Parameterizing mesoscale eddy buoyancy transport over sloping topography

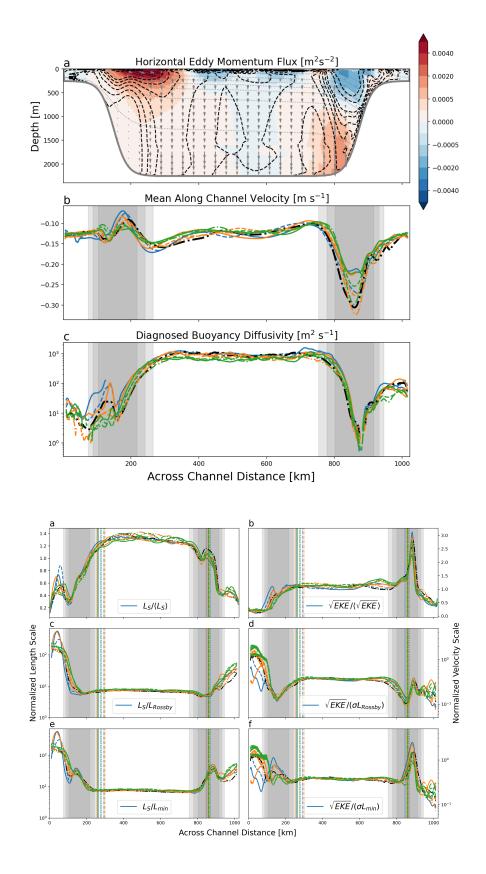
Aleksi Nummelin 1,2,3 and Pål Erik Isachsen 1,4

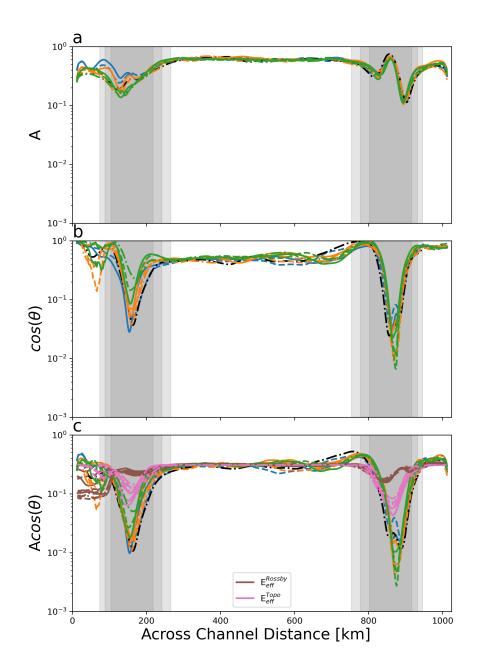
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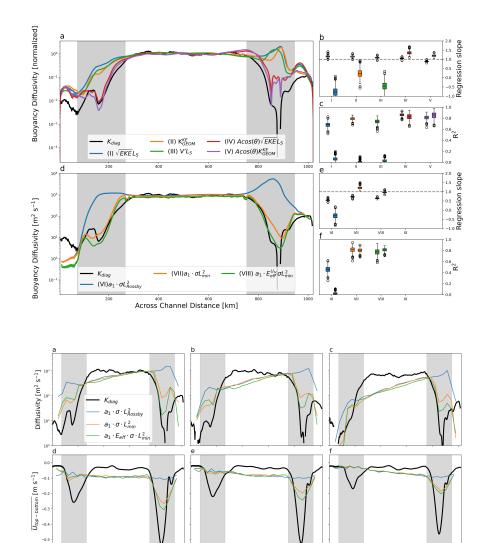
January 16, 2024

Abstract

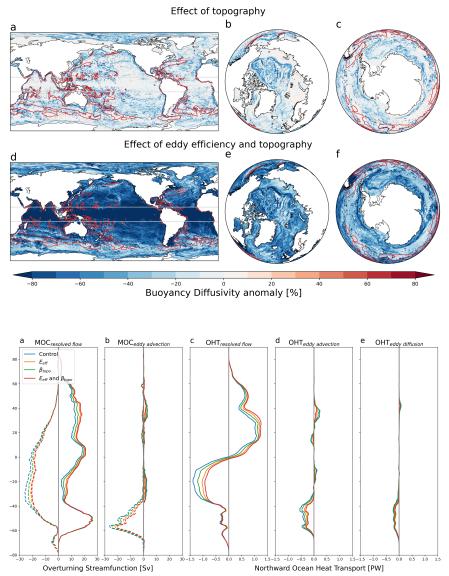
Most of the ocean's kinetic energy is contained within the mesoscale eddy field. Models that do not resolve these eddies tend to parameterize their impacts such that the parameterized transport of buoyancy and tracers reduces the large-scale available potential energy and spreads tracers. However, the parameterizations used in the ocean components of current generation Earth System Models (ESMs) rely on an assumption of a flat ocean floor even though observations and high-resolution modelling show that eddy transport is sensitive to the potential vorticity gradients associated with a sloping seafloor. We show that buoyancy transport coefficient diagnosed from idealized eddy-resolving simulations is indeed reduced over both prograde and retrograde bottom slopes (topographic wave propagation along or against the mean flow, respectively) and that the reduction can be skilfully captured by a mixing length parameterization by introducing the topographic Rhines scale as a length scale. This modified 'GM' parameterization enhances the strength of thermal wind currents over the slopes in coarse-resolution, non-eddying, simulations. We find that in realistic global coarse-resolution simulations the impact of topography is most pronounced at high latitudes, enhancing the mean flow strength and reducing temperature and salinity biases. Reducing the buoyancy transport coefficient further with a mean-flow dependent eddy efficiency factor, has notable effects also at lower latitudes and leads to reduction of global mean biases.

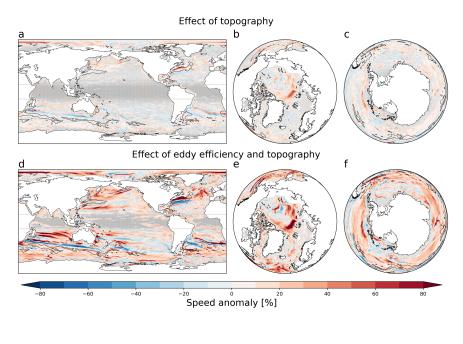


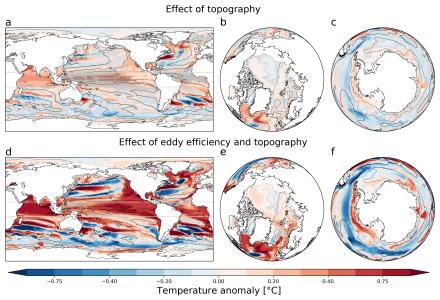


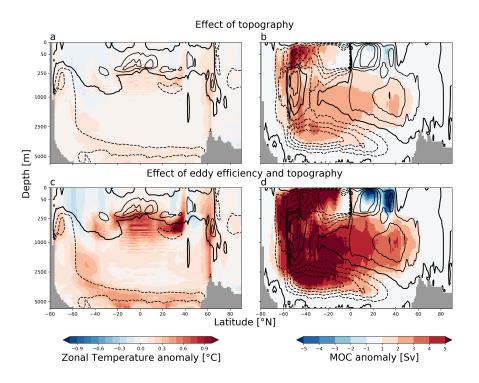


Across Channel Distance [km]









Parameterizing mesoscale eddy buoyancy transport over sloping topography

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Key 1	Points:
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9	•	Eddy buoyancy diffusivity reduction over bottom slopes can be parameterized us-
10		ing the Eady growth rate and topographic Rhines scale.
11	•	Realistic reduction in buoyancy diffusivity in a coarse-resolution model strength-
12		ens baroclinic boundary currents.
13	•	A topographically-aware eddy efficiency factor improves the parameterization and
14		further reduces biases in global simulations.

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15 Abstract

Most of the ocean's kinetic energy is contained within the mesoscale eddy field. Mod-16 els that do not resolve these eddies tend to parameterize their impacts such that the pa-17 rameterized transport of buoyancy and tracers reduces the large-scale available poten-18 tial energy and spreads tracers. However, the parameterizations used in the ocean com-19 ponents of current generation Earth System Models (ESMs) rely on an assumption of 20 a flat ocean floor even though observations and high-resolution modelling show that eddy 21 transport is sensitive to the potential vorticity gradients associated with a sloping seafloor. 22 We show that buoyancy transport coefficient diagnosed from idealized eddy-resolving sim-23 ulations is indeed reduced over both prograde and retrograde bottom slopes (topographic 24 wave propagation along or against the mean flow, respectively) and that the reduction 25 can be skilfully captured by a mixing length parameterization by introducing the topo-26 graphic Rhines scale as a length scale. This modified 'GM' parameterization enhances 27 the strength of thermal wind currents over the slopes in coarse-resolution, non-eddying, 28 simulations. We find that in realistic global coarse-resolution simulations the impact of 29 topography is most pronounced at high latitudes, enhancing the mean flow strength and 30 reducing temperature and salinity biases. Reducing the buoyancy transport coefficient 31 further with a mean-flow dependent eddy efficiency factor, has notable effects also at lower 32 latitudes and leads to reduction of global mean biases. 33

³⁴ Plain Language Summary

Due to their high computational costs, global climate models are usually run at coarse 35 spatial resolution, which does not allow them to resolve the ocean weather—mesoscale 36 eddies—which are an important part of the ocean energy cycle and contribute to mix-37 ing of tracers such as heat and carbon. Eddies are instead parameterized in an idealized 38 manner which relates the eddy-driven transport to the strength of the vertical and hor-39 izontal density gradients in the ocean. Such parameterizations do not take into account 40 impacts of large-scale bottom bathymetry which have been shown to weaken the eddy 41 driven transport. Here we use high-resolution eddy-resolving simulations to improve ex-42 isting parameterizations so that they become sensitive to the bottom slope. We show 43 that such a parameterization qualitatively captures the transport reduction seen in ide-44 alized high-resolution simulations and can also reduce errors in realistic global simula-45 tions. 46

47 **1** Introduction

At present, the ocean components of most global climate models are used at res-48 olutions that require parameterizing transport by the oceanic mesoscale (Fox-Kemper 49 et al., 2019). Although coupled simulations with eddying ocean fields are slowly emerg-50 ing (Chang et al., 2020), mesoscale eddy parameterizations are still likely part of ocean 51 models for another decade. The wave-turbulence duality of mesoscale eddy dynamics can 52 cause very rich transport behavior, involving intermittency, non-local transport by co-53 herent vortices and even up-gradient fluxes that energize the mean flow (e.g. Chen et 54 al., 2014; Yankovsky et al., 2022; Liu et al., 2023). Nonetheless, most present-day pa-55 rameterizations do not include such effects, but have their origins in the works of Gent 56 and Mcwilliams (1990); Gent et al. (1995) and Redi (1982), tackling eddy-induced ad-57 vection and tracer mixing, respectively. The 'GM' advection is specified by an overturn-58 ing streamfunction which itself is cast in terms of a horizontally down-gradient and ver-59 tically up-gradient buoyancy transport—resulting in a reduction of available potential 60 energy. 'Redi' diffusion, by contrast, mixes both active and passive tracers down-gradient 61 along isopycnals (Gent, 2011). 62

⁶³ Much of the current research focuses on how to prescribe flow-dependent eddy trans-⁶⁴ port coefficients, or eddy 'diffusivities', that set the strength of the GM advection and

Redi mixing. These are distinct processes, and the vertical structure of eddy buoyancy 65 transport certainly appears to be different from that of isopycnal Redi diffusion, includ-66 ing the diffusion of potential vorticity (PV) (see e.g. K. S. Smith & Marshall, 2009; Aber-67 nathey et al., 2013; Bachman et al., 2020). Less is known about how GM and Redi dif-68 fusivities relate laterally, but since both are sensitive to e.g. eddy energy levels, we ex-69 pect them be spatially correlated. In practice, the diffusivities, whether applied to the 70 GM or Redi scheme, are most often parameterized following mixing length theory. This 71 means that they are constructed from the product of some eddy velocity scale and a mix-72 ing length scale. Some work has gone into estimating the eddy velocity scale by imple-73 menting a prognostic equation for eddy energy (Eden & Greatbatch, 2008; Marshall et 74 al., 2012; Mak et al., 2018; Bachman, 2019; Jansen et al., 2019), but this is still very much 75 an active and incomplete field of research. So, in the latest iteration of the Climate Model 76 Inter Comparison Project (CMIP; https://explore.es-doc.org/cmip6/models/), the 77 GFDL-CM4.0 model (Adcroft et al., 2019) was, to our knowledge, the only one that used 78 a prognostic eddy energy approach to estimate the eddy velocity scale. 79

The study by Visbeck et al. (1997) therefore continues to influence the practical 80 use of the mixing length approach. Drawing on earlier works by Green (1970) and Stone 81 (1972), they proposed that the velocity scale for the GM diffusivity be based on the prod-82 uct of the growth rate of baroclinic instability in the linearized Eady model (Eady, 1949) 83 and some length scale. Assuming that the mixing length is also set by the same scale, 84 the diffusivity will then scale as the Eady growth rate and the square of the length scale. 85 Visbeck et al. (1997) associated the mixing length with the 'width of the baroclinic zone' 86 which they defined as "the width of the region where the local growth rate exceeds 10%87 of the maximum growth rate of the field". The concept, however, is hard to define in any 88 but the most idealized model geometries, and length scales therefore need to be formed 89 from more rigorous dynamical arguments. 90

