# A generalized relationship linking water balance and vegetation carbon uptake across site-to-regional scales

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#### Abstract

The linear relationship between gross primary productivity (GPP) and evapotranspiration (ET), evidenced by site-scale observations, is well recognized as an indicator of the close interactions between carbon and hydrologic processes in terrestrial ecosystems. However, it is not clear whether this relationship holds at the catchment scale, and if so, what are the controlling factors of its slope and intercept. This study proposes and examines a generalized GPP-ET relationship at 380 near-natural catchments across various climatic and landscape conditions in the contiguous U.S., based on monthly remote sensing-based GPP data, vegetation phenology, and several hydrometeorological variables. We demonstrate the validity of this GPP-ET relationship at the catchment scale, with Pearson's r [?] 0.6 for 97% of the 380 catchments. Furthermore, we propose a regionalization strategy for estimating the slope and intercept of the generalized GPP-ET relationship at the catchment scale by linking the parameter values a priori with hydrometeorological data. We validate the monthly GPP predicted from the relationship and regionalized parameters against remote-sensing based GPP product, yielding Kling-Gupta Efficient (KGE) values [?] 0.5 for 92% of the catchments. Finally, we verify the relationship and its parameter regionalization at 35 AmeriFlux sites with KGE [?] 0.5 for 25 sites, demonstrating that the new relationship is transferable across the site, catchment, and regional scales. The relationship will be valuable for diagnosing coupled water-carbon simulations in land surface and Earth system models and constraining remote-sensing based estimation of monthly ET.

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# A generalized relationship linking water balance and vegetation carbon uptake across site-to-regional scales

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# 19 Key Points:

- A generalized relationship between monthly water balance and vegetation carbon uptake
   is evaluated across the U.S. catchments
- A parameter regionalization strategy is proposed based on the linkages between
   environmental factors and the relationship's parameters
- The relationship and its parameterization are validated across the site, catchment, and regional scales
- 26

## 27 Abstract

28 The linear relationship between gross primary productivity (GPP) and evapotranspiration (ET), 29 evidenced by site-scale observations, is well recognized as an indicator of the close interactions 30 between carbon and hydrologic processes in terrestrial ecosystems. However, it is not clear 31 whether this relationship holds at the catchment scale, and if so, what are the controlling factors 32 of its slope and intercept. This study proposes and examines a generalized GPP-ET relationship 33 at 380 near-natural catchments across various climatic and landscape conditions in the 34 contiguous U.S., based on monthly remote sensing-based GPP data, vegetation phenology, and several hydrometeorological variables. We demonstrate the validity of this GPP-ET relationship 35 at the catchment scale, with Pearson's  $r \ge 0.6$  for 97% of the 380 catchments. Furthermore, we 36 37 propose a regionalization strategy for estimating the slope and intercept of the generalized GPP-38 ET relationship at the catchment scale by linking the parameter values a priori with 39 hydrometeorological data. We validate the monthly GPP predicted from the relationship and 40 regionalized parameters against remote-sensing based GPP product, yielding Kling-Gupta 41 Efficient (KGE) values  $\geq 0.5$  for 92% of the catchments. Finally, we verify the relationship and 42 its parameter regionalization at 35 AmeriFlux sites with KGE  $\geq 0.5$  for 25 sites, demonstrating 43 that the new relationship is transferable across the site, catchment, and regional scales. The 44 relationship will be valuable for diagnosing coupled water-carbon simulations in land surface 45 and Earth system models and constraining remote-sensing based estimation of monthly ET.

#### 1. Introduction 46

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48 The linear relationship between gross primary productivity (GPP) and evapotranspiration (ET) 49 has been studied by ecologists over the past decades. The relationship is considered a 50 manifestation of the tight coupling between carbon and water fluxes via both biotic and abiotic 51 processes and their interactions (Baldocchi, 1994; Baldocchi et al., 2001; Beer et al., 2007, 2009; 52 Gentine et al., 2019; Law et al., 2002; Niu et al., 2011; Ponton et al., 2006; Smallman & Williams, 2019; Y. Yang et al., 2013; Zhou et al., 2014). Understanding this relationship 53 54 provides valuable information on global carbon and water balance, vegetation growth, ecosystem 55 responses to environmental changes, and the trade-off between photosynthetic carbon assimilation and concomitant transpiration (M. Huang et al., 2015; Ito & Inatomi, 2012; Keenan 56 et al., 2013; Novick et al., 2016; Van Der Sleen et al., 2015). As such, in recent decades, the 57 58 coupling between these two processes has been recognized as essential for assessing ecosystem-59 level response to climate variability (Baldocchi, 1994; Beer et al., 2009; Brümmer et al., 2012; 60 Hatfield & Dold, 2019; Kuglitsch et al., 2008; Niu et al., 2011; Ponton et al., 2006; Xiao et al., 61 2013). Still, a better quantification of the GPP-ET relationship has been called upon to improve 62 our understanding of the consequences of the projected future changes in temperature and precipitation regimes on ecosystem carbon and water balance (Krinner et al., 2014; Niu et al., 63 64 2011; Zhou et al., 2017).

Hydrologists view ET as a critical component of water balance at the catchment scale (Abeshu & 65

66 Li, 2021; Fu, 1981; Greve et al., 2015, 2016; Ol'dekop, 1911; Pike, 1964; Sivapalan et al., 2011; Troch et al., 2009; Turc, 1954; Wang & Tang, 2014; L. Zhang et al., 2001, 2004). For instance, 67 68 the Budyko curve describes the evaporative index, a ratio of long-term mean actual ET over 69 long-term mean precipitation, as a function of climate regimes in terms of aridity index, a ratio of

70 long-term mean potential ET over long-term mean precipitation (Budyko, 1974; Chen & 71 Sivapalan, 2020; Choudhury, 1999; Li et al., 2014; Li & Sivapalan, 2014; Meira Neto et al., 72 2020; H. Yang et al., 2008; Yao & Wang, 2022; Ye et al., 2015; L. Zhang et al., 2001, 2004). 73 Parameters of the Budyko-type formulas are closely related to vegetation dynamics at the 74 catchment scale (Donohue et al., 2007, 2010; Wang & Tang, 2014; L. Zhang et al., 2001; S. 75 Zhang et al., 2016, 2018). The Horton Index, defined as the ratio of ET over total wetting (water 76 available for vaporization), has even closer linkages with a few phenological features (Abeshu & 77 Li, 2021; Brooks et al., 2011; Horton, 1933; Sivapalan et al., 2011; Tang & Wang, 2017; Troch 78 et al., 2009; Voepel et al., 2011). It is thus a step further in connecting catchment-scale water 79 balance and vegetation dynamics. However, few of these hydrologic studies focus on the GPP-80 ET relationship within the context of catchment water balance. This motivates the first objective 81 of this study to examine the GPP-ET relationship at the catchment scale across various climate

82 and vegetation regimes.

