The Influence of Large-Scale Spatial Warming on Jet Stream Extreme Waviness on an Aquaplanet

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Abstract

The effect of modified equator-to-pole temperature gradients on the jet stream by low-level polar warming and upper-level tropical warming on jet streams is not fully understood. We perform four aquaplanet simulations to quantify the impact of different sea surface temperature distributions on jet stream strength, wave amplitudes and jet stream waviness, quantified by a modified Sinuosity Index. A large-scale uniform warming scenario increases the jet strength whereas decreases in jet strength occur in two scenarios where the meridional temperature gradient is reduced. However, all scenarios indicate substantial decreases in the magnitude of large wave amplitudes, jet stream extreme waviness and reduced variability of these diagnostics, suggesting a relationship with weakened baroclinicity. Our findings contradict the earlier proposed mechanism that low-level polar warming weakens the jet stream and increases wave amplitudes and jet stream waviness. We conclude that a weaker jet stream does not necessarily become wavier.

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9 Key Points:

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10	•	Weakened jet streams do not become wavier on an aquaplanet with reduced tem-
11		perature gradients due to warming in mid- and high latitudes
12	•	The magnitude of large wave amplitudes and jet stream extreme waviness decrease
13		robustly under large-scale spatial warming on an aquaplanet

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14 Abstract

The effect of modified equator-to-pole temperature gradients on the jet stream by low-15 level polar warming and upper-level tropical warming on jet streams is not fully under-16 stood. We perform four aquaplanet simulations to quantify the impact of different sea 17 surface temperature distributions on jet stream strength, wave amplitudes and jet stream 18 waviness, quantified by a modified Sinuosity Index. A large-scale uniform warming sce-19 nario increases the jet strength whereas decreases in jet strength occur in two scenar-20 ios where the meridional temperature gradient is reduced. However, all scenarios indi-21 cate substantial decreases in the magnitude of large wave amplitudes, jet stream extreme 22 waviness and reduced variability of these diagnostics, suggesting a relationship with weak-23 ened baroclinicity. Our findings contradict the earlier proposed mechanism that low-level 24 polar warming weakens the jet stream and increases wave amplitudes and jet stream wavi-25 ness. We conclude that a weaker jet stream does not necessarily become wavier. 26

27 Plain Language Summary

This research letter considers how different patterns of atmospheric warming, like 28 low-level warming at the poles and at high altitude in the tropics, impact the jet stream, 29 which is a strong 'river' of high-altitude wind. We use numerical model simulations to 30 mimic different scenarios of warming that maintain or reduce the temperature gradient 31 between equator and poles. We find that when an Earth-like planet completely covered 32 by water warms in specific ways, it strengthens or weakens the jet stream, but reduces 33 the size of its largest waves, and makes the extreme waviness episodes less wavy. We ex-34 plain that this is possibly related to the reduced energy available to grow weather sys-35 tems. Furthermore, this research letter conclude that weakened jet streams do not nec-36 essarily become wavier, which is against the idea that weakened jet streams become wavier 37 due to warming in polar regions. 38

³⁹ 1 Introduction

Key characteristics of anthropogenic global warming are polar amplification and
upper tropospheric tropical warming (e.g., IPCC, 2021; Gulev et al., 2021; Lee et al., 2021;
Doblas-Reyes et al., 2021). These large-scale spatial warming phenomena alter the equatorto-pole temperature gradient in the lower and upper troposphere, which, in turn, initiates the "meridional tug-of-war on the jet stream" (Barnes & Screen, 2015; Shaw et al.,
2016; Stendel et al., 2021).

The impact of the altered meridional temperature gradients on the jet stream re-46 mains a subject of ongoing research (e.g., Coumou et al., 2018; Vavrus, 2018; Cohen et 47 al., 2020). Recently, Woollings et al. (2023) found that the observed weak poleward jet 48 shift could be potentially linked to upper tropospheric tropical warming. However, most 49 studies focus on the influence of amplified Arctic warming on the jet stream and several 50 hypotheses have been put forward (see e.g., Cross-Chapter Box 10.1 Doblas-Reyes et al., 51 2021). For instance, Francis and Vavrus (2012, 2015) hypothesized that a weaker jet stream, 52 caused by polar amplification, would become more wavy, potentially leading to more fre-53 quent weather extremes. This hypothesis is that a wavy jet stream is associated with 54 atmospheric blocking and Rossby wave breaking, which are known to be related to mid-55 latitude weather extremes (Woollings et al., 2018). While this hypothesis has generated 56 much discussion over the past decade, it has yet to be conclusively confirmed or refuted 57 (e.g., Barnes, 2013; Barnes & Screen, 2015; Cohen et al., 2020). 58