As proposed by Stone (1972), one obvious candidate for length scale is the inter-91 nal deformation radius, the approximate scale of the fastest unstable growth in the Eady 92 model. Solid observational evidence for the relevance of this length scale has been pre-93 sented by Stammer (1997) and Eden (2007). However, other relevant scales arise if dy-94 namics beyond the Eady framework are accounted for, most notably bottom friction and 95 potential vorticity (PV) gradients. Jansen et al. (2015), for example, examined the role 96 of bottom friction and the planetary vorticity gradient in a two-layer flat-bottom chan-97 nel model. They found that bottom friction primarily influences the vertical distribu-98 tion of eddy energy and that the mixing length in most of their simulations is set by the 99 Rhines scale, i.e. the transition scale between nonlinear and linear PV dynamics on the 100 flat-bottom planetary beta plane (Rhines, 1977). More generally, Jansen et al. (2015) 101 found that in order to cover various dynamical regimes, the smaller of several candidate 102 length scales should be chosen, and that inclusion of the Rhines scale amongst these scales 103 is important. In fact, the observational studies of both Stammer (1997) and Eden (2007) 104 specifically pointed to a minimum of the internal deformation radius and the Rhines scale 105 as a best fit for eddy length scales over much of the world ocean. 106

These principles remain the standard in state-of-the-art models, although devel-107 opment has occurred in later years. As mentioned above, there has been extensive fo-108 cus on developing prognostic equations for eddy energy. Considerable efforts have also 109 gone into studying effects of horizontal eddy anisotropy (R. D. Smith & Gent, 2004) and 110 the suppression of mixing across strong mean flows (Ferrari & Nikurashin, 2010; Klocker 111 et al., 2012, and references therein). It's worth noting, however, that most of the devel-112 opment up until recently has been guided by observed dynamics in low and mid latitudes. 113 Current parameterizations thus lack any treatment of two aspects that are potentially 114 of huge importance in high latitude oceans, namely the presence of sea ice and the po-115 tential vorticity gradients imposed by sloping bottom topography. A sea ice cover can 116 effectively have the same influence as bottom friction on growth of baroclinic instabil-117

ity as well as on dissipation of existing mesoscale and sub-mesoscale eddies (Meneghello 118 et al., 2021). This topic, however, will be left out from the present study. We will instead 119 focus on the dynamical impacts of bottom slopes, i.e. continental slopes and mid-ocean 120 ridge systems, whose imprints can be easily seen in observations of both mean currents 121 and mesoscale energy fields, especially at high northern latitudes (Nøst & Isachsen, 2003; 122 Koszalka et al., 2011; Trodahl & Isachsen, 2018). Imprints of topographic PV gradients 123 can also be seen at lower latitudes, e.g. in drifter and float paths (LaCasce, 2000; Fratan-124 toni, 2001). 125

126 Sloping bottom topography can suppress growth rate and reduce length scales of baroclinic instability (e.g. Blumsack & Gierasch, 1972; Mechoso, 1980; Isachsen, 2011; 127 Brink, 2012) as well as impact finite-amplitude eddy fields (e.g. Bretherton & Haidvo-128 gel, 1976; Vallis & Maltrud, 1993; Lacasce & Brink, 2000; K. Stewart et al., 2015; Wang 129 & Stewart, 2018). To this end, new topography-aware parameterizations have started 130 to emerge, both for eddy-induced advection and isopycnal mixing. In particular, Wang 131 and Stewart (2020) and Wei et al. (2022) tested different scaling relations for the GM 132 diffusivity in high-resolution model simulations of flows over idealized continental slopes 133 in re-entrant channels. The two works examined eddy characteristics and fluxes across 134 retrograde and prograde mean currents, respectively, meaning currents that are in the 135 opposite and same direction as topographic waves. Both studies diagnosed the eddy en-136 ergy from the high-resolution fields and used this to examine traditional mixing length 137 formulations, trying out various choices for mixing length. In addition, they tested the 138 'GEOMETRIC' formulation of Marshall et al. (2012) in which diffusivities are instead 139 constructed from eddy energy and an eddy decorrelation time scale which is set equal 140 to the inverse of the Eady growth rate. In general, the two formulations performed sim-141 ilarly, suggesting that a good knowledge of the eddy energy field is key. However, im-142 portantly, both studies also found that empirical prefactors that depend on the topographic 143 slope are needed to reproduce very weak eddy buoyancy fluxes across sloping bottom to-144 pography. 145

Wei and Wang (2021) carried on from Wang and Stewart (2020), but focused on 146 the along-isopycnal tracer (Redi) diffusivity in the same channel model—in retrograde 147 flows only. The authors constructed a parameterized Redi diffusivity from (the square 148 root of) the diagnosed eddy kinetic energy and the internal deformation radius, again 149 finding that the actual diffusivity over the slope was suppressed below the original scale 150 estimate. However, instead of testing a set of empirical slope-dependent prefactors, as 151 done by Wang and Stewart (2020) and Wei et al. (2022), this study picked up from Ferrari 152 and Nikurashin (2010) and demonstrated that mean-flow suppression could explain the 153 observed reduction in cross-slope fluxes near the surface, whereas eddy velocity anisotropy 154 contributed to the reduction close to the bottom. 155

In other words, both sets of studies (see also Brink, 2012, 2016; Hetland, 2017) con-156 cluded that eddy diffusivities over sloping bottoms are poorly reproduced by traditional 157 open-ocean scaling choices for eddy velocity and eddy length (or decorrelation time), and 158 that additional dynamical impacts of the bottom topography must be brought in. Topographically-159 induced velocity anisotropy is one obvious factor which could impact both the effective 160 eddy velocity (its orientation relative to the tracer gradient) and effective mixing length 161 or time scale. In addition, mean-flow suppression, caused by eddies propagating relative 162 to the mean flow, may also be reflected in a reduced effective mixing length, as suggested 163 by Ferrari and Nikurashin (2010, their equation 13). But such interpretations have so 164 far only been applied to Redi diffusion—now also over continental slopes (Wei & Wang, 165 2021). Whether similar dynamics lie behind the various empirically-fitted suppression 166 factors in the studies of buoyancy diffusion over continental slopes is yet an open ques-167 tion. 168

The present study will primarily focus on eddy buoyancy transport and thus on GM diffusivities. It is inspired by and builds directly on the results obtained by Wang

and Stewart (2020) and Wei et al. (2022), and, as they did, we thus limit the scope to 171 depth-averaged diffusivities. However, as noted, the above works examined prograde and 172 retrograde flows separately and also constructed diffusivities from eddy energy levels di-173 agnosed from very idealized but high-resolution fields. So here we aim to i) study fluxes 174 and diffusivities over both types of flow situations under one and the same framework, 175 ii) examine how far one can get with parameterizations that do not rely on diagnosing 176 the actual eddy energy field and, finally, iii) expand by assessing impacts both in an ide-177 alized setting and in a realistic global ocean simulation. 178

179 In the process, we revisit the question of what is the relevant eddy mixing length over continental slopes. The starting point will be the internal deformation radius since 180 this remains a relevant parameter in the Eady problem. In addition, we also consider 181 the topographic Rhines scale, i.e. the scale that marks the transition between a linear 182 topographic Rossby wave (rather than planetary Rossby wave) regime and turbulent PV 183 dynamics. The above-mentioned idealized channel studies give conflicting evidence about 184 the relevance of this scale. We are nevertheless inspired by the findings of Stammer (1997), 185 Eden (2007) and Jansen et al. (2015) and bring up this approach here again. To home 186 in on what actually goes on over the slopes, we will also diagnose the eddy velocity anisotropy 187 and, in addition, the phase relationship between velocity and tracer perturbations. This 188 second diagnostic gives additional information about dynamics not reflected in mere scale 189 estimates, at least estimates of eddy velocity. Essentially, no matter how strong the Root 190 Mean Square (RMS) eddy velocity is, if velocity perturbations are in quadrature with 191 buoyancy perturbations a zero transport results. The analysis done here will indeed show 192 that most of the topographic suppression is reflected in a degraded phase relationship 193 and that velocity anisotropy takes on a secondary role. 194

The paper is structured as follows: In section 2 we introduce the modelling tools 195 and various diagnostics and parameterizations used. In section 3 we begin by diagnos-196 ing eddy fields from high-resolution channel simulations that contain both prograde and 197 retrograde flows at the same time. We then see how far mixing-length and GEOMET-198 RIC parameterizations can take us in reproducing the diagnosed depth-averaged GM diffusivity— 199 with and without accounting for effect of anisotropy and phase relations between eddy 200 velocity and tracer perturbations. At the end of this section we examine the impact of 201 a topographically-aware parameterization in a coarse-resolution version of the channel 202 model. In section 4 we finally employ the new parameterization in realistic global ocean 203 simulation. We then take a critical look into some of our parameterization choices and 204 their interpretation in section 5 before summarizing our findings in section 6. 205

206 2 Methods

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2.1 Model setup

We use the Bergen Layered Ocean Model (BLOM), the ocean component of the 208 Norwegian Earth System Model (NorESM; Seland et al., 2020), in an idealized channel 209 configuration as well as in a realistic global setup (both configurations are published in 210 Nummelin, 2023b). BLOM uses 51 isopycnal levels (potential density referenced to 2000 dbar) 211 with a 2-level bulk mixed layer at the surface. In order to diagnose the various quanti-212 ties used in the study, we interpolate the outputs locally (in time and space) to height 213 coordinates, except for quantities that are specifically calculated from isopycnal output 214 (see below), in which case we interpolate the outputs to a new density grid so that the 215 bulk mixed layer is properly accounted for. 216

The channel setup is re-entrant in the zonal (x) direction. The domain is 416 km long (zonally) and 1024 km (y_{max}) wide (meridionally). At both sides of the channel there are continental slopes of given width (W) centered at 150 km (Y_C) from the domain edges, stretching 2000 m (D_S) in the vertical from the shelf break at 250 m depth (D_B) to the bottom of the slope at 2250 m depth. These parameters then define the bathymetry (H)across the channel (along the *y*-coordinate):

$$H(y) = \begin{cases} D_B + 0.5 \cdot D_S \left\{ 1 + \tanh\left[\frac{\pi(y - Y_C)}{W}\right] \right\}, & y < (Y_C + W) \\ D_B + 0.5 \cdot D_S \left\{ 1 + \tanh\left[\frac{\pi(y_{max} - y - Y_C)}{W}\right] \right\}, & y_{max} - y < (Y_C + W) \\ D_B + D_S, & \text{otherwise i.e. in the central basin.} \end{cases}$$

In addition, to trigger instabilities we add 2D random noise with standard deviation of 10 m to the bottom topography.

The model is initialized from rest with constant salinity and a horizontally homo-226 geneous temperature profile. The temperature, which here determines density alone, has 227 a maximum at the surface and decays exponentially towards the bottom. We place the 228 channel in the northern hemisphere, using a constant Coriolis parameter, and then force 229 the flow with a constant westward wind stress. The surface mixed layer is kept shallow 230 by parameterization of submesoscale mixed layer eddies (Fox-Kemper et al., 2008) that 231 counter the vertical mixing induced by the constant wind forcing. See Table 1 for fur-232 ther parameter settings. 233

We first run the channel model at 2 km horizontal resolution, which is eddy-resolving 234 over the deep central basin and over the slopes (see Table 2 for deformation radius) but 235 only eddy-permitting over the shallow shelves. To investigate the effects of the two bot-236 tom slopes on eddy transport and, specifically, on eddy diffusivity, we vary the initial strat-237 ification and the width of the continental slope, i.e the slope angle. The various exper-238 iments are laid out in Table 2. All simulations are spun-up for 10 years to a semi-equilibrium 239 in which domain averaged eddy kinetic energy is close to constant, and the model fields 240 are then diagnosed over an additional 5-year period (so between years 11-15). We then 241 test and compare various forms of parameterized eddy buoyancy fluxes at non-eddying 242 32 km resolution in the same idealized channel. These are also run for 15 years, with the 243 last 5 years being diagnosed. With the focus on the 5-year means, we are assuming a slowly-244 varying eddy field and attempting to parameterize its time-mean impact. However, we 245 note that geostrophic turbulence is known to be intermittent with implications for vari-246 ability in eddy transport and mixing (Busecke & Abernathey, 2019; Huneke et al., 2019; 247 G. Zhang et al., 2023; Ong et al., 2023). Also our simulations suggest that over the north-248 ern prograde slope the jet there undergoes periods of alternating strong and weak eddy 249 activity on a timescale of several months (not shown). How the time-mean view of the 250 eddy transport presented here incorporates such variability is left for future studies. 251

Finally, the impact of the most skillful parameterization is assessed in realistic global 252 simulations. These are nominal 1° resolution global forced ocean-ice experiments which 253 follow the Ocean Model Intercomparison Project, OMIP-II protocol (Tsujino et al., 2020). 254 In these simulations, the mean grid size north of $62^{\circ}N$ and south of $64.5^{\circ}S$ is approx-255 imately 32 km, similar to the coarse resolution channel. We compare simulation with an 256 existing eddy parameterization, which does not include any effects of bottom topogra-257 phy, to simulations with parameterizations that feel the bottom topography through the 258 topographic beta parameter (Figure S1, panel a-c; see section 2.2 for further definitions). 259 Each simulation is 110 year long (2 cycles of 55 long repeat cycle), and we diagnose the 260 results using the last 30 years. At this point there is still a long-term drift in the model 261 (as seen in all models following the OMIP-II protocol; Tsujino et al., 2020), but the gen-262 eral circulation has stabilized. 263

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2.2 Diagnostics and Paramaterizations

The key parameter of interest is the buoyancy diffusivity, and in this study, we focus exclusively on the depth-averaged diffusivity. We leave the development of depthvarying parameterizations for future studies. A fruitful way forward for this may be to develop a flow-dependent structure function that distributes the depth-averaged diffusivity vertically (see e.g. Bachman et al., 2020; Wei & Wang, 2021).

