that affect the conductivity profile vs. depth, such 72 as the thickness of ice crust and ocean layers, salinity and temperature profiles, etc. In-73 deed, such measurements have offered the strongest evidence yet available for the pres-74 ence of a subsurface ocean within Europa (Kivelson et al., 2000), and have been used to 75

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76	place some constraints on the properties of its ocean and ice shell (Zimmer et al., 2000;
77	Hand & Chyba, 2007; Schilling et al., 2007).
78	Magnetic sounding investigation of moons is a multi-step process. Relating mag-
79	netic measurements from a spacecraft to constraints on interior structure requires all of
80	the following steps:
81	1. An estimate of the periodic oscillations in the applied field (the "excitation" field)
82	in the frame of the moon
83	2. Hypothesized electrical conductivity structure of the interior—the layer config-
84	uration and conductivity of each
85	3. A calculation of the induced magnetic field consistent with both (1) and (2)
86	4. Removal of the planetary magnetic field, transient fields from plasma currents, and
87	spacecraft fields from measurements
88	5. Statistical comparison of the induced magnetic field for each hypothesized inte-
89	rior structure (3) against measurements processed for background removal (4) .
90	This work focuses primarily on the first of these steps.
91	The time-varying excitation field is best represented using complex coefficients that
92	represent the amplitude and phase of the magnetic field vector components at the moon,
93	called the excitation moments \mathbf{B}^e (Styczinski et al., 2022). Excitation moments can be
94	retrieved from a magnetic field time series derived from a planetary field model evalu-
95	ated at the position of the moon. Spectral analysis (e.g., a Fourier transform) can be used
96	to determine the specific frequencies or periods of the oscillations, while conventional lin-
97	ear least-squares (LLS) methods are able to estimate the amplitude and phases of the
98	oscillations at different periods. There are numerous magnetic field models that are avail-
99	able in the literature, each developed by fitting a set of spherical harmonic coefficients
100	to magnetometer data acquired by various spacecraft. Past studies examining Europa
101	and Callisto (Kivelson et al., 1999) and Ganymede (Kivelson et al., 2002) have used sim-
102	plified approximations of the excitation moments, typically considering only a single vec-
103	tor component with the largest amplitude (usually associated with the synodic period,
104	the planet's apparent rotation rate in the frame of the moon). Past study of induction
105	at Io (Khurana et al., 2011) included full vectors and additional excitation periods, but

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the authors did not provide sufficient information to determine how the relative phases of each component and period were handled or which magnetic field model was applied.

The spectra of magnetic oscillations experienced by the moons of the giant plan-108 ets have been considered in past work. However, no prior studies have provided numer-109 ical results for both the amplitude and phase of the complex excitation moments that 110 are required to calculate the induced magnetic field. Cochrane et al. (2021) and Cochrane 111 et al. (2022) each performed a frequency decomposition of the excitation spectra for the 112 moons of Uranus and Neptune, respectively, using an LLS inversion (see Section 2.1) in 113 body-fixed frames defined by the International Astronomical Union (IAU), as in this work. 114 Arridge and Eggington (2021) used a similar LLS inversion in study of the uranian moons. 115 Biersteker et al. (2023) used an LLS inversion for Europa in the IAU frame as a test case, 116 but the excitation moments were not detailed. All other prior studies have evaluated the 117 amplitude of periodic oscillations using a Fast Fourier Transform (FFT) method, which 118 is incapable of accurately determining the amplitudes and phases of excitation moments 119 due to spectral leakage that results when one or multiple sinusoids are not perfectly pe-120 riodic within the FFT sampling time series. The excitation spectra of Jupiter's large moons 121 were evaluated in System III (1965) coordinates of the planet by Seufert et al. (2011) 122 and in IAU frames by Vance et al. (2021, excluding Io). Excitation spectra for the large 123 moons of Uranus were evaluated in System III coordinates by Arridge and Eggington 124 (2021) and in moon-centric frames close to, but not identical to, IAU frames by Weiss 125 et al. (2021). A detailed description of each coordinate system is contained in the sup-126 plemental material (Section S1). 127

In this work, we provide a means of calculating the complex excitation moments 128 for all major moons of the giant planets relative to the J2000 epoch via the open-source 129 framework *PlanetMag* and include ASCII tables of results for each moon (Styczinski & 130 Cochrane, 2024c). Magnetic field models for the internal and external contributions (e.g., 131 current sheets, magnetopause currents, etc.) are available in the literature, but the di-132 versity of employed coordinate systems, model formats, and software inconsistencies can 133 make evaluation of these models difficult and time consuming. Software for evaluation 134 of some models is available, but existing frameworks are limited in scope (Table 1). Plan-135 etMaq includes all peer-reviewed magnetospheric field models for all of the giant plan-136 ets in a common Matlab package, which can be evaluated at arbitrary locations and times. 137 Each model is validated against magnetic measurements from relevant spacecraft avail-138

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able from the Planetary Data System (PDS, see Table 4). Spacecraft, planet, and moon 139 positions and trajectories are precisely determined for any input time by integration with 140 the SPICE toolkit developed by the NASA Navigation and Ancillary Information Fa-141 cility (NAIF; Acton, 1996). The excitation moments are evaluated for each moon for a 142 selected model over an era relevant to a selected spacecraft. A limited duration pertain-143 ing to the residence time of a spacecraft must be selected because the orbital and rota-144 tional parameters of the planets and moons drift over time due to tidal forcing, and so 145 too must the excitation moments. 146

Our prior work has used excitation moments calculated from precursors to what 147 has now become *PlanetMag*: Vance et al. (2021); Styczinski et al. (2021); Cochrane et 148 al. (2021); Styczinski et al. (2022); Cochrane et al. (2022); Biersteker et al. (2023); Plat-149 there et al. (2023). Because of the variation in magnetic field that is expected over long 150 time periods (known as secular variation), for future missions that entail multiple moon 151 flybys such as Europa Clipper (Vance et al., 2023) and JUICE (Fletcher et al., 2023), 152 the excitation moments can be more accurately solved for directly from joint flyby mea-153 surements. However, for single-flyby mission concepts, where long periods cannot be mea-154 sured over the course of the mission, using excitation moments extracted from a mag-155 netic field model as described in this work is essential for magnetic investigation of icy 156 bodies (Cochrane et al., 2022). 157

Several open-source software libraries and frameworks are already available for the 158 evaluation of planetary field models for the outer planets, detailed in Table 1. Most avail-159 able models focus on a single planet. To our knowledge, Table 1 includes all currently 160 available open-source software packages for evaluation of giant planet magnetic fields as 161 of this writing. No available models include features for calculation of excitation moments 162 or integration with SPICE. Therefore, we created *PlanetMag* (Styczinski & Cochrane, 163 2024b) to offer these features within a single software package. The software is thoroughly 164 documented (documentation is available at https://coreyjcochrane.github.io/PlanetMag/) 165 and a Python port is in development. 166

