## Coastal polynyas enable transitions between high and low West Antarctic ice shelf melt rates

Ruth Moorman<sup>1</sup>, Andrew F. Thompson<sup>1</sup>, and Earle Andre Wilson<sup>1</sup>

<sup>1</sup>California Institute of Technology

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#### Abstract

Melt rates of West Antarctic ice shelves in the Amundsen Sea track large decadal variations in the volume of warm water at their outlets. This variability is generally attributed to wind-driven variations in warm water transport towards ice shelves. Inspired by conceptual representations of the global overturning circulation, we introduce a simple model for the evolution of the thermocline, which caps the water warm layer at the ice-shelf front. This model demonstrates that interannual variations in coastal polynya buoyancy forcing can generate large decadal-scale thermocline depth variations, even when the supply of warm water from the shelf-break is fixed. The modeled variability involves transitions between bistable high and low melt regimes, enabled by feedbacks between basal melt rates and ice front stratification strength. Our simple model captures observed variations in near-coast thermocline depth and stratification strength, and poses an alternative mechanism for warm water volume changes to wind-driven theories.

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## Ruth Moorman<sup>1</sup>, Andrew F. Thompson<sup>1</sup>, and Earle A. Wilson<sup>2</sup>

<sup>1</sup>Environmental Science and Engineering, California Institute of Technology, Pasadena, California, USA <sup>2</sup>Department of Earth System Science, Stanford University, Stanford, California, USA

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 $Corresponding \ author: \ Ruth \ Moorman, \verb"rmoorman@caltech.edu"$ 

#### 13 Abstract

Melt rates of West Antarctic ice shelves in the Amundsen Sea track large decadal vari-14 ations in the volume of warm water at their outlets. This variability is generally attributed 15 to wind-driven variations in warm water transport towards ice shelves. Inspired by con-16 ceptual representations of the global overturning circulation, we introduce a simple model 17 for the evolution of the thermocline, which caps the warm water layer at the ice-shelf 18 front. This model demonstrates that interannual variations in coastal polynya buoyancy 19 forcing can generate large decadal-scale thermocline depth variations, even when the sup-20 ply of warm water from the shelf-break is fixed. The modeled variability involves tran-21 sitions between bistable high and low melt regimes, enabled by feedbacks between basal 22 melt rates and ice front stratification strength. Our simple model captures observed vari-23 ations in near-coast thermocline depth and stratification strength, and poses an alter-24 native mechanism for warm water volume changes to wind-driven theories. 25

#### <sup>26</sup> Plain Language Summary

Ice loss from the West Antarctic Ice Sheet contributes significantly to current and 27 projected rates of global sea-level rise. The ice sheet is primarily losing mass via glaciers 28 that flow from the Antarctic continent into the Amundsen Sea, where floating ice shelves 29 are exposed to much warmer ocean waters than elsewhere around Antarctica. In this work 30 we present a simplified mathematical model for the volume of warm water at Amund-31 32 sen Sea ice shelf fronts that reproduces observed patterns of warm water variability. The modeled variability relies on interactions between ice shelf melt and coastal polynyas, 33 regions where enhanced wintertime sea-ice production can trigger mixing that diverts 34 heat carried by warm waters away from the ice shelf and into the atmosphere. Higher 35 melt rates inhibit polynya convection, allowing more warm water into the ice shelf cav-36 ity and reinforcing a high melt state, whilst lower melt rates facilitate polynya convec-37 tion, diverting heat away from the ice shelf and reinforcing a low melt state. Interan-38 nual variations in polynya sea-ice production trigger shifts between these reinforcing states. 39 Our results promote the importance of coastal processes in explaining observed varia-40 tions in Amundsen Sea ice shelf melt, which have previously been attributed to remote 41 wind patterns. 42

#### 43 **1** Introduction

Recorded mass loss from the West Antarctic Ice Sheet (WAIS) has been driven by 44 the accelerating flow of ice streams that terminate at rapidly thinning ice shelves in the 45 Amundsen Sea embayment (Mouginot et al., 2014; Paolo et al., 2015; IMBIE Team, 2018). 46 Whilst ice shelf thinning does not directly impact the ice sheet mass balance, the restrain-47 ing or "buttressing" effect of floating ice shelves on upstream grounded ice flow is crit-48 ical for limiting ice discharge through glaciers (Fürst et al., 2016; Morlighem et al., 2020). 49 The observed thinning of buttressing ice shelves in the Amundsen Sea has been associ-50 ated with high rates of basal melt driven by modified Circumpolar Deep Water (mCDW) 51 (Adusumilli et al., 2020; Pritchard et al., 2012; Shepherd et al., 2004; Turner et al., 2017); 52 a warm (2-4°C above freezing) water mass that floods the lower layers of the West Antarc-53 tic continental shelf and carries heat from the open ocean to ice shelf cavities via glacially-54 carved troughs (Walker et al., 2007; Dutrieux et al., 2014). Future projections of the WAIS 55 require accurate representation of forcings that dictate the access of warm mCDW to 56 Amundsen Sea ice shelf cavities. 57

Hydrographic observations from the Amundsen Sea embayment reveal decadal variations in the thickness of the mCDW layer (Dutrieux et al., 2014; Jenkins et al., 2018)
 that overwhelm multidecadal ocean warming trends previously considered the driver of
 ice shelf thinning (Schmidtko et al., 2014). This decadal variability is well observed in
 front of the Dotson Ice Shelf, where sea-ice free conditions in the Amundsen Sea Polynya

(ASP) permit the collection of summertime hydrographic profiles near the ice shelf front 63 (Figure 1). Observations from 2000 to 2018 reveal high amplitude ( $\sim 400$  m), low fre-64 quency ( $\sim 10$  year period) variability in the thermocline depth, characterized by a warm 65 phase with thick mCDW from 2006-2011 followed by a cool phase with thin mCDW from 66 2012-2016 and a potential return to warm conditions in 2018 (Figure 1b,d) (Jenkins et 67 al., 2018; Kim et al., 2021). The observed thermocline variability has been linked to Dot-68 son Ice Shelf basal melt rates (Jenkins et al., 2018) and may be implicated in ice shelf 69 thinning trends, either via historical warm phases triggering geometric grounding line 70 retreat that continues to the present (Jenkins et al., 2016) or via a trend in the frequency 71 of warm phases unresolved by the short observational record (Naughten et al., 2022). 72

This mCDW thickness variability is often attributed to mechanical wind forcing. 73 Numerous studies relate eastward wind anomalies over the Amundsen shelf with warm 74 phases, suggesting these winds enhance poleward mCDW transport by barotropically 75 accelerating the Amundsen undercurrent (Assmann et al., 2013; Dotto et al., 2019, 2020; 76 Holland et al., 2019; Naughten et al., 2022). Recently, Silvano et al. (2022) affirm this 77 barotropic mechanism at short timescales, but find eastward winds have the opposite ef-78 fect on poleward mCDW transport at decadal (and longer) timescales due to baroclinic 79 adjustment of the undercurrent. Melt rate variability is more consistent with these longer 80 time scales. Variations in coastal (Yang et al., 2022), shelf-break (Kim et al., 2017; Web-81 ber et al., 2019), and shelf integrated (Kim et al., 2021) wind-driven Ekman pumping 82 are also suggested as potential drivers. Though mechanisms differ, these studies consis-83 tently present wind-driven variability of shoreward mCDW transport as the driver of ther-84 mocline depth variability and associated melt variability in the Amundsen Sea. 85