In the idealized zonal channel simulations, where buoyancy is given by temperature, the cross-channel (i.e. meridional) buoyancy diffusivity is diagnosed from

$$K_{diag} = -\frac{1}{H} \int_{H}^{0} \frac{\langle v'T' \rangle}{\partial \langle T \rangle / \partial y} dz, \qquad (1)$$

where H is bottom depth, v is meridional velocity, and T is meridional temperature. Angle brackets indicate a zonal (along-channel) mean and primes indicate deviations from such mean. So v' and T' are the across-channel velocity and temperature perturbations from the zonal mean. In (1), the flux gradient relation is evaluated at each level, before depth averaging. For analysis of the channel simulations, we also average K_{diag} over time.

In what follows, we make frequent use of depth-averaged variables, which we note with $(\bar{\cdot})$. Thus, our eddy kinetic energy density is defined in terms of depth-averaged velocities as $(-t^2) + (-t^2)$

$$EKE = \frac{\langle \overline{u}^{\prime 2} \rangle + \langle \overline{v}^{\prime 2} \rangle}{2}, \qquad (2)$$

and an velocity anisotropy factor is defined as

$$A = \frac{\langle \overline{v}^{\prime 2} \rangle}{\langle \overline{u}^{\prime 2} \rangle + \langle \overline{v}^{\prime 2} \rangle},\tag{3}$$

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$$\langle \overline{v}^{\prime 2} \rangle = 2A \cdot EKE. \tag{4}$$

(5)

Parameterizing the diffusivity starts with a scale estimate. Two approaches are currently in use, the traditional mixing length and the GEOMETRIC approach. In the first approach, we write

 $K_{ML} \propto VL,$

where V is a representative eddy velocity scale and L is a representative mixing length. If complete information exists about the high-resolution eddy fields, it is natural to set $V = \sqrt{EKE}$ or, more correctly for the cross-channel diffusion we study here, $V = \sqrt{\langle \overline{v}'^2 \rangle}$. The mixing length may intuitively be thought of as the size of eddies themselves. We examine this possibility below, estimating L from the shape of velocity spectra. Several possibilities exist for this (see e.g. Eden, 2007), but here we chose

$$L_{S} = \frac{\int |\hat{v}(k)|^{2} k^{-1} dk}{\int |\hat{v}(k)|^{2} dk},$$
(6)

where $\overline{v}(k)$ is the Fourier component of the depth-averaged cross-channel velocity at wavenumber k. The expression can be thought of as a kinetic energy-weighted mean wavelength under the spectrum.

In the second approach, the energy-based diffusivity estimate of the GEOMETRIC framework (Marshall et al., 2012; Mak et al., 2018) is constructed as

$$K_{GEOM} \propto \sigma_E^{-1} E,$$
 (7)

where σ_E is the Eady growth rate and E is the total eddy energy. The Eady growth rate is

$$\tau_E = 0.3 \frac{f}{\overline{Ri}^{1/2}} \tag{8}$$

where f is the Coriolis parameter and Ri is the geostrophic Richardson number:

$$Ri = \frac{N^2}{|\partial U_g / \partial z|^2}.$$
(9)

308 Here

$$N^{2} = -\frac{g}{\rho_{0}} \frac{\partial \rho}{\partial z}$$

$$= \frac{\partial b}{\partial z}$$
(10)

is the squared buoyancy frequency (g is gravitational acceleration, ρ is density while ρ_0 is a reference density, so that $b = -g\rho/\rho_0$ is buoyancy) and

$$\begin{aligned} |\partial U_g / \partial z| &= |\frac{g}{\rho_0 f} \nabla \rho| \\ &= |\nabla b / f| \end{aligned} \tag{11}$$

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is the magnitude of the thermal wind shear. As said, E is the total eddy energy, i.e. the sum of the EKE and EPE (eddy potential energy). The former is diagnosed using (2) above and the latter from

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$$EPE = \frac{1}{H} \sum_{i} \frac{1}{2} \frac{\rho_{i+1} - \rho_i}{\rho_0} g\langle \eta_{i+1/2}^{\prime 2} \rangle, \qquad (12)$$

where η' is the height of an isopycnal surface above its mean level. The sum is taken over n density surfaces and, as in all of the above, the prime marks deviations from the zonal mean. Note, finally, that the mixing length diffusivity becomes identical to the GEO-METRIC diffusivity if the mixing length in the former is equal to the 'Eady scale', $EKE^{1/2}\sigma_E^{-1}$, and if only EKE is used in the definition of the latter (Wei et al., 2022).

Since the work on prognostic eddy energy budgets is still a topic of active research, we set out here to parameterize both the eddy velocity and eddy length scale from coarseresolution variables. Thus, following Visbeck et al. (1997), we write

$$V_{par} \propto \sigma_E L,$$
 (13)

³²⁶ which, moving from proportionality to equality, gives

 $K_{par} = a_1 \sigma_E L^2,$

where a_1 is some proportionality constant. Two parameterizations for the eddy length scale are then assessed, namely the WKB-approximation to the internal Rossby defor-

330 mation radius,

$$L_R = \frac{\int N \, dz}{|f|},\tag{15}$$

and the parameterized version of the topographic Rhines scale,

$$L_T = \left(\frac{V_{par}}{\beta_T}\right)^{1/2} = a_T \frac{\sigma_E}{\beta_T},$$
(16)

(14)

=

where $\beta_T = (|f|/H) |\nabla H|$ is the topographic beta parameter. Here we have assumed 334 $V_{par} = \sigma_E L_T$ (Eden & Greatbatch, 2008) and introduce a constant tuning factor a_T 335 which may, for example, reflect the resolution of the bathymetric data set used. Figure 336 S2 in the supplementary material shows that in the high-resolution channel model the 337 parameterized L_T (using $a_T = 0.1$) correspond reasonably well with L_T estimate based 338 on diagnosed EKE. Note that equation 16 and the resulting velocity (13) and diffusiv-339 ity (14) formulations are the same as suggested by Held and Larichev (1996) for poten-340 tial vorticity diffusivity in beta-plane turbulence, except for their beta being the plan-341 etary beta. Here parameterized velocity and length scales are always chosen consistently 342 i.e. the parameterized diffusivities will depend on the Eady growth rate and the squared 343 length scale of choice. 344

Finally, topographic impacts on velocity anisotropy and the phase relationship between velocity and buoyancy perturbations are also diagnosed from the high-resolution channel simulation. Anisotropy is calculated from (3) while the phase relation is assessed from the cosine of the angle between the real and imaginary parts of the cross spectrum:

$$\cos(\theta) = \frac{\hat{C}o(\overline{v}', \overline{T}')}{\left[\hat{C}o(\overline{v}', \overline{T}')^2 + \hat{Q}u(\overline{v}', \overline{T}')^2\right]^{1/2}}$$
(17)

where $\hat{C}o(\overline{v}', \overline{T}')$ and $\hat{Q}u(\overline{v}', \overline{T}')$ are the real and imaginary parts of the cross spectrum, respectively (the co-spectrum and quadrature spectrum). For analysis, we average θ across all wavenumbers (k) and over time before calculating the cosine.

3 3 Eddy fluxes in a channel model

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3.1 Equilibrated flow field and eddy fluxes

Our setup (see section 2.1) is very similar to the setup in the series of papers by 355 Wang and Stewart (2018, 2020), Wei and Wang (2021), and Wei et al. (2022), except that 356 we now have continental slopes on both sides of the channel. The forcing is also slightly 357 different as we employ a westward wind stress which, unlike in the previous studies, is 358 kept constant across the channel. The mean ocean state, however, is very similar. Since 359 the channel is in the northern hemisphere, the westward wind stress sets up a northward 360 surface Ekman transport. Thus, Ekman divergence in the south and convergence in the 361 north results in a time-mean sea surface tilt which is in geostrophic balance with a west-362 ward mean flow, as shown in the two upper panels of Figure 1. The Ekman-driven over-363 turning circulation in the y-z plane lifts up isopycnals in the south so that they slope with 364 the bathymetry there. Conversely, downwelling in the north sets up isopycnals that slope 365 against the topography. 366

Despite the simple wind forcing, the total baroclinic velocity field is rather com-367 plex (Fig. 1a, black dashed lines). In the north there is a strong westward jet over the 368 slope. This jet has a significant thermal wind shear but nonetheless extends all the way 369 to the bottom. Over the southern slope the westward flow is weaker and much more surface-370 trapped. Lower layers here are almost motionless, so the depth-averaged westward flow 371 takes on a minimum over the slope (Fig. 1b). Instead there is a broad and nearly barotropic 372 westward current which has its maximum strength immediately off the seaward side of 373 the continental slope. 374

The north-south asymmetry is clearly not only a result of the stratification being 375 weaker in the south than in the north. Thus, net impacts of mesoscale eddy fluxes must 376 be taken into account. At the most basic level, the tilted isopycnals in both regions are 377 baroclinically unstable, creating an eddy field whose residual mass transport will tend 378 to counter the Ekman-driven overturning circulation. However, because mesoscale ed-379 dies also transport momentum, the mean flow field reflects, in part, the integrated ef-380 fects of eddy momentum and buoyancy fluxes. Their combined effects can be studied in 381 the Transformed Eulerian Mean (TEM) version of the zonally-averaged zonal momen-382 tum equation: 383

$$\frac{\partial \langle u \rangle}{\partial t} - f \langle v^* \rangle = \nabla_{yz} \cdot \boldsymbol{F}_{EP} + \frac{\partial \langle \tau^x \rangle}{\partial z}, \qquad (18)$$

where τ^x is the zonal wind stress and

$$\boldsymbol{F}_{EP} = -\langle v'u' \rangle \hat{\boldsymbol{j}} + f \frac{\langle v'b' \rangle}{N^2} \hat{\boldsymbol{k}}$$
(19)

is the Eliasssen-Palm (E-P) flux. It consists of a meridional eddy flux of negative u-momentum and an eddy form stress (this term arises after thickness-weighting). In (18) we have neglected small terms describing the transport of zonal mean momentum by the meridional mean flow as well as vertical flux of momentum (see Wang & Stewart, 2018). Note, however, that the eddy form stress term, which is connected to lateral buoyancy transport under the small-slope approximation, may be thought of as a vertical momentum flux. Finally, the Coriolis term contains the *residual* meridional velocity v^* , i.e. the equivalent mass transport velocity which accounts for both the Eulerian-mean flow and the mass transport by eddy correlations.

The E-P flux from the high resolution experiment 3 (Table 2) is shown as arrows 396 in the top panel of Figure 1 and its horizontal component (i.e. $-\langle v'u'\rangle$) is shown with 397 background shading. So what we see is the direction at which the eddy field transports 398 the westward momentum originally provided by the wind. In general, both in the south 399 and in the north, the downward eddy momentum flux is suppressed over the slopes, in 400 agreement with earlier studies which indicate that baroclinic instability of suppressed 401 over continental slopes. Our estimate of the depth-averaged cross-channel buoyancy dif-402 fusivity reflects this signature by being reduced by about two orders of magnitude over 403 the continental slopes (lower panel). What these simulations show, as also seen in the 404 simulations of Wang and Stewart (2018) and Manucharyan and Isachsen (2019), is that 405 eddy motions instead bring zonal momentum laterally across the slopes near the surface 406 and dump it where the ocean bottom flattens off towards the deep basin. There, over 407 the relatively flat bottom, baroclinic instability kicks in to bring the momentum down 408 to the solid ground below. 409

As lateral eddy momentum fluxes are also clearly important in this and previous 410 simulations, optimal parameterizations will likely need to be build up around down-gradient 411 PV fluxes (see e.g. Wang & Stewart, 2018). However, it is also reasonable to expect that 412 any framework which is successful at reproducing the order-of-magnitude drop in buoy-413 ancy diffusivities seen in Figure 1 will also improve the ocean state in coarse-grained mod-414 els. So we keep this focus here. Hence, on our way towards a practical parameterization 415 of a GM diffusivity over continental slopes, we begin by examining the length scales and 416 velocity scales associated with the mesoscale eddy field. This approach is motivated by 417 the mixing length argument (Prandtl, 1925), relating diffusivity to an eddy velocity scale 418 and a length scale. However, we will also compare this approach with the energy-based 419 GEOMETRIC framework (Marshall et al., 2012; Mak et al., 2018). 420

3.2 Eddy length and velocity scales

421

Estimates of eddy length and velocity scales are shown in Figure 2. The length scale 422 is estimated from (6), i.e. by calculating a spectral-weighted mean wavelength associated 423 with north-south velocity perturbations. When normalized by its mean value across the 424 channel the length scale shows a near-universal shape across the various model runs (up-425 per left panel). There is a broad maximum over the mid-basin before length scales drop 426 over the continental slopes on both sides. There is, however, a consistent local maximum 427 over mid-slope on the northern (prograde) side, coinciding with the maximum in mean 428 zonal velocity (Fig. 1). Scales then flatten out or even increase over the shelf regions. As 429 with other diagnostics below, we will largely ignore shelf values from the discussion due 430 to the model grid not fully resolving the deformation radius there and due to the prox-431 imity to model walls. For the eddy velocity scale we show the square root of depth-averaged 432 EKE. When normalized with the across-channel average (upper right panel), the eddy 433 velocity scale in all runs is reduced over the southern slope, save for a slight increase over 434 the upper parts of the slope. In stark contrast, the northern slope is dominated by a large 435 maximum, also that one centered over the upper parts of the slope. The eddy velocity 436 then drops off and flattens out over both shelf regions. 437

It would seem that forming a diffusivity from the product of these diagnosed length
and velocity scales may reproduce the observed reduction over the southern retrograde
slope (Fig. 1), at least qualitatively. But it should also be clear that this procedure would

produce a diffusivity maximum over the northern slope—for which there is absolutely
no indication in the model fields. We will return to this issue below but first examine
possible scaling approximations to the observed length and velocity scales.

