Informed Neural Networks for Flood Forecasting with Limited Amount of Training Data

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Abstract

This study presents a novel approach to improving the accuracy of flood forecast models with limited training data. Flood forecast information is crucial for early evacuation planning.

However, the probability of flooding caused by continuous heavy rainfall is increasing, even in areas where we have not installed flood forecasts.

New methods exist to provide flood forecasts, but they require long-term observations and regular updating of extensive data on the basin.

Existing methods of providing new flood forecast information require long-term observations and regular updates of extensive data on the watershed.

These requirements are related to the construction time and cost of providing flood forecasts.

To address this issue, we propose Informed Neural Networks (INN) that integrate existing domain knowledge of river engineering to enhance the performance of flood forecasts with a limited amount of training data.

We evaluated the performance of our proposed method with Japanese real-world river water levels and compared it to conventional methods such as artificial neural networks (ANN).

Our results demonstrate that the INN can significantly improve forecasting accuracy with only a small amount of training data, comparable to conventional methods trained with eight times the amount of flood data.

This study highlights the potential of INN as a novel approach for accurate and efficient flood forecasting with limited training data.

Informed Neural Networks for Flood Forecasting with Limited Amount of Training Data

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6	Key Points:
7	• We developed a methodology to improve the precision of flood forecasting
8	technology, specifically when working with limited amounts of data.
9	• The methodology incorporates a domain-specific knowledge into the architec-
10	ture and training procedure of Neural Networks (NN).
11	• Proposed method has demonstrated superior accuracy compared to conven-
12	tional methods, even under conditions of data scarcity.

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13 Abstract

This study presents a novel approach to improving the accuracy of flood forecast 14 models even if training data is limited. Flood forecast information is crucial for 15 early evacuation planning. However, the probability of flooding caused by continu-16 ous heavy rainfall is increasing, even in areas for which floods have not been antic-17 ipated. While methods exist to provide flood forecasts, they require long-term ob-18 servations, and regular updating of extensive data on the catchment basin. These 19 requirements impact the construction time and cost of providing flood forecasts. To 20 address this issue, we propose the Informed Neural Network (INN); it draws on ex-21 isting domain knowledge of river engineering to enhance the performance of flood 22 forecasts with limited amounts of training data. We evaluate the performance of 23 our proposed method by assessing Japanese real-world river water levels and com-24 pare the results to those of conventional methods such as artificial neural networks 25 (ANNs). Our results demonstrate that INN can significantly improve forecast accu-26 racy with only a small amount of training data, comparable to conventional methods 27 trained with three times the amount of flood data with three hours forecast. This 28 study highlights the potential of INN as a novel approach for accurate and efficient 29 flood forecasting with limited training data. 30

³¹ Plain Language Summary

32 This study introduces a new method called the informed neural network to enhance the accuracy of flood forecasting models when the training data is limited. 33 Accurate flood forecasts are crucial for early evacuations, as the risk of flooding due 34 to heavy rainfall is increasing even in areas without existing flood risk. Traditional 35 methods for generating flood forecasts require extensive data and continuous up-36 dates, making the process time-consuming and costly. In contrast, the INN approach 37 incorporates existing knowledge of river engineering to improve forecasting perfor-38 mance with a just a small amount of training data. We evaluate the INN method 39 with real-world river water level data from Japan, and compared it to conventional 40 methods such as artificial neural networks. The results demonstrate that the INN 41 approach significantly improves forecast accuracy, even with limited training data, 42 to match conventional methods trained with eight three more flood data with three 43 hours forecast. This study highlights the potential of INN as an innovative and effi-44 cient approach for accurate flood forecasting, particularly in situations with limited 45 training data. 46

47 **1** Introduction

Flood forecast information can enable municipalities to plan proactively and 48 residents to safely evacuate in the event of a flood. Consequently, accurate flood 49 forecasting is crucial in areas susceptible to flooding. Recently, Japan has observed 50 an increase in heavy rainfall compared to the past (Kawase et al., 2020; Hirockawa 51 et al., 2020) Kawase et al. (2020) showed central and western regions experiencing 52 record-breaking total precipitation of 48- and 72-hours at approximately 1,300 pre-53 cipitation stations in 2018. Weather officials continue to observe such unprecedented 54 heavy rains. Some studies predict that these changes are due to climate change and 55 that the rainfall trend will continue (Kusunoki et al., 2006; Kitoh & Uchiyama, 2006; 56 Duan et al., 2015; Osakada & Nakakita, 2018; Takemi & Unuma, 2020). As a result, 57 such an increase in unexperienced heavy rain cause the risk of flooding in areas pre-58 viously unaffected by it. There are 30,000 rivers in Japan, of which only 393 provide 59 forecast information. Climate change has increased the risk of thousands of rivers 60 for which flood forecasts are not provided. Therefore, it is necessary to provide flood 61

forecasts at more new locations. The cost of the forecasting system is essential when
 providing flood forecast information to many new locations.

