Multi-scale variability of internal solitary wave speed in the Sulu Sea

XiXi Li¹, Jianjun Liang², Kaiguo Fan³, and Xiaoming Li¹

¹Aerospace Information Research Institute, Chinese Academy of Sciences (CAS) ²Chinese Academy of Sciences ³State Key Laboratory of Satellite Ocean Environment Dynamics, Second Institute of Oceanography, Ministry of Natural Resources

August 22, 2023

Abstract

Internal solitary waves (ISWs) have considerable energy to drive the mixing of water masses in the Sulu Sea. The propagation speed is a critical parameter in demonstrating the dynamic characteristics of ISWs. We collected 1354 groups of ISWs' speeds from tandem satellite remote sensing images with short temporal intervals and analyzed their spatial and multi-scale temporal variations in the Sulu Sea. The wave speeds increase exponentially with water depth with a power of 0.26. The fortnightly spring/neap tidal currents cause daily variations of wave speeds up to 30%. In addition to the well-recognized stratification that leads to monthly variations of wave speed, the seasonal circulations lead to a maximum decrease of wave speeds by 0.27 m/s. With respect to interannual variations, the wave speeds increase in La Niña years and decrease in El Niño years, caused by the climatic modulation of ocean stratification.

Hosted file

971031_0_art_file_11287762_rz2qd2.docx available at https://authorea.com/users/652962/ articles/660184-multi-scale-variability-of-internal-solitary-wave-speed-in-the-sulu-sea

Hosted file

971031_0_supp_11274530_rz5ghs.docx available at https://authorea.com/users/652962/articles/ 660184-multi-scale-variability-of-internal-solitary-wave-speed-in-the-sulu-sea

Multi-scale variability of internal solitary wave speed in the Sulu Sea

- 2 Xixi Li^{1,3,5}, Jianjun Liang^{2,1,3}, Kaiguo Fan⁴ and Xiao-Ming Li^{2,1,3}
- ¹Key Laboratory of Digital Earth Science, Aerospace Information Research Institute, Chinese
 Academy of Sciences, Beijing, 100094, China.
- ²Key Laboratory of Earth Observation of Hainan Province, Hainan Aerospace Information
 Research Institute, Wenchang, 571333, China.
- ³International Research Center of Big Earth Data for Sustainable Development Goals, Beijing,
 100094, China.
- ⁴School of Meteorology and Oceanography, National University of Defense Technology,
 Changsha 410015, China
- ⁵University of Chinese Academy of Sciences, Beijing, 100049, China.
- 12

1

- 13 Corresponding authors: Xiao-Ming Li and Jianjun Liang (lixm@radi.ac.cn, liangjj@radi.ac.cn)
- 14 Key Points:
- Satellite observations yield wave speeds of ISWs in the Sulu Sea presenting multi-scale
 temporal variations from days to years.
- Tidal currents and seasonal circulations significantly modulate the wave speed.
- Evidence for interannual variation of wave speed driven by ENSO is presented.
- 19

20 Abstract

Internal solitary waves (ISWs) have considerable energy to drive the mixing of water 21 masses in the Sulu Sea. The propagation speed is a critical parameter in demonstrating the 22 dynamic characteristics of ISWs. We collected 1354 groups of ISWs' speeds from tandem 23 satellite remote sensing images with short temporal intervals and analyzed their spatial and 24 multi-scale temporal variations in the Sulu Sea. The wave speeds increase exponentially with 25 water depth with a power of 0.26. The fortnightly spring/neap tidal currents cause daily 26 variations of wave speeds up to 30%. In addition to the well-recognized stratification that leads 27 to monthly variations of wave speed, the seasonal circulations lead to a maximum decrease of 28 wave speeds by 0.27 m/s. With respect to interannual variations, the wave speeds increase in La 29 Niña years and decrease in El Niño years, caused by the climatic modulation of ocean 30 31 stratification.

32 Plain Language Summary

Internal solitary waves (ISWs) are a subsurface analogy of surface gravity waves. They 33 34 are characterized by large vertical isopycnal displacements and strong current shears. Understanding their characteristics and variations is essential to know how they generate and 35 dissipate. The Sulu Sea, which has high-frequency and strong ISWs, is a natural laboratory for 36 exploring the secrets of ISWs. The propagation speed is one of the critical parameters in studying 37 38 the characteristics of the dynamical processes of ISWs. In this paper, we collected 1354 groups of ISWs' speeds in the Sulu Sea using tandem satellite images and analyzed their spatiotemporal 39 40 variations. The results reveal that the variations of ISWs' speeds are primarily dependant on water depth, ocean stratification and background currents. Above all, it is the first time to give 41 observational evidence about the appreciable effect of tidal currents, seasonal circulations, and El 42 Niño Southern Oscillation on ISWs' speeds from days through months to years. 43

44 **1 Introduction**

Internal solitary waves (ISWs) are ubiquitous oceanic dynamics, characterized by a 45 temporal scale of tens of minutes and a spatial scale of hundreds to thousands of meters (Zheng 46 and Klemas, 1993; Apel, 2002; Jackson, 2004). They present an indispensable step for the 47 energy cascade from barotropic tides to diapycnal mixing (Garrett, 2003; Mackinnon et al., 48 49 2017). Moreover, ISWs greatly affect acoustic propagation (Zhou et al., 1991; Apel et al., 2007; Lynch et al., 2010), submarine navigation (Osborne et al., 1978; Wang et al., 2022), nutrient 50 distribution (Haury et al., 1979; Wang et al., 2007), and sediment transport (Da Silva, 2002). 51 52 Understanding their characteristics, variability, formation, and fate is important to parameterize 53 their mixing in numerical climate models (Alford et al., 2015).

