# One-Dimensional Variational Ionospheric Retrieval Using Radio Occultation Bending Angles: Part 1 -Theory

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#### Abstract

A new one-dimensional variational (1D-Var) retrieval method for ionospheric GNSS ra- dio occultation (GNSS-RO) measurements is described. The forward model implicit in the retrieval calculates the bending angles produced by a one-dimensional ionospheric electron density profile, modeled with multiple "Vary-Chap" layers. It is demonstrated that gradient based minimisation techniques can be applied to this retrieval problem. The use of ionospheric bending angles is discussed. This approach circumvents the need for Differential Code Bias (DCB) estimates when using the measurements. This new, general retrieval method is applicable to both standard GNSS-RO retrieval problems, and the truncated geometry of EUMETSAT's Metop Second Generation (Metop-SG), which will provide GNSS-RO measurements up to about 600 km above the surface. The climatological a priori information used in the 1D-Var is effectively a starting point for the 1D-Var minimisation, rather than a strong constraint on the final solution. In this paper the approach has been tested with 143 COSMIC-1 measurements. We find that the method converges in 135 of the cases, but around 25 of those have high "cost at convergence" values. In the companion paper (Elvidge et al., 2023), a full statistical analysis of the method, using over 10,000 COSMIC-2 measurements, has been made.

## **One-Dimensional Variational Ionospheric Retrieval** Using Radio Occultation Bending Angles: Part 1 -Theory

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#### Key Points:

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9	•	A new method of deriving ionospheric electron densities, using the difference be-
10		tween bending angles at two different frequencies.
11	•	It is based on a 1D variational retrieval, the solution of which is the best fit to the
12		a priori background and the observations.
13	•	The forward model assumes the ionosphere to consist of several idealised 'Vary-
14		Chap' electron density layers.

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In this paper the approach has been tested with 143 COSMIC-1 measurements. We find that the method converges in 135 of the cases, but around 25 of those have high "cost at convergence" values. In the companion paper (Elvidge et al., 2023), a full statistical analysis of the method, using over 10,000 COSMIC-2 measurements, has been made.

#### <sup>32</sup> Plain Language Summary

This paper presents a new way of estimating the density of electrons in the iono-33 sphere — the part of the Earth's atmosphere in which atoms are ionised by radiation 34 from the Sun. Radio signals sent between GNSS navigational satellites and receivers in 35 a low orbit around the Earth are delayed, and their paths are bent, by the presence of 36 electrons in the ionosphere. Previous attempts to use these observations to estimate the 37 electron density have been based on the delay of the signals. The new approach outlined 38 in this paper uses the bending incurred by the radio waves instead. Such "bending an-39 gles" have been used to infer some properties of the lower atmosphere for many years, 40 and are widely available. We demonstrate that by extending these measurements to greater 41 heights, they can provide useful information about the ionosphere as well. 42

#### 43 1 Introduction

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<sup>44</sup> The radio occultation instrument on EUMETSAT's Metop Second Generation (Metop-<sup>45</sup> SG) satellites will measure up to 600 km above the Earth's surface, and provide mea-<sup>46</sup> surements for space weather applications. The retrieval of ionospheric profile informa-<sup>47</sup> tion from GNSS radio occultation (GNSS-RO) is well established (e.g., Hajj and Romans <sup>48</sup> (1998); Schreiner et al. (1999)), using the Abel transform, which, for a circularly sym-<sup>49</sup> metric electron densities  $N_e$  and (therefore) refractive indices n, and bending angles  $\alpha$ <sup>50</sup> that are available at all impact parameters a, is given by

$$n(x) = \exp\left\{\frac{1}{\pi} \int_{x}^{\infty} \frac{\alpha(a)}{\sqrt{a^2 - x^2}} \, da\right\}.$$
(1)

However, the 600 km upper limit for the Metop-SG observations complicates the application of the Abel transform, and alternative ionospheric retrieval techniques are needed
for this particular truncated geometry. Lyu et al. (2019) have presented two new approaches
to this problem, but the more accurate approach, AVHIRO, is currently too slow for possible operational applications. They also suggest that gradient based minimisation techniques are difficult to apply to this retrieval problem because of non-linearity.

In this work, we present a new method based on a variational (or "optimal estimation") approach (Rodgers, 2000). The one dimensional variational (1D-Var) retrieval approach is used extensively in neutral atmosphere GNSS-RO applications (e.g., Healy and Eyre (2000); Palmer et al. (2000)). Variational retrieval is more flexible than the Abel transform inversion, as it does not rely on an idealised measurement geometry. Specifically, the truncated Metop-SG geometry can be accounted for in a straightforward manner as part of the forward problem,  $\mathbf{y} = \mathcal{H}(\mathbf{x})$ , which maps the electron density profile information,  $\mathbf{x}$ , to an observation  $\mathbf{y}$  — bending angles here. This is in contrast to most GNSS-RO ionospheric retrievals, which, with the exception of Hajj and Romans (1998), are based on slant total electron contents (STECs), S. This is defined as the electron

density  $N_e$  integrated along the path P between the GNSS and LEO satellites, thus:

$$S = \int_{P} N_e(s) ds. \tag{2}$$

However, STEC values derived from GNSS phase measurements are *relative* quantities. This is because there is an ambiguity in the total number of wave cycles along the path between the two satellites (e.g., Dyrud et al. (2008)).