There are two approaches for flood forecasting: rainfall-runoff-based approach 64 and data-driven-based approach. The rainfall-runoff-based approach requires various 65 data types, such as basin characteristics distribution. However, these data require 66 high quality (Hapuarachchi et al., 2011), making it challenging to acquire and contin-67 uously update the data. In contrast, the data-driven approach requires only rainfall 68 and river water level data but the need for measurements over a more extended pe-69 70 riod. Based on existing literature, a training dataset spanning at least five years and containing at least 15 flood events for data-driven methods (Mukerji et al., 2009; 71 Noymanee & Theeramunkong, 2019). Such requirements for long-term data mea-72 surements make providing flood forecast information for new sites difficult. There-73 fore, a method to achieve flood forecasting with a few types and a limited amount of 74 training data is an essential issue for flood forecasting. 75

In the field of data-driven methods, one potential solution to address the issue 76 of limited training data is to incorporate prior information into the learning process 77 of NN. This approach is known as Informed Machine Learning (IML), and many 78 groups have applied IML to various domains (Von Rueden et al., 2021). IML can 79 improve model performance by applying various types of prior knowledge, such as 80 knowledge graphs and equations, to the learning process. Many IMLs use NNs as a 81 building block, especially called Informed Neural Networks (INN). INN has achieved 82 improved model performance in many areas. Despite these advancements, identify-83 ing practical prior knowledge and corresponding Informed Machine Learning meth-84 ods for flood forecasting remains challenging. 85

This study introduces a novel method to implement INN for flood forecast-86 ing, suitable for limited training data scenarios. The proposed approach incorporates 87 prior knowledge about the "rainfall-runoff-river water level relationship" and "tank 88 model" derived from river engineering knowledge into a NN. We evaluated the per-89 formance of INN, To evaluate the INN's performance, We conducted a comparative 90 analysis between the proposed and conventional methods using flood data from a 91 river in the Kyushu region of southwestern Japan. The results indicated that the 92 proposed INN method performed as well as the conventional method when sufficient 03 training data was available. Moreover, the proposed method retained its accuracy even when the training data was limited. In contrast, when training data was lim-95 ited, the conventional ANN showed a more significant Root Mean Squared Error 96 (RMSE) up to 8 times higher than the proposed INN method. These results suggest 97 that the INN approach is a promising alternative for accurate flood forecasting when 98 limited training data is available. Overall, the proposed method offers an effective 99 solution for improving the accuracy of flood forecasting with limited training data, 100 and its potential applicability to other domains where data availability is restricted 101 warrants further exploration. 102

¹⁰³ 2 Related works

There are two kinds of approaches to flood forecasting. One is a rainfall-runoffbased approach, and another is a data-driven approach. Methods based on the rainfallrunoff approach determine the amount of water runoff from the basin and then determine river water levels. Methods based on the data-driven approach often predict river water levels directly.

Many methods were proposed related to the rainfall-runoff-based approach. This method has some parameters, such as precipitation, discharge, and basin characteristics. Especially, to account for the spatial bias of rainfall and the distribu-

tion of land features, the rainfall-runoff method often requires dividing the basin into 112 subregions, and it has been called the distributed rainfall-runoff approach (Brocca 113 et al., 2011). Rainfall-runoff approach has parameters related to catchment char-114 acteristics. Basin characteristics include terrain, soil, geology, land cover, and more 115 (Cole et al., 2006). Such parameters are not always available, and even when they 116 are, they are often of poor quality and require improvement (Hapuarachchi et al., 117 2011). Therefore, they cannot always be the best approach to provide flood forecast-118 ing for many rivers in a short period and maintain it in the future. 119

