## Detection and attribution of climate change using a neural network

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#### Abstract

A new detection and attribution method is presented and applied to the global mean surface air temperature (GSAT) from 1900 to 2014. The method aims at attributing the climate changes to the variations of greenhouse gases, anthropogenic aerosols, and natural forcings. A convolutional neural network (CNN) is trained using the simulated GSAT from historical and single-forcing simulations of twelve climate models. Then, we perform a backward optimization with the CNN to estimate the attributable GSAT changes. Such a method does not assume additivity in the effects of the forcings. The uncertainty in the attributable GSAT is estimated by sampling different starting points from single-forcing simulations and repeating the backward optimization. To evaluate this new method, the attributable GSAT changes are also calculated using the regularized optimal fingerprinting (ROF) method. Using synthetic non-additive data, we first find that the neural network-based method estimates attribuable changes better than ROF. When using GSAT data from climate model, the attribuable anomalies are similar for both methods, which might reflect that the influence of forcing is mainy additive for the GSAT. However, we found that the uncertainties given both methods are different. The new method presented here can be adapted and extended in future work, to investigate the non-additive changes found at the local scale or on other physical variables.

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#### **Key Points:**

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9	•	We present a non linear method based on neural network to attribute the global
10		mean surface air temperature variability to different forcings.
11	•	We use a CNN associated with a backward optimization to estimate the climate
12		response to the different external forcings.

The attributable forcings are consistent with those obtained using another state of-the-art method.

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#### 15 Abstract

A new detection and attribution method is presented and applied to the global mean sur-16 face air temperature (GSAT) from 1900 to 2014. The method aims at attributing the 17 climate changes to the variations of greenhouse gases, anthropogenic aerosols, and nat-18 ural forcings. A convolutional neural network (CNN) is trained using the simulated GSAT 19 from historical and single-forcing simulations of twelve climate models. Then, we per-20 form a backward optimization with the CNN to estimate the attributable GSAT changes. 21 Such a method does not assume additivity in the effects of the forcings. The uncertainty 22 in the attributable GSAT is estimated by sampling different starting points from single-23 forcing simulations and repeating the backward optimization. To evaluate this new method, 24 the attributable GSAT changes are also calculated using the regularized optimal finger-25 printing (ROF) method. Using synthetic non-additive data, we first find that the neu-26 ral network-based method estimates attribuable changes better than ROF. When using 27 GSAT data from climate model, the attribuable anomalies are similar for both meth-28 ods, which might reflect that the influence of forcing is mainy additive for the GSAT. 29 However, we found that the uncertainties given both methods are different. The new method 30 presented here can be adapted and extended in future work, to investigate the non-additive 31 changes found at the local scale or on other physical variables. 32

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#### Plain Language Summary

In order to design effective adaptation policies, it is essential to have reliable es-34 timates of the effect of anthropogenic activities on the climate. For that purpose a new 35 attribution method based on a neural network is designed and evaluated. The method 36 estimates the past global mean surface air temperatures anomalies caused by the changes 37 in the greenhouse gases concentration, the variation of anthropogenic aerosols, and the 38 variations driven by naturally occurring phenomena. To build this estimation, the data 39 from observations and climate models are used. This methodology is compared with an-40 other state-of-the-art method. The results of both methods are evaluated and discussed. 41 The proposed method provide better estimations in the case of large non-additivity of 42 the causes of climate change and can be applied to other physical variables or at the re-43 gional scale. In the case of the global mean surface air temperature, the method presented 44 provides estimation similar to other methods. 45

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#### 46 **1** Introduction

Detection and attribution of climate change is key to understanding past climate 47 change and devising adaptation policies. This problem is an important part of IPCC re-48 ports (Eyring et al., 2021) as it directly inquires about the impact of anthropogenic ac-49 tivities on the climate system. Detection aims to compare climate change with internal 50 variability. A change is detected if it exceeds the anomalies generated by the internal cli-51 mate variability. Internal variability refers to climate variations resulting from processes 52 intrinsic to the climate system, occurring in the absence of external forcing. Internal vari-53 ability may arise from processes within each of the climate system components (atmo-54 sphere, ocean, land surface, cryosphere) or may emerge from their interactions (Cassou 55 et al., 2018). For instance, the global mean surface air temperature (GSAT) varies by 56 a few tenths of degrees during the El Niño or La Niña phases of the El Niño Southern 57 Oscillation (Neelin et al., 1998). Similarly, the Pacific decadal variability and the Atlantic 58 multi-decadal variability can also influence the GSAT (Meehl et al., 2016; Z. Li et al., 59 2020). Forcing agents external to the climate system, known as external forcings, can 60 also cause climate changes. The dominant forcings in the historical period (i.e. 1850 to 61 present-day) are the increase in the concentration of greenhouse gases, the variations of 62 the aerosol concentrations, the variations of incoming solar radiation, the changes in land 63 use and stratospheric ozone concentration (Masson-Delmotte et al., 2021). Attribution 64 then aims to explain and quantify the impacts of the different forcings. Anthropogeni-65 cally driven and naturally occurring forcings are often considered separately to under-66 stand the impact of human activities. Natural forcings include the effects of natural sources 67 of aerosols and solar activity. The anthropogenic effects include the contributions of other 68 effects. Hasselmann (1993) defined a method called "optimal fingerprinting" for detec-69 tion and attribution relying on climate model simulations and observations. This method 70 has been improved to build more reliable uncertainties and to check for the consistency 71 between models and observations (Allen & Tett, 1999), or to account for the residual in-72 ternal variability in ensembles of climate model simulations (Allen & Stott, 2003). To 73 better account for the uncertainty in the estimation of forcings Ribes et al. (2013) pro-74 posed to use a regularized estimator of the covariance matrix of internal variability. A 75 review, based, among other, on regularized optimal forcing estimates, concluded that the 76 likely range (5-95% range) of the attributable anthropogenic GSAT anomaly in 2010-77 2019 relative to 1850-1900 is between +0.8 to +1.3°C (Eyring et al., 2021). The anomaly 78

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<sup>79</sup> attributable to greenhouse gases reported is  $+1.0^{\circ}$ C to  $+2.0^{\circ}$ C, while it is from  $-0.8^{\circ}$ C <sup>80</sup> to  $0.0^{\circ}$ C for other anthropogenic forcings, and from  $-0.1^{\circ}$ C to  $+0.1^{\circ}$ C for natural forc-<sup>81</sup> ings.