83 Ecologists have established the coupled relationship between photosynthetic carbon assimilation 84 and transpiration at the leaf scale (Bacon, 2004; Farguhar et al., 1989; Lloyd & Farguhar, 1994; 85 Peters et al., 2018; Seibt et al., 2008) and between GPP and ET at the ecosystem scale (Baldocchi, 1994; Beer et al., 2009; Jiang et al., 2020; Law et al., 2002; L. Yu et al., 2022; Zhou 86 87 et al., 2014, 2017) from observations. Equation (1) describes the generic GPP-ET relationship at 88 the ecosystem scale. The slope of the relationship,  $\omega$ , is referred to as water use efficiency and is 89 often estimated as the ratio of long-term mean GPP to long-term mean ET at the ecosystem scale 90 (Beer et al., 2009). When used for estimating GPP or ET, the equation is assumed to have a zero-91 intercept, i.e., GPP is negligible when ET approaches zero and vice versa (Beer et al., 2007, 92 2010; Y. Yang et al., 2013).

$$GPP = \omega ET$$

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94 However, it has been argued that an additional intercept term is needed for the ecosystem-scale 95 GPP-ET relationship (Boese et al., 2017). In other words, the intercept term is not always 96 negligible. As illustrated in Fig. 1, the zero-intercept assumption is not valid in at least three 97 cases: 1) at cropland sites after harvest GPP is zero, but ET may not be negligible due to surface 98 evaporation (see Nguyen & Choi, 2022); in evergreen forest-dominated ecosystems, there is a 99 certain level of carbon assimilation even during the winter season (see Beer et al., 2007; G. Yu et 100 al., 2008); in wetland or broadleaf forest-dominated ecosystems, significant evaporation occurs during the dormant season (see Baldocchi & Ryu, 2011). Over the past decades, many studies 101 102 provided a quantitative understanding of the biotic and abiotic implications of the slope and its 103 environmental controlling factors across vegetation types and spatial scales (Beer et al., 2009, 104 2010; Yulong Zhang et al., 2016; Zhou et al., 2014). However, there remains a lack of direct 105 quantitative assessments of the slope and its linkages to climatic and environmental factors with 106 the inclusion of the intercept term (Boese et al., 2017), let alone an understanding and assessment 107 of the intercept term. Among the very few exceptions is a study by Boese et al. (2017) at the site 108 scale, where they introduced various intercept options to Eqn. 1 to predict ET based on GPP at 109 over a hundred eddy covariance sites. However, their formulation has several limitations, such as 110 using rain-free periods only for parameter estimation and excluding the other environmental 111 conditions that could influence the stomatal opening of plants. Furthermore, the intercept term of 112 their best-performing model is entirely independent of any variable reflecting vegetation activity. 113 This motivates our second objective to derive quantitative linkages between the slope and 114 intercept of the GPP-ET relationship and climatic and environmental factors.

115 The linear GPP-ET relationship has been utilized to evaluate simulations by large-scale land surface or earth system models, for instance, regarding the coupling between water and carbon 116 117 fluxes at the regional or global scales (M. Huang et al., 2016; Ito & Inatomi, 2012; Sun et al., 118 2016; S. Yang et al., 2020, 2021; Z. Yu et al., 2017). However, most global GPP simulations 119 suffer from significant biases and uncertainties (Yahai Zhang & Ye, 2021, 2022). A recent study 120 evaluated forty-four global GPP products (nearly thirty were model-based outputs, and the rest 121 were observation-based) and found significant inconsistencies among model-based products for 122 some regions, seasons, and vegetation types (Yahai Zhang & Ye, 2021). A chief reason behind 123 these GPP simulation biases and inconsistencies is a mismatch of spatial scales, i.e., between the 124 site scale (where process understanding has been gained from local observations) and the 125 regional or global scales (where the models are developed and applied) (Xie et al., 2023). In the 126 land surface or earth system models, the global domain is discretized into grids with typical grid sizes ranging from tens to thousands of km<sup>2</sup>, far larger than the site scale, which is on the order 127 of  $< 1 \text{km}^2$  (Pastorello et al., 2020). Such a scale mismatch often leads to large model structural 128 129 uncertainty, e.g., oversimplification or poor parameterization of sub-grid heterogeneity, which is 130 non-trivial at the typical spatial resolutions that land surface or earth system models are applied (Bonan et al., 2018; Li et al., 2011, 2013; Smallman et al., 2013; Smallman & Williams, 2019). 131 132 Therefore, our third objective is to verify whether the new understanding of the GPP-ET 133 relationship gained at the catchment scale is transferable to the site scale. If so, it is possible that 134 such an understanding is also applicable at the global scale. Note that site scale refers to the scale at which individual monitoring stations are located. Catchment scale, on the other hand, refers to 135 136 the scale at which a larger area is studied as a single hydrological system.

To advance the three objectives discussed above, three specific scientific questions are used to guide our analysis at the catchment and site scales using observations to address: 1) Is the GPP-

139 ET linear relationship valid at the catchment scale? 2) If so, can we establish quantitative

- 140 linkages between environmental factors and the slope and intercept of this linear relationship at
- the catchment scale? 3) How are the new quantitative understandings transferable from the 141
- catchment scale to the site and regional scales? The rest of this paper is organized as follows: 142
- 143 Section 2 introduces the data. Section 3 describes the methods. Section 4 presents the results.
- 144 Section 5 summarizes the conclusions.

#### 2. Data 145

146 We use the catchment-scale data directly from the Catchment Attributes and Meteorology for 147 Large-Sample Studies (CAMELS) dataset (Addor et al., 2017; Newman et al., 2015). CAMELS 148 provides daily hydrometeorological observations, such as precipitation, vapor pressure, 149 shortwave radiation, minimum air temperature, maximum air temperature, and streamflow, for 150 over three decades (1982 to 2014). It also includes daily ET simulations in the same period from 151 the integrated Snow-17/SAC-SMA model (Addor et al., 2017; Burnash, 1995). Static catchment 152 attributes, including dominant vegetation type (and its areal fraction in a catchment) and Green 153 Vegetation Fraction (GVF) difference, are also available from CAMELS. GVF represents the 154 fraction of a catchment area covered by green vegetation. The green and non-green portions are 155 assumed to be areas that do or do not transpire, respectively. GVF difference is the difference 156 between the maximum and minimum monthly mean GVF. It represents the seasonal dynamics in

157 the catchment area contributing to the water balance through transpiration.

158 We also use the GPP data retrieved from Landsat GPP products over the contiguous United

159 States (CONUS) with a spatial resolution of 30-meter and a temporal resolution of 16-day

- 160 (Robinson et al., 2018). We choose Landsat GPP over the other satellite-based products because 161 it has a 36-year observational period (1991-2021), which overlaps with the CAMELS dataset for
- 162 29 years.

