

# Modeling the Impact of Geomagnetically Induced Currents on Electrified Railway Signalling Systems in the United Kingdom

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1           **Modeling the Impact of Geomagnetically Induced**  
2           **Currents on Electrified Railway Signalling Systems in**  
3           **the United Kingdom**

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7           **Key Points:**

- 8           • A model has been set up to examine geomagnetic effects on DC signalling systems  
9           on AC-electrified railways
- 10          • Signal misoperations occurred in both modelled UK railway lines when electric  
11          fields expected to arise once every 30 years were applied
- 12          • Extreme 1 in 100-year geoelectric fields would cause a large number of signal misop-  
13          erations in both UK railway lines studied

## Abstract

Studies of space weather impacts on ground-based infrastructure have been largely focused on power networks and pipelines, but railway signalling systems are also affected, with misoperations observed in several countries. This paper advances recent theoretical work on geomagnetically induced currents in railway signalling systems by modelling realistic railway lines with parameters from current industrial standards. Focusing on two example lines in the United Kingdom with different locations and orientation, a range of uniform electric fields are simulated along each modelled line. The results show that misoperations could be caused by geomagnetic interference at disturbance levels expected to recur over timescales of several decades. We also demonstrate that the UK estimate for the geoelectric field induced by a 1 in 100-year extreme storm would be strong enough to cause widespread signal misoperations in both lines studied.

## Plain Language Summary

Naturally occurring geomagnetic disturbances caused by space weather can interfere with technological infrastructure in space and on Earth. Previous measurements show that railways in several countries have been impacted, with geomagnetic interference in signalling systems causing wrong signals to be shown. Signalling misoperations can occur when currents that are induced in the rails by space weather interfere with the preset currents from railway infrastructure used to detect trains. This study demonstrates a model that analyses the impacts of geomagnetic activity on two railway lines in the United Kingdom with different orientation and location. The results show that the signalling systems on both lines are susceptible to misoperations caused by geomagnetic interference with a recurrence timescale of several decades. The UK estimates for a 1 in 100 year extreme storm were strong enough to cause a large number of signal misoperations in both lines.

## 1 Introduction

Space weather poses a risk to infrastructure in space and on the ground. Geomagnetically induced currents (GIC) are one of the foremost space weather hazards. During geomagnetic disturbances, fluctuating ionospheric currents produce changes to the magnetic fields observed at the Earth's surface. As described by Faraday's Law of Induction, this rapidly changing magnetic field drives electric currents in the Earth and through grounded conductors such as power transmission networks (Pirjola, 1985; Boteler, 2014; Lewis et al., 2022), oil and gas pipelines (Pulkkinen et al., 2002; Boteler & Trichtchenko, 2015) and railways (Darch et al., 2014).

A detailed examination of interference from geomagnetic storms in the Swedish railway signalling system was carried out by Alm (1956) and Lejdström and Svensson (1956) where a variety of test cases consisting of different track circuit setups and fault conditions were investigated and suggestions for mitigation provided. An example of railway signalling misoperations due to space weather occurred in Sweden (Wik et al., 2009) during a geomagnetic storm in July 1982, a signal changed from green to red and then reverted to green without the presence of a train in the track section or any other fault conditions. It was later estimated that a geoelectric field of 4-5 V/km was induced as a result of the storm, with the GICs driven through the railway signalling systems explaining the malfunction. Similar occurrences have also been observed in Russia where the statistical correlation between malfunctions and geomagnetic disturbances has been shown (Kasinskii et al., 2007; Ptitsyna et al., 2008; Eroshenko et al., 2010). GICs have also been observed and measured in the electrification systems of the Chinese high-speed railway, including within the track circuits (Liu et al., 2016).

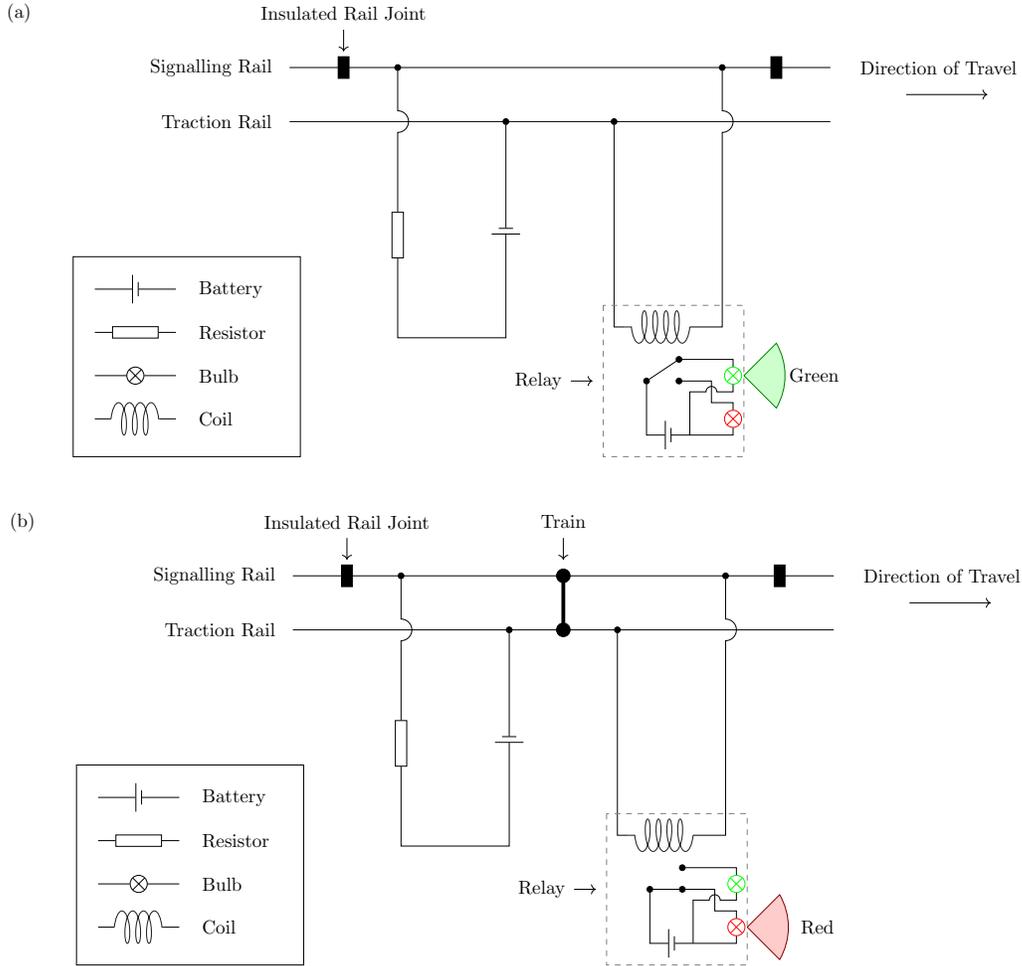
62 Severe space weather was added to the UK National Risk Register of Civil Emer-  
 63 gencies in 2012 (Cabinet Office, 2012). The UK Government’s Department for Trans-  
 64 port subsequently commissioned a report on rail resilience to space weather with the aim  
 65 of further understanding the threat that space weather posed to UK railway infrastruc-  
 66 ture (Darch et al., 2014). This report highlighted the knowledge gaps when it came to  
 67 track circuit interference, finding that “Signalling assets such as signalling and track cir-  
 68 cuits are potentially vulnerable to CMEs, and many assets are potentially vulnerable to  
 69 Single Event Effects” (p. 20). It also identified signalling systems as a potential area of  
 70 vulnerability, stating “The relative vulnerability of different types of systems (e.g. track-  
 71 based train detection) is not clear at this stage” (p. 20). In 2015, the “Space Weather  
 72 and Rail” workshop jointly organised by the European Commission’s Joint Research Cen-  
 73 tre, the Swedish Civil Contingencies Agency, the UK Department for Transport and the  
 74 US National Oceanic and Atmospheric Administration worked towards furthering un-  
 75 derstanding of space weather’s impacts on railways and raising awareness among oper-  
 76 ators (Krausmann et al., 2015).

77 In Section 2 of this paper, we provide an overview of track circuit railway signalling  
 78 systems and the mechanisms via which they can be impacted by space weather. This work  
 79 builds upon the theoretical modelling of geomagnetic induction in track circuits presented  
 80 in Boteler (2021), and in Section 3 we describe the model we have developed for this study.  
 81 We also provide details on the electrical characteristics of the rails and the track circuit  
 82 parameters that are included in our model, based on specifications from current United  
 83 Kingdom industry standards. In Section 4, we introduce the two sections of the UK rail-  
 84 way network being studied in this paper. In Section 4.1 we discuss factors that must be  
 85 considered depending on whether an entire railway line, or only a portion of the line, is  
 86 being modeled. We also examine which aspects of a railway line’s design contribute the  
 87 most to space weather susceptibility. Finally, in Section 4.2, uniform electric fields are  
 88 applied to both railway lines included in our investigation and the results discussed, first  
 89 for a range of realistic values based on geoelectric fields that have led to misoperations  
 90 in the recent past, then for a 1 in 100-year extreme event.