There are indications that the wind-driven framework is incomplete. Coastal ther-86 mocline depth and heat content variability is substantially amplified relative to the shelf-87 break in both observations and simulations (e.g. Kim et al., 2021; Silvano et al., 2022; 88 Naughten et al., 2022), a feature not directly addressed by wind-driven mechanisms. Fur-89 ther, while thermocline displacements predicted from winds correlate well with obser-90 vations, they underestimate the amplitude of coastal signals (Kim et al., 2021). Prompted 91 by this amplitude gap, we revisit the Dotson Ice Front hydrography. Years with thick 92 mCDW layers (2006-2011) are consistently associated with stronger stratification (Fig-93 ure 1d) and more buoyant, meltwater modified Winter Waters (WW) relative to years 94 with thin mCDW layers (2000, 2012-2016). Further, during warm years, modification 95 by glacial meltwater pulls WW, a remnant of the preceding winter's sea-ice modified mixed 96 layer, away from the freezing line and towards the mCDW-meltwater mixing line (the 97 "Gade Line") (Figure 1c). These hydrographic properties suggest a role for water mass 98 transformation by sea-ice, produced in large quantities in coastal polynyas generally and 99 the ASP in particular (Macdonald et al., 2023; Tamura et al., 2008, 2016), and glacial 100 ice in the observed variability. 101

Informed by a high-resolution regional ocean simulation and the observations pre-102 sented above, we introduce a simple overturning circulation model that represents the 103 transformation of mCDW into cool thermocline waters both within the Dotson Ice Shelf 104 cavity and at its entrance in the ASP. Using this model, we demonstrate that variations 105 in polynya surface buoyancy fluxes, directly related to net local sea-ice formation rates, 106 can generate large decadal scale thermocline depth variations in the absence of variable 107 shelf-break forcing, posing an alternative mechanism for observed variability. The mod-108 eled thermocline variability takes the form of transitions between bistable warm and cool 109 regimes, made possible by feedbacks between basal ice melt and stratification at the ice 110 front. With this work, we underscore that variations in mCDW consumption, in addi-111 tion to mCDW supply, can strongly influence the exposure of West Antarctic ice shelves 112 to ocean heat. This work uses the Dotson Ice Shelf as a case study, however our model 113 is applicable to other West Antarctic ice shelves fringed by coastal polynyas, including 114 Venable and Pine Island ice shelves. 115



Figure 1. (a) Map of the Amundsen Sea embayment showing open ocean bathymetry (green shading; grey contours), ice shelf cavity bathymetry (grey shading; grey contours), and the grounded ice zone (dark grey). The Dotson Ice Front is outlined in red with an enlarged view provided above. The January climatological mean (2004-2022) extent of the Amundsen Sea Polynya (ASP) is indicated by the pink contour (using Fetterer & Stewart., 2020). Locations of shipborne observations used to produce (b)-(d) are indicated in the enlarged map. (b,c) Cruise mean conservative temperature  $(\Theta)$  profiles as a function of pressure (b) and absolute salinity (S) (c). Mean profiles (solid lines) and standard deviations (shading) are calculated in density space and sorted into pressure space (as in Dutrieux et al., 2014) before being smoothed with a 5 dbar rolling mean. Water masses discussed in the main text (modified Circumpolar Deep Water, mCDW, and Winter Water, WW) are labelled. Potential density (black contours), the freezing line (thick black line), and an example Gade line indicative of mixing between mCDW and glacial meltwater (dashed black line) are shown for reference in (c). (d) Timeseries of  $\gamma$ , a bulk indicator of stratification strength calculated as the potential energy required to homogenize profiles between 5 and 750 dbars (circles), and the absolute depth of the mCDW layer  $AD_{mCDW}$ , a proxy for the thermocline depth developed by Kim et al. (2021) (crosses) (details in Supporting Information S1). AD<sub>mCDW</sub> and  $\gamma$  values are offset on the time axis for clarity. Variables required for the calculation of  $AD_{mCDW}$  were not obtained for 2006. Observations were collected in the austral summer between December (previous year) and March (listed year).

#### 116 2 Methods

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#### 2.1 Ice front overturning model

Motivated by observational evidence that the ice front thermocline depth is tied 118 to basal melt rates (Jenkins et al., 2018) and that barotropic heat transport is blocked 119 at the ice shelf front (Wåhlin et al., 2020), we present a purely baroclinic model for heat 120 transport to ice shelves reminiscent of simple models for the global overturning (Walin, 121 1982; Gnanadesikan, 1999). This baroclinic model represents the shoreward transport 122 of warm mCDW and export of cool surface water masses, including WW and glacially 123 modified CDW, within Amundsen Sea glacially carved troughs (e.g. Webber et al., 2019). 124 This exchange is facilitated by water mass transformation, which may occur within the 125 ice shelf cavity or the ASP. Transformations are modeled in a small region proximate to 126 the ice shelf front, isolating the effect of coastal forcing from shelf-break processes. 127

Key model components are illustrated in Figure 2. Warm mCDW and overlying 128 thermocline waters are represented as boxes within the small region where wintertime 129 coastal polynya sea-ice formation is concentrated (50 km meridional, 55 km zonal ex-130 tent to match the width of the Dotson Ice Shelf). The inflow of warm mCDW,  $\Psi_{in}$ , is 131 prescribed to represent remote wind-driven variations in shoreward mCDW transport. 132 This mCDW then transforms into offshore flowing thermocline waters via two pathways: 133 by melting glacial ice and mixing with the resultant meltwater in the ice shelf cavity ( $\Psi_{ice}$ ) 134 or by mixing with overlying waters  $(\Psi_{\rm P})$  (Figure 2a,b). Assuming negligible volume in-135 put from meltwater, the steady state transports balance, 136

$$\Psi_{\rm in} = \Psi_{\rm ice} + \Psi_{\rm P}.\tag{1}$$

The partitioning of mCDW transformation into  $\Psi_{ice}$  and  $\Psi_{P}$  is set by the thickness and relative buoyancy (i.e. stratification) of the mCDW and surface boxes. As illustrated in Figure 2c, the thermocline depth (*h*) and the thickness of the underlying mCDW layer ( $h_{mCDW}$ ) evolve according to,

$$\frac{\mathrm{d}h}{\mathrm{d}t} = \frac{1}{L} \Big[ \Psi_{\mathrm{ice}} + \Psi_{\mathrm{P}} - \Psi_{\mathrm{in}} \Big],\tag{2}$$

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where L is the meridional model extent and H is the ice front water column thickness (taken as 700 m).  $\Psi$  terms are converted from thickness fluxes to volume transports (1 Sv  $= 10^6 \text{ m}^3 \text{ s}^{-1}$ ) via the model zonal extent.

 $h_{\text{mCDW}} = H - h$ ,

For the evolution of the stratification strength, we define buoyancy as the vertical acceleration a water mass experiences due to density perturbations, i.e.  $b_i \equiv g\rho_i/\rho_0$ . The buoyancy of the mCDW layer  $(b_{\rm mCDW})$  is kept constant, justified by the minimal variability in mCDW density in observations (Figure 1c). We set

$$b_{\rm mCDW} = 0, \tag{4}$$

(3)

referencing our system to the buoyancy of the mCDW layer, such that the buoyancy dif-  
ferential between mCDW and thermocline waters, a metric for the ice front stratifica-  
tion strength, is 
$$\Delta b = b - b_{mCDW} = b$$
 where b is the buoyancy of thermocline waters.  
The stratification strength ( $\Delta b$ ) then evolves according to the divergence of buoyancy  
fluxes from the thermocline (Figure 2c),

$$\frac{\mathrm{d}\Delta b}{\mathrm{d}t} = \frac{1}{L} \left[ (vb)_{\mathrm{in}} - (vb)_{\mathrm{out}} \right] + \frac{1}{h} \left[ (wb)_{\mathrm{in}} - (wb)_{\mathrm{out}} \right]$$
(5)

