Validation of subgrain-size piezometry as a tool for measuring stress in polymineralic rocks

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Abstract

We deformed samples with varied proportions of olivine and orthopyroxene in a deformation-DIA apparatus to test the applicability of subgrain-size piezometry to polymineralic rocks. We measured the stress within each phase in situ via X-ray diffraction during deformation at a synchrotron beamline. Subgrain-size piezometry was subsequently applied to the recovered samples to estimate the stress that each phase supported during deformation. For olivine, the final in-situ stresses are consistent with the stresses estimated via subgrain-size piezometry, both in monomineralic and polymineralic samples, despite non-steady state conditions. However, stress estimates from subgrain-size piezometry do not reliably record the in-situ stress in samples with grain sizes that are too small for extensive subgrain-boundary formation. For orthopyroxene, subgrain boundaries are typically sparse due to the low strains attained by orthopyroxene in olivine-orthopyroxene mixtures. Where sufficient substructure does exist, our data supports the use of the subgrain-size piezometry to strong minerals that may have experienced little strain. Stresses estimated by X-ray diffraction also offer insight into stress partitioning between phases. In mixtures deformed at mean stresses > 5 GPa, orthopyroxene supports stresses greater than those supported by olivine. This stress partitioning is consistent with established theory that predicts a slightly higher stress within a 'strong' phase contained in a material consisting of interconnected weak layers. Overall, these results demonstrate that subgrain-size piezometry is a valuable tool for quantifying the stress state of polymineralic rocks.

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10 Key Points:

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Subgrain sizes are insensitive to the presence of secondary phases in polymineralic rocks.

The grain size of a rock influences what portion of the deformation history the sub grain size records.

Stresses estimated from individual phases in a mixture do not necessarily record the
 bulk stress applied to the rock.

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17 Abstract

We deformed samples with varied proportions of olivine and orthopyroxene in a 18 deformation-DIA apparatus to test the applicability of subgrain-size piezometry to polymin-19 eralic rocks. We measured the stress within each phase in situ via X-ray diffraction during 20 deformation at a synchrotron beamline. Subgrain-size piezometry was subsequently ap-21 plied to the recovered samples to estimate the stress that each phase supported during 22 deformation. For olivine, the final in-situ stresses are consistent with the stresses estimated 23 via subgrain-size piezometry, both in monomineralic and polymineralic samples, despite 24 non-steady state conditions. However, stress estimates from subgrain-size piezometry do 25 not reliably record the *in-situ* stress in samples with grain sizes that are too small for exten-26 sive subgrain-boundary formation. For orthopyroxene, subgrain boundaries are typically 27 sparse due to the low strains attained by orthopyroxene in olivine-orthopyroxene mix-28 tures. Where sufficient substructure does exist, our data supports the use of the subgrain-29 size piezometer on orthopyroxene. These results do, however, suggest that care should 30 be taken when applying subgrain-size piezometry to strong minerals that may have ex-31 perienced little strain. Stresses estimated by X-ray diffraction also offer insight into stress 32 partitioning between phases. In mixtures deformed at mean stresses > 5 GPa, orthopy-33 roxene supports stresses greater than those supported by olivine. This stress partitioning 34 is consistent with established theory that predicts a slightly higher stress within a 'strong' 35 phase contained in a material consisting of interconnected weak layers. Overall, these re-36 sults demonstrate that subgrain-size piezometry is a valuable tool for quantifying the stress 37 state of polymineralic rocks. 38

³⁹ Plain Language Summary

To measure the stresses previously supported by exhumed lower-crustal and upper-40 mantle rocks, we rely on examining features in the rocks that have a calibrated relationship 41 with stress. One such metric is based on the size of subgrains, which are distinct crys-42 tallographic regions within individual grains that comprise a rock. Experiments on rocks 43 composed of a single mineral have shown the subgrain size to have an inverse relationship 44 with stress. However, the majority of rocks are composed of multiple minerals. In addition, 45 subgrain sizes generated in the experiments used in the calibrations each record a single, 46 steady-state stress, whereas natural rocks are often subject to complex stress histories. 47

We test the applicability of using subgrain size to estimate stress in rocks containing more than one mineral through high-temperature, high-pressure experiments paired with *in-situ* X-ray diffraction. Results indicate that stresses estimated from subgrain sizes in rocks composed of more than one mineral are a good indication of the final stress experienced by a sample regardless of the deformation history. However, additional parameters, such as the amount of strain and the grain size relative to the subgrain size, need to be considered when applying this method to natural rocks.

55 **1 Introduction**

Paleostress estimates from exhumed rocks provide critical insight into the mechanical 56 state of Earth's lithosphere (e.g., Kohlstedt & Weathers, 1980), strain localisation along plate 57 boundaries (e.g., Ambrose et al., 2018; Boutonnet et al., 2013), and elastic loading of the 58 mid-crust through the earthquake cycle (e.g., Trepmann & Seybold, 2019). Such stresses 59 can be estimated via paleopiezometry, that is, the relationship between stress and specific 60 microstructural features (e.g., Nicolas, 1978; Tullis, 1979). The most widely implemented 61 paleopiezometer is based on the mean size of dynamically recrystallised grains, which 62 follows an inverse power law with differential stress in monomineralic rocks (e.g., Karato et 63 al., 1980; Luton & Sellars, 1969; Shimizu, 2008; Stipp & Tullis, 2003; Twiss, 1986). However, 64 grain sizes in a polymineralic rock can be influenced by the presence of secondary phases 65 that pin migrating grain boundaries (Cross & Skemer, 2017; Evans et al., 2001; Hiraga et 66 al., 2010; Smith, 1948; Tasaka et al., 2017). Consequently, grain-size piezometry tends to 67 overestimate paleostresses when applied to well-mixed polymineralic rocks (e.g., Hansen 68 & Warren, 2015). 69

An alternative proxy for paleostress in polymineralic rocks is subgrain size (Twiss, 70 1986). Subgrains are crystallographic regions enclosed by low-angle (typically $< 10-15^{\circ}$) 71 boundaries within individual grains (Karato, 2012, page 94). As with grain size, an inverse 72 relationship exists between differential stress and the spacing of subgrain boundaries (e.g., 73 Durham et al., 1977; Karato et al., 1980; Raleigh & Kirby, 1970; Servi et al., 1952; Toriumi, 74 1979). However, subgrain-size piezometry offers three potential advantages over grain-75 size piezometry. First, low-angle boundaries have lower mobilities than grain boundaries 76 (e.g., Huang et al., 2000) and are therefore more resistant to post-kinematic static annealing 77 (Qin et al., 2003). Second, mean subgrain sizes exhibit the same relationship with stress in 78 both relict and recrystallized grains (see Figure 8 in Ross et al., 1980, and Figure 6 in Trimby 79

et al., 1998) meaning no distinction is required between the two grain populations. Finally,
 for a given stress, subgrain size is thought to be unaffected by the presence of secondary
 minerals (Hansen & Warren, 2015; White, 1979).

Recently Goddard et al. (2020) calibrated a new subgrain-size piezometer using elec-83 tron backscatter diffraction (EBSD), a widely used technique for characterising microstruc-84 tural features. This new piezometer was calibrated using both olivine and quartz, resulting 85 in a generalised relationship that could potentially be applied to other minerals without 86 the need for additional calibration. Subgrain size therefore provides a powerful tool for 87 estimating stress from natural polymineralic rocks. Nevertheless, two key uncertainties 88 remain. First, although subgrain sizes should be unaffected by the presence of secondary 89 phases as they are intragranular features (Hansen & Warren, 2015; White, 1979), no study 90 has directly tested this idea. Second, it is unclear how subgrain size relates to stress under 91 non-steady-state conditions. Nearly all piezometers are calibrated using experiments in 92 which stress has reached a steady state (e.g., Karato et al., 1980; Stipp & Tullis, 2003), and 93 thus the statistics of microstructural features are likewise assumed to be invariant with fur-94 ther strain. Recent work has been conducted to explore how grain size responds to changes 95 in stress (e.g., Kidder et al., 2016; Soleymani et al., 2020), however, the equivalent published 96 work on subgrain-size piezometry is limited and inconclusive. As natural rocks often un-97 dergo significant stress changes, for example during exhumation (Behr & Platt, 2011) or 98 during the seismic cycle (e.g., Campbell & Menegon, 2019; Menegon et al., 2021), under-99 standing how subgrain sizes respond to changing stresses is vital to accurately interpreting 100 the rock record. 101

To address these questions, we conducted experiments on synthetic polymineralic 102 samples of olivine and orthopyroxene using a deformation-DIA (D-DIA) apparatus at 103 beamline 6-BM-B of the Advanced Photon Source synchrotron, Argonne National Labo-104 ratory, Illinois. To explore the extent to which subgrain size tracks stress in non-steady-105 state systems, we incorporated temperature and strain-rate steps into most experiments. 106 We compared stresses measured *in situ* via X-ray diffraction to those estimated from EBSD 107 maps of recovered samples and the subgrain-size piezometer of Goddard et al. (2020). In 108 addition, we explored how stress partitioning between phases in the polymineralic aggre-109 gates compared to Handy's (1994) model for two-phase flow. 110

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Our results support the hypothesis that subgrain sizes are unaffected by the presence 111 of secondary phases. The stresses estimated from subgrain-size piezometry are consistent 112 with the final stresses measured *in-situ*, irrespective of the stress histories that preceded 113 them. Stress partitioning within individual phases is also found to be consistent with that 114 expected from models of like microstructures. As such, this study broadens the applica-115 bility of subgrain-size piezometry to polymineralic natural rocks. However, we also cau-116 tion that careful consideration should be taken when using the subgrain-size piezometer 117 to infer the bulk strength of polymineralic rocks, especially in low-strain or fine-grained 118 samples. 119

120 2 Methods

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2.1 Sample Synthesis

D-DIA experiments consisted of a stack of two samples deformed in series. Figure 1 illustrates a typical sample assembly. One of the samples was commonly olivine, which was used as a stress sensor in the experiments. Given the use of olivine to calibrate the original subgrain-size piezometer, these monomineralic samples were also used as a control when comparing stress measurements from X-ray diffraction to those from piezometry. Other samples consisted of olivine orthopyroxenite or harzburgite, which contained 85 vol.% and 30 or 50 vol.% of orthopyroxene, respectively.

Samples were synthesised either at Brown University or the University of Minnesota. 129 LT-DrySC, a dry olivine sample, was synthesised at Brown University from San Carlos 130 olivine with particle sizes 10–32 μm. This dry olivine was made from a 'wet olivine', which 131 had \sim 0.5–0.7 wt% deionised water added to the olivine powder prior to hot pressing. Pow-132 ders were sealed in a nickel jacket and hot pressed at a confining pressure of 1.3 GPa and 133 temperature of 900°C for 24–26 hours in a triaxial, Tullis-modified Griggs apparatus, us-134 ing solid NaCl as the confining medium. To dehydrate, the sample was placed in a 1 atm 135 CO/CO₂ furnace at 1000°C and a P_{O_2} of ~10⁻¹⁰ atm for 10 hours. 136

At the University of Minnesota, samples were synthesised from powders of Bamble enstatite and San Carlos olivine, with particle sizes < 10 μm. For samples 33 and PT-1166, powders of olivine were combined with 1% enstatite to buffer the silica activity. For sample PT-1299HiFe, enstatite was mixed in ethanol with olivine powder in a 30:70 ratio. For PI-2056, powders of enstatite and pure olivine were similarly prepared, as well as 50:50 and



Figure 1. Schematic illustration of a typical D-DIA sample assembly, modified from Durham et al. (2002) and Hansen et al. (2019).