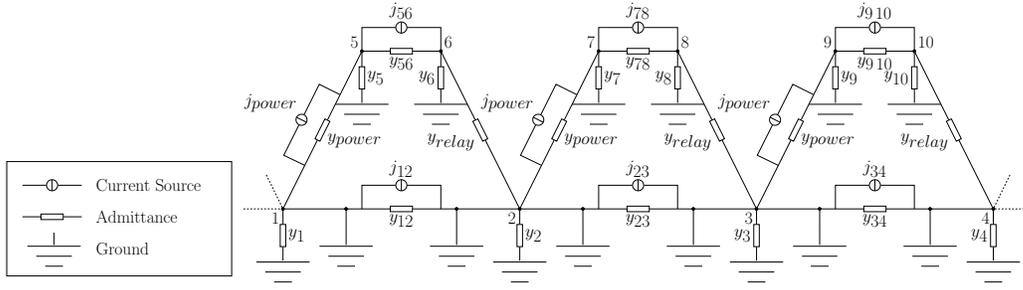
## 91 2 Track Circuits

92 Track circuits are one of the main signalling systems designed to detect trains along  
 93 a railway line. Figure 1 shows the operational principles of a track circuit on an AC-electrified  
 94 railway line. Insulated rail joints (IRJs) are spaced along one of the rails (the signalling  
 95 rail) which separates it into blocks; the other rail (the traction rail) is not broken into  
 96 sections as it provides the return path for the traction current used to power the train.  
 97 A voltage source is placed at the start of the block which drives a current through the  
 98 signalling rail and into a relay at the end of the block, and this current energises the re-  
 99 lay which causes a green signal to be displayed, indicating there is no train present, as  
 100 shown in (a). However, if a train is occupying the block, the wheels and axle redirect the  
 101 current before it can reach the end, and the relay is not energised leading to a red sig-  
 102 nal that indicates a train is present, as shown in (b). The lengths of track circuit blocks  
 103 and the traction rail can vary depending on if the section is located in a rural or an ur-  
 104 ban area. The two lines investigated in this study had a range of track circuit block lengths  
 105 from 0.4–1.9 km and traction rail lengths of around 34 km and 76 km; for comparison,  
 106 values for the Swedish railway studied by Alm (1956) and Lejdström and Svensson (1956)  
 107 were 1 km and 4 km for track circuit blocks and 100 km for the traction rail.

108 By design, the normal operation of a track circuit relay requires it to energise or  
 109 de-energise at specific current thresholds. This balance can be offset by geomagnetically  
 110 induced currents which can either work to de-energise a relay in a block with no train  
 111 present causing a ‘right side failure’ (a mode of failure that does not compromise the safety  
 112 of trains) or energise a relay in a block with a train present causing a ‘wrong side fail-  
 113 ure’ (one which does compromise the safety of trains).



**Figure 1.** Circuit diagram of a railway signalling track circuit for a single block along a network in the cases of (a) the absence of a train in the block and (b) a train occupying the block. Insulated rail joints separate each block from its neighbours, while the continuous rail is connected across all blocks. A power supply is connected to the side of the circuit from which the train enters (left in this case) and an accompanying resistor to protect it from short-circuiting; the relay is on the far end of the block (right in this case), formed of resistors and an electromagnet which in (a) is energised by the power supply, causing the switch to be in the configuration to display a green light, indicating the section is clear. When a train enters the block, as in (b), the wheels and axle short circuit the power supply causing the electromagnet to be de-energised, and the switch falls to the configuration that displays a red light, indicating the section is occupied.



**Figure 2.** Circuit diagram showing the nodal admittance network of three track circuits separated by insulated rail joints and connected by the traction rail. The components making up the network are the current source and admittance of the power supply ( $j_{power}$  and  $y_{power}$  respectively), the admittance of the relay ( $y_{relay}$ ), the admittance to the ground at each node (e.g.,  $y_1$ ,  $y_2$ ), the admittance due to the rail between nodes, (e.g.,  $y_{12}$ ,  $y_{23}$ ), and the currents induced in the rails due to the geoelectric field between nodes (e.g.,  $j_{12}$ ,  $j_{23}$ ).

### 114 3 Constructing the Network

#### 115 3.1 Geomagnetic Induction Modeling

116 The analysis in this paper builds upon modeling techniques for geomagnetic induction  
 117 in track circuits developed by Boteler (2021) and references therein. Each rail is con-  
 118 sidered to be a transmission line with series impedances and parallel admittances equi-  
 119 valent to the resistance of the rails and the leakages to the ground respectively. The trans-  
 120 mission line model for each rail is then converted to an equivalent-pi circuit constructed  
 121 with admittances and current sources (Boteler, 2013), and the circuits for both rails are  
 122 combined with the track circuit relay components to form a nodal admittance network,  
 123 as shown in Figure 2. By design, the traction rail is also periodically connected to the  
 124 earth to avoid hazardous voltage build-ups, and these grounding points are also included  
 125 at this stage.

126 The power supply current sources,  $I_{power}$ , are calculated using Equation 1, where  
 127  $V_{power}$  is the power supply voltage and  $r_{power}$  is the power supply resistance.

$$I_{power} = \frac{V_{power}}{r_{power}} \quad (1)$$

128 The current sources induced as a result of the electric field are calculated with Equa-  
 129 tion 2, where  $E_{\parallel}$  is the electric field component parallel to the rail and  $Z$  is the series  
 130 impedance of the rail.

$$I_E = \frac{E_{\parallel}}{Z} \quad (2)$$

131 The sum of current sources directed into each node is combined to form  $[J]$  (a ma-  
 132 trix of nodal current sources). Equation 3 shows the relationship between  $[J]$ , the volt-  
 133 ages at each node ( $[V]$ ), and the network admittances ( $[Y]$ ). In  $[Y]$  the diagonal terms  
 134 are equal to the sum of all admittances connected to that node, the off-diagonal terms  
 135 are given by the negative of the admittance between nodes, and  $[V]$  is the voltage at each  
 136 node.

$$[J] = [Y][V] \quad (3)$$

137 The nodal voltages can be obtained by inverting the matrix  $[Y]$  and multiplying  
 138 by the nodal current sources  $[J]$ , as shown in Equation 4. The difference between two  
 139 nodal voltages on either side of the relay gives the potential difference across the relay,  
 140 and thereafter the current flowing across the relay can be calculated.

$$[V] = [Y]^{-1}[J] \quad (4)$$

## 141 **3.2 Rail and Track Circuit Properties**

142 Obtaining realistic values for the electrical characteristics of an AC railway net-  
 143 work is crucial to analysing the impacts of GICs in DC signalling systems to the best  
 144 degree of accuracy. The sections of track considered in this paper are 2-track with single-  
 145 rail return and no earth wires, where 2-track means that there are two pairs of rails side-  
 146 by-side, one for each direction of travel.

### 147 **3.2.1 Rail resistance**

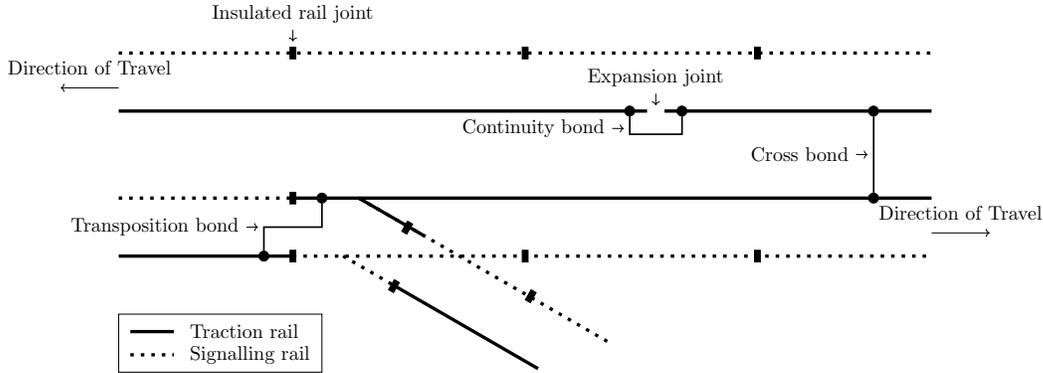
148 The railway lines being modelled use UIC 60 ( $60 \text{ kg m}^{-1}$ ) rail (NR/GN/ELP/27312,  
 149 2006), the dimensions are provided by *British Steel: Rail Product Range* (2020) from which  
 150 a cross-section area of  $7600 \text{ mm}^2$  was calculated. We have used a value of  $220 \text{ n}\Omega \text{ m}$   
 151 for the resistivity of British Steel Grade 700 steel giving a resistance per unit length of the  
 152 rail as  $0.0289 \Omega \text{ km}^{-1}$ . Mariscotti (2020) and sources therein provide the same value for  
 153 the per unit length resistance of UIC 60 rail.

### 154 **3.2.2 Earthing and bonding**

155 The traction rail itself is not entirely continuous since track geometry or safety de-  
 156 sign features will call for occasional gaps or side switching. In such cases, both sides of  
 157 each break in the rail are bonded together to ensure a continuous path for traction re-  
 158 turn current to flow. Figure 3 illustrates some of the cases where bonding is needed. These  
 159 include, but are not limited to, continuity bonds used to bridge expansion joints (designed  
 160 to account for the thermal expansion that rails experience with seasonal temperature changes),  
 161 cross bonds (used to connect all traction rails on a line together with a path to ground  
 162 to ensure low impedance is maintained throughout the line) and transposition bonds (used  
 163 when the traction rail switches sides). The latter requirement can arise in numerous cir-  
 164 cumstances, including at turnouts (junctions) where they are needed to avoid the short-  
 165 circuiting of adjacent track circuits. The traction rail is also bonded to all of the over-  
 166 head line equipment (OLE) structures, in particular the masts located approximately  
 167 every 60 m along the rail. The mast foundations connect the whole system to Earth, con-  
 168 tributing significantly to the leakage to ground from the traction rail (Keenor, 2021).