159 where,

$$(vb)_{\rm in} = \frac{\Psi_{\rm ice}\Delta b_{\rm melt}}{h}, \quad \text{and}$$
(6)

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$$(vb)_{\rm out} = \frac{\Psi_{\rm in}\Delta b}{h}.$$
(7)

Here,  $\Delta b_{melt}$  is the buoyancy of waters transformed by mixing with glacial meltwater, relative to  $b_{mCDW}$ , which we determine from hydrography to be  $6.7 \times 10^{-3}$  m s<sup>-2</sup> (lightest waters in Figure 1c). The vertical buoyancy budget comprises a prescribed surface buoyancy flux due to net sea-ice formation,

$$(wb)_{\rm out} = -F_{\rm surf} \tag{8}$$

(negative  $F_{\text{surf}}$  values lower surface ocean buoyancy) and buoyancy loss to the underlying mCDW layer ( $(wb)_{\text{in}}$ ). The latter simplifies to

$$(wb)_{\rm in} = \frac{\Psi_{\rm P} b_{\rm mCDW}}{L} - \frac{\kappa_{\rm P} (b - b_{\rm mCDW})}{h} = -\frac{\kappa_{\rm P} \Delta b}{h}.$$
(9)

given  $b_{\rm mCDW} = 0$ . In (9) we select h as the most appropriate length-scale controlling diffusive vertical buoyancy transfer, since a thicker surface layer poses greater resistance to entrainment at its lower boundary when the primary energy source driving mixing is input at the surface.

The form of the polynya diffusivity term in (9),  $\kappa_{\rm P}$ , is central to the feedbacks described in this study. Simply put,  $\kappa_{\rm P}$  is a smoothed step function that transitions from



Figure 2. Schematic illustration of the ice front overturning model under (a) diffusive  $(\kappa_{\rm P} \rightarrow \kappa_{\rm diff})$  and (b) convective  $(\kappa_{\rm P} \rightarrow \kappa_{\rm conv})$  conditions. The thermocline and modified Circumpolar Deep Water (mCDW) layers are shaded blue and red respectively, and the ice shelf is shaded grey. Thick and dashed red arrows show the primary and secondary transformation pathways associated with each state. Thickness and buoyancy fluxes ( $\Psi_{\rm in}, \Psi_{\rm ice}, \Psi_{\rm P}$  and  $F_{\rm surf}$ ) are indicated. (c) Schematic of the thickness and buoyancy budgets of the thermocline (upper; thickness and buoyancy evolved explicitly) and mCDW (lower; thickness evolved implicitly, buoyancy held constant) layers. The implied buoyancy budget of the mCDW layer is shown in grey, however  $b_{\rm mCDW}$  does not evolve.

a small diffusive end member  $\kappa_{\text{diff}}$  when the thermocline is buoyant to a large convective end member  $\kappa_{\text{conv}}$  when the thermocline approaches the density of the underlying mCDW. The effect is analogous to rapid transitions to vertical homogeneity triggered by static instability in simple models of open ocean polynyas (Martinson et al., 1981; Boot et al., 2021). Functionally, we define  $\kappa_{\text{P}}$  as,

$$\kappa_{\rm P}(\Delta b) = \frac{\kappa_{\rm conv} - \kappa_{\rm diff}}{2} \left( 1 - \tanh\left(\phi(\Delta b - \Delta b_{\rm crit})\right) \right) + \kappa_{\rm diff},\tag{10}$$

where  $\kappa_{\text{conv}}$  (10<sup>-2</sup> m<sup>2</sup> s<sup>-1</sup>) and  $\kappa_{\text{diff}}$  (10<sup>-4</sup> m<sup>2</sup> s<sup>-1</sup>, taken from Pine Island Ice Front observations, Garabato et al., 2017) are vertical diffusivities,  $\Delta b_{\text{crit}}$  (5 × 10<sup>-4</sup> m s<sup>-2</sup>) is a small stratification strength at which turbulent convection onsets, and  $\phi$  (5×10<sup>4</sup>) is a parameter determining the steepness of the onset of convection. Our results are not sensitive to reasonable perturbations of the parameters.

The polynya mass transport term  $\Psi_{\rm P}$  is obtained from (9) by assuming an advectiondiffusion balance of buoyancy holds in the vertical (for details of similar parameterizations see Marshall & Zanna, 2014; McDougall & Dewar, 1998; Munk, 1966),

$$\Psi_{\rm P} = -\frac{\kappa_{\rm P}L}{h}.\tag{11}$$

Finally, the ice cavity overturning  $\Psi_{ice}$  is taken to be linearly proportional to mCDW thickness,

$$\Psi_{\rm ice} = \alpha h_{\rm mCDW} = \alpha (H - h), \tag{12}$$

where  $\alpha$  (2.1×10<sup>-3</sup> m s<sup>-1</sup>) is diagnosed from the WAIS 1080 regional simulation (see §2.2 and Supporting Information S2).

To summarize, the ice front overturning model is described by the following coupled differential equations for the thermocline depth (h) and stratification strength  $(\Delta b)$ ,

$$\frac{\mathrm{d}h}{\mathrm{d}t} = \frac{1}{L} \Big[ \alpha (H-h) - \frac{\kappa_{\mathrm{P}}L}{h} - \Psi_{\mathrm{in}} \Big], \tag{13}$$

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$$\frac{\mathrm{d}\Delta b}{\mathrm{d}t} = \frac{1}{Lh} \Big[ \alpha (H-h) \Delta b_{\mathrm{melt}} - \Psi_{\mathrm{in}} \Delta b \Big] + \frac{1}{h^2} \Big[ F_{\mathrm{surf}} h - \kappa_{\mathrm{P}} \Delta b \Big]. \tag{14}$$

All parameter values except  $\kappa_{\rm P}$  are diagnosed from observations or WAIS 1080 (§2.2), and  $\Psi_{\rm in}$  and  $F_{\rm surf}$  are prescribed forcings representing the supply of mCDW (a remote forcing) and polynya surface buoyancy fluxes from sea-ice (a local forcing).

#### 205 2.2 Regional general circulation model

In addition to the ice front overturning model, we utilize monthly mean output from 206 WAIS 1080, a high-resolution ( $\sim 3$  km horizontal spacing) regional configuration of the 207 Massachusetts Institute of Technology general circulation model (MITgcm) that repre-208 sents the Antarctic Peninsula to the western edge of the Amundsen Sea (Flexas et al., 209 2022). The model is forced at the surface by the European Centre for Medium-Range 210 Weather Forecasts (ECMWF) reanalysis version 5 (ERA5; Hersbach et al., 2020) and 211 integrated from 1992 to 2019. WAIS 1080 explicitly represents freezing and melting within 212 ice shelf cavities of a fixed shape, making it suited to the study of ocean ice-shelf inter-213 actions at relatively short timescales. We use the control simulation from Flexas et al. 214 (2022), who provide additional model details, to constrain the values of parameters ( $\alpha$ ) 215 and forcings  $(F_{\text{surf}}, \Psi_{\text{in}})$  of the ice front overturning model that are difficult to obtain 216 directly from observations (details in Supporting Information S2). 217

#### 218 3 Results

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#### 3.1 Steady state model behavior