However, the optimal fingerprinting has several limitations such as the loss of in-82 formation due to the reduction of the temporal and spatial dimensionality of data, needed 83 to make a proper approximation of the covariance matrix of internal variability. Another 84 problem is the additivity assumption where the individual forcing effects are summed 85 together to estimate the climate response to the sum of forcings even if it is verified for 86 the attribution of historical GSAT (Marvel et al., 2015; Shiogama et al., 2013). This ad-87 ditivity assumption also found to be invalid for precipitation (Marvel et al., 2015), the 88 surface air temperature changes driven by greenhouse gases and aerosols can be non-additive 89 over the extra-tropical regions such as the Arctic (Deng et al., 2020) or the Southern Hemi-90 sphere (Pope et al., 2020). 91

To take account of non-additive changes, we present here a new method for attribut-92 ing past climate using machine learning. A neural network is a machine learning method 93 consisting of consecutive hidden layers of nonlinear transformations and adjustable weights 94 and biases which are determined by applying gradient descent using backpropagation 95 (Goodfellow et al., 2016). It is a statistical tool increasingly used in recent years in many 96 scientific fields (Choudhary et al., 2022). Convolutional neural networks (CNN, Yamashita 97 et al. (2018)) are a class of non-linear neural networks used notably in imagery problems 98 (O'Shea & Nash, 2015). Their main characteristic is the use of a learnable kernel that 99 slides along the input data. The CNNs have also shown their great capacity to analyze 100 time series and other one-dimensional patterns (Kiranyaz et al., 2021) and have become 101 common machine learning tools. For instance, without being exhaustive, neural networks 102 have been used in climate science to predict the evolution of El Nino Southern Oscilla-103 tion (Ham et al., 2019), to identify storm structures (Gagne II et al., 2019), for weather 104 prediction (Lam et al., 2022; Gagne II et al., 2019), or for detection studies (Labe & Barnes, 105 2021; Barnes et al., 2019). However, they are still emerging in large parts of the geosciences. 106 Here, we propose an alternative attribution framework based on a CNN to account 107 for interactions between the forcings. To the best of our knowledge, this is the first at-108

tempt to apply a neural network to the problem of detection and attribution of climate

- change. We compare the results obtained with the neural-network based attribution method
- with those resulting from regularized optimal fingerprinting. We chose to study the GSAT

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as it is widely studied in the detection and attribution literature in order to properly introduce our methodology. We investigate the effects of greenhouse gases, anthropogenic aerosols and natural forcings. In the future, this attribution method based on a neural network could be applied to other physical variables such as precipitation, or changes at the regional scale where non-additivity are expected to be more important (Good et al., 2015).

To evaluate our neural network based attribution method and compare it to regularized optimal fingerprinting, we first build synthetic data to assess the ability of methods to take non-addivities into account. Then we use a perfect model approach. This consists of removing data coming from one climate model and treating its simulations as pseudo-observations. The estimated effect of each forcing is then compared to their actual simulated effects.

The article is organized as follows. In section 2, we present the data and the preprocessing applied and how we built up synthetic data. In section 3, we present the neural network and its direct performance. We also introduce the two attribution methods used in this paper : backward optimization and regularized optimal fingerprinting (ROF). In section 4, we present the results obtained by the two attribution methods. Finally in section 5, we conclude and discuss the limitations as well as future perspectives.

#### <sup>130</sup> 2 Model and Data

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#### 2.1 Climate models simulations

In this section, we present the climate model data used in this study. We use the monthly surface air temperature from the outputs of the Coupled Model Intercomparison Project 6 phase (CMIP6; Eyring et al. (2016)) and of the Detection and Attribution Model Intercomparison Project (DAMIP; Gillett et al. (2016)) panel of CMIP6. All simulations from CMIP6 use the same experimental protocol with identical boundary conditions based on reconstructions and observations.

We use the historical simulations, called HIST, to obtain estimation of the combined effect of the forcings. These simulations use as variable boundary conditions all external forcings from 1850 to 2014. This includes the reconstructed concentrations of greenhouse gases, anthropogenic aerosols and ozone, and the estimated past variations of solar incoming radiation and land-use.

We also use single-forcing simulations to obtain estimation of the individual effect 143 of the forcings. These simulations use as variable boundary conditions only one of the 144 external forcings, all the other external forcings being fixed at their value from 1850. We 145 use the single-forcing simulations hist-GHG denoted later GHG, hist-aer denoted AER, 146 and hist-nat denoted NAT dedicated respectively to greenhouse gas concentrations, an-147 thropogenic aerosols, and natural forcings (i.e. volcanic aerosol and solar variations) as 148 variable forcings for the same period (1850-2014). The effect of stratospheric ozone and 149 land use was not investigated as only a few simulations have been performed in CMIP6, 150 and because their effective radiative forcings are much smaller than the ones of green-151 house gases, aerosols or natural forcings (Smith et al., 2020). 152

We also use the preindustrial control simulations, called PI, to estimate of the ef-153 fects of internal variability. These control simulations use fixed forcings from their es-154 timated pre-industrial levels corresponding that of 1850. The PI simulations are multi-155 centennial with usually a single realization for each climate model. These simulations 156 show a small drift due to incomplete spin-up or nonclosure of the energy budget (Hobbs 157 et al., 2016). Hereafter such small long-term drift (Irving et al., 2021) is deleted from 158 each PI simulations by removing a quadratic trend (Gupta et al., 2013) of the simulated 159 GSAT before analysis in all simulations. 160

All simulations but PI includes multiple realizations called ensemble members and denoted later as members. The members use different initial conditions which are sampled from the PI simulation. We use 12 atmosphere-ocean general circulation models (AOGCMs, see Tab. 1 for details) where at least two members are available for the simulations HIST, GHG, AER and NAT.

Model	$n_{GHG}$	$n_{AER}$	$n_{NAT}$	$n_{HIST}$	PI (yr)	$\sigma_{PI}$ (°C)	Reference
CanESM5	50	30	30	65	1000	0.10	Swart et al. (2019)
CESM2	3	3	2	11	500	0.13	Danabasoglu et al. (2020)
IPSL-CM6-LR	10	10	10	32	1000	0.15	Boucher et al. $(2020)$
ACCESS-ESM1-5	3	3	3	30	500	0.11	Ziehn et al. $(2020)$
BCC-CSM2-MR	3	3	3	3	600	0.17	Wu et al. (2019)
CNRM-CM6-1	9	10	10	30	500	0.13	Voldoire et al. $(2019)$
FGOALS-g3	3	3	3	6	700	0.10	Li et al. (2020)
HadGEM3	4	4	4	5	500	0.11	Roberts et al. $(2019)$
MIROC6	3	3	3	50	500	0.13	Tatebe et al. $(2019)$
MRI-ESM2.0	5	5	5	7	500	0.10	Yukimoto et al. (2019)
NorESM2-LM	3	3	3	3	500	0.15	Seland et al. $(2020)$
GISS-E2-1-G	5	7	15	19	500	0.15	Kelley et al. $(2020)$

**Table 1.** Presentation of the climate models used.  $n_{GHG}$ ,  $n_{AER}$ ,  $n_{NAT}$  and  $n_{HIST}$  denote the number of members used for GHG, AER, NAT and HIST. The duration of the PI simulation is indicated, in yr.  $\sigma_{PI}$  denotes the year to year standard deviation of the GSAT from PI, in °C.