163 Figure 2 summarizes the data used in this study. Harmonization and processing of the data from 164 various sources are detailed in the following seven steps:

- 1) The CAMELS dataset provides an integrated Snow-17/SAC-SMA model output for ten 165 166 optimal parameter sets. We collect the daily ET produced with each parameter set and compute the daily ensemble mean  $(ET_{ensemble})$ . 167
- 2) The annual ensemble mean ET ( $\overline{ET}_{ensemble}$ ) is then validated against the observed annual 168 mean ET ( $\overline{ET}_{obs}$ ).  $\overline{ET}_{obs}$  is calculated as annual mean precipitation minus annual mean runoff depth (estimated from the observed streamflow and catchment area). We only 169 170 keep those CAMELS catchments satisfying  $\frac{|\overline{ET}_{obs} - \overline{ET}_{ensemble}|}{\overline{ET}_{obs}} \times 100\% \le 10\%$  for further 171 172
- analysis.
- 173 3) For catchments selected in Step 2, we remap the gridded Landsat GPP to each catchment 174 and then convert the 16-day to monthly time series.
- 175 4) We identify 1986-2010 as the study period during which all hydroclimatic variables and 176 Landsat GPP data are continuously available (i.e., no missing data) for most catchments 177 selected in Step 2. After filtering out catchments with missing data, we obtain 392 178 catchments.
- 179 5) We define the dominant vegetation cover for each catchment as the single vegetation type 180 covering at least 50% of the drainage area. Hence, we exclude those catchments that do 181 not have any vegetation type covering no less than 50% of the catchment area. We finally obtained 380 catchments with drainage areas ranging from 6.25 to 25,818 km<sup>2</sup> (Fig. 3). 182
- 183 6) For convenience, we classify the 380 catchments into six groups based on their dominant 184 vegetation type, resulting in three forested and three non-forested catchment groups

- 185 (Table 1). Forested catchments include Deciduous Broadleaf (DBF) (89), Evergreen 186 Forest (Needle leaf + Broadleaf) (EF) (25), and Mixed Forests (MF) (50) dominated 187 catchments. Non-forested catchments include Croplands plus Croplands/Natural 188 Vegetation Mosaic (CL/NVM) (111), Grasslands (GL) (46), and a combination of 189 Savannas, Woody Savannas, and Open/Closed Shrublands, hereafter WSSL catchments 190 (59).
- 191
  7) We calculate some climatic variables based on the existing CAMELS data. For instance,
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Figure 3 shows the spatial maps (for the 380 catchments) of dominant vegetation types (Fig. 3a),
the ensemble annual mean ET in 1986-2010 (Fig. 3b), and the long-term mean annual GPP in
1986-2010 (Fig. 3c).

201 In addition to the catchment-scale data, we collect the site-scale monthly data over CONUS, 202 mainly from the AmeriFlux dataset (Pastorello et al., 2020). We select 35 AmeriFlux sites in 203 CONUS, as listed in Table 2, with a minimum of 36 months (not necessarily continuous) of both 204 GPP and ET observations in 1986-2010. Note that the data's starting years, ending years, and 205 lengths vary among the sites. Table 2 provides more details about these sites. We obtain daily 206 forcing data from Daymet (Thornton et al., 2021), including minimum and maximum 207 temperature, actual vapor pressure, shortwave radiation, and snow for the 35 sites. For 208 consistency, we also group these sites into the six classes of vegetation types, which yielded five 209 DBF, four EF (all evergreen needleleaf), five GL, eight WSSL (three open shrublands, three 210 closed shrublands, one savannah, and one woody savannah), and thirteen CL/NVM (twelve CL 211 and one NVM) sites.

# 212 **3. Methods**

213 In this study, we first develop a generic expression of the GPP-ET linear relationship that 214 includes both the slope and intercept at the catchment scale (3.1). Data at the catchment scale 215 described above are used to evaluate the validity of the GPP-ET linear relationship and calibrate 216 the parameters (slope and intercept) of the relationship. Analysis is then performed to understand 217 the spatial variability of the parameter values and to derive a multilinear regression relationship 218 between the parameters and various climatic and environmental factors. The regression 219 relationship is used to regionalize the parameters, and the validity of the regionalization is further 220 tested at the site scale using the site-specific data described above. The statistical analysis 221 techniques used in this study are briefly described in 3.2.

# **3.1.** Generic form of GPP- ET relationship at the catchment scale

In catchment hydrology, normalization is a typical strategy to form a generic formula by minimizing the impacts of catchment size or magnitudes of any specific variables (Abeshu & Li, 2021; Chen et al., 2013; Chen & Sivapalan, 2020; Wang & Tang, 2014; Ye et al., 2015). Here we assume that normalized monthly GPP and ET at the catchment scale are linearly related as

$$\frac{\text{GPP}_{\text{m}}}{\text{GPP}} = a \frac{\text{ET}_{\text{m}}}{\text{ET}} + b \tag{2}$$

227 Where  $GPP_m$  and  $ET_m$  are monthly GPP (gC/m<sup>2</sup>/day) and ET (mm/day) at the catchment scale,

respectively, and  $\overline{\text{GPP}}$  and  $\overline{\text{ET}}$  are their corresponding long-term averages. **a** and **b** are dimensionless linear coefficients.

- 230 Rearranging Eqn. (2) for  $GPP_m$ , we get
- 231

$$GPP_{m} = \frac{\overline{GPP}}{\overline{ET}} (aET_{m} + b\overline{ET}).$$
(3)

232  $\frac{\overline{\text{GPP}}}{\overline{\text{ET}}}$  is essentially the long-term mean ecosystem water use efficiency. Eqn. (3) can be simplified 233 as

$$GPP_m = \beta ET_m + \alpha \overline{ET}$$
(4)

234 Where  $\beta (gC/m2/mm)$  and  $\alpha (gC/m2/mm)$  are two parameters. Eqn. (4) represents a two-235 parameter linear relationship between GPP and ET that can be used to predict GPP given ET.  $\beta$ 236 quantifies the increasing rate of GPP with increasing ET and vice versa, implying vegetation 237 carbon uptake per unit of water use.  $\alpha$  is associated with the dormant season when GPP or ET is low. The intercept term (i.e.,  $\alpha * \overline{ET}$ ) is analogous to the residual conductance term employed in 238 239 plant stomatal conductance models (Medlyn et al., 2011). If  $\alpha > 0$ , plant carbon uptake persists even when both transpiration and evaporation stop due to low VPD ( $ET \approx 0$  and GPP > 0). If 240 241  $\alpha < 0$ , evaporation continues to occur when there is no GPP associated with the above-ground 242 biomass (ET > 0 and GPP  $\approx$  0). If  $\alpha \approx 0$ , evapotranspiration and carbon uptake approach zero 243 simultaneously ( $ET \approx 0$  and  $GPP \approx 0$ ).

244 Note that if  $\alpha = 0$ , Eqn. (4) essentially reduces to Eqn. (1). Hereafter, we refer Eqn. (1) to as 245 function-I and Eqn. (4) as function-II for future comparison. We determine the parameters for 246 function-I and function-II in two stages. In the first stage, monthly GPP and ET data for each 247 catchment (see Section 2) from 1986 to 2002 were used to calibrate the parameters. We then 248 utilize these calibrated parameters to determine monthly GPP in 2003-2010 and verify them 249 against Landsat GPP. The parameter values obtained in the first stage are denoted as 250 "calibrated". In the second stage, we explore and derive quantitative regression relationships 251 between the calibrated *function-II* parameters and climatic and environmental factors such as 252 precipitation, solar radiation, VPD, geography (i.e., the latitude and longitude at the centroid of 253 each catchment), etc. This way, the function-II parameters can be estimated a priori instead of 254 through calibration and are denoted as "estimated". Note that these quantitative regression 255 relationships, if successfully derived, can be used to regionalize the function-II parameters and 256 provide parameter estimates over sparsely measured locations (Ali et al., 2014; Beck et al., 2020; 257 Merz & Blöschl, 2004; Ye et al., 2014).