These STEC values can be "leveled" using the pseudo-range measurements for the same path, but this processing step introduces a differential code bias (DCB), which also requires estimation. Here we show how bending angles are related to the derivative of STEC,  $\partial S/\partial a$ , where *a* is the impact parameter of the ray path. Taking the derivative removes the sensitivity to any constant offsets (the DCBs) and simplifies the problem.

We note that bending angles are assimilated in most global numerical weather prediction (NWP) data assimilation systems without bias correction, and they are considered "anchor measurements" because they constrain the bias corrections applied to other measurements (e.g., Poli et al. (2010)). However, in the ionospheric data assimilation literature, radio occultation STECs with bias corrections (DCBs) are still usually assimilated, e.g. Angling and Cannon (2004); Yue et al. (2011); Angling et al. (2021).

The purpose of this paper is to describe the theoretical basis of the new ionospheric 1D-Var retrieval approach. This includes a description of the multiple Vary-Chap layer electron density profile, the relationship between the derivative of the slant TEC and bending angle, and the 1D-Var assimilation system. A companion paper, Elvidge et al. (2023), presents a full statistical validation of the method.

#### <sup>89</sup> 2 Data assimilation preliminaries

In a variational retrieval system the estimate of the state vector is obtained using the observations combined with *a priori* information. Since the observations, and *a priori* information, are only known up to certain levels of confidence these are usually described using probability density functions (PDFs). By assuming Gaussian PDFs, and that the observation and background errors are uncorrelated, Bayes' theorem can be used to show that this problem can be framed as the minimization of a cost function J (e.g. Talagrand (2010)):

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$$J(\mathbf{x}) = \frac{1}{2} (\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}_b) + \frac{1}{2} (\mathbf{y}_o - \mathcal{H}(\mathbf{x}))^T \mathbf{R}^{-1} (\mathbf{y}_o - \mathcal{H}(\mathbf{x})).$$
(3)

Here,  $\mathbf{x}_b$  is the background state (specifically, the parameters that define the vertical electron density profile), **B** is the background error covariance matrix,  $\mathbf{y}_o$  is the set of observations (specifically, bending angles as a function of impact parameter), **R** is the observation error covariance matrix, and  $\mathcal{H}$  is the forward operator, which generates pseudo observations from a particular state.

The retrieval solution,  $\mathbf{x}_a$ , is the state which minimises the cost function, and it should be consistent with both the background  $\mathbf{x}_b$  and the observations  $\mathbf{y}_o$ , to within their expected error statistics. The bending angle profile provides useful information about all the ionospheric variables in the state vector  $\mathbf{x}$ , and the uncertainty in the estimate of  $\mathbf{x}$  is significantly reduced as a result of making the measurement. In this context, a

useful feature of a 1D-Var retrieval is that it provides the following estimate of the the-108 oretical solution error covariance matrix,  $\mathbf{A}$  in terms of  $\mathbf{B}$  and  $\mathbf{R}$ 109

$$\mathbf{A} = (\mathbf{B}^{-1} + \mathbf{H}^{\mathrm{T}} \mathbf{R}^{-1} \mathbf{H})^{-1}$$
(4)

where  $\mathbf{H}$  is the matrix of partial derivatives of the forward model with respect to the state 111 vector elements:  $\mathbf{H} = \partial \mathcal{H} / \partial \mathbf{x}$ . In well-posed problems the diagonal elements of the A 112 matrix are significantly smaller than the corresponding diagonal elements of the  $\mathbf{B}$  ma-113 trix  $(A_{i,i} \ll B_{i,i})$ . 114

The 1D-Var approach should be more robust to measurement noise than the Abel 115 transform because it is a weighted least-squares approach; it will not over-fit the mea-116 surements if the assumed observation error statistics,  $\mathbf{R}$ , are a reasonable approxima-117 tion of the actual observation error statistics. The retrieval also produces useful diag-118 nostics of the quality of the solution. These include the number of iterations required 119 to converge, and the cost at convergence,  $J(\mathbf{x}_a)$ , the expectation value of which is half 120 the size of the observation vector,  $E[2J(\mathbf{x}_a)] = m \pm \sqrt{2m}$  (e.g., Rodgers (2000)), if the 121 assumed error statistics are well specified. 122

Practical details of the solution method are discussed in Section 5.