Equilibrated solutions of the ice front overturning model map a hysteresis loop for the thermocline depth in response to varying surface buoyancy forcing  $(F_{surf})$  when the

supply of mCDW from the shelf-break ( $\Psi_{in}$ ) is held fixed (Figure 3a). Thus, warm and 222 cold regimes can be realized with the same mCDW supply. This hysteresis loop is en-223 abled by a positive feedback between the depth of the ice front thermocline and the strat-224 ification of the ice front water column, the physics of which are parameterized in our ver-225 tical diffusivity term  $\kappa_{\rm P}$ . A shallow ice front thermocline, equivalent to a thick mCDW 226 layer, supports high melt rates within the cavity. The ensuing meltwater provides an ad-227 ditional buoyancy input to the thermocline that suppresses convection and reinforces the 228 shallow thermocline position (upper "branch" of the hysteresis loop, Figure 3a). By con-229 trast, a deep ice front thermocline, equivalent to a thin mCDW layer, is associated with 230 a weaker ice shelf melt rate and a reduced input of buoyant meltwater to the thermo-231 cline, comparatively preconditioning the water column for convection and reinforcing the 232 deep thermocline position (lower "branch", Figure 3a). This feedback produces bistable 233 "diffusive" ( $\kappa_{\rm P} = \kappa_{\rm diff}$ , thick mCDW) and "convective" ( $\kappa_{\rm P} = \kappa_{\rm conv}$ , thin mCDW) 234 steady states for a fixed supply of mCDW associated with a  $\sim 400$  m thermocline depth 235 differential. In this idealized model, most convective steady states are unstably strat-236 ified  $(\Delta b < 0)$  as they arise when strong negative buoyancy forcing is continuously ap-237



Figure 3. (a) Dependence of the model steady state on  $F_{\text{surf}}$  when  $\Psi_{\text{in}}$  is held fixed at the mean WAIS 1080 value (0.06 Sv). The model is evolved to steady state after incrementally increasing and decreasing values of  $F_{\text{surf}}$  (direction indicated by arrows) spanning the range simulated in WAIS 1080. The forward and reverse pathways are offset to aid visualization. Text inset identifies solutions associated with  $\kappa_{\text{P}} = \kappa_{\text{conv}}$  ("convective steady states") and  $\kappa_{\text{P}} = \kappa_{\text{diff}}$  ("diffusive steady states"). (b-e) Plots showing equilibrated h (b,d) and  $\Delta b$  (c,e) values associated with diffusive steady states (b,c) and convective steady states (d,e) for a range of  $\Psi_{\text{in}}$  and  $F_{\text{surf}}$  forcing values. Regions of each phase space left white do not support steady states with the relevant  $\kappa_{\text{P}}$  value. Magenta contours outline the parameter space able to support both diffusive and convective steady states to with h > 700 m (depth of the water column) are not physical, but are shown here since transient forcing in this region is permissible.

plied. These bistable states have comparable mCDW depths to the observed warm and
cool phases (Figure 1d), although available observations of cool phases are stably stratified (Webber et al., 2017; Yang et al., 2022).

Bistability occurs over a large portion of the explored forcing space (magenta con-241 tour, Figure 3b-e), which spans realistic ranges of  $F_{\rm surf}$  and  $\Psi_{\rm in}$  (monthly mean values 242 span  $-1.7 \times 10^{-7}$  to  $0.5 \times 10^{-7}$  m<sup>2</sup> s<sup>-3</sup> and 0 to 0.3 Sv in WAIS 1080). Forcing com-243 binations that support only one steady state solution are referred to as monostable. Fig-244 ure 3b-e suggests variations in both  $F_{\text{surf}}$  (vertical paths in Figure 3b-e) and  $\Psi_{\text{in}}$  (hor-245 izontal paths) can generate hysteresis by shifting the system from one monostable re-246 gion to the other via the bistable region. Whilst Figure 3 displays numerically equilibrated 247 model output, a benefit of this model's simplicity is that it permits analytical solutions 248 for end member cases and easy exploration of parameter space (Supporting Information 249 S3). Overall, model behavior is not qualitatively sensitive to reasonable parameter per-250 turbations; a summary of our sensitivity assessment appears in Table S1. 251

#### 252

#### 3.2 Transient model behavior

The presence of bistability in this simple model poses an alternate explanation for 253 the decadal scale  $\sim 400$  m thermocline depth variations observed at the Dotson Ice Front. 254 The observed variability could, as previously implied, be a low frequency response to low 255 frequency variations in the supply of mCDW to the ice front. Alternatively, our simple 256 model suggests that transient perturbations of either mCDW supply or coastal surface 257 buoyancy fluxes could trigger transitions between self-reinforcing deep and shallow ther-258 mocline states, perhaps explaining the large amplitude and persistent nature of the ob-259 served cool and warm phases. This possibility is tested with transiently forced exper-260 iments. 261

The ice front overturning model is initialized with either weak or strong stratifi-262 cation and forced with WAIS 1080 climatological mean  $F_{\text{surf}}$  and  $\Psi_{\text{in}}$  values until an-263 nual patterns of ice front stratification  $(\Delta b)$  and thermocline depth (h) equilibrate. The 264 WAIS 1080 climatology lies sufficiently within the bistable forcing region (yellow shad-265 ing, Figure 4a,b) to support temporally varying solutions that persist in their initial regime. 266 These equilibrated simulations are then transiently forced with perturbed climatologies 267 to prompt regime transitions that persist when the forcing returns to the original pat-268 tern. Two winter perturbations are constructed by decreasing the May-September  $F_{\rm surf}$ 269 or  $\Psi_{in}$  forcing by a constant offset, and two summer perturbations are constructed by 270 increasing the December-April  $F_{surf}$  or  $\Psi_{in}$  forcing by a constant offset. Winter and sum-271 mer perturbations are then tested for their ability to drive transitions from the diffusive to the convective regime and vice versa. Seasonal perturbations are chosen based on the 273 strong seasonality of  $F_{surf}$ ; we also use a seasonal perturbation for  $\Psi_{in}$  experiments for 274 consistency, although  $\Psi_{in}$  has a more complex annual pattern (Figure 4b inset). 275

Figure 4a,b show the smallest amplitude winter and summer offsets that trigger 276 regime shifts within two consecutive years of perturbed forcing. When regime transitions 277 are simulated (Figure 4c,e,f), lags between the thermocline response and stratification 278 response align with observations. In agreement with the observed transition from a warm 279 phase to a cool phase between 2009 and 2012 (Figure 1d), thermocline depth anomalies 280 lag buoyancy anomalies during modeled transitions to convective conditions (Figure 4c). 281 The shoaled thermocline observed in 2018 may represent a transition to warm phase con-282 ditions with the opposite lag, thermocline shoaling preceding stratification strengthen-283 ing. If so, the simulated lags between thermocline depth anomalies and buoyancy anoma-284 lies in both  $\Psi_{\rm in}$  and  $F_{\rm surf}$ -driven transitions to diffusive conditions (Figure 4d,e) are also 285 consistent with observations. 286

In addition to capturing the nature of observed transitions between warm and cool phases at the Dotson Ice Front, our idealized model anticipates the shallow bias and di-

minished variability of the ice front thermocline depth in WAIS 1080 ( $0^{\circ}$ C isotherm depth 289 ranges from 440-820 m in observations and only 255-420 m in WAIS 1080). When the 290 ice front overturning model is forced with the full WAIS 1080 1992-2019 timeseries of 291  $F_{\rm surf}$  and  $\Psi_{\rm in}$ , rather than climatological values, simulations initialized with convective 292 conditions rapidly transition to diffusive conditions and remain there (Figure S5), con-293 sistent with WAIS 1080 failing to capture convective events. In general, transitions to 294 convective states required larger deviations from the WAIS 1080 forcing than transitions 295 to diffusive states. Significantly stronger negative  $F_{\text{surf}}$  values than those simulated in 296 WAIS 1080 were needed to generate a regime shift within a single year (minimum win-297 ter values of  $-3 \times 10^{-7}$  m<sup>2</sup> s<sup>-3</sup> compared to minimum WAIS 1080 forcing of  $-1.7 \times$ 298  $10^{-7}$  m<sup>2</sup> s<sup>-3</sup>), thus our choice to present results of two-year perturbations in Figure 4. 299 ERA5 has been shown to underestimate near-surface wind speeds along the Antarctic 300 coastline (Caton Harrison et al., 2022) and this may induce an underestimation of win-301 ter  $F_{\text{surf}}$  minima in WAIS 1080, alternatively, WAIS 1080 and our idealized model may 302 exaggerate the barrier to convection. Observational estimates indicate gross annual ASP 303 sea-ice formation varies significantly, ranging from  $139 \text{ km}^3$  to  $80 \text{ km}^3$  from 2017 to 2020 304 (Macdonald et al., 2023), suggesting the large interannual variations in surface buoyancy 305 forcing needed to trigger regime shifts in our model are plausible. 306