### 258 **3.2.** Statistical methods

259 The seasonal dynamics of meteorology, hydrology, and vegetation play an essential role in 260 understanding the spatial variations of the slope and intercept of the GPP-ET linear relationship. 261 The Seasonality Index (SI), as defined below, is used to quantify the seasonal dynamics of different processes. Various statistical metrics, including Pearson and Spearman's correlation 262 263 coefficients and Kling-Gupta Efficiency, are used to evaluate the validity of the GPP-ET linear 264 relationship. Principal Component Analysis is used to determine the variance of the parameters 265 of the GPP-ET relationship explained by climatic and environmental factors. Lastly, the 266 Variance Inflation Factor (VIF) is used to determine the multicollinearity between the various

- climatic and environmental factors used as predictors in a regression formula to predict the
   parameters of the GPP-ET relationship. These various statistical methods are briefly explained
   below.
- 270 Seasonality Index (SI): SI applies to a time series of any time-varying variable and quantifies its
- seasonal distribution. SI is computed with the Walsh & Lawler (1981) method. SI ranges between 0 and 1.833, indicating that this variable uniformly occurs over the 12 months in a year and within a single month respectively.
- and within a single month, respectively.
- 274 *Pearson correlation coefficient (Pearson's r): Pearson's r* is a statistical metric used to evaluate 275 the linearity of a relationship between paired data. Its numerical value ranges from -1 to +1, 276 where a perfect positive and negative association is indicated by values of +1 and -1, 277 respectively, while a value of 0 indicates no association. Evans (1996) provides the following 278 interpretation of the absolute values of Pearson's r as: < 0.2 - very weak, 0.2 to 0.4 – Weak, 0.4
- to 0.6 Moderate, 0.6 to 0.8 Strong,  $\geq 0.8$ –Very strong.
- 280 Spearman's correlation (Spearman's  $\rho$ ): Spearman's correlation is a statistical measure that 281 assesses the strength and direction of a monotonic relationship between paired data, whether it is
- 282 linear or not. The magnitude of the correlation coefficient ranges from -1 to +1, indicating
- 283 perfect negative and positive monotonic relationships, respectively. The absolute value of
- 284 Spearman's  $\rho$  is often interpreted using the following rule of thumb: 0 to 0.20 negligible, 0.21
- $285 \qquad \text{to } 0.40-\text{weak}, 0.41 \text{ to } 0.60-\text{moderate}, 0.61 \text{ to } 0.80-\text{strong}, \text{and } 0.81 \text{ to } 1.00-\text{very strong}.$
- *Kling-Gupta Efficiency (KGE)*: We use KGE (Kling et al., 2012) as the goodness-of-fit measure for calibrating and validating *function-I* and *function-II*. The KGE value ranges between
- $288 -\infty$  to 1. KGE = 1 implies a perfect agreement between observed and simulated data.
- 289 *Principal Component Analysis (PCA)*: we use PCA to measure how much variability of 290 parameters,  $\beta$  and  $\alpha$ , can be explained by the catchment climatic and geographic variables.
- Variance Inflation Factor (VIF): Multicollinearity between components of any regression formula is tested using the VIF method (Miles, 2014; Neter et al., 1983). Generally, if 5.0 < VIF < 10.0, the multicollinearity issue requires further investigation. VIF >10 is a sign of severe multicollinearity and must be corrected. Remedial measures are necessary until VIF is less than 5.0 between any two components. A typical remedial strategy is to use more tolerant regression techniques such as the least absolute shrinkage and selection operator (LASSO) and Ridge regression (Dormann et al., 2013; Franke, 2010).

# 298 **4. Results**

# **4.1.** Validating the GPP-ET linear relationship at the catchment scale

Linearity analysis via Pearson's r suggests that the catchment-scale GPP-ET linear relationship 300 is indeed valid regardless of catchment size, climate, topography, or vegetation type (Fig. 4). 301 302 *Pearson's r* in 1986-2010 is higher than 0.6 for 97% of the 380 catchments, and is higher than 303 0.8 for 88% of them. Only 12 (3%) catchments have Pearson's r lower than 0.6. These 12 304 catchments are all located in an arid climate, and WSSL dominates 9 of them. The relatively low 305 Pearson's r values in the arid catchments are likely due to two reasons: i) the uncertainty in ET 306 estimation from the SAC-SMA model (Newman et al., 2015) and ii) the increase in the relative 307 importance of evaporation components besides transpiration. Note that, even among these 3% 308 catchments, *Pearson's r* is still no less than 0.4 except for two catchments, indicating a certain 309 level of linearity.

Fig. 4 also shows the scatter plots of monthly GPP versus ET normalized by their corresponding long-term mean in 1986-2010 for 16 representative catchments (Fig. 4a-p). The 16 catchments are selected in two steps. First, the 380 catchments are divided into three geographic groups based on longitude: the eastern, western, and central US regions. Then six catchments from the eastern, five from the central, and five from the western US are selected based on the strength of GPP seasonality, i.e., SI values ranging from the minimum to the maximum. Clearly, the

316 intercept is not negligible for some catchments and varies even among the same vegetation types.

317 Indeed, *function-II* performs better than *function-I* in those catchments dominated by grasslands 318 and shrubs, as suggested by Fig. 5. In this study, we calibrate the parameters for both *function-I* 319 and *function-II* in the calibration period 1986-2003 and use the calibrated parameters to predict 320 the monthly GPP in the validation period 2003-2010. Fig. 5 displays the monthly KGE values 321 (between the predicted and observed GPP time series) for all 380 catchments (map in the middle) 322 in 2003-2010. It also shows the predicted and observed monthly GPP time series for the 16 323 representative catchments (Fig. 5a-p). For those catchments dominated by grasslands and shrubs 324 (Fig. 5b, c, d, g, and m), *function-I* is subject to at least noticeable overestimation in June-August 325 when GPP is highest and underestimation in November-January when GPP is lowest. However, 326 function-II eliminates these noticeable biases. Fig. 5q summarizes this comparison between function-I and function-II in terms of Cumulative Distribution Function (CDF) for the KGE 327 328 values (between the observed and predicted monthly GPP) in the calibration and validation 329 periods, respectively. A CDF curve here describes the percentage of the 380 catchments with 330 their KGE values below a certain threshold. For example, CDF at KGE = 0.8 indicates the 331 percentage of the 380 catchments with KGE  $\leq 0.8$ . Function-II achieves KGE  $\geq 0.8$  for 333 of 332 the 380 catchments, whilst *function-I* achieves  $KGE \ge 0.8$  for only 158 catchments. Over the 333 CONUS domain, function-II performs better by better capturing both the maximum and 334 minimum of the GPP values, hence better capturing the seasonality of the GPP time series.

335 The calibrated slope,  $\beta$ , values from *function-II* are larger than those calibrated  $\omega$  values from 336 function-I (i.e., the ratio of long-term mean GPP to long-term mean ET) values at ~70.5% of the 337 380 catchments suggesting that the insights on the slope of the GPP-ET relationship gained from 338 previous site-scale studies may not be directly applicable to the catchment and larger scales. 339 the absolute values of the calibrated intercept,  $\alpha * \overline{ET}$ , are nonzero Moreover. (i.e., >0.05gC/m<sup>2</sup>/day) for 96% of the 380 catchments. This indicates that, in part, including the 340 341 intercept in the linear equation is responsible for the calibrated slope being consistently greater 342 than the traditional ones in a large proportion of the catchments. Hence, the previous 343 understanding of the GPP-ET relationship needs to be reexamined at the catchment scale via the 344 lens of *function-II* and its parameters.