85:15 ratios of enstatite to olivine. Powders were tumbled for at least 12 hours in a plastic 142 bottle with plastic-coated iron balls and subsequently dried on a hot plate at 60°C until all 143 the ethanol had evaporated. Powders were then placed in a 1 atm CO/CO₂ furnace, with 144 a P_{O_2} of $\sim 10^{-10}$ atm, in which temperature was ramped up to 1000°C over 10 hours and 145 then held constant for 12 hours before cooling. The sample powders were cold pressed 146 at \sim 100 MPa into a Ni can on top of a layer of NiO powder, which was present to buffer 147 oxygen fugacity. For sample PI-2056, the cold press consisted of roughly equal layers of 148 the aforementioned different compositional ratios. Samples were vacuum hot-pressed in a 149 gas-medium apparatus at a vacuum pressure on the interior of the jacket of ~ 10 Pa and at a 150 confining pressure of 300 MPa (Meyers et al., 2017). Hot presses were carried out at 1250°C 151 under a small uniaxial load (~1 MPa) to aid compaction. For PT-1299HiFe and PI-2056, the 152 hot press was continued until compaction effectively ceased, which took between 0.5 and 153 1.3 hours. Samples 33 and PT-1166 were part of a series that were hot-pressed for between 154 3 and 60 hours to produce different grain sizes. 155

156 **2.2 Sample Assembly**

Hot presses were cored using a diamond coring drill to produce right-cylindrical sam-157 ples of diameters 1.05-1.19 mm, which were subsequently ground to a height of 0.55 ± 0.05 158 mm. For each experiment, a pair of samples were stacked between dense alumina pistons 159 and then machinable alumina. Discs of nickel foil were placed between each component 160 within the assembly to act as strain markers and also control the oxygen fugacity at the 161 Ni/NiO buffer. The circumference of the samples was also wrapped in Ni foil. The assem-162 bly stack was placed within concentric sleeves of MgO and graphite, which provided an 163 insulator and a resistive heater, respectively (See Figure 1). All components were placed 164 inside a mullite sphere, which acted as the solid confining medium, itself residing within 165 a pyrophyllite cube. The pyrophyllite cells were soft-fired for 3 hours at 900°C prior to 166 sample assembly, which enabled them to flow during initial compression to form a gasket 167 between the six anvil cells. Completed assemblies were sealed using a zirconia cement, 168 ground to be square, and then left in an oven at \sim 120°C for \geq 2 hours to ensure an anhy-169 drous state. 170

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2.3 Experimental Procedure

We generated the desired stress state in the sample in the same manner as previous 172 investigations implementing D-DIA experiments (Durham et al., 2009; Mei et al., 2010; 173 Wang et al., 2003; Weidner et al., 2010). Pressure was applied to the pyrophyllite assembly 174 cube through a hydraulically-loaded anvil in contact with each cube face. Pressurisation 175 from the main loading ram applied equal load to all six anvils simultaneously, generating a 176 hydrostatic compressive stress. Temperature was controlled using a calibrated relationship 177 with heater power, as the inclusion of a thermocouple tends to degrade the mechanical 178 stability of the sample assembly (Dixon & Durham, 2018). Once target pressures, here 179 equivalent to mean stress ($(\sigma_v+2\sigma_h)/3$), and temperatures were reached, differential stress 180 was generated by independently advancing the vertical anvils, each controlled by driving 181 a hydraulic syringe pump at a constant rate. Due to compressibility of the syringe fluid, 182 the experimental boundary conditions are neither truly constant strain rate nor constant 183 load. Moreover, changes in heater power (i.e., temperature) led to minor changes in the 184 strain rate of the sample during an experiment. Nevertheless, nominally constant strain 185 rates were reached after an initial loading phase. Meanwhile, the main ram was servo 186 controlled to maintain a nominally constant mean stress (Durham et al., 2002). 187

During each experiment, a high-energy, white X-ray source was used to provide *in-situ* 188 stress and strain measurements via energy-dispersive X-ray diffraction and X-ray radiog-189 raphy, respectively. Ten solid-state detectors were arranged downstream of the sample at 190 a variety of fixed azimuths (ψ) and at an angle of 6.5° (2 θ) to the beam direction (Figure 191 1). The Bragg angle of 6.5° was fixed through the use of conical slits and provided a col-192 limated signal that ensured X-rays arriving at the detectors were diffracted from within 193 the sample, and not from the surrounding assembly components. Each analysed peak 194 within the diffraction spectrum corresponds to an $\{hkl\}$ plane whose atomic spacing, or 'd-195 spacing', was calculated through Bragg's law and the fixed diffraction angle. This energy-196 to-d-spacing conversion, as well as the Bragg angle, was calibrated at least once every seven 197 experiments (typically every two days) using an alumina-powder standard. 198

Diffraction spectra were collected, alternating between the top and the bottom samples, for durations of 20 to 60 seconds depending on the clarity of the peaks. Peaks used in this analysis are highlighted in Figure 2 and correspond to the {130}, {131}, and {112} planes in olivine and the {421}, {610}, and {321} planes in orthopyroxene.



Figure 2. X-ray diffraction spectrum collected for 20 seconds in a harzburgite sample. The measured data are plotted as a blue line. Green and orange lines represent key diffracting planes in olivine and orthopyroxene, respectively. Peak labels outlined in bold are those used to measure stress in this experimental series.

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Mean stress and differential stress were calculated from the measured *d*-spacing of $\{hkl\}$ peaks following previous work (e.g., Durham et al., 2009; Hansen et al., 2019; Mei et al., 2010; Wang et al., 2013; Weidner et al., 2010). Mean stress (*P*) was measured from the $\{130\}$ peak of olivine, calculated using the third-order Birch-Murnaghan equation of state for olivine,

$$P = \left(\frac{3\left(K_{0} + K_{\rm T}^{'} \triangle T\right)}{2}\right) \left[\left(\frac{V_{0,\rm T}}{V}\right)^{\frac{7}{3}} - \left(\frac{V_{0,\rm T}}{V}\right)^{\frac{5}{3}}\right] \left\{1 + \frac{3}{4}\left(K_{\rm P}^{'} - 4\right) \left[\left(\frac{V_{0,\rm T}}{V}\right)^{\frac{2}{3}} - 1\right]\right\},\tag{1}$$

where ΔT is the difference in temperature relative to the temperature at which the thermal expansion measurements were made, K_0 is the bulk modulus and K'_T and K'_P are the temperature and pressure derivatives of K_0 , respectively. Values of 129.4 GPa for K_0 and 4.29 for K'_P were taken from Abramson et al. (1997). For K'_T , a value of -0.0224 GPa K⁻¹ was taken from Kumazawa and Anderson (1969). The unit-cell volume, V, was calculated for each diffraction pattern during the experiment through

$$V = \left[d_{\rm p} \left(h^2 + k^2 + l^2 \right)^{\frac{1}{2}} \right]^3, \tag{2}$$

where $d_{\rm p} = \frac{d_{\rm v}+2d_{\rm h}}{3}$, $d_{\rm v}$ is the *d*-spacing measured at the vertical azimuth, and $d_{\rm h}$ is the *d*-spacing measured at the horizontal azimuth. To calculate $d_{\rm h}$ and $d_{\rm v}$, *d*-spacing was plotted against ψ and then a sine wave was fit to the data. $d_{\rm h}$ and $d_{\rm v}$ were taken to be the maximum and minimum of the sine wave, which sit 90° apart. $V_{0,\rm T}$ is the unit-cell volume at the experiment temperature and ambient pressure, and is calculated as

$$V_{0,\mathrm{T}} = V_0 \exp\left(2.55 \times 10^{-5} \times (T - T_0) + \frac{1}{2} \times 1.15 \times 10^{-8} \times (T^2 - T_0^2)\right),\tag{3}$$

where V_0 is the unit-cell volume at ambient temperature and pressure, T is the temperature,

and T_0 is the temperature at which the measurements of thermal expansion were made.

²²¹ Differential stress, σ , was calculated using the difference in *d*-spacing between the ²²² horizontal and vertical directions,

$$\sigma = \left(\frac{1}{2G_{\rm R}}\right)^{-1} \frac{d_{\rm h} - d_{\rm v}}{d_{\rm p}},\tag{4}$$

where $G_{\rm R}$ is the X-ray shear modulus calculated assuming the Reuss (isostress) condition (Singh et al., 1998) and using the elastic constants from Abramson et al. (1997) and Isaak (1992).

Prior to fitting peaks in the diffraction data, the intensity spectra were smoothed using 226 a Savitzky-Golay filter and interpolated with a spline function. Due to the complicated 227 diffraction patterns present in mixtures of olivine and orthopyroxene, peak locations were 228 identified by fitting Gaussians to the highest intensity portions of each individual peak, 229 rather than by fitting a mixing model of multiple Gaussians. When compared to the peak-230 fitting model (peakfit.m, O'Haver, 2018, page 340-358) used by Hansen et al. (2019) on 231 a representative set of diffraction patterns for monophase olivine, stress and mean stress 232 measurements were similar. 233

Axial strain was obtained by using digital image cross-correlation to precisely measure the positions of the nickel-foil strain markers in X-ray radiographs. By applying this technique, we were able to resolve subpixel shifts in foil location, resulting in precision in axial strain measurement of 10^{-5} to 10^{-4} (Hansen et al., 2019).

Deformation experiments were conducted at temperatures and mean stresses of 238 800–1270°C and 1.6–9.7 GPa, respectively. Prior to deformation, each sample was annealed 239 at temperatures of 800–1100°C for 5–20 minutes to relax any internal stress heterogeneity 240 introduced during pressurisation (see Figure 1 of Wallis et al., 2020). To test which portion 241 of the stress history the subgrain size records, all except one experiment were subjected to 242 either steps in temperature, steps in strain rate, or both. At the end of each experiment, 243 samples were quenched, the vertical anvils were withdrawn, and mean stress from the 244 main loading ram was decreased slowly under approximately hydrostatic conditions. 245

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2.4 Microstructural Analysis

To prepare the samples for microstructural analysis after deformation, the graphite furnace and all components within were extracted from the sample assembly and mounted on a glass slide using Logitech Epothin resin. Thick sections were formed by grinding the experimental column down on a Buehler Petrothin, at the University of Oxford, until it was a thickness of 1.2–1.8 mm. The ground surface was subsequently remounted on a fresh glass slide, the old glass slide removed, and the new free surface ground until a central section of the sample remained. At this stage, blobs of UV resin were placed around the edges of the slides to help stabilise the samples during final polishing. Samples were then
 reground on the Petrothin to thicknesses in the range 0.2–0.6 mm with a flat central section
 exposed for polishing. All surfaces were polished with a Planocloth polishing cloth, 0.3
 µm alumina powder, and water for 2–4 hours. Samples were subsequently polished with
 colloidal silica, as necessary, for 0.3–2.5 hours. Prior to EBSD data collection, samples were
 coated with 5–8 nm of carbon to minimise charging in the scanning electron microscope.