#### 3 Theory and observations 124

#### 3.1 Theory 125

To overcome the need for estimation of the Differential Code Biases (DCBs) in this 126 work the derivative of slantwise TEC S, with respect to the impact parameter  $a, \partial S/\partial a$ , 127 is assimilated. The latter is the quantity used in the Abel transform solution for refrac-128 tivity (see Eqn 14 in Schreiner et al. (1999)), and we will show that, to a good approx-129 imation, it is proportional to the difference between the L2 and L1 bending angles, plus 130 a term that involves the electron density at the LEO. 131

The STEC is the integrated electron density  $(N_e)$  along the path P between the 132 GNSS and the LEO satellites (see Eqn (2)). To a first approximation the delay  $\phi_i$  (in 133 m) in the phase of the carrier wave (of frequency  $f_i$ ), relative to the vacuum, accumu-134 lated along the path P is given by 135

$$\phi_i = \int_{\Sigma} ($$

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 $= \int_{P} (n_i - 1) ds$  $= \int_{P} -\kappa N_e / f_i^2 ds$  $= -\kappa S / f_i^2$ (5)

where  $n_i$  is the refractive index at frequency  $f_i$ , which is approximately given by (e.g. 139 Schreiner et al. (1999)) 140

$$n_i - 1 \approx -\kappa N_e / f_i^2, \tag{6}$$

in which the proportionality constant  $\kappa \approx 40.3 \text{ m}^3 \text{s}^{-2}$ . 142

If the electron density is assumed to be only a function of height (i.e. is spherically 143 symmetric), the STEC S between a GNSS satellite at radius  $r_G$  and a LEO satellite at 144 radius  $r_L$  is easily shown, from Eqn (2) to be given approximately by 145

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$$S = \int_{a}^{r_{L}} \frac{rN_{e}(r)}{\sqrt{r^{2} - a^{2}}} dr + \int_{a}^{r_{G}} \frac{rN_{e}(r)}{\sqrt{r^{2} - a^{2}}} dr$$
147
$$= \left[\int_{a}^{r_{L}} + \int_{a}^{r_{G}}\right] \frac{rN_{e}(r)}{\sqrt{r^{2} - a^{2}}} dr$$
(7)

in which  $N_e(r)$  is the electron density at radius r, and the impact parameter a is nearly 148 equal to the radial distance to the tangent point,  $r_T$ . (For example, even for a high elec-149 tron density of  $3 \times 10^{12}$  m<sup>-3</sup> at a height of 300 km, which is appropriate for the F2 peak 150

in daytime, solar maximum conditions,  $n_i - 1 \approx -8 \times 10^{-5}$  at the L2 frequency of about 151 1.2 GHz. This means that a and  $r_T$  differ by less than 600 m.) 152

Assuming the electron density is zero at the GNSS, integrating Eqn (7) by parts 153 gives 154 ral

$$S = N_e(r_L)\sqrt{r_L^2 - a^2} - \left[\int_a^{r_L} + \int_a^{r_G}\right]\sqrt{r^2 - a^2}\frac{dN_e(r)}{dr}\,dr \tag{8}$$

The derivative of Eqn (8) with respect to a is: 156

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$$\frac{\partial S}{\partial a} = -\frac{N_e(r_L)a}{\sqrt{r_L^2 - a^2}} + a \left[ \int_a^{r_L} + \int_a^{r_G} \right] \frac{dN_e(r)/dr}{\sqrt{r^2 - a^2}} \, dr. \tag{9}$$

Eqn (9) is singular at  $a = r_L$ , as noted in Lei et al. (2007). This singularity is nec-158 essary for the Abel inversion using slantwise TECs to be well-behaved. 159

Note that the integrals in Eqn (9) are closely proportional to the standard Abel 160 transform approximation to the ionospheric bending angle at impact parameter a and 161 frequency  $f_i$ ,  $\alpha_i(a)$ , namely (Vorob'ev & Krasil'nikova, 1994; Kursinski et al., 1997; An-162 gling et al., 2018): 163

164 
$$\alpha_{i}(a) = -2a \int_{r_{T}}^{\infty} \frac{dn_{i}(r)/dr}{n_{i}\sqrt{(n_{i}r)^{2}-a^{2}}} dr$$
165 
$$\simeq \frac{\kappa a}{f_{i}^{2}} \left[ \int_{a}^{r_{L}} + \int_{a}^{r_{G}} \right] \frac{dN_{e}(r)/dr}{\sqrt{r^{2}-a^{2}}} dr, \qquad (10)$$

using  $\log n_i \approx n_i - 1 = -\kappa N_e / f_i^2$ , as in Eqn (6),  $n_i \approx 1$  (and therefore  $r_T \approx a$ ) where 166 appropriate, and replacing the infinite upper limits of the integrals by distances to the 167 satellites. 168

The vertical gradient of the phase delay in Eqn (5) is  $\partial \phi_i / \partial a = -(\kappa / f_i^2) \partial S / \partial a$ . 169 Therefore, given measurements at two frequencies,  $f_1$  and  $f_2$ , and assuming straight line 170 paths with the same impact parameter, a, we can use Eqn (9) to write the difference in 171 the phase delay gradients as: 172

$$\frac{\partial(\phi_1 - \phi_2)}{\partial a} = -\kappa \left(\frac{1}{f_1^2} - \frac{1}{f_2^2}\right) \frac{\partial S}{\partial a}$$

$$= \kappa \left(\frac{f_1^2 - f_2^2}{f_1^2 f_2^2}\right) \left(a \left[\int_a^{r_L} + \int_a^{r_G}\right] \frac{dN_e(r)}{\sqrt{r^2 - a^2}} dr - \frac{N_e(r_L)a}{\sqrt{r_L^2 - a^2}}\right). (11)$$