Most studies about projected waviness changes with comprehensive climate mod-59 els indicate a decrease in waviness (Barnes & Polvani, 2015; Cattiaux et al., 2016; Pe-60 ings et al., 2017) but with a large intermodel spread. To disentangle processes in highly 61 nonlinear climate models, numerous studies have attempted to replicate Arctic ampli-62 fication through prescribed sea-ice loss in climate models and test the influence on cir-63 culation (Screen et al., 2018; Smith et al., 2019). However, the findings of these stud-64 ies are still inconclusive, confirming the link (Mori et al., 2019), noting no clear differ-65 ences in waviness (e.g., Ogawa et al., 2018; Blackport & Screen, 2020) or showing weak 66 responses to sea-ice loss (Smith et al., 2022). To even further reduce complexity in the 67 search of causality, highly idealized modeling studies have investigated the impact of changes 68 in the meridional temperature gradient alone. However, they have focused on migration 69 of the storm track (Butler et al., 2010), on the effect of blocking (Hassanzadeh et al., 2014) 70 and temperature variability (Schneider et al., 2015) rather than on waviness changes. Schemm 71 and Röthlisberger (2024) do study jet stream waviness changes, however only under uni-72 form warming. 73

This research letter focuses on changes of jet stream extreme waviness, associated 74 with large amplitude waves and weather extremes, in an highly idealized model frame-75 work. We have conducted four simulations with the OpenIFS model in aquaplanet con-76 figuration in which we have increased the Sea Surface Temperatures (SSTs) while either 77 maintaining or reducing the meridional gradients. Compared to previous highly ideal-78 ized studies (Butler et al., 2010; Hassanzadeh et al., 2014) we retained moist processes 79 that can yield significant feedback on the dynamics (Vallis, 2020). Moreover, a more re-80 alistic mean temperature distribution and meridional temperature gradient reductions 81 are established compared to previous studies (Hassanzadeh et al., 2014; Schneider et al., 82 2015).83

Conducting these simulations, we aim to determine the influence of large-scale spatial warming on jet stream extreme waviness. We first discuss the modeled influence of the altered SSTs on the zonal mean temperature distribution and the atmospheric jet. Thereafter we discuss if the changed mean state possibly leads to changes in the largest amplitudes of the waves in the jet stream, jet stream extreme waviness and cut-off segments related to blocking highs and cut-off lows that are associated with weather extremes (Cattiaux et al., 2016).



Figure 1. a) Prescribed SST [°C] profiles as a function of latitude for the four model experiments. The profiles are zonally uniform and symmetric about the equator. b) Sinuosity Index [-] visualized for a selected timestep of the [CNTRL]-simulation. The black dashed contour line is the average Z500 isohypse [m] based on the original SI metric and the black solid contour line is the average Z500 isohypse based on our modified SI method. Shading denotes the 500-hPa wind speed [m s⁻¹]. Coastlines are included for reference, but are nonexistent in the simulations.

91 2 Methods

2.1 OpenIFS

We use the numerical weather prediction model OpenIFS, developed by the European Center for Medium Range Weather Forecasts (ECMWF). OpenIFS shares the same dynamical core and physical parametrizations as the Integrated Forecast System (IFS) which is used for operational weather forecasting at ECMWF. However, compared to IFS, OpenIFS lacks data assimilation capacity and is not coupled to an ocean model. We use version Cy43r3v2 that was operational between July 2017 and June 2018 (documentation online at https://www.ecmwf.int/en/publications/ifs-documentation).

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2.2 Experimental Setup

The experimental setup and initial conditions follow Sinclair and Catto (2023). The 101 simulations run in the aquaplanet configuration with fixed zonally uniform SSTs. The 102 incoming solar radiation is specified at the equinoctial value to remove seasonal varia-103 tion, but a diurnal cycle is present. The simulations run at T255 resolution (grid spac-104 ing of about 78 km at the equator) and with 60 vertical model levels with the model top 105 at 0.1 hPa. The initial conditions are modified from a randomly selected real atmospheric 106 state from the ERA5-reanalysis (Hersbach et al., 2020). First, the land-sea mask is changed 107 to cover the whole globe by ocean. Second, the surface geopotential is set to zero every-108 where. Finally, the atmospheric fields are interpolated to the new flat surface in regions 109 where there is topography on Earth. 110

We conduct four experiments, i.e. [CNTRL], [SST4], and [PA] following Sinclair and Catto (2023) and an additional Reduced Temperature Gradient [RTG] simulation. The simulations are selected because compared to [CNTRL] they establish large-scale spatial warming with upper tropical warming in [SST4], polar amplification in [PA] and gradual warming from the equator resulting in a large meridional temperature gradient reduction in [RTG]. Through executing these four simulations we are able to study the impact of large-scale spatial warming on jet stream waviness.