We start by comparing the diagnosed L and V with the classical Stone (1972) pre-444 diction. So the diagnosed length scale is normalized by the internal deformation radius 445 L_R (15) and the diagnosed velocity scale is normalized by the product of the Eady growth 446 rate (8) and the deformation radius, so $V_{scaled} = \sigma_E L_R$. Leaving out any constant pref-447 actors here, we see that both length scales and velocity scales are well represented by 448 449 Stone-type scaling in the mid-basin (middle panels). The normalized length scales then drop slightly over the lower parts of both slopes, indicating that the deformation radius 450 overestimates scales there somewhat. Finally, there is a dramatic rise in normalized scales 451 over the upper parts of both slopes as the deformation radius drops towards the shal-452 low shelves. As with length scales, the normalized velocities drop over the lower parts 453 of the slopes before rising again over the upper parts. The normalization brings the EKE 454 peak over the upper parts of the slope down to values similar to those seen over the mid-455 basin, as the EKE peak there coincides with the region of stronger thermal shear. 456

Finally, following the suggestion by (Eden, 2007) and (Jansen et al., 2015), we normalize by selecting a smooth minimum of length scales:

$$L_{min} = \frac{L_R L_T}{L_R + L_T},\tag{20}$$

where L_T is the topographic Rhines scale (16). The results are similar over the central basin since the deformation radius is the smaller of the two scales there (the Rhines scale blows up). But now both normalized length and velocity scales peak over the slopes where the Rhines scale becomes the smaller of the two—and is quite clearly too small to explain the observed fields. As such, consideration of the topographic Rhines scale does not seem to bring any improvement in skill in predicting eddy length scales and velocity scales over the continental slopes.

But before rejecting this scaling choice it is worth noting again that the construction of a diffusivity from the original (non-normalized) length and velocity scale estimates would obviously result in a diffusivity maximum over the central northern slope. Such a maximum is in no way suggested from Figure 1. What may be missing from the story here is a consideration of how eddy velocity anisotropy and the velocity-temperature phase relationship may act to bring diffusivities down over the slopes. So we turn to this issue next.

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459

3.3 Anisotropy and phase relationship

Figure 3 shows the eddy velocity anisotropy A(3) and the cosine of the phase an-475 gle between real and imaginary parts of the \overline{v}' and \overline{T}' cross-spectra (17). As expected, 476 the eddy velocity field is close to being isotropic in the middle of the basin (upper panel). 477 Values there are around 0.6, implying that cross-channel velocity fluctuations \overline{v}' are in 478 fact slightly larger than along-channel fluctuations \overline{u}' . The eddy fluctuations then be-479 come much more anisotropic towards the continental slopes, with A values over the up-480 per parts of the slope close to 0.1 (0.2) in the north (south). This implies that \overline{v}' is about 481 70% (50%) smaller than \overline{u}' in the north (south). A notable exception is a peak over the 482 center of the northern slope where \overline{v}' is about 50% larger than \overline{u}' . We have also tested 483 other measures of anisotropy, such as the velocity based measure used by K. Stewart et 484 al. (2015) that takes rotational aspects into account, and the results are similar to those 485 shown here. 486

The general behavior of increased anisotropy over the slopes, with $|\overline{v}'| < |\overline{u}'|$, will work to reduce the scale-based diffusivity there. But the variations in A from mid-basin values are not great and the mid-slope peak (where $|\overline{v}'| > |\overline{u}'|$) would actually increase the estimates there. So we conclude from this that velocity anisotropy alone can not explain the consistent drop in diffusivity by two orders of magnitude over the slopes seen in Figure 1. The phase relation, however, is able to explain the observed order-of-magnitude drop over the slopes, as the \overline{v}' and \overline{T}' fields are close to 90° out of phase there (middle panel). Importantly, the low phase agreement over the northern slope largely cancels the local peak in anisotropy.

The lower panel in Figure 3 shows the product of A and $\cos(\theta)$ (blue lines), an indication of their combined effect. The total suppression is dominated by the information carried in the phase relationship, and velocity anisotropy primarily plays a role near the edges of the two slopes. The suppression over the slopes amounts to more than an order of magnitude, so it is an effect which clearly needs to be parameterized.

The slope-dependent prefactors which previous studies have needed to invoke to explain buoyancy diffusion in similar channel simulations are, in effect, attempts at such parameterization (Brink, 2012, 2016; Hetland, 2017; Wang & Stewart, 2020; Wei et al., 2022). However, at this point we temporarily detour from those earlier studies and instead take as a starting point an expression which bears some resemblance to the final form of the mean-flow suppression factor proposed by Ferrari and Nikurashin (2010). Thus, we construct an 'eddy efficiency' factor as

$$E_{eff} = \frac{1}{1 + a_2 \left(U_{bc}^2 / V^2 \right)}.$$
(21)

Here, U_{bc} is the large-scale baroclinic flow speed obtained after subtracting the depth-509 averaged velocity, V is the eddy velocity scale and a_2 is an additional scaling factor which 510 we here take to be constant. The expression does not have a rigorous basis but a sim-511 ple intuitive interpretation. U_{bc} is directly related to the thermal wind shear and, hence, 512 to the underlying energy source of baroclinic instability (e.g. Sutyrin et al., 2021). Qual-513 itatively, if U_{bc} is large and the flow is baroclinically unstable, one would expect V to 514 be relatively large, giving $E_{eff} \sim O(1)$ (unless a_2 is very large). But if V remains small 515 despite large U_{bc} , some dynamical constraints must be reducing the efficiency of baro-516 clinic energy conversion, implying $E_{eff} \ll 1$. The above interpretation hinges on the 517 parameterized V being an adequate approximation of the actual eddy velocity scale. 518

We evaluate (21) at each depth but then take the mean over the water column. The 519 large-scale baroclinic flow U_{bc} is extracted directly from the resolved (and zonally-averaged) 520 velocity field, while the eddy velocity is parameterized from (13). The lower panel of Fig-521 ure 3 shows the resulting efficiency factor, using L_{min} as length scale. The prefactor a_2 522 has been manually tuned to match the mid-basin values of $A \cdot cos(\theta)$, but it is clear that 523 using $L = L_T$ can produce a suppression over the continental slope which is in qual-524 itative agreement with $A \cdot \cos(\theta)$ over both slopes for a range of different simulations. 525 Allowing for another prefactor in front of the whole expression (effectively our a_1 param-526 eter) would enable a good quantitative match both over the mid-basin and the slope re-527 gions. In contrast, the comparison clearly shows that using L_B as length scale does not 528 reproduce the needed behavior over the slopes. We note that several tests with using the 529 thermal wind instead of U_{bc} and with evaluating (21) with depth averaged-quantities (in-530 stead of taking the mean of a depth dependent expression) all produce similar results. 531 Here we chose to use U_{bc} due to the ease of implementation at coarse resolution. 532

⁵³³ 3.4 Parameterized diffusivity

Given the above results, we proceed to examine parameterizations of the diagnosed buoyancy diffusivity. The aim is to capture the order-of-magnitude reduction in diffusivities from the mid-basin to the slope regions. The results are shown in Figure 4 where we distinguish between partial parameterizations (panels a-c) and full parameterizations (panels d-f). The partial parameterizations include extensive information about the mesoscale field itself (such as EKE and L_S) which would not be directly available in a coarse-resolution

model, whereas the full parameterizations only use information of the zonally and temporally-540 averaged background buoyancy field, Coriolis frequency, and topographic beta, and are 541 therefore suitable for direct implementation in any existing coarse-resolution model. The 542 one exception is an estimate (VII) which combines diagnosed EKE with a parameter-543 ized length scale. Panels a and d are from one single simulation, showing both the ac-544 tual depth-averaged diffusivity diagnosed (black line) and the various approximations 545 (distinguished by Roman numerals and color). Panels b-c and e-f then show statistics 546 over both slope regions collected over the whole range of simulations. 547

548 A first thing to notice from the partial parameterizations is that the mixing length (I) and GEOMETRIC (II) approaches behave nearly identically. This suggests that i) 549 EKE and EPE are proportional to each other, as found in the simulations of Wei et al. 550 (2022), and ii) that our diagnosed eddy scale, L_S , reflects the 'Eady scale' $L_E = \sqrt{EKE\sigma_E^{-1}}$ 551 (Larichev & Held, 1995; Jansen et al., 2015; Kong & Jansen, 2021). As also noted by Wang 552 and Stewart (2020), both approaches thus give reduced diffusivities over the southern 553 retrograde slope (squared Pearson correlation coefficient r^2 is 0.49 and 0.66, for I and 554 II, respectively; note that $r = cov(x, y)/(\sigma_x \sigma_y)$). But the reduction is still underesti-555 mated by up to one order of magnitude and reflected as a large relative error. More im-556 portantly, over the prograde slope in the north, both approaches result in a serious qual-557 itative mismatch, as the high EKE and EPE levels there (EKE seen in Fig. 2; EPE not 558 shown) produce a non-existing diffusivity peak over mid-slope. Although σ_E also peaks 559 over the northern slope (not shown), this is not enough to pull down K_{GEOM} there. We 560 note that the peak in K_{GEOM} over the southern shelf might be spurious as the defor-561 mation radius is not well resolved there, which is why we have left the shelves out of this 562 analysis. 563

The observed discrepancies, particularly the qualitative mismatch over the north-564 ern slope, confirms that scaling arguments alone are unable to reproduce the diagnosed 565 diffusivities—even with knowledge of eddy energy levels and eddy sizes. It is worth not-566 ing that this is in line with previous studies (e.g. Wang & Stewart, 2020; Wei et al., 2022) 567 who found that such scaling estimates needed to be multiplied by slope-dependent pref-568 actors to align with diagnosed diffusivities. Here, we instead explicitly examine the role 569 of velocity anisotropy and the velocity-temperature perturbation phase relationship. Ac-570 counting for the diagnosed velocity anisotropy, so that \sqrt{EKE} will be replaced with v'571 (III), improves the mixing length estimate slightly but not nearly enough. Multiplying 572 the two estimates by $A\cos\theta$, however, largely removes the diffusivity peak in the north 573 and even produces a clear suppression over the slope—for both the mixing length and 574 GEOMETRIC estimate (IV and V). The values are still higher than the observed dif-575 fusivity (mean absolute relative error stays above 100%) but r^2 increases to 0.71 and 0.77 576 for (IV) and (V), respectively. Over the retrograde slope in the south the match is even 577 closer, with r^2 reaching 0.92 and 0.85 for (IV) and (V), respectively. 578

Guided by the observed agreement between the mixing length and GEOMETRIC estimates above, we focus on the former approach when examining how well full parameterizations can do. So we assume that a diffusivity can be written as the Eady growth rate times the square of a length scale. Including our efficiency factor, the effective diffusivity becomes

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$$K = a_1 \frac{K_0}{1 + a_2 \left(U_{bc}^2/V^2\right)},\tag{22}$$

where $K_0 = \sigma_E L^2$ is the scaling estimate of diffusivity before considering the efficiency factor and where, as discussed above, we have a choice to make for the length scale. For the constant parameters, we chose $a_1 = 0.25$ so that mid-basin values of VI closely match with the diagnosed diffusivities across all cases, and we use the same a_1 for (VIII) and (IX), whereas for (VII) we use $a_1 = 0.66$. Coefficients a_2 and a_T are then tuned manually such that the correlation between the diagnosed diffusivities and estimates (VIII) and (IX) over the slopes (Fig. 4f) is maximized across all cases. We start by looking at K_0 first. Using the traditional Stone (1972) expression where the length scale is taken to be the internal deformation radius everywhere, seriously overestimates diffusivities over both slope regions (VI). The estimate, in fact, bears some resemblance with both the mixing length and GEOMETRIC estimates based on diagnosed eddy quantities (I and II), but with even larger discrepancies over the slope regions.