## 345 **4.2.** Understanding the *function-ll* parameters

The spatial patterns of the calibrated  $\beta$  and  $\alpha$  values (Fig. 6) are similar to that of the annual 346 mean GPP (Fig. 3). Roughly,  $\beta$  decreases from northeast to southwest, except for catchments 347 348 along the Pacific Northwest coast. Physically,  $\beta$  represents the vegetation carbon uptake per 349 millimeter of water. At a given geographic longitude,  $\beta$  and  $\alpha$  increase and decrease with 350 latitude, respectively. Their spatial patterns are closely related to the climate and environmental 351 factors of CONUS that vary with latitude. Generally, mean annual vapor pressure deficit and 352 solar radiation decrease northward, and precipitation seasonality is strong in the central and 353 western US and weak in the eastern US and the Rocky Mountains. Furthermore, the phase index 354 between PET and precipitation is moderately negatively correlated with  $\alpha$  (Spearman's  $\rho = -$ 0.40) but exhibits no significant association with  $\beta$ . On the other hand, the parameter  $\beta$  is 355

- negatively correlated with the aridity index (Spearman's  $\rho = -0.65$ ), which is only moderately
- and positively associated with  $\alpha$  (*Spearman's*  $\rho = 0.436$ ). Both parameters are also significantly
- associated with precipitation frequency (*Spearman's*  $\rho = 0.7$  for  $\beta$  and -0.565 for  $\alpha$ ). The spatial
- 359 variability of  $\beta$  and  $\alpha$  also shows strong agreement with the peak mean monthly GVF values
- 360 (Spearman's  $\rho$  is 0.75 for  $\beta$  and -0.9 for  $\alpha$ ).

361 The systematic difference in these parameters in catchments with different dominant vegetation 362 types is further shown in Fig. 7. The catchment vegetation phenological cycle imposes 363 significant control on the GPP-ET relationship. In Fig. 7a, from top to bottom, the mean 364 calibrated  $\beta$  values (averaged across the catchments) are largest in the DBF-dominated 365 catchments, followed by MF, EF, WSSL, and GL. The large values of  $\beta$  in DBF-dominated 366 catchments can be attributed to their markedly distinct phenological stages, including leaf 367 regeneration and senescence, resulting in a rapid shift in carbon uptake between the transient and 368 dormant states. Photosynthesis rarely occurs during the dormant state, even when ET persists due to soil evaporation. The high values of  $\beta$  reflect the combined effect of DBF characteristics and 369 370 environmental factors resulting in a strong GPP seasonality. EF maintains foliage year-round, 371 and even during the dormant season, carbon uptake is higher than other vegetation types, which 372 increases further with greening-up. The phenological characteristics of the EF and the dominant 373 effect of PET result in a relatively subdued GPP seasonality compared to DBF, hence, lower  $\beta$ 374 values in comparison. MF is a mixture of DBF and EF, so its calibrated  $\beta$  values reasonably lie 375 between those of the two, reflecting a property that emerged from the combined characteristics 376 of EF and DBF forests. In GL catchments, gross primary productivity is primarily driven by 377 temperature and precipitation (both magnitude and timing) and hence, highly dynamic and varies 378 on a days-to-weeks scale. In these catchments, ET is often close to total water availability 379 (Abeshu & Li, 2021). These factors result in very similar monthly variations in ET and GPP, as 380 indicated by the  $\beta$  value only slightly greater than one. The WSSL vegetation is combined herbaceous and forested; as such, their calibrated  $\beta$  values lie reasonably between those of 381 382 forested and grassland catchments. For the last vegetation group, i.e., CL/NVM, the phenological 383 stages include temporary crop cover, harvest, and a bare soil period. The phenology and climate 384 characteristics are similar to that of DBF, but human factors also influence this group through 385 fertilization and other management practices that promote crop growth and harvest. The 386 similarity between CL/NVM and DBF explains why the CL/NVM covers have the second-387 highest calibrated  $\beta$  value (on average) after DBF.

388 The calibrated  $\alpha$  values are non-negligible ( $|\alpha| > 0.05 gC/m^2/day$ ) for 360 of the 380 389 catchments and exhibit systematic differences among the vegetation types. Fig. 7b suggests that 390 positive  $\alpha$  values primarily exist in the catchments dominated by WSSL (51 of 59 catchments), 391 EF (17 of 25 catchments), and some GL (16 of 46 catchments). The positive  $\alpha$  values suggest a 392 condition under which plant continues to take up carbon, but ET diminishes during the dormant 393 season. For instance, low VPD (high humidity) translates to low transpiration and soil 394 evaporation. However, plant carbon uptake can persist, driven by the energy from solar radiation. 395 Negative  $\alpha$  values prevail in the catchments dominated by DBF, MF, GL, and CL/NVM, 396 indicating that soil evaporation takes over during the dormant season when photosynthesis 397 diminishes via phenological processes (DBF, MF, and GL) or human activities (CL/NVM). GPP 398 happens only in the presence of light, but given sufficient VPD, ET occurs all the time; as such, 399 the absence of light can result in a scenario where ET > 0 while GPP = 0. A similar scenario can 400 also manifest under the condition where daytime processes are diminished (i.e., GPP and 401 daytime ET are zero), but night-time ET is not, as daytime and night-time ET respond differently

402 to low VPD levels (Han & Wang, 2021). Catchments with  $\alpha > 0$  are located in the coastal areas 403 of the Pacific Northwest, Pacific Coast, Southwest, Gulf Coast, and the southern part of the 404 Great Plains (for GL) (see Fig. 3a and Fig. 6b). Particularly in the southwestern coastal areas, the 405 winter period atmospheric river precipitation strongly influences the NDVI (Albano et al., 2017). 406 Hence, to a certain degree, this also contributes to  $\alpha$  being relatively larger and positive in that 407 area. The winter temperature is relatively mild in these regions of CONUS (Lute & Luce, 2017). 408 The winter temperature decreases systematically from the coastal regions inland, where the rest 409 of the catchments are located. The magnitude of  $\alpha$ , in general, can be attributed to plant 410 functionality and winter temperature. Plants have a minimum threshold for freezing temperature, 411 beyond which plant radiation conversion efficiency diminishes to zero, hence no photosynthetic 412 activities (i.e., GPP = 0). However, driven by solar radiation, soil, and canopy surface 413 evaporation may persist, leading to ET > 0 even when transpiration is nonexistent, resulting in 414  $\alpha < 0$ . Further, during the winter days, the daytime process, including GPP and ET, might be 415 inhibited by the absence of sufficient photoperiods, but night-time ET can still occur. The  $\alpha$ 416 values are particularly greater than zero in the western U.S.