The control simulation [CNTRL] follows the SST-profile QObs of Neale and Hoskins 118 (2000) that tries to resemble Earth's SSTs. It has maximum SSTs of 27°C on the equa-119 tor decreasing poleward to 0° C at 60° latitude from where they remain constant (Fig-120 ure 1a). The [SST4] simulation has a uniform warming of 4°C compared to the [CNTRL] 121 simulation (Figure 1a). This results in upper tropical warming (Sinclair et al., 2020; Sin-122 clair & Catto, 2023). The polar amplification simulation [PA] (AA in Sinclair & Catto, 123 2023) uses the QObs SST distribution between 45° S and 45° N, with SSTs set to 5° C pole-124 ward of these latitudes to mimic polar amplification (Figure 1a). Compared to [CNTRL] 125 the SSTs of the [RTG] simulation are gradually warmed from the equator with the max-126 imum temperature increase of 5°C occurring poleward of 60° latitude (Figure 1a). This 127 additional simulation is conducted to simulate a more realistic equator-to-pole temper-128 ature gradient reduction, with warming occurring in the subtropics, mid-latitudes, and 129 polar regions, rather than just at high latitudes as in the [PA] simulation. 130

Each simulation is run for a total of 11 years. This simulation length is long enough to capture internal variability as there is no seasonal cycle in our simulations. However, to ensure a balanced state is achieved, the first year of each simulation is discarded. Model output is saved every six hours on 22 pressure levels between 1000 hPa and 10 hPa.

2.3 Jet Stream Waviness Quantification

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To quantify waviness different methods exist (e.g. Francis & Vavrus, 2012; Chen 136 et al., 2015; Cattiaux et al., 2016; Di Capua & Coumou, 2016; Röthlisberger, Martius, 137 & Wernli, 2016; Martin, 2021). Dynamical approaches use concepts based on energy con-138 servation while geometric approaches aim to capture the shape of the waves (Vavrus, 2018). 139 We use the geometric Sinuosity Index (SI) by Cattiaux et al. (2016) because their method 140 includes cut-off segments related to blocking highs and cut-off lows and has been used 141 in conjunction with the Local Wave Activity metric (Chen et al., 2015) without diver-142 gent outcomes (Blackport & Screen, 2020). Moreover, the SI method is defined at the 143 500 hPa pressure level that has the advantage to be insensitive to heating (Barnes, 2013; 144 Cattiaux et al., 2016). SI is computed every 6 hours to capture synoptic-scale variabil-145 itv. 146

¹⁴⁷ Cattiaux et al. (2016) compute the SI as a measure of the mean flow around 50° ¹⁴⁸ latitude. First they calculate the average 500-hPa geopotential height, Z500, between ¹⁴⁹ 30° and 70° latitude. Then, Cattiaux et al. (2016) define the SI as the ratio between the ¹⁵⁰ length of the isohypse with the estimated Z500 value to the circumference of the Earth ¹⁵¹ at 50° latitude.

Unfortunately, the original SI metric does not adequately capture the jet stream 152 in the aquaplanet setup (Figure 1b). Specifically, the isohypse do not align well with the 153 wind maxima associated with the jet stream and also contains segments at high latitudes 154 that are unrelated to the jet stream or atmospheric blocks. To address this issue, we de-155 velop a new method to determine the latitudinal range $\Delta \phi$ over which to calculate the 156 Z500 average. Specifically, we identify $\Delta \phi$ in each hemisphere where the time mean zonal 157 mean magnitude of the horizontal wind vector at 500 hPa V_{500} exceeds half of its cli-158 matological maximum of $[\overline{V_{500}}]$ (Figure S1), where the overbar represents time mean and 159 square brackets denoted the zonal mean. By using this method, we find the following 160 latitude ranges per simulation per hemisphere: (21.4°N, 47.4°N) & (22.1°S, 47.4°S) for 161 the [CNTRL]-simulation, $(22.8^{\circ}N, 51.6^{\circ}N) \& (22.1^{\circ}S, 51.6^{\circ}S)$ for the [SST4] simulation, 162 (20.7°N, 49.5°N) & (21.4°S, 49.5°S) for the [RTG] simulation and (20.7°N, 45.3°N) & (21.3°S, 163 45.3°S) for [PA]. We find the same latitude ranges if we use the zonal mean zonal wind 164 $([\overline{u}_{500}])$ instead of $[\overline{V}_{500}]$. Between the above mentioned latitudinal ranges we calculate 165 the average Z500 at every timestep which is then used as the selected value of the iso-166 hypse to calculate its length. 167