Reductions in  $\Psi_{in}$ , whether transient (Figure 4d) or more sustained (Figure S6), 307 do not trigger transitions to convective conditions for any physical choice of offset (en-308 forcing  $\Psi_{\rm in} > 0$ ). Such regime shifts are not supported as reducing  $\Psi_{\rm in}$  initially strength-309 ens ice front stratification in our simulations. This anticorrelation between thermocline 310 depth and stratification when  $\Psi_{in}$  is reduced is not supported by observations or WAIS 311 1080, however, and may reflect the simplicity of our model. These experiments affirm 312 the possibility that polynya forcing can drive realistic transitions to cool phases, but do 313 not negate the possibility that variable mCDW supply could also drive such transitions. 314 Both forcings appear able to drive realistic transitions to warm conditions. 315

#### **4 Discussion and Outlook**

This study intentionally targets a simplified representation of West Antarctic coastal 317 ocean dynamics to highlight mechanistic links between surface forcing, interior mixing, 318 thermocline depth variations, and overturning pathways on the West Antarctic conti-319 nental shelf. The key result is the identification of positive feedbacks that are indepen-320 dent of the supply of mCDW from the continental shelf break. These feedbacks involve 321 interactions between basal ice shelf melt rates and thermocline stratification strength at 322 the ice shelf front and provide a plausible explanation for the amplitude and duration 323 of multi-year warm and cool phases observed, for example, at the Dotson Ice Front. The 324 modeled thermocline variability tracks the strength of convection in the adjacent coastal 325 polynya and successfully reproduces observed stratification changes, not previously iden-326 tified, associated with transitions between the warm and cool phases. The importance 327 of coastal convection to this feedback highlights the need to appropriately represent ver-328 tical mixing when simulating West Antarctic ocean-forced ice shelf melt. Modeled shifts 329 in convection strength can be triggered by both variable mCDW supply from the con-330 tinental shelf break (a remote forcing), and variable surface buoyancy fluxes within the 331 polynya (a local forcing). Since future trends in mCDW supply from the shelf-break and 332 sea-ice production in coastal polynyas may not align, understanding the relative impor-333 tance of these forcings is important for projecting future melt. Finally, given the pos-334 itive feedback identified cannot be represented in ocean models that apply fixed melt-335 water inputs, our results emphasize that future work should utilize models that simu-336 late basal melt within cavities. As a first step on this path, we show that the idealized 337 model predicts the shallow, steady bias of the Dotson Ice Front thermocline in the WAIS 338 1080 model based on its forcing, demonstrating the power of using idealized models to 330 interpret biases in complex models. 340



Figure 4. (a, b) The forcing parameter space partitioned into regions supporting only one steady state solution (diffusive in red; convective in blue) and both solutions (bistability in yellow. Climatological mean  $F_{surf}$  and  $\Psi_{in}$  values from the WAIS 1080 simulation are shown within this forcing space (solid black lines) with arrows indicating the progression of an annual cycle. Winter perturbed forcings (dashed lines) and summer perturbed forcings (dotted lines) are indicated within the forcing space for  $F_{surf}$  experiments (a) and  $\Psi_{in}$  experiments (b). Forcing climatologies are shown as a function of time in inset panels for clarity. (c-f) Full time series of h(solid grey lines) and  $\Delta b$  (dashed grey lines) alongside January-March mean values (black crosses and circles, respectively) from transient forcing experiments described in the main text. Shaded regions indicate the perturbation period (years 4 and 5) and whether a winter (blue; c,d) or summer (red; e,f) perturbation was prescribed.

The idealized representation of coastal dynamics in this study neglects certain pro-341 cesses that merit discussion. The most notable simplification is that WW, meltwater mod-342 ified CDW, and other surface waters are combined in a single box. As a result, the spa-343 tial structure of glacial meltwater plumes exiting the cavity (e.g. Garabato et al., 2017; 344 Zheng et al., 2021) and exiting the model domain are omitted, and buoyancy from melt-345 water is uniformly distributed above the thermocline. This simplification may lead to 346 spurious stratification strengthening in response to reductions in mCDW supply (Fig-347 ure 4d), as unresolved structures may remove meltwaters from the ice shelf front more 348 rapidly than our model suggests. The truncated vertical structure of our model also leads 349 to unrealistic year-round convection during cool phases in transiently forced simulations 350 (Figure 4). In the real ocean, positive  $F_{\text{surf}}$  forcing during summer months may halt con-351 vection by stratifying a small fraction of the upper water column whilst leaving the deep 352 thermocline position intact. In our model, positive buoyancy fluxes are distributed over 353 the full thermocline depth, presenting an exaggerated barrier to restratification. Con-354 sequently, the water column convects year-round rather than being preconditioned for 355 the annual recurrence of convection. Another noteworthy simplification is that, since  $\Psi_{\rm in}$ 356 and  $F_{\text{surf}}$  are prescribed, we neglect feedbacks that influence their magnitude. Shoreward 357 mCDW transport in the Amundsen Sea may decrease (Moorman et al., 2020; Beadling 358 et al., 2022) or increase (Si et al., 2023) in response to coastal freshening, and coastal 359 sea-ice formation rates may likewise be sensitive to coastal freshening by meltwater. Fi-360 nally, we note that this model does not represent advection of non-local meltwater to the 361 ice front (e.g. by the Antarctic Coastal Current Flexas et al., 2022). The ability for our 362 idealized model to capture key features of observed Amundsen Sea mCDW variability 363 despite these simplifications speaks to the importance of ice front thermocline stratifi-364 cation strength to ocean-driven glacial melt variability on decadal timescales. 365

This work builds on regional modeling (St-Laurent et al., 2015; Caillet et al., 2022; 366 Bett et al., 2020; Naughten et al., 2022), idealized modeling (Petty et al., 2013; Silvano 367 et al., 2018), and observational evidence (Webber et al., 2017) indicating coastal buoy-368 ancy forcing can modulate ocean heat availability at West Antarctic ice shelves. At the 369 Pine Island Ice Front, anomalously strong coastal surface buoyancy fluxes can explain 370 the cool period observed from 2011 to 2013 in regional models and observations(St-Laurent 371 et al., 2015; Webber et al., 2017). At longer timescales, simulated transitions between 372 cool and warm Amundsen shelf states closely track surface buoyancy forcing changes (Caillet 373 et al., 2022). For the Dotson Ice Shelf, Caillet et al. (2022) simulate persistent low or 374 high melt rates in response to strong negative and positive perturbations to surface buoy-375 ancy forcing, respectively, and large decadal variations in melt rates for intermediate sur-376 face buoyancy forcing perturbations, consistent with the bistability mechanism presented 377 here (see Figure 5 in Caillet et al., 2022). Idealized models have primarily been used to 378 assess the Amundsen Sea mean state, with bulk mixed layer models indicating a lead-379 ing role for buoyancy fluxes in setting the shallow winter mixed layer depths typical of 380 the West Antarctic shelf relative to other Antarctic regions (Petty et al., 2013; Silvano 381 et al., 2018). Whilst Amundsen Sea variability at interannual and longer timescales has 382 not been targeted with idealized models, there is precedent elsewhere. For example, con-383 ceptual models have been used to interrogate bistable low and high melt states of the 384 Filchner-Ronne Ice Shelf enabled by coastal buoyancy feedbacks analogous to those iden-385 tified here (Hazel & Stewart, 2020). Our approach incorporates the consideration of buoy-386 ancy central to these results into a "thermocline model" framework based on closing wa-387 termass transformation pathways, a framework originally applied to the global overturn-388 ing circulation (e.g. Gnanadesikan, 1999; Marshall & Zanna, 2014; Thompson et al., 2019). 389