EBSD data were collected on a field-emission gun scanning-electron microscope (FEG-260 SEM) either at the Department of Earth Sciences, University of Oxford; the Marine Biolog-261 ical Laboratory (Woods Hole); or the Characterization Facility, University of Minnesota. 262 At the University of Oxford, data were collected on an FEI Quanta 650 E-SEM equipped 263 with Oxford Instruments AZtec acquisition software and a NordlysNano EBSD camera. At 264 the Marine Biological Laboratory, data were collected using a Zeiss Supra 40VP FEG-SEM 265 equipped with an Oxford Instruments Symmetry EBSD detector. At the University of Min-266 nesota, EBSD data were collected using a JEOL 6500 FEG-SEM with an Oxford Instruments 267 Symmetry S2 EBSD detector. In all three systems, samples were tilted to 70° and mapped 268 at either low-vacuum (50–70 Pa $m H_2O$ or $m N_2$) or high-vacuum conditions, at an accelerating 269 voltage of 20-30 kV, with a step size of 0.075-0.5 µm. Collection conditions for individual 270 samples can be found in Supplementary Table S1. 271

Data were processed using a combination of Oxford Instruments' Channel5 or AZtec-272 Crystal software and the MTEX toolbox (version 5.7) for MATLAB[®] (Bachmann et al., 2010). 273 First, spurious olivine pixels with systematic misindexing due to pseudosymmetry were 274 corrected by applying a rotation of 60° around [100] (Bystricky et al., 2006) in Channel5 275 or AZtecCrystal. EBSD data were then processed with the MTEX toolbox. Isolated pixels 276 and "grains" comprised of < 3 pixels were removed. Pixels with mean angular deviation 277 (MAD) values > 1° were also removed. Subsequently, all non-indexed pixels, which com-278 prise 2–38% (average 21%) of each map, were filled in MTEX using a nearest-neighbour 279 method, whereby empty pixels are assigned the phase and orientation of the nearest in-280 dexed pixel. Interpolation was required for subgrain-size analysis as the centre of non-281 indexed regions are set to be boundaries in the current line-intercept MATLAB script, and 282 could therefore result in inaccurate stress estimates. Figure S1 in the supplementary infor-283 mation presents phase maps of EBSD data prior to the infill of non-indexed regions. 284

To test the effect of indexing rate on the piezometric stress measurements, samples were further polished with colloidal silica and new maps were collected for the olivineorthopyroxenite sample in San502 and for both the olivine stress sensor and harzburgite samples in San508, two key samples where the original maps contained high proportions of non-indexed pixels (25–40%). Despite the indexing rate being increased by up to 27%, the change in estimated stress was generally negligible (between 0–15%), and has no effect on the overall conclusions of this work.

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2.5 Subgrain-size Piezometry

We conducted subgrain size piezometry following the procedures laid out by Goddard 293 et al. (2020). Goddard et al. (2020) presented a single subgrain-size piezometer calibrated 294 from EBSD maps of deformed quartz aggregates and olivine aggregates, in which subgrain 295 size was normalised by the Burgers vector, and differential stress was normalised by the 296 shear modulus. Subgrain size was defined as the average spacing between boundaries with 297 misorientation angles $\geq 1^{\circ}$. As such, it is important to ensure that EBSD maps have angular 298 precision $< 1^{\circ}$ (ideally $< 0.5^{\circ}$) to avoid the creation of spurious 1° boundaries. Here, we 299 find that some EBSD maps contain isolated pixels misoriented from their neighbours by 300 $\geq 1^{\circ}$ (e.g., Supplementary Figure S2), which we attribute to two sources. First, angular 301 uncertainties arising from application of the Hough transform for automated indexing, 302 commonly on the order of 0.5° (Maitland & Sitzman, 2007). Second, high concentrations of 303 isolated geometrically necessary dislocations, not contained within subgrain boundaries, 304 given the relatively high differential stresses (> 1 GPa) experienced by samples in this 305 study. 306

To avoid the inclusion of spurious 1° boundaries, we instead use a modified subgrainsize piezometer (Figure 3), recalculated for a critical misorientation angle of 2° from the EBSD maps used in the original calibration by Goddard et al. (2020) :

$$\frac{\lambda}{b} = 10^{1.1\pm0.3} \left(\frac{\sigma}{\mu}\right)^{-1.1\pm0.1} \tag{5}$$

where λ is the mean line-intercept length, *b*, is the Burgers vector, σ , is the equivalent stress, and μ is the shear modulus. This new calibration also includes an additional cleaning step of removing pixels with mean angular deviation of > 1°. Note that the stresses applied

- to quartz in Figure 3 have also been corrected for friction in accordance with Holyoke and
- ³¹⁴ Kronenberg (2010).



Figure 3. Recalibration of the subgrain-size piezometer based on boundaries with misorientation angles of $\geq 2^{\circ}$. Mean line-intercept length, λ , normalised by the Burgers vector, *b*, is plotted as a function of the equivalent stress, σ , normalised by the shear modulus, μ . The original 1°-piezometer by Goddard et al. (2020) has been added for comparison (dashed black line) as well as the grain-size piezometer for olivine (van der Wal et al., 1993). Currently, no equivalent grain-size piezometer exists for orthopyroxene. For further explanation of the different data subsets, see Goddard et al. (2020).

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For consistency with Goddard et al. (2020), subgrain size was measured using the line-intercept method. To ensure that we used an adequate number of intercepts for robust measurement of the subgrain size, we systematically increased the number of intercepts until the line-intercept length became essentially invariant (varying < 2.5% from the previous measurement). The mean-line intercept length was calculated as the arithmetic mean of intercepts measured both parallel and perpendicular to σ_1 . The mean grain size of each phase, λ_{gs} , was also measured using the line-intercept method with the minimum misorientation angle of a grain boundary defined as 15°, and with no geometric correction applied.

For the initial calibration of the subgrain-size piezometer, temperature and pressure had a negligible impact on the shear modulus and Burgers vector values used to normalise

the piezometer, at least over the range of temperature-pressure conditions used in the cal-326 ibration experiments (Goddard et al., 2020). However, the olivine samples used for the 327 original piezometer calibration were deformed at a pressure of 0.3 GPa, which is signifi-328 cantly lower than the mean stresses used here (1.6–9.7 GPa). These elevated mean stresses 329 have a particularly significant impact on the shear modulus of olivine, which increases 330 by 4–16% relative to its value at room pressure. Therefore, we chose to correct the shear 331 moduli and Burgers vectors of olivine and orthopyroxene using the pressure derivatives 332 given in Table 1. The corrected Burgers vectors and shear moduli give stresses that, on av-333 erage, are 7% greater than those based on using the uncorrected values, with a maximum 334 difference of 12%. 335

For each piezometric stress estimate, an error was calculated using a Monte-Carlo-336 based approach. We assumed that the probability distribution of the subgrain size, pre-337 exponential constant, and exponent all follow lognormal distributions with standard de-338 viations (in log units) of 0.13, 0.3, and 0.1, respectively, and with means given by the mea-339 sured or best-fit values. These standard deviations were determined in the initial calibra-340 tion of the subgrain piezometer, as described in Appendix A. We then randomly drew val-341 ues from these distributions and used them to predict the differential stress. This process 342 was repeated 10,000 times, and the standard deviation in the distribution of differential 343 stresses was taken to be the error in the stress measurement. A full description of this 344 method can be found in Appendix A. 345

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Table 1. Pressure dependence of shear moduli and Burgers vectors for olivine and orthopyroxene

Mineral	G _o (GPa)	$\partial G/\partial P$	$\partial^2 G/\partial^2 P$ (GPa ⁻¹)	<i>b</i> (μm)	$\partial b/\partial P$ (µmGPa ⁻¹)	$\partial^2 b / \partial^2 P$ (µmGPa ⁻²)
Ol Opx	$77.8^{\rm a}$ $78.1^{\rm d}$	$1.71^{\rm b}$ $1.45^{\rm d}$	$-0.054^{ m b}$ 0	$\begin{array}{rl} <\!\!a\!\!> & \!\!4.75^{\rm c}\times10^{-4} \\ <\!\!c\!\!> & \!\!5.20^{\rm e}\times10^{-4} \end{array}$	$-8.377^{\rm b} \times 10^{-3}$ $-1.548^{\rm f} \times 10^{-6}$	$\begin{array}{c} 2.088^{\rm b} \times 10^{-4} \\ 8.2180^{\rm f} \times 10^{-8} \end{array}$

^aMao et al. (2015)

^bAbramson et al. (1997)

^cDeer et al. (1988, page 4)

^dChai et al. (1997)

 $^{\rm e}\textsc{Deer}$ et al. (1988, page 158)

^fAngel and Hugh-Jones (1994)

347 3 Results

348 **3.1 Mechanical Data**

We performed seven experiments in total: one with an olivine stress sensor stacked in series with an olivine-orthopyroxenite sample, five with an olivine stress sensor stacked in series with a harzburgite sample, and one with two samples of harzburgite stacked in series. Table 2 lists the temperatures, strain rates, mean stresses, and final strains for each sample. The final stress indicated by each diffraction peak can be found in Table 3, and the peak and average stresses can be found in Supplementary Tables S2 and S3, respectively.

355

3.1.1 Olivine Stress Sensor Stacked Against Olivine-Orthopyroxenite

Mechanical data for San502, which consisted of an olivine-orthopyroxenite sample 356 stacked against an olivine stress sensor, are displayed in Figure 4. Due to the low propor-357 tion of olivine (15%) within the olivine-orthopyroxenite sample, stresses were only calcu-358 lated for orthopyroxene. Initially, differential stress increased with strain. The apparent 359 Young's modulus of \sim 40 GPa from this period is too low to represent purely elastic de-360 formation, which is associated with an elastic modulus of \sim 200 GPa for olivine. As we 361 measure stresses from the sample directly, we can rule out machine-compliance effects. 362 Therefore, we infer that our experiments yielded early during loading and progressively 363 hardened. 364

Samples were first deformed at a temperature of 800°C and at strain rates of 2.9×10^{-5} 365 s^{-1} and $2.5 \times 10^{-5} s^{-1}$, for the olivine stress sensor and olivine-orthopyroxenite sample, 366 respectively until a strain of 0.016 was reached in the olivine and a strain of 0.014 in the 367 olivine orthopyroxenite. At this point, the displacement rate was decreased resulting in 368 strain rates of 1.9×10^{-5} s⁻¹ in the olivine and 1.4×10^{-5} s⁻¹ in the olivine orthopyroxenite. 369 After a further ~ 0.02 strain, temperature was increased to 900°C so that deformation could 370 continue at a lower differential stress. After the change in temperature, the olivine stress 371 sensor and olivine-orthopyroxenite sample deformed at strain rates of 4.4×10^{-5} s⁻¹ and 372 $2.3 \times 10^{-5} \text{ s}^{-1}$, respectively. 373

During the final deformation step, the average flow stresses in the olivine stress sensor (590–690 MPa) were similar to those measured from the {421} and {321} peaks in orthopyroxene within the olivine-orthopyroxenite sample (620 MPa and 670 MPa, respectively).