¹⁶⁸ Moreover, Cattiaux et al. (2016) use a constant normalization of circumference of ¹⁶⁹ the Earth at 50° latitude, but to account for the latitudinal jet stream migration we nor-¹⁷⁰ malize the length of the Z500 isohypse with the circumference of the Earth at the mean ¹⁷¹ latitude of the selected isohypse $\tilde{\phi}_{Z500}$. The resulting modified SI is defined as follows:

$$SI(\phi, t) = \frac{\operatorname{arclength}(Z500_{\Delta\phi}(t))}{2\pi a \cos(\tilde{\phi}_{Z500}(\phi, t))},\tag{1}$$

where $Z500_{\Delta\phi}$ is the average geopotential height at 500 hPa between the above mentioned latitudinal ranges per simulation per hemisphere $_{\Delta\phi}$, *a* denotes the radius of Earth and $\tilde{\phi}_{Z500}$ is the mean latitude of the selected Z500 isohypse. A value of SI=1 indicates a straight westerly atmospheric flow, whereas SI values in the range 2-3 indicate a strongly meandering flow with the average Z500 isohypse being 2-3 times longer than the circumference of the Earth at the mean latitude.

Further, we use the meridional extent defined as the difference between the maximum and minimum latitude of the selected Z500 isohypse, to quantify the wave amplitude (Barnes, 2013). Moreover, the SI metric enables the possibility to differentiate between the circumglobal isohypse and cut-off segments related to blocking highs and cut-off lows that are associated with weather extremes, as shown by Cattiaux et al. (2016). We only maintain cut-off segments that are larger than the circumference of a circle with radius of 78 km (i.e. 1 grid cell).

¹⁸⁶ 3 Mean State Response in Temperature (gradient) and Zonal Wind

All simulations display zonal mean climatologies of temperature and zonal wind that are generally consistent with observations of the Earth's atmosphere (Figure 2, row 1 and 3). The core of the jet streams are located near 30° latitude at tropopause level. The dynamical tropopause, defined as the 2 PVU-surface, has physically plausible values that vary between 100 hPa in the tropics and 300 hPa at the poles (Figure 2). The simulations exhibit almost perfect symmetry, as would be expected from the aquaplanet set up.

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3.1 [SST4] simulation

The [SST4] simulation reveals the most substantial tropospheric warming of all simulations. Climatological temperature increases of over 5 K are ubiquitous (Figure 2a). The warming signal is particularly strong in the upper tropical troposphere, exceeding 10 K due to enhanced latent heat release in the rising branch of the Hadley cells (not shown). The tropospheric warming leads to a deeper troposphere, as indicated by the lifted dynamic tropopause (Figure 2, column 1). Furthermore, the lower polar stratosphere cools, which is potentially due to a weakened Brewer-Dobson circulation.

The combined impact of the deeper troposphere, upper tropospheric tropical warm-202 ing and lower stratospheric polar cooling in the [SST4] simulation results in an enhanced 203 meridional temperature gradient around 200 hPa (Figure 2d). The most significant in-204 crease in the meridional temperature gradient occurs at approximately 25° latitude at 205 tropopause level. Wind speeds in the core of the subtropical jet stream strengthened con-206 sistently by approximately 6%, from 53.3 m s⁻¹ to 56.9 m s⁻¹. The core of the jet stream 207 also shifts upward by 25 hPa, from 175 hPa in [CNTRL] to 150 hPa in the [SST4] sim-208 ulation. However, stronger increases exceeding 10 m s^{-1} in zonal wind occur above the 209 jet stream cores due to an increase in the jet stream height, consistent with the increase 210 height of the trop pause (Figure 2g). The upward shift of the jet core is also evident by 211 the decrease in the zonal wind speed below the jet core in the (sub)tropical regions. In 212 addition to the deeper zonal wind distribution, we also find a poleward shift in the jet 213 stream position caused by an expanding tropical atmosphere. The tropical warming pushes 214



Figure 2. Atmospheric zonal mean climatologies of the ten year simulations. Shading shows the atmospheric responses $(|\overline{\text{EXPERIMENT}}|-|\overline{\text{[CNTRL]}}|)$ in temperature $[\overline{T}]$ [K] (a, b, c), meridional temperature gradient $[\frac{dT}{dy}]$ [K 100 km⁻¹] (d, e, f) and zonal wind $[\overline{u}]$ [m s⁻¹] (g, h, i) for the [SST4] simulation (column 1), [RTG] simulation (column 2) and [PA] simulation (column 3). Black contour lines represent the [CNTRL] simulation climatologies (labels indicate their values) and magenta contour lines the dynamical tropopause at the 2PVU surface — dashed magenta lines the equivalent in the experiment.

the polar edge of the baroclinic zone poleward as visible in the band of increased temperature gradients and zonal winds in the mid-latitudes (Figures 2d and 2g).