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Package name	Planet	Language(s)	Archive reference	Publication
KS2005	Jupiter	IDL	N/A^{a}	Khurana and Schwarzl (2005)
KMAG2012	Saturn	Fortran	Khurana $(2020)^b$	N/A
$JupiterMag^{c}$	Jupiter	Python and $C++^d$	James et al. $(2024a)^e$	Wilson et al. (2023)
HSH	Jupiter	Python, Matlab, IDL	Wilson et al. $(2022)^f$	Wilson et al. (2023)
iturn-Mag-Model	Saturn	Python, Matlab, IDL	N/A^g	N/A
lanetMagFields	All planets	Python	Barik and Angappan (2024a) ^{h}	Barik and Angappan (2024b)
libinternal field	All planets	Python and $C++^d$	${ m N}/{ m A}^i$	N/A

Table 1. Open-source software packages currently available for evaluation of planetary magnetic field models. All packages focus on a single planet except *plan*- \mathbf{or} integration wi etMagFields

"https://github.com/NASA-Planetary-Science/Saturn-Mag-Model"

^ehttps://github.com/mattkjames7/JupiterMag

Available GitHub repositories:

fhttps://github.com/rjwilson-LASP/PSH

ⁱhttps://github.com/mattkjames7/libinternalfield

h https://github.com/AnkitBarik/planetMagFields

167 2 Methods

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For most moons, the magnetic field of the parent planet varies little on the spa-168 tial scale of the moon. As a result, it is customary to consider only the oscillations in 169 the mean field across each moon, approximated as that evaluated at the body center. 170 Notable exceptions are Io, with as much as a 58 nT difference, Europa with a 7.3 nT dif-171 ference, and Mimas with a 4.9 nT difference from the sub-planetary point to its antipode, 172 all of which we have calculated using the default models implemented in *PlanetMag* (Ta-173 bles 2 and 3). Periodic oscillations in the difference in the local magnetic field across the 174 body contribute excitation moments of degree 2 and higher, which will decay faster than 175 $1/r^3$ except in the case of highly asymmetric bodies (Styczinski et al., 2022). Magnetic 176 induction from excitations of degree 2 may be significant for sounding of Io, but calcu-177 lation of these moments is left for future work. 178

Excitation moments associated with the time-varying portion of the mean field are of spherical harmonic degree 1 and can be represented by complex vector components aligned to the axes of the desired coordinate system. The ambient field at the body center at time t can be represented with

 $\mathbf{B}_{\rm amb}(t) = \sum_{k} \mathbf{B}_{k}^{e} e^{-\mathrm{i}\omega_{k}t},\tag{1}$

where \mathbf{B}_{k}^{e} are the time-varying field vectors periodically oscillating at angular frequencies ω_{k} , including the static field at $\omega_{\mathrm{DC}} = 0$. The ambient field is complex in general the measurable field is evaluated by taking the real part of the complex total (Jackson, 1999).

To retrieve the excitation moments in the frame of the moon, we first determine 188 the location of the moon in the coordinates of the planetary field model using SPICE— 189 each required frame is defined in our custom frames kernel or built-in to the SPICE satel-190 lites kernels. Next, we evaluate the planetary magnetic field model (Tables 2 and 3) over 191 a period of time that spans the desired epoch with a number of sampling times N (by 192 default, $\mathcal{O}(10^6)$) and rotate this field vector into the desired frame of the moon using trans-193 formation functions implemented in SPICE. The excitation moments can then be extracted 194 from the resultant time series, $\mathbf{B}_i = \mathbf{B}_{\text{model}}(t_i)$. For rapid evaluation of the underly-195 ing models in *PlanetMag*, we have implemented a direct calculation of spherical harmon-196 ics and their derivatives in the Schmidt normalization up to degree 10. At distances of 197 the orbiting moons, the higher-degree harmonics have negligible contributions. We have 198

Table 2. Model combinations implemented in *PlanetMag* for Jupiter. The default model, under which we have calculated excitation moments for the major moons, is highlighted in **bold**. Parameters for each model are hard-coded, with spherical harmonic coefficients read from text files at run time. Analytical current sheet models for both C1981 and C2020 use the formulation of Connerney et al. (1981) with overall fit parameters listed in each publication.

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Model name	Description and references
VIP4+C1981	Voyager–Io flux tube footprint–Pioneer degree-4 model of
	Connerney et al. (1998) (more precisely reported by Connerney
	(2007)) along with the analytical current sheet model of
	Connerney et al. (1981).
O6+K	Degree-6 partial fit of Connerney (1992) to primarily Voyager 1 $$
	magnetic data, along with the current sheet model of Khurana
	(1997).
KS2005	Combined magnetosphere model of Khurana and Schwarzl
	(2005). Uses the VIP4 intrinsic field model, but with the dipole $% \left(2005\right) \left(1-2\right) \left(1-$
	moment rotated to match the O6 orientation, and a current
	sheet model constrained by crossings inferred from magnetic
	data of Galileo and all prior spacecraft to visit the planet.
JRM09+C2020	Juno Reference Model through 9 orbits, a degree-20 intrinsic
	field model (Connerney et al., 2018) and the analytical current
	sheet model of Connerney et al. (2020) , updated to pair with
	the JRM09 model. Both are fit to Juno data. Moments are
	well-resolved up to degree 10. For C2020, we use the overall fit
	parameters contained in Table 1 of Connerney et al. (2020) .
JRM09+C1981	JRM09 model with current sheet of Connerney et al. (1981).
	This is the model used by Vance et al. (2021).
VIP4+K	VIP4 model with current sheet of (Khurana, 1997). This is the
	model studied by Seufert et al. (2011).
JRM33+C2020	Degree-30 intrinsic field of Connerney et al. (2022) through
	Juno's first 33 orbits along with current sheet model of
	Connerney et al. (2020), also fit to Juno data. Moments up
	to degree 13 are well-resolved.

Table 3. Models implemented in *PlanetMag* for planets beyond Jupiter. Default models, under which we have calculated excitation moments for the major moons, are highlighted in **bold**. Parameters for each model are hard-coded, with spherical harmonic coefficients read from text files at run time. Analytical current sheet models for Cassini 11 use the formulation of Connerney et al. (1981) with overall fit parameters listed in Dougherty et al. (2018).