120 A typical model in the data-driven approach is the statistical model. The autoregressive moving average (ARMA) (Valipour et al., 2012) and autoregressive in-121 tegrated moving average (ARIMA) (Valipour et al., 2013) are representative and 122 basic models in this area. A statistical model related to ARMA and ARIMA is re-123 ported to be more efficient regarding computational cost and generalization com-124 pared to the rainfall-runoff approach (Aziz et al., 2014). In the statistical model, 125 several methods treat floods as stochastic processes and predict probability distribu-126 tions from historical data(Kroll & Vogel, 2002). However, even the more advanced 127 models need improvement in terms of the accuracy of short-term forecasts and the 128 complexity of their applicationa (Mosavi et al., 2018). The machine learning (ML) 129 model is another data-driven approach. ML models for flood forecasting include a 130 variety of algorithms such as neural networks (NN) (Le et al., 2019; Elsafi, 2014; F.-131 J. Chang et al., 2007), neuro-fuzzy(Mukerji et al., 2009; Chen et al., 2006; Roodsari 132 et al., 2019), and support vector machines (Han et al., 2007; Yan et al., 2018). ML 133 models also include algorithms such as NNs that can deal with nonlinearities in the 134 rainfall-runoff process. ML models are reported to have better performance and less 135 complexity than physical models (Abbot & Marohasy, 2014). The issue with these 136 data-driven approaches is the long-term measurement data. Several literatures have 137 reported 15 to 45 flood data events or 5 to 20 years of measurements to build ML 138 models (Song et al., 2019; Mukerji et al., 2009; Nguyen & Chen, 2020; Noymanee & 139 Theeramunkong, 2019). 140

To address the issue of long-term measurement data, Researchers attempt to 141 integrate prior knowledge into the ML models pipeline that has been made in the 142 fields of physical and natural phenomena. These attempts are called informed ma-143 chine learning (IML) The main goal of this endeavor is to improve accuracy and 144 challenge the problem of limited training data volume. These efforts are based on 145 the taxonomy proposed by Von Rueden et al. (2021) and are divided into several 146 methods depending on the representation of prior knowledge. In particular, for prob-147 lems involving natural phenomena and physical systems, the type of existing knowl-148 edge that describes the system includes algebraic equations. One idea in an attempt 149 to integrate this algebraic equation into the machine learning pipeline is loss func-150 tion modification. Karpatne et al. (2017) achieved accuracy beyond conventional 151 techniques by adding the equation relating water temperature and density to the 152 loss function for the lake temperature modeling using NNs. Loss function modifica-153 tion by differential equations, another option, is also a subset of Algebraic equations. 154 Zhu et al. (2019) has achieved higher accuracy than conventional methods for the 155 problem of surrogate modeling of systems described by differential equations using 156 NNs, without using training data, by using the equation as a loss function. These 157 improvements show the possibility of INN for a limited amount of data by chang-158 ing the loss function based on the algebraic equation. The next category of possible 159 prior knowledge is knowledge graphs, which represent the relationships among the 160 elements of the system. M. B. Chang et al. (2016) applies a network structure of 161 NNs that dynamically changes from scene to scene to predict the motion of multi-162 ple rigid bodies that affect each other. It achieves improved accuracy over conven-163 tional static network structures. This result indicates the possibility of a network 164 structure of NNs suitable for the target system. In flood forecasting by IML, Qian 165

et al. (2019) use simulation results by the finite volume method as training data to 166 speed up the two-dimensional flood simulation by the shallow water wave equation 167 and train the neural network. As a result, they achieved 50,000 times faster than the 168 simulation. Accelerating prediction using such existing simulation results is called 169 surrogation and is one of the applications of IML. Bhasme et al. (2021) used IML 170 to improve annual water balance prediction accuracy. In this research, they define 171 the relationship between the variables of the physical model that predicts runoff by 172 learning with ML models. Mahesh et al. (2022) used IML to predict spatiotemporal 173 floods on one-dimensional channels. IML was realized by setting the loss function of 174 NNs based on the Saint Venant equation. When compared with ML models, IML 175 showed higher performance. In IML, although there are many studies on physics and 176 natural phenomena, there are still few studies on hydrology, and there needs to be 177 knowledge about the problem of a limited amount of training data for flood forecast-178 ing. Therefore, we set the following questions to obtain new knowledge about the 179 applicability of IML, especially INN, in flood forecasting. The overall research ques-180 tion this paper tries to answer is, "Can INN be applied to flood forecasting when 181 flood data are limited?" Consequently, the following two questions about INN is 182 needed to be answered. 183

- Can INNs perform as other conventional flood forecasting methods in the condition of a sufficient amount of training data?
- 2. Can INN maintain the performance rather than conventional methods in the condition of a limited amount of training data?