We take away two important lessons for future studies of warm West Antarctic shelf seas. Firstly, the dynamics that govern the exposure of ice shelves to ocean heat must account not only for variability in mCDW supply, but also mCDW consumption or transformation, with the latter having received significantly less attention. Secondly, we cannot neglect the dynamical effects of meltwater in a salinity stratified system; ongoing observational monitoring and accurate simulation of ice front stratification strength shouldbe prioritized.

#### <sup>397</sup> Open Research Section

Data and code required to reproduce all figures in the main text and Supporting Information provided at https://doi.org/10.5281/zenodo.7987113. A binder environment (see https://mybinder.org/ for details) has been constructed so that readers can open, edit, and execute all code from a browser (click "launch binder" button on the GitHub repository home page linked to the listed doi). Editing within the binder environment will not alter the original file, so readers should feel free to manipulate provided code.

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# Supporting Information for "Coastal polynyas enable transitions between high and low West Antarctic ice shelf melt rates"

Ruth Moorman<sup>1</sup>, Andrew F. Thompson<sup>1</sup>, and Earle A. Wilson<sup>2</sup>

<sup>1</sup>Environmental Science and Engineering, California Institute of Technology, Pasadena, California, USA

 $^2\mathrm{Department}$  of Earth System Science, Stanford University, Stanford, California, USA

## Contents of this file

- 1. Text S1 to S3  $\,$
- 2. Figures S1 to S6
- 3. Table S1

Introduction The SI includes a summary of techniques used to analyze the historical observational data sets employed in this study (S1), the methods for deriving model parameters and forcing fields from the WAIS 1080 numerical output (S2, Figures S1-3), a brief summary of how the idealized model responds to parameter perturbations (S3, Figure S4), and two additional transiently forced simulations not included in the main text (Figures S5-6). We refer to Jupyter Notebooks, provided in linked GitHub repository (https://github.com/ruth-moorman/Moorman-et-al-GRL-submission-2023) accompanied by a binder environment so that readers can open, edit, and execute all code from a browser.

## Text S1.

Here we provide details of the  $\gamma$  and  $AD_{mCDW}$  metrics presented in Figure 1d.

Following Simpson, Allen, and Morris (1978) and Venables and Meredith (2014), we define the stratification metric  $\gamma$  as the potential energy of the water column relative to the potential energy of a mixed water column. This choice is made in lieu of buoyancy frequency metrics, which are found to be sensitive to an arbitrary choice of thermocline depth. The diagnosed potential energy is effectively the energy input required to homogenize the water column to a given depth. Functionally, this metric  $\gamma$  is defined as

$$\gamma = \int_{h_2}^{h_1} (\rho - \langle \rho \rangle) gz \, dz \quad \text{where} \quad \langle \rho \rangle = \frac{1}{h_2 - h_1} \int_{h_2}^{h_1} \rho \, dz. \tag{1}$$

We take  $h_1$  to be a near surface depth (5 m) and  $h_2$  to be a depth sufficiently deep to be typically located below the thermocline yet shallow enough so that the deepest measurement in at least half of the 49 profiles used in this study exceed  $h_2$  (here 750 m). For a vertically mixed column,  $\gamma = 0$  with  $\gamma$  growing increasingly positive for increasingly stable stratification. Only those profiles with a maximum depth exceeding  $h_2$  are used in the calculation of  $\gamma$ , since the value of the integrated metric is artificially reduced by missing values. At least 2 profiles meet this criterion for each cruise year and the choice  $h_2 = 750$  m. The temporal pattern is not sensitive to reasonable perturbations (up to and greater than 100 m) of  $h_1$  and  $h_2$ . Interactive code used to compute this metric and test its sensitivity to  $h_1$  and  $h_2$  are available in the notebook "Figure1.ipynb" of the provider jupyter binder environment and GitHub repository.

Details of the metric used for the depth of the mCDW layer,  $AD_{mCDW}$ , are provided in Kim et al. (2021) and the "Figure1.ipynb" notebook. The method simultaneously solves

for volume fractions of mCDW, WW, and glacial meltwater, comprising each point of a vertical profile of temperature, salinity, and dissolved oxygen given end member characteristics of the three water masses. Volume fractions are then vertically integrated and  $AD_{mCDW}$  is taken as the depth of the profile minus the integrated mCDW volume fraction. Thermocline depths calculated by this method are shallow biased relative to a visual identification of thermoclines identified from temperature profiles, as WW is modified by mCDW. However, the temporal pattern agrees with simpler methods based on isotherm depths. We choose to present  $AD_{mCDW}$  since isotherm based metrics were found to be sensitive to the choice of isotherm. All code and additional details (including methods of determining end member water mass characteristics) are available in "Figure1.ipynb" of the provided jupyter binder environment.

## Text S2.

Here we describe how estimates of  $\alpha$ ,  $F_{surf}$ , and  $\Psi_{in}$  are diagnosed from WAIS 1080 output. Further details and interactive code generating these values and associated figures may be found in "Supplementary\_2.ipynb".

## Ice-shelf melt coefficient: $\alpha$

In our idealized model, we parameterize the 2D transport of buoyancy (units  $m^3 s^{-3}$ ) from the ice shelf cavity into the upper, thermocline box due to ice shelf melt as

$$h(vb)_{\rm in} = \alpha \, h_{\rm mCDW} \, \Delta b_{\rm melt}. \tag{2}$$

Using WAIS 1080 output, this 2D transport of buoyancy into the ocean thermocline box can be diagnosed as the total buoyancy transport to the ocean from basal ice shelf melt

X - 4

 $(m^4 s^{-3})$  divided by the idealized model width (m),

$$h(vb)_{\rm in} = \frac{1}{L_x} \int_A F_{\rm iceshelf} \, dA. \tag{3}$$

Here  $L_x$  (m) is the model zonal extent,  $F_{\text{iceshelf}}$  (m<sup>2</sup> s<sup>-3</sup>) is the simulated buoyancy flux from the ice shelf to the ocean within the ice shelf cavity at each horizontal grid point on the ice shelf draft, and A is horizontal area of the ice shelf cavity (white box in Figure S1). Combining Ficeshelf1 and Ficeshelf2, we estimate the value of the parameter  $\alpha$  as,

$$\alpha = \frac{1}{L_x \, h_{\rm mCDW} \, \Delta b_{\rm melt}} \int_A F_{\rm iceshelf} \, dA \tag{4}$$

where  $L_x = 55$  km and  $\Delta b_{\text{melt}} = 6.7 \times 10^{-3}$  m s<sup>-2</sup> (as described in the main text), while  $h_{\text{mCDW}}$  and the integrated buoyancy flux term are diagnosed from WAIS 1080.