3.2 [RTG] simulation

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The [RTG] simulation warms in the lower to mid-troposphere at high latitudes, with 218 a maximum warming of approximately 4.5 K that extended into the mid-latitudes, from 219 where the warming gradually reduces to values of 1 K in the subtropics (Figure 2b). In 220 contrast to the upper tropical warming in the [SST4] simulation, the [RTG] simulation 221 shows cooling in this region. The cooling can be attributed to decreased latent heat re-222 lease in the rising branch of the Hadley cells (not shown). The tropospheric warming in 223 the [RTG] simulation also results in a deeper troposphere, as indicated by the increased 224 height of the dynamic tropopause poleward of 30° latitude (Figure 2, column 2). 225

Overall, the effect of lower tropospheric polar warming and upper tropospheric trop-226 ical cooling causes a substantial reduction in the tropospheric meridional temperature 227 gradient (Figure 2e). The strongest decrease up to $0.2 \text{ K} 100 \text{ km}^{-1}$ occurs in the mid-228 latitudes between 25° latitude and 50° latitude in the middle troposphere (Figure 2e). 229 In turn, the reduced meridional temperature gradient impacts the zonal circulation. Zonal 230 winds in the [RTG] simulation decrease substantially throughout the whole troposphere 231 (Figure 2h). Most prominently, the core of the jet stream weakens by approximately 15%232 to 45.4 m s^{-1} . 233

3.3 [PA] simulation

Compared to the [RTG] simulation, the warming of the lower to mid-troposphere
in the [PA] simulation is more confined to higher latitudes (Figure 2c). The maximum
warming of 4 K occurs poleward of 60° latitude in the lower troposphere, while equatorward of 45° latitude, the temperature response was neutral, ranging from -1 K to 1 K.

The most prominent effect of the low-level polar warming is the decrease in the merid-239 ional temperature gradient on the poleward edge of the baroclinic zone in the mid-latitudes 240 up to 0.3 K 100 km⁻¹ near the surface (Figure 2f). This is the strongest tropospheric 241 meridional temperature-gradient reduction of all experiments and is expected from the 242 prescribed [PA] SST-profile (Figure 1a). The reduced temperature-gradient causes a de-243 crease in zonal wind aloft, poleward of the jet stream core (Figure 2i). Apart from slightly 244 enhanced jet core strength from 1.1 m s^{-1} to 54.4 m s^{-1} , no notable wind speed changes 245 occur in the subtropics of the [PA] simulation. 246

²⁴⁷ 4 Jet Stream Waviness Response

Next, we study the impact of the altered mean atmospheric state on wave ampli tudes, waviness of the jet stream, cut-off segment lengths and the variability within the
 distributions of these diagnostics (Figure 3).

Our focus is on the extreme tails of the meridional extent and SI distributions, as-251 sessed through changes in their respective 98th percentiles compared to the [CNTRL] 252 simulation (Figure 3). They correspond to large wave amplitudes and high waviness events 253 that are associated with weather extremes (e.g., Francis & Vavrus, 2015; Cattiaux et al., 254 2016; Röthlisberger, Pfahl, & Martius, 2016; Coumou et al., 2018), and therefore more 255 sociatally relevant than the mean. To test if the 98^{th} percentiles differ statistically sig-256 nificantly we use the nonparametric quantile test (Johnson et al., 1987). We use the al-257 ternative hypothesis 'less' which tests if the probability of the 98^{th} percentile of the ex-258 periment simulation has higher values than the [CNTRL] simulation. We also tested the 259 90^{th} and 95^{th} extreme percentiles (not shown) which gave qualitatively the same results 260 (except for the waviness and cut-off segments diagnostics in the [SST4] simulation). For 261



Figure 3. Violin plots for the 6-hourly distributions of (a) the meridional extent [°] of the average Z500 in the latitudinal range of the selected Z500 isohypses, (b) Sinuosity Index [-] and (c) the length of the cut-off segments of the selected Z500 isohypses [km]. Labeled horizontal bars indicate the 98^{th} , 75^{th} and 25^{th} percentile (from top to bottom), and the vertical dotted line represents the interquartile range.

completeness we also analyze the median $(50^{th} \text{ percentiles})$ of each diagnostic differs from [CNTRL] using the Brown-Mood test.

Lastly, the variability in the distributions is studied by the interquartile ranges because the distributions are not normally distributed. To evaluate the statistical differences among these interquartile ranges, we employ bootstrapping. Comparisons among the resulting distributions of the computed interquartile ranges (Figure S2) are conducted using a student's t-test.