Switching temporarily to a hybrid estimate, with a diagnosed velocity scale but a 597 mixing length set to be the smooth minimum of the deformation radius and the param-598 eterized topographic Rhines scale (VII; $a_T = 0.5$), improves the skill considerably, giv-599 ing in suppressed diffusivities over both slopes. We note that over the slopes, where L_T 600 is selected, the diffusivity estimate is essentially a topographic version of the Rhines-based 601 estimate tested by Jansen et al. (2015). They too found that this scaling (with plane-602 tary rather than topographic beta) reproduced diagnosed diffusivities well in an two-layer 603 channel model. Interestingly, in our simulations the skill of this hybrid parameterization 604 is better than both estimates using full eddy quantities (I and II). Our interpretation is 605 that our parameterized L_T is a better estimate of the eddy mixing length than the di-606 agnosed eddy size L_S (which, from the close correspondence between I and II must re-607 flect the Eady scale L_E). 608

Finally, using the full parameterization with Eady growth rate and the minimum 609 length scale squared (VIII) leads to further improvements over the slopes where the pa-610 rameterized diffusivities now drop by nearly two orders of magnitude, approaching the 611 behavior of the diagnosed diffusivities. Multiplying this estimate with the parameter-612 ized efficiency factor (IX) improves the match somewhat over both slopes, especially in 613 terms of the mean absolute relative error, which drops from 215% (70%) to 116% (53%) 614 while r^2 increases from 0.73 (0.62) to 0.79 (0.64) over the southern (northern) slope. We 615 note that across all parameterizations the correlation is higher over the southern slope 616 than the northern slope, whereas the relative error shows the opposite pattern. This in-617 dicates that if one would further tune a_1 , it would be possible to further reduce the rel-618 ative error metric, especially over the southern slope. However, here, for simplicity, we 619 chose a_1 such that the diagnosed and parameterized diffusivities match in the central basin. 620 We also note (not shown) that scaling by E_{eff} improves the hybrid estimate (VI) such 621 that its performance becomes similar to estimate (IX). 622

A summary of these findings is in order. The parameterized eddy velocity scale and 623 eddy mixing length, whether based on L_R or L_T , do not reproduce their diagnosed counterparts (\sqrt{EKE} and L_S) over the continental slopes, as seen from Figure 2. But the 625 failure of diagnosed eddy energy and L_S in predicting a diffusivity over the slopes, par-626 ticularly over the prograde slope in the north, also indicates that these eddy quantities 627 do not give the full story. In particular, the eddy scale—which also appears to be related to EKE via the Eady length scale $L_E = EKE^{1/2}\sigma_E^{-1}$ —is not a good predictor of the 628 629 effective mixing length. Accounting for the phase relationship between eddy velocity and 630 buoyancy perturbations and, to a lesser degree, the eddy anisotropy brings the estimates 631 much closer to the actual diffusivity. Our attempts at full parameterizations then clearly 632 shows that L_T is a much better choice than L_R over both continental slopes. And the 633 comparison between estimates VII and VIII even suggests that $V_{par,T} \propto \sigma_E^2/\beta_T$ is a 634 slightly better predictor for the effective eddy mixing velocity over the slopes than the 635 square root of eddy kinetic energy. Thus, a further consequence appears to be that the 636 need for an explicit suppression factor (our E_{eff}) for the fully parameterized diffusiv-637 ity becomes smaller. We leave further examination of this topic for later and instead carry 638 on to see what effects the parameterized expression (IX) will have when used to actu-639 ally operate in coarse-grained, non-eddying, simulations. 640

3.5 Performance in a coarse-resolution channel simulation

641

Before moving to realistic global simulations, we test the proposed parameteriza-642 tions in a coarse-resolution channel setup. This setup has the same geometry as the high-643 resolution channel setup, but differs in resolution (from 2 km to 32 km) and in that the 644 the GM-Redi parameterization scheme is activated. The model is forced and run sim-645 ilarly to the high-resolution setup, but some parameter settings, such as timestep and 646 viscosity, are necessarily modified. Acknowledging that the channel setup is quite spe-647 cific, and in anticipation of the global simulations to be studied next, we have kept tun-648 649 ing of the coarse-resolution channel setup to a minimum.

Figure 5 shows parameterized buoyancy diffusivities and the time-mean density field 650 in three of the equilibrated simulations that had wide continental slopes but differing ini-651 tial stratification. We chose to use the wide continental slope case because that is best 652 resolved at 32 km resolution. We also show the corresponding diagnosed quantities from 653 the corresponding high-resolution simulations for comparison (black lines). As in Fig-654 ure 4, we show the three versions of the parameterized diffusivity (and corresponding den-655 sity structure): one using the internal deformation scale (with $a_1 = 8$), one using the 656 minimum between internal deformation scale and topographic Rhines scale (with $a_1 =$ 657 8 and $a_T = 0.1$) and, finally, one using the minimum and also applying the parame-658 terized eddy efficiency factor (with $a_1 = 32$, $a_2 = 1$, and $a_T = 0.1$). Choosing $a_T =$ 659 0.1 is consistent with the high-resolution model diagnostics as it provides a reasonable 660 fit in terms of the order of magnitude between the full and parameterized versions of the 661 topographic Rhines scale (see Figure S2 in supplementary material). Together, constants 662 a_1 and a_T scale the diffusivity estimate by 0.08 (without E_{eff}) and 0.32 (with E_{eff}) over 663 the sloping regions. These appear similar to the scaling coefficients used in Figure 4 (~ 0.25 , 664 see figure caption) as well as previously reported values with mixing length theory: 0.33665 by Wang and Stewart (2018) and 0.17 by Wei et al. (2022), both focusing on buoyancy 666 diffusivity, as well as 0.2 by Wei and Wang (2021), although they focused on along isopy-667 cnal diffusivity. 668

The tuning of a_1 was done to approximately match the mid-basin parameterized 669 diffusivity with the corresponding diagnosed diffusivity in the high-resolution simulations. 670 And yet, Figure 5 shows that the parameterized diffusivities have a clear north-south gra-671 dient in the magnitude whereas their diagnosed counterpart does not (panels a-c). The 672 discrepancy is caused by a stronger difference in stratification between north and south 673 at coarse resolution (see Figure S3 in the supplementary material) which directly impacts 674 the internal deformation radius used by the parameterization over the central flat region. 675 Despite this, we push forward and review the performance of the different parameter-676 izations over the continental slopes. The deformation scale-based parameterization (Fig. 677 5a-c, orange line) clearly does worst, producing local diffusivity maxima over both slopes, 678 as also seen in Figure 4 (blue line). Thus, there are only very weak lateral density fronts, 679 or thermal wind shears, over the continental slopes. Essentially, the high parameterized 680 diffusivities effectively wash out any density front there (see Fig. 5d–f for density struc-681 ture and Fig. S3 for the density gradients). This, it should be remembered, is exactly 682 the effect one wishes to reduce with a slope-sensitive parameterization. 683

The run using a parameterization which selects the minimum of the two length scales 684 does much better over both continental slopes where the topographic Rhines scale kicks in. With suppressed diffusivities, the density front which is set up by the topographic 686 PV gradient is no longer washed out completely, especially in the north (see Fig. 5g-l 687 for density structure and Fig. S3 for the density gradients). The result is an enhanced 688 689 thermal wind shear over the northern slope, albeit with a lower absolute strength than in the high-resolution simulation (about a factor two lower). In the south, where the ver-690 tical stratification is much weaker, the parameterization is not able to set up a strong 691 thermal wind shear, although the location and strength of the surface density front has 692 improved. Further scaling by the eddy efficiency E_{eff} (Fig. 5, green) enhances the dif-693

fusivity reduction slightly in the north, but not necessarily in the south. Therefore, the feedback to the resolved fields strengthens the baroclinic jet in the north further, but not in the south.

Clearly, there remains significant discrepancies between the low-resolution and high-697 resolution fields. Some may be due to higher levels of implicit (numerical) diffusion in 698 the coarse-resolution simulations, but others likely reflect limitations in the parameter-699 ization. More extensive tuning, e.g. based on matching the baroclinic transport over the 700 slopes, would likely bring the coarse resolution simulations closer to the high-resolution 701 fields. But the aim here has primarily been a qualitative examination, and even with a 702 minimum of tuning the behavior over the slopes is robust, as the response to the differ-703 ent parameterizations is consistent across all cases. All in all, the above results are en-704 couraging in that the Rhines-based parameterization is able to reduce wash-out of the 705 density fronts over the slopes—particularly over the prograde slope in the north. How-706 ever, although the channel setup is a reasonable test bed for development, it is extremely 707 idealized and lacks multiple features from the real world (e.g. variable Coriolis param-708 eter, uneven topography and complex atmospheric forcing). Therefore, we also test the 709 slope-aware parameterization in the realistic global domain next. 710

711 4 Realistic global model simulations

712

4.1 Eddy parameterization adjustments

We carry out a control simulation and 5 different perturbation experiments. For 713 simplicity, the focus will mostly be on a comparison between the control simulation and 714 two of the perturbation experiments. All of these simulations operate with 2D diffusiv-715 ities based on the depth-averaged Eady growth rate and a square length scale, as in (14). 716 The control run selects a length scale from the minimum of the internal deformation ra-717 dius and the planetary Rhines scale (not the topographic Rhines scale). Then, in two 718 distinct 'topo' runs we i) introduce the topographic Rhines scale as an additional length 719 scale and ii) also turn on the eddy efficiency factor E_{eff} . The OMIP 'topo' runs then 720 differ slightly from the coarse-resolution channel setup in the choice of constant scaling 721 factors. The constant factor a_1 which scales the overall diffusivity magnitude is set to 722 3 and factor a_2 used in E_{eff} is set to 1. In addition, we adjust L_T by trying $a_T = 1$ 723 and $a_T = 0.5$. We view these constants as tuning factors specific to one particular setup; 724 for example, a_T is impacted both by the quality of the parameterized Rhines scale (Fig. 725 S2) as well as the bottom topography dataset. Here we calculated the topographic beta 726 parameter based on the model's bathymetry. An improved approach might be to take 727 a high-resolution bathymetry product and low-pass filter it up to the mesoscale—e.g. to 728 the deformation radius or slightly above—before calculating the slopes. Further anal-729 ysis is left for future studies, but in Figure S1 (supplementary material) we show that 730 the model bathymetry-based β_T is a reasonable fit to high resolution bathymetry-based 731 β_T (using 15 second resolution bathymetry by Sandwell et al., 2022) after filtering to the 732 local deformation radius. Finally, in all runs the diffusivity magnitude is scaled down with 733 a resolution function (Hallberg, 2013) when the deformation radius is resolved by the 734 model grid. 735

For simplicity, the along-isopycnal (Redi) tracer diffusivity is set to be the same as the GM diffusivity. We have assessed the impact of this choice in a set of additional experiment included in the supplementary material (Fig. S4) and summarized the findings in section 4.2.

To put the OMIP experiments in some context, it should be mentioned that the model settings for the control run are similar to the NorESM model version used in the latest Climate Model Intercomparison Project (CMIP6) except for some aspects of the GM diffusivity formulation. The CMIP6 version of the model included a mixing length formulation where the length scale was selected as the minimum of the internal deformation radius and the planetary Rhines scale—as in our control simulation. However,
the local Eady growth rate was then evaluated at each model level, rendering a 3D profile for both eddy driven advection (GM) and for along isopycnal mixing (Redi). Finally,
the scaling-based diffusivity was adjusted by a zonal velocity-dependent mean flow suppression following Ferrari and Nikurashin (2010), and as in the experiments here, a resolution function (Hallberg, 2013) was also used.

The lack of vertical structure of the 2D parameterization proposed here, turned out 751 752 to be a clear deficiency in the global domain as our initial simulations showed an unrealistically strong sensitivity to bottom slopes in the low and mid-latitude deep ocean. 753 For example, large reductions in the parameterized diffusivity across mid-ocean ridges 754 were not seen in eddy-permitting studies that diagnosed eddy diffusivity in the global 755 domain (e.g., Bachman et al., 2020). Therefore, to reduce the topographic impact on eddy 756 fluxes in strongly stratified low and mid-latitude regions, we added an ad hoc 'limiter' 757 of topographic effects—based on the assumption that if the resolved flow does not feel 758 the bottom then it is unlikely that mesoscale eddies would do so either. Specifically, the 759 topographic Rhines scale is scaled by $cos(\alpha)^{-10}$ which rapidly increases the topographic 760 Rhines scale when the angle α between the resolved depth-averaged flow and the bot-761 tom slope tangent vector deviate by more than $\sim 30^{\circ}$ i.e. when the resolved depth-averaged 762 flow is not aligned with the bottom slope. 763

4.2 Model response in the global domain

764

As expected, introducing the topographic Rhines scale leads to locally reduced dif-765 fusivities over sloping topography, as shown in Figure 6 (top row). The effect is enhanced 766 at high latitudes with a $\sim 50\%$ reduction over Arctic and Antarctic continental slopes. 767 Bringing in the eddy efficiency E_{eff} (see Figure S6 and text S6 in the supporting infor-768 mation for an estimate of the E_{eff} pattern) leads to additional and more severe diffu-769 sivity reduction globally, also away from topographic features (bottom row). This is also 770 in agreement with recent studies (admittedly focusing on Redi mixing) that found that, 771 at large scales, the scaling by mean-flow dependent suppression has the largest impact 772 on diffusivity (Stanley et al., 2020; W. Zhang & Wolfe, 2022; Holmes et al., 2022). Note 773 that in the tropics, the diffusivity is limited by the grid resolution function (Hallberg, 774 2013), i.e. the diffusivity is reduced when the grid size is smaller than the local defor-775 mation radius. Therefore, the large relative reduction in tropical diffusivity is small in 776 absolute terms and less important there as transport is dominated by the resolved flow. 777 Finally, we note that a comparison between the top and the bottom rows in Figure 6 shows 778 that in multiple continental slope regions, especially in the Arctic and around Antarc-779 tica, the eddy efficiency simply enhances the response seen with the topographic Rhine 780 scale. Indeed, the diffusivity reduction due to introducing the topographic Rhines scale 781 and due to eddy efficiency are close to linearly additive (not shown). 782

As the impact of eddy efficiency on diffusivity is more broad, its impact on flow speed, 783 temperature, and salinity is also more widespread than the impact of the topographic 784 Rhines scale alone. Table 3 collects bias reductions (relative to the control case) across 785 5 different experiments while Figures 7–9 show the spatial patterns for subsurface (100-786 200 m) current speed and temperature, as well as zonal-mean temperature and zonally-787 integrated overturning streamfunction anomalies for the two 'topo' experiments that are 788 in focus here (the overturning volume streamfunction is diagnosed by dividing the online-789 calculated overturning mass streamfunction with a constant reference density, $\rho_0 = 1000$ 790 kg m $^{-3}$). We show results for the subsurface response since the surface response in these 791 forced simulations is strongly forced by the non-responsive atmosphere. Both the topo-792 graphic Rhines scale alone and its combination with eddy efficiency increase the mean 793 kinetic energy of the resolved flow globally (at 100-200 m depth, by 2.7% and 10.5%, 794 respectively). This increase is especially noticeable over sloping bathymetry where the 795

two impacts contribute approximately equally to the overall increase (over slopes where $\beta_T > 5 \cdot 10^{-10} \text{m}^{-1} \text{s}^{-1}$ kinetic energy at 100–200 m depth increases by 9.1% and 20.8%, respectively). The two modifications also warm the ocean below the global thermocline and cool the surface, reducing the overall temperature bias at depth. But they increase the temperature bias at the thermocline (Table 3; Fig. 9a,c).