- However, stresses measured from the {610} peak in orthopyroxene were considerably
- greater, averaging 1050 MPa.



Figure 4. Stress as a function of strain for experiment San502, which consists of an olivine stress sensor paired against an olivine orthopyroxenite. Stresses from olivine and orthopyroxene are in green and orange, respectively. The red dashed vertical line represents a change in temperature, the black vertical line represents a change in displacement rate, and $\sigma_{\rm M}$ refers to the mean stress during the final conditions of the experiment (see Table 2 for values).

379 3.1.2 Olivine Stress Sensor Stacked Against Harzburgite

Mechanical data for the five experiments consisting of a harzburgite sample and olivine stress sensor are presented as stress-strain curves in Figure 5. Four of these experiments were deformed at temperatures in the range 1100–1270°C and average mean stresses in the range 4.7–9.4 GPa. Experiment San508 was deformed at 900°C and at average mean stresses of 1.6–2.5 GPa.

In all samples except the stress sensors in San391 and San404, stress initially increased with strain. Low apparent moduli from these portions of the stress-strain curves suggest that yielding was instantaneous within the temporal resolution of our experimental measurements. Steeper gradients at < 1% strain in the mixtures in San390 and San404 suggest deformation may have initially been elastic, but data from these segments of loading are sparse.

In most experiments, temperature and/or the displacement rate of the vertical rams were modified during deformation to change the differential stress. During experiments San391 and San396, the temperature was raised to decrease the differential stress. In experiment San404, the displacement rate of the vertical rams was reduced, also to decrease the differential stress. In experiments San396 and San508, the ram displacement rate was instead increased. These changes in displacement rate and temperature are indicated inTable 2, and the stress-strain curves are presented Figure 5.



Figure 5. Stress as a function of strain for olivine stress sensors (left) paired against harzburgites (right). Stresses from olivine and orthopyroxene are in green and orange, respectively. The red dashed vertical lines represent changes in temperature, the black vertical lines represent changes in displacement rate, and $\sigma_{\rm M}$ refers to the mean stress during the final conditions of the experiment (see Table 2 for values).

397

Stresses in samples in San404 and San508 evolved to constant values whereas stresses 398 in the other harzburgite-bearing experiments decreased progressively over time. This re-399 duction in stress may be due to an increase in temperature as a result of changes to the 400 furnace during deformation (e.g., changes in furnace shape or movement of the sample 401 relative to the hot zone). As stated above, temperature is calculated based on a calibrated 402 relationship between furnace power and temperature (Dixon & Durham, 2018). Therefore, 403 deviations in the furnace shape or the position of a sample relative to the hot zone from that 404 of the calibration assembly would lead to discrepancies between the calculated and actual 405 temperature. As temperature is an input into the equation for mean stress (see Eqs 1 & 3), 406 comparing the differential-stress and mean-stress curves can give an indication of whether 407 temperature increased. An artificially low apparent temperature (i.e., when the tempera-408 ture based on the furnace calibration is lower than the actual temperature experienced by 409 the samples) leads to an artificially low apparent mean stress. Thus, a decrease in both 410 mean stress and differential stress during an experiment may be indicative of an increase 411 in temperature. The simultaneous drop in the calculated mean stresses (see Figure S3) and 412 differential stresses suggests that temperature did increase throughout experiments San404 413 and San508. However, as mean stress and temperature only play a minor role in the calcu-414 lation of the X-ray shear modulus and thus the calculation of the differential stress-and 415 as piezometers are thought to be temperature independent (e.g., Stipp & Tullis, 2003)—the 416 precise cause of the drop in stress is not directly relevant to this study. 417

In the olivine stress sensors, average stresses from each of the three diffraction peaks 418 are typically consistent to within 20 MPa, with the exception of San390, which is consistent 419 to within 70 MPa. For olivine within harzburgites, stresses from the three peaks differ by up 420 to 450 MPa, with the $\{130\}$ peak typically giving the greatest stress. For orthopyroxene in 421 harzburgite, the difference in stresses calculated from the {421} and {321} peaks is within 422 40 MPa, with the exception of San390, where calculated stresses differ by up to 110 MPa. 423 If stresses from the $\{610\}$ peak are included, the difference in the stress increases up to 690 424 MPa. 425

For four of the experiments involving harzburgite, strain in the olivine stress sensor (0.22–0.41) was significantly greater than that in the harzburgite (0.06–0.13), indicating that harzburgite was stronger than olivine at the high pressures (4.7–9.4 GPa) and temperatures (1100–1270°C) of these experiments. Stresses measured in the harzburgite sample by X-ray diffraction were also, in all cases, greater in orthopyroxene than in olivine. In experiment San396, the diffraction patterns in orthopyroxene in the harzburgite were too noisy
 to measure stress, and as such, it was not possible in this instance to compare how stress
 was partitioned between olivine and orthopyroxene.

In experiment San508, which was conducted at relatively low mean stresses of 1.6–2.5 GPa and a temperature of 900°C, strain was greater in the mixture (0.22) than in the olivine sample (0.16). Within the mixture, the average stresses calculated from the peaks from orthopyroxene (170–280 MPa) lay within the range of stresses calculated from the peaks from olivine (-50–330 MPa).

439

3.1.3 Harzburgite Stacked Against Harzburgite

To attain greater strains within harzburgite, two samples of the same composition 440 were deformed together in a single experiment (San409), reaching a total strain of 0.28 441 (Figure 6). The samples initially deformed elastically, following the elastic modulus of 442 harzburgite (Christensen, 1966), to strains of 0.005-0.01, after which the samples yielded 443 and proceeded to strain harden. To take the samples through a variety of different stresses, 444 the temperature and displacement rate of the experiment were modified at four and three 445 points, respectively (see Table 2 and Figure 6). Temperature was first increased from 1100°C 446 to 1150°C, and then subsequently increased further to 1250°C. After ~0.14 strain, the tem-447 perature was reduced to 1200°C and then further reduced to 1150°C at 0.23 strain to pre-448 vent the differential stress from relaxing below the noise level. Changes in the experimental 449 conditions led to strain rates of 1.7×10^{-5} s⁻¹ to 4.5×10^{-5} s⁻¹. 450

Average stresses calculated from the {421} and {321} peaks in orthopyroxene (290–410
MPa) are consistent with the stresses from the olivine peaks (180–430 MPa), whereas stresses
calculated from the {610} peaks were considerably greater (660 MPa and 690 MPa for the
top and bottom samples, respectively).

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Figure 6. Stress versus strain curves for harzburgites in experiment San409. The central Ni foil was not usable for strain measurements in this experiment. As a result, stresses for each sample are plotted instead against the total strain of the combined sample stack. The red dashed vertical lines represent changes in temperature, the black vertical lines represent changes in displacement rate, and $\sigma_{\rm M}$ refers to the mean stress during the final conditions of the experiment (see Table 2 for values).

Experiment	Position	Sample	Starting material	Temperature	Strain rate ^a	Average mean	Final mean	Total strain
				(°C)	$(\times 10^{-5} s^{-1})$	stress ^b (GPa)	stress (GPa)	
San390	Тор	Ol	33	1100	22.3	5.0 ± 0.5	4.1	0.41
	Bottom	Hz(Px30)	PT-1299HiFe	1100	2.5	4.9 ± 0.5	4.1	0.06
	Top	$H_7(P_{\rm V}30)$	Pt-1200HiFo	1100	0.7	5.1 ± 0.2	5.5	0.04
San391	юр	112(1,000)	11-12/)11114	1150	0.2	5.0 ± 0.3	4.5	0.08
	Bottom	Ol	33	1100	1.8	5.2 ± 0.2	5.6	0.10
	Dottom	OI	55	1150	2.7	5.1 ± 0.3	4.6	0.28
San396				1100	1.3	9.1 ± 0.1	9.1	0.02
	Тор	Hz(Px30)	PL-1299HiFe	1270	2.3	8.2 ± 0.3	7.8	0.04
				1270	9.0	6.3 ± 0.9	5.2	0.13
			PT-1166	1100	2.3	9.4 ± 0.2	9.7	0.03
	Bottom	Ol		1270	7.9	8.3 ± 0.3	7.9	0.10
				1270	22.0	6.5 ± 0.9	5.2	0.35
	Top	01	IT-DrySC	1100	8.6	7.2 ± 0.1	7.3	0.07
San404		01	LI-DIYSC	1100	1.3	7.0 ± 0.1	6.9	0.22
0001101	Bottom	Bottom Hz(Px30) PL-1299HiFe	PL_1200HiFo	1100	0.7	7.0 ± 0.1	7.1	< 0.01
	Dottom		1 L-12/911110	1100	0.6	7.0 ± 0.0	6.9	0.07
				1100	1.7	7.7 ± 0.2	8.0	0.02
		Tor U ₂ (D ₂ /20)		1100	1.8	7.9 ± 0.0	8.0	0.03
				1150	1.8	7.7 ± 0.2	7.6	0.04
$San 400^c$	Top			1250	3.9	6.9 ± 0.4	6.3	0.12
Ja11409	Iop	112(1 x30)	1 L-12991 III e	1250	4.5	6.0 ± 0.1	6.0	0.14
				1200	4.5	5.5 ± 0.3	4.9	0.21
				1200	4.2	4.9 ± 0.0	4.9	0.23
				1150	4.2	4.7 ± 0.2	5.0	0.28

			Table 2 – cont	tinued from pre	evious page			
Experiment	Position	Sample	Starting material	Temperature	Strain rate ^a	Average Mean	Final Mean	Total strain
-		-		(°C)	$(\times 10^{-5} s^{-1})$	stress b (GPa)	stress (GPa)	
				1100	1.7	7.8 ± 0.2	8.1	0.02
				1100	1.8	8.1 ± 0.1	8.2	0.03
				1150	1.8	7.9 ± 0.1	7.8	0.04
San 400c	Bottom	$U_{\tau}(D_{\nu}(20))$	DI 1200 LIE	1250	3.9	7.0 ± 0.4	6.3	0.12
San409*	Dottom	Hz(Px30)	r L-1299-111Fe	1250	4.5	6.1 ± 0.1	6.0	0.14
				1200	4.5	5.6 ± 0.3	5.2	0.21
				1200	4.2	5.1 ± 0.1	5.1	0.23
				1150	4.2	5.0 ± 0.3	5.7	0.28
			PI-2056	800	2.5	N/A	N/A	0.01
	Тор	OrthoPy(Px85)		800	1.4	N/A	N/A	0.03
San502				900	2.4	N/A	N/A	0.11
0441002				800	2.9	2.5 ± 0.5	3.0	0.02
	Bottom	Ol	PI-2056-ol	800	1.9	3.2 ± 0.1	3.4	0.03
				900	4.4	2.3 ± 0.2	2.1	0.17
	Тор	Hz(Px50)	PI-2056	900	3.3	1.6 ± 0.3	1.9	0.04
				900	3.6	2.1 ± 0.1	2.2	0.06
San508				900	5.6	2.5 ± 0.1	2.3	0.22
Curicoo				900	1.2	2.0 ± 0.1	2.2	0.02
	Bottom	Ol	PI-2056-ol	900	2.3	2.3 ± 0.1	2.2	0.03
				900	4.8	2.5 ± 0.1	2.3	0.16

TT 1 1 A 1 6

^aStrain rate is taken as the gradient between strain and time fit through linear regression. ^bMean stress calculated using the {130} peak in the olivine in each sample. ^cDue to a tilt in the middle foil, all reported strains and strain rates for this experiment are the average for the entire assembly.