### 169 **3.2.3 Leakage admittance**

170 The leakage admittance of a rail is determined by the rail fastenings, sleepers (crossties)  
 171 and the ballast, and varies over a wide range due to environmental conditions and un-  
 172 derlying ground. NR/GN/ELP/27312 (2006) gives the conventional figure for leakage  
 173 admittance used by Network Rail to be  $0.125 \text{ S km}^{-1}$ , however, the configuration of the  
 174 rails means that the signalling and traction rails have different leakage admittance. The  
 175 signalling rails have insulating pads that reduce leakage, giving a leakage admittance of  
 176  $0.1 \text{ S km}^{-1}$ ; the traction rails are bonded to OLE structures, this results in a much larger  
 177 leakage admittance of  $1.6 \text{ S km}^{-1}$ . Another factor considered in this study is the addi-  
 178 tional leakage from earth mats bonded to the traction return circuit at traction feeder



**Figure 3.** A schematic diagram showing the usage of the various bonds required to ensure a continuous path for the current is provided in the traction rail. Along the top traction rail, a continuity bond is used to bridge the gap over an expansion joint designed to protect rails from the effects of thermal expansion during seasonal temperature changes; along the bottom traction rail, transposition bonds are used to temporarily switch the sides of the traction rail due to a turnout (junction) to avoid short-circuiting the track circuit in the branch; connecting both traction rails is a cross bond, designed to ensure voltages are evenly spread across all rails in a line to decrease the hazard of unsafe voltages building up along a rail.

179 stations, these structures increase the leakage by 10 S for each feeder station (NR/SP/SIG/50004,  
 180 2006). In the lines examined in this study, a feeder station is located between Preston  
 181 and Lancaster.

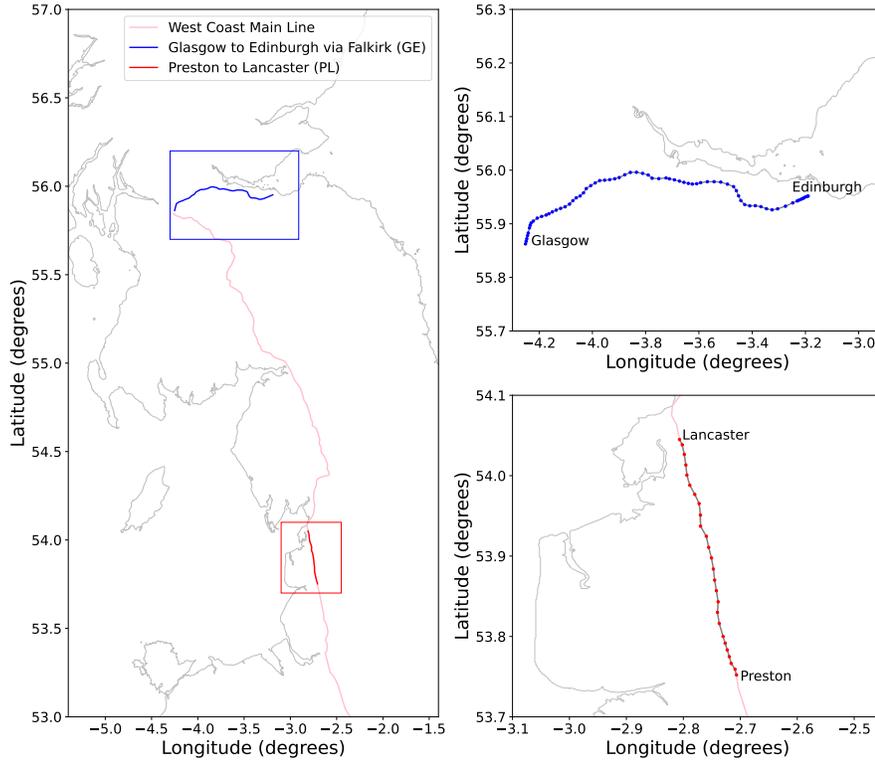
### 182 3.2.4 Track circuits

183 Track circuit parameters, including power supply and relay components, vary across  
 184 the world and even within a specific country, with many different types of equipment and  
 185 configurations being used. For the UK lines, we obtained the relevant data from the Net-  
 186 work Rail Standards Portal. In this study, we have used the combination of ‘BR867 AC  
 187 Immune DC Track Feed Unit’ (NR/BR/867, 1990) and the ‘BR939A Miniature Trac-  
 188 tive Armature AC Immune DC Neutral Track Relay’ (NR/BR/939A, 1971). This rep-  
 189 represents the preferred design according to the most recent Network Rail standards (NR/PS/SIG/11755,  
 190 2000). The side of the track circuit from where the train enters consists of a 10 V power  
 191 supply in series with a  $7.2\Omega$  resistor to limit the current when short-circuited by the lo-  
 192 comotive, the far end consists of the relay coil with a resistance of  $20\Omega$ . The pickup cur-  
 193 rent of the relay is 0.081 A with the dropout current being 68 per cent of that value at  
 194 0.055 A, this means when the current flowing through an energised relay drops below 0.055 A,  
 195 the relay will be de-energised and for it to be energised again, the current will need to  
 196 exceed 0.081 A.

## 197 4 Results

### 198 4.1 Railway Line Modeling

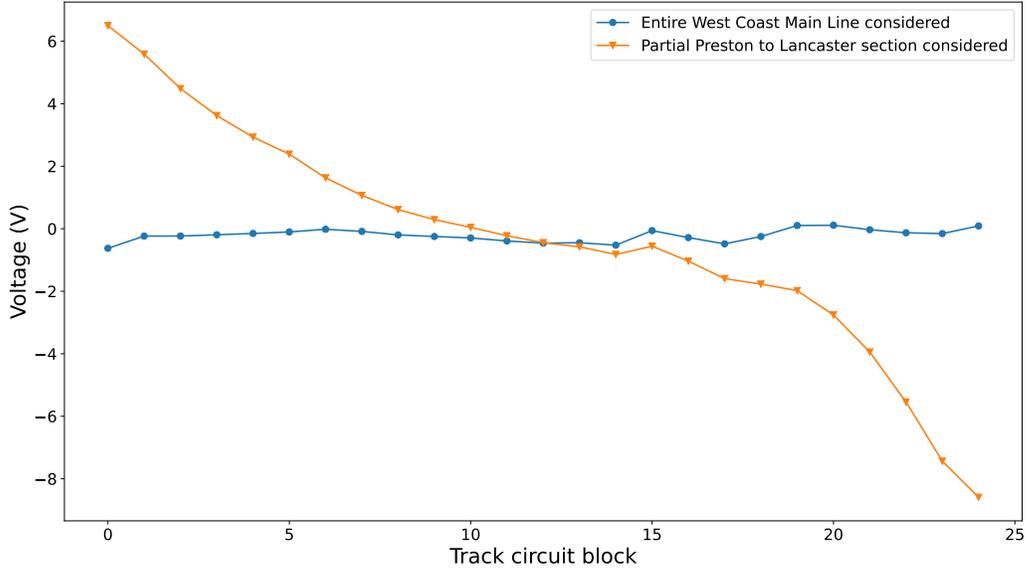
199 The geographical data for the railway lines studied, i.e., the longitudes and lati-  
 200 tudes of points along the line were obtained from OpenStreetMap. The lengths of track  
 201 circuit blocks and hence their start and end points were estimated using Network Rail  
 202 Sectional Appendices and the railway tracking website Traksy (<https://traksy.uk/live>).  
 203 Once the lines were separated into blocks, the orientation of each block in the line was



**Figure 4.** A geographic map of a northern portion of the United Kingdom showing both chosen railway lines for study in this paper with areas of interest highlighted and enhanced (top right and bottom right) to show the locations of signals. The top line (blue) is the Glasgow to Edinburgh via Falkirk line, stretching in an east-west orientation; the bottom line (red) is a portion of the West Coast Main Line from Preston to Lancaster, with the extension beyond those sections displayed opaquely, stretching in a north-south orientation.

204 calculated and used to determine the parallel electric field component along each line seg-  
 205 ment.

206 The sections of the railway network chosen for this study are introduced in Fig-  
 207 ure 4: the 76 km Glasgow to Edinburgh via Falkirk line and a 34 km portion of the West  
 208 Coast Main Line from Preston to Lancaster. Both lines are electrified with 50 Hz AC at  
 209 25 kV. The two sections were selected for their different orientation (east-west for Glas-  
 210 gow to Edinburgh and north-south for Preston to Lancaster) and different geological ter-  
 211 rane. For the following analyses, we will consider only the track in one direction of travel,  
 212 eastwards for Glasgow to Edinburgh and northwards for Preston to Lancaster. Each track  
 213 circuit is assumed to consist of one power supply at the start of the block (relative to  
 214 the direction of travel) and one relay at the end of the block.



**Figure 5.** The voltage profiles along the traction rail between Preston and Lancaster with different termination conditions. The orange line with triangles shows the voltage profile where the traction rail ends have been set at Preston and Lancaster; the blue line with dots shows the profile where the traction rail has been extended with  $310 \times 1$  km blocks south of Preston and  $230 \times 1$  km blocks north of Lancaster with orientations representative of the general line geometry to account for the portions of the West Coast Main Line beyond the area of study.

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#### 4.1.1 Modeling a Section of a Line

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When modeling track circuits within a section of traction rail that extends beyond the area of study such as the Preston to Lancaster segment of the West Coast Main Line (WCML), the entire length of the rail must be represented in the model to provide a valid voltage profile along the traction rail section and accurate current values across the relays. To more accurately model the geomagnetic interference on the Preston to Lancaster section,  $310 \times 1$  km blocks before the section and  $230 \times 1$  km blocks after the section have been included in the model, with orientation representative of the general line geometry of the WCML. The Preston to Lancaster section of the line still uses the original estimated block lengths, which range from 0.6–1.8 km. Figure 5 compares the voltage profiles along the section of traction rail between Preston and Lancaster when (1) the ends of the traction rail are set at Preston and Lancaster and (2) the ends of the traction rail are extended to encompass the entire WCML using the method detailed above. It can be seen that the voltage profile is significantly different if the entire length of the traction rail is not considered. If detailed information about the adjacent rail sections is not available, but the adjacent rails are uniform and nearly straight, they can be represented by an equivalent ‘active termination’ (Boteler, 1997) where the external portion of the rail is a single voltage source and series resistance connected to ground. Calculations with active terminations to represent the northern and southern sections of the WCML give almost identical results to those from calculations including the additional representative sections beyond the area of study.