The buoyancy flux  $F_{\text{iceshelf}}$  (m<sup>2</sup> s<sup>-3</sup>) is defined functionally as (positive values increase the ocean buoyancy),

$$F_{\text{iceshelf}} = \frac{g\alpha_0}{\rho_{surf}c_p} Q_{H,\text{ice}} - g\beta_0 S_{surf} Q_{FW,\text{ice}}$$
(5)

where  $g = 9.8 \text{ m s}^{-2}$  (gravity),  $\alpha_0 = 4.8 \times 10^{-5} \text{ K}^{-1}$  (thermal expansion coefficient),  $\beta_0 = 7.8 \times 10^{-4}$  (haline contraction coefficient),  $c_p = 3992 \text{ J kg}^{-1} \text{ K}^{-1}$  (specific heat capacity of seawater),  $\rho_{surf} = 1026 \text{ kg m}^{-3}$  (approximate surface cell density),  $S_{surf} = 34$ (approximate surface cell salinity),  $Q_{H,\text{ice}} =$  net heat flux from the ice (positive increases  $\theta$ ) (WAIS 1080 output), and  $Q_{FW,\text{ice}} =$  net freshwater flux from the ice (positive increases S) (WAIS 1080 output). Figure S1 shows time mean WAIS 1080  $F_{\text{iceshelf}}$  values for ice shelves in the Amundsen Sea Embayment and delineates (white box) the Dotson Ice Shelf horizontal region integrated over in alpha. Whilst the adjacent Dotson and Crosson ice shelves are connected in WAIS 1080, there is negligible flow between them across the

eastern boundary of the delineated region. The mCDW layer thickness,  $h_{\rm mCDW}$  (m), is approximated as the thickness below the 0°C thermocline, computed from temperature spatially averaged over the ice front region (red box in Figure S1). Figure S2 shows  $h_{\rm mCDW}$ directly diagnosed from WAIS 1080 and approximated from the ice shelf buoyancy input via alpha with  $\alpha = 0.0021$  (mean diagnosed value).

## Polynya surface buoyancy flux: $F_{surf}$

The ocean surface buoyancy flux,  $F_{\text{surf}}$  (m<sup>2</sup> s<sup>-3</sup>), is defined functionally as (positive values increase the buoyancy of the surface cell),

$$F_{surf} = \frac{g\alpha_0}{\rho_{surf}c_p} Q_{H,\text{oce}} - g\beta_0 S_{surf} Q_{FW,\text{oce}},\tag{6}$$

where  $Q_{H,\text{oce}} =$  net surface heat flux (positive increases  $\theta$ ) (WAIS 1080 output),  $Q_{FW,\text{oce}} =$ net surface freshwater flux (positive reduces S) (WAIS 1080 output), and all other parameters are as in Ficeshelf. To generate monthly and climatological mean timeseries of  $F_{\text{surf}}$ , which provides forcing to the idealized model (Figure S3),  $F_{\text{surf}}$  is averaged over a 55 km × 50 km region at the ice front where negative  $F_{\text{surf}}$  values are concentrated. This region is delineated in Figure S2 (red box). Our results are not qualitatively sensitive to the exact size of this region, and these values are simply intended to guide the magnitude of forcing terms.

In the main text we refer to  $F_{\text{surf}}$  as the surface buoyancy flux associated with net sea-ice formation. As defined in Fsurf,  $F_{\text{surf}}$  is the total surface buoyancy flux, not purely the buoyancy flux associated with sea-ice formation and melt. However,  $F_{\text{surf}}$  is tightly anti-correlated ( $R^2 = 0.96, p = 10^{-240}$ , Figure S3) with monthly net sea-ice formation in WAIS 1080 and so, for clarity, we refer to  $F_{\text{surf}}$  as reflecting sea-ice formation.

## Cross-shelf volume transport: $\Psi_{\rm in}$

 $\Psi_{\rm in}$  (units m<sup>2</sup> s<sup>-1</sup>) represents the net baroclinic shoreward transport of warm mCDW into the coastal region at the Dotson Ice Shelf front and the balanced offshore transport of cool thermocline waters. This term is estimated via a preliminary analysis of the Dotson Ice Front overturning circulation as simulated in WAIS 1080. We bin monthly mean volume transports across the edges of the ice front region (red box in Figure S1), and the corresponding monthly mean ocean temperature values, into surface referenced potential density ( $\sigma_0$ ) bins using monthly mean  $\sigma_0$  values. Density-binned volume transports into the ice front domain are then summed along the bounds of the box, whilst densitybinned temperatures are averaged along the bounds of the box. When cumulatively integrated through  $\sigma_0$  space, binned transports reveal a net shoreward flow of dense waters (interpreted as mCDW) and a net offshore flow of lighter waters (WW, glacial meltwater, and other surface waters), consistent with the assumptions of the model.

## Text S2.

### Analytical steady state solutions to the ice front overturning model

Analytical steady state solutions for the thickness of the thermocline layer and the thermocline stratification strengh in the ice front overturning model may be derived for known values of  $\kappa_{\rm P}$ ,

$$h_{\text{steady}} = \left(\frac{H}{2} - \frac{\Psi_{\text{in}}}{2\alpha}\right) + \sqrt{\left(\frac{H}{2} - \frac{\Psi_{\text{in}}}{2\alpha}\right)^2 + \frac{\kappa_{\text{P}}L}{\alpha}} \tag{7}$$

$$\Delta b_{\text{steady}} = \frac{\left(h_{\text{steady}} - \frac{\Psi_{\text{in}}}{\alpha}\right) \left(\frac{F_{\text{surf}}L}{2\Psi_{\text{in}}} + \Delta b_{\text{melt}}\right)}{\frac{\kappa_{\text{P}}L}{2\Psi_{\text{in}}} + \frac{H}{2} - \frac{\Psi_{\text{in}}}{\alpha}} - \Delta b_{\text{melt}}.$$
(8)

Interpretation of these solutions is complicated by the  $\Delta b$  dependence of  $\kappa_{\rm P}$  (see equation (10) of the main text). To understand (7) and (8) in light of this dependence, consider the extreme case of taking  $\phi \to \infty$  in equation (10) of the main text, which reverts  $\kappa_{\rm P}$  to a step function transitioning from  $\kappa_{\rm diff}$  to  $\kappa_{\rm conv}$  when  $\Delta b$  drops below  $\Delta b_{\rm crit}$ . In this case, (7) and (8) suggest two steady states for a given system  $(H, L, \alpha, \Delta b_{\text{melt}})$  and forcing  $(\Psi_{\rm in}, F_{\rm surf})$ ; a diffusive steady state with  $\kappa_{\rm P} = \kappa_{\rm diff}$  and a convective steady states with  $\kappa_{\rm P} = \kappa_{\rm conv}$ . In some regions of the forcing space, one of these  $\kappa_{\rm P}$  values present a contradiction. Either setting  $\kappa_{\rm P} = \kappa_{\rm diff}$  will result in  $\Delta b_{\rm steady} < \Delta b_{\rm crit}$  (indicating the diffusive solution is not sustained, white regions in Figure 3b,c of the main text) or setting  $\kappa_{\rm P} = \kappa_{\rm conv}$  results in  $\Delta b_{\rm steady} > \Delta b_{\rm crit}$  (indicating the convective solution is not sustained, white regions in Figure 3d,e of the main text). Where neither  $\kappa_{\rm P}$  value returns a contradiction, bistability is possible (region bound by yellow contour in Figure 3b-e of the main text). Smoothing the transition between  $\kappa_{\text{diff}}$  and  $\kappa_{\text{conv}}$ , by decreasing the value of  $\phi$ , primarily acts to constrict the region over which bistability is possible. Numerical solutions presented in Figure 3 of the main text agree with analytical solutions (central panels of Figure S4), though they differ in that the numerical bistable region is contracted relative to the analytical bistable region, as anticipated for nonzero values of  $\phi$ .