]	Final stre	ss: X-ray	diffraction	n (MPa)	
Experiment	Sample ^a	Olivine			Orthopyroxene		
		{112}	{131}	{130}	{421}	{610}	{321}
San390	OSS	320	310	340	-	-	-
Curloyo	Mix	680	780	1330	680	1620	1130
San391	OSS	110	120	90	-	-	-
Curlo / 1	Mix	350	140	390	380	590	500
San396	OSS	70	90	70	-	-	-
Curloyo	Mix	330	310	390	-	-	-
San404	OSS	30	70	70	-	-	-
Curror	Mix	260	130	280	170	310	220
San409	Mix:Top	420	320	510	310	740	320
Curroy	Mix:Bot	300	300	520	50	920	190
San502	OSS	620	630	650	-	-	-
Curro C	Mix	-	-	-	440	930	580
San508	OSS	230	220	180	-	-	-
2 and 2 d	Mix	250	-60	260	90	240	30

 Table 3.
 Final stresses measured by X-ray diffraction, rounded to the nearest 10 MPa.

^aOSS: Olivine stress sensor, Mix: Harzburgite or olivine orthopyroxenite

455 **3.2 Microstructural Analysis**

A map of kernel-average misorientation (KAM) for each sample is presented in Figure 456 7. Subgrain boundaries are common in olivine, both in the stress sensors and mixtures, 457 and particularly in samples deformed at temperatures $\geq 1100^{\circ}$ C. In orthopyroxene, sub-458 grain boundaries are sparse (if present at all) in experiments conducted at high tempera-459 tures and mean stresses, with the exception of experiment San409, in which the stacked 460 harzburgites reached a strain of 0.28 (Figure 6). However, subgrain boundaries are perva-461 sive within orthopyroxene in the experiments conducted at lower temperatures and mean 462 stresses (San502 and San508). 463

Average intercept lengths for boundaries with a misorientation angle of $\geq 15^{\circ}$ (i.e., grain boundaries) in the olivine stress sensors range from 1.6–6.6 µm. In the mixtures, the mean lengths are 1.9–3.7 µm and 1.7–3.0 µm for olivine and orthopyroxene, respectively. Where possible, comparisons to the initial starting microstructures show that grains within the olivine stress sensors are ~30% smaller after deformation, whereas within the mixtures

- the grain size remains roughly constant. Mean line-intercept lengths between boundaries
- with a misorientation angle of $\geq 2^{\circ}$ (i.e., subgrain boundaries and grain boundaries) are
- ⁴⁷¹ 1.3–4.8 μm in the olivine stress sensors, corresponding to stresses of 190–630 MPa as esti-
- ⁴⁷² mated by the subgrain-size piezometer (Eq. 5). In the mixtures, mean line-intercept lengths
- for olivine (1.2–2.9 μ m) and orthopyroxene (1.5–2.7 μ m) correspond to estimated stresses
- of 300–680 MPa and 340–590 MPa, respectively. The average boundary spacing and the
- ⁴⁷⁵ associated stresses are presented in Table 4.



Figure 7. Subsets of local misorientation maps from EBSD data. Phase maps of the full, unfilled datasets are presented in Figure S1 in the supplementary information. Grain and subgrain boundaries are displayed in black and white, respectively and are defined as boundaries with misorientation angles of $\geq 15^{\circ}$ and $\geq 2^{\circ}$. The compressional axis is vertical.

v) with associated piezometric stresses and errors. Both	
Grain-size measurement (λ_{gs}) and subgrain boundary spacing, that is subgrain size, measurement (.	(λ) were measured using the mean-line intercept method.
Table 4. ($(\lambda_{\rm gs})$ and (.

Fxneriment	Position	Index	Average	Gr	ain-size measuren	nent	Sul	bgrain-size	e measurement	
		rate (%)	(°) MAD	Phase	No. Intercepts	$\lambda_{\rm gs}$ (µm)	No.intercepts	(mη) γ	Stress (MPa)	Error (MPa)
	Top	72	0.40 ± 0.33	0I	60	1.6	60	1.3	630	+820/-360
San390	Bottom	68	051+038	0I	60	1.9	60	1.5	550	+720/-310
		0		Opx	50	1.7	60	1.5	590	+760/-340
	Ton	87	0.37+0.26	OI	60	2.2	70	1.9	450	+610/-260
San391	201	5		Opx	06	2.1	06	2.0	460	+620/-260
	Bottom	86	0.45 ± 0.30	OI	70	2.6	70	2.3	380	+510/-220
	Ton	62	0 41+0 36	O	40	2.3	70	2.2	400	+530/-230
San396	401	1		Opx	80	2.8	70	2.5	370	+520/-210
	Bottom	69	$0.51 {\pm} 0.38$	OI	70	3.7	70	3.2	290	+400/-170
	Top	91	0.33 ± 0.30	O	40	3.0	60	2.8	330	+460/-190
San404	Bottom	83	0 44+0 36	0I	30	2.0	70	1.6	550	+720/-300
		0		Opx	70	2.0	70	1.8	520	+700/-300
	Ton	65	0.63+0.53	O	60	1.9	60	1.2	680	+890/-380
San409				Opx	80	2.3	80	1.5	600	+780/-340
	Bottom	82	0.50+0.38	OI	60	1.9	60	1.5	570	+750/-320
		l		Opx	60	1.8	80	1.6	580	+750/-330
	Ton	62	045+035	OI	80	3.0	80	2.3	370	+490/-210
San502	dor			Opx	60	3.0	70	2.7	340	+460/-200
	Bottom	80	$0.51 {\pm} 0.36$	OI	60	4.0	70	2.1	390	+520/-230
									480^{a}	+760/-300
	Ton	87	0.39 ± 0.32	OI	80	3.7	80	2.9	300	+410/-180
San508		5		Opx	80	2.7	60	2.4	380	+510/-220
	Bottom	98	$0.29 {\pm} 0.21$	OI	60	6.6	80	4.8	190	+270/-110
^a Calculated us	ing the [00]	1] Burger's v	rector for olivi	ine, see Ap	pendix B					

476 **4 Discussion**

477

4.1 Comparing In-situ and Ex-situ Stress Measurements

A more complete understanding of the tectonic processes that occur on Earth requires 478 constraints on the strength of the lower crust and mantle, both of which are generally 479 made up of more than one mineral. The recent calibration of an EBSD-based subgrain-size 480 piezometer (Goddard et al., 2020) offers new opportunities for estimating paleostress mag-481 nitudes within exhumed polymineralic rocks, while avoiding the potential effects of grain-482 boundary pinning by secondary phases. However, to date, no study has tested whether 483 subgrain size accurately reflects stresses supported by individual phases within polymin-484 eralic rocks, nor what these piezometric stresses tell us about the overall stress experienced 485 by an aggregate. In this study, we present the first direct comparison of stresses measured 486 *in-situ* within individual phases to those recorded by the subgrain-size piezometer. 487

For consistency with the piezometer of Goddard et al. (2020), we begin by consider-488 ing the final *in-situ* stress experienced by each sample. While we have a single stress to 489 consider from subgrain-size piezometry, the different diffraction peaks in both olivine and 490 orthopyroxene provide a range of stresses. This variation in stress is a result of the plastic 491 anisotropy of olivine and orthopyroxene, as grains within plastically anisotropic materials 492 subjected to a non-hydrostatic stress field will undergo different amounts of plastic strain 493 depending on their orientation (e.g., Ashby, 1970). This heterogeneity in plastic strain is 494 accompanied by heterogeneity in elastic strain. As such, grains in different orientations 495 experience different stresses (Karato, 2021; Li et al., 2006; Wang et al., 2003; Weidner et al., 496 2010). Here, we find that the $\{130\}$ peak from olivine resulted in stresses on average 1.5 497 times greater than those from the other olivine peaks, consistent with previous observa-498 tions (e.g., Weidner et al., 2010). For orthopyroxene, the {610} peak resulted in the greatest 499 stress, on average 1.6 times greater than the $\{421\}$ and $\{321\}$ peaks. Previous studies have 500 taken the average of the stresses measured from individual diffraction peaks to represent 501 the macroscopic differential stress experienced by the sample (e.g., Li et al., 2006). How-502 ever, it is unclear whether or not the stresses measured from different diffraction peaks 503 should be evenly weighted (c.f., Burnley & Kaboli, 2019). Instead, the comparison of piezo-504 metric stresses from a single phase to those estimated from different diffraction peaks may 505 shed light on which peaks best represent the macroscopic stress in our experiments. 506

Before comparing these *in-situ* stress measurements to those gathered *ex-situ*, it is first 507 important to ensure that sufficient substructure developed for subgrain-size piezometry, 508 a criterion not met by all the samples in this study (e.g., the olivine stress sensors of 509 San396 and San404, Figure 7). One possible explanation for the lack of substructure is 510 that the grains in these samples are too small to contain subgrains of the size predicted by 511 the subgrain-size piezometer. For example, extrapolation of the grain- and subgrain-size 512 piezometers of Twiss (1977) to greater stresses results in a theoretical subgrain size larger 513 than the steady-state grain size. To test whether the grain size in our samples was large 514 enough for subgrains to form, we calculated the predicted mean-line intercept length be-515 tween subgrain boundaries, herein referred to as subgrain size, using the final stress mea-516 sured from each X-ray peak and the pressure-corrected Burgers vectors and shear moduli. 517 For each mineral, the predicted subgrain size was then compared to the measured grain 518 size to assess whether subgrains would be expected to form at the final stresses experi-519 enced by that sample. The predicted subgrain size and its comparison to grain size for 520 each phase in each sample can be found in Table S4 of the supplementary information. 521

For the olivine stress sensors in San390, San391, San396, and San404, all predicted subgrain sizes exceed the measured grain size. Similarly, the predicted subgrain sizes for both olivine and orthopyroxene in the harzburgite samples of San404 and in orthopyroxene in the harzburgite sample of San508 exceeded the measured grain sizes of the respective phases. Thus, subgrains were likely not able to form in a manner consistent with the subgrain-size piezometer, and consequently, we do not include these samples in our initial analysis.