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### 4.1.2 Modeling the Entire Line

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The methodology described above is suitable for analysing portions of lines that do not include either or both ends of the traction rail. But additional considerations have to be made when modeling the entire traction rail due to the effects of the ends of the line. To demonstrate this, a simplified track circuit model has been produced, consisting of  $70 \times 1$  km blocks all orientated directly eastwards. The track circuit voltage has been set to zero, allowing us to examine the effects of only the induced currents. Figure 6 shows the voltage profiles and nodal voltages along the traction rail and each of the signalling rails when eastward electric fields of  $-2 \text{ V km}^{-1}$  and  $-4 \text{ V km}^{-1}$  were applied. The short thin lines illustrate how rail voltage is neither constant from node-to-node nor continuous across nodes. The potential differences across the relays in each track circuit block are shown in a separate panel. The voltage profiles along the traction rail and signalling rails agree with the characteristic electrically long and electrically short profiles as shown in Boteler (2021), respectively. It can be seen that with a constant uniform electric field applied, the nodal voltages of the traction rail and signalling rails, although having different minima and maxima, decrease along the line, following a sideways S-shaped curve. At the beginning of the line, the voltages start at their maximum point, decreasing to a central plateau. At a point near the termination of the line, the nodal voltages of both rails converge, causing the potential difference across the relay to be zero. Closer to the termination of the line the polarity of the potential difference is reversed. It can also be seen that the location of the crossover point where the potential difference reverses remains constant regardless of the electric field strength applied. In Figure 7, the crossover point can be seen at track circuit block 64, and beyond that point the polarity of the currents is reversed.

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Considering this from a mathematical point of view: from Equation 4 we know that the nodal voltages are the result of matrix multiplication between the inverse of the admittance matrix ( $[Y]^{-1}$ ) and the current sources ( $[J]$ ). When we increase or decrease the electric field strength ( $E$ ), we are only changing the values of  $[J]$ , as  $[Y]$  is determined by the electrical characteristics of the rails and the track circuit components.  $[J]$  is proportional to  $E$  and inversely proportional to the rail impedance. However, as the impedances of the signalling rails and traction rail are equal, changing  $E$  scales the currents induced in all rails by the same factor. As  $[Y]^{-1}$  is constant and  $[J]$  has been scaled by a certain factor, the result of the matrix multiplication is that  $[V]$  would be scaled by the same factor. The current across the relays is determined by the relay resistance, which is constant, and the potential difference across the rail, which is the difference between two voltage nodes within  $[V]$ . This means that the potential difference is again scaled by that same factor. Consequently, when the potential difference is zero, scaling it by any factor would still result in zero, leading to a common crossover point that is independent of the electric field strength.

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### 4.1.3 Susceptibility to Geomagnetic Interference

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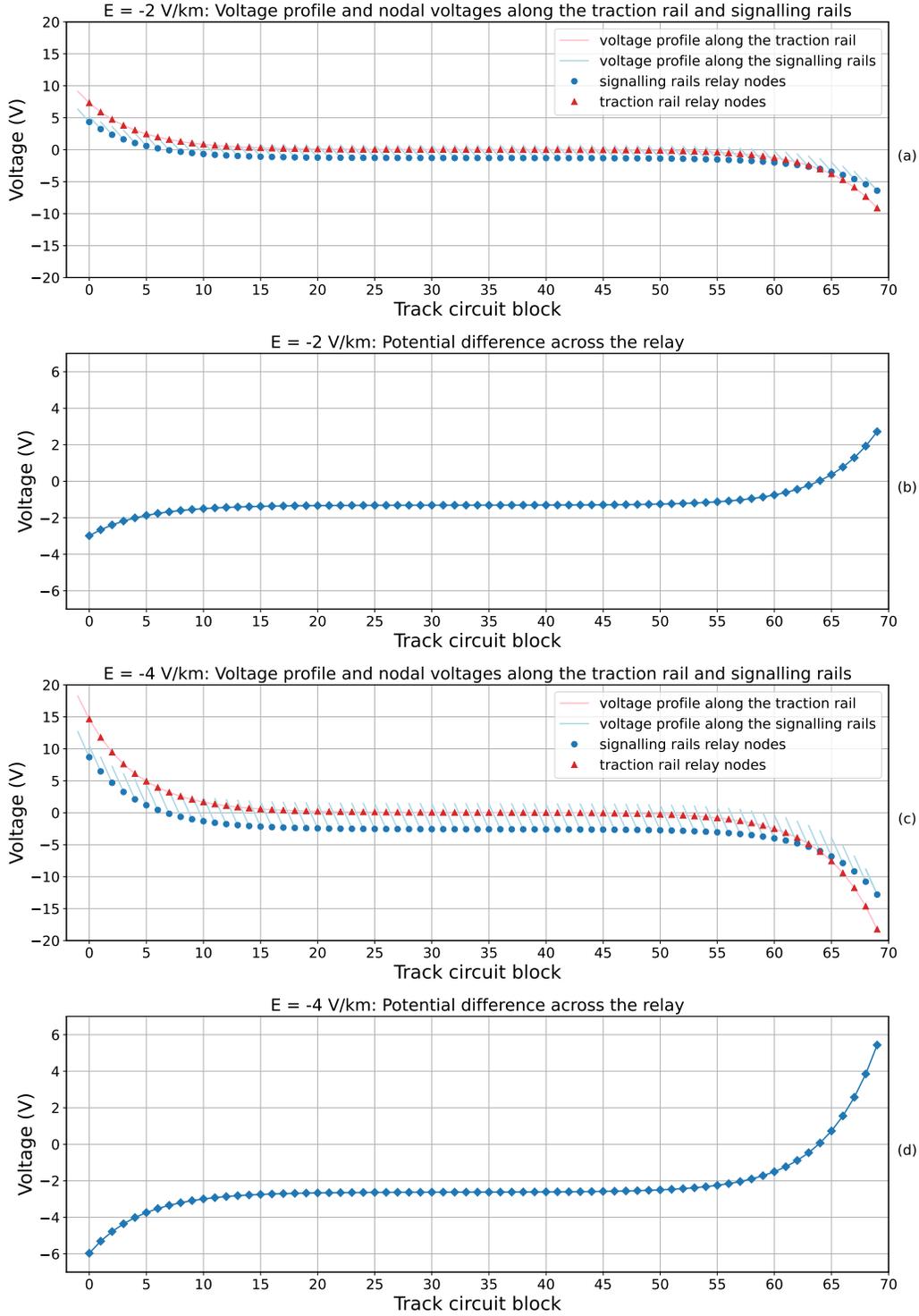
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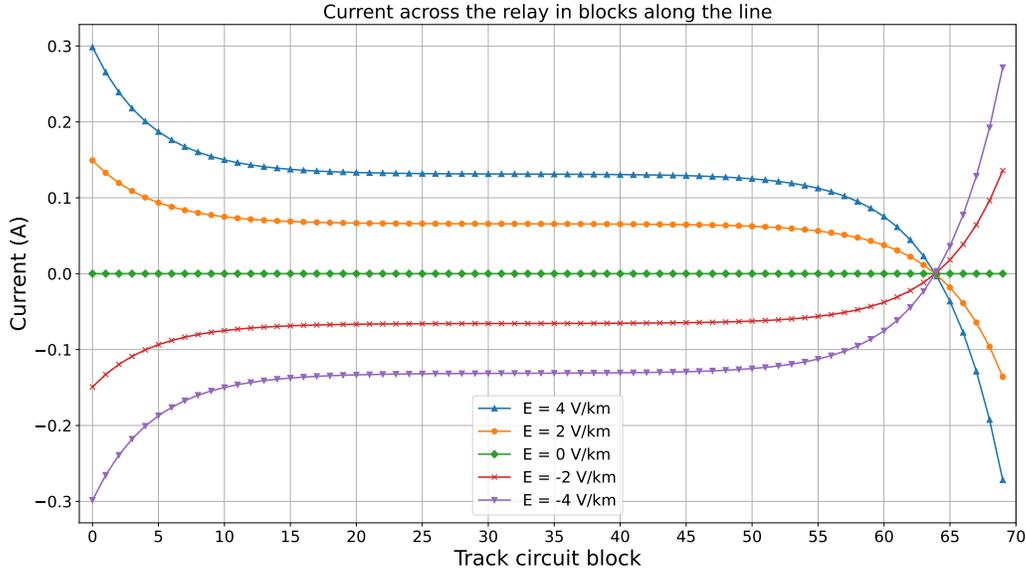
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In this section, we investigate the factors which contribute to the susceptibility of a track circuit relay to induced currents. For the Glasgow to Edinburgh line, the model was run for eastwards electric field values of 0 to  $-4 \text{ V km}^{-1}$  in increments of 0.1, recording the current across the relay in each block for every E-field value. The blocks were then sorted by length and the range of currents across each relay was plotted to determine if there was a dependence on block length. To examine the effects of the angle between a block's rails and the geoelectric field, a second set of modelled data was taken with the E-field in each block orientated along the rail. The results of this modeling are shown in Figure 8. Due to the effects of the ends of the traction rail on the voltage profiles, we split the blocks near the ends from those in the centre. When compared with blocks of similar length in the centre of the line, the range of current values across relays towards the ends of the line is larger near the start and smaller and oppositely di-



**Figure 6.** Parameters in a network of  $70 \times 1 \text{ km}$  blocks facing directly eastwards, where the track circuit voltage is set to zero. For electric field strengths of  $-2 \text{ V km}^{-1}$ : panel (a) shows the voltage profiles and nodal voltages along the traction rail (red triangles) and signalling rails (blue dots) and panel (b) shows the potential difference across the relays along the line (blue diamonds). The point at which the signalling rail voltage and traction rail voltage are equal and hence the point at which the potential difference is zero occurs at the same location regardless of electric field strength. Panels (c) and (d) are the equivalent of (a) and (b) but for  $-4 \text{ V km}^{-1}$ .