Overall, the mean overturning response in the 'topo' runs is characterized by a pos-801 itive (cyclonic) anomaly which implies that the Atlantic overturning cell and the Dea-802 con cell in the Southern Ocean strengthen, whereas the Antarctic Bottom Water cell and 803 the shallow surface overturning cells within the subtropical and subpolar gyres weaken. 804 These changes generally reduce biases. The simulated strength of the Atlantic overturn-805 ing at $26^{\circ}N$ is 15.5 Sv in the control simulation, 17 Sv when topographic Rhines scale 806 is considered, and 18 Sv with the addition of eddy efficiency, whereas the observational 807 estimate from the RAPID array ($\sim 26^{\circ}$ N) is 17±3.3 Sv (Frajka-Williams et al., 2019). 808 The Antarctic bottom water cell at 32° S weakens from 26.0 Sv in the control simulation 809 to 23.5 Sv with topographic Rhines scale and 20.3 Sv with addition of eddy efficiency, 810 whereas inverse modelling suggest 20.9 ± 6.7 Sv (Lumpkin & Speer, 2007). The Deacon 811 cell strengthens from 13.2 Sv in the control simulations to 15.2 Sv with the topographic 812 Rhines scale and 18.4 Sv when eddy efficiency is considered, whereas previous modelling 813 estimates (Döös et al., 2008) and observational estimates (Speer et al., 2000) suggest a 814 strength of 20 Sv and 20–25 Sv, respectively. 815

Some more specific impacts of the topographic Rhines scale and eddy efficiency are 816 a poleward shift and strengthening of the boundary and slope currents, with E_{eff} gen-817 erally speeding up the boundary currents at locations where observations show the core 818 of the currents (Fig. 7, observed currents in black contours). Changes in the net volume 819 transports in most key passages remain small (Table 4), but the results show a strength-820 ening of the ACC (Drake Passage transport; reduced bias), a general enhancement of wa-821 ter exchange between the Arctic and mid-latitudes (opposing influence on the bias in dif-822 ferent straits), and strengthening of the Gulf Stream (Florida–Bahamas strait transport, 823 reduced bias). The spinup of the ACC is a direct consequence of reduced diffusivities, 824 allowing for stronger thermal wind currents. In the northern North Atlantic, the cur-825 rent speed response is directly reflected in the temperature response as the Atlantic Wa-826 ter warms up along its path from the Nordic Seas to the Arctic (Fig. 8, reduced bias). 827 Despite the speed-up of the Gulf Stream off the North American coast, its observed turn-828 ing around Grand Banks off Newfoundland is not reproduced. Due to this deficiency, the 829 cold bias off Newfoundland strengthens (Fig. 8). This cold bias is a long standing issue 830 in coarse resolution ocean models (Tsujino et al., 2020) and reducing the diffusivity along 831 the current path or along the shelf break clearly does not mitigate the bias. We spec-832 ulate that, similar to the southern retrograde slope in the channel configuration and re-833 cent results on the Gulf Stream reported by Uchida et al. (2022), the eddy momentum 834 flux convergence that is not included in the parameterization plays a crucial role in de-835 termining the current path. 836

The overall overturning response leads to increasing heat transport towards the north-837 ern hemisphere (Fig. 10). The northern hemisphere subtropical peak in northward heat 838 transport in the Atlantic basin (globally) is 0.83 PW (1.07 PW) in the control simula-839 tion, 0.91 PW (1.15 PW) when topographic Rhines scale is considered, and 1.00 PW (1.26 840 PW) with the addition of eddy efficiency, whereas Trenberth et al. (2019) estimate ap-841 proximately 1.1 PW (1.6 PW). Breaking down the zonally-integrated impacts into re-842 solved and parameterized eddy components illustrates how the reduced eddy mass trans-843 port across the ACC (Fig. 10, panels a–b) also leads to less southward heat transport 844 (Fig. 10, panels c-e) and therefore a cooling of the Southern Ocean surface, but also warm-845 ing over the continental slopes (Fig. 8). Both these effects reduce the bias in the model. 846 Note that the heat transport response is dominated by eddy-driven advection with a smaller 847 contribution due to the eddy diffusion (Fig. 10, panels d-e). In contrast to the South-848

ern Ocean, in the northern mid-latitudes the overall northward mass and heat transport increase as the mean overturning spins up (Fig. 10 panels a and c; Fig. 9 right panels) and the eddy contributions actually weaken (Fig. 10, panels b, d–e).

We note again that in these OMIP experiments we have taken the eddy driven ad-852 vection ('GM') and isopycnal mixing ('Redi') coefficients to be the same, making the ori-853 gin of the response ambiguous. However, with a set of additional experiments (supple-854 mentary material, Figure S4) we show that the circulation response is mostly due to GM 855 and, to a large extent, can be constructed as a sum of experiments where GM and Redi 856 857 are changed separately (i.e. the response is linearly additive). The detailed temperature response, especially the thermocline bias, is sensitive to the treatment of the along-isopycnal 858 mixing, but here the combined response is not linearly additive. The non-linear temper-859 ature response suggest that when developing and tuning a model system the changes to 860 GM and Redi parameterizations should be made simultaneously. 861

⁸⁶² 5 Discussion

Our study has focused on a relatively small range of parameterization choices, es-863 sentially i) re-examining the topographic Rhines scale as a relevant mixing length and 864 ii) checking the importance of an additional suppression factor which we have called the 865 eddy efficiency E_{eff} . The studies by Wang and Stewart (2020) and Wei et al. (2022) did 866 a more comprehensive sweep over possible parameterization choices but did not anal-867 yse prograde and retrograde bottom slopes under one and the same framework, which 868 has been the intention here. Also, to the best of our knowledge, the current OMIP sim-869 ulations constitute the first assessment of the impacts of a topographically-aware GM 870 parameterization in realistic global ocean models. As such, this work should be taken 871 as a pragmatic investigation into what can be achieved with simple parameterization ap-872 proaches applied to existing models that do not contain a prognostic eddy energy equa-873 tion (which in itself requires parameterization choices). As with all parameterizations, 874 the options examined here are far from perfect, and below we discuss some shortcom-875 ings and unresolved questions. 876

877

5.1 The relevance of the topographic Rhines scale

Earlier idealized model studies have given conflicting evidence for the relevance of 878 the topographic Rhines scale. Jansen et al. (2019) and Kong and Jansen (2021) reported 879 that using a generalized Rhines scale which accounts for both planetary and topographic 880 beta in their eddy parameterization of flows in an idealized ACC-like domain improved 881 their model skill. More in line with our work here, the idealized channel studies of Wang 882 and Stewart (2020) and Wei et al. (2022) found the topographic Rhines scale to be a use-883 ful choice over retrograde slopes—but not over prograde slopes. This conclusion was drawn, 884 however, after an empirical slope-dependent prefactor was applied in the retrograde case 885 but not in the prograde case. Both studies also constructed diffusivities from diagnosed 886 depth-averaged EKE. In other words, they set the eddy velocity scale to be $V = \sqrt{EKE}$ 887 and then defined $L_T = \sqrt{V/\beta_T}$, i.e. using the actual definition of the topographic Rhines 888 scale. However, here we find that over both prograde and retrograde slopes, a full pa-889 rameterization using (14) with $L_T = a_T \sigma_E / \beta_T$, better reproduces diagnosed diffusiv-890 ities from our high-resolution simulations than partial a parameterization using (5) with 891 $L_T = \sqrt{V/\beta_T}$ (see Fig. 4). Although not analyzed in detail, our hypothesis is that the 892 full parameterization produces better results because it leads to a β_T^{-2} dependence for the overall diffusivity, instead of the $\beta_T^{-1/2}$ dependence when using (5) and the actual definition of L_T . The different power dependence is important because β_T varies by sev-893 894 895 eral orders of magnitude across the slopes whereas EKE and σ_E vary by less than one 896 order of magnitude (see e.g Fig. 2). 897

5.2 The interpretation of E_{eff}

913

The above results also suggest that some of the discrepancy between the pure scalingbased diffusivity and the diagnosed diffusivity is contained in the suppression factor which ours and other studies have pointed to. Although we don't try to identify the underlying dynamics here, the suppression is reflected in an imperfect phase relationship between eddy velocity and buoyancy perturbations, possibly causing larger suppression over prograde slopes.

It is worth nothing that our E_{eff} may be related to the topographic Eady prob-905 lem of Blumsack and Gierasch (1972). This connection becomes apparent if we evalu-906 ate the 2D version of (21). We begin by setting $U_{bc} = U_{tw}$, where U_{tw} is the top-to-907 bottom thermal wind shear (a 2D quantity). Then we first consider the slope region where 908 the topographic Rhines scale will be the relevant length scale. So, here, $V = \sigma_E^2 / \beta_T$, 909 where σ_E is now the depth-averaged (2D) Eady growth rate. Noting that in the Eady 910 model, where both N^2 and $\partial U_g/\partial z$ are constant, $\sigma_E = 0.3 \cdot U_{tw}/L_R$. This allows us 911 to rewrite (21) as 912

$$E_{eff} = a_1 \frac{1}{1 + a_3 \left(\beta_T L_R^2 / U_{tw}\right)^2}$$

= $a_1 \frac{1}{1 + a_3 \delta^2},$ (23)

where a_3 is a modified tuning factor. Here $\delta = \beta_T L_R^2 / U_{tw}$ is the slope parameter of Blumsack and Gierasch (1972) which measures the ratio between topographic and isopycnal slopes. Equation 23 is further supported by Figure S5 (in the supplementary material) showing reasonable correspondence (up to a constant) between U_{bc}^2 / V^2 and δ^2 .

This expression is interesting not only because it brings in the controlling param-918 eter of the modified Eady problem but also for its similarity to the slope-dependent pref-919 actor used by Wang and Stewart (2020) over retrograde slopes in the parameter regime 920 where the bottom slope is not much larger than the isopycnal slope. Their prefactor F_{MLT} 921 (from their table 3) has the topographic delta parameter to the power of one in the de-922 nominator, in contrast to our squared power. But we suggest that the impact of sam-923 pling errors in the empirical fitting be studied in future studies before the correspondence 924 is rejected. We also note that the similar studies of prograde fronts by Brink (2016) and 925 Wei et al. (2022) found best fits using similar expressions but using topographic Burger 926 number Bu in place of the delta parameter, where the two are related via $Bu = (\sigma_E/f) \delta$. 927 The latter study concluded that scalings using δ instead of Bu where not successful over 928 prograde slopes. But, again, a comparison with our results is not straightforward since 929 their diffusivities were constructed using diagnosed EKE while ours are fully parame-930 terized. The relationship between δ -based and Bu-based formulations is also an obvi-931 ous topic for future work. 932

Note, finally, that over the flat regions where the deformation radius will act as the 933 relevant length scale, the 2D version of our efficiency factor becomes constant, in agree-934 ment with the behavior seen in Figure 3. In fact, the 2D version of E_{eff} was able to qual-935 itatively reproduce the observed eddy efficiency behaviour in the idealized channel sim-936 ulations, with some changes required for the tuning constants (not shown). We nonethe-937 less chose to use the 3D version in the realistic OMIP simulations in anticipation of a 938 more complex hydrography and flow field where the various assumptions of the Eady model 939 can be expected to hold to an even lesser degree than in the channel model. Interior thick-940 ness PV gradients, for example, are expected to be small in systems that are only forced 941 by Ekman pumping, as our channel model is (see e.g. Meneghello et al., 2021; Manucharyan 942 & Stewart, 2022). In a real ocean, where e.g. thermohaline forcing can produce interior 943 PV gradients, the suppression of eddy efficiency will inevitably be governed by additional 944 non-dimensional parameters beyond Blumsack and Gierasch (1972) δ (or, alternatively, 945 the topographic Burger number). Such 3D effects, caused by thermohaline forcing in ad-946

dition to wind stress, may also be the underlying reason for why E_{eff} had a much bigger impact in the OMIP simulations than it did in the channel.