#### 2.2 Observations

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We use observations of the 2m air temperature from HadCRUT5 (Morice et al., 167 2021). The gridded data is a blend of the CRUTEM5 (Osborn et al., 2021) land-surface 168 air temperature dataset and the HadSST4 (Kennedy et al., 2019) sea-surface temper-169 ature (SST) dataset. Such a blending is necessary because there are few observations of 170 temperature at 2 meters over the oceans compared to SST observations. The resulting 171 globally averaged quantity is called global mean surface temperature (GMST) and it dif-172 fers from the GSAT which is solely based on surface air temperature. In order to cor-173 rect this we multiply by 1.06 the GMST from observation to estimate the observed GSAT, 174 as estimated by Richardson et al. (2018). 175

#### 2.3 Pre-processing

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- All monthly climate model data are aggregated to an annual mean and spatially averaged from 90°S to 90°N to provide the GSAT. We then estimate the temperature anomalies compared to the pre-industrial period.
- We remove the time mean GSAT of PI from the GHG, AER, and NAT simulations. For observations and HIST, we compute the average temperature during the 1850-1900 period and remove it from the GSAT. Hereafter we only use the data from 1900-2014 period (115 years).

The simulated and observed GSAT can be separated into a forced component and 184 an internally-generated climate variability component. To reduce the effects of internal 185 climate variability we apply a low-pass filter to the GSAT of the GHG and AER sim-186 ulations. We use a Lanczos low-pass filter (Burger & Burge, 2009), with a window size 187 of 21 years, and a cutoff period of 10 years. The endpoints are estimated by extending 188 the time series by replicating the mean value of the first and last ten years of each sim-189 ulation. This should not alter the estimated effect of greenhouse gases or aerosols on the 190 GSAT as both forcings only show multi-decadal and longer fluctuations in terms of ef-191 fective radiative forcing (Gulev et al., 2021). We do not apply this procedure to NAT 192 and HIST because the emission of aerosol from volcanic eruptions induces an intense cool-193 ing for the next 2 to 5 years, and such smoothing would degrade the forced anomalies. 194 This smoothing procedure only lead to minor improvements regarding the estimated un-195 certainties (not shown). 196

We illustrate in Fig. 1 the processed data for all climate models, observations and 197 the multi-model mean (MMM) for each forcing. To compute the MMM we first compute 198 the ensemble mean (i.e averaging all ensemble member) for each climate model and then 199 we average the 12 ensemble means. In all models, GHG shows a monotonic warming with 200 an increasing slope since the 1960's, as expected from the greenhouse gases emissions. 201 In AER, the aerosol induces a cooling with a prononced slope from the 1940's to 1980's, 202 and a plateau from 1980 to 2014. NAT shows small cooling from 0.1 to 0.4°C only oc-203 curring after the major eruptive volcanic eruptions of Agung (1963), El Chichon (1982) 204 and Pinatubo (1991). HIST shows a monotonic warming less pronounced than GHG with 205 also a cooling a few years after the major volcanic eruptions. In all simulations, the in-206 ternal variability is important, as illustrated by the fluctuations visible in each members 207 (thin lines) and is reduced in the ensemble mean (thick lines). 208

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Figure 1. GSAT anomaly simulated by each model and (lower panel only) multi-model mean (MMM) and observed GSAT. Black lines show the HIST members. Red lines show the GHG members. Green lines show the NAT members. Blue lines show the AER members. The purple line shows the observations in the lower panel. Bold lines of the same colors show the ensemble mean.

#### 2.4 Synthetic data

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To investigate the performance of the attribution methods when considering ex-210 ternal forcings with non-additive influences, a synthetic data set is generated. We gen-211 erate three time series of size 115 denoted  $f_1$ ,  $f_2$  and  $f_3$ , that represents the forced ef-212 fects of three synthetic forcings. These time series are constructed to have similarities 213 with the expected influence of the greenhouse gases, aerosol and natural forcing for  $f_1$ , 214  $f_2$  and  $f_3$ , respectively (see Fig. red, green and blue lines in 2). However, the expressions 215 of  $f_1$ ,  $f_2$  and  $f_3$  remain arbitrary and are not meant to represent simulated or observed 216 climate. We detail in Text S1 the analytic expressions used to build the time series. We 217 construct the total effect of the three forcings combined, noted r, using two additional 218 term compared to the additive case : 219

$$r = f_1 + 0.3f_1^2 + f_2 + f_3 + 0.1f_1f_2 \tag{1}$$



Figure 2. Synthetic time series  $f_1$  (red),  $f_2$  (blue),  $f_3$  (green), and r (black). A randomly chosen time series after adding the variability is illustrated for  $F_1$  (orange),  $F_2$  (dark blue),  $F_3$  (dark green) and R (grey). Colors shades indicate one standard deviation across the 100 surrogate time series obtained for each pseudo-forcings and their response.

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Using an analogy with climate, anomalies are considered to result from the addition of a forced and an internally-generated variability component (see Fig. 1). We add an additional variability to  $f_1$ ,  $f_2$  and  $f_3$  and r that only represent the forced compo-

- nent. To generate this variability, we fit a first order autoregressive (AR1) model using
- the time series obtained from the concatenated PI simulations from all models. This AR1
- model is then used to generate 410 surrogate time series that are added to  $f_1$ ,  $f_2$ ,  $f_3$  and
- r. This provides the 100 time series for each forcings denoted  $F_1$ ,  $F_2$ ,  $F_3$  and 110 time
- series R resulting from the combined forcings (see Fig. 2).

#### 228 3 Methods

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#### 3.1 Backward optimization of a neural network

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#### 3.1.1 Neural network

In this section we describe the neural network used. We determine the relationship linking the GSAT from HIST to that of GHG, AER, and NAT using a CNN. In the training procedure, we use the GSAT from AER, GHG, and NAT as inputs and the GSAT from HIST as the target. Our goal is to construct a predictor that captures the role of all forcings combined. We assume that stratospheric ozone and land use do not affect this relationship.

A schematic of the CNN used is shown in Fig 3. CNNs can be used to construct 237 relatively simple neural networks as the number of weights and biases is directly decided 238 by the size and number of the filters used. We assume that this architecture is suitable 239 in the present case the size of the data set is relatively small compared to other neural 240 network applications. This might limit the overfitting which occurs when a neural net-241 work model performs significantly better for training data than it does for new data. In 242 our case, a one-dimensional kernel is applied to the temporal dimension. To fix the val-243 ues of the weights and biases of the convolutional layers, a neural network needs a learn-244 ing data-set composed of input-output pairs. The outputs are the GSAT of one HIST 245 member while the inputs are built with one member for each single-forcing simulations. 246 We build this data set by going through all combinations of GHG, AER, NAT and HIST 247 members of the same climate model. In order to test the backward optimization (see sec-248 tion 3.3), we removed one HIST member from each climate model and 10 for the IPSL-249 CM6-LR model from these combinations to serve as test data-set. This provides for the 250 training of the neural network  $N_d = (n_{HIST} - 1) n_{GHG} n_{AER} n_{NAT}$  4-tuples for each 251 climate model except for IPSL-CM6-LR with  $(n_{HIST}-10) n_{GHG} n_{AER} n_{NAT}$  4-tuples. 252 We note  $N_d$  the total number of the 4-tuples obtained for all models. The training data-253



Figure 3. Diagram of the CNN used. Each white-filled blue rectangles represents a time series of 115 years. The input layer is shown on the left, the hidden layers on the middle and the output layer on the right. Light blue-filled rectangles represent the kernels of the different hidden layers. Dark blue-filled rectangles represent the output of the kernel. Zero-padding is shown in green with dotted lines.

set is thus of size  $N_d$  which is of the order of  $10^5$  while an individual input is of size (3,115) and its corresponding output of size (1,115). The usual practice is to go through this database a number of times to train the CNN. However, we have altered the procedure to provide a similar weight to all models during the training.

