# Diagnostics of the ionospheric conductivity based on spacecraft observations of the magnetospheric ULF waves

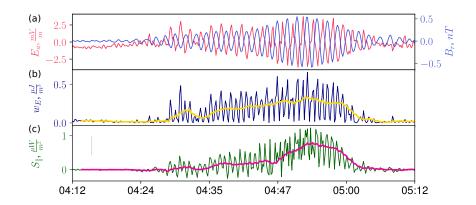
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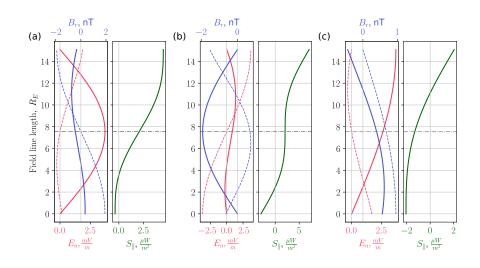
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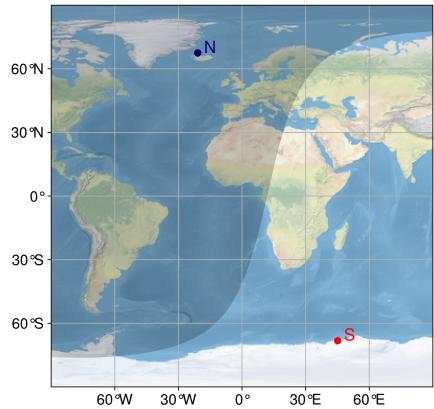
### Abstract

In 27 October 2012 the ULF wave in Pc4 range being Alfv'en wave was observed with Van Allen Probe A. In the event the parallel Poynting flux of the wave was directed towards the Northern ionosphere. Assuming that this may be caused by the asymmetry of ionospheric conductivity between the Northern and Southern hemispheres, its effect on the standing structure of the Alfv'en wave was investigated in this paper. For this purpose the analytical model with straight magnetic field lines was used. As a result the method for estimation of the Northern and Southern ionospheric conductivity was developed. It allows us to reconstruct the parallel structure of Alfv'en waves under various conditions of the ionospheric conductivity. With the method developed, the ionospheric conductivity for the October 27, 2012 event was evaluated and compared with ionosphere model IRI-2016.





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## Diagnostics of the ionospheric conductivity based on spacecraft observations of the magnetospheric ULF waves

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### Key Points:

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7	•	A method for estimating the ionospheric conductivity based on spacecraft obser-
8		vations of Alfvén waves in the magnetosphere is proposed
9	•	The parallel structure of an Alfvén wave under various conditions of the ionospheric
10		conductivity is reconstructed
11	•	The height-integrated Pedersen conductivity of the ionosphere were estimated for
12		the October 27, 2012 event

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#### 13 Abstract

In 27 October 2012 the ULF wave in Pc4 range being Alfvén wave was observed with 14 Van Allen Probe A. In the event the parallel Poynting flux of the wave was directed to-15 wards the Northern ionosphere. Assuming that this may be caused by the asymmetry 16 of ionospheric conductivity between the Northern and Southern hemispheres, its effect 17 on the standing structure of the Alfvén wave was investigated in this paper. For this pur-18 pose the analytical model with straight magnetic field lines was used. As a result the method 19 for estimation of the Northern and Southern ionospheric conductivity was developed. It 20 allows us to reconstruct the parallel structure of Alfvén waves under various conditions 21 of the ionospheric conductivity. With the method developed, the ionospheric conduc-22 tivity for the October 27, 2012 event was evaluated and compared with ionosphere model 23 IRI-2016. 24

### <sup>25</sup> Plain Language Summary

The most commonly observed ULF waves in the magnetosphere are Alfvén waves 26 standing along magnetic field line between magnetically conjugated points of the iono-27 sphere located in opposite hemispheres. In this paper we considered how the north-south 28 asymmetry of the ionospheric conductivity influences on standing Alfven wave's paral-29 lel structure. The model predicts that the structure of the Alfvén waves may differ de-30 pending on the conductivity values of Northern and Southern ionospheres. Based on the 31 32 model we developed the method to carry out a qualitative estimation of the ionospheric height-integrated Pedersen conductivity using parameters of Alfvén waves observed with 33 spacecraft in the magnetosphere. As a result, for the 27 October 2012 event the paral-34 lel structure of the observed Alfvén wave was reconstructed and the ionospheric conduc-35 tivity was estimated. We found a significant difference in the conductivity values of the 36 Northern and Southern ionospheres. The mean is that the magnetically conjugated foot-37 prints of spacecraft trajectory, where the event observed, were located on different sides 38 from the line that divides the day side and the night side of Earth (terminator line). 39

### 40 1 Introduction

Studies of the coupled system of ionosphere-magnetosphere is of crucial importance 41 for the plasma processes in the near-Earth's space. An important part of this system is 42 the ultra low frequency (ULF) waves, observed both in space and on the ground. The 43 ULF waves are the field line oscillations with frequencies of the order or lower than the 44 proton gyrofrequency. The most widespread classification categorizes these wave into reg-45 ular pulsations Pc1–5 ranges (periods from 0.2 to 600 s) and irregular Pi1–2 pulsations 46 (periods from 1 to 150 s) (Jacobs et al., 1964). These waves are interpreted in terms of 47 magnetohydrodynamic (MHD) oscillations. Major part of the ULF waves are identified 48 with the Alfvén waves standing along the field line between the magnetically conjugated 49 points of ionosphere (Dungey, 1954; Radoski, 1967; Chen & Hasegawa, 1974; Southwood, 50 1974). 51

Standing Alfvén waves are often used for the diagnostics of the magnetospheric plasma 52 (Troitskaya & Gul'elmi, 1967; Chi & Russell, 2005; Menk & Waters, 2013). Indeed, the 53 Alfvén speed is inversely proportional to square root of the mass density, thus the ob-54 served wave's frequency allows one to reproduce plasma density distribution (Berube et 55 al., 2006; Takahashi & Denton, 2007). A number of papers were devoted to calculation 56 of the structure of the standing Alfvén waves with different distributions of density and 57 other magnetospheric parameters (Cummings et al., 1969; Orr & Matthew, 1971; Allan 58 & Knox, 1979a; Leonovich & Mazur, 1993; Ozeke & Mann, 2004; Pilipenko et al., 2005; 59 Degeling et al., 2010; Petrashchuk et al., 2022). 60

However, there is yet another factor influencing wave's structure and frequency, the 61 ionospheric conductivity. The studies of the influence of the conductivity on the stand-62 ing Alfvén waves began with works (Scholer, 1970; Inoue, 1973; Maltsev et al., 1974; Hughes, 63 1974; Hughes & Southwood, 1976). Those papers considered ionosphere as a thin layer, which is justified for the long-period ULF waves (Pi2, Pc4-5). It was shown that the in-65 cident wave's magnetic field is reflected from the ionosphere due to the Pedersen con-66 ductivity, while the electric field reaches the ground due to the Hall conductivity. Fur-67 ther investigations of the ionosphere-magnetosphere interaction by means of the Alfvén 68 waves were performed in (Alperovich & Fedorov, 1984; Glassmeier, 1984; Hameiri & Kivel-69 son, 1991; Leonovich & Mazur, 1991, 1996; Yoshikawa & Itonaga, 1996; Yoshikawa et al., 70 2002; Sciffer & Waters, 2002; Cheremnykh & Parnowski, 2006; Erkaev et al., 2006; Wa-71 ters et al., 2013). 72

Two limiting cases are worth mentioning. If the conductivity is high, then the wave's electric field equals zero on the ionosphere:  $E_{\pm} = 0$ , where the "+" and "-" signs refer to the conjugate ionospheres. In this case, the oscillating magnetic field line behave as if fixed in the points of intersection with the ionosphere. This oscillation is usually called the "rigid-end" mode (Cummings et al., 1969; Sinha & Rajaram, 1997).

In the opposite case, the conductivity is very small. In this case, the field aligned derivative of the wave's electric field equals zero on the ionosphere:  $(\partial E/\partial l)_{\pm} = 0$ , where *l* is a length along the field line. As a result the field line freely slides on the ionosphere. Such mode is called the "free-end mode" (Newton et al., 1978; Allan & Knox, 1979a). In both cases, between the conjugate ionospheres fit an integer half-waves, the Alfvén waves standing along the field line with no energy flux in this direction.

However, the situation is possible where the conductivities on the Northern and 84 Southern magnetically conjugated points are drastically different. It can be caused by 85 the asymmetry of Pedersen conductivity between the Northern and Southern hemispheres. 86 This situation can occur in the polar ionosphere near the solstices, when one hemisphere 87 is illuminated for a long time and the other is correspondingly in darkness (Glassmeier 88 et al., 1999). In this case, a situation is possible where one end of the field line is fixed, 89 and the other freely slides on the ionosphere. Then between the conjugate ionospheres 90 fit an integer quarter-waves. For the first time, such possibility was mentioned in (Allan 91 & Knox, 1979a). Results of further theoretical studies of the quarter-waves were reported 92 in (Allan & Knox, 1979b; Allan, 1983; Bulusu et al., 2014, 2016). The observational ev-93 idences for the quarter-waves were presented in (Allan, 1983; Budnik et al., 1998; Bu-94 lusu et al., 2015; Obana et al., 2008, 2015). 95

The observational manifestations of the Alfvén waves at the asymmetric ionospheres are different from those in the symmetric case. Indeed, the frequency of the leading quarterwave harmonic approximately two times lower than for the half-wave, there is field aligned energy flux. Thus, the Alfvén waves can be used for diagnostics of the ionosphere (Lee et al., 2004; Ozeke & Mann, 2004; Bulusu et al., 2015; Bulusu et al., 2016; Lysak et al., 2020).