Now, we first briefly discuss the general changes of the diagnostics supported by
 statistical tests before we specifically highlight the most substantial changes found in each
 simulation.

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4.1 General changes of the diagnostics

Across all model experiments, and for each diagnostic, the 98th percentile of each distribution show the most prominent changes (Figure 3). We find that the 98th percentiles for each diagnostic is statistically significantly lower in the experiments compared to [CN-TRL] as confirmed by the quantile test at the 99% confidence interval.

The shifts in the medians are moderate and vary in sign. Despite the small magnitude of the changes, they are statistically significantly different on the Brown-Mood test at the 99% confidence interval for all diagnostics and simulations except for cut-off segments length in [SST4] and [PA] (Table S1). However, all median changes are relatively minor deviations compared to the natural variability depicted by the interquartile ranges (Figure 3).

Interestingly, the interquartile ranges for each diagnostic in every simulation decreases compared to [CNTRL]. We find that the interquartile ranges for each diagnostic is statistically significantly lower in the experiments compared to [CNTRL] as confirmed by the student's t-test at the 99% confidence interval (Table S1). Hence, this result indicates a consistent reduction in variability of the selected diagnostics across all warming scenarios.

²⁸⁹ 4.2 [SST4] simulation

Comparing the meridional extent distribution between [SST4] and the [CNTRL] (Figure 3a), the 98th percentile decreases from 55.5° to 51.3°. Despite this decrease, the median of the distribution increases slightly from 19.6° to 20.4°. Thus, with uniform warming resulting in upper tropical warming and a strengthened jet stream, there is a robust decrease in the largest wave amplitudes and a slight increase in the median amplitude.

Analyzing the SI distribution (Figure 3b), the 98^{th} percentile decreases from 1.55 in [CNTRL] to 1.51 in [SST4], indicating a decrease in extreme waviness episodes. There are no further alterations in the SI distribution, suggesting only a reduction in high-waviness episodes within [SST4].

Examining the cut-off segments distribution (Figure 3c), the 98th percentile signals a distinct reduction in the length of the longest cut-off segments under uniform warming. Marginal differences are observed in the median, indicating minimal changes in the lengths of cut-off segments of the [SST4] simulation.

4.3 [RTG] simulation

The changes observed in the extreme tail of the meridional extent distribution (Figure 3a) within [RTG] are most pronounced among all experiment simulations. The 98^{th} percentile decreases from 55.5° in [CNTRL] to 47.7° in [RTG]. There is a marginal shift in the median towards higher values. Overall, these changes in the meridional extent of [RTG] suggest that the largest wave amplitudes are smaller in weaker jet streams.

Within the SI distribution (Figure 3b) of [RTG], consistent trends emerge. A notable decrease from 1.55 to 1.44 in the 98^{th} percentile signifies a decrease in extreme waviness episodes. However, a marginal increase in SI of 0.02 in the median is observed. Consequently, weakened jet streams within [RTG] exhibit a distinct decrease in extreme waviness episodes alongside a slight increase in median waviness. This finding suggest that reduced low-level temperature gradients accompanied with weakened jet streams do not promote extreme waviness episodes.

Moreover, prominent reductions observed in the distribution depicting the length of cut-off segments (Figure 3c) within [RTG] indicate a consistent reduction in the length of these segments.

4.4 [PA] simulation

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Polar warming stands out as the sole simulation consistently manifesting reductions across all distribution characteristics for each diagnostic (Figure 3). Notably, the 98th percentile of the meridional extent (Figure 3a) decreases from 55.5° in [CNTRL] to 53.0° in [PA]. While the median undergoes a robust yet marginal decrease, collectively, these outcomes suggest a reduction in wave amplitudes under polar warming conditions.

Similar consistent reductions are evident in the SI distributions (Figure 3b). The 98th percentile notably decreases from 1.55 in [CNTRL] to 1.43 in [PA], signifying a substantial decrease in extreme waviness episodes. Additionally, we find a minimal reduction in the median SI of 0.01. These reductions across all distribution characteristics collectively reinforce the evidence supporting decreased jet stream waviness under polar warming conditions.

Once again, in the characteristics related to the length of the cut-off segments (Figure 3c), analogous trends are observed. The 98th percentile and median display reductions in the length of the cut-off segments under polar warming conditions.