⁹⁴⁹ 6 Summary and conclusions

Efforts to include topographic effects into mesoscale eddy parameterizations are 950 warranted, especially at high latitudes where observations show that hydrographic fronts 951 are typically locked to topography. The very existence of such fronts along continental 952 slopes and submarine ridges imply not merely topographic steering of large-scale cur-953 rents but also suppression of lateral mixing across topography. Yet, despite all the ob-954 servational evidence, as well as solid theoretical arguments for e.g. reduced growth rates 955 and length scales of baroclinic instability over sloping topography, most eddy parame-956 terizations still do not account for any bathymetric influence. 957

Here we have re-examined the relevance of the topographic Rhines scale in the mix-958 ing length approach to parameterizing the Gent-McWilliams buoyancy diffusivity which 959 is used for eddy advection. Constructing diffusivities using the Eady growth rate and 960 a parameterized version of the topographic Rhines scale reproduces an observed order-961 of-magnitude reduction in diffusivity over continental slopes in idealized channel sim-962 ulations. The simulations and analysis cover both prograde and retrograde continental 963 slopes, representing mean flows in the same and opposite direction to topographic waves, 964 respectively. Although differing in detail, both the observed and parameterized mixing 965 suppression are of similar order of magnitude on both sides. The skill of the parameter-966 ization is enhanced further, at least over the prograde slope, when the diffusivity is mul-967 tiplied by an eddy efficiency factor E_{eff} that is sensitive to the strength of the mean-968 flow vertical shear relative to the parameterized eddy velocity scale. Finally, we find that 969 selecting a smooth minimum of the topographic Rhines scale and the internal deforma-970 tion radius for length scale gives good skill over the entire idealized channel domain. 971

The parameterization is then tested in a realistic global ocean simulation. Com-972 parison with a simulation where topographic effects on diffusivities are not included sug-973 gests that the topography-aware parameterization enhances the sharpness of hydrographic 974 fronts and, as such, strengthens the thermal wind shear in boundary currents. The im-975 provement is particularly noticeable at high latitudes, but we also observe large impacts 976 throughout the world ocean. The globally-averaged temperature and salinity bias reduc-977 tions are in the range O(1%)-O(10%), with largest reductions seen in Southern Ocean 978 temperatures and in Atlantic Water temperatures in the Arctic. However, existing low-979 latitude thermocline biases tend to increase. 980

The complex pattern of bias changes seen is not uncommon in a realistic global model. 981 as bias reduction is very much a tuning exercise involving a range of free parameters as-982 sociated with different parameterizations (e.g. eddy transport, vertical mixing and air-983 sea-ice fluxes). Our parameterization also has free parameters and, as is common, we found 984 that the different model configurations, specifically different resolutions, might require 985 different values for these. But we did not attempt a rigorous tuning, especially not for 986 the dynamically complex OMIP simulations. Simply put, the focus at this stage has not 987 been on a well-tuned realistic global simulation, but rather on illustrating possible im-988 pacts of a topography-aware eddy parameterization. 989

The suggested parameterization is clearly incomplete. The relatively large difference in importance of the efficiency factor E_{eff} between the coarse-resolution channel simulations and the realistic OMIP simulations is one indication of this. A second one is the fact that we had to use an ad hoc limiter when applying this in the OMIP simulations. One key reason why a limiter had to be used is likely that we have been ignoring any vertical structure in eddy velocities and, ultimately, diffusivities. Fundamentally, the kinematic interaction with the bottom involves eddy bottom velocities, and a num-

ber of observations as well as theoretical arguments have indicated that these are often 997 significantly smaller than surface or even depth-averaged eddy velocities (see e.g. Kill-998 worth, 1992; Wunsch, 1997; de La Lama et al., 2016; Lacasce, 2017). The topographic 999 1000 impact, under such considerations, would probably be smaller than if estimated with depthaveraged quantities. Future work clearly needs to be put on such vertical structure, for 1001 example by taking an equivalent barotropic structure as a starting point (Killworth, 1992). 1002 We also observe that in our coarse-resolution channel simulations the flow remains too 1003 baroclinic, similar to the results presented by by Kjellsson and Zanna (2017); Yankovsky 1004 et al. (2022). Although addition of vertical structure to the buoyancy diffusivity might 1005 mitigate the issue, feeding the mean flow with vertically-distributed eddy energy (e.g. 1006 via a backscatter-type parameterizations) might be needed to resolve it (Yankovsky et 1007 al., 2022). 1008

Another key topic which we have entirely neglected in this study is the impact of 1009 bottom roughness or corrugations on fluxes—and how such impact may be asymmet-1010 ric with respect to the flow direction. As demonstrated by Wang and Stewart (2020), 1011 bottom roughness along a retrograde topographic slope can set up additional eddy buoy-1012 ancy transport and, thus, form stresses due to arrested topographic waves. The dynam-1013 ics governing such fluxes are likely distinct from those captured by our parameterizations 1014 here for smooth topography. The relevant eddy length scale, for example, is probably 1015 not the same as for transient eddies (Khani et al., 2019), and even coarse resolution mod-1016 els might be able to reproduce some of the largest standing meanders (Kong & Jansen, 1017 2021). The application of standing Rossby wave theory (e.g. Abernathey & Cessi, 2014; 1018 A. L. Stewart et al., 2023) appears to give promising results on the planetary beta plane 1019 with a flat but rough bottom. A natural next step may therefore be to examine such ideas 1020 to the 'topographic beta' problem, using e.g. the idealized two-slope model used here. 1021

Yet another issue ignored here is the role of lateral eddy momentum fluxes over con-1022 tinental slopes. As shown in Figure 1 and also highlighted in earlier studies (e.g. Wang 1023 & Stewart, 2018; Manucharyan & Isachsen, 2019), such fluxes bring wind momentum off 1024 the slopes to relatively flat regions where baroclinic instability kicks in to transfer the 1025 momentum to the ground below. The lateral momentum flux may be up-gradient in places 1026 and form eddy-driven jets, as seen offshore of the retrograde slope in our idealized sim-1027 ulations (Fig. 1). As with eddy form stress, lateral momentum fluxes also appear to be 1028 impacted by corrugated bottoms, being associated with the formation of prograde jets 1029 near the bottom (Wang & Stewart, 2020). This last effect is again probably related to 1030 the formation of arrested topographic waves, as discussed by e.g. Haidvogel and Brink 1031 (1986), as well as being linked to down-gradient PV diffusion in the finite-amplitude limit 1032 (Bretherton & Haidvogel, 1976; Vallis & Maltrud, 1993). 1033

Finally, it's worth remembering that eddy transport, even of buoyancy, may be anisotropic. 1034 So what really needs to be parameterized is a diffusion tensor rather than a single scalar. 1035 Bachman et al. (2020) discussed such anisotropy of the Redi diffusion tensor and showed 1036 that at global scale the direction of the major axis of the tensor is well correlated with 1037 the mean flow direction and the minor axis is well correlated with the gradient of Er-1038 tel PV. In addition, Nummelin et al. (2021, Appendix A) suggested that the Ferrari and 1039 Nikurashin (2010) type of mean-flow suppression indeed suppresses the across-flow Redi 1040 mixing, but that the inverse of the same factor enhances mixing in the along-flow direc-1041 tion. It remains unclear whether our eddy efficiency factor—here primarily applied to 1042 buoyancy mixing—and the other empirical scaling factors (e.g. Wang & Stewart, 2020; 1043 Wei et al., 2022) act similarly (i.e. relate to tensor anisotropy) or if they indeed suppress 1044 the overall tensor magnitude. In other words, it remains a research question whether the 1045 mean flow and topography merely direct the eddy transport or if they impact the over-1046 all magnitude of the eddy transport. Nevertheless, if the tensor major axis is correlated 1047 with the mean flow (as suggested by Bachman et al., 2020)—and if that mean flow trans-1048 port dominates over eddy transport—then the focus on the minor axis is likely justified. 1049

Name	Symbol	Value
Wind stress	$ au_x$	0.05 N m^{-2}
Horiz. grid size	$\Delta x, \Delta y$	$2 \mathrm{km}$
Baroclinic timestep	Δt	120 s
Domain x-size	L_x	$416 \mathrm{~km}$
Domain y-size	L_y	1024 km
Gravitational acceleration	g	9.806 m s^{-2}
Coriolis parameter	f_0	$1 \times 10^{-4} \text{ s}^{-1}$
Slope mid-point distance from domain edge	Y_S	$150 \mathrm{km}$
Shelf depth	H_{Shelf}	$250 \mathrm{m}$
Slope height	H_{Slope}	$2000~{\rm m}$

Table 1. BLOM model constants for the channel simulations

Table 2. Key parameters in the various high-resolution channel model experiments. L_R is the mean deformation radius in the central basin (where bottom depth is larger than 2250 m).

Name	L_R	Slope Width
Exp 1	$34.1~\pm1.3~\mathrm{km}$	$75 \mathrm{km}$
Exp 2	$34.1~{\pm}1.1~{\rm km}$	$100 \mathrm{km}$
Exp 3	$34.4~{\pm}1.0~{\rm km}$	$125 \mathrm{~km}$
Exp 4	$30.6~{\pm}1.3~{\rm km}$	$75 \mathrm{~km}$
Exp 5	$30.6~{\pm}1.2~{\rm km}$	$100 \mathrm{km}$
Exp 6	$30.4~{\pm}1.0~{\rm km}$	$125 \mathrm{~km}$
Exp 7	$24.9~{\pm}1.2~{\rm km}$	$75 \mathrm{km}$
Exp 8	$25.9~{\pm}1.0~{\rm km}$	$100 \mathrm{km}$
$\mathrm{Exp}~9$	$24.9~{\pm}1.0~{\rm km}$	$125 \mathrm{~km}$

Even if important questions remain, and despite its many shortcomings, the rel-1050 atively simple parameterization investigated here at least reduces an excessive washing 1051 out of hydrographic fronts over submarine ridges and continental slopes in ocean climate 1052 models—a known problem with eddy parameterizations that are insensitive of bathymetry. 1053 One of several important consequences of such adjustment is likely a more accurate rep-1054 resentation of oceanic heat transport across Antarctic and Greenland continental slopes 1055 and onward to the great ice sheets whose melt rates depend intimately on such trans-1056 port. On the shallow continental shelves, tides and other ageostrophic processes which 1057 we have neglected entirely here will also contribute. However, getting fluxes right across 1058 the strong fronts along the continental slopes is no less important. For this and other 1059 reasons, further scrutiny of all of the above unresolved issues related to mesoscale eddy 1060 transport and their impacts in both regional and global realistic simulations are much 1061 needed. 1062

1063 7 Open Research

The model configuration and namelists needed for reproducing the results are published in Zenodo (Nummelin, 2023b) and available at https://doi.org/10.5281/zenodo .8227381. The key model outputs (Nummelin, 2023a) needed for reproducing the analysis are published at the NIRD research data archive and available at https://archive .sigma2.no/pages/public/datasetDetail.jsf?id=10.11582/2023.00129.

Table 3. CORE-II hydrography bias (root mean square error) reduction compared to the bias of the control case. The observational data sets are the WOA 2018 climatologies for temperature (Locarnini et al., 2018) and salinity (Zweng et al., 2018). The experiment names correspond to parameterizations in Figure 4 as follows: L_T and $0.5 \cdot L_T$ correspond to (VIII), with $a_t = 1$ and $a_t = 0.5$, respectively; L_T and E_{eff} and $0.5 \cdot L_T$ and E_{eff} correspond to (IX), with $a_t = 1$ and $a_t = 0.5$, respectively. Experiment E_{eff} does not have a counterpart in Figure 4, but uses parameterization like (IX), with the exception that L_T is not considered as a length scale.

Name	zonal mean T	zonal mean S	$T_{100-200m}$	$T_{200-500m}$	$T_{500-1000m}$
Control anom.	$0.89^{\circ}\mathrm{C}$	$0.06~{\rm g/kg}$	$1.28^{\circ}\mathrm{C}$	1.11°C	$0.85^{\circ}\mathrm{C}$
$\overline{L_T}$	3.3%	2.9%	-1.8%	1.5%	3.4%
$0.5 \cdot L_T$	7.1%	7.0%	-3.8%	3.1%	7.3%
E_{eff}	16%	15%	-11%	4.9%	15%
L_T and E_{eff}	18%	16%	-13%	5.9%	20%
$0.5 \cdot L_T$ and E_{eff}	19%	18%	-15%	5.8%	22%

Table 4. Observed and simulated current transport in selected straits. The various perturbation experiments show percentage changes relative to the control case. The references for the observational values are as follows: Arctic Ocean gateway transports come from de Boer et al. (2018) with the original citations being Ingvaldsen et al. (2004) for Barents Sea Opening, Beszczynska-Möller et al. (2015) for Fram Strait, Curry et al. (2014) for Davis Strait (CAA), and Woodgate (2018); Woodgate et al. (2015) for Bering Strait; ACC transport come from Xu et al. (2020), for pure observational estimates see Koenig et al. (2014) and Donohue et al. (2016); and Florida–Bahamas Strait transport come from Larsen and Sanford (1985)

Name	obs	control	L_T	$0.5 \cdot L_T$	E_{eff}	L_T and E_{eff}	$0.5 \cdot L_T$ and E_{eff}
Barents Opening	2.1 Sv	2.4 Sv	0%	1%	4%	6%	7%
Bering Strait	$1.0 \ Sv$	$0.7 { m Sv}$	2%	3%	5%	7%	8%
Canadian Arctic	$-1.7 \ \mathrm{Sv}$	$-1.6 \ Sv$	4%	8%	14%	15%	16%
Fram Strait	-2.2 Sv	-1.3 Sv	-3%	-6%	-9%	-6%	-6%
Drake Passage (ACC)	$157.3 \ \mathrm{Sv}$	$152 \mathrm{~Sv}$	0%	1%	4%	5%	7%
Florida–Bahamas Strait	$32 \mathrm{Sv}$	$13.2 \ \mathrm{Sv}$	1%	3%	4%	5%	6%

1069 Acknowledgments

We thank the editor, Stephen Griffies, and three anonymous reviewers for their comments
and suggestions that led to a much improved manuscript. This work was funded in part
by the two Research Council of Norway projects KeyClim (295046) and TopArctic (314826).
A. Nummelin would like to thank Mats Bentsen for the help with the initial model setup.

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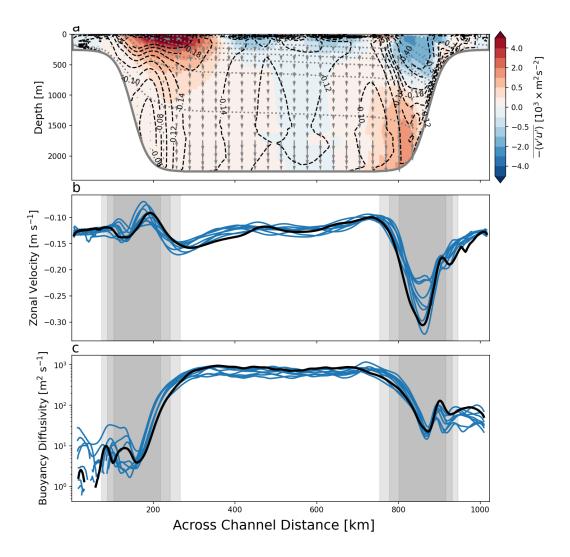


Figure 1. Cross section of zonally and temporally-averaged (a) mean zonal velocity (dashed black contours), mean density (dotted gray contours), E-P flux (gray arrows) and its horizontal component (meridional eddy flux of negative u-momentum; shading, note that the units have been scaled by 10^3 and here the bar denotes time-mean), (b) vertically-averaged zonal velocity and (c) vertically-averaged meridional buoyancy (temperature) diffusivity. In panels b and c the blue lines show results from the various experiments listed in Table 2. The black line is experiment 3 and corresponds to the case shown in panel a. Gray shading shows the location of the slope regions in the different simulations (where 300 m < H < 2250 m). For some of the simulations the diffusivity lines are broken because of negative diffusivities that are not shown on the log scale.