Usually, ionospheric conductivities are determined in several ways. One method 102 is based on the using of the models of the atmosphere, ionosphere and magnetic field with 103 equations derived in (Maeda, 1977). For example, paper (Obana et al., 2015) used the 104 atmosphere model MSISE-90, the ionosphere model IRI 95, and near-Earth geomagnetic 105 field model IGRF 95. In another method the ground based instruments are used. The 106 difficulty here appears in the necessity to use either data of combined observations from 107 different instruments, for example, all sky cameras and riometers (Senior et al., 2008); 108 either, special radar measurement programs and empirical models ought to be used (Ieda 109 et al., 2014). Also, the low-orbital satellite data can be used, like SWARM mission. In 110 the case of single satellite, calculation of the ionospheric conductivity demands using rather 111

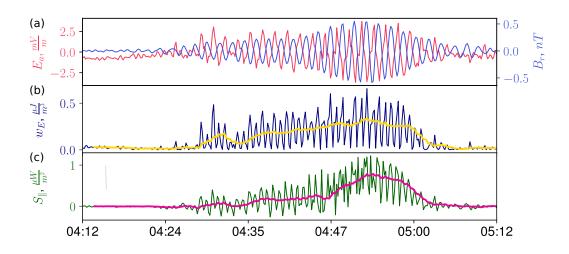


Figure 1. Peculiarities during the 27 October 2012 event: (a) the radial component of the wave's magnetic field  $B_r$  (blue line) and the azimuthal component of the wave's electric field  $E_a$  (red line); (b) the electric field energy density  $w_E$  (dark blue line) and  $\overline{w}_E$  (yellow line) averaged over the wave period T = 100 c(c) the same for parallel Poynting flux  $S_{\parallel}$  (green line) and  $\overline{S}_{\parallel}$  (red line).

complicated method which give results only along the satellite trajectory (Juusola et al.,
 2016).

#### <sup>114</sup> 2 27 October 2012 wave event

Let us consider the 27 October 2012 event, in which a poloidal Alfvén wave was 115 observed with The Van Allen Probe A. The wave was registered in the morning part of 116 the magnetosphere at a distance  $6.2R_E$ . During the event we observed the resonance 117 generation of the ULF wave by the 38 keV electron flux. The electron flux was injected 118 to the magnetosphere due to the substorm. The wave was the fundamental harmonic of 119 the standing Alfvén wave with a frequency 10 mHz and azimuthal wave number  $m \approx$ 120 110 - 115. The wave interacted with electrons via the drift resonance and was gener-121 ated through the gradient instability. The detailed study of the event is presented in (Mikhailova 122 et al., 2022). 123

We revealed several peculiarities during the 27 October 2012 event studying, which 124 were not mentioned in (Mikhailova et al., 2022). At the figure (Fig. 1) the wave field com-125 ponents, the electric field energy density  $w_E$  and the parallel Poynting flux  $S_{\parallel}$ , and their 126 values averaged over the wave period T = 100 c are presented. One can see that phase 127 shift between the radial component of the wave's magnetic field  $B_r$  and the azimuthal 128 component of the wave electric field  $E_a$  is about 180°, rather than 90°, as is usually ex-129 pected for standing waves. Moreover the Poynting flux was directed toward the North-130 ern ionosphere (Fig. 1b). We suggest that these observational peculiarities can be caused 131 by the asymmetry of Pedersen conductivity between the Northern and Southern iono-132 spheres. 133

### <sup>134</sup> **3** Principal equations

Let us consider the equation for an Alfvén wave. In the homogeneous background magnetic field and plasma it has a form:

$$\frac{\partial^2 E_j}{\partial l^2} + k_{\parallel}^2 E_j = 0, \tag{1}$$

where  $E_j$  is a component of the wave electric field (under index j is assumed r for the radial component and a for azimuthal one),  $k_{\parallel} = \omega/v_A$  is the parallel component of wave vector,  $\omega$  is the wave frequency,  $v_A$  is the Alfvén speed, l is a coordinate along the magnetic field line. The parallel component of electric field is not considered because it equals to zero in a MHD approximation. We assume the straight magnetic field lines.

The boundary condition for Alfvén waves on the ionosphere were determined in a lot of papers (Hughes, 1974; Hughes & Southwood, 1976; Newton et al., 1978; Leonovich & Mazur, 1991). It can be written in the form

$$E_j|_{l_{\pm}} = \mp i \frac{\epsilon^{\pm}}{k_{\parallel}} \frac{\partial E_j}{\partial l}\Big|_{l_{\pm}}, \qquad (2)$$

where  $l_{\pm}$  is the coordinate of the Southern  $(l_{-})$  and Northern  $(l_{+})$  ionospheric boundaries, the dimensionless parameter  $\epsilon^{\pm}$  is inversely proportional to the height-integrated Pedersen conductivity  $\Sigma_{P}^{\pm}$ ,

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$$e^{\pm} = \frac{c^2}{4\pi\Sigma_P^{\pm}v_A},\tag{3}$$

c is the speed of light. Eq. (2) assumes the field to enter to the ionosphere on the normal to it. For more general case, see (Leonovich & Mazur, 1991). The boundary condition (2) determines the damping decrement of the standing Alfvén wave under dissipation in the ionosphere. This one is caused by ionospheric Joule heating at the field line
basement (Southwood & Hughes, 1983).

We use the coordinate  $l_{-} = 0$  as a coordinate of the Southern ionosphere boundary and  $l_{+} = l_{I}$  as a coordinate of the Northern one. The length of the magnetic filed line  $l_{I}$  can be obtained from the expression

$$l_I = LR_E \int_{-\theta_I}^{\theta_I} \sqrt{1 + 3\sin^2\theta} \cos\theta d\theta, \qquad (4)$$

(5)

where L is a McIlwain parameter,  $\pm \theta_I$  is the geomagnetic latitude of the Southern (-) and Northern (+) points of intersection of the magnetic field line with the ionosphere. The latitude can be found from the magnetic filed line equation of the dipole magnetic field  $r = LR_E \cos^2 \theta$ , assuming  $r = R_E + h_I$ , where  $h_I$  is height of the upper boundary of the ionosphere (Chapman & Sugiura, 1956).

The dimensionless conductivity parameter  $\epsilon^{\pm}$  (3) let us to take into account different values of Pedersen conductivity at the points of intersection. They are

1. High conductivity of the ionosphere at both the hemispheres:  $\epsilon^{\pm} \ll 1$ ;

<sup>164</sup> 2. Low conductivity of the ionosphere at both the hemispheres:  $\epsilon^{\pm} \gg 1$ ;

<sup>165</sup> 3. Asymmetric conductivity at the different hemispheres:  $\epsilon^+ \gg 1, \epsilon^- \ll 1$ .

It was assumed at all these cases that the ionospheric conductivities at the different hemispheres have the different absolute value.

The general solution of the wave equation (1) can be represented as

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$$E_j = C_1 \exp\left(ik_{\parallel}l\right) + C_2 \exp\left(-ik_{\parallel}l\right).$$

Using boundary condition (2) we found the expression for the coefficients  $C_1$  and  $C_2$ , and equation for the parallel wave vector  $k_{\parallel}$ :

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$$(1 - \epsilon^{-})(1 - \epsilon^{+}) \exp(ik_{\parallel}l_{I}) - (1 + \epsilon^{-})(1 + \epsilon^{+}) \exp(-ik_{\parallel}l_{I}) = 0.$$
(6)

To solve (6) let us consider two limiting cases: (i) high conductivity,  $\epsilon^{\pm} \ll 1$ ; (ii) low conductivity,  $\epsilon^{\pm} \gg 1$ . In both cases, the parallel wave vector can be represented in the form  $\pi N$ 

$$k_{\parallel} = k_0 + \delta k, \quad k_0 = \frac{\pi N}{l_I},\tag{7}$$

where N is the harmonic wave number, and  $\delta k$  is a small addition caused by small value of  $\epsilon^{\pm}$  in the first case and small value of  $(\epsilon^{\pm})^{-1}$  in the second case. As result, we found the small value  $\delta k$  and the wave electric field, and, correspondingly, wave magnetic field

$$B_a = -i\frac{c}{\omega}\frac{\partial E_r}{\partial l}, \quad B_r = i\frac{c}{\omega}\frac{\partial E_a}{\partial l} \tag{8}$$

the parallel Poynting flux averaged over the wave period

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$$\overline{S}_{\parallel} = \frac{c}{8\pi} (E_r B_a^* - E_a B_r^*). \tag{9}$$

In the case of high ionospheric conductivity,  $\epsilon^{\pm} \ll 1$ , the parallel structure of the wave's electromagnetic field is determined as

$$E_{a,r} = \begin{pmatrix} E_{a0} \\ E_{r0} \end{pmatrix} \left[ \sin k_0 l - i \left( \frac{\epsilon^- + \epsilon^+}{l_I} l - \epsilon^- \right) \cos k_0 l \right]$$
(10)

$$B_{a,r} = \begin{pmatrix} -B_{a0} \\ B_{r0} \end{pmatrix} \left[ \frac{\epsilon^- + \epsilon^+}{k_0 l_I} \cos k_0 l - \left( \frac{\epsilon^- + \epsilon^+}{l_I} l - \epsilon^- \right) \sin k_0 l + i \cos k_0 l \right]$$
(11)

where  $E_{a0}$  and  $E_{r0}$  are the amplitudes of the azimuthal and radial components of the wave electric field, and

$$B_{a0} = E_{r0} \frac{k_0 c}{\omega}, \quad B_{r0} = E_{a0} \frac{k_0 c}{\omega}$$
(12)

<sup>190</sup> are the amplitudes of the azimuthal and radial components of the wave magnetic field.