Model name	Planet	Description and references	
B2010	Saturn	Intrinsic field model of Burton et al. (2010) fit to Cassini mag-	
		netic data. Includes a degree-1 fit to an externally applied	
		field.	
Cassini 11	Saturn	Degree-12 (with only up to degree 11 well-resolved) intrinsic	
		field model of Dougherty et al. (2018) fit to Cassini magnetic	
		data, including from the Grand Finale orbits. Includes a cur-	
		rent sheet model.	
Cassini 11+	Saturn	Degree-14 intrinsic field model of Cao et al. (2020); similar to	
		Cassini 11 but with different regularization and using a subset	
		of Grand Finale orbits.	
Q3	Uranus	Quadrupole-resolved, degree-3 fit of Connerney (1987) to Voy-	
		ager 2 magnetic data. Includes a degree-1 fit to an externally	
		applied field.	
$\mathbf{AH5}$	Uranus	Auroral Hexadecapole $L = 5$ intrinsic field model of Herbert	
		(2009). Moments up to degree 4 fit to Voyager 2 magnetic data	
		and auroral observations. This is the model studied by Weiss	
		et al. (2021) and Cochrane et al. $(2021)^a$.	
08	Neptune	Degree-8 intrinsic field model of Connerney et al. (1992) fit	
		to Voyager 2 magnetic data. Moments above degree 3 are not	
		uniquely determined.	

^aAlso studied by Arridge and Eggington (2021) along with a magnetopause model.

also have begun to implement an evaluation of each available model of the magnetic fields
 from selected magnetopause current models, but these models are considered prelimi nary and have not been used in determining the excitation moments in this work.

Numerous coordinate systems have been considered in past magnetic sounding in-202 vestigations. In this work, we evaluate all excitation moments in the IAU frame of each 203 moon in Cartesian coordinates. This approach has several advantages. The IAU frames 204 are implemented in all SPICE kernels containing the moons, which enables simple con-205 version between coordinate systems and evaluation of spacecraft trajectories using func-206 tions built-in to SPICE. More importantly, IAU frames are fixed to the surface of the 207 body. Integration with SPICE in evaluating the excitation moments in the frame of the 208 body thus enables a proper accounting for all motional effects on the periodic compo-209 nents of the excitation field, including libration, apsidal precession, etc. These effects are 210 significant for some bodies, as in the case of Europa, where excitation at the true anomaly 211 period (TA; the time between periapsis crossings) differs from that at the orbital period 212 (the time between ascending node crossings), including in terms of the affected compo-213 nents (Table 5). IAU frames are the only ones considered in past work that have been 214 body-fixed frames. See Section S1 for a description of the IAU frames and others imple-215 mented in *PlanetMag*, including those used in past studies. 216

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2.1 Inversion of excitation moments

Using the magnetic field vector time series \mathbf{B}_i sampled at times t_i in the IAU frame of a moon, we perform a frequency decomposition of the excitation moments using an LLS optimization approach. The model magnetic field can be estimated as the real part of a superposition of sinusoids in terms of the excitation moments and their corresponding angular frequencies:

$$\mathbf{B}_{\text{model}}(t) \approx \text{Re}\{\mathbf{B}_{\text{amb}}(t)\} = \sum_{k} \left[\mathbf{B}_{k,\text{Re}}^{e}\cos(\omega_{k}t) + \mathbf{B}_{k,\text{Im}}^{e}\sin(\omega_{k}t)\right],\tag{2}$$

where $\mathbf{B}_{k}^{e} = \mathbf{B}_{k,\mathrm{Re}}^{e} + i\mathbf{B}_{k,\mathrm{Im}}^{e}$. These coefficients can be found by minimizing the sum of squared errors, i.e. $\sum_{i} (\mathbf{B}_{\mathrm{model}}(t_{i}) - \mathrm{Re}\{\mathbf{B}_{\mathrm{amb}}(t_{i})\})^{2}$. There are a total of 6F+3 coefficients for each inversion, where F is the number of frequencies used in the inversion. This includes 6 coefficients for every excitation frequency—the real and imaginary part for each vector component of the magnetic field vector—and 3 coefficients in the static background magnetic field vector. In the following, the index k refers specifically to the real or imaginary part of a frequency component. Given a list of expected excitation frequencies $\mathbf{f} = \{f_k\}$, the LLSoptimized coefficients for the excitation moments can be directly calculated using classical methods (for reference, see Markovsky & Van Huffel, 2007). The LLS inversion is calculated as follows. For $\omega_k = 2\pi f_k$, the columns of the design matrix X_{ik} are $\cos(\omega_k t_i)$ for the real part of each excitation moment and $\sin(\omega_k t_i)$ for the imaginary part. Each row in X_{ik} corresponds to a time t_i in the time series, i.e.

$$X_{ik} = \begin{bmatrix} \cos(\omega_1 t_1) & \sin(\omega_1 t_1) & \cos(\omega_2 t_1) & \sin(\omega_2 t_1) & \dots & \cos(\omega_F t_1) & \sin(\omega_F t_1) & 1 \\ \cos(\omega_1 t_2) & \sin(\omega_1 t_2) & \cos(\omega_2 t_2) & \sin(\omega_2 t_2) & \dots & \cos(\omega_F t_2) & \sin(\omega_F t_2) & 1 \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots & \vdots & \vdots \\ \cos(\omega_1 t_N) & \sin(\omega_1 t_N) & \cos(\omega_2 t_N) & \sin(\omega_2 t_N) & \dots & \cos(\omega_F t_N) & \sin(\omega_F t_N) & 1 \end{bmatrix}.$$
(3)

The same design matrix with 2F+1 columns is used for each vector component. The eigenvectors of X_{ik} are the columns of the weight matrix W, such that

$$W = \left(X_{ik}^T X_{ik}\right)^{-1} \tag{4}$$

$$B_{j,k}^e = (\mathbf{B}_i \cdot \hat{\mathbf{e}}_j) X_{ik} W, \tag{5}$$

where $B_{j,k}^e$ lists the real and imaginary parts of the excitation moment for vector component j and $\hat{\mathbf{e}}_j$ is a unit vector in the direction of component j. The product $X_{ik}W$ is commonly referred to as the pseudo-inverse. The results for $B_{j,k}^e$ from Equation 5 are those that minimize the sum of squared errors. The complex excitation moments for each frequency k are then constructed from

$$\mathbf{B}_{k}^{e} = \sum_{j} \left(B_{j,k,\mathrm{Re}}^{e} + \mathrm{i} B_{j,k,\mathrm{Im}}^{e} \right) \hat{\mathbf{e}}_{j} \tag{6}$$

²⁴⁸ and the LLS fit to the input time series can be evaluated with

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$$\mathbf{B}_{\text{amb}} = (\mathbf{B}_k^e)^T X_{ik}.$$
(7)

The list of excitation frequencies \mathbf{f} of the moments are identified from the natural spectrum of oscillations in an FFT of the time series \mathbf{B}_i . Each Fourier spectrum is rich in driving field oscillations, typically including the synodic period, the orbital period, and the harmonics and beats of these two fundamental periods. These frequencies are precisely calculated from information contained in cartographic reports (see Section S1.1 in the supplemental material) and retrieved from the SPICE planetary constants kernel.