For some samples, the range in stresses calculated from X-ray diffraction resulted in 529 predicted subgrain sizes that straddled the measured grain size. Specifically, the stress 530 measured from the {130} peak from olivine in the harzburgites of experiments San391, 531 San396, San409, and San508, as well as the stress measured from the {112} peak in San508, 532 are the only ones predicted to be sufficient to produce subgrains within the constraints of 533 the grain size. Similarly, for orthopyroxene only the $\{610\}$ and $\{321\}$ peaks in San391 and 534 the {610} peaks in San409 give stresses great enough to predict subgrain sizes smaller than 535 the grain sizes. In our analysis, we include these samples but identify those diffraction 536 peaks that give stresses too low for subgrain boundaries to be extensively developed at the 537 measured grain sizes. 538

For olivine, stresses from subgrain-size piezometry are plotted against a range of 539 stresses measured from X-ray diffraction in Figure 8. Open markers indicate individual 540 diffraction peaks for which the stress was sufficiently low that the subgrain size predicted 541 by the piezometer is larger than the grain size of the sample. Based on analysis of the ac-542 tivity of different slip systems (see Appendix B), a piezometric stress was also calculated 543 for the olivine stress sensor of San502 by normalising the line-intercept length by the [001]544 Burgers vector (5.98Å, Deer et al., 1988, page 4, pressure correction from Abramson et al., 545 1997) rather than the [100] Burgers vector used for the other olivine samples. The change in 546 Burgers vector increases the calculated stress from 390 to 480 MPa for San502. The stresses 547 calculated using the [100] and the [001] Burgers vectors are both plotted in Figure 8 for 548 comparison. 549



Figure 8. Comparison of *ex-situ* stresses from subgrain-size piezometry and final *in-situ* stresses from X-ray diffraction from olivine in both monomineralic and polymineralic samples. Error bars are calculated using a Monte-Carlo based approach, as described in Section 2.5 and Appendix A. The size of each data point is scaled by the total strain experienced by the sample. Stresses from individual X-ray peaks for which the predicted subgrain size is larger than the measured grain size of the sample are plotted as open symbols. The black solid line is 1:1 and the dashed horizontal line marks the upper calibration limit for olivine in the subgrain-size piezometer (Goddard et al., 2020). Two stresses from subgrain-size piezometry have been plotted for the stress sensor of San502, one where the mean-line intercept length was normalised by the length of the [100] Burgers vector and one where it was normalised by the length of the [001] Burgers vector.

A strong correlation exists between the *in-situ* stress measurements from the $\{130\}$ 550 diffraction peaks and the *ex-situ* stress measurements, in both the monomineralic and polymin-551 eralic samples (Figure 8). A moderate correlation also exists for the $\{112\}$ peak, as these 552 stresses are often similar to those from the $\{130\}$ peak. The stresses from the $\{131\}$ peak 553 tend to be significantly lower than those calculated from the other diffraction peaks, and 554 in most cases are low enough that the subgrain size predicted by the piezometer is larger 555 than the measured grain size (open symbols in Figure 8). For the few samples that can 556 confidently be compared, X-ray stresses from the $\{131\}$ peak lie within the uncertainty of 557 the piezometric stresses. Recently, Girard and Karato (2022) demonstrated that the bulk 558 stress experienced by a sample is most accurately represented by the diffraction peak pro-559 viding the greatest stress measurement, here the $\{130\}$ olivine peak. Given the particularly 560 close correspondence between the $\{130\}$ stresses and the stresses measured via subgrain-561 size piezometry, we conclude that subgrain-size piezometry accurately reflects the stress 562 within individual phases in a polymineralic rock. 563

Subgrain-size piezometry therefore provides a powerful tool for measuring stress in 564 natural rocks, but care must be taken when applying it to extremely fine-grained samples. 565 For example, olivine within polymineralic regions of the Erro-Tobbio peridotite in Italy, 566 have average grain sizes as low as 5 µm (Linckens & Tholen, 2021). Such small grain 567 sizes would require differential stresses of > 175 MPa to form subgrains, an unrealistic 568 condition considering shear zones are regions of weakening and localisation (e.g., Skemer 569 et al., 2010; Stenvall et al., 2019; Warren & Hirth, 2006). As many other natural shear zones, 570 such as the Josephine peridotite (\sim 250 μ m, Hansen & Warren, 2015) and the Oman-United 571 Arab Emirates ophiolite ($\geq 100 \,\mu\text{m}$ Ambrose et al., 2018), are relatively coarse grained, the 572 application of subgrain-size piezometry remains broad. 573

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4.2 Subgrain-size Piezometry as a Tool For Unpicking Complex Stress Histories

A key challenge in paleopiezometry lies in accounting for the potentially complex stress histories experienced by natural samples, compared to samples deformed in the laboratory that often experience steady-state deformation (Kidder et al., 2016; Speciale et al., 2022). It is currently not clear how much strain is required to set or reset the stress recorded by the subgrain size. Previous work on olivine by Ross et al. (1980) compared constant strain rate and constant stress experiments to those in which the stress, strain rate, or temperature was varied incrementally. In those experiments, subgrain sizes were

found to decrease with increasing stress but did not coarsen with decreasing stress, sug-582 gesting that the subgrain size is set by the maximum stress applied to a sample. However, 583 experiments on steel by Qin et al. (2003) found that subgrains were able to coarsen if con-584 tinuously strained under stresses of a reduced magnitude, suggesting that strain, rather 585 than time, is important for subgrain coarsening. Goddard et al. (2020) also demonstrated a 586 correlation between subgrain-boundary spacing and the final stress experienced by olivine 587 and quartz deformed in the laboratory, despite some samples having experienced greater 588 (peak) stresses earlier in their deformation history. 589

To test how subgrain sizes respond to complex stress histories, we subjected the sam-590 ples in all but one of our experiments to either temperature or strain-rate steps, which 591 imparted strains between 0.01 and 0.25. Based on the initial calibration by Goddard et al. 592 (2020), we would expect stresses estimated using the subgrain-size piezometer to match 593 the final stresses measured through X-ray diffraction. Indeed, as seen in the previous sec-594 tion, such a correlation is apparent in Figure 8. However, some of the samples with grain 595 sizes predicted to be too small to contain subgrains still contain numerous subgrain bound-596 aries (e.g., the olivine stress sensor in San390 and the harzburgite in San404 in Figure 7). It 597 is therefore possible that the subgrain boundaries within these samples formed during an 598 earlier portion of the deformation history under a differential stress greater than the final 599 stress. 600

To explore whether these 'unexpected' subgrain boundaries correspond to an earlier 601 part of the deformation history, we plot in Figure 9 both the peak stresses and the final 602 stresses measured by X-ray diffraction for samples not presented in Figure 8. To be clear, 603 in all these remaining experiments the grain sizes were too small to accommodate sub-604 grains of the size predicted by the piezometer based on the final stress measured by X-ray 605 diffraction. We exclude data from the olivine stress sensor for experiment San404, as the 606 predicted subgrain size from the peak stress was also too large to be accommodated within 607 the grains. 608

The subgrain size in the samples with the most prolific intragranular boundaries give piezometric stresses that match the peak stress experienced during each experiment. The remaining two samples—the olivine stress sensors in experiments San391 and San396—give piezometric stresses that are midway through the peak stress and the final stress implying that their subgrains underwent some coarsening. Notably, during experiments San391 and

San396 the stress reductions were the result of increases in temperature from 1100°C to 614 1150°C and 1100°C to 1270°C, respectively. The two experiments that instead record the 615 peak stresses were held at 1100°C. We therefore conclude that, at higher temperatures, 616 subgrain boundaries are more easily removed. Ross et al. (1980) conducted experiments 617 at temperatures of 1000–1300°C, however the majority of experiments used for piezome-618 try were conducted at 1100°C. Our experiments at the equivalent temperature that exhibit 619 little subgrain evolution are roughly consistent with the observations of Ross et al. (1980). 620 Therefore, if the grain size is too fine for the subgrains to coarsen to the size determined by 621 a new lower stress, and temperatures are relatively low, subgrain structure within a rock 622 could relate to a previous, even transient, high stress. 623



Figure 9. Comparison of *ex-situ* stress, from subgrain-size piezometry, and *in-situ* stress, from X-ray diffraction, for olivine in all samples for which the subgrain size predicted by the final stress was larger than the measured grain size. Black symbols represent the peak stress measured by X-ray diffraction. Horizontal arrows link the peak stress to the final stress experienced by the sample. The black solid line is 1:1 and the dashed horizontal line represents the calibration limit for olivine in the subgrain-size piezometer (Goddard et al., 2020). For clarity we did not include error bars, though errors on the piezometric stress estimates can be found in Table 4.

4.3 Subgrain-size Piezometry in Orthopyroxene

The experiments presented here provide an opportunity to explore whether the subgrainsize piezometer published by Goddard et al. (2020) can be reliably applied to orthopyroxene, a mineral not included in the original calibration. Such analysis would greatly expand the use of this piezometer and negate the common requirement to calibrate a subgrain-size piezometer for each mineral of interest. Stresses from subgrain-size piezometry of orthopy630

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roxene are plotted against those from X-ray diffraction in Figure 10. Similar to Figures 8 and 9, we identify, with open symbols, stresses from X-ray diffraction that are too low for subgrains to form at the grain sizes of these samples.



Figure 10. Comparison of *ex-situ* stress, from subgrain-size piezometry, and *in-situ* stress, from X-ray diffraction, for orthopyroxene in all samples. Black symbols represent the peak stress measured by X-ray diffraction and black horizontal arrows link the peak stress to the final stress experienced by the sample. Error bars are calculated using the Monte-Carlo based approach, as described in Section 2.5 and Appendix A. Stresses from individual peaks for which the subgrain size predicted by the piezometer was larger than the measured grain size are plotted as open symbols. The black solid line is 1:1.

There is no consistent relationship between the stresses preserved by the subgrain-633 boundary spacing in orthopyroxene and either the peak stresses or the final stresses expe-634 rienced by the sample. However, this lack of correlation is expected given the limited intra-635 granular substructure within the orthopyroxene in most samples. In addition, the low total 636 strains in most of the mixtures, alongside the greater strength of orthopyroxene compared 637 to olivine at high confining pressures (e.g., Raterron et al., 2016), indicates that the former 638 may account for very little of the total strain of the aggregate. We therefore limit further 639 discussion to experiments San409 and San508, in which the total strain of the harzburgite 640 exceeds 0.20, and experiment San502, in which the sample is mostly orthopyroxene (85%) 641 and a total strain of 0.11 was reached. 642

For experiment San409, the final stresses in the top and bottom samples measured
 through X-ray diffraction (310–740 MPa and 50–920 MPa, respectively) straddle those mea sured by subgrain-size piezometry (600 MPa and 580 MPa, respectively), though the large

range in *in-situ* stresses limits the significance of this comparison. For experiment San502, 646 the stress of 340 MPa from subgrain-size piezometry is close to the final stress of 440 MPa 647 measured from the {421} peak, but is less than the stresses of 930 MPa and 580 MPa from 648 the $\{610\}$ and $\{321\}$ diffraction peaks, respectively. For San508, the grain size is too small 649 to form subgrains of the size predicted by the piezometer based on the final stress. How-650 ever, the stresses from X-ray diffraction only began to drop during the final 0.02 of strain. 651 The previous 0.12 of strain occurred under a near constant stress of 360-410 MPa, which 652 is consistent with the stress of 380 MPa measured in the orthopyroxene by subgrain-size 653 piezometry. 654

These results broadly support the use of subgrain-size piezometry on orthopyroxene as long as sufficient substructure exists. These experiments also highlight the effects of large strength contrasts when applying the subgrain-size piezometer, as the strain experienced by an individual mineral is an important factor in determining whether subgrains in that mineral evolve to the size predicted by the piezometric relationship.