In the opposite low conductivity case,  $\epsilon^{\pm} \gg 1$ , the Alfvén wave's parallel structure can be represented as

$$E_{a,r} = \begin{pmatrix} E_{a0} \\ E_{r0} \end{pmatrix} \left[ \cos k_0 l - i \left[ \left( \frac{1}{\epsilon^-} + \frac{1}{\epsilon^+} \right) \frac{l}{l_I} - \frac{1}{\epsilon^-} \right] \sin k_0 l \right]$$
(13)

$$B_{a,r} = \begin{pmatrix} -B_{a0} \\ B_{r0} \end{pmatrix} \left[ \left( \frac{1}{\epsilon^{-}} + \frac{1}{\epsilon^{+}} \right) \frac{\sin k_0 l}{k_0 l_I} - \left[ \left( \frac{1}{\epsilon^{-}} + \frac{1}{\epsilon^{+}} \right) \frac{l}{l_I} - \frac{1}{\epsilon^{-}} \right] \cos k_0 l + i \sin k_0 l \right]$$
(14)

For the case of the asymmetric ionosphere (low conductivity of the Northern ionosphere,  $\epsilon^+ \gg 1$ , and high conductivity of the Southern ionosphere,  $\epsilon^- \ll 1$ , the parallel wave vector is

$$k_{\parallel} = \frac{1}{2}k_0 + \delta k \tag{15}$$

<sup>199</sup> the parallel structure is represented as

$$E_{a,r} = \begin{pmatrix} E_{a0} \\ E_{r0} \end{pmatrix} \left[ \sin \frac{k_0 l}{2} - i \left[ \left( \epsilon^- + \frac{1}{\epsilon^+} \right) \frac{l}{l_I} - \epsilon^- \right] \cos \frac{k_0 l}{2} \right]$$
(16)

$$B_{a,r} = \frac{1}{2} \begin{pmatrix} -B_{a0} \\ B_{r0} \end{pmatrix} \left[ 2\left(\epsilon^{-} + \frac{1}{\epsilon^{+}}\right) \frac{\cos\frac{k_{0}l}{2}}{k_{0}l_{N}} - \left[\left(\epsilon^{-} + \frac{1}{\epsilon^{+}}\right) \frac{l}{l_{N}} - \epsilon^{-} \right] \sin\frac{k_{0}l}{2} + i\cos\frac{k_{0}l}{2} \right] (17)$$

Let us consider properties of the wave's parallel structure on the equator, where  $l = l_I/2$ . Expressions for the azimuthal component of the wave's electric field  $E_a$ , the radial component of the magnetic field and the parallel Poynting flux  $S_{\parallel}$  are presented in Table 1, where  $\Delta \phi$  is the phase shift between  $B_r$  and  $E_a$  components, and

$$S_0 = \frac{c^2 k_0}{16\pi\omega} (E_{a0}^2 + E_{r0}^2).$$
(18)

It is worth to note that only the highest order terms are written.

Table 1. Expressions for the azimuthal component of the wave's electric field  $E_a$ , the radial component of the magnetic field and the parallel Poynting flux on the geomagnetic equator for the fundamental harmonic (N = 1)

Case	$E_a\left(\frac{l_I}{2}\right)$	$B_r\left(\frac{l_I}{2}\right)$	$\overline{S}_{\parallel}\left(rac{l_{I}}{2} ight)$	$\Delta \phi$
$ \frac{\epsilon^{\pm} \ll 1}{\epsilon^{\pm} \gg 1} $	$E_{a0}$	$-\frac{B_{r0}}{2}(\epsilon^+ - \epsilon^-)$	$S_0\left(\epsilon^+ - \epsilon^- ight)$	$ \begin{array}{c} \sim 180^{\circ}, 0^{\circ} \\ \sim 180^{\circ}, 0^{\circ} \end{array} $
$\epsilon^{-} \gg 1$ $\epsilon^{+} \gg 1, \ \epsilon^{-} \ll 1$	$-i\frac{1}{2}\left(\frac{1}{\epsilon^{+}}-\frac{1}{\epsilon^{-}}\right)$ $\frac{E_{a0}}{2\sqrt{2}}$	$iB_{r0} \ irac{B_{r0}}{2\sqrt{2}}$	$S_0 \left( \frac{1}{\epsilon^+} - \frac{1}{\epsilon^-} \right)$ $S_0 \left[ \frac{1}{2} \left( \frac{1}{\epsilon^+} - \epsilon^- \right) - \frac{1}{k_0 l_I} \left( \frac{1}{\epsilon^+} + \epsilon^- \right) \right]$	$\sim 180^{\circ}, 0^{\circ}$ $\sim 90^{\circ}$

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The following properties of the standing Alfvén wave on the geomagnetic equator
 are apparent from Table 1:

2111. The phase shift between the electric  $E_a$  ( $E_r$ ) and magnetic  $B_r$  ( $B_a$ ) fields for the212symmetric conditions is close to 180° or 0°, and for asymmetric conditions to 90°;2132. Since conductivities  $\Sigma_P^{\pm} \propto 1/\epsilon^{\pm}$ , then for the symmetric conditions the absolute214value and direction of the parallel Poynting flux  $S_{\parallel}$  is determined by the differ-215ence of the ionospheric conductivities ( $\epsilon^{\pm} \gg 1$  case) or their reverse values ( $\epsilon^{\pm} \ll 1$  case).2173. For the asymmetric conditions, the absolute value and direction of the parallel Poynt-

ing flux is determined by the combination of the conductivity of one ionosphere and the conductivity reverse value of the other.

The correctness of the results is indicated by the coincidence of the phase shift under symmetric and asymmetric conditions at the boundaries of the ionosphere with early theoretical work (Newton et al., 1978; Southwood & Kivelson, 2001).

### 4 Ionospheric conductivity estimation model

Expressions received for standing Alfvén wave allow to estimate ionospheric conductivity based on spacecraft data processing of observing magnetospheric Alfvén waves. Inputs include wave parameters such as its period or frequency and wave electric and magnetic field and spacecraft coordinates. Since  $v_A = \omega/k_{\parallel}$  and  $k_{\parallel} \approx k_0 \equiv \pi N/l_I$  for  $\epsilon^{\pm} \ll 1$  and  $\epsilon^{\pm} \gg 1$  symmetric cases, then as follows from eq. (3)

$$\Sigma_P^{\pm} = \frac{c^2 k_0}{4\pi\omega\epsilon^{\pm}} = \frac{Nc^2}{4l_I\omega\epsilon^{\pm}} \tag{19}$$

where the length of magnetic field line  $l_I$  can be defined from (4).

With obtained model, the universal method of ionospheric conductivity estimation was developed. It is required to determine ratio between conductivities. For this point, the maximum value of the parallel Poynting flux averaged over the wave period  $\overline{S}_{\parallel}$  is used (Fig. 1c). Also, the period-averaged energy density of the wave electric or magnetic field

$$\overline{w}_E = \frac{1}{16\pi} (E_r E_r^* + E_a E_a^*), \quad \overline{w}_B = \frac{1}{16\pi} (B_r B_r^* + B_a B_a^*). \tag{20}$$

corresponding to this time is used. For example, as follows from Table 1 for the fundamental harmonic (N = 1) at the magnetic equator for  $\epsilon^{\pm} \ll 1$  case we have

$$\overline{w}_E = \frac{1}{16\pi} (E_{a0}^2 + E_{r0}^2). \tag{21}$$

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$$\left(\epsilon^{+} - \epsilon^{-}\right) = \frac{\omega}{c^{2}k_{0}} \frac{S_{\parallel}}{\overline{w}_{E}}.$$
(22)

For  $\epsilon^{\pm} \gg 1$  case we have

$$\overline{w}_B = \frac{1}{16\pi} (B_{a0}^2 + B_{r0}^2) = \frac{c^2 k_0^2}{16\pi\omega^2} (E_{a0}^2 + E_{r0}^2).$$
(23)

243 and

$$\left(\frac{1}{\epsilon^+} - \frac{1}{\epsilon^-}\right) = \frac{k_0}{\omega} \frac{\overline{S}_{\parallel}}{\overline{w}_B}.$$
(24)

If the height-integrated Pedersen conductivity of one ionosphere is known (for example, Southern  $\Sigma_P^-$ ), then using the observed values of the period-averaged parallel Poynting flux and energy density the conductivity of the other ionosphere (Northern  $\Sigma_P^+$ ) can be calculated with eq. (19) and eq. (22) or eq. (24) depending on the case under consideration

The principle of operation is simple and requires only the availability of the data 250 from magnetospheric observation of Alfvén wave. Moreover, data from one spacecraft 251 is enough for the method to work. Note using method has disadvantage at this stage of 252 development. The fixed height-integrated Pedersen conductivity of one hemisphere is set 253 manually. This can be done using reference theoretical conductivity values or using other 254 empirical models or direct measurements. Thus, the characteristic height-integrated Ped-255 ersen conductivity is of order of  $10^8$  km/s (~ 10 mho) for the daytime ionosphere and 256  $10^7$  km/s (~ 1 mho) for the nighttime ionosphere (Leonovich & Mazur, 1993; South-257 wood & Hughes, 1983). 258

Let's obtain criterion for distinguishing cases of high and low ionospheric conductivity ("fixed-end" or "free-end" mode of Alfvén wave). Providing the wave is observed near the geomagnetic equator, the expressions from Table. 1 are valid. For high conductive ionosphere, the difference between the dimensionless values of hemispheres conductivity according to Table. 1 is defined as:

$$\left(\epsilon^{+} - \epsilon^{-}\right) = -\frac{2\omega}{k_{0}c} \frac{B_{r}}{E_{a}} \tag{25}$$

Since the ionosphere is high conductive medium  $\epsilon^{\pm} \ll 1$ , the relation between the magnetic and electric field of the observed ULF wave is as follows:

$$\left|\frac{2\omega}{k_0 c} \frac{B_r}{E_a}\right| \ll 1 \tag{26}$$

For the low ionospheric conductivity  $\epsilon^{\pm} \gg 1$ , the inverse dimensionless values of hemispheres conductivity according to Table. 1 is written as:

$$\left(\frac{1}{\epsilon^+} - \frac{1}{\epsilon^-}\right)^{-1} = -\frac{\omega}{2k_0c}\frac{B_r}{E_a}$$
(27)