Three steps are applied. First, a climate model is randomly selected. Secondly, we randomly select one 4-tuple from the chosen climate model. Then the CNN is trained using the three GSAT time series dedicated to (GHG, AER, NAT) as input and the GSAT dedicated to HIST as the target. We iterate this process by repeating it 5.10<sup>6</sup> times. A lower number of iterations was found to degrade the backward optimization results (not shown), but the results are otherwise similar when increasing the number of iterations.

A neural network uses hyperparameters which are the variables that determine the network structure and those which determine how the network is trained. The hyperparameters are chosen using a cross-validation, as detailed in Text S2 and Fig. S1. The chosen architecture has three convolutional hidden layers, a kernel size of 5 for all layers and 32 filters for each layer.

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#### 3.2 Performance of the CNN

Before presenting the neural network dedicated to the attribution method in the 270 next section, we investigate the performance of the CNN in estimating the total effect 271 of forcing from the effect of each forcing separately. First, we train the CNN using the 272 data from all models and estimate the mean training RMSE made in predicting the data 273 for each model separately. Second, we successively train the CNN leaving out the data 274 from one model and estimate the mean cross-validation RMSE in predicting the left-out 275 model data. Because internal variability is included in the training data, we expect the 276 RMSE to exceed the internal variability in all climate models. The training RMSE is 277 within 0.10°C and 0.25°C for the different climate models. Indeed, the models with large 278 training RSME (Fig. 4 blue bars) corresponds to those simulating a large internal vari-279 ability, as estimated by the standard deviation of the GSAT of the PI simulation (Tab. 280 1), where the forced signal is absent. 281

The CNN also should produce an estimated GSAT similar to the mean output from 282 the training data, which is expected to be similar to the MMM from HIST. The train-283 ing RMSE may also reflect a forced signal in the HIST simulations distinct from the other 284 models. The amplitude of the RMSE increases to 0.15°C-0.35°C when using cross-validation. 285 This suggest that the CNN does not overfit. HadGEM3 and, to a lesser extent, FGOALS-286 g3 and GISS-E2-1-G, show differences much larger than the training RMSE when the 287 data from these models is used for the validation. This might reflect important singu-288 larities for these three models, which is probably linked to their singular response to forc-289 ings. This might be linked to the equilibrium climate sensitivity which quantifies the abil-290 ity of a model to warm up when greenhouse gases increase. It depends on the feedbacks 291 acting in the climate system, and remains poorly constrained by observations (Sherwood 292 et al., 2020). GISS-E2-1-G simulate one of the lowest equilibrium climate sensitivity, while 293 HadGEM2 has one of the highest sensitivity. In addition, FGOALS-g3 simulate almost 294 no response to anthropogenic aerosols (see Fig. 1) 295

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#### 3.2.1 Backward optimization

In this section we describe how we use the CNN to perform climate change attribution. The backward optimization is a method that infers the most likely input of the CNN from a given output. To attribute climate change from the CNN, we calculate such

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Figure 4. RMSE between the CNN output and the GSAT of HIST, in °C, when using (blue bar) the training data and (cross validation, orange bar) when using the data of a model left out in the training.

input, which provides the GSAT attributed to the three forcings from the total GSAT anomaly observed or simulated. This is a neural network interpretation method (Toms et al., 2020; Gagne II et al., 2019; McGovern et al., 2019) also known as variational inversion when applied to a geophysical model (Brajard et al., 2012). A scheme of the procedure is given in Fig. 5. This optimal input is determined by minimizing a dedicated cost function and using the backpropagation. The cost function, called J, is:

$$J(\mathbf{X}) = \text{MSE}(\mathbf{y}, \text{CNN}(\mathbf{X})) + B \text{ MSE}(\mathbf{X}, \bar{\mathbf{X}}) + C\sigma_{HF}$$
(2)

where  $\mathbf{X} = (x_{GHG}, x_{AER}, x_{NAT})$  is the optimal input to be determined, i.e. a triple of 306 115-yr time series corresponding to the GSAT induced by greenhouse gases, anthropogenic 307 aerosols and natural forcing.  $\mathbf{X}$  is the three time series obtained with the MMM of the 308 simulations GHG, AER and NAT (see Fig. 1, lower panel). MSE denotes the mean squared 309 error. y is the desired output of the neural network.  $\sigma_{HF}$  is the sum of the time stan-310 dard deviation of the high-pass filtered time series obtained from  $x_{GHG}$  and  $x_{AER}$  us-311 ing a Lanczos high-pass filter with a window of size 21, a cutoff period of ten years. B312 and C are two adjustable real parameters. 313

The first term on the right hand side of equation (2) measures the mean square 314 error between the desired output and the CNN output. The second term, also known 315 as a background term, is applied so that the results are similar to a first guess, taken from 316 the MMM in order to avoid absurd and nonphysical solutions. Although this term is not 317 standard for the backward optimization of a neural network, it is however used for the 318 variational inversion procedure used in data assimilation (Brajard et al., 2012; Fablet 319 et al., 2021). The last term is used to build smooth GSAT time series for the forcings 320 associated with greenhouse gases and anthropogenic aerosols. Again, this term is not used 321 for the natural forcings, so that the effects from volcanic aerosols remains unsmoothed, 322 with cooling peaks lasting two to five years, as expected. 323

When estimating the optimal input, the initial input is iteratively updated using a back-propagation to minimize  $J(\mathbf{X})$  until it is smaller than a fixed value, called A. To reduce the computational cost, the minimization process is stopped after 500 iterations if  $J(\mathbf{X})$  does not converge. The backward optimization of a neural network has multiple solutions and the method is sensitive to the initial value used for  $\mathbf{X}$ . Therefore, for each of the twelve climate models, we randomly select with repetition 100 (10 during the perfect model approach) triples of the GSAT time series among the members of GHG,

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Figure 5. Schematic of the backward optimization attribution process with one entry denoted  $\mathbf{y}$  at the right. The 1200 backward optimization results are at the bottom. The learned CNN is in the middle in dark blue. J(X), the cost function of the backward optimization is on the top. X denote the optimized input and  $\hat{\mathbf{y}}$  denotes its image by the CNN. The 1200 starting points are on the left.

AER, and NAT as first guess for the initial states. These initial states are chosen as they 331 represent physically coherent inputs. This provides 1200 initial physically coherent val-332 ues for  $\mathbf{X}$  which sample the internal climate variability and the spread among the dif-333 ferent models. This generates 1200 backward optimizations. This estimation is empir-334 ical and does not account for the internal variability of the target of the backward op-335 timization. For each year, the 90% confidence intervals of the optimal input is then es-336 timated using  $\pm 1.64$  standard deviations among the backward optimization results as-337 suming a Gaussian distribution. 338

The choice of A (iteration stop treshold), B (background term) and C (smoothing term) was fixed empirically as the other hyperparameters of the neural network. We found that these parameters do not significantly modify the results of the backward optimisation (see Text S3, Tab. S1 and Tab. S2). We select A = 0.05, B = 0.01 and C =0.1.