There is a fortuitous cancellation of errors relevant to this problem. In the processing 175 of real measurements, bending angle values are derived from the Doppler shift values as-176 suming that the refractive index at the LEO satellite is unity:  $n(r_L) = 1$ . For circu-177 lar orbits this assumption does not affect the impact parameter, a, but it introduces a 178 frequency dependent negative bias,  $b_i$ , in the observed bending angles<sup>1</sup>. This is equal to 179 (see Eqn A6 of Schreiner et al. (1999)): 180

$$b_i = -\frac{\kappa}{f_i^2} \frac{N_e(r_L)a}{\sqrt{r_L^2 - a^2}},$$
(12)

which, being inversely proportional to the square of the frequency, cancels out in the usual 182 dual frequency ionospheric correction of the bending angles (Vorob'ev & Krasil'nikova, 183 1994). The observed ionospheric bending angles,  $\tilde{\alpha}_i(a)$ , will therefore be related to the 184

 $<sup>^1</sup>$  The proportionality between Doppler shift and impact parameter for circular orbits is also exploited in the Full Spectral Inversion (FSI) technique (Jensen et al., 2003).

true bending angles,  $\alpha_i(a)$ , (see Eqn (10)), according to

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$$\tilde{\alpha}_i(a) = \alpha_i(a) + b_i(a)$$

$$= \frac{\kappa a}{f_i^2} \left[ \int_a^{r_L} + \int_a^{r_G} \right] \frac{dN_e(r)/dr}{\sqrt{r^2 - a^2}} \, dr - \frac{\kappa a}{f_i^2} \frac{N_e(r_L)}{\sqrt{r_L^2 - a^2}}.$$
 (13)

188 Comparison with Eqn (11) therefore reveals that

$$\frac{\partial(\phi_1 - \phi_2)}{\partial a} \simeq \tilde{\alpha}_2(a) - \tilde{\alpha}_1(a). \tag{14}$$

Therefore, the ionospheric retrieval can use either observed bending angle differences or the derivative of phase delay differences with respect to impact parameter.

#### 3.2 Observations

Accurate estimation of the uncertainty of the observations is crucial to ensure the observations are not over-fitted. In general it is difficult to estimate the uncertainty of observations, since in most cases there is no additional, independent, reference truth.

As well as errors in the observations themselves, there are also errors arising from 196 the use of a 1D-retrieval rather than a more realistic 3D-retrieval. Such errors obviously 197 depend on the electron density distribution, which varies with location, time of day and 198 solar conditions. To estimate these errors, electron density distributions appropriate to 199 145 Metop-SG occultations have been generated with 1D and 3D versions of the clima-200 tological ionosphere electron density model NeQuick (Nava et al., 2008), at four differ-201 ent solar activity levels, represented by the solar radio flux at 10.7 cm ( $F_{10.7}$ ). Specif-202 ically we use  $F_{10.7}$  values of 80, 130, 180, 230 solar flux units (sfu) (where 1 sfu =  $10^{-22}$ 203  $Wm^{-2}Hz^{-1}$ ). 204

For each altitude h the absolute mean electron density error  $\epsilon$  across all  $4 \times 145 =$ 580 simulated occultations is calculated thus:

$$\epsilon(h) = \frac{1}{580} \sum_{i=1}^{580} \left| N_i^{3D}(h) - N_i^{1D}(h) \right|$$
(15)

where  $N^{1D}(h)$  and  $N^{3D}(h)$  are the electron densities in the 1D- and 3D-NeQuick models at height h.  $(N_i^{3D}(h)$  is taken at the same longitude and latitude as  $N_i^{1D}(h)$ .) To ensure that "rare" geometries, such as occultations that cross the day/night terminator, do not distort the statistics, any outliers at each altitude are removed. Outliers are defined as any value which is less than 1.5 times the interquartile range (IQR) below the first quartile (Q1) of the data, or greater than 1.5 times the IQR above the third quartile (Q3), i.e. only data, d, in the range

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$$Q1 - 1.5IQR \le d \le Q3 + 1.5IQR \tag{16}$$

are kept at each altitude. The bending angle profile resulting from passing the 1D elec-216 tron density difference  $\epsilon(h)$  in Eqn (15) through the Abel transform (which is *linear* in 217  $N_e$ ) is shown in Figure 1. The blue vertical line at 2.10  $\mu$ rad shows the average mean ab-218 solute error, and shows that 2.0  $\mu$ rad is an excellent single value error to use. It is com-219 parable to the value used in neutral atmosphere applications in the middle/upper strato-220 sphere. For example, ECMWF uses 3.0  $\mu$ rad above about 32 km when assimilating GNSS-221 RO data. It is clear, however, that the error is height-dependent. Rather than directly 222 using the average errors from Figure 1, which are subject to sampling errors themselves, 223 the following Gaussian fit to the data is used in the 1D-Var retrieval: 224

bending angle error = 3.8 
$$\mu$$
rad × exp $\left[-\frac{1}{2}\left(\frac{h-270}{110}\right)^2\right]$  (17)

where h is the altitude in km. A minimum value of 1.0  $\mu$ rad is imposed. Eqn (17) is plotted in red in Figure 1. This function provides a similar residual sum of squares error as using a 5<sup>th</sup> order polynomial fit, but without the associated numerical instabilities.