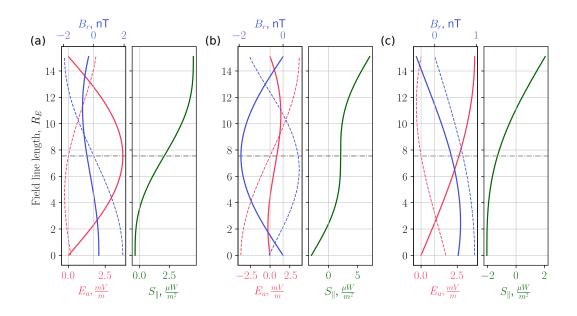


Figure 2. Parallel structure of the Alfvén wave and field aligned Poynting vector component calculated using the ionospheric conductivity estimation model for for the following cases: (a)  $\epsilon^{\pm} \ll 1$ , (b)  $\epsilon^{\pm} \gg 1$ , (c)  $\epsilon^{+} \gg 1$ ,  $\epsilon^{-} \ll 1$ . The solid lines are the real part of calculated values, the dashed lines are the imaginary ones

Then using that fact that the ionosphere is low-conducting  $\epsilon^{\pm} \gg 1$ , we obtain next result for relation between magnetic and electric fields of the observed wave:

$$\left|\frac{\omega}{2k_0c}\frac{B_r}{E_a}\right| \gg 1\tag{28}$$

Criteria (26) and (28) means that the proposed parameter  $\epsilon^{\pm}$  should be greater than unity in the case of low conductivity. Otherwise, there is a case of high ionospheric conductivity. The case when proposed criteria equal to unity is not considered due to the fact that the decay decrement will have a value of the order of the wave frequency. It means the wave attenuates very quickly and cannot exist.

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### 5 Estimation ionospheric conductivity during the 27 October 2012 event

The event of 27 October 2012 was observed near geomagnetic equator. Thus, the model proposed in section 4 is applicable for estimation of ionospheric conductivity. Fig. 2 shows an example of how, based on spacecraft data, it is possible to restore the standing structure of the observed wave for different ionosphere conductivity conditions.

Phase shift between radial magnetic field and azimuthal electric field is about 180°
for symmetric conditions on ionosphere (Fig.2a,b). Furthermore the case of asymmetric ionospheric conductivity represented on Fig.2c is not suitable because of the peculiarities of the observed wave.

The criteria (26) and (28) were checked for distinguishing symmetric conductivity conditions on the ionosphere. The criterion (26) is met during the observed wave event. In this case one can conclude that ionospheric conductivity was high for both the hemispheres and the almost "fixed-end" mode of the wave was established. Then standing structure of the wave according to the simulation results had the forms as shown in the Fig. 2a. Besides, we known that the observed wave was in the drift resonance with energetic electrons, and if ionospheric conductivity were low, then the azimuthal electric field of the wave would be asymmetrical and the drift resonance would not be observed.

According to the observational data and equations in Table 1 the difference between 296 dimensionless conductivity parameters for both hemisphere  $\epsilon^+ - \epsilon^-$  is equal to 0.476. It 297 is assumed that the difference in the conductivity values may be caused by the fact that 298 the footprints of the spacecraft trajectory, where the event observed, were located on dif-200 ferent sides from the terminator line. For verification, the Tsyganenko model T96 (Tsyganenko, 300 1996) was used to calculate the spacecraft footprints. The terminator line was computed 301 using the Cartopy library of the Python (Met Office, 2010 - 2015). The results are shown 302 in Fig. 3 for the time 04:53 UT when the maximum value of parallel Poynting flux  $\overline{S}_{\parallel}$ 303 was registered (Fig. 1a). At that time the spacecraft was located at the magnetic field 304 line corresponding to the magnetic shell  $L \approx 6.2R_E$ . Fig. 3 shows that the northern 305 footprint of spacecraft trajectory is located on the night-side ionosphere, and the south-306 ern one is on the day-side ionosphere. 307

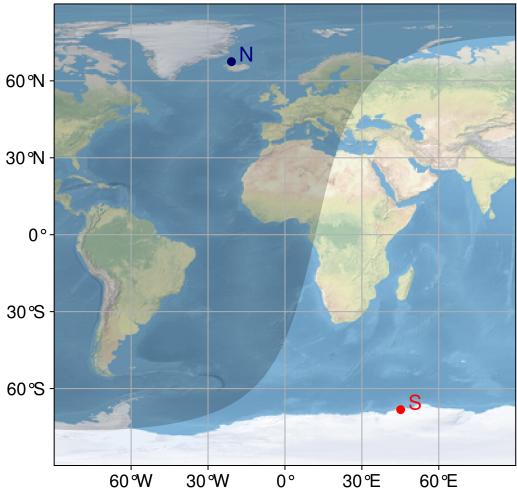
As mentioned in section 4 in order to estimate height-integrated Pedersen conduc-308 tivity the fixed conductivity for one hemisphere is required to set up. In our research, 309 height-integrated Pedersen conductivity in the Southern hemisphere  $(\Sigma_P)$  is given by the 310 ionosphere model IRI-2016 (Bilitza et al., 2017). The values of height-integrated Ped-311 ersen conductivity is represented in Table 2 based on IRI-2016 model and our method. 312 The order of value of the obtained height-integrated conductivities is consistent with the 313 theoretical estimates from the papers (Southwood & Hughes, 1983; Leonovich & Mazur, 314 1993) and observational results in (Obana et al., 2008; Ieda et al., 2014; Obana et al., 315 2015). Dimensionless conductivity parameter for the Northern hemisphere according to 316 the IRI-2016 model is greater than one. Therefore, the observed wave must be the quarter-317 wave, what means the phase shift between electric and magnetic field of the wave should 318 be around 90°. But according to spacecraft data, this is not observed (Fig. 1a).

**Table 2.** Height-integrated Pedersen conductivity for the Northern and Southern footprints of the magnetic field line on the 27 October 2012 according to the suggested method at 04:53 UT and the ionosphere model IRI-2016 at 05:00 UT. The last are taken at an altitude of 1000 km above sea

	IRI-2016	Our method
$\overline{\Sigma^-, \text{ mho } (\text{km/s})}$	9.610 (8.65	$5 \times 10^{6}$ )
$\epsilon^{-}$	0.04	.3
$\overline{\Sigma^+, \text{ mho } (\text{km/s})}$	$0.190 (1.71 \times 10^6)$	$0.795 (7.16 \times 10^6)$
$\overline{\epsilon^+}$	2.172	0.519

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There are two factors which can explain difference in the values of height-integrated 320 Pedersen conductivity for Northern hemisphere  $\Sigma_P^+$ . As shown in Fig. 3 the footprints 321 of magnetic field line is located in polar region. In (Bjoland et al., 2016) with compared 322 IRI-2016 model and EISCAT Svalbard radar, it was shown that at the high-latitudes re-323 gions model IRI-2016 can underestimate electron density. Another study (Lyakhov et 324 al., 2019) also showed that in transit time (04-08 MLT, from nighttime to daytime), only 325 25% of calculations based on the IRI-2016 model are within the instrumental accuracy 326 of DE-2 satellite measurements  $(0\pm15\%)$ . The model IRI-2016 may incorrectly take into 327



## 2012-10-27 04:53:00UT

Figure 3. Terminator line and Northern (N) and Southern (S) footprints of the magnetic field line calculated using Tsyganenko model T96 (Tsyganenko, 1996) for the altitude 1000 km above the sea. The terminator and footprints were evaluated from data of event 27 October 2012 at 04:53 UT

account the conditions of the external ionosphere and twilight at all altitudes. Also, it can not properly consider the impact of ionization processes in night side ionosphere.

On the other hand, our proposed method is limited. The use of assumptions that the field enter to the ionosphere on the normal to it, straight magnetic field lines and the requirement of the wave be observed near the geomagnetic equator, influence estimation the relationship between the conductivities. However, the method shows the possibility to use spacecraft data to estimate ionospheric conductivity and their influence on structure of standing Alfvén. The method can be improved by using the dipole model of the magnetic field.

### **6** Conclusion

The effect of different conductivity of the magnetically conjugated parts of the iono-338 sphere on the structure of standing Alfvén waves using an analytical model with straight 339 magnetic field lines is considered in this paper. Based on the model, a method was de-340 veloped that allows to estimate the height-integrated Pedersen conductivity at magnet-341 ically conjugated points of the ionosphere with spacecraft observations of magnetospheric 342 Alfvén waves. A criterion distinguishing the "fixed-end" and "free-end" of the half-wave 343 mode of the standing Alfvén wave was also obtained from the model. Due to the pro-344 posed method, the observational features of the October 27, 2012 event were explained 345 by the difference in conductivity values at the Northern and Southern ionosphere. Pro-346 ceeding to the criteria, a half-wave mode of the Alfvén wave with almost "fixed-end" at 347 magnetically conjugated points of the ionosphere was proved to be observed for this event. 348 With given Pedersen conductivity for the Southern ionosphere from IRI-2016 model, the 349 conductivity for the Northern ionosphere was estimated. It is shown that the difference 350 in the conductivity values are caused by the fact that footprints of spacecraft trajectory, 351 where the event observed, were located on different sides from the terminator line. 352

### 353 Data Availability Statement

The Van Allen Probes data used in this paper are available at the CDAWeb site (https://cdaweb.gsfc.nasa.gov/pub/data/rbsp/rbspa/). The height-integrated Pedersen conductivity data are available at World Data Center for Geomagnetism, Kyoto (https://wdc.kugi.kyoto-u.ac.jp/ionocond/sigcal/index.html).

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Figure 1.

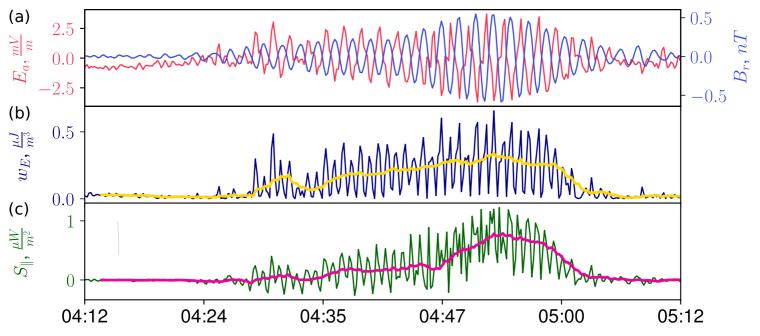


Figure 2.