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#### 3.3 Regularized optimal fingerprints

We evaluate the performance of the neural network based method for detection and attribution by comparing its results to those obtained with the regularized optimal fingerprinting (ROF, Ribes et al. (2013)). This last method is widely used and has already been applied to the air surface temperature using CMIP6 data by Gillett et al. (2021).

The ROF method is based on a multivariate linear regression and on the assumption that the observed change can be obtained with the sum of the forced anomalies for each forcing (the so-called fingerprints) plus internal variability.

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The observed GSAT denoted  $\mathbf{y}$ , is given by:

$$\mathbf{y} = \beta \mathbf{X} + \epsilon \tag{3}$$

with  $\beta = (\beta_{GHG}, \beta_{AER}, \beta_{NAT})$  the scaling factors and  $\mathbf{X} = (X_{GHG}, X_{AER}, X_{NAT})$ the effects of all the forcings on the GSAT.  $\epsilon$  represents the effect of internal variability, assumed to be a Gaussian white noise.

We use greenhouse gases, anthropogenic aerosols and natural forcings as three individual forcings and neglect the other forcings. **X** is estimated in this case by using the MMM of GHG, AER and NAT simulations.

To perform such a regression, a common method is to reduce the dimension of data using the leading empirical orthogonal functions calculated in PI. This reduces the number of spatial dimensions and allows an accurate estimation of the internal variability covariance matrix. But such a method involves an arbitrary choice of the number of EOFs used to truncate the data. The ROF method (Ribes et al., 2013) avoids this arbitrary choice using a regularized estimation of the covariance matrix to estimate the scaling factors.

The response of climate to the *i*-th forcing is detected if  $\beta_i$  is significantly differ-366 ent from zero. If the confidence interval of  $\beta_i$  includes one, this shows consistency be-367 tween observations and simulated climate model responses. We use the total least square 368 (TLS) method (Allen & Stott, 2003) to perform the regression and estimate the scaling 369 factors, which accounts for the residual internal variability in the MMM. The internal 370 variability is assumed to be the same in GHG, AER and NAT members, which prevents 371 the use of different smoothing to the GSAT simulated in GHG and AER, as done for the 372 backward optimization, or in NAT. As the internal variability is largely reduced by the 373 ensemble averaging in the MMM, we estimate the attributable warming in GSAT by  $\beta_i X_i$ 374

for the i-th forcing. This should lead to an attributable warming similar to  $\beta_i \hat{X}_i$  using

the estimated  $X_i$  by the TLS instead of  $X_i$ . Estimates of attributable warming in GSAT

for each year can then be obtained by  $\sum \beta_i X_i$ . Following Gillett et al. (2021), the in-

ternal variability is sampled by concatenating all available simulations after subtraction

<sup>379</sup> of the mean of the corresponding model ensemble. To account for the subtraction of the

ensemble mean, we multiply for each model, the anomalies by  $\sqrt{\frac{n}{n-1}}$ , where n is the en-

semble size. For each simulation, the equivalent size corresponding to the MMM is es-

382 timated using:

$$N = \frac{M^2}{\sum_{i=1}^{M} \frac{1}{n_i}} \tag{4}$$

with M the number of different climate models used (in our case 12) and  $n_i$  the num-383 ber of members available for the i-th climate model. To estimate the uncertainty in the 384 GSAT effect attributable to the *i*-th forcing, it is necessary to take into account the un-385 certainty of  $\beta_i$  and the internal variability contained in  $X_i$ . For each year and forcing, 386 the uncertainty in the attributable GSAT is calculated using 1000 random draws assum-387 ing a gaussian distribution for both  $\beta_i$  and  $X_i$ . The mean and standard errors of  $\beta_i$  are 388 estimated as in Allen and Stott (2003). The mean and standard deviation of  $X_i$  are es-389 timated from the size N of the MMM and the standard deviation of the GSAT obtained 390 from the PI runs. We first calculate the standard deviation for each model (as given in 391 Tab. 1), average the values obtained across models, and then divide by the square root 392 of N. This procedure is valid under the conditions that the uncertainties of  $\beta_i$  and  $X_i$ 393 are Gaussian, uncorrelated and small compared to their respective means. The latter hy-394 pothesis is not verified for GSAT anomalies close to zero for  $X_i$ , such as those obtained 395 in the first decades of our time series (see Fig. 1), or for the GSAT of NAT. Thus the 396 uncertainties for the attributable GSAT are to be taken with caution. 397

398

#### 4 Attribution performances

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#### 4.1 Performance on synthetic data

To investigate the performance of the backward optimization and ROF in the case of non-additive data, we applied the two attributions methods to the synthetic data presented in section 2.4. Fig. 6ac shows the time series of the estimated effect of the three synthetic forcings and  $f_1$ ,  $f_2$  and  $f_3$  the ground truth time series. We use the 100 sur-



Figure 6. Estimated  $f_1$ ,  $f_2$  and  $f_3$  given by (a) ROF and (c) backward optimization. The original  $f_1$ ,  $f_2$  and  $f_3$  ground truth lines are shown in bold. Histograms shows the distribution of the RMSE of the results of b) ROF and d) backward optimization compared to the ground truth.

rogate time series generated for each forcings and their response denoted  $F_1$ ,  $F_2$ ,  $F_3$  and 404 R, instead of the simulated GSAT from GHG, AER, NAT and HIST, respectively. The 405 10 R time series remaining are used as pseudo-observation, noted  $\mathbf{y}$  previously. For the 406 backward optimisation the estimated forced effect  $f_1$  (Fig. 6c, red lines) show some vari-407 ability but is centred around the true  $f_1$  (purple line). For ROF (Fig. 6a, red lines), the 408 estimated  $f_1$  are systematically larger than the true  $f_1$  at the end of the time series. Sim-409 ilarly,  $f_2$  (Fig. 6c, blue and dark blue lines) is well estimated by the backward optimiza-410 tion, while ROF (Fig. 6a) produce an estimated  $f_2$  with an important variability and 411 an overestimation in most of the cases. The  $f_3$  forcing is well estimated by both meth-412 ods, but with more variability for backward optimization. 413

The RMSE between the effect estimated by the different attribution methods and the ground truth are shown in 6bd in the form of boxplot. For ROF the mean RMSE value is 0.14°C for  $f_1$ , 0.12°C for  $f_2$  and 0.01°C for  $f_3$ . These values are for backward optimization of 0.05°C for  $f_1$ , 0.04°C for  $f_2$  and 0.04°C for  $f_3$ . Backward optimization therefore provides errors smaller than ROF in case of the non-additive forcing generated, while the use of ROF lead to important errors.