Figure 1. Mean absolute difference in bending angles derived from electron density differences  $\epsilon(h)$  defined by Eqn (15). Vertical average in blue. Fitting function in Eqn (17) in red.

#### <sup>229</sup> 4 Electron density model

To reconstruct the ionosphere from the observations described in Section 3.2 a model electron density state is needed for the assimilation. Here we assume that the ionosphere can be modelled as a collection of one-dimensional 'Vary-Chap' electron layers.

<sup>233</sup> The standard description (e.g. Wang et al. (2021)) of a Vary-Chap electron den-<sup>234</sup> sity profile (described in Reinisch et al. (2007) as a generalization of an  $\alpha$ -Chapman pro-<sup>235</sup> file based on the work by Rishbeth and Garriott (1969)) with a height-dependent scale <sup>236</sup> height, H(h), is given by

$$N_e(h) = N_m \left(\frac{H(h)}{H_m}\right)^{-\frac{1}{2}} \exp\left(\frac{1}{2}\left[1 - u - \exp(-u)\right]\right),$$
(18)

238 where

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 $u = \int_{h_m}^h \frac{1}{H(h)} \, dh.$  (19)

In these equations  $N_m$  is the peak electron density, which occurs at  $h = h_m$ .  $H_m$  is the scale height at  $h_m$ .

The estimation of the Vary-Chap parameters in AVHIRO is based on minimizing a least squares cost function, with two terms (Lyu et al., 2019). The first term is the fit to a previous state estimate (rather than a "background" constraint); the second is the fit to the observed STEC measurements, which can be calculated from the L1 minus L2 phase delay measurements.

In practice the height-dependent scale height, H(h), in Equation 18 can be difficult to determine (Wang et al., 2021; Kutiev et al., 2009; Nsumei et al., 2012). Throughout this work the scale height used in the Vary-Chap profile varies linearly with height



Figure 2. Example of a Vary-Chap profile with 'standard' parameters given by Eqn (26).

(above the peak). This means that Eqns (18) and (19) reduce to

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$$N_e(h) = N_m \left(\frac{H(h)}{H_m}\right)^{-\frac{1}{2}} \exp\left(\frac{1}{2}[1-u-\exp(-u)]\right), \text{ where } (20)$$

$$u = \log(H/H_m)/k \quad \text{and} \tag{21}$$

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$$H(h) = H_m + k(h - h_m).$$
 (22)

These equations apply if  $h > h_m$ . If  $h \le h_m$ , or if  $k \le 10^{-3}$ , the 'standard' Chapman layer approximation, which is given by the limit as k tends to 0 of the above, applies. This is given by:

$$N_e(h) = N_m \exp\left(\frac{1}{2}[1-u-\exp(-u)]\right), \quad \text{where}$$
(23)

$$u = (h - h_m)/H_m \quad \text{and} \tag{24}$$

$$H(h) = H_m. (25)$$

The Vary-Chap profile defined by Eqns (20) to (22), using the 'standard F2' values of

$$N_m = 2 \times 10^{12} \text{ electrons m}^{-3}$$

$$h_m = 300 \text{ km}$$

$$H_m = 50 \text{ km}$$

$$k = 0.15$$

$$(26)$$

#### is plotted between 100 km and 600 km in Figure 2.

This one layer Vary-Chap profile provides a good approximation to the standard electron density profile. However, a better approximation can be formed through the addition of multiple Vary-Chap profiles, for example one for each ionospheric layer (D, E, F1 and F2). It can also be beneficial to introduce a "topside" layer, to try to account for the systematic underestimation of electron densities above the F2 peak height given by the Vary-Chap model. (Prol et al. (2019) show that an F2 scale height that varies

		Parameter	rs	
	$N_m  ({\rm m}^{-3})$	$h_m \ (\mathrm{km})$	$H_m \ (\mathrm{km})$	k
D-Region	$2 \times 10^8$	70	5	0.05
E-Region	$5 \times 10^{10}$	110	20	0.05
F1-Region	$5 \times 10^{11}$	205	30	0.05
F2-Region	$2 \times 10^{12}$	300	50	0.15
"Topside"	$3 \times 10^{11}$	500	250	0.50

Table 1. Default Vary-Chap Parameters for up to 5-layers



Figure 3. Examples of multi-layer Vary-Chap profiles with the parameters given in Table 1.

quadratically, rather than linearly, with height gives a better fit to topside sounder measurements.) Various multi-layer Vary-Chap profiles using the parameters in Table 1 are
shown in Figure 3.