¹⁸⁸ **3** Materials and Methods

3.1 Study Area and Data Acquisition

The study area in this study is shown in 1. Oyodo River is located in the Kyushu 190 region of southwestern Japan, with a basin area of 2,230 km^2 and a length of 107 km. 191 The source of the Oyodo River is Nakadake, and the river's main channel passes 192 through the Miyakonojo Basin, mountainous areas, and the Miyazaki Plain. The 193 river has caused damage from flooding 12 times between 1936 and 2005 due to rain-194 fall during the rainy season. The predicted flood site, Hiwatashi, is located in the 195 middle reaches of the Oyodo River, $52 \ km$ from the source, and has a basin area 196 of 861 km^2 . At Hiwatashi, the government set the river water level of 6 m as the 197 flood warning level and 9.2 m as the flood hazard level to warn of flooding. We con-198 structed the data used for study validation from the river water level history of the 199 Oyodo River, following the work of (Hitokoto et al., 2017). Extract flood events ex-200 ceeding 6 m from the river water level and precipitation data. One event should 201 be from 72 hours before to 48 hours after the river water level peak. From 1990 to 202 2014, we have constructed 23 flood events, of which four flood events (1990, 1993, 203 2004, and 2005) had river water levels exceeding 9.2 m. We use fourteen rainfall sta-204 tions and four river water level stations around and upstream of the basin to obtain 205 data for the same period. We obtained all data from the Water Information Sys-206 tem database of the Ministry of Land, Infrastructure, Transport, and Tourism in 207 Japan(Ministory of Land, Infrastructure, Transport, and Tourism in Japan, 2021). 208

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3.2 Conventional ANN for flood forecasting

This section describes the conventional ANN based on the work of Hitokoto et al. (2017). A schematic diagram illustrating flood forecasting with an ANN is presented in Figure 2. The model takes three kinds of input data: river water levels at the forecast location, the river water level at the upstream location, precipitation in the basin, and outputs predicted river water levels. The river water level data for in-



Figure 1. Location of the Hiwatashi gauging station, related rivers and near by stations. This map uses the data from standard elevation map published by Geospatial Information Authority of Japan and edited by NTT Advanced Technology Corporation.

put is hourly data for a certain period for the location of the flood forecast and its 215 upstream locations. The input rainfall is the observed and predicted rainfall at mul-216 tiple locations in the basin. The ANN model comprises three fully connected layers, 217 with ReLu activation functions applied to the first and second layers. We trained 218 the ANN in two stages. As a pre-training step, the middle layers are optimized as 219 denoising autoencoders. The denoising autoencoders have the same number of out-220 put variables as inputs, and it is trained to regenerate input from noise-added input. 221 Next, the learning process is performed using the parameters optimized as denois-222 ing autoencoders as the initial values. In this learning process, the river water level 223 and rainfall data are used as input data and river water level data are used as train-224 ing data. The river water level data is hourly data for a certain period at the flood 225 forecasting location and upstream. The precipitation data are also hourly for a cer-226 tain period at multiple locations around the basin. This ANN is optimized to min-227 imize the mean squared error between the predicted and actual river water levels. 228 Adam optimizer was used to update parameters. Dropouts were applied to avoid 229 over-fitting. Learning stops after a predetermined number of epochs. The number of 230 neurons in the middle layer, batch size, learning rate, dropout rate, and number of 231 epochs are subject to hyperparameter tuning. 232

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3.3 Prior knowledge and proposed INN architecture

We propose an INN integrating two prior knowledge into an ANN to prevent performance degradation on limited training data. The first knowledge is the rainfallrunoff and water level relationship. The rainfall refers to precipitation, especially in the basin to be forecasted, and runoff refers to the water moving over and unmanuscript submitted to Water Resources Research



Figure 2. Architecture of conventional ANN. It has three middle leyar and with multiple inputs and one output. The input includes river water level at forecast location, river level at upstream location and precipitation in the basin.