54 Sulu Sea (SS, Figure 1a) is a natural laboratory to study the characteristics and dynamic processes of ISWs (Apel et al., 1985; Liu et al., 1985; Liu et al., 2019). The ISWs in the SS are 55 thought to be generated by the lee-wave mechanism (Apel et al., 1985). The ebb tide traps a 56 57 thermocline depression; then, as the tide turns, the depression escapes upstream over the sill barrier. They are formed near the Pearl Bank sill and propagate through the basin to dissipate as 58 they reach Palawan Island (Apel et al., 1985; Jackson et al., 2011). During their lifetime in the 59 60 SS, complex factors can affect the ISWs' generation and evolution: the fortnightly spring/neap tidal cycle, seasonal circulations in the upper layer (Cai et al., 2009; Han et al., 2009), and the 61

climate effect related to the El Niño–Southern Oscillation (ENSO) (Klein et al., 1999). However,
 how these factors affect the dynamic processes of ISWs in the SS is still poorly understood.

Propagation speed is one of the critical parameters to understanding dynamics and 64 energetics of the ISWs (Jackson et al., 2009; Lien et al., 2012; Zhang et al., 2022), also called 65 wave speed (Liu et al., 1985). Many studies have tried to figure out the characteristics and 66 variations of wave speed. By deploying moorings along a wave propagation path, researchers 67 estimate wave speed according to the wave arrival times at nearby moorings (Ramp et al., 2010; 68 Huang et al., 2017). However, field experiments are often costly and may introduce uncertainties 69 due to the considerable distance between mooring sites. Since the launch of the SEASAT in 70 1978, satellite remote sensing has been proven to be a powerful tool in investigating ISWs 71 (Alpers et al., 1985; Da Silva et al., 1998; Jackson et al., 2007). With the advantage of large 72 73 spatial coverage and high temporal resolution, satellite images are widely used for estimating wave speed. In the early days, the wave speed was roughly calculated with a single satellite 74 image containing two wave packets separated by one tidal period (Porter and Thompson, 1999; 75 Li et al., 2000; Liu et al., 2004). Later, the emergence of multi-source and multi-type satellites 76 provides conditions for using tandem satellite images to calculate the wave speed (Liu et al., 77 2014). 78

79 Based on satellite observations and field measurements, many studies show that wave speed is primarily dependent on water depth (Jackson et al., 2009; Liu et al., 2014; Lindsey et al., 80 2018; Liu et al., 2019; Tensuban et al., 2021) and has seasonal variations mainly controlled by 81 ocean stratification (Gises et al., 1998; Liu et al., 2014; Cho et al., 2016; Liu et al., 2019). 82 However, in this study, we found that the wave speed in the SS is also strongly modulated by 83 tidal currents, seasonal circulations, and ENSO. Thus, the wave speed in the SS exhibits a multi-84 scale temporal variation, from daily through monthly to interannual variation due to the 85 abovementioned environmental factors. 86

Here, we show such a multi-scale variation of wave speed by in the SS by collecting 1354 groups of wave speeds using tandem satellite images with temporal intervals typically shorter than 20 minutes. The details of the data and method are described in Section 2. Section 3 presents the spatial and multi-scale temporal variations of the wave speeds. Discussion and conclusions are in Section 4.

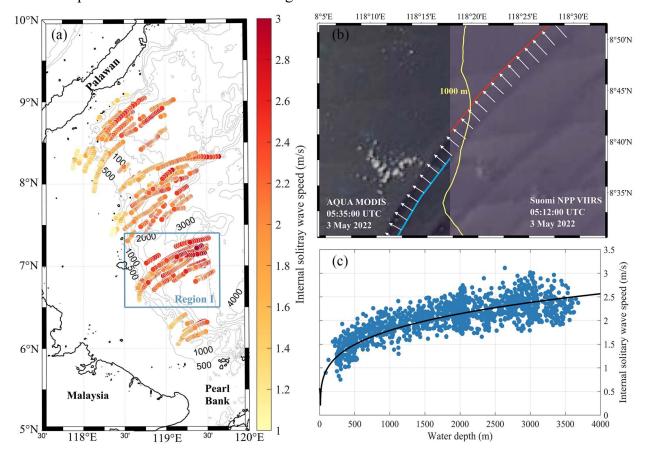
92 **2 Data and Methods**

93 2.1 Satellite images

This study uses satellite images taken by Moderate Resolution Imaging 94 Spectroradiometer (MODIS) onboard Aqua and Visible Infrared Imaging Radiometer Suite 95 (VIIRS) onboard Suomi National Polar-orbiting Partnership (NPP) satellites. The former has a 96 swath of 2330 km and the latter has an even wider swath of 3060 km. The MODIS and VIIRS 97 data have a spatial resolution of 250 m and 375 m, respectively. Large swath coverage and 98 99 moderate spatial resolution of the two sensors are particularly effective in tracking ISWs with spatial scales of thousands of meters in the SS. Combining the two sensors additionally yields 100 short temporal intervals of observations for accurate estimation of wave speeds. Finally, we 101 102 collected 41 image pairs acquired by NPP/VIIRS and AQUA/MODIS (called NPP-AQUA pair hereafter) from 2015 to 2022 with temporal intervals ranging from 5 to 19 minutes. 103

104 2.2 ISW speeds estimated from tandem satellite images

The MODIS and VIIRS data are projected into GCS_WGS_1984 geographic coordinate system. We draw a line normal (white arrows in Figure 1b) to the two dark strips of the same ISW observed by two satellites (red and blue lines) and then measured the length of the normal line. The wave speed was calculated by dividing the spatial displacement of the ISW by the temporal interval of the two satellite images. In total, 1354 groups of wave speeds were obtained, and their spatial distribution is shown in Figure 1a.