The list **f** is refined iteratively in order to best reproduce the time series \mathbf{B}_i with 257 Equation 2 after inverting for the excitation moments. At each of the following steps, 258 we evaluate an FFT of the residuals, i.e. the difference between the input time series and 259 its reproduction using Equation 2. The process is continued until the residual spectrum 260 has no peaks over 1 nT, a commonly considered detection threshold, and minimal peaks 261 below this threshold, which essentially represent noise. An example residual FFT for the 262 magnetic field that Europa experiences, after completion of this process, is shown in Fig-263 ure 1. 264

We first find the excitation moments with just the known synodic period and side-265 real orbit period. Next, we add a wide array of beats and harmonics associated with these 266 excitation periods. The frequencies of remaining unknown peaks in the residual spec-267 trum are determined numerically using linear combinations of the leakage-spread points 268 in the spectrum near the peak, successively until the peak is precisely determined. Ex-269 amples of such peaks unrelated to beats and harmonics include true anomaly periods for 270 moons with marked apsidal precession, including Europa and Enceladus. After each such 271 peak is precisely determined, its harmonics and beats with other excitation periods are 272 added to \mathbf{f} . Finally, once all peaks in the residual spectrum are below $1 \, \mathrm{nT}$, frequencies 273 are removed from \mathbf{f} , starting with those associated with the lowest amplitudes in the LLS-274 inverted excitation moments, until as few amplitudes below 1 nT are included among the 275 moments and no peaks in the residual spectrum are over 1 nT. 276

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2.2 Model validation

To confirm the correct implementation of the many models we have included in *PlanetMag*, we compare each against spacecraft magnetic measurements gathered near the relevant planet. The datasets we compare are all available from the PDS. All data comparisons demonstrate close agreement with the evaluated model (Figure 2).

PlanetMag employs a direct calculation of spherical harmonics and their derivatives up to degree 10 in spherical coordinates in the Schmidt normalization for evaluation of intrinsic field models. In order to confirm that these calculations have been implemented correctly, we undertook a cross-comparison with the same calculations under different normalizations with *MoonMag* (Styczinski, 2023). *MoonMag* features the same calculations with complex, orthonormal spherical harmonics and with real-valued

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Figure 1. Fast Fourier Transform (FFT) of the residuals from inversion of the excitation spectrum for Europa, during the Juno era and with the JRM33+C2020 model as detailed in Table 2. The residuals are the differences for each evaluation time between a vector component of the model field and the reproduction generated with the inverted excitation moments, i.e. $\Delta \mathbf{B}_i = \mathbf{B}_{\text{model}}(t_i) - \text{Re}\{\mathbf{B}_{\text{amb}}(t_i)\}$. Several key excitation periods that are very stable over the input era exhibit a marked reduction in power in the residual spectrum, demonstrating that these excitation periods are well-represented by the inverted moments. Some other excitations, such as those at the true anomaly and orbital periods, do not show the same reduction despite being well-captured because these periods drift over time.



Figure 2. Comparison of Cassini 11+ model predictions and measurements from the Cassini spacecraft for the B_{θ} component (top) and differences for all components (bottom) in System III spherical coordinates during the year 2016. Each row shows the same data—on the left, the comparison is chronological, and on the right, the comparison is organized by distance from Saturn. Models implemented for the other giant planets show similar agreement with the compared measurements.

Table 4. Default combinations of planetary magnetic field models and data sources used for validation. Implemented models are described in Tables 2 and 3. In each case, we have used "survey" or "summary" data, which are averaged or decimated to provide lower-rate measurements that are more manageable for analyses over long time scales. We used Juno (1 s planetocentric) and high-resolution Galileo data only in validating model evaluation and calculation of the externally applied field from the excitation moments using Equation 7 against moon encounter data.

Planet	Default model	Spacecraft	PDS data volume
Jupiter	JRM33+C2020	Galileo, Juno	GO-J-MAG-3-RDR-MAGSPHERIC-
			SURVEY-V1.0 (Kivelson et al., 1997b),
			GO-J-MAG-3-RDR-HIGHRES-V1.0
			(Kivelson et al., 1997a), JNO-J-3-FGM-
			CAL-V1.0 (Connerney, 2022)
Saturn	Cassini 11 $+$	Cassini	CO-E/SW/J/S-MAG-4-SUMM-
			1 MINAVG-V2.1 (Dougherty et al., 2019)
Uranus	AH5	Voyager 2	VG2-U-MAG-4-SUMM-U1COORDS-
			48SEC-V1.0 (Ness, 1993)
Neptune	08	Voyager 2	VG2-N-MAG-4-SUMM-NLSCOORDS-
			12SEC-V1.0 (Ness, 1989)

Schmidt-normalized harmonics, both in Cartesian coordinates. We constructed a HEALpix map (Gorski et al., 2005) for evaluation under all 3 methods of calculating the magnetic field at the planet surface for each pure multipole moment (e.g., each combination of n, m, and $\sin m\phi$ or $\cos m\phi$) and compared the results, addressing any discrepancies until all methods produced the same results up to machine precision.

293 **3 Results**

The magnitude of the magnetic field for each of the giant planets evaluated with *PlanetMag* at the IAU-defined planetary radius is shown in Figure 3. *PlanetMag* is designed for evaluation of planetary field models at arbitrary locations and times in the middle magnetosphere for each planet, where the majority of the moons reside. Magnetodisk models and spherical-harmonic intrinsic field models break down at distances





on the scale of the magnetopause standoff distance (e.g., $\sim 50R_J$ for Jupiter) and lim-299 iting our evaluation to degree 10 for the intrinsic field means that regions within 1-2300 planetary radii of the 1 bar surface will not be modeled accurately due to the missing 301 higher-order moments. We have used the capabilities of our implementation with the de-302 fault models described in Tables 2 and 3, precise ephemerides from SPICE, and our LLS 303 inversion method to determine the excitation moments for all major moons in the outer 304 solar system. A subset of the excitation moments for Europa is detailed in Table 5. The 305 excitation field can be calculated at arbitrary times using Equation 2. For example, ig-306 noring the smaller excitations not included in Table 5, the instantaneous excitation field 307 at Europa $\mathbf{B}_{amb}(t)$ in the IAU frame is computed with 308

$$\mathbf{B}_{amb}(t) \approx \operatorname{Re}\{\mathbf{B}_{syn}^{e}\} \cos(\omega_{syn}t) + \operatorname{Im}\{\mathbf{B}_{syn}^{e}\} \sin(\omega_{syn}t) + \\
\operatorname{Re}\{\mathbf{B}_{synHarm}^{e}\} \cos(\omega_{synHarm}t) + \operatorname{Im}\{\mathbf{B}_{synHarm}^{e}\} \sin(\omega_{synHarm}t) + \\
\operatorname{Re}\{\mathbf{B}_{orb}^{e}\} \cos(\omega_{orb}t) + \operatorname{Im}\{\mathbf{B}_{orb}^{e}\} \sin(\omega_{orb}t) + \\
\operatorname{Re}\{\mathbf{B}_{TA}^{e}\} \cos(\omega_{TA}t) + \operatorname{Im}\{\mathbf{B}_{TA}^{e}\} \sin(\omega_{TA}t) + \\
\operatorname{Re}\{\mathbf{B}_{syn-TA}^{e}\} \cos(\omega_{syn-TA}t) + \operatorname{Im}\{\mathbf{B}_{syn-TA}^{e}\} \sin(\omega_{syn-TA}t),$$
(8)

where t is in TDB seconds relative to J2000 (also called ephemeris time ET in SPICE), $\omega_k = 2\pi/T_k$ with T_k in s, and \mathbf{B}_k^e are the complex excitation moment vectors listed in Table 5. The full set of excitation moments we have calculated using default models is compiled into ASCII data tables (Styczinski & Cochrane, 2024c).