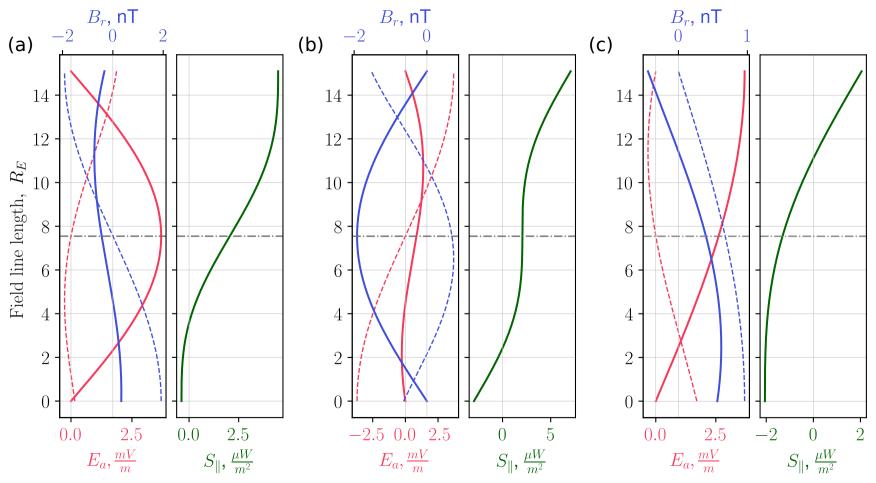
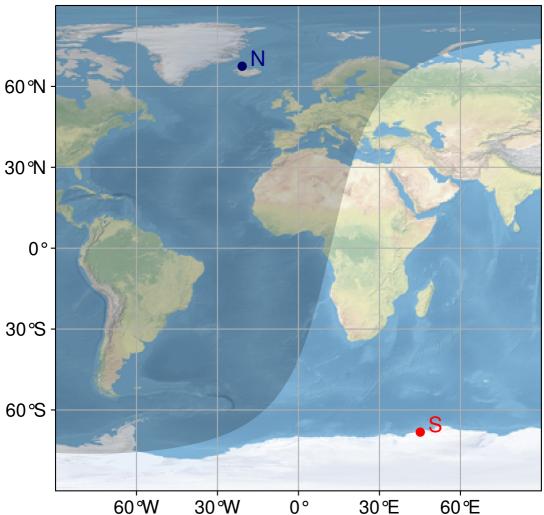


Figure 3.

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## Diagnostics of the ionospheric conductivity based on spacecraft observations of the magnetospheric ULF waves

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### Key Points:

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7	•	A method for estimating the ionospheric conductivity based on spacecraft obser-
8		vations of Alfvén waves in the magnetosphere is proposed
9	•	The parallel structure of an Alfvén wave under various conditions of the ionospheric
10		conductivity is reconstructed
11	•	The height-integrated Pedersen conductivity of the ionosphere were estimated for
12		the October 27, 2012 event

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#### 13 Abstract

In 27 October 2012 the ULF wave in Pc4 range being Alfvén wave was observed with 14 Van Allen Probe A. In the event the parallel Poynting flux of the wave was directed to-15 wards the Northern ionosphere. Assuming that this may be caused by the asymmetry 16 of ionospheric conductivity between the Northern and Southern hemispheres, its effect 17 on the standing structure of the Alfvén wave was investigated in this paper. For this pur-18 pose the analytical model with straight magnetic field lines was used. As a result the method 19 for estimation of the Northern and Southern ionospheric conductivity was developed. It 20 allows us to reconstruct the parallel structure of Alfvén waves under various conditions 21 of the ionospheric conductivity. With the method developed, the ionospheric conduc-22 tivity for the October 27, 2012 event was evaluated and compared with ionosphere model 23 IRI-2016. 24

### <sup>25</sup> Plain Language Summary

The most commonly observed ULF waves in the magnetosphere are Alfvén waves 26 standing along magnetic field line between magnetically conjugated points of the iono-27 sphere located in opposite hemispheres. In this paper we considered how the north-south 28 asymmetry of the ionospheric conductivity influences on standing Alfven wave's paral-29 lel structure. The model predicts that the structure of the Alfvén waves may differ de-30 pending on the conductivity values of Northern and Southern ionospheres. Based on the 31 32 model we developed the method to carry out a qualitative estimation of the ionospheric height-integrated Pedersen conductivity using parameters of Alfvén waves observed with 33 spacecraft in the magnetosphere. As a result, for the 27 October 2012 event the paral-34 lel structure of the observed Alfvén wave was reconstructed and the ionospheric conduc-35 tivity was estimated. We found a significant difference in the conductivity values of the 36 Northern and Southern ionospheres. The mean is that the magnetically conjugated foot-37 prints of spacecraft trajectory, where the event observed, were located on different sides 38 from the line that divides the day side and the night side of Earth (terminator line). 39

### 40 1 Introduction

Studies of the coupled system of ionosphere-magnetosphere is of crucial importance 41 for the plasma processes in the near-Earth's space. An important part of this system is 42 the ultra low frequency (ULF) waves, observed both in space and on the ground. The 43 ULF waves are the field line oscillations with frequencies of the order or lower than the 44 proton gyrofrequency. The most widespread classification categorizes these wave into reg-45 ular pulsations Pc1–5 ranges (periods from 0.2 to 600 s) and irregular Pi1–2 pulsations 46 (periods from 1 to 150 s) (Jacobs et al., 1964). These waves are interpreted in terms of 47 magnetohydrodynamic (MHD) oscillations. Major part of the ULF waves are identified 48 with the Alfvén waves standing along the field line between the magnetically conjugated 49 points of ionosphere (Dungey, 1954; Radoski, 1967; Chen & Hasegawa, 1974; Southwood, 50 1974). 51

Standing Alfvén waves are often used for the diagnostics of the magnetospheric plasma 52 (Troitskaya & Gul'elmi, 1967; Chi & Russell, 2005; Menk & Waters, 2013). Indeed, the 53 Alfvén speed is inversely proportional to square root of the mass density, thus the ob-54 served wave's frequency allows one to reproduce plasma density distribution (Berube et 55 al., 2006; Takahashi & Denton, 2007). A number of papers were devoted to calculation 56 of the structure of the standing Alfvén waves with different distributions of density and 57 other magnetospheric parameters (Cummings et al., 1969; Orr & Matthew, 1971; Allan 58 & Knox, 1979a; Leonovich & Mazur, 1993; Ozeke & Mann, 2004; Pilipenko et al., 2005; 59 Degeling et al., 2010; Petrashchuk et al., 2022). 60

However, there is yet another factor influencing wave's structure and frequency, the 61 ionospheric conductivity. The studies of the influence of the conductivity on the stand-62 ing Alfvén waves began with works (Scholer, 1970; Inoue, 1973; Maltsev et al., 1974; Hughes, 63 1974; Hughes & Southwood, 1976). Those papers considered ionosphere as a thin layer, which is justified for the long-period ULF waves (Pi2, Pc4-5). It was shown that the in-65 cident wave's magnetic field is reflected from the ionosphere due to the Pedersen con-66 ductivity, while the electric field reaches the ground due to the Hall conductivity. Fur-67 ther investigations of the ionosphere-magnetosphere interaction by means of the Alfvén 68 waves were performed in (Alperovich & Fedorov, 1984; Glassmeier, 1984; Hameiri & Kivel-69 son, 1991; Leonovich & Mazur, 1991, 1996; Yoshikawa & Itonaga, 1996; Yoshikawa et al., 70 2002; Sciffer & Waters, 2002; Cheremnykh & Parnowski, 2006; Erkaev et al., 2006; Wa-71 ters et al., 2013). 72

Two limiting cases are worth mentioning. If the conductivity is high, then the wave's electric field equals zero on the ionosphere:  $E_{\pm} = 0$ , where the "+" and "-" signs refer to the conjugate ionospheres. In this case, the oscillating magnetic field line behave as if fixed in the points of intersection with the ionosphere. This oscillation is usually called the "rigid-end" mode (Cummings et al., 1969; Sinha & Rajaram, 1997).

In the opposite case, the conductivity is very small. In this case, the field aligned derivative of the wave's electric field equals zero on the ionosphere:  $(\partial E/\partial l)_{\pm} = 0$ , where *l* is a length along the field line. As a result the field line freely slides on the ionosphere. Such mode is called the "free-end mode" (Newton et al., 1978; Allan & Knox, 1979a). In both cases, between the conjugate ionospheres fit an integer half-waves, the Alfvén waves standing along the field line with no energy flux in this direction.

However, the situation is possible where the conductivities on the Northern and 84 Southern magnetically conjugated points are drastically different. It can be caused by 85 the asymmetry of Pedersen conductivity between the Northern and Southern hemispheres. 86 This situation can occur in the polar ionosphere near the solstices, when one hemisphere 87 is illuminated for a long time and the other is correspondingly in darkness (Glassmeier 88 et al., 1999). In this case, a situation is possible where one end of the field line is fixed, 89 and the other freely slides on the ionosphere. Then between the conjugate ionospheres 90 fit an integer quarter-waves. For the first time, such possibility was mentioned in (Allan 91 & Knox, 1979a). Results of further theoretical studies of the quarter-waves were reported 92 in (Allan & Knox, 1979b; Allan, 1983; Bulusu et al., 2014, 2016). The observational ev-93 idences for the quarter-waves were presented in (Allan, 1983; Budnik et al., 1998; Bu-94 lusu et al., 2015; Obana et al., 2008, 2015). 95

The observational manifestations of the Alfvén waves at the asymmetric ionospheres are different from those in the symmetric case. Indeed, the frequency of the leading quarterwave harmonic approximately two times lower than for the half-wave, there is field aligned energy flux. Thus, the Alfvén waves can be used for diagnostics of the ionosphere (Lee et al., 2004; Ozeke & Mann, 2004; Bulusu et al., 2015; Bulusu et al., 2016; Lysak et al., 2020).