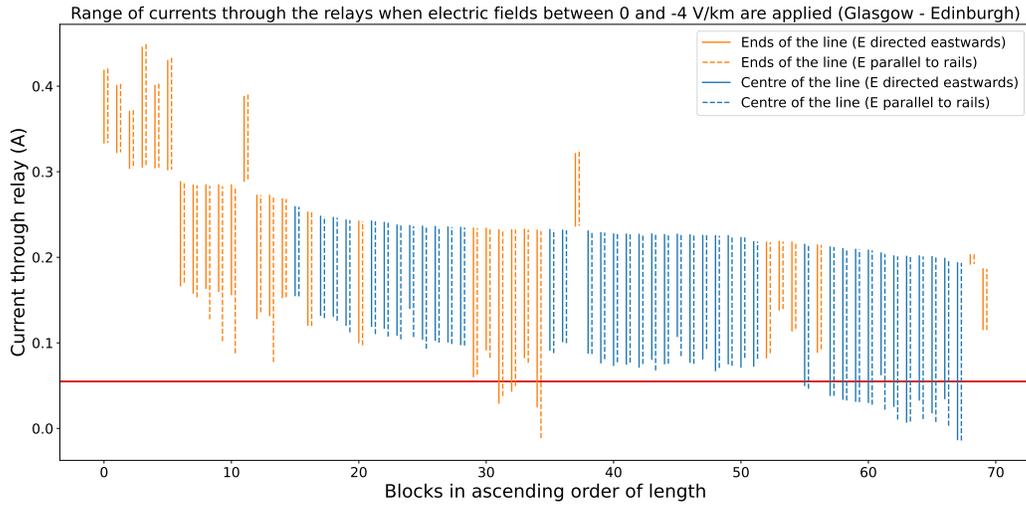
**Figure 7.** Parameters in a network of  $70 \times 1$  km blocks facing directly eastwards, where the track circuit voltage is set to zero: the current across the relays along the line for electric field strengths ranging from  $4 \text{ V km}^{-1}$  to  $-4 \text{ V km}^{-1}$ . Independent of electric field strength, the currents cross zero at a common point.

288 rected near the termination. The angle between the E-field and the rails has a definite  
 289 impact, the currents induced in the section will be largest when the E-field is parallel  
 290 to the rail and zero when the E-field is perpendicular to the rail. Most of the rails in blocks  
 291 between Glasgow and Edinburgh are closely aligned with the direction of the E-field so  
 292 the currents through most of the relays experience only minor variation, the exceptions  
 293 we see are mainly due to the northwards orientation of the track leaving Glasgow be-  
 294 fore turning east towards Edinburgh. If we consider only blocks at the centre of the line,  
 295 the length of the blocks is a first-order indicator of the current through the relay. Con-  
 296 sidering the case when the E-field is aligned with the rails (shown by blue dashed lines  
 297 in Figure 8), relay misoperations occur where the blocks are the longest. Other subtle  
 298 effects can also be noted, i.e., the length of surrounding blocks, which affects the cur-  
 299 rent across the relay of a block in between. This analysis was repeated for Preston to  
 300 Lancaster with a northwards electric field without the need to filter blocks near the ends  
 301 due to it being a central segment of the West Coast Main Line. The results, as shown  
 302 in Figure 9, agree with those for Glasgow to Edinburgh, i.e., the longer blocks are more  
 303 susceptible to geomagnetic interference than shorter ones.

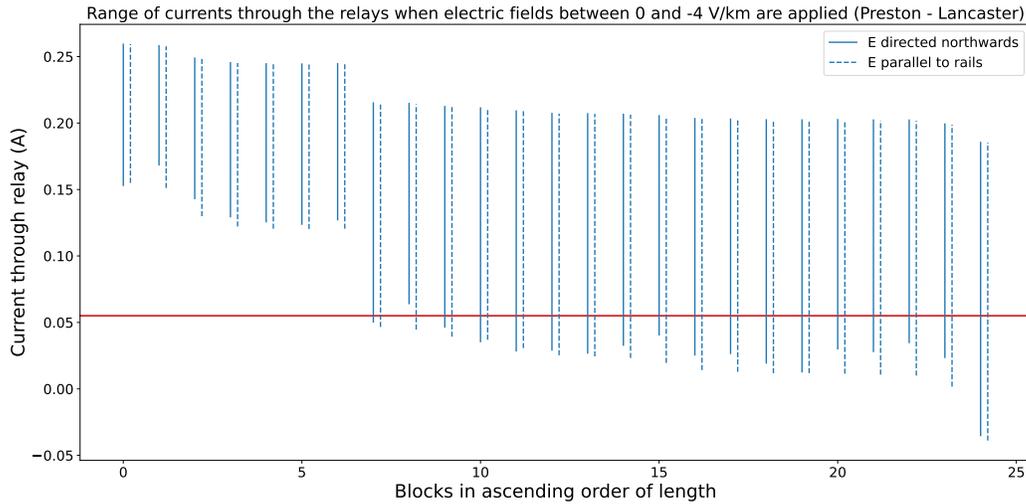
## 304 4.2 Applying Electric Fields

### 305 4.2.1 Uniform Electric Fields

306 For the following analysis, a range of uniform electric field values between  $\pm 4 \text{ V km}^{-1}$   
 307 have been applied. They are based on the lower limit of geoelectric field values observed  
 308 in Sweden during the storm of July 1982, where interference on railway signalling was  
 309 observed (Wik et al., 2009). Each block is assumed to be absent of any trains meaning  
 310 all signals should be displaying a green light, with the current flowing through the relay at  
 311 a value above the relay dropout threshold.



**Figure 8.** The range of currents across each relay in blocks along the line between Glasgow and Edinburgh for electric fields between 0 and  $-4 \text{ V km}^{-1}$ . Solid lines show the results for when there is an angular separation between the rails and the electric field, and the dashed lines show the results for when the electric field is parallel to the rails in each block. Blocks at the centre of the rail are shown as blue lines and blocks at the ends as orange lines. The horizontal red line indicates the threshold below which the track circuit would de-energise.



**Figure 9.** The range of currents across each relay in blocks along the line between Preston and Lancaster for electric fields between 0 and  $-4 \text{ V km}^{-1}$ . Solid lines show the results for when there is an angular separation between the rails and the electric field, and dashed lines show the results for when the electric field is parallel to the rails in each block. The horizontal red line indicates the threshold below which the track circuit would de-energise.

Figure 10 shows the current through the relay of each track circuit block along the two sections assuming no external electric field is applied, the line below each main panel is a schematic representation of all the signals along the section where a green outline with no fill indicates normal operation and black outline with red fill indicates a false signal. It can be seen that all relays are operating normally, with the differences in current arising from network design factors such as the length of blocks and the inclusion of traction feeder stations.

Assuming the field is uniform across the entire area of the section, electric fields ranging from 4 to  $-4 \text{ V km}^{-1}$  increasing in intervals of  $0.1 \text{ V km}^{-1}$  were applied. For the “east-west” orientated Glasgow to Edinburgh line, the electric field was aligned to geographic east ( $E_y$ ). For the “north-south” orientated Preston to Lancaster section, a geographic north direction ( $E_x$ ) was chosen.

For Glasgow to Edinburgh, the threshold westward electric field value at which signal misoperations begin to occur is  $E_y = -2.8 \text{ V km}^{-1}$ . At the most negative electric field ( $E_y = -4 \text{ V km}^{-1}$ ) of the range we have applied, the currents induced in the track circuits are sufficiently strong to cause 14 of the relays to de-energise, displaying false signals as seen in Figure 11. With Glasgow to Edinburgh, as we are modeling the entire line, it is also important to look at the case of positive (eastward) electric fields due to the reversed potential difference beyond the crossover point. At  $E_y = 4 \text{ V km}^{-1}$ , the de-energisation of the blocks beyond the crossover can be seen in Figure 12 when compared with the profiles of the negative electric fields. However, no signal misoperations occur due to the short length of the blocks towards the termination of the line.