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### 4.2 Evaluation of the performances in attributing climate changes : perfect model approach

To evaluate the performance of the backward optimization and ROF we use a per-422 fect model approach that relies on climate model data only. This approach consists of 423 using the data from all but one of the climate models to perform our two attribution meth-424 ods. In the case of backward optimization, this implies that we do not use the data from 425 a climate model during the CNN training phase, in the starting points, or in the MMM 426 calculation. For ROF, the data of a model are not used to construct the climate noise 427 estimate or included in the MMM. We use a HIST member of the test dataset (see Sec-428 tion 3.3) from each climate model as the target for the attribution methods. The attributable 429 anomalies associated with each forcing are then compared with the ensemble mean of 430 the GHG, AER and NAT simulations of the removed climate model, even if it includes 431 some residual internal variability, especially when the number of members is small. We 432 use the paradigm that "climate models are statistically indistinguishable from the truth" 433 (Ribes et al., 2017; Hargreaves, 2010; van Oldenborgh et al., 2013), where the difference 434 between observations and models is assumed to be distributed as the difference between 435

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any pairs of climate models. We therefore assess the capability of the attribution methods when using observations by investigating only climate models. This approach is called
a perfect model approach by analogy with the methods developed for seasonal (DoblasReyes et al., 2013) or decadal (Hawkins et al., 2011) climate forecast.

Figure 7 illustrates the attributable anomalies calculated from an HIST member for each climate model. The ensemble means of GHG, AER and NAT simulations for that climate model are shown for comparison. The differences between the attributable anomalies and the ensemble means of GHG, AER and NAT are also quantified in Fig. 8ab and 8ef with the RMSE and the time mean difference between the two time series. Lastly, the widths of the 90% confidence intervals in 2000-2014 are compared in Fig. 8cd.

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The two methodologies show a monotonic warming induced by the greenhouse gases that intensified in the 1970's for all climate models. The cooling effect of anthropogenic aerosols is also consistent for both methods, with an intensified cooling in the 1970's, also known as global dimming (Wild, 2009), followed by a stabilization in the 2000's. Lastly, the changes attributable to natural forcings are small in both methods, except for the cooling following the major volcanic eruptions.

For the backward optimization, the RMSE is 0.14°C, 0.20°C and 0.12°C when av-453 eraged across the 12 models for the effects of greenhouse gases, anthropogenic aerosols 454 and natural forcing, respectively (see dashed line in Fig. 8a). ROF provides an average 455 RMSE of 0.20°C, 0.15°C and 0.12°C for these forcings (dashed lines in Fig. 8b), so the 456 errors are similar in both methods. Moreover ROF shows an average positive bias of 0.09°C 457 for greenhouse gases. All other biases for ROF and for backward optimization are almost 458 zero. ROF, therefore seems to over-estimate the effect of greenhouse gases which is not 459 the case of the backward optimization. 460

However, RMSE and biases are affected by the residual internal variability included in ensemble means especially when only a few members are available. The RMSE and biases are therefore weak indicators for models with few members. The width of the confidence intervals for greenhouse gases and anthropogenic aerosols obtained with the backward optimisation are smaller than those obtained with ROF from the 1970's, while they are larger from 1900 to 1940. Although the uncertainty provided by the confidence intervals of ROF was verified using a perfect model approach in Gillett et al. (2021), some

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Natural forcings attributable change

Ensemble mean of NAT

Attributable GSAT in °C calculated for ROF and backward optimization from Figure 7. (black line) a HIST member. The GSAT is decomposed into the attribuable changes due to (red line) greenhouse gases; (blue line) anthropogenic aerosols and (green line) natural forcings. For comparison, the ensemble mean of (purple line) GHG, (dark blue line) AER and (beige line) NAT is indicated. Color shades show the 90% confidence intervals of the attributed GSAT. -22-



**Figure 8.** Performances of attribution methods using a perfect model approach. a) RMSE when using ROF for the attributable GSAT anomaly of (red) greenhouse gases, (blue) anthropogenic aerosols, (green) natural forcing. b) Same as a) for the backward optimization. c) Width of the 90% percent confidence intervals in 2000-2014 when using ROF. d) same as c) but for backward optimization e) Time mean difference between the estimated and ensemble mean GSAT attribuable to the forcings when using ROF. f) Same as e) for backward optimization. Dashed lines shows average values across the 12 climate models.

authors suggested that ROF underestimates such uncertainty because of insufficient con-468 sideration in the internal variability (Li et al., 2021; DelSole et al., 2019). This suggests 469 that the confidence intervals given by the backward optimisation are also underestimated, 470 and that further improvements would be needed to evaluate them in more details. 471

The width of the confidence intervals for the effect of natural forcing (Fig. 8cd, green 472 points) is in ROF much lower than this obtained with the backward optimization. This 473 might be explained by the calculation of the confidence intervals of ROF which is not 474 adapted to small anomalies (see section 3.4) as obtained for natural forcings. Moreover 475 we evaluate the uncertainty for the backward optimization by sampling both the inter-476 model and internal variability contained in the starting points, so that the confidence 477 intervals are rather homogeneous in time and for the three forcings. We suggest that both 478 estimations need to be refined using larger ensembles of simulations. This would allow 479 a more systematic assessment of the uncertainties using the perfect model approach. 480

Figures 7 and 8 also show that the cooling from anthropogenic aerosols is overes-481 timated in FGOALS-g3 in backward optimization results compared to the ensemble mean, 482 and underestimated in CanESM5 and HadGEM3. It is likely that effect of external forc-483 ings in these three models is very different from the other models. For instance, FGOALS-484 g3 simulates a negligible effect for the aerosols in AER (see Fig. 1). CanESM5 and HadGEM3 485 simulate a warming induced by greenhouse gases (see GHG simulation) larger than the 486 other models, probably associated with the important equilibrium climate sensitivity of 487 these models. The backward optimization fails to reproduce these singular behaviors, 488 being mostly governed by the multi-model consensus. The CNN-based method, i.e. the 489 backward optimization, shows results less variable between models than ROF. The back-490 ward optimization attributable changes are more consistent with the multi-model con-491 sensus, which is hardly affected by removing the data from one climate model. In con-492 trast, in ROF the MMM time series is rescaled with the scaling factors (see section 3.3). 493 This leads to important errors when the data used as pseudo-observation is taken from 494 a model with a large sensitivity (see for instance CanESM5). 495

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Figure 7 is only based on the use of a single historical simulation for each model. Therefore, we also investigate if the attribuable changes are affected by a modification 497 of the historical member. The attribuable GSAT is estimated with the two methods from 498 the ten HIST IPSL-CM6-LR member from the test data (see section 3.1.1). The RM-499

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SEs, the biases and the width of confidence intervals are obtained with respect to the
ensemble mean of the single-forcing simulations of the IPSL-CM6-LR model (Fig. S2).
Backward optimization presents much less variable results between members than ROF
in terms of RMSE or bias, except for natural forcing. The amplitude of the confidence
intervals is slightly increases for the backward optimization compared to ROF. It results
that backward optimization is less affected by internal variability than ROF.

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#### 4.3 Attribution of the observed GSAT

After studying the performance of ROF and backward optimization for synthetic data and in a perfect model approach, we apply both methods to the observed GSAT anomalies.