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4.4 Stress Partitioning from X-ray Diffraction

The results of this study are, to the best of our knowledge, the first to provide direct 661 evidence that subgrain sizes reflect the stress supported by an individual phase deforming 662 in an aggregate. A relevant question that still remains, however, is how these measured 663 stresses relate to the macroscopic stress applied to the rock. In the work presented here, 664 the general lack of subgrains in orthopyroxene within experiments deformed at a high 665 mean stress limits the use of subgrain-size piezometry as a tool for exploring stress parti-666 tioning. However, stress partitioning can still be explored via X-ray diffraction. Relatively 667 few studies to date have used X-ray diffraction in this way (Li et al., 2007; Wang et al., 668 2013) and no studies, to our knowledge, have used this method in olivine-orthopyroxene 669 systems. 670

When considering stress partitioning, the relevant question is how the stress within an individual phase relates to the bulk stress experienced by a rock. Stacked samples have previously been assumed to nominally experience the same stress (e.g., Hansen et al., 2019). This assumption holds true for our experiment San409, in which the same material was used for both the top and bottom samples (Figure 6). If the same were true of our other experiments, then the stress supported by the sample of monomineralic olivine in each ex-

periment should represent the bulk stress of the adjacent polymineralic sample. However, 677 in all experiments conducted at high mean stresses (> 5 GPa), differential stresses mea-678 sured within the mixture were significantly greater than those in the olivine stress sensor 679 (Figure 5). Silber et al. (2022) suggested that such differences in stress within an assembly 680 can occur if the samples are weak relative to the confining medium. Our stacked sam-681 ples cannot therefore be used to explore how stresses within each phase relate to the bulk 682 stress, but we can see how different conditions affect the relative stresses within olivine 683 and orthopyroxene. 684

We calculated the average stress from each peak over the final controlled conditions 685 of the experiment, that is, after the final temperature or displacement-rate step (see sup-686 plementary Table S3). For experiment San409, we instead averaged stress over the final 687 0.2 strain, due to the small amount of strain under each set of conditions. Of the stresses 688 calculated from the three peaks, we consider the least and greatest values to represent the 689 'stress range' of each phase in the mixture, and compare these in Figure 11. In experiments 690 performed at high mean stresses (> 5 GPa) and temperatures (1100–1270°C), the mean of 691 three X-ray diffraction stresses is 1.2–1.7 times greater in orthopyroxene than olivine. How-692 ever, in experiment San508, which was deformed at a lower mean stress of \leq 4 GPa, the 693 stresses supported by olivine and orthopyroxene are the same within error. 694



Figure 11. Comparison of the average differential stresses measured in olivine and orthopyroxene by X-ray diffraction. The boxes, colour coded for mean stress, cover the full range of stresses calculated from the different diffraction peaks of each phase.

695 696 This observation of a greater stress supported by the orthopyroxene when at high mean stress can be considered in relation to Handy's (1994) rheological mixing model.

As the harzburgites in this study consist mainly of olivine (\sim 70%), and as orthopyroxene 697 is stronger than olivine at these experimental conditions (e.g., Raterron et al., 2016), the 698 phase distribution within these samples can be categorised as interconnected weak layers 699 (Handy, 1990). Stresses within the individual phases of samples with interconnected weak 700 layers have been proposed to lie close to the isostress limit (Handy, 1994), also known as 701 the Sachs model, in which it is assumed that each grain within an aggregate experiences the 702 same stress tensor (Sachs, 1928). Handy's (1994) model predicts a slight variation from the 703 Sachs model, with marginally greater stress within the 'strong' phase in mixtures when the 704 viscosity contrast between phases is less than one order of magnitude. The greater stresses 705 within the strong orthopyroxene in this study are therefore consistent with Handy's (1994) 706 model. Similarly, work by Li et al. (2007) using X-ray diffraction to explore stresses within 707 composites of varying proportions of MgO and spinel measured greater stresses within 708 the strong phase when it comprised just 25% of the mixture. Clearly, in-situ stress mea-709 surements make a good dataset to examine polymineralic mixing models, which can then 710 enable more accurate interpretations of stress estimates from natural samples. 711

712 **5 Conclusions**

We deformed olivine and olivine-orthopyroxene mixtures in a D-DIA apparatus at 713 temperatures and mean stresses similar to mantle conditions. In-situ stress measurements 714 from X-ray diffraction are compared to *ex-situ* measurements from subgrain-size piezome-715 try. A good correlation between the *in-situ* and *ex-situ* stresses in olivine in both monomin-716 eralic and polymineralic aggregates demonstrates that subgrain size is unaffected by grain-717 boundary pinning by secondary minerals. Subgrain size also displays a good correlation 718 with the final stress experienced by the sample, even in experiments with complex stress 719 histories. However, this study identifies a number of important factors to consider when 720 applying subgrain-size piezometry to natural rocks. First, in polymineralic rocks, caution 721 must be taken in applying the subgrain-size piezometer to strong minerals that undergo 722 little strain, such as those behaving as passive clasts within a deforming matrix. Second, 723 while some initial data for orthopyroxene looks promising, further experiments are still 724 required to confirm the applicability of the Goddard et al. (2020) piezometer to minerals 725 other than quartz and olivine, with which it was calibrated. Third, very fine-grained rocks 726 may not have grain sizes sufficiently large to host subgrains that have formed under low 727 stresses. Therefore, in particularly fine-grained samples, the stresses measured from ex-728

isting subgrains may not necessarily record the most recent stress state if the associated
 subgrain size was larger than the grain size, but may instead record earlier deformation as sociated with greater stresses and finer subgrain sizes. Finally, for the compositional ratios
 of samples deformed at high mean stresses of 4.7–9.4 GPa in this study, the stresses sup ported by orthopyroxene and olivine in harzburgites are not equal. As such, care must be
 taken when extrapolating the stress measured from an individual phase to the bulk stress
 experienced by the sample.

736 6 Data Availability Statement

Mechanical data from the Deformation-DIA experiments alongside EBSD data of re covered samples are available from OSF via https://doi.org/10.17605/OSF.IO/UATJG (Goddard
 et al., 2023). Codes for processing EBSD data can be found at https://github.com/
 RellieGoddard/SGPiezometry.git.

741

742 Appendix A Error Estimation on the Subgrain-size Piezometer

We use a Monte-Carlo-based approach to estimate the errors in our subgrain-size mea-743 surements, the errors in parameters in the subgrain-size piezometer, and errors in stress es-744 timates. The procedures described here are carried out in log units under the assumption, 745 which is validated below, that errors in measurements of subgrain size are lognormally dis-746 tributed. As an initial step, we refit the piezometer to the data determined using a threshold 747 misorientation angle of 2°, above which boundaries are measured. For each measurement 748 of subgrain size used in this refitting, we assume that the probability of measuring the true 749 subgrain size is represented by a normal distribution (in log units) with standard devia-750 tion equal to the error in subgrain-size measurement. This error is justified below to be 751 approximately 0.13 log units. We then randomly select a value from that distribution and 752 perturb the measured subgrain size by that amount. This new data set of stresses and per-753 turbed subgrain sizes is then used to determine the parameter values for the subgrain-size 754 piezometer using a linear least-squares approach. This process is repeated 10,000 times, 755 randomly generating new perturbed measurements on each iteration. The distributions of 756 best-fit parameter values determined over all of these iterations are illustrated in Figures 757 A1a and b. The means of these distributions are, within three significant digits, equivalent 758 to the parameter values determined by a least-squares fit to the unperturbed data set. We 759

take the standard deviation of these distributions to reflect the error in estimation of the piezometer parameters, resulting in a pre-exponential constant of 1.1 ± 0.3 and an exponent of -1.1 ± 0.1 .



Figure A1. Estimation of error on best-fit parameters for the subgrain-size piezometer. Distributions of parameter estimates from 10,000 individual fitting exercises for (a) the exponent and (b) the preexponential constant in the piezometer. The means of the distributions are indicated in red. The standard deviations of the distributions are taken to represent the error in the estimate. (c) Best-fit piezometer compared to data used for calibration and 67% and 95% confidence intervals. Confidence intervals are estimated assuming that the error in subgrain-size measurement is 0.13 log units.

Figure A1 compares the best-fit piezometer to the measured data. This figure also 763 includes 67% and 95% confidence intervals determined using one or two times the error in 764 the subgrain-size measurement, respectively. We compare these confidence intervals to the 765 distribution of data as a check on the validity of our error estimation. We find that setting 766 the error on subgrain-size measurement to 0.13 log units, as presented in Figure A1, results 767 in 67% and 95% confidence intervals that contain 67% and 94% of the data, respectively. 768 This exercise not only demonstrates that an error of 0.13 log units in our subgrain-size 769 measurements is consistent with the data, but it also provides confidence that the error in 770 those measurements is lognormally distributed. 771

A similar procedure can be used to estimate the errors in stresses predicted using the 772 piezometer. Here we again assume that the probability distributions for the subgrain size, 773 pre-exponential constant, and exponent follow lognormal distributions with standard de-774 viations (in log units) given by 0.13, 0.3, and 0.1, respectively, and with means given by the 775 measured or best-fit values. We randomly draw values from these distributions and use 776 them in conjunction with appropriate values of the Burgers vector and shear modulus to 777 make a prediction of the applied differential stress. This process is repeated 10,000 times to 778 generate a distribution of predicted stresses. The mean of this distribution (in log units) is 779

equivalent to the predicted stress used simply with the measured subgrain size and best-fit piezometer parameters. We take the standard deviation of this distribution to represent the error in the predicted stress. As an illustrative example, for a measured subgrain size of 1.5 µm with Burgers vector of 0.475 nm and shear modulus of 77.8 GPa, we estimate the normalised stress to be $10^{-2.2\pm0.4}$ and the absolute stress to be 510^{+680}_{-290} MPa.