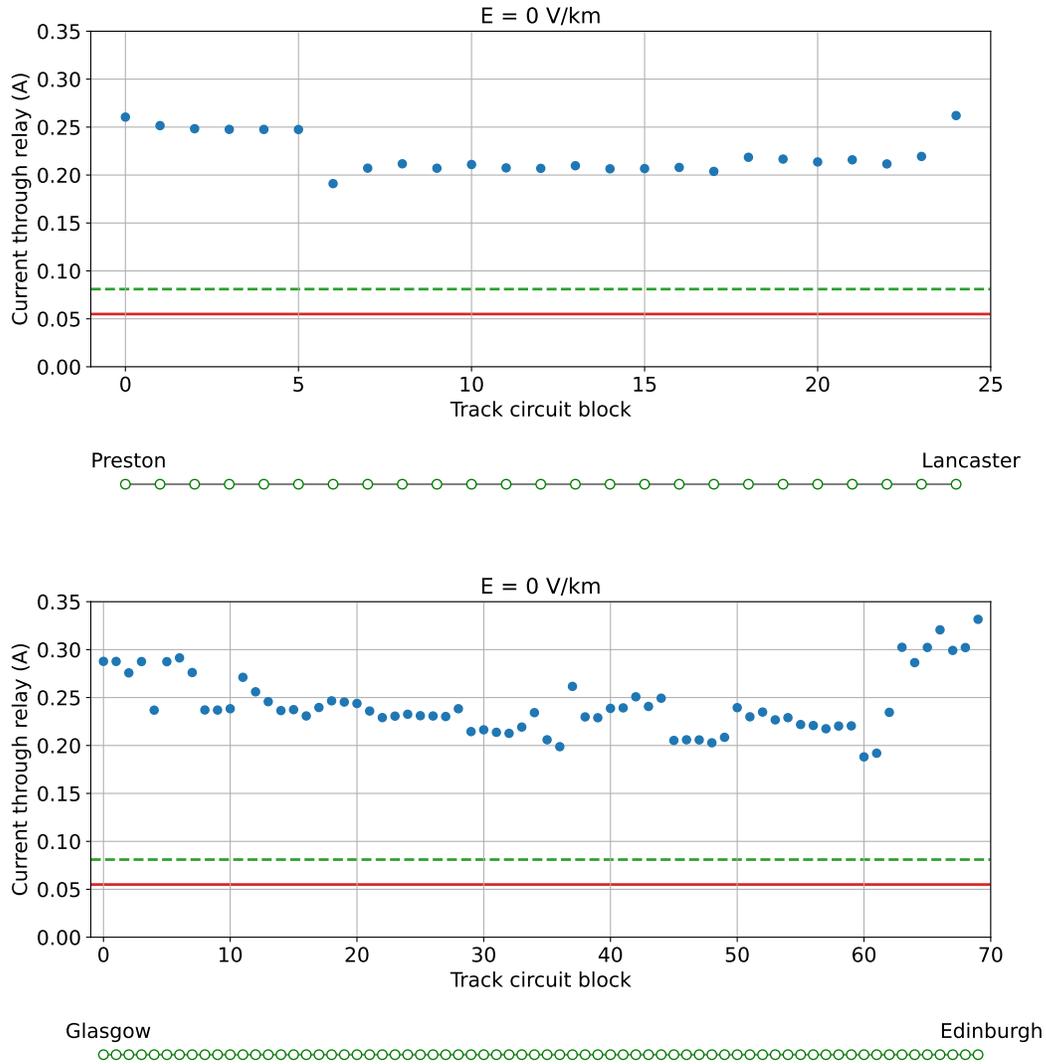
For Preston to Lancaster, the threshold southward electric field value at which signal misoperations begin to occur is  $E_x = -2.5 \text{ V km}^{-1}$ . At  $E_x = -4 \text{ V km}^{-1}$ , the currents induced in the track circuits cause 17 of the relays to be de-energised, as seen in Figure 13. As Preston to Lancaster is a central segment of the WCML, positive (northward) electric field values are not considered.

#### 4.2.2 1 in 100 Year Extreme

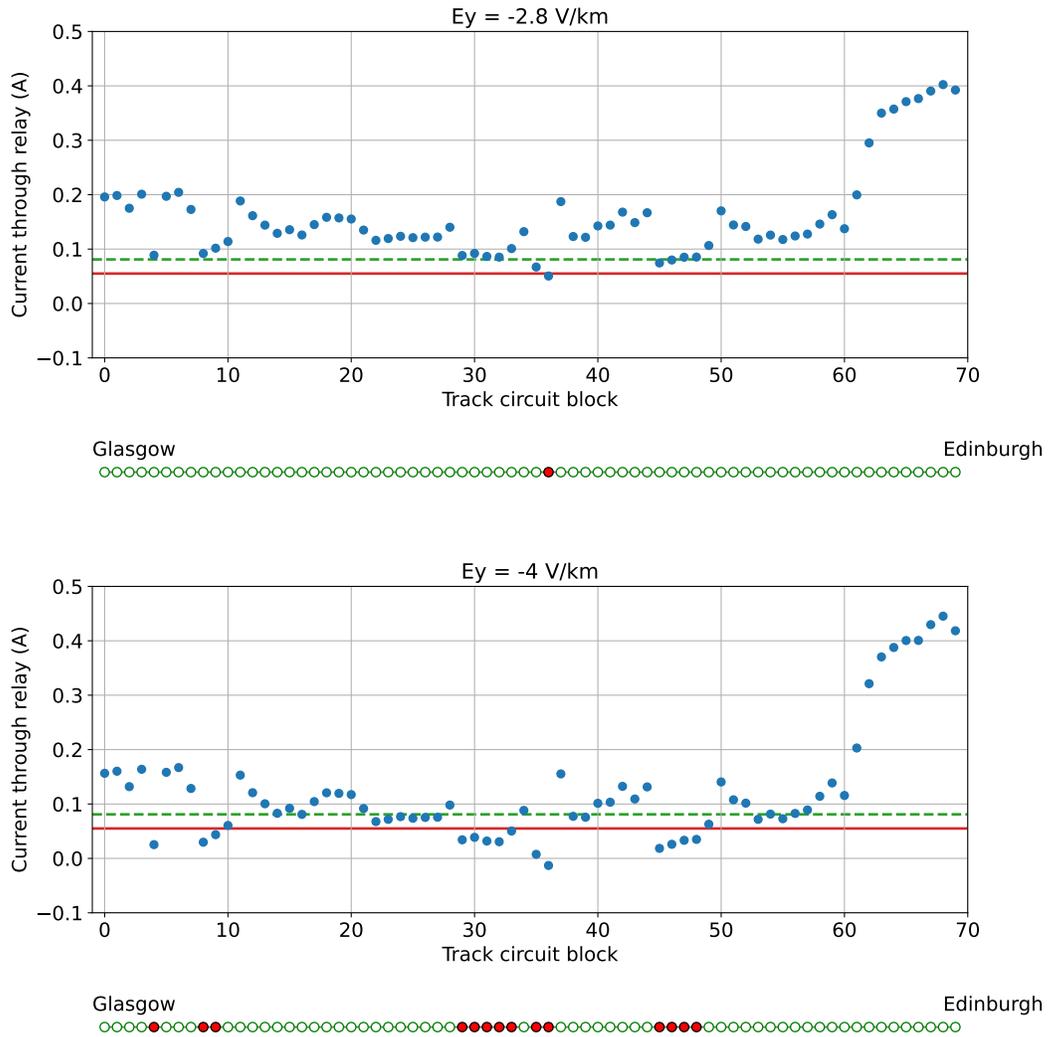
An estimate for a 1 in 100-year extreme geoelectric field for the UK is estimated by Beggan et al. (2013) to be approximately  $5 \text{ V km}^{-1}$ . As we are considering an extreme case, we set the value to be negative (opposite to the direction of travel) for both lines being modelled. The currents across the relays for sections A and B are shown in Figures 14 and 15 respectively, with nearly all of the relays being de-energised between Preston to Lancaster and almost half of all relays being de-energised between Glasgow and Edinburgh. This suggests that a 1 in 100-year extreme geoelectric field value applied to the two railway sections would result in significant signal misoperations.

## 5 Discussion

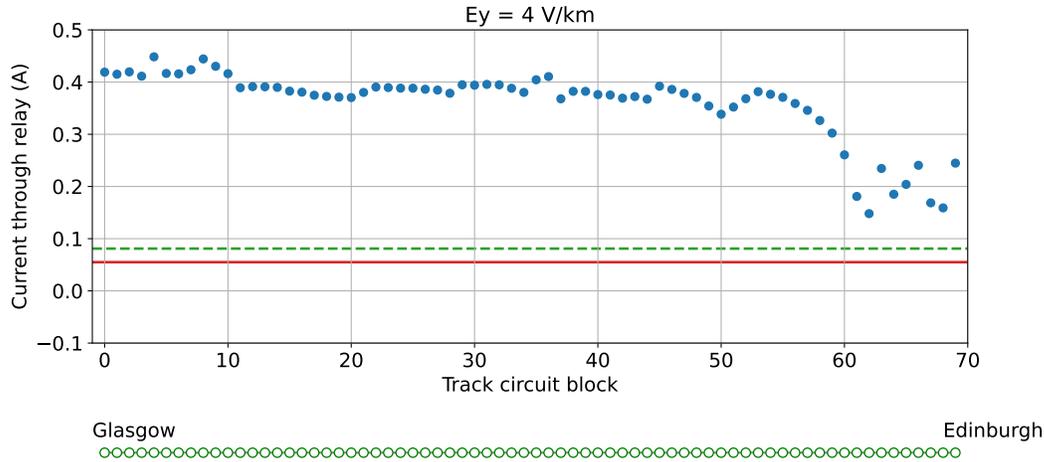
This study expands upon the theoretical work of Alm (1956), Lejdström and Svensson (1956) and Boteler (2021) by modeling realistic railway lines with parameters from current industrial standards. The electrical characteristics and parameters for the rails and track circuit components are specific to the UK 25 kV, 50 Hz AC railway lines, e.g., the West Coast Main Line and the Glasgow to Edinburgh via Falkirk line. These values can be replaced as necessary which allow the modeling to be used for any combination of rails, blocks and relay types, provided the data for those components are available. The main reason we chose a section of the West Coast Main Line was because it is one of the UK’s most important railway lines. It provides rail links to major cities, including an arterial connection between England and Scotland. With a pre-pandemic estimate of 35 million passengers annually (Department for Transport, 2015), the West Coast Main Line provides crucial services including local and regional travel as well as



**Figure 10.** In the absence of a train: the current through each of the track circuit relays between Preston and Lancaster (top panel) and Glasgow to Edinburgh (bottom panel) with no geoelectric field applied. The blue dots indicate the current of each relay, the red (solid) line shows the threshold below which the track circuit would de-energise and display an incorrect signal, and the green (dashed) line shows the threshold the current would need to rise above to re-energise if de-energised. Below each plot is a schematic view of each signal and whether it is operating correctly. An unfilled green dot means normal operation, so in this case, all signals on both lines show no misoperations.