Usually, ionospheric conductivities are determined in several ways. One method 102 is based on the using of the models of the atmosphere, ionosphere and magnetic field with 103 equations derived in (Maeda, 1977). For example, paper (Obana et al., 2015) used the 104 atmosphere model MSISE-90, the ionosphere model IRI 95, and near-Earth geomagnetic 105 field model IGRF 95. In another method the ground based instruments are used. The 106 difficulty here appears in the necessity to use either data of combined observations from 107 different instruments, for example, all sky cameras and riometers (Senior et al., 2008); 108 either, special radar measurement programs and empirical models ought to be used (Ieda 109 et al., 2014). Also, the low-orbital satellite data can be used, like SWARM mission. In 110 the case of single satellite, calculation of the ionospheric conductivity demands using rather 111

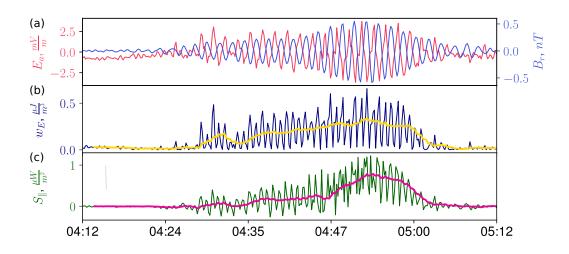


Figure 1. Peculiarities during the 27 October 2012 event: (a) the radial component of the wave's magnetic field  $B_r$  (blue line) and the azimuthal component of the wave's electric field  $E_a$  (red line); (b) the electric field energy density  $w_E$  (dark blue line) and  $\overline{w}_E$  (yellow line) averaged over the wave period T = 100 c(c) the same for parallel Poynting flux  $S_{\parallel}$  (green line) and  $\overline{S}_{\parallel}$  (red line).

complicated method which give results only along the satellite trajectory (Juusola et al.,
 2016).

#### <sup>114</sup> 2 27 October 2012 wave event

Let us consider the 27 October 2012 event, in which a poloidal Alfvén wave was 115 observed with The Van Allen Probe A. The wave was registered in the morning part of 116 the magnetosphere at a distance  $6.2R_E$ . During the event we observed the resonance 117 generation of the ULF wave by the 38 keV electron flux. The electron flux was injected 118 to the magnetosphere due to the substorm. The wave was the fundamental harmonic of 119 the standing Alfvén wave with a frequency 10 mHz and azimuthal wave number  $m \approx$ 120 110 - 115. The wave interacted with electrons via the drift resonance and was gener-121 ated through the gradient instability. The detailed study of the event is presented in (Mikhailova 122 et al., 2022). 123

We revealed several peculiarities during the 27 October 2012 event studying, which 124 were not mentioned in (Mikhailova et al., 2022). At the figure (Fig. 1) the wave field com-125 ponents, the electric field energy density  $w_E$  and the parallel Poynting flux  $S_{\parallel}$ , and their 126 values averaged over the wave period T = 100 c are presented. One can see that phase 127 shift between the radial component of the wave's magnetic field  $B_r$  and the azimuthal 128 component of the wave electric field  $E_a$  is about 180°, rather than 90°, as is usually ex-129 pected for standing waves. Moreover the Poynting flux was directed toward the North-130 ern ionosphere (Fig. 1b). We suggest that these observational peculiarities can be caused 131 by the asymmetry of Pedersen conductivity between the Northern and Southern iono-132 spheres. 133

### <sup>134</sup> **3** Principal equations

Let us consider the equation for an Alfvén wave. In the homogeneous background magnetic field and plasma it has a form:

$$\frac{\partial^2 E_j}{\partial l^2} + k_{\parallel}^2 E_j = 0, \tag{1}$$

where  $E_j$  is a component of the wave electric field (under index j is assumed r for the radial component and a for azimuthal one),  $k_{\parallel} = \omega/v_A$  is the parallel component of wave vector,  $\omega$  is the wave frequency,  $v_A$  is the Alfvén speed, l is a coordinate along the magnetic field line. The parallel component of electric field is not considered because it equals to zero in a MHD approximation. We assume the straight magnetic field lines.

The boundary condition for Alfvén waves on the ionosphere were determined in a lot of papers (Hughes, 1974; Hughes & Southwood, 1976; Newton et al., 1978; Leonovich & Mazur, 1991). It can be written in the form

$$E_j|_{l_{\pm}} = \mp i \frac{\epsilon^{\pm}}{k_{\parallel}} \frac{\partial E_j}{\partial l}\Big|_{l_{\pm}}, \qquad (2)$$

where  $l_{\pm}$  is the coordinate of the Southern  $(l_{-})$  and Northern  $(l_{+})$  ionospheric boundaries, the dimensionless parameter  $\epsilon^{\pm}$  is inversely proportional to the height-integrated Pedersen conductivity  $\Sigma_{P}^{\pm}$ ,

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$$e^{\pm} = \frac{c^2}{4\pi\Sigma_P^{\pm}v_A},\tag{3}$$

c is the speed of light. Eq. (2) assumes the field to enter to the ionosphere on the normal to it. For more general case, see (Leonovich & Mazur, 1991). The boundary condition (2) determines the damping decrement of the standing Alfvén wave under dissipation in the ionosphere. This one is caused by ionospheric Joule heating at the field line
basement (Southwood & Hughes, 1983).

We use the coordinate  $l_{-} = 0$  as a coordinate of the Southern ionosphere boundary and  $l_{+} = l_{I}$  as a coordinate of the Northern one. The length of the magnetic filed line  $l_{I}$  can be obtained from the expression

$$l_I = LR_E \int_{-\theta_I}^{\theta_I} \sqrt{1 + 3\sin^2\theta} \cos\theta d\theta, \qquad (4)$$

(5)

where L is a McIlwain parameter,  $\pm \theta_I$  is the geomagnetic latitude of the Southern (-) and Northern (+) points of intersection of the magnetic field line with the ionosphere. The latitude can be found from the magnetic filed line equation of the dipole magnetic field  $r = LR_E \cos^2 \theta$ , assuming  $r = R_E + h_I$ , where  $h_I$  is height of the upper boundary of the ionosphere (Chapman & Sugiura, 1956).

The dimensionless conductivity parameter  $\epsilon^{\pm}$  (3) let us to take into account different values of Pedersen conductivity at the points of intersection. They are

1. High conductivity of the ionosphere at both the hemispheres:  $\epsilon^{\pm} \ll 1$ ;

<sup>164</sup> 2. Low conductivity of the ionosphere at both the hemispheres:  $\epsilon^{\pm} \gg 1$ ;

<sup>165</sup> 3. Asymmetric conductivity at the different hemispheres:  $\epsilon^+ \gg 1, \epsilon^- \ll 1$ .

It was assumed at all these cases that the ionospheric conductivities at the different hemispheres have the different absolute value.

The general solution of the wave equation (1) can be represented as

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$$E_j = C_1 \exp\left(ik_{\parallel}l\right) + C_2 \exp\left(-ik_{\parallel}l\right).$$

Using boundary condition (2) we found the expression for the coefficients  $C_1$  and  $C_2$ , and equation for the parallel wave vector  $k_{\parallel}$ :

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$$(1 - \epsilon^{-})(1 - \epsilon^{+}) \exp(ik_{\parallel}l_{I}) - (1 + \epsilon^{-})(1 + \epsilon^{+}) \exp(-ik_{\parallel}l_{I}) = 0.$$
(6)

To solve (6) let us consider two limiting cases: (i) high conductivity,  $\epsilon^{\pm} \ll 1$ ; (ii) low conductivity,  $\epsilon^{\pm} \gg 1$ . In both cases, the parallel wave vector can be represented in the form  $\pi N$ 

$$k_{\parallel} = k_0 + \delta k, \quad k_0 = \frac{\pi N}{l_I},\tag{7}$$

where N is the harmonic wave number, and  $\delta k$  is a small addition caused by small value of  $\epsilon^{\pm}$  in the first case and small value of  $(\epsilon^{\pm})^{-1}$  in the second case. As result, we found the small value  $\delta k$  and the wave electric field, and, correspondingly, wave magnetic field

$$B_a = -i\frac{c}{\omega}\frac{\partial E_r}{\partial l}, \quad B_r = i\frac{c}{\omega}\frac{\partial E_a}{\partial l} \tag{8}$$

the parallel Poynting flux averaged over the wave period

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$$\overline{S}_{\parallel} = \frac{c}{8\pi} (E_r B_a^* - E_a B_r^*). \tag{9}$$

In the case of high ionospheric conductivity,  $\epsilon^{\pm} \ll 1$ , the parallel structure of the wave's electromagnetic field is determined as

$$E_{a,r} = \begin{pmatrix} E_{a0} \\ E_{r0} \end{pmatrix} \left[ \sin k_0 l - i \left( \frac{\epsilon^- + \epsilon^+}{l_I} l - \epsilon^- \right) \cos k_0 l \right]$$
(10)

$$B_{a,r} = \begin{pmatrix} -B_{a0} \\ B_{r0} \end{pmatrix} \left[ \frac{\epsilon^- + \epsilon^+}{k_0 l_I} \cos k_0 l - \left( \frac{\epsilon^- + \epsilon^+}{l_I} l - \epsilon^- \right) \sin k_0 l + i \cos k_0 l \right]$$
(11)

where  $E_{a0}$  and  $E_{r0}$  are the amplitudes of the azimuthal and radial components of the wave electric field, and

$$B_{a0} = E_{r0} \frac{k_0 c}{\omega}, \quad B_{r0} = E_{a0} \frac{k_0 c}{\omega}$$
(12)

<sup>190</sup> are the amplitudes of the azimuthal and radial components of the wave magnetic field.