309

Hodograms showing a planar projection of the path traced by the magnetic field 314 vector in a selected plane are shown in Figure 4. Lines in these diagrams appear thick 315 or smeared due to superposition of multiple excitations, each contributing vectors of vary-316 ing amplitudes and phases. The hodograms have been constructed from the same data 317 as those used to calculate the excitation moments—a time series of the default model 318 for each planet at the location of each moon for approximately 10⁶ equally-spaced time 319 steps spanning a particular era. We chose the Juno era for Io, Europa, and Ganymede 320 due to relevance for analyzing Juno flyby data from each moon, and the Galileo era for 321 Callisto. We used the VIP4+K model to calculate the excitation moments for Callisto 322 instead of the default in Table 2. This is because the planar models of Connerney et al. 323 (1981) and Connerney et al. (2020) do not capture the bendback of the current sheet, 324 which contributes significantly to the field at Callisto's relatively large orbital distance 325 (about $26.3R_J$), as compared to hinged current sheet models such as Khurana (1997) 326

Table 5. Example excitation moments for the 5 strongest oscillations at Europa over the Juno era, relative to the J2000 epoch. These moments were evaluated with the JRM33 intrinsic field model (Connerney et al., 2022) and the analytical current sheet model of Connerney et al. (2020). No magnetopause currents were modeled in calculating these values. A full list of excitation moments for all large moons of the giant planets and for all implemented models and spacecraft eras is available as a Zenodo archive (Styczinski & Cochrane, 2024c).

Excitation name	Period (h)	Excitation moment vector (IAU frame, nT)
Synodic	11.23	$(131.4 - 173.1i)\hat{x} + (-65.5 - 35.4i)\hat{y} + (-4.8 - 15.2i)\hat{z}$
Synodic harmonic	5.62	$(16.8 + 4.7i)\hat{x} + (2.9 - 11.3i)\hat{y} + (1.3 + 1.6i)\hat{z}$
Orbital	85.2	$(-7.4 + 7.7\mathrm{i})\hat{x} + (-2.3 - 2.7\mathrm{i})\hat{y} + 0.5\mathrm{i}\hat{z}$
True anomaly (TA)	84.6	$(-0.5 - 0.1)\mathbf{i}\hat{x} - 0.2\hat{y} + (8.6 - 5.9\mathbf{i})\hat{z}$
Synodic–TA beat	12.95	$(4.6 + 2.3i)\hat{x} + (1.6 - 3.4i)\hat{y} + (0.4 - 0.2i)\hat{z}$

(Khurana & Schwarzl, 2005). For the moons of Saturn, we used the Cassini era because
of the wealth of data available from that mission. For moons of Uranus and Neptune,
we used the Voyager era, a 6-month period centered on the Voyager 2 flyby of each planet
from which in situ data were gathered.

The excitation moments shift over time and will yield different results when calculated with different planetary field models. All magnetic field models implemented in *PlanetMag* can be used to calculate excitation moments over any duration supported by the loaded SPICE kernels.

335

4 Discussion and conclusions

The planetary magnetic field models in *PlanetMag* show favorable comparison to 336 the spacecraft measurements from which the models were derived (e.g., Figure 2), which 337 implies they have been correctly implemented. Spurious signals from disturbances in the 338 surrounding plasma environment, which are not captured in planetary field models, will 339 not affect the long-term periodicity of the excitation field, and so will not affect the ex-340 citation moments. However, periodic motion or variance in the plasma around each moon, 341 oscillating at the same key periods, especially that driven by the same excitations as those 342 we calculate in this work, will affect the excitation moments. Accounting for such effects 343



Figure 4. Hodograms for large moons in the outer solar system. The represented data are those used to calculate the excitation moments (Styczinski & Cochrane, 2024c), i.e. the default models in Tables 2 and 3, except for Callisto, for which we have used VIP4+K. Each diagram shows the path traced by the tip of the magnetic field vector projected into the IAU xy (equatorial) plane in nT, except for the moons of Saturn which show the IAU xz plane. All panels have an equal aspect ratio, showing an equivalent range along both axes.

is beyond the scope of this work. The principle of superposition dictates that the contributions from plasma can be summed independently from those of the excitation field from the broader magnetosphere, but the contributions from plasma that react to the same excitations will tend to decrease the driving field and thus change the net timevarying field in the frame of the moon.

The effects of periodic variance in the plasma environment have never been self-349 consistently modeled along with the excitation field in magnetic sounding investigations, 350 although Schilling et al. (2007) modeled how the variance in Europa's plasma environ-351 ment may affect inferences of its interior structure. Future work, including analysis of 352 measurements from the Europa Clipper mission, must account for periodicity in the plasma 353 environment to most accurately estimate the excitation moments applied to the moon. 354 Plasma motion may also contribute its own excitations at periods not matching those 355 from the planetary field (e.g., Schilling et al., 2008; Blöcker et al., 2016; Harris et al., 2021), 356 which could confound efforts to isolate the induced magnetic field. 357

Magnetic fields in the frame of each moon are not constructed of perfectly sinu-358 solidal contributions, so the excitation moments can never perfectly reproduce the input 359 time series. The excitation frequencies \mathbf{f} are not constant over time, because tidal per-360 turbations from mutual gravity and the dissipation of energy inside each body change 361 their orbital elements and rotational properties over time. Many such effects are con-362 sidered in the development of IAU frames and in trajectory calculations with SPICE. 363 However, while accounting for these drifts in motional parameters promotes a more com-364 plete description of excitation moments, as in the case of the TA period at Europa, it 365 also adds a small amount of noise to the excitation spectrum. This is why the orbital 366 and TA periods do not show the same dramatic reduction in represented power as the 367 shorter-period, more stable excitations in the residual spectrum for Europa (Figure 1). 368

As currently implemented in *PlanetMag*, the list of excitation frequencies **f** used to define the design matrix X_{ik} is specified manually using the procedure detailed in Section 2.1. The list **f** is hard-coded for each moon and calculated at run time from parameters in the SPICE planetary constants kernel and some manually determined excitation periods. An algorithmic method of determining the signal components, as is typical with the related method of Independent Components Analysis (Hyärinen & Oja, 2000; Hyvärinen, 2013), would have advantages and disadvantages. Removing the need for ap-

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plying judgement or an arbitrary cutoff in acceptable residual power would improve the reproducibility of the determined excitation periods. However, drift in orbital and rotational parameters over time suggests that prioritizing expected oscillation periods may result in excitation moments that are of greater explanatory value in magnetic sounding investigations, and may be more accurate when extrapolated beyond the calculated time series era.