417 Fig. 7a and b show systematic agreement between the variations of  $\beta$  and  $\alpha$  with vegetation types, indicating that catchments with strong seasonal variations in GVF have larger  $\beta$  values 418 419 and smaller  $\alpha$  values (e.g., DBF) and vice versa (e.g., WSSL). The above differences in the 420 function-II parameters among the vegetation regimes can be further explained by the GVF 421 difference (Fig. 7c). GVF difference at the catchment scale quantifies the seasonal changes in the 422 spatial coverage of active greenness within a catchment. For forested catchments, GVF generally 423 decreases from DBF to MF to EF. Both  $\beta$  and  $\alpha$  show a systematic pattern, with  $\beta$  showing a 424 pattern similar to GVF and  $\alpha$  opposite to GVF. DBF has thick canopies at the peak of the 425 growing period and loses most leaves in winter, resulting in relatively large temporal dynamics 426 of spatial cover (GVF difference> 0.4). EF catchments, on the other hand, maintain most of the 427 canopy cover year-round (GVF difference < 0.2). The MF type, as expected, lies between the 428 two, reflecting the influence of both vegetation types. From Fig. 7c, one can see that GL 429 catchments have a wide range of GVF values, implying that some catchments are dominated by 430 perennial grasslands with low GVF differences, while others are seasonal grasslands with higher 431 GVF differences. The GVF difference is generally low in the WSSL catchments (<0.2) because 432 this category is a mixture of forest and grasslands (perennial or seasonal), and the green canopy 433 coverage remains relatively stable throughout the year. To generalize, catchments with rapid 434 seasonal change in spatial cover are characterized by relatively high positive slope and high 435 negative intercept in the GPP-ET linear relationship, while catchments with subdued seasonal 436 dynamics are characterized by relatively smaller slope and smaller but positive intercept in the 437 GPP-ET relationship. To a certain degree, these characteristics indicate a space-time similarity of 438 catchment vegetation dynamics.

## 439 **4.3.** Regionalizing the *function-ll* parameters

Taking advantage of the insights gained from the above analyses, we attempt to regionalize the function-II parameters by estimating the function-II parameters a priori at the regional scale. Parameter regionalization is an effective strategy to transfer the process-based understanding from gaged to ungaged catchments and from catchment- to regional scale (Abeshu & Li, 2021; Guo et al., 2014; Ye et al., 2014). We aim to identify regression relationships between the target variables ( $\beta$  and  $\alpha$  in this case) and climate and other environmental factors as predictors. We do not explicitly include phenological variables, such as GVF, as predictors primarily because the

- 447 phenological characteristics of vegetation are already closely related to climate and448 environmental conditions.
- 449 The environmental factors for consideration are mostly static, such as geographic locations, soil
- 450 properties, geography, etc. The climatic factors are expressed in terms of seasonality index,
- mean, maximum, or minimum values extracted from the corresponding time series in 1986-2010.
   Here we select the climate and environmental predictor variables based on two criteria: 1)
- 453 observational data of these factors should be extensively available globally; 2) the factors should
- 454 have good monotonic relationships with  $\beta$  and  $\alpha$ , at least for some vegetation types. After a few
- 455 rounds of trial and error, we identify the following predictor variables that satisfy the two criteria
- 456 and lead to the best possible regression formulas: Geographic latitude (Lat), Long-term mean
- 457 VPD ( $\overline{VPD}$ ), Minimum monthly mean VPD ( $VPD_{min}$ ), Long-term mean shortwave radiation
- 458 ( $\overline{SWR}$ ), Minimum monthly mean SWR ( $SWR_{min}$ ), Long-term mean snow fraction ( $\overline{SF}$ ), and the
- 459 Seasonality index of monthly precipitation  $(SI_p)$ .
- 460 We use Spearman's  $\rho$  to determine whether the above predictors have monotonic relationships with  $\beta$  and  $\alpha$  for each vegetation type, as shown in Fig. 8. For instance, latitude has moderate to 461 462 strong monotonic relationships with both  $\beta$  and  $\alpha$  (|*Spearman's*  $\rho$ | > 0.4) among most vegetation 463 regimes, except for WSSL.  $\overline{SWR}$  has strong monotonic relationships with both  $\beta$  and  $\alpha$ 464 (|Spearman's  $\rho$ | > 0.6) in catchments dominated by DBF, MF, GL, CL/NVM. Furthermore, we 465 perform principal-component-analysis (PCA) to assess if the predictors included in Fig. 8 466 explain the most variability in the *function-II* parameters, as shown in Fig. 9. It appears that the first two PCA components alone can explain more than 80% of the variability of both  $\beta$  and  $\alpha$ 467 468 within each vegetation regime, suggesting that these climatic and environmental factors can potentially well predict both  $\beta$  and  $\alpha$  for each vegetation regime at the catchment scale. 469

470 We obtain two multilinear regression formulas for 
$$\beta$$
 and  $\alpha$ , separately.

$$\beta = 1.615 - 0.0056(ln(\overline{SWR}) * Lat) - 2.087 ln ln (\overline{VPD}) - 1.081(\overline{SF} * SI_P)$$
(5)

$$\alpha = 7.956 + 1.958 \left( \ln \ln VPD_{min} * Lat \right) + 1.369(SI_P + SF) - 1.364SWR_{min}$$
(6)

471 It is possible that multicollinearity exists among the predictors. Hence, we check for 472 multicollinearity using VIF. The VIF is < 2.75 for  $\beta$ , and < 5.50 for  $\alpha$ , indicating that the 473 regression formulas (Eqn. 5 and 6) are reasonably free from multicollinearity (Fig. 9).

474 Fig. 10 shows that the regression formulas well capture the spatial variability of  $\beta$  and  $\alpha$ . KGE and  $r^2$  are 0.71 and 0.73 for  $\beta$ , and 0.81 and 0.79 for  $\alpha$ , respectively. Between the two 475 parameters,  $\alpha$  generally shows a lower difference between the estimated and predicted values. 476 477 About 72% of catchments for  $\beta$  and 78% for  $\alpha$  are within a 20% margin of error (i.e., absolute 478 difference divided by actual value). Thirty-nine (~10% of 380: 13 WSSL, 12 EF, 12 GL, and 2 479 CL/NVM) catchments show a deviation larger than 20% for both parameters. We further apply 480 the estimated  $\beta$  and  $\alpha$  values in *function-II* against Landsat GPP shows KGE > 0.5 and > 0.80 for 92% and 62% of the catchments, respectively (Fig. 11). Only 30 of the 380 catchments have 481 482 KGE below 0.5, and only three have KGE less than zero. The dominant vegetation types in these 483 30 catchments are GL (15), EF (7), and WSSL (7). The two regression formulas can thus 484 reasonably well regionalize the *function-II* parameters, enabling the transferability of *function-II* 485 over the whole contiguous U.S.