Figure 3. A block diagram showing the relationship between rainfall-runoff and water levels. Rainfall flows into the basin, merges with the upstream flow of the river, and affects water levels.

der the surface of the land in the basin area. Understanding this relationship and 238 deriving flow rate into rivers is one of the significant interests of river engineering. 239 Then, the rainfall-runoff and water level relationship can be understood as shown 240 in the block diagram in Figure 3. First, rain falls on the basin, and the water flows 241 upstream through various pathways. Next, the volume of water from the river up-242 stream is combined to form the river. This flow rate and physical shape define the 243 water level at a point of the river. Integrating this prior knowledge into the ANN is 244 performed by modifying the structure of the NN as shown in figure 4 to mimic the 245 block diagram in figure 3. First, the network is divided into two parts. Part 1 is a 246 NN that converts rainfall in a watershed to river flow. Part 2 is a NN that converts 247 the amount of water from the basin to the river and the flow rate from upstream 248 to the predicted water level. The inputs are the precipitation in the basin to Part 1 249 and the river level upstream to Part 2. Part1 outputs three kinds of vector named 250 $\Delta S, R, Q$, and ΔS is the input to Part2. This network architecture modification 251 aims to create a model that suits the task of flood forecasting. 252

The second piece of prior knowledge is the tank model. As mentioned above, 253 the rainfall-runoff relationship is a significant issue in river engineering, and many 254 models have been proposed to explain its behavior. The tank model simulates a 255 basin as a tank and models the relationship between rainfall, basin storage, and 256 runoff. In the tank model, rainfall is fed into the tank, some of it accumulates, and 257 some water flows out as runoff. This model is one of the simplest rainfall-runoff 258 models, and this tank model was chosen for its simplicity of integration into the 259 INN. The tank model is composed of three variables, as follows: 260

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$$\Delta S(t) = R(t - \tau) + Q(t) \tag{1}$$

t is the time each value was observed. τ is the time delay between rainfall-runoff. 262 $\Delta S(t)$ is water strage change in the tank (basin). $R(t-\tau)$ is precipitation with time 263 delay. Q is the runoff flow rate. Equation 1 represents the relationship between rain-264 fall with time delay and conservation of tank storage and runoff. The integration 265 of the tank model into the ANN is done in the following procedure. The output of 266 Part 1, which is responsible for rainfall-runoff, is divided into the tank model vari-267 ables: rainfall R, tank storage change ΔS , and runoff Q. Next, add the penalty term 268 $loss_{penalty}$ shown below to the loss function. 269

$$loss_{penalty} = \sum_{i \in n} |\Delta S_i(t) - R_i(t - \tau) - Q_i(t)|$$
(2)

²⁷¹ *n* is a predefined number of elements in each vector output from part 1. This is the ²⁷² just transition of the term $R(t - \tau)$ and Q(t) in Equation 1 and when $loss_{penalty} = 0$ ²⁷³ Equation 2 is equivalent to Equation 1. And each outputs ΔS , R, Q in 4 are cor-²⁷⁴ resoponding to $\Delta S_i(t)$, $R_i(t - \tau)$, $Q_i(t)$ in Equation 2. Since this penalty term is



Figure 4. The proposed INN architecture. It is designed to simulate the relationship between rainfall-runoff and water levels. This architecture has two parts: Part1 and Part2. Part1 has precipitation input, and Part2 has Part1 output and water level input.

optimized to be zero during the learning process, it is expected that Part 1 will be 275 optimized to mimic the behavior of the tank model. Moreover, since $\Delta S(t)$ is de-276 fined as having a linear relationship with the amount of runoff to the river, $\Delta S(t)$ 277 of Part 1 in Figure 4 is input to Part 2. Note that these two changes are not math-278 ematically complete constraints that satisfy the tank model and rainfall-runoff rela-279 tionship. Thus the output of Part 1 need not match the values of each variable when 280 the tank model is built for the same basin. Same as conventional ANN, the number 281 of neurons in the middle layer, batch size, learning rate, dropout rate, and number 282 of epochs are subject to hyperparameter tuning. 283