Calculation of spherical harmonics and their derivatives for intrinsic field models 382 is limited in *PlanetMag* to degree 10. We have written bespoke functions for this pur-383 pose, which speeds up calculations dramatically because of the recursion relations used 384 to evaluate arbitrary spherical harmonics, and the more complicated solutions that are 385 required for their derivatives, both of which are required to calculate magnetic fields from 386 multipole moments. We evaluated the harmonics and their derivatives with Mathemat-387 ica for all spherical harmonic calculations implemented in *PlanetMag* and *MoonMag*. Tran-388 scribing these to machine-readable calculations and validating the result was a tedious 389 process. Although future versions may include calculations to greater than degree 10, 390 the induced fields at the locations of the large moons are primarily dominated by mul-391 tipole moments of octupole order and below. Current sheet models typically have a large 392 influence on the field experienced by each moon, and at their orbital distances typically 393 the dipole moment is the only significant multipole moment. Therefore, we caution users 394 of the software about its use in regions near the planet, where the unmodeled high-degree 395 moments will have the greatest effect, and very far from the planet, where current sheet 396 models are less accurate, but we consider the current implementation well-suited for ap-397 plication near the moons. 398

PlanetMag is the first open-source package to feature the calculation of the exci-399 tation moments \mathbf{B}^{e} critical for magnetic sounding investigations. It is also the first soft-400 ware supporting the evaluation of magnetic field models across the outer solar system 401 with SPICE integration, which extends its utility far beyond our intended development 402 purpose, which is the precise calculation of \mathbf{B}^{e} . Complex excitation moments determined 403 with as much attention to the well-known orbital and rotational parameters of the plan-404 ets and moons as we have included enable time-dependent comparisons to spacecraft data 405 of planetary and induced fields with unprecedented accuracy. We make this software and 406 data available so that they may be used to improve current estimates and future anal-407 yses of spacecraft magnetic data. 408

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409 Open Research

Data used in this work were generated using the open-source *PlanetMag* software 410 hosted on GitHub (https://github.com/coreyjcochrane/PlanetMag). A Zenodo archive 411 of the most recent version is available at https://doi.org/10.5281/zenodo.10554762 412 (Styczinski & Cochrane, 2024a). PlanetMag is released under an Apache-2.0 license. The 413 v1.0.2 release associated with this manuscript is archived at https://doi.org/10.5281/ 414 zenodo.10864719 (Styczinski & Cochrane, 2024b). A Zenodo archive of the output data 415 for excitation moments of the major moons with the default planetary field models (Ta-416 bles 2 and 3) is available at https://doi.org/10.5281/zenodo.10864716 (Styczinski 417 & Cochrane, 2024c). This work uses products from the NASA Planetary Data System 418 from several volumes: VG2-U-MAG-4-SUMM-U1COORDS-48SEC-V1.0 (Ness, 1993), 419 VG2-N-MAG-4-SUMM-NLSCOORDS-12SEC-V1.0 (Ness, 1989), GO-J-MAG-3-RDR-420 MAGSPHERIC-SURVEY-V1.0 (Kivelson et al., 1997b), GO-J-MAG-3-RDR-HIGHRES-421 V1.0 (Kivelson et al., 1997a), CO-E/SW/J/S-MAG-4-SUMM-1MINAVG-V2.1 (Dougherty) 422 et al., 2019), and JNO-J-3-FGM-CAL-V1.0 (Connerney, 2022). 423

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Supporting information for "*PlanetMag:* Software for evaluation of outer planet magnetic fields and corresponding excitations at their moons"

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- 9 Introduction

¹⁰ This supplement contains a detailed description of the frames implemented in *PlanetMag* and definitions of ¹¹ their associated coordinate systems.

S1. Frames and coordinate systems

Below, we describe the IAU frames and those considered in past work for comparison. All frames described 12 here are implemented in *PlanetMaq* via a custom frames kernel for use with SPICE. Past studies have typically 13 used $\phi\Omega$ coordinate systems (e.g., Zimmer et al., 2000) or spherical coordinates in the System III frame (SPRH) 14 of the parent planet (Seufert et al., 2011; Arridge & Eggington, 2021) for evaluating the excitation moments. 15 Although $\phi\Omega$ and SPRH coordinate systems are preferable for modeling and analysis of magnetospheric plasmas, 16 neither is fixed to the surface of the moon. Because all large moons in our solar system rotate synchronously, 17 the IAU axes can be approximated by one or more 90° rotations from SPRH or $\phi\Omega$ coordinates. However, the 18 exact rotations vary throughout the orbital and true anomaly periods by up to several degrees, which introduces 19 artifacts to the excitation spectrum. 20

In every case where a direction is specified from one body to another, or reference is made to a body's center, the center of mass is implied for each.

S1.1. IAU, System III, and SPRH frames

Parameterizations for IAU frames are adopted by resolution at an IAU General Assembly and described in 23 reports of the IAU Working Group on Cartographic Coordinates and Rotational Elements, which we call the 24 CCWG. IAU frames are defined for all major planetary objects in the solar system and are body-fixed and 25 planetocentric, with the origin at the body center. In these frames, which are built-in to SPICE, the \hat{z} axis is 26 always directed along the rotation axis of the body, on the north side of the invariable plane—defined by the net 27 angular momentum vector of the entire solar system. The northward normal of the invariable plane defines the 28 \hat{z} direction for International Celestial Reference System (ICRF), an inertial frame used in evaluating planetary 29 ephemerides (the ICRF \hat{x} direction is through the Earth equator at the vernal equinox at J2000). 30

For all planets and large moons except those in the Uranus system and Triton (which orbits Neptune in a 31 retrograde direction), the IAU \hat{z} axis is directed along the angular momentum vector of the body relative to 32 its parent. For the Uranus system and Triton, \hat{z} is in the opposite direction. The \hat{x} direction is orthogonal to 33 \hat{z} , directed from the body center toward the plane containing an arbitrary feature used to define the 0° (prime 34 meridian) longitude for the body. For all moons, this is a feature intended to direct \hat{x} approximately toward 35 the parent planet. For all planets, this is a feature intended to face a particular direction at a particular epoch 36 (Section S1.1.1). The \hat{y} direction completes a right-handed coordinate system, approximately along the orbital 37 velocity vector relative to the parent planet for the uranian moons and Triton and opposite the orbital velocity 38 vector for all other large moons. The IAU x axis tracks the 0° longitude feature, and so moves with the surface 39 of the body. 40

For the giant planets, which generally lack stable surface features, the IAU frame typically rotates at the same rate as the System III frame (Archinal et al., 2018a), which is defined by periodicity in the magnetic field of the planet or features tied to the magnetic field. These features are believed to be fixed to the motion of the deep intrain of the planet. The System III former hear the $\hat{\alpha}$ direction planet by periodicity in the magnetic field of the deep

interior of the planet. The System III frame always has the \hat{z} direction along the angular momentum vector of the

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planet and 0° longitude along the direction of the IAU prime meridian. SPRH, a coordinate system sometimes
 used in spacecraft data analysis, is a spherical representation of the System III frame.