The resulting five-layer Vary-Chap model provides an excellent approximation to 276 the ionosphere, with a realistic looking E and F1 region. Using a fifth layer for the top-277 side addresses the underestimation as highlighted by Prol et al. (2019). In practice the 278 addition of the D-region layer has very little impact on the overall profile. Figure 4 shows 279 the difference between a five-layer (F2+F1+E+D+Topside) and four-layer (F2+F1+E+Topside)280 version, i.e. the difference in electron density by including the D-layer. As expected the 281 impact of including a D-Region in the model increases with decreasing altitude, although 282 the maximum difference is approximately  $2 \times 10^7 \text{m}^{-3}$ , which is over three orders of mag-283 nitude smaller than the absolute density at that altitude. The differences are insignif-284 icant, yet they add considerable time to the calculations. (See Section 6.2.) 285

### <sup>286</sup> 5 Practical considerations

The equations of Sections 3.1 and 4 are encoded numerically as follows. The forward model calculates the electron density profile defined by the four Vary-Chap parameters  $\{N_m, h_m, H_m, k\}$  according to Eqns (20)–(25). The integrals needed to calculate the slantwise TEC, S, according to Eqn (8) are estimated numerically by Simpson's rule, using at least 30 points between the tangent point and the LEO (counted twice), and



**Figure 4.** Electron density difference between using a five-layer (F2+F1+E+D+Topside) and four-layer (F2+F1+E+Topside) Vary-Chap model.

10 points between the LEO and the GNSS (counted once). The integrable singularity 292 at r = a is handled by working in terms of  $\cosh^{-1}(r/a)$  rather than r. The procedure 293 is repeated for each Vary-Chap layer. The resulting  $\partial S/\partial a$  is related to the vertical gra-294 dient of the excess phases according to Eqn (11), and this in turn is equated to the bend-295 ing angle differences according to Eqn (14). The resulting forward modelled bending an-296 gles  $\mathcal{H}(\mathbf{x})$  are then compared to the observed bending angle differences  $\mathbf{y}_o$  over the range 297 500-175 km, which is considered broad enough to capture the key features of the iono-298 sphere, without complicating the solution by trying to model smaller scale structures at 299 lower altitudes. 300

The tangent linear model, **H**, which is needed to minimise the cost function  $J(\mathbf{x})$ of Eqn (3), and the solution error covariance matrix **A** via Eqn (4), is calculated by evaluating manually differentiated counterparts of the non-linear model.

The cost function  $J(\mathbf{x})$  is minimised by means of a standard version of the Levenberg-304 Marquardt minimisation algorithm (Press et al., 1992), in which the 'diagonal weight-305 ing factor' (usually called  $\lambda$ ), which determines how closely the change in x follows the 306 path of steepest descent, is multiplied by 0.1 if the cost function is decreasing, and by 307 100 if the cost function starts increasing. Iterations are deemed to have converged when 308 changes to the state vector or to the cost function are sufficiently small. In addition, 'un-309 physical' state vector components, such as negative peak electron densities, are handled 310 during the iterative phase of the minimisation, usually by resetting them to a few per-311 cent of the associated errors, i.e. the square roots of the diagonal elements of **B**. These 312 are deliberately chosen to be rather large — typically around  $\{5.0 \times 10^{11} \text{ m}^{-3}, 100 \text{ km},$ 313 20 km, 0.05} for  $\{N_m, h_m, H_m, k\}$  respectively. 314

The results of this paper have been produced by code written in Python 3.0. Another, widely available version, which is written in Fortran 95, has been part of the Radio Occultation Processing Package (ROPP) since version 11.0 (released January 2022). ROPP is a collection of software, build scripts, test scripts and documentation, which is intended to help users to process RO data. It is maintained, developed and supported by EUMETSAT, through the Radio Occultation Meteorology Satellite Applications Facility (ROM SAF), and freely available to download from its website (ROM SAF, 2023).



**Figure 5.** Comparison between the 1D-Var electron density profile retrieval with the Abel transform, and AVHIRO model (Lyu et al., 2019).

Users should bear in mind that ROPP is under constant development, and that its code may not therefore exactly match that described in this paper. The differences, however, should be small.

#### 325 6 Results

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#### 6.1 Example retrievals

The 1D-Var retrieval results are compared with the AVHIRO retrieval (Lyu et al., 327 2019), and an Abel transform solution. The Abel transform retrievals are not absolute 328 electron density values, because we do not add the electron density at the LEO to the 329 profile. In addition, we have not corrected (calibrated) the bending angles to only in-330 clude the section of the path below the LEO satellite, by subtracting positive elevation 331 values with the same impact parameter (see Section 3.1 of Schreiner et al. (1999)). How-332 ever, the Abel solution should indicate whether or not the 1D-Var results look reason-333 able. Our implementation of the Abel transform assumes that the L2–L1 bending an-334 gle differences vary linearly in the vertical between observations. This means that the 335 Abel transform is linear, so the retrieved electron density profile can be computed as a 336 matrix multiplied by a vector of (differenced) bending angles. 337

The performance of the 1D-Var is illustrated with four cases (see Elvidge et al. (2023) for the complete analysis), which have been chosen for their differing retrieval characteristics and convergence properties.