The attributable GSAT changes are similar for ROF and backward optimization 510 (see Fig. 9). For example, in 2000-2014, ROF provides a GSAT attributable to green-511 house gases of 1.28°C (90% confidence interval of [0.85°C,1.71°C]), while it is -0.33°C 512 ([-0.80°C,0.12°C]) for anthropogenic aerosols and 0.01°C ([0.0°C,0.02°C]) for natural forc-513 ing. In comparison, backward optimization finds attributable changes of 1.42°C ([1.03°C,1.80°C]), 514 -0.61°C ([-1.16°C, -0.06°C]) and 0.02°C ([-0.33°C, 0.38°C]), respectively, for these three forc-515 ings. Nevertheless, backward optimization provides more noisy time series and more cool-516 ing during volcanic eruptions. The similarity of the results between ROF and backward 517 optimization suggests that the GSAT changes are largely additive as found in Marvel 518 et al. (2015) or Shiogama et al. (2013). 519

The attributable changes of the GSAT given by ROF are much comparable to that of Gillett et al. (2021) who studied the effect of other forcings (land use and ozone) together with the greenhouse gases. Their results for the 2010-2019 decade provide a 5%-95% range of the attributable warming of [1.2°C,1.9°C] for greenhouse gases and other forcings, [-0.7°C,-0.1°C] for anthropogenic aerosols and [0.01°C,0.06°C] for natural forcing. We verified that the ROF results shown in Fig. 9 remain similar when we take into account other forcings together with the greenhouse gases influence (see Fig. S3).

Backward optimization shows a slightly smaller uncertainty for greenhouse gases and anthropogenic aerosols than ROF toward the end of the time series, but a larger uncertainty range for natural forcings, as found and discussed in section 4.2. We can note that the reconstruction of the observations by the backward optimization is by construc-

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**Figure 9.** (Top) Attributable GSAT anomaly, in °C, as given by ROF for the effect of the (red) greenhouse gases, (green) natural forcings and (blue) anthropogenic aerosols. The black line shows the observed GSAT. The color shade shows the 90% confidence interval. (Bottom) : same as top, but for backward optimization.

tion very close to the observations (see Fig. S4) and captures most of the internal variability contained within the observations.

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#### 4.4 Focus on the main backward optimization results

The backward optimization uncertainties are computed sampling various initial inputs. Backward optimization is often used with an all-zeros starting point (Toms et al., 2020) even if McGovern et al. (2019) have optimised the initial inputs by using coherent starting points as done in the present study. Figure 10 shows the boxplots of the attributable changes in 2000-2014 when using the observations and backward optimization, as previously discussed in section 4.3, classified according to the climate models used for the initial input.

The attributable changes produced by the backward optimization are influenced 541 by the climate model used to generate the initial input. For example, CanESM5 sim-542 ulates large warming in response to greenhouse gases (see Fig. 1), probably linked to its 543 large equilibrium climate sensitivity. When using the outputs of CanESM5 as initial in-544 put of the backward optimization, large attributable changes are obtained for both the 545 greenhouse gases and the anthropogenic aerosols. On the other hand, when using an ini-546 tial input from FGOALS-g3 the changes due to the greenhouse gases and the anthro-547 pogenic aerosols are small. For each forcing, we analyse the dispersion of the GSAT anoma-548 lies over the years 2000-2014 by estimating the mean GSAT attributable to the use of 549 all starting points for each of the 12 climate models. The variability explained by the 550 model is calculated by is the standard deviation across these 12 attributable GSAT. The 551 residual variability which accounts for the internal variability of the starting points is 552 estimated by the standard deviation of the 1200 attributable GSAT after subtracting for 553 each time series the average response obtained with their respective climate model. The 554 standard deviation explained by the model of the starting point is 0.22°C for greenhouse 555 gases, 0.29°C for anthropogenic aerosols and 0.14°C for natural forcings. The residual 556 standard deviation is of 0.06°C for the greenhouse gases, 0.09°C for the anthropogenic 557 aerosols and 0.1°C for the natural forcings. The residual variance therefore is smaller than 558 this associated with the climate model for each forcing, especially for the greenhouse gases. 559 The range of attribution results is about 1°C for all forcings, with some particular mod-560 els providing attribuable anomalies at the head or the tail of the inter-models distribu-561 tion when used as starting point. Removing or modifying these outliers to improve the 562

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**Figure 10.** Boxplots of the attributable changes in 2000-2014 when using observation and backward optimization, classified according to the climate model used as initial inputs for (A) the greenhouse gases (B) the anthropogenic aerosols and (C) the natural forcings.

backward optimization results have been considered. However, selecting these initial inputs may imply a selection of climate models which needs to be associated with a careful investigation of the physical mechanisms (Coquard et al., 2004).

#### 566 5 Discussion and conclusion

We present a method for detection and attribution of climate data based on a back-567 ward optimization of a convolutional neural network (CNN). We trained the CNN on 568 the simulated GSATs obtained from outputs of twelve CMIP6 climate models. We then 569 performed a backward optimization to estimate the attributable changes. This method-570 ology does not assume that the effects of the external forcings are additive. Such addi-571 tivity implies that the total changes simulated by the forcings can be obtained by the 572 sum of the changes due to the individual forcings. The additivity assumption is an im-573 portant limitation when focusing on precipitation (Marvel et al., 2015) or at regional scale 574 (Pope et al., 2020; Deng et al., 2020). We evaluated the effect of internal variability and 575 model dispersion by using different starting points sampling the simulated distributions. 576 We compared the results of the CNN backward optimization with those obtained using 577 the regularized optimal fingerprinting (ROF) (Allen & Stott, 2003; Ribes et al., 2013). 578 In order to assess the ability of backward optimization to deal with non-additivities in 579 forcing compared to ROF we used synthetic data, which, unlike GSAT, have a strong 580 non-additive behavior. In that case, the backward optimization results are more simi-581 lar to the true forced effect of the forcings than when using ROF which assumes addi-582 tivity. To see if this results can be generalised additional investigations need to be con-583 ducted using either different synthetic data or real non-additive climate data, as for in-584 stance the precipitation field. 585

We also designed a perfect model approach to evaluate the skill of the two meth-586 ods. We successively removed the data of each climate model and used an historical mem-587 ber of the removed climate model as pseudo-observation. The attributable changes of 588 each forcing are then compared to their actual effect simulated in the corresponding en-589 semble mean of single-forcing simulations. Backward optimization is found to provide 590 performances similar to that obtained with ROFs in terms of RMSEs or bias. The con-591 fidence intervals of the backward optimization are smaller for greenhouse gases and an-592 thropogenic aerosols in the last years of the studied period and much larger for natu-593 ral forcings than those obtained by ROF. As the calculation of the uncertainty applied 594

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in ROF has been previously shown to be also underestimated (DelSole et al., 2019), this 595 suggests that backward optimization leads to an even larger underestimation. This might 596 be linked to the internal variability of the target time series, which is not accounted for 597 in the neural network-based method. A solution to solve this issue would be to gener-598 ate surrogate time series for the backward optimization and repeat the backward opti-599 mization. Larger ensemble of single forcing simulations, such as those proposed in the 600 Large Ensemble Single Forcing Model Intercomparison Project (D. M. Smith et al., 2022), 601 would also be required to refine of the estimated errors. In addition, the changes attribuable 602 to natural forcings in the backward optimization have a larger uncertainty than the one 603 of ROF. This is suggested to be an artefact of the estimated uncertainty used, which may 604 be flawed for small changes. Many aspects of the backward optimization can be improved 605 in future works. The backward optimization process can also be improved by giving weights 606 based on the realistic simulation of the interannual to decadal variability. Indeed, the 607 procedure presented here is designed to produce a close agreement between the recon-608 structed time series and the observations (or pseudo-observations). As shown in Fig. S4, 609 the reconstructed time series, i. e. the image of the CNN using the backward optimiza-610 tion results, closely follow the observations. The CNN might instead be designed to only 611 reproduce the forced component of the anomalies excluding the internal variability un-612 related to climate forcings. A better treatment of the initial state could be also inves-613 tigated, excluding or penalizing the time series used as initial input when inconsistent 614 with observations. In addition, giving different weights to each climate models accord-615 ing to their performance in reproducing observed features could be considered, such as 616 the observed GSAT evolution in Ribes et al. (2021). 617