3.4 Model Development

The same gauging and perception data are used for the ANN and the devel-285 opment of the proposed INN. ANN and INN were optimized to minimize the mean 286 squared error of training data. The model is trained with the water level at time 287 t + n, n hours ahead of the Hiwatashi gauging station at time t, as the objective 288 value. The inputs to the model are the water level at Hiwatashi gauging station at 289 time t and one hour ahead at time t-1, the water level upstream at time t, t-1, t-2290 and the hourly rainfall from t + n - 1 to t + n - 5 at the precipitation gauging 291 location. Note that the actual rainfall values are used to train and test even if the 292 rainfall values are in the future from time t. The Adam optimizer was used in the 293 training process for each model. Hyperparameter tuning is performed by grid search 294 for the number of training epochs, the number of neurons in the middle layer, the 295 learning rate, and the dropout rate. The data used for development is divided into 296 training data and validation data for hyperparameter tuning, which are separated 297 from test data. 298

299 4 Result

Two comparisons were conducted to compare the INN and some conventional methods. The results were evaluated in terms of RMSE. The RMSE is obtained by the following,

$$RMSE = \sqrt{\frac{1}{N} \Sigma_t \left(L(t) - L_{prediction}(t) \right)^2}$$
(3)

N is the number of water level samples. L(t) is the water level at time t, $L_{prediction}$ is the predicted water level at time t.

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4.1 Comparison with conventional methods for a sufficient amount of training data

The result of the conventional ANN and the proposed method forecast for the 308 Hiwatashi gauging station is shown in Figure 5 and Figure 6 The prediction results 309 follow the transition of the ground truth. During periods of water level over three 310 meters (between two gray dashed lines), the predictions are more consistent with 311 the ground truth than the results of ANN in case of the year 2004 and 2005. Both 312 the ANN and the INN predictions are unstable in the year 1990 and 1993. These 313 unstable predictions may be due to noise in the input observed variables in these 314 test sets. 315

The RMSE of the flood forecast results at the Hiwatashi gauging station is shown in Figure 7. Conventional methods are ANN, a hybrid of ANN and distributed runoff model (hybrid), distributed runoff model (runoff), embedding, and the proposed method. In addition, ANN1 is the result traced from Hitokoto et al. (2017), and ANN2 is the result of in-house code. The difference between ANN1 and ANN2



Figure 5. Forecast for the Hiwatashi gauging station in the year 1990, 1993, 2004, and 2005 by conventional ANN2 model. The black points with black lines denote the observed river level as ground truth, and the red solid line shows the forecast river level up to 6 hours ahead. The area between the two gray dotted lines displays the range of data over which the RMSE was evaluated.

is that it uses a framework for implementation, and hyperparameter tuning is per-321 formed on a test set and a separate validation set. Figure 7 -(a), (b), (c), and (d) 322 show the results for 1990, 1993, 2004, and 2005. The RMSE for ANN1, hybrid, runoff, 323 and embedding is traced from Hitokoto et al. (2017) and Okuno et al. (2021). Each 324 figure shows the RMSE of the predicted and actual values for the 1 to 6 hourly fore-325 cast horizons. Each method's RMSE is distributed in the $0.04 \ m$ to $1.2 \ m$ range. In 326 the case of the proposed method, the values are distributed in the range of 0.038 m327 to 0.85 m, and it was never the worst accuracy in all cases. In case (a)Year 1990, 328 the RMSE proposed becomes large when forecasting 5 hours, but in all other years, 329 the RMSE is about the same compared to other methods. Unlike other results, the 330 proposed method and ANN2 are hyperparameter-tuned with a test set and a com-331 pletely isolated validation set. Considering this difference in experimental conditions, 332 the proposed method has sufficient performance. Based on this result, the domain 333 knowledge which was combined with INN does not cause performance degradation 334 even in the condition of not limited training data. 335

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4.2 Sensitivity analysis about the number on the flood data in the training data

The proposed method should maintain high performance even under condi-338 tions where there is not a sufficient amount of data. To verify the performance of 339 INN under such conditions, we performed a sensitivity analysis. The RMSE at the 340 Hiwatashi gauging station with different test data is shown in Figure 8 and Figure 341 9. We compared the conventional method (ANN2) and the proposed method in this 342 study. Each figure shows the result for 1993 and 2004. In Figure 8, for (a)1 hour 343 forecast and (b)3 hours forecast, the RMSE of INN does not increase as the number 344 of flood events in the training data decreases. On the other hand, in conventional 345 ANN2, the RMSE tends to rise rapidly as the number of flood data becomes smaller. 346 The RMSE value of Proposed is smaller than that of ANN2 when the training set 347 has less number of flood data (6 >). In the (c)6 hours forecast, the magnitude of 348



Figure 6. Forecast for the Hiwatashi gauging station in the year 1990, 1993, 2004, and 2005 by proposed INN model. The black points with black lines denote the observed river level as ground truth, and the red solid line shows the forecast river level up to 6 hours ahead. The area between the two gray dotted lines displays the range of data over which the RMSE was evaluated.