In the opposite low conductivity case,  $\epsilon^{\pm} \gg 1$ , the Alfvén wave's parallel structure can be represented as

$$E_{a,r} = \begin{pmatrix} E_{a0} \\ E_{r0} \end{pmatrix} \left[ \cos k_0 l - i \left[ \left( \frac{1}{\epsilon^-} + \frac{1}{\epsilon^+} \right) \frac{l}{l_I} - \frac{1}{\epsilon^-} \right] \sin k_0 l \right]$$
(13)

$$B_{a,r} = \begin{pmatrix} -B_{a0} \\ B_{r0} \end{pmatrix} \left[ \left( \frac{1}{\epsilon^{-}} + \frac{1}{\epsilon^{+}} \right) \frac{\sin k_0 l}{k_0 l_I} - \left[ \left( \frac{1}{\epsilon^{-}} + \frac{1}{\epsilon^{+}} \right) \frac{l}{l_I} - \frac{1}{\epsilon^{-}} \right] \cos k_0 l + i \sin k_0 l \right]$$
(14)

For the case of the asymmetric ionosphere (low conductivity of the Northern ionosphere,  $\epsilon^+ \gg 1$ , and high conductivity of the Southern ionosphere,  $\epsilon^- \ll 1$ , the parallel wave vector is

$$k_{\parallel} = \frac{1}{2}k_0 + \delta k \tag{15}$$

<sup>199</sup> the parallel structure is represented as

$$E_{a,r} = \begin{pmatrix} E_{a0} \\ E_{r0} \end{pmatrix} \left[ \sin \frac{k_0 l}{2} - i \left[ \left( \epsilon^- + \frac{1}{\epsilon^+} \right) \frac{l}{l_I} - \epsilon^- \right] \cos \frac{k_0 l}{2} \right]$$
(16)

$$B_{a,r} = \frac{1}{2} \begin{pmatrix} -B_{a0} \\ B_{r0} \end{pmatrix} \left[ 2\left(\epsilon^{-} + \frac{1}{\epsilon^{+}}\right) \frac{\cos\frac{k_{0}l}{2}}{k_{0}l_{N}} - \left[\left(\epsilon^{-} + \frac{1}{\epsilon^{+}}\right) \frac{l}{l_{N}} - \epsilon^{-} \right] \sin\frac{k_{0}l}{2} + i\cos\frac{k_{0}l}{2} \right] (17)$$

Let us consider properties of the wave's parallel structure on the equator, where  $l = l_I/2$ . Expressions for the azimuthal component of the wave's electric field  $E_a$ , the radial component of the magnetic field and the parallel Poynting flux  $S_{\parallel}$  are presented in Table 1, where  $\Delta \phi$  is the phase shift between  $B_r$  and  $E_a$  components, and

$$S_0 = \frac{c^2 k_0}{16\pi\omega} (E_{a0}^2 + E_{r0}^2).$$
(18)

It is worth to note that only the highest order terms are written.

Table 1. Expressions for the azimuthal component of the wave's electric field  $E_a$ , the radial component of the magnetic field and the parallel Poynting flux on the geomagnetic equator for the fundamental harmonic (N = 1)

Case	$E_a\left(\frac{l_I}{2}\right)$	$B_r\left(\frac{l_I}{2}\right)$	$\overline{S}_{\parallel}\left(rac{l_{I}}{2} ight)$	$\Delta \phi$
$ \frac{\epsilon^{\pm} \ll 1}{\epsilon^{\pm} \gg 1} $	$E_{a0}$	$-\frac{B_{r0}}{2}(\epsilon^+ - \epsilon^-)$	$S_0\left(\epsilon^+ - \epsilon^- ight)$	$ \begin{array}{c} \sim 180^{\circ}, 0^{\circ} \\ \sim 180^{\circ}, 0^{\circ} \end{array} $
$\epsilon^{-} \gg 1$ $\epsilon^{+} \gg 1, \ \epsilon^{-} \ll 1$	$-i\frac{1}{2}\left(\frac{1}{\epsilon^{+}}-\frac{1}{\epsilon^{-}}\right)$ $\frac{E_{a0}}{2\sqrt{2}}$	$iB_{r0} \ irac{B_{r0}}{2\sqrt{2}}$	$S_0 \left( \frac{1}{\epsilon^+} - \frac{1}{\epsilon^-} \right)$ $S_0 \left[ \frac{1}{2} \left( \frac{1}{\epsilon^+} - \epsilon^- \right) - \frac{1}{k_0 l_I} \left( \frac{1}{\epsilon^+} + \epsilon^- \right) \right]$	$\sim 180^{\circ}, 0^{\circ}$ $\sim 90^{\circ}$

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The following properties of the standing Alfvén wave on the geomagnetic equator
 are apparent from Table 1:

2111. The phase shift between the electric  $E_a$  ( $E_r$ ) and magnetic  $B_r$  ( $B_a$ ) fields for the212symmetric conditions is close to 180° or 0°, and for asymmetric conditions to 90°;2132. Since conductivities  $\Sigma_P^{\pm} \propto 1/\epsilon^{\pm}$ , then for the symmetric conditions the absolute214value and direction of the parallel Poynting flux  $S_{\parallel}$  is determined by the differ-215ence of the ionospheric conductivities ( $\epsilon^{\pm} \gg 1$  case) or their reverse values ( $\epsilon^{\pm} \ll 1$  case).2173. For the asymmetric conditions, the absolute value and direction of the parallel Poynt-

ing flux is determined by the combination of the conductivity of one ionosphere and the conductivity reverse value of the other.

The correctness of the results is indicated by the coincidence of the phase shift under symmetric and asymmetric conditions at the boundaries of the ionosphere with early theoretical work (Newton et al., 1978; Southwood & Kivelson, 2001).

### 4 Ionospheric conductivity estimation model

Expressions received for standing Alfvén wave allow to estimate ionospheric conductivity based on spacecraft data processing of observing magnetospheric Alfvén waves. Inputs include wave parameters such as its period or frequency and wave electric and magnetic field and spacecraft coordinates. Since  $v_A = \omega/k_{\parallel}$  and  $k_{\parallel} \approx k_0 \equiv \pi N/l_I$  for  $\epsilon^{\pm} \ll 1$  and  $\epsilon^{\pm} \gg 1$  symmetric cases, then as follows from eq. (3)

$$\Sigma_P^{\pm} = \frac{c^2 k_0}{4\pi\omega\epsilon^{\pm}} = \frac{Nc^2}{4l_I\omega\epsilon^{\pm}} \tag{19}$$

where the length of magnetic field line  $l_I$  can be defined from (4).

With obtained model, the universal method of ionospheric conductivity estimation was developed. It is required to determine ratio between conductivities. For this point, the maximum value of the parallel Poynting flux averaged over the wave period  $\overline{S}_{\parallel}$  is used (Fig. 1c). Also, the period-averaged energy density of the wave electric or magnetic field

$$\overline{w}_E = \frac{1}{16\pi} (E_r E_r^* + E_a E_a^*), \quad \overline{w}_B = \frac{1}{16\pi} (B_r B_r^* + B_a B_a^*). \tag{20}$$

corresponding to this time is used. For example, as follows from Table 1 for the fundamental harmonic (N = 1) at the magnetic equator for  $\epsilon^{\pm} \ll 1$  case we have

$$\overline{w}_E = \frac{1}{16\pi} (E_{a0}^2 + E_{r0}^2). \tag{21}$$

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$$\left(\epsilon^{+} - \epsilon^{-}\right) = \frac{\omega}{c^{2}k_{0}} \frac{S_{\parallel}}{\overline{w}_{E}}.$$
(22)

For  $\epsilon^{\pm} \gg 1$  case we have

$$\overline{w}_B = \frac{1}{16\pi} (B_{a0}^2 + B_{r0}^2) = \frac{c^2 k_0^2}{16\pi\omega^2} (E_{a0}^2 + E_{r0}^2).$$
(23)

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$$\left(\frac{1}{\epsilon^+} - \frac{1}{\epsilon^-}\right) = \frac{k_0}{\omega} \frac{\overline{S}_{\parallel}}{\overline{w}_B}.$$
(24)

If the height-integrated Pedersen conductivity of one ionosphere is known (for example, Southern  $\Sigma_P^-$ ), then using the observed values of the period-averaged parallel Poynting flux and energy density the conductivity of the other ionosphere (Northern  $\Sigma_P^+$ ) can be calculated with eq. (19) and eq. (22) or eq. (24) depending on the case under consideration

The principle of operation is simple and requires only the availability of the data 250 from magnetospheric observation of Alfvén wave. Moreover, data from one spacecraft 251 is enough for the method to work. Note using method has disadvantage at this stage of 252 development. The fixed height-integrated Pedersen conductivity of one hemisphere is set 253 manually. This can be done using reference theoretical conductivity values or using other 254 empirical models or direct measurements. Thus, the characteristic height-integrated Ped-255 ersen conductivity is of order of  $10^8$  km/s (~ 10 mho) for the daytime ionosphere and 256  $10^7$  km/s (~ 1 mho) for the nighttime ionosphere (Leonovich & Mazur, 1993; South-257 wood & Hughes, 1983). 258

Let's obtain criterion for distinguishing cases of high and low ionospheric conductivity ("fixed-end" or "free-end" mode of Alfvén wave). Providing the wave is observed near the geomagnetic equator, the expressions from Table. 1 are valid. For high conductive ionosphere, the difference between the dimensionless values of hemispheres conductivity according to Table. 1 is defined as:

$$\left(\epsilon^{+} - \epsilon^{-}\right) = -\frac{2\omega}{k_{0}c} \frac{B_{r}}{E_{a}} \tag{25}$$