**Figure 11.** In the absence of a train, for each of the geoelectric fields applied: the current through each of the 75 track circuit relays between Glasgow and Edinburgh. The blue dots indicate the current of each relay, the red (solid) line shows the threshold below which the track circuit would de-energise and display an incorrect signal, and the green (dashed) line shows the threshold the current would need to rise above to re-energise if de-energised. Below each plot is a schematic view of each signal and whether it is operating correctly, an unfilled green dot means normal operation and a filled red dot indicates a misoperation. In this case, there are signal misoperations at  $E_y = -2.8 \text{ V km}^{-1}$  (1 misoperation) and  $E_y = -4 \text{ V km}^{-1}$  (14 misoperations).



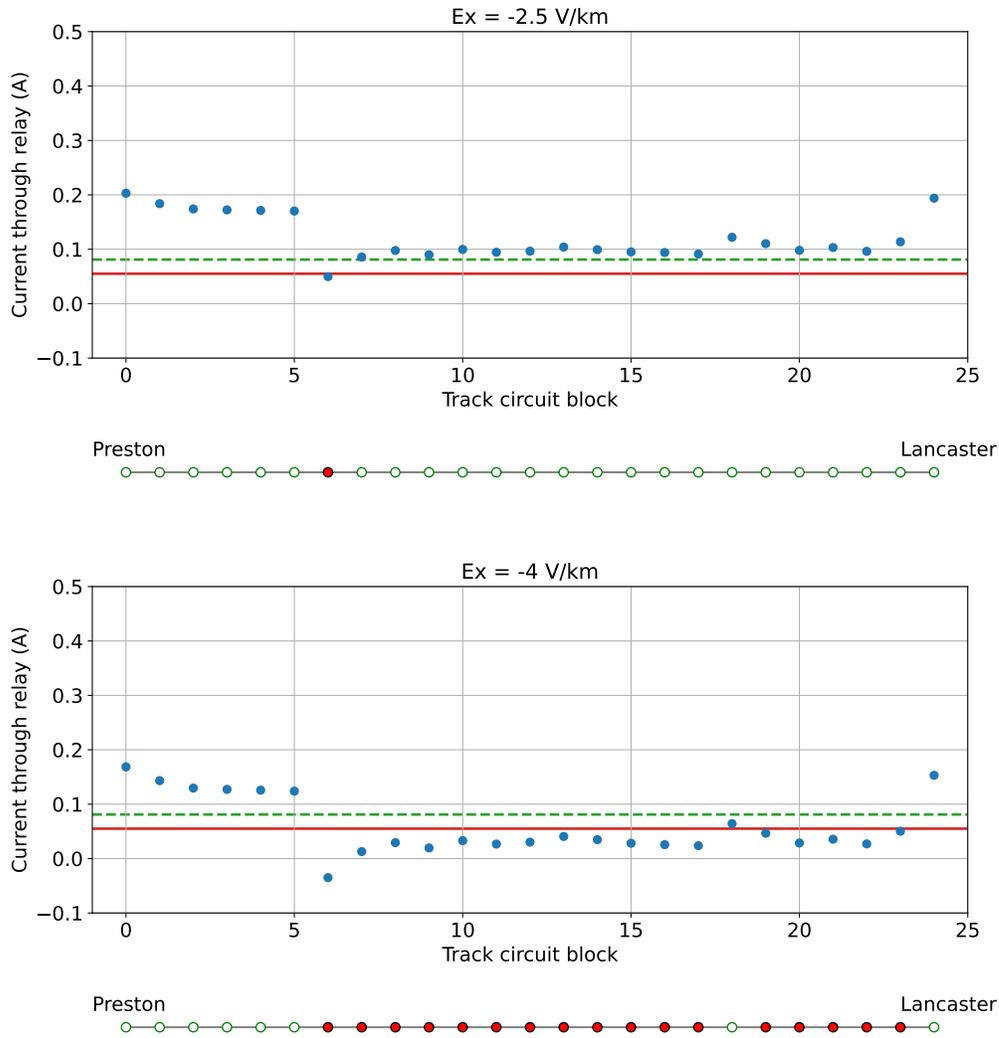
**Figure 12.** In the absence of a train, for each of the geoelectric fields applied: the current through each of the 75 track circuit relays between Glasgow and Edinburgh. The blue dots indicate the current of each relay, the red (solid) line shows the threshold below which the track circuit would de-energise and display an incorrect signal, and the green (dashed) line shows the threshold the current would need to rise above to re-energise if de-energised. Below each plot is a schematic view of each signal and whether it is operating correctly, an unfilled green dot means normal operation and a filled red dot indicates a misoperation. In this case, there are no signal misoperations at  $E_y = 4 \text{ V km}^{-1}$ .

361 freight. The Glasgow to Edinburgh via Falkirk line was chosen for its east-west orien-  
 362 tation and due to it being a connection between two major cities.

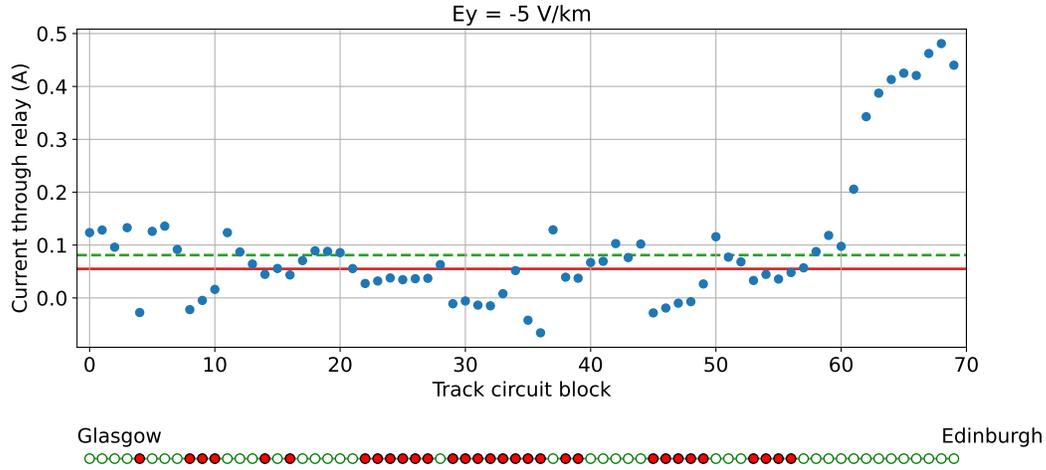
363 The model showed that the potential difference across track circuit relays near to  
 364 the ends of the line can vary greatly from those in the centre even if they have identi-  
 365 cal properties and parameters. This means that the susceptibility of a track circuit block  
 366 to induced currents cannot simply be determined from its length and orientation (i.e.,  
 367 alignment to the direction of the electric field). However, we have also shown that those  
 368 assumptions are valid when studying sections of a longer line that are not near the ends  
 369 of the traction rail.

370 The range of electric field values used in this analysis ( $\pm 4 \text{ V km}^{-1}$ ) is based on the  
 371 electric field magnitude that caused signalling systems to misoperate in Sweden during  
 372 a geomagnetic storm in July 1982 (Wik et al., 2009), where a value of  $4\text{-}5 \text{ V km}^{-1}$  was  
 373 estimated. It was demonstrated that the two UK lines studied would have experienced  
 374 signal misoperations if subjected to a geoelectric field of this magnitude. Comparing the  
 375 electric field values at which signal misoperations begin to occur with estimates of elec-  
 376 tric fields across the UK for different timescales by Beggan et al. (2013), the value is equiv-  
 377 alent to an event that could occur once every 30 years. Electric fields in the UK estimated  
 378 for a 1 in 100-year extreme geomagnetic field by Beggan et al. (2013) were demonstrated  
 379 to cause significant disruptions to the two lines studied, with a large number of signal  
 380 misoperations occurring.