# 486 **4.4.** Verifying *function-ll* at the Site-scale

- 487 Lastly, we evaluate whether *function-II* (Eqn. 4) and its parameter regionalization (Eqn. 5 and 6) 488 at the catchment scale are transferable to the site scale. We compare the simulated GPP (using 489 the site-scale climate and other data described in Section 2) against the AmeriFlux GPP 490 observations at 35 sites and the monthly scale. The results show that *function-II* captures the sitescale GPP reasonably well, as indicated by  $R^2 \ge 0.5$  for 32 sites and KGE  $\ge 0.5$  for 25 sites 491 492 (Table 3). The mean and median KGE across all sites are 0.51 and 0.61, respectively. The few 493 sites with relatively poor performances are mainly located in the western U.S., where Eqn. 5 494 performs relatively poorly even at the catchment scale.
- 495 Figure 12 depicts the monthly time series of simulated and observed GPP at five sites, one for 496 each vegetation type. The model captures the reference data well for the DBF site but 497 underestimates the peak values (Fig. 12a). The function consistently overestimates for the EF site 498 (Fig. 12b). Given that the intercept coefficients of both sites are < 0 and the seasonal patterns are 499 reasonably captured (Table 3), the overestimation is mainly due to underestimated intercept (i.e., 500 underestimated  $\alpha$ ), underestimated long-term ET, or both. For WSSL and GL (Fig. 12c and d), 501 the model captures the reference data reasonably well. Similar to the DBF site, the CL/NVM 502 results show poor performance in terms of magnitude but capture the patterns well (Fig. 12e). 503 Further, in general, the poor performances could be attributed to parameter estimation 504 uncertainties. For most of these sites, seeing that the temporal dynamics are captured well in both 505 magnitude and pattern, other than the peak GPP months, the cause is likely a bias in peak period 506 ET (i.e., underestimation) or decoupling between ET and GPP (i.e., linearity does not apply) 507 during this period. Overall, *function-II* provides reasonable estimates of GPP at the site scale, 508 with only three sites having KGE less than zero. Hence our results suggest that *function-II* works 509 across a wide range of spatial scales, given that the study catchments also span a wide range of 510 sizes.

# 511 **5. Discussions**

512 In this study, two GPP-ET formulas at monthly scales are evaluated at the catchment scale: the 513 traditional one-parameter relationship (function-I) and the newly proposed two-parameter 514 relationship (function-II). Typically, the slope of a GPP-ET relationship is considered as the 515 long-term ecosystem water use efficiency (WUE), which reflects climatic and phenological 516 controls on vegetation carbon gain and water consumption. The superior performance of *function-II* suggests that the *function-II* slope,  $\beta$ , is a more reliable estimator of WUE than the 517 518 function-I slope,  $\omega$ . Fig. 13 shows that  $\beta$  significantly differs from  $\omega$  in most catchments, particularly for cases where  $\omega$  was larger than  $2\text{gC/m}^2/\text{mm}$ . Compared to  $\beta$ ,  $\omega$  overestimates 519 520 WUE in the southwestern catchments dominated by EF and WSSL, where seasonality of GPP is 521 weak, and underestimates it in those northeastern catchments dominated by DBF, MF, GL, and 522 CL/NVM, where seasonality of GPP is strong.

523 WUE is a widely employed indicator for evaluating an ecosystem's adaptability to changing 524 environmental conditions. An overestimation of WUE may create the impression that ecosystems 525 are more resilient to water stress than they truly are, impacting our understanding of their 526 adaptability to climate change (J. Huang et al., 2016). Furthermore, such overestimation can 527 misrepresent an ecosystem's contribution to carbon sequestration, implying it can assimilate 528 more carbon dioxide per unit of water consumed than it actually can (Keenan et al., 2013). 529 Furthermore, fluctuations in WUE under extreme circumstances can trigger cascading effects on 530 ecosystem functioning. For instance, overestimating WUE may lead to a false sense of ecosystem resilience to drought, whereas underestimation could result in overlooking the 531 532 potential repercussions of drought or other water stresses on ecosystems (Leuzinger et al., 2011). 533 Such misjudgments can prompt improper management decisions and produce adverse ecological 534 consequences. An underestimation of WUE may lead to similar misjudgments as above except in 535 an opposite direction, e.g., overestimation of ecosystem resiliency under water stress. Reliable 536 estimation of WUE across diverse plant species and ecosystems is crucial for biodiversity 537 conservation, as it helps identify species and ecosystems more susceptible to climate change 538 (Chaves et al., 2003). Such knowledge can inform targeted conservation efforts to safeguard 539 vulnerable species and habitats.

540 Despite the improved performance of function-II (over function-I), certain limitations persist. 541 Firstly, the GPP-ET linearity is weaker in some catchments than the rest due to noticeable 542 contribution from surface evaporation. Hence the proposed function could be further improved in 543 such areas. Secondly, the proposed function does not capture monthly peak GPP values in some 544 cases. The likely reasons include: biases in ET estimation, WUE may vary from one season to another (or vary at a longer time scale) instead of being constant. Both are beyond the scope of 545 546 this study and left for future work. Lastly, ET is used as a whole instead of partitioning explicitly into transpiration and evaporation. ET partitioning is a long-standing challenge in both ecologic 547 548 and hydrologic communities. These limitations, nevertheless, do not affect our conclusions, but 549 rather open new opportunities for future research.

# 550 **6. Conclusions**

This study presents a generalized monthly GPP-ET relationship that works well across the catchment and site scales, hence regional scale as well. Driven by three objectives and the corresponding scientific questions, we have analyzed data at 380 catchments across CONUS. For the question "*Is the GPP-ET linear relationship valid at the catchment scale*", we find a strong linear relationship between monthly GPP and ET for most catchments (*Pearson's r* > 0.6 for 97%

556 of the 380 catchments) except for a few arid catchments dominated by woody savanna or 557 shrublands. We also find a non-negligible linear intercept of the GPP-ET relationship at the 558 catchment scale for 360 catchments. Hence, we argue that a new, generalized GPP-ET 559 relationship with a non-zero intercept is more suitable at the catchment and monthly time scale. 560 For the question "Can we establish quantitative linkages between environmental factors and the 561 slope and intercept of this linear relationship at the catchment scale", we have established 562 quantitative linkages between the parameters of the new GPP-ET relationship and the climatic 563 and environmental factors. We have also developed and validated a parameter regionalization 564 strategy (based on multilinear regression analysis), enabling the transferability of the new GPP-565 ET relationship from gaged to ungauged catchments. For the question "How is the new 566 quantitative understanding transferable from the catchment scale to the site and regional 567 scales", we have verified the new GPP-ET relationship and its parameter regionalization at 35 568 AmeriFlux sites with relatively satisfactory performance. We attribute the seemingly higher 569 biases at the site scale (compared to the catchment scale) to the difference in the input data 570 sources and the uncertainty in the parameter regionalization. Taken together, we suggest that the 571 new GPP-ET relationship and its parameter regionalization can be transferable across the site, 572 catchment, and regional scales.

573 The outcomes from this study have at least three important implications: 1) They can bridge the 574 ecological and hydrologic communities by providing a unified understanding of ET (water cycle) 575 and its linkages to vegetation productivity (carbon cycle). Any future new understanding of GPP 576 from the ecologic community and water balance from the hydrologic community can likely 577 further advance our understanding of this generalized GPP-ET relationship, coupling between 578 the water and carbon cycles, and other individual ecological and hydrologic processes. 2) They 579 can be used as physically meaningful indicators of the coupled hydrological-ecological processes 580 to diagnose the simulation results from land surface and earth system models. Such diagnosis 581 will shed light on the possible deficiencies in these models' structures or parameterizations for 582 representing hydrological and ecological processes and their interactions. 3) They can be used to 583 provide physical constraints for remote sensing-based ET products. Such products have been 584 subject to substantial biases, particularly during cloudy days. Remote-sensing measurements 585 provide valuable GPP and ET products at various spatiotemporal resolutions, but almost all of 586 these products are obtained from optical spectral measurements, which clouds can easily 587 contaminate. This can lead to uncertainty in the measurement quality of each revisit at a certain 588 location, especially for regions with persistent cloud cover throughout the year, such as the 589 Amazon (Samanta et al., 2012; Xu et al., 2019). This research provides a foundation for 590 recompiling GPP and ET products from multiple instruments with varying resolutions. Given the 591 GPP-ET relationships shown in this paper, it is extraordinarily meaningful to apply the GPP-ET 592 relationships obtained from different ecosystems to multiple satellite products, which could 593 reduce uncertainties and reproduce data products with enhanced spatial and temporal coverage.