Since the ionosphere is high conductive medium  $\epsilon^{\pm} \ll 1$ , the relation between the magnetic and electric field of the observed ULF wave is as follows:

$$\left|\frac{2\omega}{k_0 c} \frac{B_r}{E_a}\right| \ll 1 \tag{26}$$

For the low ionospheric conductivity  $\epsilon^{\pm} \gg 1$ , the inverse dimensionless values of hemispheres conductivity according to Table. 1 is written as:

$$\left(\frac{1}{\epsilon^+} - \frac{1}{\epsilon^-}\right)^{-1} = -\frac{\omega}{2k_0c}\frac{B_r}{E_a}$$
(27)

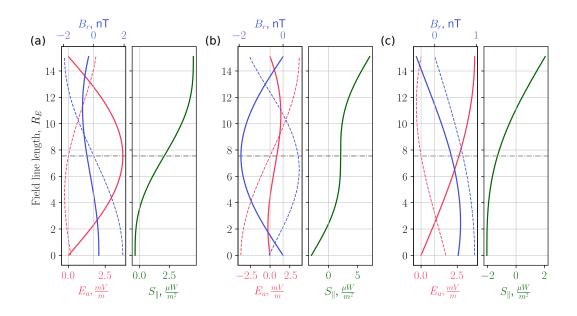


Figure 2. Parallel structure of the Alfvén wave and field aligned Poynting vector component calculated using the ionospheric conductivity estimation model for for the following cases: (a)  $\epsilon^{\pm} \ll 1$ , (b)  $\epsilon^{\pm} \gg 1$ , (c)  $\epsilon^{+} \gg 1$ ,  $\epsilon^{-} \ll 1$ . The solid lines are the real part of calculated values, the dashed lines are the imaginary ones

Then using that fact that the ionosphere is low-conducting  $\epsilon^{\pm} \gg 1$ , we obtain next result for relation between magnetic and electric fields of the observed wave:

$$\left|\frac{\omega}{2k_0c}\frac{B_r}{E_a}\right| \gg 1\tag{28}$$

Criteria (26) and (28) means that the proposed parameter  $\epsilon^{\pm}$  should be greater than unity in the case of low conductivity. Otherwise, there is a case of high ionospheric conductivity. The case when proposed criteria equal to unity is not considered due to the fact that the decay decrement will have a value of the order of the wave frequency. It means the wave attenuates very quickly and cannot exist.

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### 5 Estimation ionospheric conductivity during the 27 October 2012 event

The event of 27 October 2012 was observed near geomagnetic equator. Thus, the model proposed in section 4 is applicable for estimation of ionospheric conductivity. Fig. 2 shows an example of how, based on spacecraft data, it is possible to restore the standing structure of the observed wave for different ionosphere conductivity conditions.

Phase shift between radial magnetic field and azimuthal electric field is about 180°
for symmetric conditions on ionosphere (Fig.2a,b). Furthermore the case of asymmetric ionospheric conductivity represented on Fig.2c is not suitable because of the peculiarities of the observed wave.

The criteria (26) and (28) were checked for distinguishing symmetric conductivity conditions on the ionosphere. The criterion (26) is met during the observed wave event. In this case one can conclude that ionospheric conductivity was high for both the hemispheres and the almost "fixed-end" mode of the wave was established. Then standing structure of the wave according to the simulation results had the forms as shown in the Fig. 2a. Besides, we known that the observed wave was in the drift resonance with energetic electrons, and if ionospheric conductivity were low, then the azimuthal electric field of the wave would be asymmetrical and the drift resonance would not be observed.

According to the observational data and equations in Table 1 the difference between 296 dimensionless conductivity parameters for both hemisphere  $\epsilon^+ - \epsilon^-$  is equal to 0.476. It 297 is assumed that the difference in the conductivity values may be caused by the fact that 298 the footprints of the spacecraft trajectory, where the event observed, were located on dif-200 ferent sides from the terminator line. For verification, the Tsyganenko model T96 (Tsyganenko, 300 1996) was used to calculate the spacecraft footprints. The terminator line was computed 301 using the Cartopy library of the Python (Met Office, 2010 - 2015). The results are shown 302 in Fig. 3 for the time 04:53 UT when the maximum value of parallel Poynting flux  $\overline{S}_{\parallel}$ 303 was registered (Fig. 1a). At that time the spacecraft was located at the magnetic field 304 line corresponding to the magnetic shell  $L \approx 6.2R_E$ . Fig. 3 shows that the northern 305 footprint of spacecraft trajectory is located on the night-side ionosphere, and the south-306 ern one is on the day-side ionosphere. 307

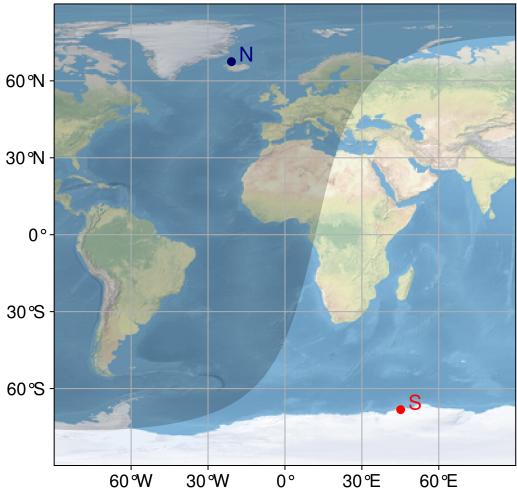
As mentioned in section 4 in order to estimate height-integrated Pedersen conduc-308 tivity the fixed conductivity for one hemisphere is required to set up. In our research, 309 height-integrated Pedersen conductivity in the Southern hemisphere  $(\Sigma_P)$  is given by the 310 ionosphere model IRI-2016 (Bilitza et al., 2017). The values of height-integrated Ped-311 ersen conductivity is represented in Table 2 based on IRI-2016 model and our method. 312 The order of value of the obtained height-integrated conductivities is consistent with the 313 theoretical estimates from the papers (Southwood & Hughes, 1983; Leonovich & Mazur, 314 1993) and observational results in (Obana et al., 2008; Ieda et al., 2014; Obana et al., 315 2015). Dimensionless conductivity parameter for the Northern hemisphere according to 316 the IRI-2016 model is greater than one. Therefore, the observed wave must be the quarter-317 wave, what means the phase shift between electric and magnetic field of the wave should 318 be around 90°. But according to spacecraft data, this is not observed (Fig. 1a).

**Table 2.** Height-integrated Pedersen conductivity for the Northern and Southern footprints of the magnetic field line on the 27 October 2012 according to the suggested method at 04:53 UT and the ionosphere model IRI-2016 at 05:00 UT. The last are taken at an altitude of 1000 km above sea

	IRI-2016	Our method
$\overline{\Sigma^-, \text{ mho } (\text{km/s})}$	9.610 (8.65	$5 \times 10^{6}$ )
$\epsilon^{-}$	0.04	.3
$\overline{\Sigma^+, \text{ mho } (\text{km/s})}$	$0.190 (1.71 \times 10^6)$	$0.795 (7.16 \times 10^6)$
$\overline{\epsilon^+}$	2.172	0.519

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There are two factors which can explain difference in the values of height-integrated 320 Pedersen conductivity for Northern hemisphere  $\Sigma_P^+$ . As shown in Fig. 3 the footprints 321 of magnetic field line is located in polar region. In (Bjoland et al., 2016) with compared 322 IRI-2016 model and EISCAT Svalbard radar, it was shown that at the high-latitudes re-323 gions model IRI-2016 can underestimate electron density. Another study (Lyakhov et 324 al., 2019) also showed that in transit time (04-08 MLT, from nighttime to daytime), only 325 25% of calculations based on the IRI-2016 model are within the instrumental accuracy 326 of DE-2 satellite measurements  $(0\pm15\%)$ . The model IRI-2016 may incorrectly take into 327



## 2012-10-27 04:53:00UT

Figure 3. Terminator line and Northern (N) and Southern (S) footprints of the magnetic field line calculated using Tsyganenko model T96 (Tsyganenko, 1996) for the altitude 1000 km above the sea. The terminator and footprints were evaluated from data of event 27 October 2012 at 04:53 UT

account the conditions of the external ionosphere and twilight at all altitudes. Also, it can not properly consider the impact of ionization processes in night side ionosphere.

On the other hand, our proposed method is limited. The use of assumptions that the field enter to the ionosphere on the normal to it, straight magnetic field lines and the requirement of the wave be observed near the geomagnetic equator, influence estimation the relationship between the conductivities. However, the method shows the possibility to use spacecraft data to estimate ionospheric conductivity and their influence on structure of standing Alfvén. The method can be improved by using the dipole model of the magnetic field.

### **6** Conclusion

The effect of different conductivity of the magnetically conjugated parts of the iono-338 sphere on the structure of standing Alfvén waves using an analytical model with straight 339 magnetic field lines is considered in this paper. Based on the model, a method was de-340 veloped that allows to estimate the height-integrated Pedersen conductivity at magnet-341 ically conjugated points of the ionosphere with spacecraft observations of magnetospheric 342 Alfvén waves. A criterion distinguishing the "fixed-end" and "free-end" of the half-wave 343 mode of the standing Alfvén wave was also obtained from the model. Due to the pro-344 posed method, the observational features of the October 27, 2012 event were explained 345 by the difference in conductivity values at the Northern and Southern ionosphere. Pro-346 ceeding to the criteria, a half-wave mode of the Alfvén wave with almost "fixed-end" at 347 magnetically conjugated points of the ionosphere was proved to be observed for this event. 348 With given Pedersen conductivity for the Southern ionosphere from IRI-2016 model, the 349 conductivity for the Northern ionosphere was estimated. It is shown that the difference 350 in the conductivity values are caused by the fact that footprints of spacecraft trajectory, 351 where the event observed, were located on different sides from the terminator line. 352

### 353 Data Availability Statement

The Van Allen Probes data used in this paper are available at the CDAWeb site (https://cdaweb.gsfc.nasa.gov/pub/data/rbsp/rbspa/). The height-integrated Pedersen conductivity data are available at World Data Center for Geomagnetism, Kyoto (https://wdc.kugi.kyoto-u.ac.jp/ionocond/sigcal/index.html).

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