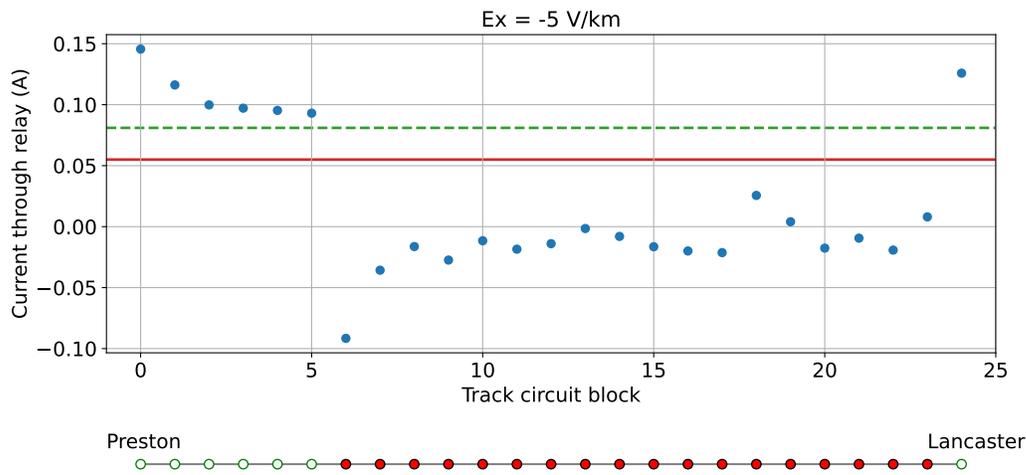
381 While the electrical characteristics of the rails used in this study are the conven-  
 382 tional values given in Network Rail standards, there can be variation in these param-  
 383 eters. For example, the leakage from the rails to the ground is affected by the weather,  
 384 increasing in wetter conditions and decreasing in drier conditions. The model was re-  
 385 run using the range of leakage from the rails to the ground from Network Rail standard



**Figure 13.** In the absence of a train, for each of the geoelectric fields applied: the current through each of the 25 track circuit relays between Preston and Lancaster with various geoelectric field strengths applied. The blue dots indicate the current of each relay, the red (solid) line shows the threshold below which the track circuit would de-energise and display an incorrect signal, and the green (dashed) line shows the threshold the current would need to rise above to re-energise if de-energised. Below each plot is a schematic view of each signal and whether it is operating correctly, an unfilled green dot means normal operation and a filled red dot indicates a misoperation. In this case, there are signal misoperations at  $E_x = -2.5 \text{ V km}^{-1}$  (1 misoperation) and  $E_x = -4 \text{ V km}^{-1}$  (17 misoperations).



**Figure 14.** In the absence of a train, for each of the geoelectric fields applied: the current through each of the 75 track circuit relays between Glasgow and Edinburgh. The blue dots indicate the current of each relay, the red (solid) line shows the threshold below which the track circuit would de-energise and display an incorrect signal, and the green (dashed) line shows the threshold the current would need to rise above to re-energise if de-energised. Below each plot is a schematic view of each signal and whether it is operating correctly, an unfilled green dot means normal operation and a filled red dot indicates a misoperation. In this case, almost half of the signals are showing misoperations.



**Figure 15.** In the absence of a train, for each of the geoelectric fields applied: the current through each of the 25 track circuit relays between Preston and Lancaster with various geoelectric field strengths applied. The blue dots indicate the current of each relay, the red (solid) line shows the threshold below which the track circuit would de-energise and display an incorrect signal, and the green (dashed) line shows the threshold the current would need to rise above to re-energise if de-energised. Below each plot is a schematic view of each signal and whether it is operating correctly, an unfilled green dot means normal operation and a filled red dot indicates a misoperation. In this case, almost all of the signals are showing misoperations.

NR/GN/ELP/27312 (2006), and the results are as follows. It was found that when the leakage to the ground was maximised ( $0.4 \text{ S km}^{-1}$  for the signalling rail and  $2 \text{ S km}^{-1}$  for the traction rail), the threshold electric field values at which signal misoperations begin to occur was lowered for both Glasgow to Edinburgh and Preston to Lancaster to  $-0.9 \text{ V km}^{-1}$  and  $-0.7 \text{ V km}^{-1}$  respectively. When the leakage to the ground was minimised ( $0.025 \text{ S km}^{-1}$  for the signalling rail and  $1.53 \text{ S km}^{-1}$  for the traction rail), the threshold electric field values at which signal misoperations begin to occur was raised for both Glasgow to Edinburgh and Preston to Lancaster to  $-4.3 \text{ V km}^{-1}$  and  $-4 \text{ V km}^{-1}$  respectively. This means we are more likely to see signal misoperations on days that are wetter than average and vice versa. We also tested the impact of altering the rail resistance, but it was found that varying either or both of the rail's resistance values did not result in a significant change to the results.

It was shown that signal misoperations only occurred when the applied electric field was negative (i.e. opposite to the general direction of travel). This was due to the field being orientated such that the induced currents mostly contributed towards de-energising the relays, flowing across the relay in a direction opposite to the current provided by the track circuit power supply. When the applied electric field was positive, the relays became more energised. This was the general case for most of the track circuit blocks, but if the model includes the entirety of the traction rail, the currents across the relays in blocks near a characteristic crossover point become less sensitive to the changes in the electric field. In blocks beyond the crossover point, the direction of current across the relays will be reversed, becoming increasingly energised with a more negative electric field. In the case of the Glasgow to Edinburgh line, the blocks beyond the crossover point do not de-energise sufficiently to cause a misoperation even when the electric field is at the maximum positive value of the range used in this study, this is mainly due to the length of those blocks, which happen to be the shortest ones on the line as they are approaching the terminal station in a large city. It is worth noting that this paper only considers one direction of each line studied, depending on the orientation and layout of the track circuits, positive electric fields could cause signal misoperations in other cases, e.g., for the opposite direction of travel.

In this study, we have focused on geoelectric fields of constant direction and magnitude, when in reality they typically vary in intensity and direction over time. We note that the impact of time-varying fields will need to be considered in future work. For example, the duration over which geoelectric fields must maintain a given strength and/or orientation to cause a misoperation remains unclear. In such cases, the characteristic response times of various types of track circuits to current changes will also need to be examined. Furthermore, given the diverging/converging current flows shown in Figure 7, the possibility of charge build-up (that may work to oppose the geoelectric field) should be explored.

The impact of space weather on railway signalling is but one aspect of a multifaceted system that is intrinsically connected. Alongside signalling systems, the operation of a railway network also relies upon many interdependent systems such as power transmission, communication and Global Navigation Satellite Systems (GNSS), all of which are susceptible to the effects of space weather (Hapgood et al., 2021). The UK report on rail resilience to space weather Darch et al. (2014) states: "Accidents are rarely caused by a single failure; compound effects from multiple impacts are likely to create a problem" (p.5). Considering the delays that the railway network could be subjected to in the case of extensive signalling misoperations, passengers could potentially be trapped on a stationary train for extended periods. This is especially likely if other interdependent systems are also affected. The onboard air-conditioning and toilet systems are unable to continue operating for long periods without external power sources, subjecting passengers to uncomfortable and potentially harmful conditions. In this eventuality, if passengers were to take it upon themselves to leave the train unaided, then they would be sub-

439 jected to severe risk due to currents flowing in the rails, trains on adjacent lines and a  
 440 plethora of other hazards from walking unattended along a potentially remote section  
 441 of track.

442 The simplification of not including trains in the model was necessary at this initial  
 443 stage of model development. This also aided in getting an overview of the fundamental  
 444 principles of how induced currents affect the rails and infrastructure without other  
 445 sources of interference. While this setup was ideal for analysing the ‘right side failures’  
 446 that occur when trains are absent from track circuit blocks, a study into the more hazardous  
 447 case of ‘wrong side failures’ will be greatly beneficial to furthering our understanding  
 448 of geomagnetic interference in railway signalling systems. We consider that to be a  
 449 natural next step for this research.

## 450 6 Conclusion

451 This study presents the most realistic model of geomagnetic interference in DC signalling  
 452 systems on AC-electrified railway lines to date. Built upon the techniques detailed  
 453 in Boteler (2021) we have modelled two sections of the UK railway network, the north-  
 454 south orientated Preston to Lancaster section of the West Coast Main Line and the east-  
 455 west orientated Glasgow to Edinburgh via Falkirk line.

456 Comparing these two sections, the model showed that the extent to which induced  
 457 currents can affect track circuit relays depends heavily on whether the section studied  
 458 includes the ends of the traction rail or whether it is part of a longer line. When con-  
 459 sidering the impact on relays in the centre of a line it can be seen that block length is  
 460 a first-order indicator of current across the relays. The angular difference between the  
 461 rail orientation and the electric field direction is also a factor, with blocks aligned par-  
 462 allel to the electric field having the largest currents induced along them. There are also  
 463 further subtle effects such as the lengths of blocks adjacent to a given track circuit block  
 464 which can affect the overall voltage profile.

465 Uniform electric fields of magnitude comparable to those reported in Sweden (Wik  
 466 et al., 2009) were applied to the track sections in our model. The threshold electric field  
 467 that generated sufficiently strong GICs to cause relay de-energisation in the Glasgow to  
 468 Edinburgh line was  $-2.8 \text{ V km}^{-1}$ . For the Preston to Lancaster section of the West Coast  
 469 Main Line, the threshold electric field that caused signal misoperations was  $-2.5 \text{ V km}^{-1}$ .  
 470 These values are equivalent to those generated by events that could occur approximately  
 471 once every 30 years. When electric field was strengthened to  $-4 \text{ V km}^{-1}$ , many misop-  
 472 erations occurred on both lines. For the Glasgow to Edinburgh line, in the blocks after  
 473 the crossover point where the polarity of the potential difference is reversed, an electric  
 474 field of  $4 \text{ V km}^{-1}$  was insufficient to cause any misoperations, mainly due to the short  
 475 length of those blocks.

476 Applying a 1 in 100-year extreme geoelectric field, estimated to be  $-5 \text{ V km}^{-1}$ , the  
 477 GICs generated were strong enough to severely affect the signals in the Glasgow to Ed-  
 478 inburgh and Preston to Lancaster lines. In this case, nearly all of the signals in both sec-  
 479 tions would misoperate, leading to significant operational impacts.

## 480 7 Open Research

481 Network Rail standard documents can be obtained from [https://global.ihs.com/  
 482 csf\\_home.cfm?&csf=NR](https://global.ihs.com/csf_home.cfm?&csf=NR). The magnetic storm data are accessible at [https://www.intermagnet  
 483 .org/data-donnee/download-eng.php](https://www.intermagnet.org/data-donnee/download-eng.php). The OpenStreetMap railway geometry data and  
 484 the processed data using information from Traksy (<https://traksy.uk/live>) and the Net-  
 485 work Rail Sectional Appendix are available at DOI: 10.17635/lancaster/researchdata/580.

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