Overall, the attributable changes obtained with the backward optimization are con-618 sistent with recent attribution results, as reviewed in Eyring et al. (2020a). This con-619 firms the previous detection and attribution results on the GSAT. This study also shows 620 that neural networks can be used to explore the CMIP databases through the backward 621 optimization presented here. Such a method could be deployed on other physical vari-622 ables, such as precipitation. It could also easily be applied to spatial average instead of 623 global mean where the non-additivities could be an obstacle. Lastly, a similar method 624 applied on gridded data could also be considered without major modifications given that 625 CNNs can easily process images. 626

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#### 6 Open Research

**Data Availability Statement** 628 The CMIP6 data is available through the Earth System Grid Federation (Cinquini 629 et al., 2014) and can be accessed through different international nodes. For example,: 630 https://esgf-node.ipsl.upmc.fr/projects/esgf-ipsl/ 631 Codes used in this article for the backward optimization and the figures are from 632 Bône (2023) software available freely at https://doi.org/10.5281/zenodo.7248662. 633 The ROF results have been obtained using the Eyring et al. (2020b) software (version 634 2.9.0) that can be freely found at https://github.com/ESMValGroup/ESMValTool/releases/ 635 tag/v2.9.0. 636

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## Supporting Information for "Detection and attribution of climate change using a neural network"

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- 1. Text S1 to S4
- 2. Figures S1 to S3
- 3. Tables S1 to S2

#### Introduction

This supporting information gives some details on the construction of the synthetic data. We present how the  $f_1$ ,  $f_2$  and  $f_3$  time series are constructed. The methodology adopted for the choice of the hyperparameters for the neural network and the backward optimization is alsopresented. Then, the effect of the internal variability is investigated by repeating ROF and backward optimization using the HIST member from IPSL-CM6-LR the changes of the attributable anomalies are illustrated when accounting land use and ozone forcing in ROF. Lastly, we illustrate the reconstitution of the observation by the CNN.

#### Text S1. Synthetic dataset

We define three time series,  $f_1$ ,  $f_2$  and  $f_3$  as  $t \in \{1, 2, 3...115\}$ :

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$$f_1 = 6.10^{-5}t^2 + 2.10^{-3}t$$
  
 $f_2 = -0.5sin(\frac{t\pi}{150})$   
 $f_3 = 1.10^{-5}t^2 - 1.10^{-3}t + f_{add}(t)$ 

 $f_{add}$  is a term added to represent the effect of three pseudo-volcanic eruptions for  $t \in \{9, 49, 89\}$ . This term is an additional anomaly that last for five years and is defined as :  $f_{add} = e^{\frac{2}{3}(t-t_j)}$  if  $t \in [t_j, t_j + 4]$  and  $t_j \in \{9, 49, 89\}$  and 0 otherwise

:

#### Text S2. Choice of hyper-parameters of the neural network

The hyperparameters of the CNN are the number of hidden layers, the cost function, the non-linear activation function, the size of the kernel, the length of the hidden layers, the learning rate, the type of padding used, and the batch size. The effects of the type of padding, the activation function, the batch size and the learning rate have not been investigated. We use the RMSE cost function and zero-values padding. A non-linear activation function is used between the hidden layers of the neural network in our case the hyperbolic tangent function. To determine the other hyper-parameters we use a cross validation. We considered the data from the 12 models but leaving out the data of one climate model. We train a CNN using the remaining models. The process was repeated by excluding successively each climate model. For each CNN built we also select randomly a historical member of the climate model left out as pseudo-observations, and perform the backward optimization. We compare the results to the ensemble mean of the simulations for this climate model. The mean value of the 12 backward optimization RMSE, is illustrated in Fig. S1 for different sets of hyperparameters.

The backward optimization RMSE are between 0.18°C and 0.41°C. The number of filters of the layer shows the largest influence, with a reduction of the RMSE for increasing length of the hidden layers. The number of hidden layers and the kernel sizes does not affect the RMSE. We choose the architecture that gives the lowest backward optimization RMSE while keeping a small number of weights and biases with three hidden layers, a kernel sizes of 5 and number of filters of 32.

:

#### Text S3. Choice of the hyper-parameter of the backward optimization

Tables S1 and S2 shows the mean RMSE of the backward optimization described, for differents values of A, B, and C. The difference of performance is small in all experiments. We noted that large values of A and B reduce dramatically the variability of results of the backward optimization (not shown) and select A=0.05, B=0.01 and C=0.1. We choose a non-zero value for B to keep a background term although it only has a marginal effect on the RMSE.



**Figure S1.** A) Mean cross-validation RMSE (in °C) for differents kernel sizes and number of filters while using three hidden layers. B) same as A) but with 5 hidden layers.

**Table S1.**Mean cross-validation RMSE (in °C) of the backward optimization fordifferent values of A and B, while C is fixed to 0.1.

	A=0.01	A=0.05	A=0.1
B=0	0.205	0.190	0.189
B=0.01	0.199	0.189	0.190
B=0.1	0.191	0.191	0.192

Table S2. Mean cross-validation RMSE (in  $^{\circ}\mathrm{C})$  of the backward optimization for different values of B and C, while A is fixed to  $0.05^\circ\mathrm{C}.$ 

	C=0	C=0.01	C=0.1
B=0	0.188	0.187	0.188
B=0.01	0.190	0.188	0.189
B=0.1	0.191	0.191	0.191

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**Figure S2.** Performances of attribution methodologies on the 10 removed IPSL-CM6-LR members A) RMSE distribution when using ROF and all 10 removed members as pseudo-observation for the attributable GSAT anomaly of (red) greenhouse gases, (blue) anthropogenic aerosols, (green) natural forcing. B) Same as A) for the backward optimization. C) Distribution of the widths of the 90 % percent confidence intervals in 2000-2014 when using ROF. D) same as C) but for backward optimization E) Distribution of the time mean differences between the estimated and ensemble mean GSAT attribuable to the forcings when using ROF. F) Same as E) for backward optimization.



**Figure S3.** Attributable GSAT anomalies calculated from ROF with observations when using anthropogenic aerosols, natural forcing and greenhouse gases as forcings (top) anthropogenic aerosols, natural forcing and greenhouse gases and other anthropogenic effect combined (bottom).



**Figure S4.** (Black) Observed GSAT anomalies, in °C, and (blue) the mean reconstruction of the observation by the CNN. Color shade shows the 90% percents confidence intervals of the mean reconstruction obtained across the 1200 backward optimization results available.