### Summary of parameter sensitivity

These analytical solutions provide a fast and convenient means of exploring the sensitivity of model output to parameter choices. "Supplementary\_3.ipynb" in the provided jupyter binder environment generates analytical versions of Figure 3 (main text) for the full suite of possible cases wherein each model parameter is both positively and negatively perturbed. Figure S4 illustrates the model steady state sensitivity to changes in  $\alpha$  as an

example; all other cases are available in the provided notebook. Table S1 summarizes the effects of varying each parameter, both on the analytical steady state solutions (explored in the jupyter notebok) and on transiently forced simulations (not shown). The positive feedbacks and related bistablity underpinning our main results depend on their being a nonlinearity to the dependence of vertical mixing on stratification strength. Within the confines of our choice to represent vertical mixing as a smoothed step function of stratification strength, we find that parameter perturbations can change the absolute magnitude of the thermocline depths associated with diffusive and convective conditions, can alter the length of the simulated lag between thermocline depth and stratification strength changes during regime transitions, and can change the strength of forcing perturbation required to trigger a regime transition. Small perturbations to the parameter values used in this study do not alter our key results, however, removing the jump in vertical mixing strength at the onset of convection does remove the described behavior.

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Figure S1. Time mean  $F_{\text{iceshelf}}$  and  $F_{\text{surf}}$  values from WAIS 1080 diagnosed according to equations Ficeshelf and Fsurf.  $F_{\text{iceshelf}}$  is defined for regions with positive ice shelf draft and  $F_{\text{surf}}$ is defined for regions of open ocean (zero ice shelf draft). The grounded ice zone is delineated with grey shading. Grey contours in the open ocean indicate bathymetry (500 m, 1000 m, 4000 m). The white dashed box indicates the region over which  $F_{\text{iceshelf}}$  is computed (the Dotson Ice Shelf) and the red dashed box indicates the region over which  $F_{\text{surf}}$ ,  $\Psi_{\text{in}}$ , and  $h_{\text{mCDW}}$  are computed (the Dotson Ice Front).



Figure S2. Timeseries of  $h_{\rm mCDW}$  defined as either the thickness below the 0°C isotherm determined from monthly WAIS 1080 temperature output spatially averaged over the ice front region (black), or a linear function of spatially integrated Dotson Ice Shelf buoyancy fluxes (see equation Ficeshelf) with  $\alpha$  set to 0.0021 (blue). The first three years (translucent lines) show worse agreement between the direct and parameterized  $h_{\rm mCDW}$  values, possibly a result of model spinup.



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Figure S3. Monthly mean values (grey) and climatological mean monthly values (blue) of  $F_{\text{surf}}$  (upper) and  $\Psi_{\text{in}}$  (lower) as diagnosed from WAIS 1080. (right) Correlation between  $F_{\text{surf}}$  and monthly net sea-ice formation rates in the Dotson ice front region.



Figure S4. Illustration of the sensitivity of analytical steady-state solutions to perturbations of the parameter  $\alpha$ . Each column contains panels equivalent to Figure 3b-e of the main text, except analytical solutions rather than numerically equilibrated solutions are shown. The central column shows analytical steady-state solutions to our model when the default (main text) parameter values are used (these panels may be directly compared to Figure 3b-e). Columns to the left and right show analytical steady-state solutions when  $\alpha$  is reduced and increased, respectively.



Figure S5. Thermocline depth changes and stratification strength changes simulated in response to monthly (as opposed to climatological) WAIS 1080 forcing. The same forcing is applied to the model initialized in warm conditions (red) and cold conditions (blue). Crosses, circles, solid lines, and dashed lines are as in Figure S6. Black horizontal line is  $\Delta b_{crit}$ , stratification strength does not drop below this value following initialization.



Figure S6. Similar to Figure 4d for the main text. In Figure 4d, winter (May-September)  $\Psi_{in}$  values are shifted downwards for two consecutive years. Here the full annual pattern of  $\Psi_{in}$  is downshifted (by the same amount as in Figure 4d, the maximum offset that ensures  $\Psi_{in} > 0$ ) for 5 consecutive years. Whilst this forcing pattern generates large decadal scale fluctuations in the thermocline depth, it does not trigger regime change as the accompanying stratification changes do not promote the onset of convection.

**Table S1.**Dominant effects of increasing the magnitude of a parameter on the analyticalsteady state solutions to the ice front overturning model and the implied effect on transiently

forced solutions. Effects of decreasing parameter magnitudes are the converse in all cases.

Parameter	Effect (analytical steady state)	Implied Effect (transient)
	$\alpha$ dictates the sensitivity of meltwater generation to the thickness of the	Stronger perturbations are needed to
	ice front mCDW layer. Increasing $\alpha$ acts to:	force diffusive to convective transitions
	- strengthen the ice front stratification associated with a given thermocline	and weaker perturbations are sufficient
α	depth	to force convective to diffusive transi-
	- deepen the steady state thermocline associated with a given mCDW	tions. Both convective and diffusive
	inflow	solutions are associated with deeper
	- shift the bistable region towards negative $F_{\rm surf}$ values (see Figure S3.1)	thermoclines.
$\Delta b_{\rm melt}$	$\Delta b_{\rm melt}$ similarly dictates the sensitivity of ice front stratification strength	Same as $\alpha$ , except does not effect end
	to basal ice melt. It has a similar effect to $\alpha$ except it only influences	member thermocline depths
	steady state stratification strengths, not steady state thermocline depths.	
	$\kappa_{\text{diff}}$ only effects diffusive end member solutions and increasing it acts to:	
	- deepen the steady state thermocline associated with diffusive end mem-	Diffusive solutions are associated with
	bers	deeper thermoclines generally and
$\kappa_{ m diff}$	- contract the bistable region from below such that diffusive solutions	transitions to convective solutions are possible with weaker perturbations.
	are not supported for a wider range of negative $F_{\rm surf}$ values (when	
	$\kappa_{\rm diff}~=~\kappa_{\rm conv}$ bistability disappears altogether as the end member so-	
	lutions converge)	
	$\kappa_{\rm conv}$ only effects convective end member solutions and increasing it acts	
	to:	
	- deepen the steady state thermocline associated with convective end	Convective solutions are associated
ĸ	members	with deeper thermoclines generally
n <sub>conv</sub>	- expand the bistable region from above such that convective solutions are	and transitions to diffusive solutions
	supported for a wider range of positive $F_{\rm surf}$ values (when $\kappa_{\rm diff}$ and $\kappa_{\rm conv}$	require stronger perturbations.
	become more similar bistability contracts, when $\kappa_{\rm diff}$ and $\kappa_{\rm conv}$ become	
	more different bistability expands)	
		Stronger perturbations are needed to
	Simply changes the stratification strength at which convection onsets. Increasing $\Delta b_{\rm crit}$ will shift the bistable region towards positive $F_{\rm surf}$ values.	force convective to diffusive transitions
$\Delta b_{ m crit}$		and weaker perturbations are sufficient
		to force diffusive to convective transi-
		tions.
	Increasing $\phi$ makes $\kappa_{\rm P}$ more step-like, therefore bringing the numerical	
$\phi^a$	model behavior closer to the analytical solution. Decreasing $\phi,$ by con-	Transitions will require greater pertur-
	trast, smooths out $\kappa_{\rm P}.$ This renders more solutions with steady state	bations when $\phi$ is larger
	stratification strength close to the critical buoyancy unstable, and thus	battons when $\psi$ is larger.

 $^{a}$  analytical solutions are independent of  $\phi$ , its effect has been assessed using numerical solutions

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