119

Figure 1. (a) The spatial variation of the wave speeds in the Sulu Sea. Each dot represents a displacement of ISW and its color means the magnitude of wave speed. The gray line is the isobath and the black line is the coastline. The blue solid rectangles show the study region for Section 3.2. (b) presents an NPP-AQUA pair of images acquired on 3 May 2022. The red and blue lines are the wave crests in the MODIS and VIIRS images, respectively. White arrows represent the displacements of the ISW.The yellow line represents 1000 m isobath. (c) shows the variation of wave speed with water depth. The black line represents the fitting curve.

2.3 Linear phase speeds derived from the Sturm-Liouville equation

The phase speed of a linear internal wave can be determined by solving the Sturm-Liouville (S-L) equation (Gill, 1982)

$$\frac{d}{dz}\left[(U_B(z) - c_0)^2 \frac{d\varphi}{dz}\right] + N^2 \varphi = 0 \tag{1}$$

subject to the boundary conditions:

$$\varphi(0) = \varphi(-H) = 0 \tag{2}$$

where φ and c_0 represent the vertical structure and linear phase speed, respectively. $U_B(z)$ is the 123 background current velocity. N^2 is the squared buoyancy frequency relating to the stratification. 124 *H* is water depth. Information about bathymetry, ocean stratification, and background currents 125 are all needed to solve equation (1). We obtained the local bathymetry in 15 arc-second interval 126 grids from GEBCO 2022 datasets (GEBCO Compilation Group, 2022). The Hybrid Coordinate 127 Ocean Model (HYCOM) run at 1/12° resolution provides information about ocean stratification 128 and background current (Chassignet et al., 2007). Argo profiling data in 2007, 2008, 2009, and 129 2015 to 2019 are used to obtain actual ocean stratification data (see details in S1). 130

131 In a two-layer ocean model, c_0 can be calculated by

$$c_0 = \sqrt{\frac{g\sigma h_1 h_2}{h_1 + h_2}} \tag{3}$$

where h_1 and h_2 are the upper and lower depths, respectively. *g* is the gravitational acceleration, $\sigma = 2(\rho_2 - \rho_1)/(\rho_2 + \rho_1)$ is the relative layer density difference, and $\rho_1(\rho_2)$ is the density of the upper (lower) layer.

135 ISWs are nonlinear waves, and thus their wave speed c is not equal to the linear phase speed 136 c_0 . According to the Korteweg-de Vries (KdV) theory, the two speeds are related by the 137 following equation:

$$c = c_0 + \frac{\alpha \eta_0}{3} \tag{4}$$

138 where η_0 is the wave amplitude and α is the nonlinear coefficient. Equation 4 predicts that wave 139 speed consistently exceeds linear phase speed because the productive of α and η_0 is positive.

140 **3 Spatiotemporal characteristics of ISW speed**

141 3.1 Spatial variation

As shown in Figure 1a, the wave speeds roughly increase from the shallow Pearl Bank 142 (5.87°N, 119.8°E), peak at the place near 7°N (the marked Region I), and then gradually decrease 143 towards Palawan Island. For a single ISW, its speed decreases from east to west, corresponding 144 to a decreasing water depth. For example, in Figure 1b, the ISW acquired on 3 May 2022 has a 145 higher average speed (2.32 m/s) on the east side of the 1000 m isobath than on its west side (1.71 146 m/s). Thus, the bathymetry in the SS has a significant impact on the spatial variation of wave 147 speeds. We derived the relationship between the wave speeds (c) and water depth (H), as 148 presented by the fitting curve (black line) in Figure 1c. The fitting formula is: 149

$$c = 0.421 \times (0.274 \times H + 0.647)^{0.261}$$
⁽⁵⁾

The formula suggests that the wave speeds increase exponentially with water depth with a power of 0.26, indicating that the water depth significantly modulates the wave speeds. Thus, this strong bathemetry effect may interfere with our study of the impacts of tidal currents, ocean stratification, and background currents on wave speeds. To reduce this interference, here, we define $H_0 = 500$ m as the threshold (see details in S2), beyond which the the effect of bathymetry can be neglected.

In addition, Figure 1c demonstrates that wave speeds vary considerably for the same water depth, suggesting the temporal variations and manual error in estimating wave speeds from satellite images. Statistically, based on a large amount of data, the manual error will not influence the following analysis about the temporal variations of wave speeds.

160 3.2 Daily variation

According to equation 4, tidal currents may influence the wave speed by changing the wave amplitude η_0 (Apel et al., 1985). To explore the effect of tidal currents, we delineated Region I (see details in S3) as the study area where wave speeds from 16 ISWs were extracted. We compared these wave speeds and their linear counterparts with the maximum ebb tidal current speeds corresponding to the wave generation. The dark-red dots in Figure 2a are the satellite-derived wave speeds, which reveals that they increase by 31% when the maximum ebb current speeds increase from 50 cm/s to 91 cm/s. The fitting function is:

$$c = 8.85 \times 10^{-5} \times U_{wavemax}^{2} + 2.055 \tag{6}$$

where $U_{wavemax}$ represents the maximum ebb tidal current speed predicted by the barotropic tidal models. Here we use the regional TPXO tidal solutions in the Indian Ocean (Egbert and Erofeeva, 2002). The estimation of $U_{wavemax}$ is described in the S4. It is the first time to show how the tidal currents quantitively affect the wave speeds (Equation 6).