³³⁴ 5 Discussion and Concluding Remarks

We perform four idealized aquaplanet simulations to study the causality between 335 large-scale spatial warming and jet stream extreme waviness. The results of the exper-336 iments contribute to the open question whether the future jet stream is influenced by 337 large-scale spatial warming (e.g., Barnes & Screen, 2015; Shaw et al., 2016; Stendel et 338 al., 2021) and how jet stream waviness would alter (e.g., Vavrus, 2018; Coumou et al., 339 2018; Cohen et al., 2020). To quantify jet stream waviness on an aquaplanet, we adjust 340 the latitudinal range and the normalization latitude in the computation of the Sinuos-341 342 ity Index by Cattiaux et al. (2016). Using this waviness metric we are able to analyze the length of cut-off segments, which are related to blocking highs and cut-off lows that 343 are associated with mid-latitude weather extremes (Cattiaux et al., 2016). 344

The idealized aquaplanet simulations generate robust responses in the mean zonal climates of temperature, temperature gradients and zonal wind. Most notably, we find substantial decreases in (large) wave amplitudes, (extreme) jet stream waviness and cutoff segments for almost all simulations in each diagnostic. We enumerate the most prominent results and highlight differences between the simulations:

- In the [SST4] simulation, uniform warming of 4 K leads to upper tropospheric tropical warming, enhanced meridional temperature gradients, and strengthened jet streams. All three of the circulation diagnostics we consider show a significant decrease in their 98th percentiles and interquartile ranges, thus indicating the extreme waviness events become less wavy and less variable with uniform warming. The median of wave amplitudes, however, show a robust, but marginal increase.
- 2. Gradual warming from the equator to 5 K at the poles in the [RTG] simulation substantially reduces meridional temperature gradients and weakens jet streams, especially in the subtropical jet core region. All three of the circulation diagnostics we consider depict even more significant decrease in their 98th percentiles in [RTG]. This implies extreme waviness episodes become even less wavy and less variable with meridional temperature gradient reductions. Also in [RTG] the median of wave amplitudes show a marginal increase.
- 3. Polar warming at high latitudes in the [PA] simulation reduces meridional temperature gradients, primarily in the mid-latitudes and the lower troposphere, that weakens jet streams aloft. The [PA] simulation consistently manifest reduction in the 98th percentiles, medians and interquartile ranges across all three diagnostics. This leads to robust reduced wave amplitudes, decreased waviness episodes and reduced length of cut-off segments in conjunction with decreased variability.

Compared to [CNTRL], the reduced wave amplitudes observed in the [RTG] and 369 [PA] simulations align with findings from Hassanzadeh et al. (2014), who report a de-370 crease in wave amplitude with reduced meridional temperature gradients in dry model 371 simulations. Furthermore, Hassanzadeh et al. (2014) find reduced areas affected by at-372 mospheric blocking in simulations with reduced temperature gradients. While we did not 373 specifically detect blocking, our results indicate consistent findings with shortened cut-374 off lengths in the reduced temperature gradient simulations [PA] and [RTG]. The only 375 highly idealized study that focuses on jet stream waviness specifically is Schemm and 376 Röthlisberger (2024). They find decreased waviness in 4 K uniform warmed aquaplanet 377 simulations with SSTs representing a summer and winter hemisphere. This is consistent 378 with what we find in [SST4]. 379

The magnitude of all (statistically significant) responses in the median of [SST4], [RTG] and [PA] is small compared to the natural variability of the [CNTRL] simulation. This has previously been noted for reanalysis data (e.g., Barnes, 2013; Screen & Simmonds, 2013; Screen, 2014), comprehensive climate models (e.g., Cattiaux et al., 2016), models with induced sea-ice loss alone (e.g., Blackport & Screen, 2020; Smith et al., 2022) and highly idealized simulations (Hassanzadeh et al., 2014; Schneider et al., 2015).

Additionally, the natural variability reduces as evidenced by the robust decrease 386 in the interquartile range of the distributions of wave amplitude, jet stream waviness and 387 cut-off segments. This suggests that large-scale spatial warming makes the atmospheric 388 circulation less variable. The reduced variability in the experiment simulations is poten-389 tially caused by weakened baroclinicity and, hence, the jet stream is less affected by syn-390 optic waves. Schemm and Röthlisberger (2024) find a reduction of synoptic wave am-391 plitude with uniform warming and state that these waves play a more substantial role in shaping the geometric waviness of the jet stream. Indeed, Sinclair and Catto (2023). 393 with identical [SST4] and [PA] simulations, find for uniform warming weakened Eady 394 growth rates and for polar amplification weakened growth rates in the low-to-middle tro-395 posphere on the poleward side of the jet, but slight increases in the mid-to-upper tro-396 posphere at high latitudes. For our [RTG] simulation we expect even larger reductions 397 in baroclinicity because the natural variability is the lowest in all simulations. 398

Our results contradict the mechanism proposed by Francis and Vavrus (2012, 2015), that a reduced temperature gradient, consequently, a weaker zonal flow, would lead to amplified and more wavy jet streams, resulting in increased weather extremes. Their hypothesis, however, leans on the linearity assumption of barotropic Rossby wave theory, which may not fully encompass the highly nonlinear behavior observed in the real atmosphere and the aquaplanet's atmosphere. This might be because barotropic Rossby wave theory does not describe nonlinear baroclinic growth of synoptic waves.