For Jupiter and Saturn, the IAU and System III frames are identical. For Uranus, the IAU frame has \hat{y} and 47 reversed from the System III frame. For Neptune, the IAU frame was changed in the 2015 CCWG Report \hat{z} 48 (Archinal et al., 2018b) to be a System II frame, which rotates along with stable atmospheric features. This 49 definition has not yet been implemented in SPICE as of planetary constants kernel (PCK) pck00010.tpc and 50 the IAU frame is not used for Neptune in *PlanetMag*. The latest PCK available, pck00011.tpc, implements 51 this System II frame for Neptune, which differs from that used to derive the available magnetic field models for 52 Neptune. We continue to use pck00010.tpc in *PlanetMag* for this reason. A more detailed description of the 53 54 definitions of the IAU frames for the giant planets follows.

55 S1.1.1. IAU frame definitions for the giant planets

Jupiter — System III (1965): This frame is described well by P. Seidelmann and Divine (1977), and was 56 adopted by the CCWG by the time of their first report (Davies et al., 1980). The rotation rate was selected based 57 on many years of radio observations. It was revised in the 2000 report (P. K. Seidelmann et al., 2002) to be more 58 precise based on recent work, but reverted in the 2009 report (Archinal et al., 2011) due to subsequent challenges 59 raised against the updated rotation rate. The prime meridian is defined such that System III (1957.0) longitudes, 60 which used a slightly different rotation period, coincide with System II longitudes at the 1957.0 epoch. However, 61 a mistake in evaluating System II at 1957-01-01 00:00:00.000 UTC instead of the same time TDB (Coordinated 62 Universal Time vs. Barycentric Dynamical Time, a difference of about $41.2 \,\mathrm{s}$) in calculating the observed central 63 meridian longitude means the agreement is only approximate. Jupiter System II revolves with the mid-latitude 64 atmospheric rotation rate (Dessler, 2002). Ultimately, the System III prime meridian is arbitrary and since the 65 frame has seen widespread adoption in magnetic modeling, it is sufficient to use the J2000 definition as a reference. 66 67 **Saturn** — **System III:** This frame was defined by Desch and Kaiser (1981) as the Saturn Longitude System (SLS) and was adopted by the CCWG in the 1982 report (Davies et al., 1983), with the planetary rotation 68 period revised in a private communication from M. L. Kaiser to M. E. Davies. Also referred to as L1 in Voyager 69 1/2 data hosted on the Planetary Data System (PDS). The prime meridian is selected to coincide with the 70 Saturn ascending node of the planet's orbit on its equator at the 1980.0 epoch, 1980-01-01 00:00:00.000 UTC. 71 The 1982 report (Davies et al., 1983) contains expressions for the prime meridian location relative to the J2000 72 epoch, which remain unchanged in the latest CCWG report (Archinal et al., 2018a). Axisymmetry of the Saturn 73 magnetic moments (no moments are even reported for $m \neq 0$ in the literature) mean that the prime meridian 74 definition does not impact modeling of the internal field, but the same is not true of the external current systems 75 (Andrews et al., 2019). Subsequent research has resulted in alternative systems, namely SLS2 (Kurth et al., 76 2007) and SLS3 (Kurth et al., 2008). These systems vary the rotation rate to maintain an observed peak in radio 77 intensities at 100° subsolar longitude. The varying rotation rate implies that these coordinate systems may not 78 rotate with the deep interior of the planet, and the SLS system remains that preferred by the CCWG. 79

Uranus — **System III:** The first CCWG report defined the prime meridians of Saturn, Uranus, and Neptune 80 to coincide with the ICRF x axis (direction of Earth vernal equinox from the solar system barycenter) at the 81 J1950 epoch, 1950-01-01 00:00:00 TDB. Uranus is the only planet that still retains this definition in the latest 82 report (Archinal et al., 2018a). The rotation rate was updated in the 1985 report (Davies et al., 1986) based 83 on preliminary analysis from Voyager 2, with the prime meridian being briefly (and perhaps accidentally) set to 84 the ICRF x direction at J2000 for this report only. The rotation rate, based on Desch, Connerney, and Kaiser 85 (1986), has not been updated since the 1986 report. The z axis for the IAU frame is opposite to the rotation 86 direction, because the angular momentum vector is greater than 90° away from the z axis of the ICRF frame, and 87 IAU convention stipulates this condition. This frame is not typically used in analysis of magnetic data, primarily 88 because of the ubiquity of spherical coordinates with the polar axis aligned to the angular momentum vector, in 89 opposition to the IAU definition. 90

Neptune — **System II:** Following the Voyager 2 flyby of Neptune, a radio-derived rotation period based 91 on Warwick et al. (1989) was adopted by the IAU. The 1950.0 ICRF x axis definition for the prime meridian 92 was retained until the current System II definition was adopted in the 2015 report (Archinal et al., 2018b) based 93 on observations of remarkably stable cloud features reported by Karkoschka (2011). The System II definition 94 uses the rotation period inferred from the South Polar Feature and South Polar Wave identified by Karkoschka 95 (2011), and the prime meridian is located at the average of the longitudes of both features. This meridian is 96 stated to coincide with the System III (1950.0) meridian at 1989-08-03 12:00:00 UTC. The System II frame is not 97 yet implemented in the latest recommended version of the SPICE planetary constants kernel, pck00010.tpc. 98

S1.2. Frames for planetary field models

Each intrinsic field model implemented in *PlanetMag* is evaluated using the coordinates specified in the peerreviewed publication that describes the model. Generally, these coordinates match those in which the available spacecraft measurements are reported for the planet. Current sheet models often use unique coordinate systems, but these are referenced to the same standard systems. All models for a particular planet use a single coordinate system, as follows.

Jupiter: System III (1965), implemented as the IAU_JUPITER frame in SPICE.