The strong tidal current creates ISWs with large amplitude (Wang et al., 2011); the larger the amplitude, the greater the nonlinear part of the wave speeds ($\alpha\eta_0/3$ in equation 4). However, the linear phase speed (the dark-blue dots in Figure 2a) is independent of wave amplitude and varies with ocean stratification and background currents. The speeds used here are all acquired in April, May and June (called AMJ month hereafter, seeing details in S3). Thus, ocean stratification and background currents (dominated by monsoon) have small change, and so do the linear phase speeds.

Figure 2b presents the $U_{wavemax}$ and the corresponding wave speeds estimated from equation 6 in a typical spring/neap tidal cycle, showing synchronized changes in the $U_{wavemax}$ and wave speeds on a daily scale. The wave speeds increase by 30% from the neap to spring tide period, indicating that tidal currents significantly impact the daily variation of the wave speeds.

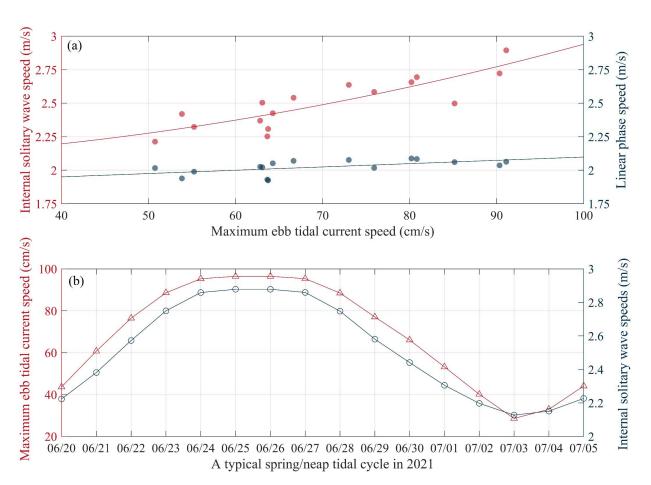
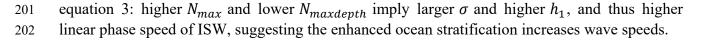


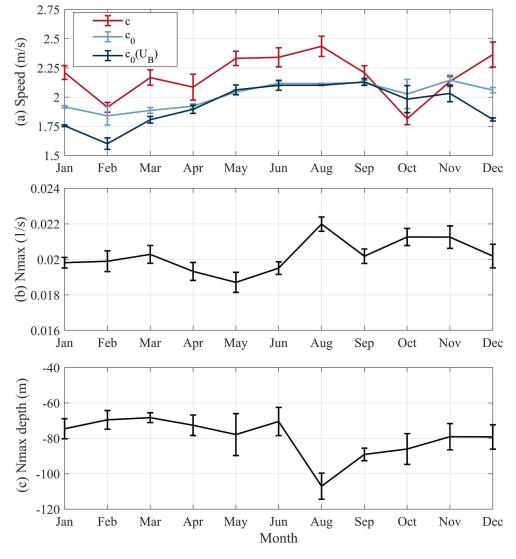
Figure 2. (a) The relationship between the satellite-derived speeds (red dots) and their linear phase speeds (dark-blue dots) with the maximum ebb tidal current speeds. The lines with different colors represent the fitting curve for the corresponding scatterd dots. (b) The maximum ebb tidal currents (red triangles) and the corresponding wave speeds (dark-blue circles)in a typical spring/neap tidal cycle from 20 June 2021 to 5 July 2021.

188 3.3 Monthly variation

In this section, 1231 groups of wave speeds (see details in S3) were used to study their monthly variation (*c* in Figure 3a). The wave speed decreases from January to February, and then fluctuates up until August. After that, it rapidly drops to the lowest value in October and then maintains its upward trend until December.

Ocean stratification is a recognized factor that impacts the monthly wave speed variation. 193 To analyze the effects of stratification on wave speeds, we collected profiling data from all Argo 194 floats in the SS to derive monthly averages of the maximum value of buoyancy frequency 195 (N_{max}) and the depth at N_{max} $(N_{maxdepth})$, which are shown in Figure 3b and 3c, respectively. 196 It is worth noting that the ISWs were not detected in tandem satellite images in July during 2015 197 to 2022, therefore, the N_{max} and $N_{maxdepth}$ in July are also excluded in comparsion. From 198 Figure 3a to 3c, we found that N_{max} ($N_{maxdepth}$) reaches its highest (lowest) in August, while 199 the corresponding wave speed is also the largest in August. This result can be explained by 200





203

Figure 3. (a) The monthly variations of satellite-derived wave speeds (c), HYCOM-derived linear phase speeds without (c_0) and with $(c_0(U_B))$ background currents. (b) and (c) presents the monthly variation of N_{max} and $N_{maxdepth}$ estimated from Argo profiling data, respectively. The vertical bars represent ranges of one standard deviation.

208

Previous studies show a basin-scale anticyclonic/cyclonic circulation in the upper layer of SS caused by the summer/winter monsoon (Cai et al., 2009; Han et al., 2009). This unique feature may also play a role in modulating the monthly variation of wave speeds. Here, we used the HYCOM datasets to estimate the corresponding linear phase speeds of the satellite-derived wave speeds (c) through equation 1 without (c_0) and with ($c_0(U_B)$) background currents ($U_B(z)$ in equation 1). The monthly variations of c, c_0 , and $c_0(U_B)$ in Figure 3a show that the background currents do modulate the wave speeds, especially from October to March with differences up to 0.27 m/s between c_0 and $c_0(U_B)$, indicating that the background currents impact the monthly variation of the wave speeds.