Appendix B Choice of Burgers vector for Experiments San502 and San508

The subgrain-size piezometer presented by Goddard et al. (2020), was calibrated us-786 ing high-temperature experiments in which dislocation creep of olivine occurs primarily 787 by the slip system (010)[100] (e.g., Bai et al., 1991; Hansen et al., 2014; Wallis et al., 2019). 788 However, two experiments from this study, San502 and San508, were carried out at lower 789 temperatures (\leq 900°C) where the (100)[001] slip system, and particularly [001] screw dislo-790 cations, can instead dominate deformation (e.g., Carter & Ave'Lallemant, 1970; Druiventak 791 et al., 2011; Gaboriaud et al., 1981; Idrissi et al., 2016; Wallis et al., 2020). Here, we interpret 792 the slip systems active in these two samples based on the pole figures and misorientation 793 inverse pole figures. The pole figures are lower-hemisphere projections, are constructed 794 using one point per grain and a kernel half-width of 5°, and are oriented such that the 795 maximum principal stress axis (σ_1) is vertical. For all inverse pole figures, misorientation 796 axes were plotted for neighbouring pixels with misorientation angles between 2° and 15°. 797 Colour scales in Figures B1–B3 represent multiples of uniform distribution (MUD). 798

Pole figures and inverse pole figures for olivine in both the olivine stress sensor and the 799 harzburgite sample of experiment San508 are plotted in Figure B1. Olivine exhibits a crystal 800 preferred orientation (CPO) with [100] and [001] axes in girdles perpendicular to σ_1 and 801 [010] axes in a cluster parallel to σ_1 . Taken in isolation, this CPO indicates that (010) is the 802 slip plane of the dominant slip system and that [100] and/or [001] is the dominant Burgers 803 vector. The misorientation axes of olivine form a dominant cluster parallel to [001] and a 804 secondary cluster parallel to [010]. Misorientation axes parallel to [001] are characteristic of 805 tilt boundaries composed of edge dislocations on the (010)[100] slip system. Misorientation 806 axes parallel to [010] can result from three possible types of subgrain boundary, specifically 807 tilt boundaries composed of edge dislocations on the (001)[100] or (100)[001] slip systems 808 and twist boundaries composed of [100] and [001] screw dislocations. Taken together, these 809 observations indicate that (010)[100] was the dominant slip system, whilst (001)[100] and 810 or (100)[001] were also active but to a lesser degree. 811



Figure B1. Pole and inverse pole figures for olivine in the stress sensor and harzburgite samples of San508. Colour represents multiples of uniform distribution (MUD).



Figure B2. Pole and inverse pole figures for olivine in the stress sensor and olivine-orthopyroxenite samples of San502. Colour represents multiples of uniform distribution (MUD).

Figure B2 contains the equivalent pole figures and inverse pole figures for olivine in 812 both the stress sensor and the olivine-orthopyroxenite sample in experiment San502. In 813 all pole figures olivine displays no discernible CPO. For the stress sensor, this lack of CPO 814 may in part be due to the low number of grains available for analysis (195). However, this 815 reasoning does not apply to the olivine in the olivine orthopyroxenite, for which 648 grains 816 were measured. Despite the lack of CPOs, the presence of subgrain boundaries within 817 olivine in both the stress sensor and the mixture implies that dislocations were active dur-818 ing deformation. Similar to San508, olivine in both samples exhibits subgrain boundaries 819 with misorientation axes clustered approximately parallel to [001] and [010]. Unlike San508, 820 the olivine in the olivine orthopyroxenite also contains subgrain boundaries with misori-821 entation axes clustered parallel to [100]. These latter subgrain boundaries can represent tilt 822 boundaries composed of (010)[001] edge dislocations. In both cases the cluster parallel to 823 [001] is secondary in strength. Without crystal preferred orientations it is not possible to 824 identify the exact slip system, however the misorientation axes indicate that (010)[100] is 825

not likely to be the dominant slip system and therefore the dominant Burgers vector waslikely [001].

Figure B3 presents pole and inverse pole figures for orthopyroxene in San502 and 828 San508. In both cases, misorientation axes of subgrain boundaries are predominantly clus-829 tered around [010], indicating that the subgrain boundaries are formed by dislocations on 830 the (001)[100] and/or (100)[001] slip systems. Both samples also exhibit a submaximum 831 of misorientation axes parallel to [001], indicating a subpopulation of subgrain bound-832 aries composed of dislocations on the (010)[100] and/or (100)[010] slip systems. In sample 833 San502, both [100] and [010] axes are clustered parallel to σ_1 with [001] axes in a girdle nor-834 mal to σ_1 . These grain orientations indicate that [001] was the dominant slip direction in 835 this sample and, in combination with the interpretations from misorientation axes of sub-836 grain boundaries, suggest that (100)[001] is the dominant slip system. In sample San508, 837 [100] axes are randomly oriented, [010] axes cluster parallel to σ_1 , and [001] axes form a 838 girdle normal to σ_1 . These grain orientations suggest that (010)[001] was the slip system 839 providing the greatest contribution to grain rotations. Overall, these results indicate that 840 [001] was the dominant Burgers vector in orthopyroxene in these experiments, which is 841 consistent with previous observations of experimental and natural samples (Jung et al., 842 2010). 843



Figure B3. Pole figures and inverse pole figures for orthopyroxene in the harzburgite sample of San508 and the olivine-orthopyroxenite sample of San502. Colour represents multiples of uniform distribution (MUD).

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Journal of Geophysical Research: Solid Earth

Supporting information for

Validation of subgrain-size piezometry as a tool for measuring stress in polymineralic rocks

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Additional Supporting Information (Files uploaded separately)

1. Table S4

Introduction

Supplementary material provides: phase maps of unfilled electron backscatter diffraction (EBSD) data (Figure S1); example of angular precision in EBSD map of experiment San409 (Figure S2); mechanical data, specifically plots of mean stress against time, for all experiments (Figure S3); table of EBSD collection conditions (Table S1); table of average stresses of each experiment, measured through X-ray diffraction (Table S2); table of the peak stresses of each experiment, measured through X-ray diffraction (Table S2); table of the peak stresses of each experiment, measured through X-ray diffraction (Table S3); and caption for Table S4, which is uploaded separately in an Excel spreadsheet. Figure S1: Phase maps of the unfilled EBSD data (after being subjected to the cleaning process described in Section 2.4). Grain boundaries, defined as having a misorientation angle of $\geq 15^{\circ}$, are drawn in black.







Figure S2: Local misorientation map from EBSD data of the top harzburgite sample in experiment San409. Misorientation profiles across two example grains are also displayed. Grain and subgrain boundaries are in black and white, respectively. Grain boundaries are defined as boundaries with misorientation angles of $\geq 15^{\circ}$, while subgrain boundaries are defined as boundaries with misorientation angles of $\geq 1^{\circ}$. The compressional axis is vertical.





Figure S3: Mean stress plotted against time for all experiments. Mean stress was measured from X-ray diffraction on the $\{130\}$ peak within olivine in both the stress sensor and, where possible, the mixture.

Experiment	Sample ^a	Filename	Collection	Accelerating	Step	Indexed	MAD ^{c,d}
No.			$location^b$	voltage kV	size (μm)	$pixels^d$ (%)	Statistic
San390	OSS	San390_Ol_small_area2_rotated.ctf	UoO	30	0.1	72.0	0.40 ± 0.33
San390	Mix	San390_Hz_rotated.ctf	UMN	20	0.075	68.0	$0.51{\pm}0.38$
San391	OSS	San391_Ol_close_rotated.ctf	UoO	30	0.1	86.0	0.45 ± 0.30
San391	Mix	San391_hz_rotated.ctf	MBL	20	0.1	87.0	0.37 ± 0.26
San396	OSS	San396_olivine_rotated.ctf	UMN	20	0.1	69.0	$0.51{\pm}0.38$
San396	Mix	San396-hz_rotated.ctf	UMN	20	0.1	62.0	0.41 ± 0.36
San404	OSS	San404_Ol_rotated_sub.ctf	U ₀ O	30	0.2	90.7	0.33 ± 0.30
San404	Mix	San404_bot_Rotation_Hz.ctf	UoO	30	0.2	83.0	0.44 ± 0.36
San409	Mix-Top	San409_top_rotated.ctf	U ₀ O	30	0.2	65.0	0.63 ± 0.53
San409	Mix-Bot	San409_bot_rotated.ctf	U ₀ O	30	0.2	82.0	0.50 ± 0.38
San502	OSS	San502_load_cell_rotated.ctf	MBL	30	0.2	80.0	$0.51{\pm}0.36$
San502	Mix	San502_orthopyroxene_remapped	MBL	30	0.3	79.0	0.45 ± 0.35
		_subset_rotated.ctf					
San508	OSS	San508_loadcell_500nm_rotated.ctf	MBL	20	0.5	98.3	0.29 ± 0.21
San508	Mix	San508_mix_300nm_rotated.ctf	MBL	20	0.3	87.0	0.39 ± 0.32
^a OSS: Olivine	stress sensor,	Mix: Harzburgite or olivine orthopyroxenite					

Table S1: Collection conditions

^bUoO: University of Oxford, UMN: University of Minnesota, MBL: Marine Biology Laboratory, Woods Hole

 $^{\rm c}{\rm Mean}$ angular deviation $^{\rm d}{\rm Calculated}$ from EBSD data prior to cleaning and infilling in MTEX

	$Sample^{a}$	Peak stress: X-ray diffraction (MPa)						
Experiment		Olivine			Orthopyroxene			
		{112}	{131}	{130}	$\{421\}$	$\{610\}$	${321}$	
San390	OSS	590	700	720	-	-	-	
	Mix	1140	1120	1590	1420	2100	1350	
San391 ^b	OSS	560	610	710	-	-	-	
Sanovi	Mix	750	640	910	980	1310	1010	
San396	OSS	1130	1370	1480	-	-	-	
	Mix	1490	1340	1750	-	-	-	
San404	OSS	100	100	100	-	-	-	
5011101	Mix	530	470	600	610	720	770	
San409	Mix-Top	1250	1510	1810	1490	2910	1630	
Samo	Mix-Bot	1180	1300	1680	1410	2420	1660	
San502	OSS	830	1250	1300	-	-	-	
	Mix	-	-	-	1110	1650	1270	
San508	OSS	330	350	420	-	-	-	
200000	Mix	430	250	340	410	370	360	

Table S2: Peak stresses from X-ray diffraction, rounded to the nearest 10 MPa.

^aOSS: Olivine stress sensor, Mix: Harzburgite or olivine orthopyroxenite

^bIgnoring anomalous data point

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Table S3: Average stress measured from X-ray diffraction rounded to the nearest 10 MPa. The data used to calculated the average stress is indicated in the table.

	$Sample^{a}$	Calculated from	Average stress: X-ray diffraction (MPa)					
Experiment			Olivine			Orthopyroxene		
			{112}	{131}	{130}	$\{421\}$	$\{610\}$	${321}$
San390	OSS	whole experiment	470	520	540	-	-	-
Salisso	Mix	whole experiment	930	910	1360	1040	1730	1150
San391	OSS	after T step	250	240	260	-	-	-
Sanoor	Mix	after T step	470	250	530	570	830	610
San396	OSS	after rate step	290	290	300	-	-	-
Sallooo	Mix	after rate step	610	500	780	-	-	-
San404	OSS	after rate step	30	50	40	-	-	-
Starror	Mix	after rate step	250	110	270	260	330	290
San409	Mix-Top	final 0.2 strain	360	200	430	340	660	320
, call 100	Mix-Bot	final 0.2 strain	250	180	380	290	690	410
San502	OSS	after T step	590	590	690	-	-	-
Starrooz	Mix	after T step	-	-	-	620	1050	670
San508	OSS	after final rate step	250	240	260	-	-	-
Sanooo	Mix	after final rate step	330	-50	250	190	280	170

^aOSS: Olivine stress sensor, Mix: Harzburgite or olivine orthopyroxenite

Caption for Table S4, uploaded separately

Mean line-intercept length predicted using the 2°-subgrain-size piezometer, final stress measured from X-ray diffraction, and final pressure measured through X-ray diffraction of the {130} peak in olivine. A cross in the 'SGs' column indicates that the grain-size was large enough for subgrains to form in equilibrium with the final stress.