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976 Figure 5: Spatial map of KGE for 380 catchments during the validation period (2003–2010). The 977 CDF describes the percent of catchments with a KGE value less than or equal to a certain 978 magnitude of interest. The 16 catchments for which the validation-period time series plots are 979 displayed are the same as those in Fig. 4a-p. The USGS site number and validation-period KGE 980 for *function-Il/function-II* in parenthesis are listed on top of each time series plot. Cumulative 981 Distribution Function (CDF) plot of *function-I* and *function-II* performance over the calibration 982 and validation periods are shown in Fig. 5q.

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- 994 Figure 10: Verifying the multivariable linear regression formulas for estimating  $\beta$  (a, b) and  $\alpha$  (c,
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- 996 parameters are gC/m2/mm.
- 997 Figure 11: Spatial map of validation period KGE for 380 catchments with estimated *function-II*
- 998 parameters. The 16 catchments for which the validation-period time series plots are displayed are 999 the same as those in Fig. 4a-p. The KGE is for the entire study period (1986-2010).
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- Figure 13: Difference between beta and omega across CONUS (13a) and between vegetation regimes (13b).

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Table 1: Catchments group based on dominant vegetation cover type.

Group	Vegetation type(Count)	Group Name	Count
1	Deciduous Broadleaf(89)	DBF	89
2	Evergreen Neadleaf Forest(22) Evergreen Broadleaf Forest(3)	EF	25
3	Mixed Forests(50)	MF	50
4	Croplands(46) Croplands/Natural Vegetation Mosaic(65)	CL/NVM	111
5	Savannas(4) Woody Savannas(45) Open Shrublands(7) Closed Shrublands(3)	WS-SL	59
6	Grasslands(46)	GL	46

Site ID	Lon	Lat	Vegetation	Start Date	End Date	β	α	KGE	$\mathbf{R}^2$
				2	2				
US-ARM	-97.49	36.61	CL/NVM	2003-01	2020-12	1.69	-0.01	0.64	0.66
US-Bil	-121.50	38.10	CL/NVM	2016-08	2021-12	0.74	0.73	0.3	0.87
US-Bi2	-121.54	38.11	CL/NVM	2017-05	2021-12	0.74	0.74	0.14	0.79
US-CF1	-117.08	46.78	CL/NVM	2017-05	2020-12	2.01	-0.61	0.58	0.87
US-CF2	-117.09	46.78	CL/NVM	2017-05	2020-12	1.99	-0.60	0.62	0.85
US-CF3	-117.13	46.76	CL/NVM	2017-06	2021-12	1.98	-0.59	0.61	0.84
US-CF4	-117.13	46.75	CL/NVM	2017-06	2021-12	1.98	-0.59	0.66	0.89
US-Ne1	-96.48	41.17	CL/NVM	2001-06	2020-12	2.19	-0.39	0.54	0.87
US-Ro1	-93.09	44.71	CL/NVM	2004-01	2016-12	2.79	-1.20	0.61	0.76
US-Ro5	-93.06	44.69	CL/NVM	2017-01	2020-12	2.78	-1.19	0.5	0.63
US-Ro6	-93.06	44.69	CL/NVM	2017-01	2021-12	2.78	-1.19	0.81	0.81
US-Tw3	-121.65	38.12	CL/NVM	2013-06	2018-05	0.77	0.79	0.31	0.87
US-HWB	-77.85	40.86	CL/NVM	2015-08	2018-08	2.68	-0.88	0.6	0.78
US-Ha1	-72.17	42.54	DBF	1991-11	2020-12	2.90	-0.97	0.58	0.83
US-MMS	-86.41	39.32	DBF	1999-02	2020-12	2.51	-0.80	0.54	0.94
US-MOz	-92.20	38.74	DBF	2004-06	2019-12	2.29	-0.56	0.61	0.93
US-UMd	-84.70	45.56	DBF	2007-06	2021-12	3.10	-1.26	0.61	0.94
US-xBR	-71.29	44.06	DBF	2017-02	2021-12	2.94	-0.88	0.73	0.94
<b>US-GLE</b>	-106.24	41.37	EF	2005-01	2020-09	3.36	-0.93	-0.1	0.57
US-Ho2	-68.75	45.21	EF	2002-06	2020-12	3.03	-1.11	0.46	0.73
US-Me2	-121.56	44.45	EF	2002-01	2020-12	2.01	0.31	0.68	0.81
US-NR1	-105.55	40.03	EF	1999-01	2016-12	3.38	-0.79	0.06	0.71
US-KFS	-95.19	39.06	GL	2008-01	2019-12	2.26	-0.35	0.79	0.67
US-KLS	-97.57	38.77	GL	2012-05	2019-12	1.79	-0.07	0.65	0.59
US-ONA	-81.95	27.38	GL	2016-05	2020-12	1.35	0.90	0.86	0.79
US-Ro4	-93.07	44.68	GL	2014-01	2021-12	2.77	-1.18	0.66	0.92
US-Sne	-121.75	38.04	GL	2016-06	2020-12	0.80	0.76	-0.48	0.19
US-Rms	-116.75	43.06	WSSL	2014-10	2020-09	2.30	-0.20	0.87	0.94
US-Rwe	-116.76	43.07	WSSL	2003-02	2007-09	2.27	-0.21	0.16	0.88
US-Rwf	-116.72	43.12	WSSL	2014-06	2020-09	2.14	-0.12	0.72	0.94
US-Jo2	-106.60	32.58	WSSL	2010-08	2020-12	0.69	0.65	0.49	0.36
US-Rws	-116.71	43.17	WSSL	2014-10	2020-09	1.61	-0.02	0.73	0.67
US-SRC	-110.84	31.91	WSSL	2008-03	2014-06	0.39	0.97	-0.14	0.56
US-Wjs	-105.86	34.43	WSSL	2007-05	2021-12	1.09	0.32	0.8	0.76
US-Mpj	-106.24	34.44	WSSL	2008-01	2020-12	1.21	0.28	0.66	0.45

1045 <u>Table 2: Ameriflux sites used in this study</u>

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1056 Figure 2: Conceptual illustration of GPP-ET relationship scenarios





Figure 3: Catchment data used in this study. The CAMELS dataset along with remote sensing
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1131 Figure 6: Spatial patterns for the calibrated *function-II* parameters: a) slope and b) intercept

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1189 Figure 9: Percent of Explained Variance (EV) by all the predictors shown in Fig. 8 and by the

1190 first two principal components (PC1 and PC2) of the predictors for the calibrated parameters: (a) 1191 for the parameter  $\beta$  and (b) for the parameter  $\alpha$ .





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