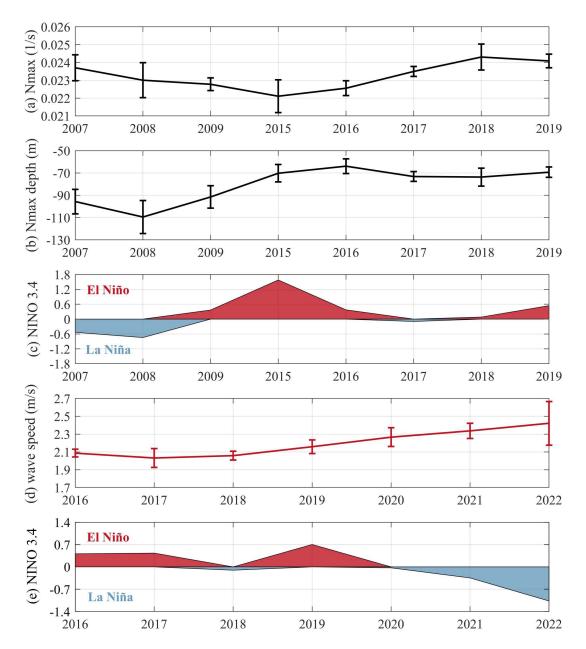
There are some other interesting findings in Figure 3a. In October and November, the c_0 are higher than *c*, contrary to the KdV theory (equation 4). After superimposing the background currents, the result in November is consistent with the KdV theory, but the result in October still challenges it. The reason for this condradiction may be a flaw in the KdV theory or the uncertainty of the model-derived stratification for calculating phase speeds.

223 3.4 Interannual variation

On interannual scales, the ENSO affects the stratification of the SS by changing 224 precipitations and sea surface temperature. Generally, the stratification is strengthened in La 225 Niña years and weakened in El Niño years (DeCarlo et al., 2015; Emberson et al., 2021). The 226 occurrence of La Niña and El Niño years can be diagnosed by the NINO3.4 index of ENSO 227 (Trenberth and Stepaniak, 2001). To investigate the effect of ENSO on wave speed, we collected 228 all available Argo profiling data in the SS for estimating the N_{max} and $N_{maxdepth}$. Figure 4a, 4b 229 and 4c show the interannual variations of N_{max} , $N_{maxdepth}$, and the NINO3.4 index, respectively. 230 The N_{max} increases and the $N_{maxdepth}$ decreases with the decrease of the NINO3.4 index. 2015 231 was a strong El Niño year, in which the N_{max} reaches its lowest value among the eight years and 232 $N_{maxdepth}$ also becomes shallow. The Pearson correlation coefficients are -0.46 (the NINO3.4 233 index and N_{max}) and 0.68 (the NINO3.4 index and $N_{maxdepth}$), suggesting that stratification was 234 enhanced with the decrease of the NINO3.4 index. Besides, according to Section 3.3, greater 235 N_{max} and smaller $N_{maxdepth}$ imply greater c_0 , indicating that there is a negative correlation 236 between wave speed and NINO3.4 index. 237

We collected 759 wave speeds from 46 ISWs to examine our analysis of the impact of ENSO on wave speeds (see details in S3). The comparison between wave speed and the NINO3.4 index from 2016 and 2022 (no ISW was detected in tandem satellite images in the AMJ month of 2015) is made with the following cautions: the NINO3.4 index used here is the average of AMJ month for each year to ensure the consistency of data during comparison since the wave speeds are only collected in the AMJ month.

The interannual variations of wave speeds (Figure 4d) and the NINO3.4 index (Figure 4e) are presented. Their Pearson correlation coefficient is -0.79, suggesting that there is a strong year-to-year inverse correlation between wave speed and the NINO3.4 index. In specific, the wave speed increases in La Niña years and decreases in El Niño years, in agreement with our theoretical analysis based on the Argo data.



249

Figure 4. The interannual variations: the annual averages of the N_{max} (a) and the $N_{maxdepth}$ (b) from Argo profiling data in the Sulu Sea and the NINO3.4 index (c) in 2007, 2008, 2009, 2015, 2016, 2017, 2018, and 2019; the averages of wave speeds (d) and the NINO3.4 index (e) in AMJ month from 2016 to 2022. The vertical bars represent ranges of one standard deviation.

4 Summary and Discussion

In this study, we collected 1354 groups of wave speeds in the SS from tandem satellite images with temporal intervals below 20 minutes. Based on these data, we analyzed their spatiotemporal variations and identified the potential contributing factors. The full picture of the spatial variation of wave speeds has been provided, and the multi-scale temporal variations from daily through monthly to interannual variations have also been demonstrated. Tidal current plays a significant role in modulating the daily changes of wave speeds by dominating the wave's amplitude, while the combined effect of ocean stratification and background circulations modifies the monthly variation of wave speeds. The interannual variation of wave speeds contributed by ENSO is also found. We found that the Pearson correlation coefficient between wave speeds and the NINO3.4 index of ENSO is -0.79. The high negative correlation suggests that ISWs have a speedup in La Niña years and a slowdown in El Niño years.

We present a statistical formula for the close relationship between the wave speed and the maximum ebb tidal current speed, which has never been shown in previous studies due to the limited data volume (Apel et al., 1985; Zhao et al., 2006). The results support the study about the modulation of tidal currents on the amplitude of ISWs. However, how the tidal currents quantitatively modulate the wave amplitude needs further study.