Proposed RMSE changes more than in (a) and (b) for the number of flood data. 349 Under conditions where the number of flood data is five or less, three-quarters of the 350 cases have a smaller RMSE than ANN2. The result in Figure 9 has the same trend 351 as in Figure 8. The RMSE value of Proposed is smaller than that of ANN2 when the 352 training set has less number of flood data (5 >). In the (c)6 hours forecast, the mag-353 nitude of Proposed RMSE changes more than in (a) and (b) for the number of flood 354 data. Same as Figure 8, under conditions where the number of flood data is five or 355 less, three-quarters of the cases have a smaller RMSE than ANN2. 356

357 5 Disscusion and Conclusion

In this study, we proposed a novel approach to flood forecasting methods with 358 NNs. The proposed method is an INN that integrates existing knowledge of rainfall-359 runoff, river-level relationships, and the tank model in river engineering with con-360 ventional ANNs. Integrating the existing knowledge into the INN was performed by 361 modifying the network architecture and adding a penalty term. These two changes 362 aim to improve the initial conditions and the learning process of NNs. We applied 363 the proposed INN to a real-world river in Japan to test its performance. Under con-364 ditions where there was sufficient training data, the proposed INN was performed, 365 as well as several critical conventional methods. When the training data was lim-366 ited, it significantly outperformed the conventional ANN. This difference tended to 367 increase as the forecast horizon became small. The improvement in results is due to 368 changes in the network architecture based on existing knowledge and the addition of 369 a penalty term. This change is assumed to be due to the initial learning conditions 370 and the optimizer's contribution to improving the learning process. These results are 371 a new contribution that shows a practical way to improve the accuracy of INNs with 372 a limited amount of training data. The proposed INN will enable the provision of 373 flood forecasting systems with a short development time in areas where flood fore-374 casting has not been installed, thereby reducing the risk to life during floods. INN 375



Figure 7. RMSEs of 1 to 6-hour forecasts for 4 test cases (a)year 1990,(b) year 1993,(c)year 2004, and (d)year 2005. We compared the performance of the proposed method with that of ANNs from the literature (ANN1), the distributed runoff-rainfall model (runoff), the hybrid model of ANN and runoff (hybrid), predictions based on dynamical system theory (embedding), and the performance of ANNs based on in-house experimental codes (ANN2). Note that the results for ANN1, runoff, hybrid, and embedding were scanned for values from Hitokoto et al. (2017) and Okuno et al. (2021)



Figure 8. RMSE for 1993 test data versus the number of flood data in the training data set. The red line is the proposed method, and the black line is the conventional ANN with in house implementation (ANN2).



Figure 9. RMSE for 2004 test data versus the number of flood data in the training data set. The red line is the proposed method, and the black line is the conventional ANN with in house implementation (ANN2).

will help to cope with heavy rainfall in unprecedented areas due to recent climate change. Overall, we obtained favorable results for the questions set in section 2.

The future work of this research is the following two. First, the INN proposed 378 in this study was designed to integrate two simple pieces of existing knowledge for 379 ease of implementation. Therefore, the performance when other existing knowledge 380 is integrated has yet to be discovered, and what kind of existing knowledge is more 381 suitable for integration is an important question. Second, the river tested in this 382 study is the only one in Japan, and its performance in other Japanese rivers and 383 rivers around the world with larger basins is still being determined. So, evaluation of 384 the proposed INN on more diverse rivers is necessary. In addition, the performance 385 of the proposed technology for more complex phenomena where factors other than 386 rainfall affect floods is also the subject of future research. 387

6 Open Research Section

The rainfall and river water level data used in this study are freely available at (Ministory of Land, Infrastructure, Transport, and Tourism in Japan, 2021)(http://www1.river.go.jp/). The data is freely accessible, but you must select a location and time period. Re-

lated metadata (location name and time period) is listed in (Hitokoto et al., 2017).

The elevation map data is freely available at (Geospatial Information Authority of

Japan, 2020)(https://maps.gsi.go.jp/vector/#7).

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