#### 6.1.1 Case 1

The first case, shown in Figure 5, can be considered a good retrieval, and is the same example as shown in the top right panel of Figure 4 in Lyu et al. (2019). The 1D-Var retrieval uses two layers, an F2 layer and F1 layer. The three approaches agree very similarly around the profile peak (between approximately 200 and 400 km) but the 1D-Var solution differs from the AVHIRO and the Abel transform solutions outside this region.



Figure 6. Comparison between the 1D-Var electron density profile retrieval with the Abel transform retrieval of a COSMIC-2 profile and a nearby ionosonde. Also shown are the observations and the forward modelled solution in bending angle space (i.e.  $\alpha_2 - \alpha_1$ ). (Ionosonde profiles above the peak appear as dashed lines, as they are less reliable there.)

#### 6.1.2 Case 2

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The second case, shown in Figure 6, compares the 1D-Var retrieval with those from 348 COSMIC-2 (UCAR Cosmic Program, 2019) and a closely located ionosonde. Ionoson-349 des step through a range of HF frequencies transmitted vertically upwards and measure 350 the return echoes, which enables them to image the vertical profile of the ionosphere up 351 to the peak density. (Ionosonde density profiles above the peak are less reliable, because 352 they depend on a background model, which is why they are plotted as dashed lines in 353 this paper.) Ionosonde observations are widely used as reference observations for com-354 parative studies (e.g. Feltens et al. (2011); Elvidge et al. (2014); Scherliess et al. (2011)). 355 Here an ionosonde observation (profile) from within 200 km of the location of the oc-356 cultation have been used to demonstrate the 1D-Var retrieval. (A full statistical study 357 is undertaken in Elvidge et al. (2023)). Also shown is the convergence in bending angle 358 space, i.e. the observed (blue) and forward modelled solution (green) bending angle dif-359 ferences  $\alpha_2 - \alpha_1$ . 360

In this case the 1D Var solution is in very close agreement with the ionosonde ob-361 servations throughout the whole profile. Above approximately 300 km and below 160 362 km there are some deviations from the observations, but these are small. The COSMIC-363 2 retrieval is also very good, but overestimates the peak electron density. The COSMIC-364 2 profile shows more structure below 150 km, presumably resulting from the variabil-365 ity in the  $\alpha_2 - \alpha_1$  observations in that region. The 1D-Var solution is the result of fit-366 ting observations between 500 and 175 km (see Section 5), and therefore has no knowl-367 edge of this structure. Even so, the forward modelled bending angle differences give a 368 reasonable fit through the observations. 369

#### 6.1.3 Case 3

The third case, Figure 7, again compares the 1D-Var retrieval with COSMIC-2 and a nearby ionosonde (in the same manner as described in Section 6.1.2) and both the COSMIC-



**Figure 7.** Comparison between the 1D-Var electron density profile retrieval with the Abel transform retrieval of a COSMIC-2 profile and a nearby ionosonde. (Ionosonde profiles above the peak appear as dashed lines, as they are less reliable there.)

2 and 1D-Var retrievals are fairly similar. The peak heights of the profiles, at about 200 km, 373 are similar and both are slightly higher than that reported by the ionosonde. (But note 374 that autoscaled ionosonde observations should be treated carefully, and the errors in the 375 F2 peak height can be reasonably large (as much as 10%, according to Themens et al. 376 (2022)). The COSMIC-2 retrieval slightly overestimates the peak density whilst the 1D-377 Var slightly underestimates it. Between the peak of the electron density profile and about 378 150 km, the COSMIC-2 retrieval more closely matches the observations. Above about 379 275 km the two retrievals are very similar. (Differences from the ionosonde profile in this 380 region should be treated skeptically, for reasons explained in Section 6.1.2.) 381

#### 6.1.4 Case 4

In the final case, shown in Figure 8, the COSMIC-2 retrieval is generally closer to the ionosonde observation than the 1D-Var retrieval. Again, both retrievals have similar heights of peak density, but the COSMIC profile more closely matches the observations above and below the peak. However the COSMIC-2 retrieval returns negative electron densities below 100 km, whereas the 1D-Var retrieval cannot, for reasons described in Section 5.

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### 6.2 Convergence and computational expense

Elvidge et al. (2023) provides a full statistical analysis of the results of the 1dvar retrievals compared to Abel-transform-based COSMIC-2 retrievals. This section simply provides a flavour of the 1D-Var ionospheric retrieval method's performance on 145 bending angle profiles provided by the Institut D'Estudis Espacials de Catalunya (IEEC) in Barcelona, Spain. These are COSMIC-1 measurements from September 18, 2011. The data contains the "geometry free"  $(\phi_1 - \phi_2)$  phase differences as function of impact parameter, *a*, up to the COSMIC-1 satellite, which operated at an altitude of about 800 km.