Saturn: Saturn Longitude System (SLS), also known as S1, implemented as the IAU_SATURN frame in SPICE. 105 **Uranus:** Uranus Longitude System (ULS), also known as U1, as defined by Ness et al. (1986) and named by 106 Herbert (2009). \hat{z} is aligned with the planet's angular momentum vector, the prime meridian is arbitrarily defined 107 108 using the Voyager 2 trajectory, and the frame rotates along with the intrinsic magnetic moments. This frame is obtained by inverting the z axis of the IAU_URANUS frame and rotating to set the Voyager 2 position at 1986-01-24 109 18:00:00, about 1 s from closest approach (CA), to be 302°W in the ULS frame. From the most up-to-date SPICE 110 kernel reconstructing the Voyager 2 trajectory, vgr2.ura111.bsp, and the pck00010.tpc planetary constants 111 kernel, the IAU longitude of the spacecraft at this time was about 225.3°E. The ULS frame is a constant offset 112 from the IAU frame and thus rotates with the IAU frame. The Voyager 2 magnetic measurements and trajectory 113 from the Uranus flyby are reported in ULS coordinates. 114

Neptune: Neptune Longitude System (NLS), as defined by Connerney, Acuña, and Ness (1992). \hat{z} is aligned 115 with the planet's angular momentum vector, defined by Connerney et al. (1992) to have right ascension $\alpha_0 =$ 116 298.90° and declination $\delta_0 = 42.84^\circ$, which we assume to be in reference to the ICRF frame at J2000. The prime 117 meridian orientation is defined using 167.7°W at 0356 spacecraft event time (SCET, equivalent to UTC in this 118 case) on day-of-year 237 (August 25) of the year 1989. The Voyager 2 trajectory determined from the latest 119 SPICE kernels (vg2_nep097.bsp) in this frame does not match the data reported in PDS (volume VG2-N-MAG-120 4-SUMM-NLSCOORDS-12SEC-V1.0). We have implemented the frame defined by Connerney et al. (1992) as 121 NLS_RADEC and a second frame, NLS, that is equivalent to the IAU_NEPTUNE frame implemented in SPICE based on 122 the 2009 CCWG report (Archinal et al., 2011) but rotated to place Voyager 2 at a planetocentric west longitude of 123 167.7°, a rotation of 12.0140°. The NLS frame much more closely approximates the Voyager 2 trajectory detailed 124 in this frame along with the magnetic data on PDS, but some systematic offset is still present from an unknown 125 source. See Figure S1 for a comparison of the NLS trajectory against that reported in the PDS data. 126

S1.3. Frames for magnetic investigation of moons

Past investigations have primarily used $\phi\Omega$ frames. These frames are common in analysis of plasma flow and 127 moon-plasma interactions because the axes rotate along with the moon as it orbits and the xy plane is coplanar 128 with that of the planet's System III frame, related by a rotation about \hat{z} . In $\phi\Omega$ frames, the \hat{z} direction is aligned 129 to the parent planet's spin angular momentum vector, $\hat{x} = -\hat{r} \times \hat{z}$, where \hat{r} is the direction from the parent planet 130 to the moon, and \hat{y} completes the right-handed set. \hat{y} is approximately toward the parent planet, \hat{x} is in the 131 corotation direction—approximately along the orbital velocity vector, and \hat{z} is approximately along the moon's 132 angular momentum vector in the case of natural moons that orbit near the planet's spin equator. Because each 133 moon's orbit is elliptical, the axes rotate in a non-uniform fashion, faster near periapsis and slower near apoapsis. 134 A comparison between the IAU frame, which is fixed to the body surface, and the $\phi\Omega$ frame for Europa, $E\phi\Omega$, is 135 shown in Figure S2. In *PlanetMag*, we have implemented $\phi \Omega$ frames only for the moons of Jupiter, to facilitate 136 comparison to past studies. These frames are available in *PlanetMag* as IO_PHI_O, EUROPA_PHI_O, etc. Note also 137 that the above descriptions of these frames may vary for retrograde orbits, as in the case of Triton. 138

S1.4. Additional frames for evaluation of models in the literature

For convenience and comparison to prior work, we have also implemented the following frames, all of which are centered on the planet:

Planet-Sun-Orbit: \hat{x} is directed toward the Sun. \hat{y} is directed along the component of the Sun's instantaneous inertial velocity vector, as seen from the planet, that is normal to \hat{x} , and \hat{z} completes the right-handed set. Available in *PlanetMag* as JSO, KSO, USO, and NSO for Jupiter, Saturn, Uranus, and Neptune, respectively.

Planet–Sun–Magnetic: \hat{x} is directed toward the Sun. \hat{y} is along $\mathbf{M} \times \hat{x}$, where \mathbf{M} is the instantaneous 144 magnetic dipole moment vector. \hat{z} completes the right-handed set. A model must be selected for the orientation 145 of the dipole moment. These frames are available in *PlanetMaq* with the following model dipole orientations: 146 JSM — O4 (Acuña & Ness, 1976), used in magnetosphere shape calculations in KS2005 model (Khurana & 147 Schwarzl, 2005); KSM — Cassini 11 (Dougherty et al., 2018); USM — Offset, tilted dipole (OTD) (Ness et al., 148 1986), used in magnetopause field calculations of Arridge and Eggington (2021); NSM — O8 (Connerney et 149 al., 1992). Originally defined by Acuña and Ness (1976) and given this name in Bagenal and Wilson (2016, 150 https://lasp.colorado.edu/home/mop/files/2015/02/CoOrd_systems12.pdf). 151



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Figure S1. Comparison of the Voyager 2 trajectory in the NLS frame as reported in PDS data (volume VG2-N-MAG-4-SUMM-NLSCOORDS-12SEC-V1.0) vs. our implementation of the frame using the latest reconstruction using SPICE kernels.



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Figure S2. Angle between \hat{x} for the IAU frame for Europa and the $E\phi\Omega$ coordinate system commonly used in past magnetic sounding investigations throughout the first 2 orbital periods following the J2000 epoch. The IAU frame is fixed to the body surface; the $E\phi\Omega$ axes vary throughout Europa's orbital period as it librates.

Planet–Dipole–Solar–Zenith: \hat{z} is directed toward the Sun. \hat{y} is along $\hat{\mathbf{M}} \times \hat{z}$, where $\hat{\mathbf{M}}$ is along the dipole moment vector and the same models are selected as in the Planet–Sun–Magnetic frames. \hat{x} completes the right-handed set, approximately antiparallel to $\hat{\mathbf{M}}$. Available in *PlanetMag* as JDSZ, KDSZ, UDSZ, and NDSZ. This frame is described in application to Jupiter by Alexeev and Belenkaya (2005), but not named therein. Used in Arridge and Eggington (2021) magnetopause model based on shape defined by Shue et al. (1997), for which this frame makes evaluation simple.

Solar-Magnetic-Planet: \hat{z} is along \hat{M} as defined in the models selected for the Planet-Sun-Magnetic frames. \hat{y} is along $\hat{r}_{Sun} \times \hat{z}$, where \hat{r}_{Sun} is directed toward the Sun. \hat{x} completes the right-handed set. The xyplane of this frame is the magnetic dipole equator, and $\phi = 0$ in spherical coordinates in this frame coincides with the sub-solar longitude. Available in *PlanetMag* as SMJ, SMK, SMU, and SMN.

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