According to the monthly averages of the wave speeds and their linear phase speeds, we 271 found that the latter is higher than the former in October (Figure 3a), contrary to the KdV theory. 272 Similar situations happened in previous studies (Liu et al., 2019; Tensubam et al., 2021) but were 273 274 attributed to the background current that was not considered when estimating the linear phase speeds. However, our results reveal that even though the background circulation has been 275 included, the result in October still cannot be explained by the KdV theory. Deficiencies of the 276 KdV theory or the uncertainty of the model-derived stratification for calculating phase speeds 277 may take this responsibility. In the future, further theoretical derivations, field measurements, 278 and numerical simulations should be carefully designed and performed to interpret this 279 interesting finding in October and improve the theoretical system for describing the 280 characteristics of the ISWs. 281

We present for the first time a clear effect of ENSO on the wave speeds, which does not 282 focus exclusively on the effect of ENSO on the occurrence frequency of ISWs, as in previous 283 studies (DeCarlo et al., 2015; Chonnaniyah et al., 2021), but is more concerned with their 284 dynamical processes. However, we have to point out that this study is restricted to a single 285 season (spring) due to data limitations. More research on interannual variation of wave speed in 286 different seasons are needed for verification in the future. Additionally, the same analysis can be 287 expanded to study the interannual variations of wave speed and its relationship with ENSO in 288 289 other hot spot regions, such as the SCS (Qu et al., 2004; Fang et al., 2006) and the Lombok Strait (Aiki et al., 2011), where there are strong ISWs and significant impacts from ENSO. 290

291 Acknowledgements

This research was supported by the National Science Fund for Distinguished Young Scholars (42025605) and National Natural Science Foundation of China (42006193).

294 Data Availability Statement

The AQUA MODIS images and Suomi NPP VIIRS images were downloaded from NASA (https://worldview.earthdata.nasa.gov/). HYCOM data were accessed from the Center for Ocean-Atmospheric Prediction Studies (https://www.hycom.org/dataserver). GEBCO used here was obtained from the British Oceanographic Data Center (https://www.gebco.net/). Argo profiling data were downloaded from https://www.euro-argo.eu/. The NINO3.4 index was downloaded from the University Corporation for Atmospheric Research (https://www.cgd.ucar.edu/). The TPXO tide model is available at https://www.tpxo.net/regional.

302 **References**

- Aiki, H., Matthews, J. P., & Lamb, K. G. (2011). Modeling and energetics of tidally generated
 wave trains in the Lombok Strait: Impact of the Indonesian Throughflow. *Journal of Geophysical Research*, 116(C3). doi:10.1029/2010jc006589
- 306 Alford, M. H., Peacock, T., MacKinnon, J. A., Nash, J. D., Buijsman, M. C., Centurioni, L. R.,
- ... (David) & Tang, T.-Y. (2015). The formation and fate of internal waves in the South China
 Sea. *Nature*, 521(7550), 65–69. doi:10.1038/nature14399.
- Alpers, W. (1985). Theory of radar imaging of internal waves. *Nature*, 314, 245–247,
 doi:10.1038/314245a0
- 311 Apel, J. R., Holbrook, J. R., Liu, A. K., & Tsai, J. J. (1985). The Sulu Sea Internal Soliton
- 312 Experiment. Journal of Physical Oceanography, 15(12), 1625–1651, doi:10.1175/1520-

313 0485(1985)015<1625:tssise>2.0.co;25(1985)015<1613:niweit>2.0.co;2

- Apel, J. R. (2002). Oceanic internal waves and solitons. *An atlas of oceanic internal solitary waves*. Global Ocean Associates, 1-40.
- Apel, J. R., Ostrovsky, L. A., Stepanyants, Y. A., & Lynch, J. F. (2007). Internal solitons in the
- 317 ocean and their effect on underwater sound. *The Journal of the Acoustical Society of America*,
- 318 121(2), 675-722, doi: 10.1121/1.2395914.
- 319 Cai, S., He, Y., Wang, S., & Long, X. (2009). Seasonal upper circulation in the Sulu Sea from
- satellite altimetry data and a numerical model. Journal of Geophysical Research, 114(C3),
- doi:10.1029/2008jc005109
- 322 Chassignet, E. P., Hurlburt, H. E., Smedstad, O.M., Halliwell, G.R., Hogan, P.J., Wallcraft, A.J.,

- Baraille, R., Bleck, R. (2007). The HYCOM (hybrid coordinate ocean model) data assimilative system. *Journal of Marine Systems*, 65, 60–83, doi: 10.1016/j.jmarsys. 2005.09.016.
- 326 Cho, C., Nam, S. H., & Song, H. C. (2016). Seasonal variation of speed and width from

kinematic parameters of mode-1 nonlinear internal waves in the northern East China Sea.

Chonnaniyah, Osawa, T., Wayan Gede Astawa Karang, I., & As-syakur, A.R. (2021). Variability

- *Journal of Geophysical Research: Oceans*, 121(8), 5942-5958, doi:10.1002/2016JC012035

- of Internal Solitary Waves Detection in the Lombok Strait Observed by Sentinel-1 SAR: The
- Role of Monsoon, IOD, and ENSO. 2021 7th Asia-Pacific Conference on Synthetic Aperture
- 332 Radar (APSAR), 1-5.