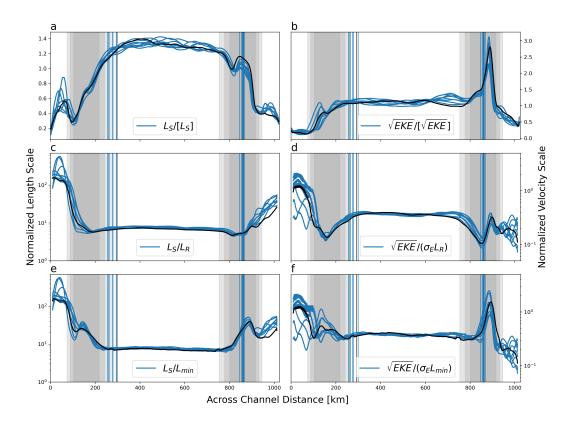


Figure 2. Diagnosed length scales (panels on the left) and velocity scales (panels on the right) for all experiments. All measures are zonal and time averages that have been normalized. The top row (panels a and b) are normalized by the basin-mean values (denoted by square brackets). Length scales in panel c and panel e are normalized by the deformation radius (L_R) and by the mimimum of deformation radius and topographic Rhines scale (L_{min}) , respectively. In panels d and f we normalize by the parameterized velocity scale, using length scales from c and e, respectively. Colors and line styles as in Fig. 1. Gray shadings indicate the slope regions (similar to Fig. 1) and vertical lines indicate the location of maxima in depth-averaged velocity in each experiment.

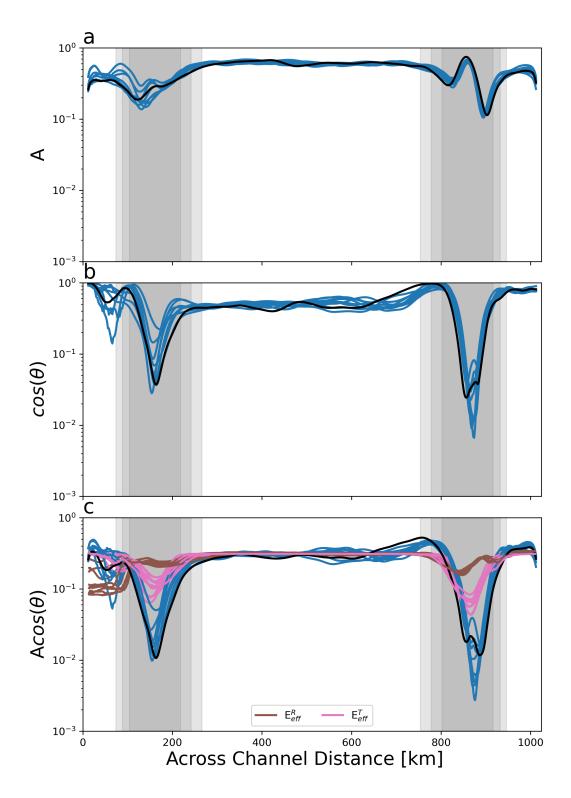


Figure 3. Measures of anisotropy and phase angle relationships: (a) eddy velocity anisotropy (A), (b) cosine of the phase angle between \overline{T}' and \overline{v}' and (c) the product of (a) and (b), as well as the parameterized eddy efficiency factors E_{eff} (brown when using deformation radius, pink when using the topographic Rhines scale). In panel c we use $a_2 = 10$ for E_{eff} . To match the mid-basin values of E_{eff} with $A\cos(\theta)$, we scale E_{eff}^R with 0.35 and E_{eff}^T with 0.32. Colors and line styles as in Fig. 1, and gray shadings indicate the slope regions.

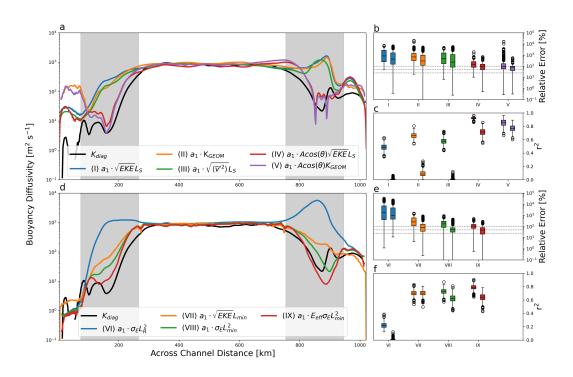


Figure 4. Partly-parameterized (a–c) and fully-parameterized (d–f) across-slope buoyancy diffusivities. The left panels show across-basin profiles for experiment 3 (Table 2) whereas the right panels summarize the statistical comparison between the diagnosed and parameterized diffusivities across all experiments (b–c, e–f; relative error is defined as $|(K_{par} - K_{diag})|/K_{par}$, where K_{par} is one of the parameterization (I)-(IX); r^2 is based on linear regression using 200 points across all cases that is repeated 5000 times). Boxes and whiskers come in pairs, with the one on the left (right) corresponding to the southern (northern) slope. Linear regressions are done over the slope regions only (gray shading; similar to Fig. 1). In panels a and d, the estimates I-IX are scaled by constant a_1 optimized to match the mid-basin diffusivity, and in addition we use $a_T = 0.5$ (for VII-IX), and $a_2 = 2$ (for IX). The a_1 values are 0.1, 1.17, 0.09, 0.31, 3.77, 0.25, 0.66, 0.25, and 0.25 for estimates I-IX, respectively. In panels b and e, the dashed gray lines correspond to 25%, 50%, 100% absolute relative error.

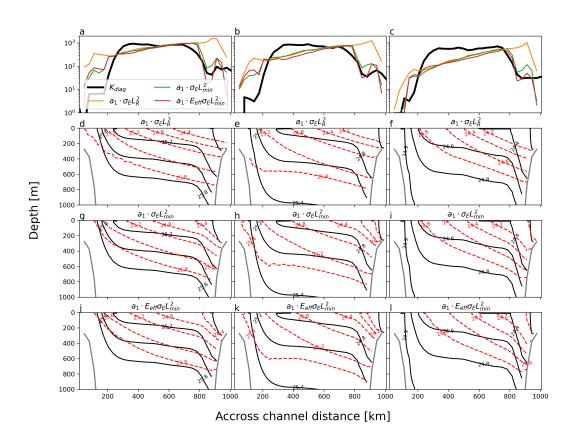


Figure 5. Buoyancy diffusivity (top row) and potential density anomaly (referenced to 0 dbar) in the upper 1000 m of the coarse-resolution channel simulation compared to the high-resolution simulation (black line; coarse-grained to the coarse resolution grid). The different columns show experiments with different stratification such that the initial conditions are the same as for Exp 3, 6 and 9 in the left, middle and right columns, respectively (the initial stratification decreases to the right). For panels d-l, title indicates the parameterization. Bottom topography is indicated with a gray line

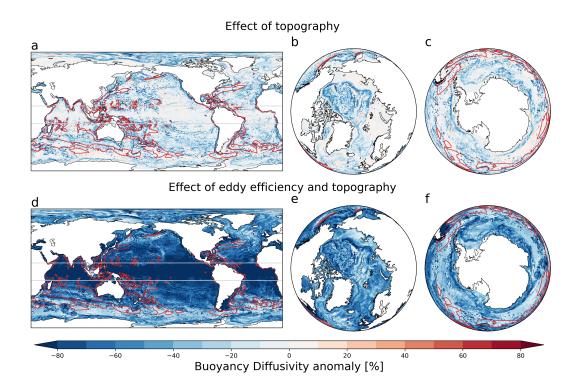


Figure 6. Anomalies from the control case in parameterized (depth-averaged) GM diffusivity due to implementation of (top row) the topographic Rhines scale and (bottom row) eddy efficiency in addition to the topograhic Rhines scale. Red contours show the 1000 m² s⁻¹ isoline for diffusivity in the control case and light gray contours show areas in the tropics where the grid size is smaller than the internal deformation radius and therefore the resolution function (Hallberg, 2013) reducing the GM coefficient is in effect.

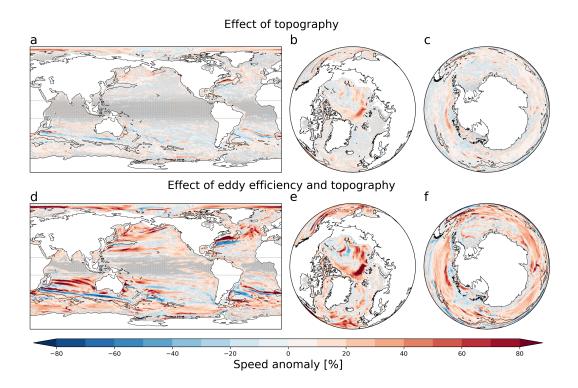


Figure 7. Flow speed anomalies from the control case at 100–200 m depth due to implementation of: (top row) the topographic Rhines scale and (bottom row) eddy efficiency in addition to the topograhic Rhines scale. Black contours show the 0.25 m s⁻¹ isolines for observational estimate of the quasi-geostrophic current speed (Buongiorno Nardelli, 2020) in the same 100–200 m depth interval. Gray dots mark grid cells where 30 year mean is not significantly different from the control case at 5% significance level (student's t-test).

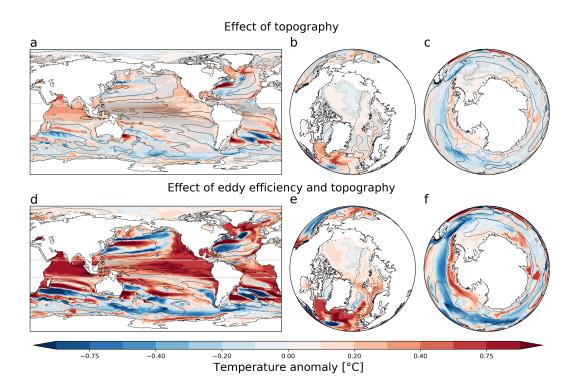


Figure 8. Temperature anomalies from the control case between 100–200 m depth due to implementation of: (top row) the topographic Rhines scale and (bottom row) eddy efficiency in addition to the topograhic Rhines scale. Black contours show the $\pm 1^{\circ}$ C (solid/dashed) isoline for the control case bias relative to the WOA observations. Therefore, whenever solid (dashed) contours surround blue (red) areas the bias is reduced. Gray dots mark grid cells where 30 year mean is not significantly different from the control case at 5% significance level (student's t-test).

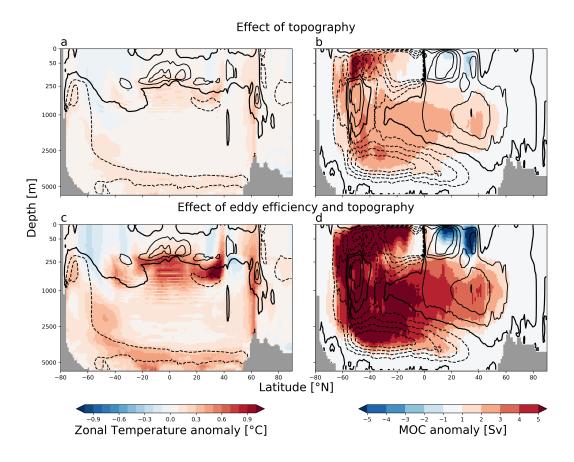


Figure 9. Zonal-mean temperature anomalies (left panels) and global meridional overturning stream function (MOC) anomalies (right panels), relative to the control simulation, due to implementation of: (top row) the topographic Rhines scale and (bottom row) eddy efficiency in addition to the topograhic Rhines scale. For temperature, black contours show the control case bias relative to the WOA observations in 0.25°C intervals (dashed for negative, solid for positive, the thick solid curve shows the zero contour). Therefore, whenever solid (dashed) contours surround blue (red) areas the bias to the observations is reduced. For the MOC, the contours show the control case MOC at 5 Sv intervals with the thick solid curve indicating the 0 Sv contour. Therefore solid (dashed) contours surrounding red (blue) indicates intensifying overturning. Similar to Figs. 7-8, a student's t-test is applied here, but gray dots are now shown as all values are significant at 5% level.

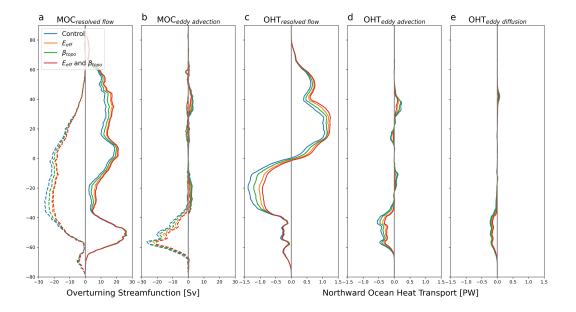


Figure 10. Resolved and eddy contributions to the global meridional overturning circulation (MOC, panels a and b) and to the global northward ocean heat transport (OHT, panels c–e). For the MOC we show the maximum (solid) and minimum (dashed) below 500 m to avoid the shallow surface overturning cells. For the OHT we show both advective and diffusive eddy contributions (panels d and e, respectively).