The simulated differenced bending angles  $\alpha_2 - \alpha_1$  are computed with a finite difference approximation to  $\partial(\phi_1 - \phi_2)/\partial a$ . The vertical separation between the bending



**Figure 8.** Comparison between the 1D-Var electron density profile retrieval with the Abel transform retrieval of a COSMIC-2 profile and a nearby ionosonde. (Ionosonde profiles above the peak appear as dashed lines, as they are less reliable there.)

 Table 2.
 Average time per iteration, percentage of observations which converge, and statistics

 of the number of iterations needed for convergence, for up to five Vary-Chap layers

	Time per iteration (seconds)	Observations that converged	Mean $\pm$ std dev no. of iterations
1 layer	0.99	98.6%	$16.2 \pm 7.1$
2 layers	2.22	85.5%	$34.1\pm8.0$
3 layers	4.06	66.7%	$28.1\pm9.1$
4 layers	6.72	65.2%	$28.7\pm9.1$
5 layers	9.98	58.7%	$30.7 \pm 11.4$

angles is typically 500 m. A common radius of curvature of 6371 km is used for all cases
 since it was not included in the test datasets.

Although adding layers seems to improve the overall shape of the retrieved ionosphere, this comes at the cost of higher computational time and number of iterations required for the 1D-Var to converge. This is shown in Table 2. Note that the maximum number of iterations was set to 50. Any retrievals needing more iterations than this were recorded as convergence failures, and discarded from further analysis.

It can be seen from Table 2 that the average time per iteration increases as the num-406 ber of layers increases. However after an immediate jump in the average number of it-407 erations when using one- and two-layer models, the average number of iterations for con-408 verging observations remains fairly steady (at around 30). This leads to a monotonic in-409 crease in the average total length of time needed for an observation to converge using 410 the 1D-Var, as shown in Figure 9. In addition, the percentage of observations that con-411 verge continually decreases as the number of layers increases, from 98.6% with just one 412 layer to only 58.7% with five layers. More realistic retrieved electron density profiles there-413 fore come at a cost in CPU time computational and robustness. 414



Figure 9. Average time taken per iteration (blue) and average length of time for an observation to converge (red).

#### 415 **7** Discussion and Conclusions

This paper has described a new 1D-Var ionospheric retrieval method. This approach can be applied to the Metop-SG measurement geometry, which will truncate the ionospheric GNSS-RO measurements around 600 km above the surface, as well as 'standard' GNSS-RO measurement geometry, in which measurements are assumed to be available at all heights.

The original plan was to use the difference between the slantwise TECs of the L1 and L2 radio signals, expressed as a function of impact parameter, but the L2-L1 observed bending angle differences have been used instead. This approach is closer to the way that GNSS-RO data is used in neutral atmosphere applications, such as operational NWP.

A new 1D ionospheric bending angle forward operator has been developed, which
computes L2-L1 bending angle differences as a function of impact parameter. This operator assumes that the ionospheric electron density can be modeled as a collection of
'Vary-Chap' layers. As suggested by a comparison of bending angles generated by 1Dand 3D-NeQuick electron density models, the L2-L1 bending angle uncertainty is assumed
to be a constant 2.0 µrad, and vertical error correlations are neglected.

We find that gradient-based minimisation techniques can be successfully applied to this retrieval problem, and that the non-linear, nested exponential nature of the Vary-Chap profiles (see Eqn (20)) does not cause problems. This is in contrast to the assertion of Lyu et al. (2019). Typically, at least two out of three retrievals converge within 50 iterations, although this convergence rate decreases as more Vary-Chap layers are introduced. The iteration count, and the high final cost functions of the retrievals that fail to converge, provide useful diagnostic information, as does the automatically-generated solution error covariance matrix **A**.

A few example 2-layer 1D-Var retrievals have been compared against the results of the AVHIRO method, Abel transform retrievals, and nearby ionosondes. In general the 1D-Var method performs at least as well as AVHIRO and the Abel transform, and produces a close fit to the observed bending angle differences  $\alpha_2 - \alpha_1$  in the region where it is supposed to. By construction, 1D-Var also avoids one drawback of the Abel inversion technique, namely the generation of negative electron densities. Adding more layers can improve the fit, but at the cost of longer CPU times and a lower convergence rate.

The *a priori* information is essentially a first guess used to start the minimisation, rather than a strong constraint on the final 1D-Var solution, because the background errors are (deliberately) rather large. Better *a priori* information might speed up convergence but would not necessarily improve the 1D-Var solution. It would, however, make it easier to screen out poor bending angles at the start of the minimisation.

The key suggestion of this paper is that differenced (L1-L2) bending angles could be used in ionospheric data assimilation (DA) systems. Usually, slantwise TEC values are assimilated in such systems, but these require a correction for the Differential Code Biases (DCBs). But constant DCBs during the occultation will not affect the bending angles derived from raw phase delays, and can therefore be ignored. This claim should be tested in the context of a more formal data assimilation system.

#### 457 8 Open Research

458 COSMIC-1 data are available from (UCAR, 2014). The processed files from the 459 IEEC and AVHIRO output may be requested from Dr Hernández-Pajares.

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