327

329

- 333 Da Silva, J., Ermakov, S., Robinson, I., Jeans, D., Kijashko, S., (1998). Role of surface films in
- ERS SAR signatures of internal waves on the shelf: 1. Short-period internal waves. *Journal of*
- *Geophysical Research: Oceans*, 103, 8009–8031.
- Da Silva, J. C. B. (2002). On the observability of internal tidal waves in remotely-sensed ocean
 colour data. *Geophysical Research Letters*, 29(12). doi:10.1029/2001gl013888.
- 338 DeCarlo, T. M., Karnauskas, K. B., Davis, K. A., & Wong, G. T. F. (2015). Climate modulates
- internal wave activity in the Northern South China Sea. *Geophysical Research Letters*, 42(3),
- 340 831–838, doi:10.1002/2014gl062522
- Egbert, G. D., & Erofeeva, S.Y. (2002). Efficient inverse modeling of barotropic ocean tides.
- *Journal of Atmospheric and Oceanic technology*, 19, 183–204.
- 343 Emberson, R., Kirschbaum, D., & Stanley, T. (2021). Global connections between El Nino and
- landslide impacts. *Nature Communications*, 12(1), doi:10.1038/s41467-021-22398-4

- 345 Fang, W. D., Guo, J. J., Shi, P., & Mao, Q. W. (2006). Low frequency variability of South China
- Sea surface circulation from 11 years of satellite altimeter data. *Geophysical Research Letters*,
 33(22), doi: 10.1029/2006GL027431.
- Garrett, C. (2003). Internal tides and ocean mixing. *Science*, 301(5641), 1858-1859,
 doi:10.1126/science.1090002
- 350 GEBCO Compilation Group. (2022). GEBCO_2022 Grid. doi:10.5285/e0f0bb80-ab44-2739 351 e053-6c86abc0289c.
- 352 Giese, G. S., Chapman, D. C., Collins, M. G., Encarnacion, R., & Jacinto, G. (1998). The
- 353 Coupling between Harbor Seiches at Palawan Island and Sulu Sea Internal Solitons. *Journal of*
- 354 Physical Oceanography, 28(12), 2418–2426. doi:10.1175/1520 355 0485(1998)028<2418:tcbhsa>2.0.co;2
- Gill, A. E. (1982). International Geophysics. *Atmosphere-Ocean Dynamics*. Amsterdam. The
 Netherlands: Elsevier.
- Han, W. Q., Moore, A. M., Levin, J., Zhang, B., Arango, H. G., Curchitser, E., Lorenzo, E. D.,
- 359 Gordon, A. L., & Lin, J. L. (2009). Seasonal surface ocean circulation and dynamics in the
- 360 Philippine Archipelago region during 2004-2008. Dynamics of Atmospheres and Oceans,
- 361 47(1-3), 114-137, doi:10.1016/j.dynatmoce.2008.10.007
- Haury, L. R., Briscoe, M. G., & Orr, M. H. (1979). Tidally generated internal wave packets in
 Massachusetts Bay. *Nature*, 278(5702), 312–317. doi:10.1038/278312a0.
- 364 Huang, X. D., Zhang, Z. W., Zhang, X. J., Qian, H. B., Zhao, W., & Tian, J. W. (2017). Impacts
- 365 of a Mesoscale Eddy Pair on Internal Solitary Waves in the Northern South China Sea
- 366 revealed by Mooring Array Observations. Journal of Physical Oceanography, 47(7), 1539-
- 367 1554, doi: 0.1175/JPO-D-16-0111.1.

- 368 Jackson, C. R. (2004). An Atlas of internal solitary-like waves and their properties, 2nd ed.,
- 369 Global Ocean Associates, Washington, D. C. [Available at
 370 http://www.internalwaveatlas.com/Atlas2index.html]
- Jackson, C., (2007). Internal wave detection using the moderate resolution imaging
 spectroradiometer (MODIS). *Journal of Geophysical Research: Oceans*, 112.
- Jackson, C. R. (2009). An empirical model for estimating the geographic location of nonlinear
- internal solitary waves. *Journal of Atmospheric and Oceanic Technology*, 26(10), 2243-2255,
- 375 doi:10.1175/2009JTECHO638.1
- Jackson, C., Arvelyna, Y., & Asanuma, I. (2011). High-Frequency Nonlinear Internal Waves
 Around the Philippines. *Oceanography*, 24(01), 90–99. doi:10.5670/oceanog.2011.06.
- 378 Klein, S. A., Soden, B. J., Lau, N. C. (1999). Remote Sea Surface Temperature Variations during
- ENSO: Evidence for a Tropical Atmospheric Bridge. *Journal of Climate*, 12(4), 917–932.
 doi:10.1175/1520-0442(1999)012<0917:rsstvd>2.0.co;2.
- Li, X. P., Clemente-Colon, P., & Friedman, K. (2000). Estimating oceanic mixed layer depth from internal wave evolution observed from RADARSAT-1 SAR. *Johns Hopkins Apl Technical Digest*, 21(1), 130-135.
- 384 Lien, R. C., D'Asaro, E. A., Henyey, F. S., Chang, M. H., Tang, T. Y., & Yang, Y. J. (2012).
- Trapped core formation within a shoaling nonlinear internal wave. *Journal of Physical Oceanography*, 42, 511-525, doi: 10.1175/2011JPO4578.1.
- Lindsey, D. T., Nam, S. H., & Miller, S. D. (2018). Tracking oceanic nonlinear internal waves in
- the Indonesian seas from geostationary orbit. Remote Sensing of Environment, 208, 202-209,
- doi: 10.1016/j.rse.2018.02.018.

- 390 Liu, A. K., Holbrook, J. R., & Apel, J. R. (1985). Nonlinear Internal Wave Evolution in the Sulu
- 391 Sea. Journal of Physical Oceanography, 15(12), 1613–1624, doi:10.1175/1520 392 0485(1985)015<1613:NIWEIT>2.0.CO;2
- Liu, A. K., Ramp, S. R., Zhao, Y., & Tang, T. Y. (2004). A case study of internal solitary wave
- propagation during ASIAEX 2001, *IEEE Journal of Oceanic Engineering*, 29(4), 1144-1156,
 doi:10.1109/JOE.2004.841392.
- Liu, B., Yang, H., Zhao, Z., & Li, X. (2014). Internal solitary wave propagation observed by
 tandem satellites. *Geophysical Research Letters*, 41(6), 2077–2085,
 doi:10.1002/2014gl059281.
- Liu, B., & D'Sa, E. J. (2019). Oceanic Internal Waves in the Sulu-Celebes Sea Under Sunglint
 and Moonglint. *IEEE Transactions on Geoscience and Remote Sensing*, 1–11,
 doi:10.1109/tgrs.2019.2904402.
- Lynch, J. F., Lin, Y. T, Duda, T. F., & Newhall, A. E. (2010). Acoustic ducting, reflection,
 refraction, and dispersion by curved nonlinear internal waves in shallow water. *IEEE Journal of Oceanic Engineering*, 35, 12-27.
- 405 MacKinnon, J. A., Zhao, Z., Whalen, C. B., Waterhouse, A. F., Trossman, D. S., Sun, O. M., ...
- 406 & Alford, M. H. (2017). Climate Process Team on Internal Wave–Driven Ocean Mixing.
- Bulletin of the American Meteorological Society, 98(11), 2429–2454, doi:10.1175/bams-d-160030.1.
- 409 Osborne, A., Burch, T., & Scarlet, R. (1978). The influence of internal waves on deep-water
- 410 drilling. Journal of Petroleum Technology, 30, 1497-1504, doi.org/10.2118/6913-PA.

- 411 Porter, D. J., & Thompson, D. R. (1999). Continental shelf parameters inferred from SAR
- 412 internal wave observations. *Journal of Atmospheric and Oceanic Technology*, 16(4), 475-487,

413 doi:10.1175/1520-0426(1999)016<0475:CSPIFS>2.0.CO;2.

- 414 Qu, T., Kim, Y. Y., Yaremchuk, M., Tozuka, T., Ishida, A., & Yamagata, T. (2004). Can Luzon
- 415 Strait Transport Play a Role in Conveying the Impact of ENSO to the South China Sea?
- 416
 Journal
 of
 Climate,
 17(18),
 3644–3657.
 doi:10.1175/1520

 417
 0442(2004)017<3644:clstpa>2.0.co;2
- 418 Ramp, S. R., Yang, Y. J. Yang, & Bahr, F. L. Bahr (2010). Characterizing the nonlinear internal
- 419 wave climate in the northeastern South China Sea. *Nonlinear Processes in Geophysics*, 17(5),
- 420 481–498, doi:10.5194/npg-17-481-2010.
- Tensubam, C. M., Raju, N. J., Dash, M. K., & Barskar, H. (2021). Estimation of internal solitary
 wave propagation speed in the Andaman Sea using multi–satellite images. *Remote Sensing of Environment*, 252, 112123, doi:10.1016/j.rse.2020.112123.
- Trenberth, K. E., & Stepaniak, D. P. (2001). Indices of El Nino Evolution, Journal of Climate,
- 425 14(8), 1697-1701, doi: 10.1175/1520-0442(2001)014<1697:LIOENO>2.0.CO;2.
- 426 Wang, Y. H., Dai, C. F., & Chen, Y. Y. (2007). Physical and ecological processes of internal
- 427 waves on an isolated reef ecosystem in the South China Sea, *Geophysical Research Letters*, 34,
- 428 L18609, doi:10.1029/2007GL030658.
- 429 Wang, C., & Pawlowicz, R. (2011). Propagation speeds of strongly nonlinear near-surface
- 430 internal waves in the Strait of Georgia, Journal of Geophysical Research, 116(C10), doi:
- 431 116(C10). doi:10.1029/2010jc006776.

- 432 Wang, T. X., Huang, X. D., Zhao, W., Zheng, S. H., Yang, Y.C., & Tian, J. W. (2022). Internal
- solitary wave activities near the Indonesian submarine wreck site inferred from satellite
 images, *Journal of Marine Science and Engineering*, 10(2), 197, doi: 10.3390/jmse10020197.
- 435 Zhang, X. D., & Li, X. F. (2022). Satellite data-driven and knowledge-informed machine
- learning model for estimating global internal solitary wave speed. *Remote Sensing of Environment*, 283, 113328, doi: 10.1016/j.rse.2022.113328.
- Zheng, X. H., & Klemas, V. (1993). Statistical and dynamical analysis of internal waves on the
 continental shelf of the middle Atlantic bight from space shuttle photographs, *Journal of Geophysical Research*, 98(C5), 8495-8504, doi: 10.1029/92jc02955.
- Zhao, Z. X., & Alford, M. H. (2006), Source and propagation of internal solitary waves in the
 northeastern South China Sea. *Journal of Geophysical Research: Oceans*, 111(11),
 doi:10.1029/2006JC003644.
- Zhou, J. X., Zhang, X. Z., & Rogers, P. H. (1991). Resonant interaction of sound wave with
- internal solitons in the coastal zone. *The Journal of the Acoustical Society of America*, 90(4),
- 446 doi: 10.1121/1.401632.