Another possible explanation for these results contradicting the mechanism pro-406 posed by Francis and Vavrus (2012, 2015), is the use of an aquaplanet where the absence 407 of zonal asymmetries, like orography and land-sea contrasts, eliminates many Rossby wave sources. Moon et al. (2022), have identified thermal forcing, arising from land-sea con-409 trasts, in conjunction with weakened flow, as pivotal factors for generating wavier jet streams. 410 Thus, future idealized experiments could introduce extra complexity by introducing SST 411 perturbations (Brayshaw et al., 2008; Schemm et al., 2022), simple continents (Brayshaw 412 et al., 2009), orography or all these aspects (Brayshaw et al., 2011) in combination with 413 temperature gradient reductions. This approach could provide a more comprehensive un-414 derstanding of the impact of temperature gradient modifications on jet stream circula-415 tion changes and increased weather extremes. 416

In summary, results from our study demonstrates that large-scale spatial warming on an aquaplanet affects meridional temperature gradients and jet streams. Both strengthened and weakened jet streams show robust decreases in the magnitudes of large wave amplitudes and extreme episodes of jet stream waviness. We suggest that these results are related to reduced baroclinicity in all simulations. Ultimately, we conclude that weaker jet streams do not necessarily become wavier.

423 6 Open Research

424

Data archiving is underway. We plan to archive at Zenodo.

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Supporting Information for "The Influence of Large-Scale Spatial Warming on Jet Stream Extreme Waviness on an Aquaplanet"

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Figure S1. Time mean zonal mean of the magnitude of the 500-hPa horizontal wind vector $[\overline{V_{500}}]$ [m s⁻¹] for each simulation. Horizontal dashed lines show the half of the maximum $[\overline{V_{500}}]$ thresholds and vertical dashed lines the latitude range where this thresholds was exceeded. These latitude ranges are used to estimate the modified Sinuosity Index.

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Figure S2. Distributions of the interquartile ranges of (a) meridional extent [°], (b) Sinuosity Index [-] and (c) cut-off segments length [km] for each simulation obtained from bootstrapping. In this process, we iteratively resample the data 5000 times for each simulation and diagnostic and maintain the same sample size of the original datasets. Subsequently, interquartile ranges are computed for each of these 5000 resamples. The dashed vertical lines are the means of the distributions and the continuous vertical lines are the interquartile ranges from the original datasets (Figure 3).

Table S1. P-values from quantile test, Brown-Mood test and student's t-test that tests 6-hourly distributions $(N = 2 \times (10 \times 365 \times 4) + 2 \times (8) = 29216$, because we simulate ten years, including two leap years, of two identical hemispheres). For the quantile test on the 98th the alternative hypothesis 'less' is chosen. Hence, it tests if the probability of the 98th percentile of the experiment simulation has higher values than the [CNTRL] simulation. A Brown-Mood test is identical to a two-sided quantile test at the 50th percentile. P-values of student's t-test that tests interquartile range distributions obtained by bootstrapping (N=5000). P-values lower than p=0.01 are bold and there the simulation differ from the [CNTRL] simulation in a statistically significant manner on the 99% confidence interval. P-values smaller than p=0.0005 — and larger than zero — are shown with p<0.000.

[CNTRL] vs.	Meridional Extent	Sinuosity Index	Length Cut-off Segments
[SST4]	p<0.000	p=0.001	p<0.000
[RTG]	p < 0.000	p < 0.000	$p{<}0.000$
[PA]	p < 0.000	p < 0.000	p = 0.004
Brown-Mood test $(50^{th} \text{ percentile})$:			
[CNTRL] vs.	Meridional Extent	Sinuosity Index	Length Cut-off Segments
[SST4]	p<0.000	p<0.000	p=0.054
[RTG]	p < 0.000	p < 0.000	$p{<}0.000$
[PA]	p<0.000	p<0.000	p = 0.023
Student's t-test:			
[CNTRL] vs.	Meridional Extent	Sinuosity Index	Length Cut-off Segments
[SST4]	p<0.000	p<0.000	p<0.000
[RTG]	p < 0.000	p<0.000	$p{<}0.000$
[PA]	p<0.000	p<0.000	p<0.000

Quantile test $(98^{th} \text{ percentile})$: