Detection of tectonic and volcanic deformation as anomalies in InSAR: deep-learning tailored to differential data

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Abstract

There are now more interferograms being generated from global satellite radar datasets than can be assessed by hand. The reliable, automatic detection of true displacement from these data is therefore critical, both for monitoring deformation related to geohazards and understanding solid earth processes. We discuss improvements to an unsupervised, event agnostic method for automatically detecting deformation in unwrapped interferograms. We use an anomaly detection framework that recognises any deformation as "anomalies" by learning the 'typical' spatio-temporal pattern of atmospheric and other noise in sequences of interferograms. Here, we present developments to our prototype model, ALADDIn (Autoencoder-LSTM based Anomaly Detector of Deformation in InSAR) using (1) a self-attention training technique to exploit redundancy in interferogram networks to capture the temporal structure of signals and (2) the addition of synthetic data for training. We evaluate the impact of these developments using two geophysical scenarios: (1) the detection of the same M_w 5.7 earthquake used to test our original model (20.03.2019, south-west Turkey), (2) the persistent uplift of Domoyu volcano (17.05.2017 to 14.12.2018, Argentina). We make a quantitative evaluation of the performance of our method using synthetic test data and find that for peak displacements exceeding a few cm and of length-scale greater than a few hundred metres, overall detection accuracy is 80 to 90%.

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9 Key Points:

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10	•	We present a novel, unsupervised deep learning architecture tailored to differential
11		InSAR to flag anomalous deformation
12	•	Customised, iterative training system based on temporal self-attention improves model
13		accuracy, but training just on synthetic data does not
14	•	Highest accuracy is for signals with peak line-of-sight displacement of a few cm and
15		of a length scale bigger than a few hundred meters.

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16 Abstract

There are now more interferograms being generated from global satellite radar datasets than 17 can be assessed by hand. The reliable, automatic detection of true displacement from these 18 data is therefore critical, both for monitoring deformation related to geohazards and under-19 standing solid earth processes. We discuss improvements to an unsupervised, event-agnostic 20 method for automatically detecting deformation in unwrapped interferograms. We use an 21 anomaly detection framework that recognises any deformation as "anomalies" by learning 22 the 'typical' spatio-temporal pattern of atmospheric and other noise in sequences of interfer-23 ograms. Here, we present developments to our prototype model, ALADDIn (Autoencoder-24 LSTM based Anomaly Detector of Deformation in InSAR) using (1) a self-attention training 25 technique to exploit redundancy in interferogram networks to capture the temporal struc-26 ture of signals and (2) the addition of synthetic data for training. We evaluate the impact 27 of these developments using two geophysical scenarios: (1) the detection of the same M_w 28 5.7 earthquake used to test our original model (20.03.2019, south-west Turkey), (2) the 29 persistent uplift of Domoyu volcano (17.05.2017 to 14.12.2018, Argentina). We make a 30 quantitative evaluation of the performance of our method using synthetic test data and 31 find that for peak displacements exceeding a few cm and of length-scale greater than a few 32 hundred metres, overall detection accuracy is 80 to 90%. 33

³⁴ 1 Introduction

The abundance of routinely acquired Synthetic Aperture Radar (SAR) imagery from 35 missions such as the European Space Agency's Sentinel-1 (and anticipated for the NASA-36 ISRO SAR Mission - NISAR) has led to a surge in deep-learning-based approaches for the 37 detection of deformation (Anantrasirichai et al., 2018; Gaddes et al., 2019; Rouet-Leduc et 38 al., 2021). These efforts are critical for optimising the usefulness of large Interferometric 39 SAR (InSAR) datasets for monitoring deformation, given that the high volumes and rates of 40 data (1000-2000 images/day, $\approx 10 \text{ TB/day}$) prevents systematic manual analysis. Detecting 41 deformation in InSAR datasets is critical for monitoring geohazards (especially volcanoes 42 (Ebmeier et al., 2018), slow landslides (Bekaert et al., 2020) and anthropogenic deformation 43 (Semple et al., 2017) and for our understanding of broader tectonic processes (Elliott et 44 al., 2020)). Deep learning approaches also have the potential to transform the emphasis 45 of scientific research, allowing the automated discovery of signals in uniformly analysed 46 regional or global datasets rather than studies focused on locations where deformation is 47 already well known. 48

Deep learning has been widely applied to the field of remote sensing, (e.g., (Sharma 49 et al., 2020; Ren et al., 2021; Shakeel et al., 2019), mostly to satellite datasets that com-50 prise time sequences of images. In contrast, InSAR has a unique spatio-temporal structure, 51 as interferograms provide information about changes between two dates (differential data). 52 However, the majority of applications of deep learning to InSAR so far have used 2D spatial 53 patterns of phase in individual interferograms (Anantrasirichai et al., 2018). This has al-54 lowed the application of off-the-shelf models like AlexNet (Krizhevsky et al., 2012) or U-Net 55 (Ronneberger et al., 2015), e.g., modified by (Chen et al., 2022) for semantic segmentation 56 of active landslides. A disadvantage of this is that off-the-shelf methods are rigid in terms 57 of input size (e.g., the input size of VGG (Simonyan & Zisserman, 2015) is $224 \times 224 \times$ 58 3, where 224 is the size of an image in X and Y dimensions and 3 represents the R(red), 59 G(green) and B(blue) channels of a digital image) because they are built on existing models 60 that were initially trained on RGB images. An alternative approach is to use time-series de-61 rived from interferograms to obtain time sequences of images for input (Gaddes et al., 2019), 62 although this requires an additional processing step that also has the potential to introduce 63 errors. Most deep learning approaches applied so far for InSAR data are supervised and 64 tailored to detect specific deformation events (Anantrasirichai et al., 2018; Sun et al., 2020; 65 Rouet-Leduc et al., 2021). These approaches are either trained on event-specific labelled 66 interferograms (Anantrasirichai et al., 2018) or on synthetic data specifically designed for a 67

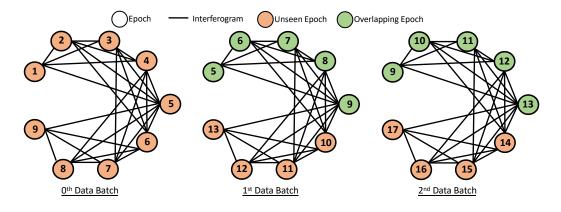


Figure 1. Cartoon of the dataset structure where each line represents an interferogram made by subtracting corresponding epochs (single date images) represented by circles. We consider a combination of 9 epochs (Time t^1 to t^9) that constructs 26 interferograms, to be a single 'data batch'. Moving along in time with a temporal overlap, the next data batch consists of 9 epochs but from t^5 to t^{13} and so on. For illustration purposes, only three consecutive data batches are shown here. The interferograms (input) constructed from the relevant epochs (output) are shown in orange when they are first passed to the model and green when they have been passed twice due to the overlapping nature of input data. The data network constructed within each batch is such that epochs from t^1 to t^5 are connected to the following four epochs but for the last 4 epochs from t^6 to t^9 , each epoch connects only with the following available epochs in the data batch. For example at epoch t^8 , it is used to construct interferograms with t^9 only, these connections can be visualized by the 'lines' in each data batch. Only one line is going forward from t^8 to t^9 .

particular task, for example, to detect volcanic deformation (Anantrasirichai et al., 2019),
 landslides (Zhang et al., 2022; Chen et al., 2022), anthropogenic signals (Radman et al.,
 2021; Anantrasirichai et al., 2020) or tectonic deformation (Rouet-Leduc et al., 2021).

Here, we present the development of an alternative approach based on anomaly detec-71 tion and tailored specifically to the differential structure of InSAR data, where individual 72 images (interferograms) represent the difference in phase between two temporally sepa-73 rated SAR images. InSAR data are very different to the video time-series commonly used 74 to develop machine learning analysis methods, where a single image, on the other hand, 75 records information at a specific moment in time (for example surveillance video time-series 76 (Nawaratne et al., 2019)). A particular challenge presented by InSAR data is the often very 77 low signal-to-noise ratio (SNR), because the contribution of deformation to the phase in 78 an individual interferogram may be an order of magnitude lower than contributions from 79 changes in atmospheric properties. We aim to develop an approach that is event-agnostic, 80 sensitive to both low-rate and transient deformation, and insensitive to errors associated 81 with higher level InSAR processing (e.g., time-series smoothing, fading signal in time series 82 constructed from short-timespan interferograms). 83

Our previous prototype work (ALADDIn: Autoencoder-LSTM based Anomaly Detec-84 tor of Deformation in InSAR (Shakeel et al., 2022)), was trained on sequences of unwrapped 85 interferograms from northern Turkey. We use a fully convolutional network (FCN) (Long 86 et al., 2015) that comprises a CNN-LSTM-based encoder and decoder, separated by a neu-87 ral network. Although the model is capable of detecting deformation as an anomaly, we 88 observed a lack of temporal dependency in some results, and qualitative analysis showed 89 that estimations of deformation varied more than expected for independent estimations of 90 the same epoch. For ALADDIn, a group of 9 epochs (making 26 interferograms, see Figure 91

1), makes up a single 'data batch', and is treated independently from the next batch. A
 comparison of epochs that were estimated by sequential batches (green circles in Figure 1)
 showed that ALADDIn sometimes estimated different spatial patterns of phase for the same
 epoch due to poor perception of the temporal connection between batches.

In this study, we present important improvements to the ALADDIn approach compris-96 ing (1) an improved training method that makes use of the redundancy in interferogram 97 networks to incorporate information about the temporal structure of signals from multiple 98 data batches and (2) the addition of synthetic data for training. We take a transfer learning qq 100 (Torrey & Shavlik, 2010) approach by re-purposing the pre-trained model from ALADDIn (Shakeel et al., 2022) with our new model for longer interferogram sequences. In addition, we 101 assess the performance of our method using three different scenarios. We evaluate and com-102 pare our models on a synthetic test dataset consisting of multiple variations of magnitude 103 and wavelength of an anomaly representing deformation (figure 5). We use the magnitude 104 5.7 earthquake from southwestern Turkey previously used as a test for ALADDIn (Shakeel 105 et al., 2022) to illustrate the impact of our method improvements (figure 7). We then assess 106 the impact of our choice of 'patch' size on anomalous deformation retrieved while exploring 107 the potential for reproducing long-lived variations in displacement rate using a volcanic test 108 case from Domuyo volcano, Argentina (figure 8). 109

110 2 Methodology

We aspire to provide a method for learning from very large, unlabelled InSAR datasets 111 without the need for manual interpretation. The process of labelling interfeorgrams to 112 act as training data is labour intensive, potentially subjective and requires a priori choices 113 about the characteristics of deformation considered interesting. In principle, more diverse 114 data results in more accurate outputs for deep learning methods (Marcus, 2018), but for 115 unlabelled datasets, this relies on the model architectures being intelligent enough to focus on 116 useful information as there is no 'target' or ground truth (set of actual input interferogram as 117 shown in figure 3(b), referred to as 'GT') available. Our solution is to approach the analysis 118 of large, unlabeled InSAR datasets as an anomaly detection problem, where anomalies 119 are any phenomena that differ from the dataset's "normal" spatio-temporal patterns. For 120 InSAR, we consider 'normal' phenomena to arise from any contributions to phase not caused 121 by changes to the Earth's surface. These are generally dominated by atmospheric phase 122 contributions, but may also include errors in estimations of satellite orbitals and 'nuisance' 123 signals associated with processing such as unwrapping errors, e.g. (Emardson et al., 2003; 124 Simons & Rosen, 2007). 125

Autoencoders (Baldi, 2012) and fully convolutional networks (FCN) (Long et al., 2015), 126 are types of network architectures commonly deployed to perform unsupervised tasks (Bengio 127 et al., 2012). The input and output of such models are identical, so the models learn the 128 underlying distribution of the data and represent them in the form of low-dimensional fea-129 ture embedding. These embedding act as a bridge between an encoder and a decoder (the 130 main components of an autoencoder), that encrypts and de-crypts useful information about 131 multiple attributes of the data. For the task of anomaly detection, these models are trained 132 on 'normal' data so that they learn the distribution of 'normality' (Gong et al., 2019). After 133 training, when these models are tested on anomalous data, they predict the output with 134 high reconstruction loss as they are unable to accurately reconstruct the anomaly (as they 135 are rare and never seen by the model). Different combinations of layers can be added to 136 these architectures to meet the objectives of the task and to suit the particular data prop-137 erties. The wide applications of autoencoders for anomaly detection include (Zhao et al., 138 2017; Gong et al., 2019). 139

Both ALADDIn (Shakeel et al., 2022) and the developments presented here take an anomaly-detection approach based on the use of autoencoders and thus avoid both timeconsuming pixel-wise labelling for training data and are agnostic in terms of deformation

detected. By using networks of interferograms as inputs we treat spatial and temporal 143 patterns co-dependently and do not rely on the derivation of time series from interferograms 144 that could introduce further artefacts. We exploit the fact that 'normal' signals associated 145 with individual SAR acquisition dates ('epochs') contribute to related interferograms with 146 a temporal pattern that is quite distinct from deformation, which appears as 'anomalous'. 147 Our model is trained to predict background epoch time-series from the noise in a redundant 148 network of interferograms. Because deformation has a distinct temporal structure, we can 149 therefore separate it from the predicted baseline signals. 150

151 2.1 Dataset details

We use Sentinel-1 InSAR data for training and testing our model. Our input data 152 are networks of unwrapped interferograms in radar coordinates generated automatically by 153 the COMET LiCSAR processing system (Lazecký et al., 2020)¹. This system constructs 154 interferograms with the 4 shortest possible timespans both forwards and backwards from 155 each epoch (as illustrated in the figure 1). For a satellite repeat time of 6 days, this results 156 in each epoch contributing to 8 interferograms (6,12,18,24 days). We re-purpose the model 157 pre-trained for ALADDIn here, using a transfer learning approach. ALADDIn was trained 158 on data from Turkey (Shakeel et al., 2022) and here, we use the same training dataset 159 (LiCSAR Frame name: $014A_04939_131313$, data spanning from the year 2017 to 2019) 160 that was first passed through ALADDIn and its predictions are used to initiate the training 161 of our new temporal self-attention model. This dataset was selected on the basis that they 162 were not expected to contain any known examples of deformation, but were dominated by 163 atmospheric signals. 164

The frame is divided into cubes of size $256 \times 256 \times 26$ pixels, covering an area of \approx 165 20.5 $km \times 20.5 km$. This is done in order to manage the model's complexity and the 166 memory needed to train a large number of parameters. Also, instead of passing the entire 167 time series to each training iteration, a set of 26 interferograms (abbreviated to IFGM) that 168 cover 9 epochs (abbreviated to EP) are passed, with a 50% spatial overlap (in both N-S 169 and E-W directions). This set is called a data batch and is shown in the figure 1, where 170 circles represent EP and the lines connecting each circle i.e. EP represents the IFGMs. The 171 9 EP long temporal sliding window moves with a stride of 4, ensuring a > 50% temporal 172 overlap between subsequent input sequences. Each EP in the sequence is connected to all 173 subsequent and preceding EP by the 26 IFGM, up to a maximum distance of 4 forward and 174 backward in time. For instance, the central EP is linked to all other EP by 8 IFGM, but all 175 other EP in the data batch are linked with fewer than 8, with the first and last EP in the 176 batch being linked with a maximum of 4 IFGM (as illustrated in the figure 1, where only 177 four lines/IFGMs can be seen linking EP at t^1 and t^9). 178

179

2.2 New network architecture using temporal self-attention

We designed the network architecture of this training system to exploit redundancy in 180 the input interferogram network, that is, that information about each epoch may appear in 181 multiple interferograms (figure 1). Despitef a high detection rate (91.25% overall performance 182 accuracy on a synthetic deformation test case) ALADDIn (Shakeel et al., 2022), produced 183 a different set of solutions for the five EP that overlap between data batches (figure 1 green 184 circles represent overlapping EPs in the data network). We, therefore, aim to design a 185 system that predicts realistically similar spatio-temporal patterns for EPs in the overlap 186 between data batches. 187

¹ The unwrapped radar-coordinate data format with which the interferograms were saved until the year 2019, is no longer saved. However, the exact data format on which this model is trained can be reconstructed from the LiCSAR intermediate products that are preserved

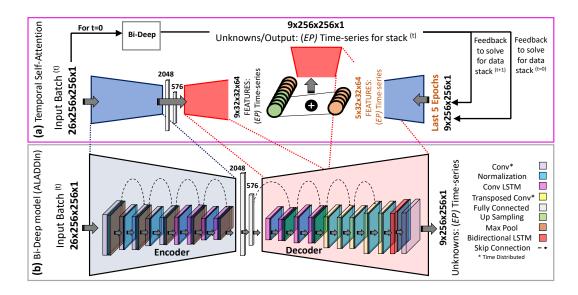


Figure 2. Illustration of network architecture and self-attention training scheme. (b) Bi-Deep model from AlADDIn pipeline (Shakeel et al., 2022) is used for pre-trained weights and to initiate predictions for self-attention. The layers used to create the architecture are: time-distributed 2D convolutional, maxpooling, normalization, 2D convolutional LSTM, fully connected layers, transpose convolutions, upsampling and a bi-directional LSTM layer. Skip connections are also in place to merge features. For temporal self-attention in (a) the decoder is disconnected to fuse features from the overlapping epochs from the previous data batch^(t-1). The pre-predictions from the previous data batch^(t-1) is passed through a mini-encoder consisting of a pair of time-distributed conv and two convolutional LSTMs

The base of the deep learning model is a fully convolutional network, including an autoencoder combined with a neural network as shown in figure 2(b). We use the same number of layers as used in the encoder and decoder of ALADDIn (Shakeel et al., 2022). In fact, instead of initializing the weights of these layers from scratch, transfer learning (incorporation of previously learned knowledge(Torrey & Shavlik, 2010)) is applied and the previously trained weights are utilized to begin training.

The encoder translates the hidden features/distributions of the input data batch, which 194 is a batch of interferograms (26x256x256) (figure 1). The neural network then converts the 195 features that are learned from IFGMs into the form of EPs (9x256x256). This converted 196 feature space is then decoded and interpreted to predict the unknown EP time-series. This 197 EP time-series should be spatially and temporally consistent (in a sequential manner), re-198 gardless of the overlapping nature of the data batches. The features learned for every (data 199 $batch^{(t-1)}$) batch should therefore facilitate learning for its proceeding (data $batch^{(t)}$), es-200 pecially for overlapping epochs, as they are already been computed in the previous iteration 201 when $(data \ batch^{(t-1)})$ was processed. This form of attentive learning (a mechanism that 202 focuses on specific temporal regions in a sequence to create a representation of it, for ex-203 ample, here have focused specifically on overlapping EPs.) is introduced in the decoder 204 part of the model. The continuity of the decoder is interrupted and predictions of the last 5 205 epochs (data batch^(t-1)) are fed back by passing them through a mini encoder. These fea-206 tures are combined with the first 5 epochs ($data \ batch^{(t)}$). The merged features are passed 207 to the rest of the decoding layer to make refined epoch predictions. In this way, the cyclic 208 nature of deep learning model training and backpropagation is not affected. Because no 209 previous prediction is available in the case of the very first $data \ batch^{(t=0)}$, the 5 epochs are 210 constrained only by features using the Bi-deep model of ALADDIn (Shakeel et al., 2022). 211

The model consists of a set of convolutional and convolutional Long Short Term Memory 212 (LSTM) with pooling layers in the encoder. The purpose of pooling layers is to down-213 sample the input, by taking, for example, a minimum, maximum or average value. In this 214 model, we have used maximum pooling (referred to as maxpool), to gather the maximum 215 value of features within a window size. Likewise, transposed convolutions and convolutional 216 LSTM with upsampling layers are combined in the decoder. In between the encoder and 217 decoder, the neural network consists of three 1D fully connected (FC) layers. The 3D 218 convolution layer spans the input spatially in all dimensions, whereas the Long shot-term 219 memory (LSTM) layer (originally 1D) is capable of maintaining memory with the help of 220 learnable 'forget', 'input' and 'output' gates. This, when combined with the convolutional 221 operation, serves for any multi-dimensional input. This layer is tailored for the specific task 222 of learning both spatial and temporal patterns co-dependently. Every convolution layer is 223 followed by a normalization layer and maxpool for downsampling in the encoder. Similarly, 224 in the decoder, every convolutional LSTM is followed by normalization and upsampling 225 layer. Transposed convolutions (often called deconvolutions) perform similar operations but 226 with broadcasting the feature map instead of downsizing. The mini-encoder used for the 227 attention of overlapping 5 epochs consists of 2 pairs of convolutions, convolutional LSTM 228 following normalization and maxpooling layers. 229

The neurons used in the fully connected layers are 2048 and 576 (see figure 2). These 230 number of neurons are of immense importance, as they are used for converting the feature 231 maps from 26 interferograms (at the encoder side) to 9 epochs (at the decoder side). For 232 example, the size of data after being processed by the encoder is downsized from $26 \times 256 \times$ 233 256×1 to $26 \times 8 \times 8 \times 1$ then the decoder should receive an input of $9 \times 8 \times 8 \times 1$. Hence, 234 the neurons in the 2nd FC layer are computed by multiplying the dimensions $9 \times 8 \times 8 \times 1$ 235 = 576. So, it can be unrolled back into the dimension = $9 \times 8 \times 8 \times 1$ and used by the 236 multi-dimensional layers in the decoder. Tanh activation functions are used for every layer. 237 This function ranges from [-1 to 1] which is ideal for this model, as negative values are 238 equally important as positive values. 239

Furthermore, skip connections are added for feature reusability and to avoid the problem 240 of vanishing gradients (Hochreiter, 1998), where the weights (calculated by each layer in a 241 'deep' model) gradually decrease to zero and backpropagation fails. In deep convolutional 242 models, this problem often occurs and hinders learning. Skip connections are represented 243 by dotted lines in figure 2(b), their purpose is to re-use the output of layers and feed to 244 deeper layers, to merge the information and process - adding more features helps to dodge 245 the vanishing gradient problem. Finally, a bidirectional convolutional LSTM layer is added, 246 that spans the output both forwards and backwards and combines features to refine the 247 predictions. Two loss functions are used to constrain the model: 248

$$Loss_{IFG} = \sum_{i=1}^{n} (Output_{IFGM} - Input_{IFGM})^{2}$$
$$Loss_{EP} = \sum_{i=1}^{n} (5_{epochs^{t}} - 5_{epochs^{t-1}})^{2}$$
$$Loss = Loss_{IFG} + Loss_{EP}$$
(1)

where n is the number of interferograms in the case of $Loss_{IFG}$, it refers to the loss com-249 puted between reconstructed interferograms by the model and the input interferograms 250 which is also the ground truth. $Loss_{EP}$ is the difference between the current predictions of 251 overlapping epochs and the previous ones, so here n is 5, and the accumulated loss is then 252 backpropagated. With TensorFlow (Abadi et al., 2015) as the backend, the model is trained 253 using Keras (Chollet et al., 2015), a deep learning API. While training, the batch size was 254 set to 1 due to the size of the images in memory being so large. A model can learn features 255 through gradual changes to a loss as opposed to abrupt fluctuations when the learning rate 256 is lower. We therefore selected a learning rate for the Adam optimizer (Kingma & Ba, 2014) 257 of 0.00001. 258

259 2.3 Framework for Anomaly Detection

When our model is tested against anomalous data, we expect to find high spatial resid-260 uals between our input data and our predicted signals and/or a high overall reconstruction 261 error. Due to the event-agnostic nature of our approach, we do not rely on identifying 262 specific patterns in the reconstruction error. Because we have no preconceptions about the 263 spatial size, intensity and temporal structure of an anomaly, we design a novel detection 264 framework to pick up all kinds of anomalies with a minimum possible rate of false positives. 265 The prediction for every input data batch is refined based on the estimations of findings from 266 previous data batches. We take full advantage of this capability and introduce "shuttling" 267 during test time. "Shuttling" as its name suggests, completes multiple passes in forward and 268 backward directions for all of the data batches, as shown in figure 3(a), here for illustration 269 purposes the data contains three batches only. During the backward pass, the data is flipped 270 spatial as well because now the pre-EP image serves as the post-EP image to compute the 271 interferogram which is: $post_{EP} - pre_{EP}$. The residuals (RES) shown in figure 3(b) reveal 272 that reconstruction is more accurate after shuttling is implemented and the residuals are 273 near zero after the second forward pass. Input IFGMs that have spatial data gaps or pixels 274 with missing values ('NaN') are a data error and one such IFGM is shown in figure 3(b) 275 black boxes. If 'NaN' is passed through the model, it will propagate through the model due 276 to backpropagation and diminish the learning to a 'NaN'. To avoid this, we identify these 277 missing values and replace them with a zero. This introduces box-like patterns of zeros in 278 the input, but as we are enforcing the model to learn both temporal and spatial patterns. 279 This helps the model to predict even when the input is zero (as shown in the black boxes of 280 the figure 3 (b) 'PRED'). Even though the model makes estimates for missing pixels, these 281 box-like patterns are passed in the 'RES' through subtraction of PRED and GT. 282

Once the data are shuttled completely (terminated at the third pass, when no improvement results is observed), we expect anomalies to appear as a residue in residual (RES) IFGM as shown in6. An interferogram captures the changes that occurred between two dates, so potentially spans multiple EPs. An anomaly will therefore always show up in several interferograms for our data structure. We first reduce the residuals to a set of N_{EI_r} "residual epoch intervals" that are mutually exclusive in order to precisely detect the temporal window of an anomaly. Since an EP interval is a different image that spans two subsequent EP, so, N_{EI_r} is one less than the total number of EP. As N_{EI_r} are computed from the entire set of residual (RES) interferograms rather than just one residual image, these intervals are more noise-resistant than the shortest spanning set of residual "daisychain" interferograms. We execute a linear least squares inversion on a pixel-by-pixel basis of our N_{IFGM_r} residuals in order to estimate this set of N_{EI_r} residual epoch intervals (based on the SBAS approach (Berardino et al., 2002)):

$$d_{IFGM_r} = G.m,\tag{2}$$

where d_{IFGM} is an array of size $N_{IFGM_r} \times 1$ containing all N_{IFGM_r} residual interferograms' pixel values, m is also an array of size $N_{EI_r} \times 1$ containing values of residual EP intervals that we wish to solve for, and G is the design matrix of size $N_{IFGM_r} \times N_{EI_r}$ for this system of equations, which only contains 1s and 0s. For a set of six residual interferograms $(IFGM_{12_r}, IFGM_{13_r}, IFGM_{14_r}, IFGM_{23_r}, IFGM_{24_r}, IFGM_{34_r})$ that are created from four epochs $(EP_{1_r}, EP_{2_r}, EP_{3_r}, EP_{4_r})$, matrix G is displayed as an example in Eq 3. This system will output three epoch intervals $(EI_{12_r}, EI_{23_r}, EI_{34_r})$ based on the residuals.

$$\begin{pmatrix} IFGM_{12_r} \\ IFGM_{13_r} \\ IFGM_{23_r} \\ IFGM_{24_r} \\ IFGM_{34_r} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} EI_{12_r} \\ EI_{23_r} \\ EI_{34_r} \end{pmatrix}$$
(3)

Instead of using all residuals of the overlapping epochs, we only use the latest ones predicted by the model, which should be the most reliable. Also, we perform the linear least square

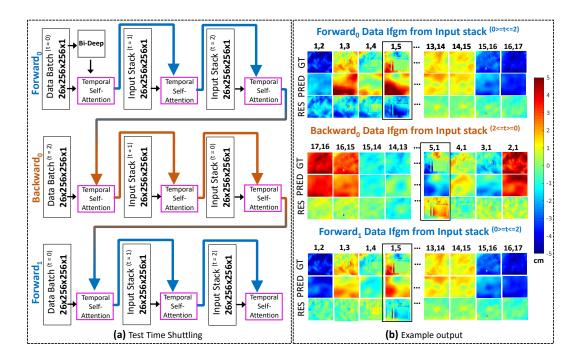


Figure 3. (a) Temporal self attentive training and test-time shuttling procedure is illustrated here. Features of overlapping EP (green circles in figure 1) from data batch^{t-1} are fed in the model (pink box) for every batch^t as we move across time from batch^{t=0} to batch^{t=2}. While testing the same procedure is repeated for backward interferograms (both in space and time). The last IFGMs of forward pass (e.g., 15,16 and 16,17) are now the first IFGMs of the backward pass (e.g., 17,16 and 16 and 16,15). This process is called shuttling, it is repeated for another forward pass and so on until no change in the output is observed (only three passes are shown here for illustration purposes). (b) Shows an example output from of the process, where 'GT' refers to ground truth IFGMs (output of the model) and 'RES' are the residual IFGMs computed by subtracting PRED from GT to measure what is missed by the model. Shuttling helps to achieve model predictions that are close to the input 'GT'. In comparison of 'RES' of forward₀ (top row) and with 'RES' of forward₁ (bottom row), it is clear that the 'RES' is near zero. Black boxes enclosing IFGM 1,5 in all shuttling iterations display an example of spatial data gaps or pixels with missing or 'NaN' values, that are replaced with a zero before passing through the model.

inversion for both, forward progressing data and backward progression data, to create two independent sets of residuals *EP* intervals for detection. The presence of spatial anomalies is then automatically identified in these intervals using two complementary analysis techniques: density-based clustering (DBSCAN) (Kriegel et al., 2011) and semivariogram analysis (Wackernagel, 2013).

The residual epoch intervals are predicted to have values close to zero in the absence 290 of anomalous deformation because the model will accurately reconstruct them (e.g. see 291 figure 3(b), but in the event of an anomaly or multiple anomalies within a sequence, the 292 spatial structure of that anomaly will be visible in at least one epoch residual. Our goal is 293 thus to separate 'normal' intervals from the anomalous ones, without any prior knowledge of 294 where anomalies anomalies appear in a sequence. We use a clustering algorithm (DBSCAN) 295 (Kriegel et al., 2011) that does not require an a-priori specification of the number of clusters 296 to locate anomalies. To ensure we detect all anomalies, we use both, forward and backward 297

independent sets of RES *EP* intervals and perform DBSCAN combining them, establishing two as the minimum number of points in a cluster.

To distinguish between larger areas that are normal and anomalies with specific spatial 300 frequencies (such as deformation that is distributed over small regions), we take into account 301 the spatial variability measured by the semivariogram. By clustering or just computing bulk 302 differences between the actual and reconstructed images (e.g. by a Mean Squared Error), 303 these localised but significant changes are less likely to be found. We anticipate that residual 304 epoch intervals (constructed using residual interferograms i.e. ground truth - prediction) 305 that contain no anomalies will all have a similar spatial structure and, consequently, similar 306 empirical semivariograms, whereas epoch intervals that do contain anomalies will have semi-307 variograms that significantly deviate from this typical structure. For each residual epoch 308 interval a semivariogram is computed, and the root-mean-squared-error between each semi-309 variogram and all others in the complete set of residual epoch intervals across all sequences is 310 calculated. In order to minimise the number of false positives, the classified anomalies from 311 the semivariogram and clustering analysis of epoch interval time series are combined using 312 the AND operation. The variables and parameters used for both these analysis method are 313 same as ALADDIn (Shakeel et al., 2022). 314

315 **3** Training with Synthetic Data

The anomaly detection model is built by understanding the continuous background 316 atmospheric noise (normality). So when an anomalous event (earthquake, volcano, etc) 317 occurs, the model detects it with high error - as the model fails to understand it due to 318 its anomalous nature. The data used to train our model is real InSAR data from a region 319 of Turkey, that do not contain any anomalous activity, but does contain data errors like 320 unwrapping errors that introduce anomaly like patterns in the IFGMs. Deep learning models 321 have been presented in the past to pick unwrapping errors (Zhou et al., 2021; Sica et al., 322 2020; Wang et al., 2021), ALADDIn (Shakeel et al., 2022) also detects these as an anomaly. 323 The spatial data gaps and missing values for pixels also introduce artifacts in the data. In 324 an attempt to further improve the detection accuracy of our method, a synthetic training 325 data set is designed based on realistic background atmospheric noise. Synthetic datasets 326 are commonly used to train deep learning models, as employing it overcomes the problem 327 of data imbalance (Anantrasirichai et al., 2019). We test the impact of using synthetic 328 training data on the performance of our model. We expected that the addition of synthetic 329 training data should reduce any impact of unwrapping and other processing-related errors. 330 We construct our synthetic interferograms by first generating synthetic epoch images from 331 which to build them. Our simple synthetic 'normal' (non-deforming) data set is made up 332 from phase (ϕ) contributions from a planar ramp (ϕ_{ramp} , representing residual errors in 333 estimation of satellite orbits), stratified troposphere (ϕ_{strat_atm}) and turbulent troposphere 334 $(\phi_{turb,atm}, \text{described in terms of maximum phase variance}, maxvar and characteristic length)$ 335 scale exponent, α), similar to (Ebmeier, 2016) and described as: 336

$$\phi_{ramp} = aX + bY + c$$

$$\phi_{strat_atm} = kH$$

$$\phi_{turb_atm} = \sqrt{maxvar} * \exp(-r * \alpha)$$

$$\phi_{EP} = \phi_{ramp} + \phi_{strat_atm} + \phi_{turb_atm}$$
(4)

where X and Y are pixel locations and H is the elevation from digital elevation model (DEM). The appropriate parameters are estimated using linear least square inversions (e.g., eq 2), where matrix $d_I F G$ is the interferogram patch, reshaped as 65536×1 array, G is the design matrix (size: 65536×4) containing horizontal pixel location (X), vertical pixel location (Y), elevation (H) and ones (for constant c) and m is the desired output of 4 parameters (a,b,c,k). These values are computed for each patch location for all available time acquisitions of the Turkey data frame used for training. We estimate the parameters (maxvar, α) for

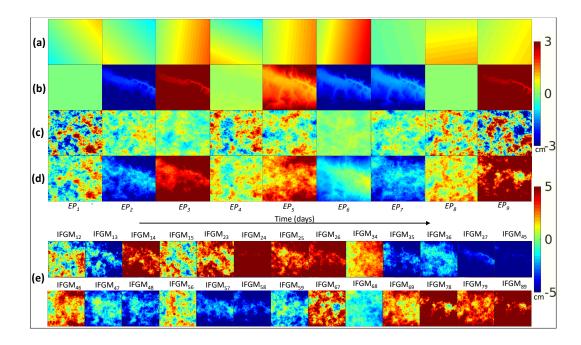


Figure 4. Visualization of the synthetic training data. (a) Planar ramp ($Component_A$), (b) Stratified tropospheric ($Component_B$), (c) turbulent tropospheric ($Component_C$), (d) synthetic 9 epoch generated by aggregating all components (eq 4). (e) 26 synthetic interferograms, following the data structure presented in figure 1 are made using the generated epochs shown in (d). The line-of-sight displacement is measured in cm on a scale of -5 to 5 cm for (d) and (e), where as (a), (b) and (c) are measured on a scale of -3 to 3 cm.

 (ϕ_{turb_atm}) using the residual interferogram after removal of $\phi_{strat_atm} + \phi_{ramp}$:

$$R = d_{IFG} - G.m,\tag{5}$$

To generate the synthetic EP, a, b, k, c, maxvar and α are drawn randomly from a distribution of each of these parameters with mean = 0 and standard_deviation estimated their distribution in the training dataset. Because the variables are computed using interferograms, their sigma values are divided by $\sqrt{2}$ so that it can be used to draw a distribution for EP images.

We use the same network architecture described in Section 2.2, but synthetic data replaces the real data for training of both the Bi-Deep model of ALADDIn and temporal self-attention model. The one main difference when using synthetic training data is in the estimation of the loss function. Previously, we have been using the predicted epochs to reconstruct interferograms to compute loss function. Now, we use the aggregated loss of interferograms and epochs, to take advantage of having synthetic 'ground truth' of *EP* themselves.

349 4 Results and Analysis

We evaluate the performance of our improved models on the basis of (1) temporal consistency in overlapping data batches, (2) the range of anomalies detectable in terms of spatial and temporal scale, (3) the models ability to process large areas using sliding spatial and temporal windows and (4) its ability to detect a range of deformation types. We make a quantitative assessment of the detection capabilities of our model using very simplified synthetic deformation (Section 4.1, Figure 5). Our first real-data test case, the 20th March 2019 Southern Turkey magnitude 5.7 earthquake, was also selected to allow us to assess the
impact of the developments presented here using a relatively high SNR deformation pattern
(Section 4.2, Figure 7. The second, more challenging test, involves relatively high rate
deformation (> 10 cm/yr) at Domuyo volcano, Agentina, that is nevertheless not apparent
in individual shorter timespan interferograms due to high magnitude atmospheric noise
(Section 4.3, Figure 8).

4.1 Tests on synthetic data

362

We select which model to apply to real datasets, by using synthetic tests to evaluate the performance of all four model variants: (1) ALADDIn trained on real data (the prototype model presented by (Shakeel et al., 2022), (2) Temporal self attention model trained on real data, (3) ALADDIn trained on synthetic data and (4) Temporal self attention model trained on synthetic data.

We design a synthetic test to compute the accuracy and assess the capacity of our models in terms of the wavelength and magnitude of the deformation signal that can be accurately reconstructed from our model. For simplicity, we use a 2D Gaussian spatial displacement pattern with varying magnitude and wavelength, and add it at eight random instances in a test patch location of Turkey data frame (LiCSAR frame $014A_04939_{-131313}$ i.e. the southern section of our training frame reserved for evaluation purposes) that has never been seen by the model during training. The variance of this dataset ranges from 0.1 to 22 with a mean value of 2.4. Noise is dominated by atmospheric phase contributions with typical wavelengths of 10's km. Our synthetic deformation anomaly takes the form:

$$Z(x,y) = A.\exp(-(x^2 + y^2)/r)$$
(6)

where r is the exponential length-scale or wavelength, that varies from 10 m to 12 km. A 368 is the scaling parameter that is directly proportional to the magnitude or peak-value that 369 varies from 1 cm to 11 cm (almost doubling each time to cover maximum range with fewer 370 test variations). The spatial coordinates x and y are relative to the location of Gaussian 371 peak. This means that the SNR for this test dataset range from 0.0003 to 70 (1 cm peak 372 displacement) to 0.0000003 to 1.7 (11 cm peak displacement). The magnitudes shown on the 373 y-axes of Figure 5a reflect peak displacement, which means that the average displacement 374 values are in practise much lower. The detection thresholds indicated by the pink boxes 375 on Figure 5a are therefore very conservative and we are in practise are likely to be able 376 to detect lower average magnitudes of deformation, depending on SNR and interferogram 377 network redundancy (see Section 4.3). 378

We examine a total of 105 scenarios, each consisting of 10 data batches (spanning from 379 to 28^{th} July 2017 to 18^{th} April 2018), containing 8 synthetic anomalies. The test set is 380 passed through all four models and a comparative analysis is done on a quantitative as 381 well as qualitative basis. Figure 5 (a) shows a heat-plot of true positive rate (TPR also 382 called the Recall). As it is a synthetic dataset, ground truth is known before hand and 383 one-hot encoding (an array of zeros and ones representing whole dataset) of ground truth 384 and predictions are computed, where a label '0' is for normal data and '1' for an anomaly. 385 TPR (Recall) is then plotted for each test sample and for each model. The two network 386 architectures ALADDIn and Temporal self-attention, along with their synthetically trained 387 counterparts, follow similar patterns of performance. Both ALADDIn and Synth-ALADDIn 388 perform weakly with a low TPR (Recall) (<20 % and lower) even for higher magnitudes 389 and wavelengths. The temporal self-attention model and its synthetic counterpart perform 390 better, with higher TPR (Recall) (>60%) for lower magnitudes (2 cm) and higher wave-391 lengths. The mean recall is then plotted in comparison with the mean false positive rate 392

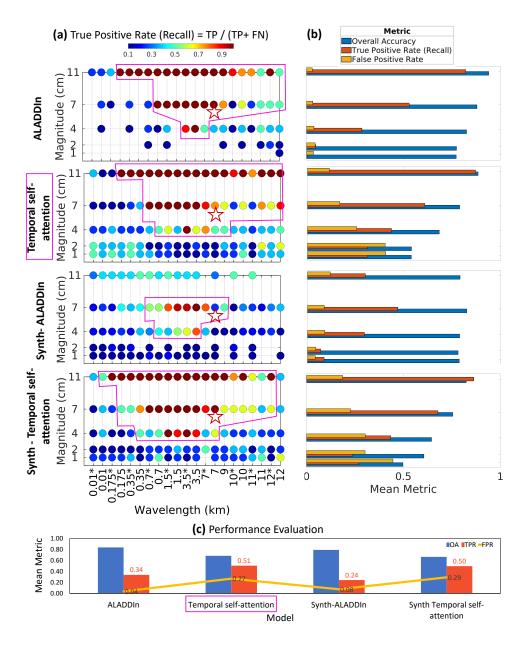


Figure 5. (a) Heat map plot of true positive rates (Recall) for all four model, ALADDIn (Shakeel et al., 2022), Temporal self-attention, synthetic-ALADDIn (trained on synthetic data) and synthetic-Temporal self-attention (trained on synthetic data). SNR ranges from (0.0003 to 70) for 11 cm peak value and (0.0000003 to 1.7) for 1 cm. For 4 cm SNR ranges from (0.00004 to 11). Pink polygon on each of these plots display the region of accurate detection of each model. The x-axis corresponds to wavelengths starting from 10 m to 12 km, '*' represents the same wavelength but with different location (bottom left corner) on the patch. Y-axis corresponds to varying magnitudes from 1 cm to 11 cm. The red star marks the size of the Turkey earthquake shown in Figure X. (b) Bar plots illustrating mean recall (orange), mean false positive rate (yellow) and mean overall accuracy (blue) for all four models. Note that the detectable displacement magnitudes quoted here are peak values in a dataset with a background of variance of 0.6 m, and are therefore very conservative.

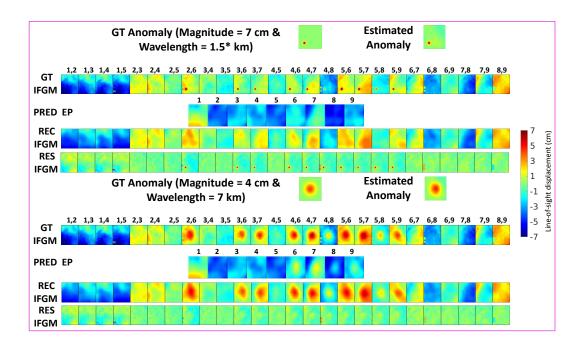


Figure 6. The output of two synthetic data batches for the Temporal self-attention model. The figure shows two examples of synthetic anomalies, (top) magnitude 7 cm and wavelength 1.5 km and (bottom) magnitude 4 cm and wavelength 7km. 'GT IFGM' is ground truth interferogram, 'PRED *EPs*' is the predicted epoch, 'REC IFGM' is the reconstructed interferograms made using PRED *EPs* and 'RES IFGM' is the residual interferogram that carries the anomalous signal missed by the predictions.

(FPR) and mean overall accuracy for each magnitude, as follows::

$$TPR(Recall) = TP/(TP + FN)$$

$$FPR = FP/(FP + TN)$$

$$OA = (TP + TN)/(TP + TN + FP + FN)$$
(7)

where TP is true positive, FP is false positive, TN is true negative and FN is false negative. 394 Negative here corresponds to the 'normal' data or 0's and positive corresponds to anomalies 395 or 1's. OA is the overall accuracy, TPR and FPR are true and false positive rates respec-396 tively. The plots in figure 5 (c) shows that average overall accuracy of each model is greater 397 than 70%, dominated by a high specificity (high TN rate). The FPR increases as we move 398 across the models, largely because the model is fitting to the 'normality' it learned from 399 the training data, leaving greater residuals and resulting in false flags. These FPs includes 400 unwrapping errors and missing data as well as signals due to deformation. The models that 401 do a better job of predicting 'normal' interferogram patterns therefore flag more of the errors 402 in the input data, which are classified as anomalies according to our tests. The temporal 403 self-attention model has proven to be the most accurate one when compared to its synthetic 404 counterpart because the former's FPR is lower (as shown in figure 5 (b)). Figure 6 displays 405 the results of temporal self-attention for two synthetic test scenarios both for low magnitude 406 and greater wavelength (bottom) and for higher magnitude and lower wavelength (top). The 407 model accurately estimates the spatial structure of flagged anomaly as shown in figure 6. 408 The capacity of each model - that is the range of anomaly wavelengths and magnitudes it is 409 capable of flagging - is indicated by the pink polygons on figure 5(a)). The area of polygon 410 is much greater for Temporal Self-attention and its synthetic counterpart than the original 411 ALADDIn model. 412

Models	$\mathbf{F1}$	F0.5	$\mathbf{F2}$
ALADDIn	0.36	0.39	0.34
Temporal self-attention	0.41	0.37	0.45
Synth-ALADDIn	0.26	0.30	0.24
Synth Temporal self-attention	0.37	0.33	0.43

 Table 1.
 Fbeta Measure

Similar trends can be seen in Table 1, where Fbeta score is considered to balance the 413 affect of minimizing FP (Precision) or minimizing FN (maximizing TP) (Recall). These 414 two factors are combined with a beta values of (1, 0.5 and 2) to compute the Fbeta scores. 415 It is calculated using eq 8. When beta is 1, where recall and precision are given equal 416 importance, Temporal self-attention has the maximum score of 0.41. But when beta is 417 decreased to 0.5, this mean that the measure is focusing more towards minimizing FP then 418 the score of ALADDIn is greatest with 0.39. Whereas, when beta is 2, that is giving more 419 weight to the Recall then again Temporal self-attention has the maximum score of 0.45. The 420 analysis proves that the Temporal self-attention model is best as it outperforms all others 421 models in terms of balancing a high recall. We emphasise the recall in our analysis, because 422 we do not want the model to miss any anomalies. While FP can always be reviewed by 423 human intervention, we prioritise not missing an event that might be anomalous. 424

$$Fbeta = \frac{((1 + beta^2) \times Precision \times Recall)}{(beta^2 \times Precision + Recall)},$$
(8)

425

426

4.2 Real case study (I): 2019 Turkey earthquake

We use a 5.7-magnitude earthquake that took place in southern Turkey on 20^{th} March 427 2019 (Elliott et al., 2020), and was previously used to test ALADDIn (Shakeel et al., 2022) 428 to evaluate the accuracy of our models. This south-western region of Turkey has experienced 429 major earthquakes in the past (M_w 7.0 in 1914 (Ambraseys, 1988), M_w 6.2 in 1971 (Taymaz 430 & Price, 1992), M_w 6.2 in 1995 (Wright et al., 1999) and M_w 6.6 in year 2017 (Karasözen 431 et al., 2018)). InSAR data that has been analysed by our model, estimates deformation of 432 approximately 4 cm (as reported by (Elliott et al., 2020)), shown in figure 7 (c). The data 433 for this test case is processed from the time-period 18^{th} September 2018 to 10^{th} April 2019. 434 We divide the data into 7 data batches (according to figure 1), comprising 32 epoch intervals 435 in total. This test region is never seen by any of the models during training. The method 436 ALADDIn successfully detected this earthquake and estimated its spatial structure, but due 437 to the overlapping data structure, two variations of the same instantaneous anomaly were 438 retrieved, as shown in figure 7 (a). It can be seen that the Temporal self-attention model 439 constructs one, more accurate, estimate (the spatial structure in the EI_r closely matches 440 with the GT structure captured in the IFGMs) of epoch-interval whereas the two variations 441 estimated by ALADDIn are different in terms of spatial pattern (shown in figure 7 (a)). On 442 comparison of residual intervals EI_r (figure 7 (a)) with the estimated earthquake structure 443 (figure 7 (d)), it can be seen that the proposed method produces an anomaly pattern in the 444 residuals closer to actual structure (as reported by (Elliott et al., 2020)). The 10 anomalous 445 interferograms (shortest 6-day to longest 24-day) spanning the earthquake are all flagged by 446 the model. These are marked red in the plot shown in figure 7 (c) as compared to the rest 447 'black' (normal) interferograms. The estimated spatial structure of the flagged anomaly by 448 the Temporal Self-attention model is shown in figure 7 (e). 449

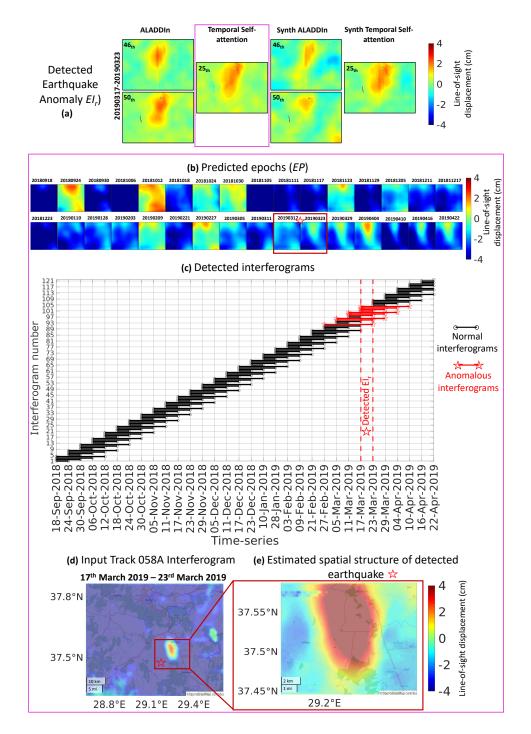


Figure 7. Test results of real earthquake of all four models are shown in this figure. (a) shows the detected residual based epoch intervals (EI_r) of all four models. (b) Shows the predicted epoch (EPs) for the Temporal Self-attention model. The red box enclose the 2 EPs that cover earthquake date (20.03.2019), represented by a red star. (c) Shows the network of interferogram used for testing with detected interferograms marked red, covering the detected earthquake interval (marked with red dotted line). (d) Shows the shortest interferogram capturing the earthquake anomaly. (e) Shows the zoomed in patch of estimated spatial structure of the detected anomaly.

4.3 Real case study (II): Domuyo Volcano, Argentina

450

We apply our most accurate model - Temporal Self-attention trained on real data - to an 451 additional real test case. We select a well-documented period of uplift at Domuvo volcano. 452 Argentina (Lundgren et al., 2020; Astort et al., 2019; Derauw et al., 2020), because this 453 allows us to examine (1) how our model trained on real InSAR data from northern Turkey 454 performs in a location with completely different atmospheric conditions and topography and 455 (2) how well we can detect persistent rather than transient deformation, and (3) how our 456 model performs when the deformation signal (in this case - 64×40 km) exceeds our patch 457 458 size $(20.5 \times 20.5 \text{ km})$.

Domuyo stratovolcano (4702 m elevation), in northern Patagonia, is thought to be late 459 Pleistocene (but possibly Holocene) age. It has no record of historical activity, but a major 460 hydrothermal field centred southwest of the volcano's flanks has a very high thermal energy 461 release and recent gas-driven explosions, which imply the presence of an active magmatic 462 system (Chiodini et al., 2014; Lundgren et al., 2020). Further evidence for this comes from 463 uplift, which has been attributed to the intrusion of volatile-rich magma at 6.5-7 km depth 464 (Astort et al., 2019), and has occurred in lagged correlation with edifice-wide warming 465 (Lundgren et al., 2020). Domuyo subsided between 2008 and approximately 2013, before 466 entering a phase of uplift in 2014 with a maximum rate of 15 cm/yr. Uplift slowed until 467 early 2021, when the volcano began to subside. We selected a period of relatively high-rate 468 uplift between May 2017 and December 2018 for our method test (Figure 8a). Over this 469 interval deformation was relatively constant, so we expect every interferogram to be flagged. 470

This case study also provides the opportunity to assess the implications of applying deep 471 learning to automatically processed, noisy InSAR data sets with significant of data gaps. 472 The network design for standard LiCSAR processing relies on short timespan interferograms: 473 4 forward connections for each epoch, maximum interferogram length of 48 days for 12 474 day acquisition intervals, as at Domuyo. This means that even for the relatively high rate 475 persistent deformation at Domuyo, displacements in individual interferograms are commonly 476 < 1 cm, well below the level of atmospheric contributions (Figure 8b). Furthermore, the 477 standard LiCSAR network design is not optimised for regions with major seasonal variations 478 in phase coherence (e.g., snow cover). This results in loss of coherence in our test dataset, 479 relative to a network tailored to include only summer-summer interferograms (Lundgren et 480 al., 2020). 481

The interferograms we analysed also had a minimum 12 day interval as compared to 482 our training data which had a minimum of 6 day gap. Where there were large gaps between 483 use-able interferograms in the automatically processed data, epochs were skipped. The 484 sample interferograms shown in Figure 8 illustrate typical data gaps (circle), low coherence 485 with unwrapping errors (square), low SNR (inverted triangle and square) and an example 486 of a high SNR image where the Domuyo displacements are visible (triangle). Although our 487 training dataset did include regions of poor coherence, it did not include data gaps as shown 488 in Figure 8a (circle), so these are flagged as anomalies, leading to a high FPR. 489

Our method successfully identifies all 170 interferograms as containing anomalies (all 490 44 epochs flagged) in our test dataset - as expected for a steady displacement signal. It 491 performs well both for high and low SNR interferograms (Figure 8e), although large data 492 gaps and unwrapping errors result in false positives. These results demonstrate the trans-493 ferability of training using data from Northern Turkey to a completely different geographic 494 setting, with very different topography, vegetation, patterns and therefore interferogram 495 noise. Our estimation of the accumulated deformation from our automatic detection is 496 very consistent with displacements estimated using conventional analysis methods such as 497 'stacking' (compare Figure 8 b and d). 498

These results also demonstrate how our method can be used to process larger regions using a 'sliding window' approach, and stitching the results together to reconstruct the

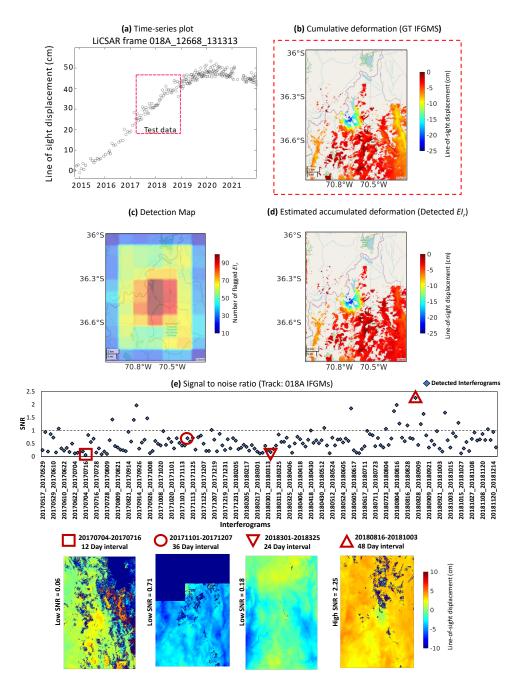


Figure 8. (a) Time series of displacements at Domuyo Volcano, made from LiCSBAS time series algorithm (Morishita et al., 2020) using LiCSAR interferograms (b) Cumulative deformation estimated from a stack of the displacement rates for all GT IFGMs, assuming a linear displacement rate. (c) Detection map showing flagged EI_r on a patch by patch basis (spatial and temporal sliding window for processing). (d) Our final estimation of the spatial structure of deformation of all detected epoch intervals. (e) (Top) SNR, as estimated as the ratio of peak displacement to interferogram variance with deforming area masked, for the processed region of interest for all interferograms. (Bottom) Interferograms with lower SNR are displayed in comparison to the one with higher SNR (red triangle). All of which are detected by the model.

deformation pattern. We extract the southwest corner of the automatically processed inter-501 ferograms centred on Domuyo and with dimensions of $\sim 13000 km \times 11000 km$ (1048×896 502 pixels). This region is further divided into 60 overlapping patches of size 256×256 and each 503 patch is independently passed through the model and detection framework. The data spans 504 from 17^{th} May 2017 to 14^{th} December 2018 (~ 1.5 years), which results in 10 data batches 505 with 44 epoch intervals for each patch location. All the flagged epoch intervals of each patch 506 are visualized on a heat map (detection map shown in figure 8 (c)). While the total number 507 of epoch intervals is 44 the overlapping nature of patches means that each pixel location is 508 covered by at least 4 patches, except the boundaries, hence epoch intervals EI_r are flagged 509 by multiple patches. Patch overlap also mitigates the impact of data gaps and low coherence 510 in the area of interest. A key benefit of using a CNN is translation invariance, which has 511 proved to be beneficial in this case and has resulted in spatially consistent output, despite 512 the fact that the whole area is processed on patch by patch basis in a sliding window scheme 513 and stitched together at the end. This property of our CNN is comes from the spatial over-514 lap in our training dataset. Our final prediction of total displacement spanning May 2017 515 to December 2018 is a union of all the detections for all patches (Figure 8d). 516

517 5 Discussion

While Deep Learning methods cannot replace detailed analysis of specific deformation 518 events (including tailored InSAR processing, atmospheric correction and time series analysis) 519 flagging of anomalies in very large datasets has the potential to be a powerful tool for finding 520 new tectonically significant signals. Traditional methods for analysing InSAR mitigate the 521 impact of low SNR in individual interferograms by methods including stacking (Pritchard 522 & Simons, 2004), construction of time series (Lundgren et al., 2001), (Rouet-Leduc et al., 523 2021), filtering (Dalaison & Jolivet, 2020), etc. Some of these methods, especially when 524 used in combination, are capable of detecting relatively low magnitude deformation (e.g., 525 <10 mm/yr). However, they commonly rely on deformation signals being either persistent, 526 high magnitude relative to noise, or having an a priori idea of signal pattern (e.g., parametric 527 fitting for expected co-seismic or inter-seismic deformation patterns). An advantage of 528 the anomaly detection methodology proposed here, is that it is similarly successful in the 529 detection of transient events that occur in a single epoch (Section 4.2) and long term, 530 persistent signals (Section 4.3). Here, we discuss (1) the performance of our iterative, 531 temporal self attention scheme and (2) suggest directions for the future developments for 532 anomaly detection in InSAR and (3) describe the potential of our method for application 533 to global datasets. 534

535

5.1 Performance of new network architecture

⁵³⁶Our new deep learning architecture and iterative training scheme for our model presents ⁵³⁷significant improvements to the protoype model in our previous work (ALADDIn (Shakeel ⁵³⁸et al., 2022)). The requirement of temporal consistency in particular improved our ability ⁵³⁹to accurately reconstruct the spatial structure of flagged displacement signals as assessed ⁵⁴⁰by comparison to both individual interferograms (Figure 7d) and stacked data (e.g., Figure ⁵⁴¹8b). The ability both to flag and reconstruct the spatial structure of deformation as part of ⁵⁴²a single pipeline is an additional advantage of our anomaly detection process (Section 2.3).

The flagging of deformation and reconstruction of its spatial structure is highly depen-543 dent on the quality of input data. For example, data gaps and unwrapping errors resulted 544 in many false positive detections in the Domuyo dataset, as can be seen in the non-zero 545 values for detection in the areas surrounding the Domuyo displacement signal (Figure 8c). 546 This makes the overall accuracy for our method in this location lower than it was in Turkey. 547 However, this is mitigated by the redundancy introduced by our 'sliding' patches (Section 548 5.2). SNR, estimated as ratio of peak displacement over the volcano to background variance 549 with volcanic areas masked, is also relatively low at Domuyo (Figure 8e). More than 90~%550

of the input interferograms have low SNR (as highlighted by a dashed line on Figure 8e), but the model successfully detects the anomaly even with SNR as low as 0.06.

553 5.2 Potential for global deformation flagging

Although our model is trained only on an ascending InSAR dataset from northern 554 Turkey, it is successful in flagging both the 2019 southern Turkey earthquake and the Do-555 muyo uplift in Argentina. This demonstrates that our approach does not necessarily require 556 tailored training data sets for settings with different atmospheric noise, although it is possi-557 ble that this might improve model performance. Our anomaly detection approach to InSAR 558 data exploits the redundancy in networks of interferograms to learn the relationship between 559 interferograms and the signals attributable to each epoch (differential data structure), and 560 is therefore not sensitive to the specific spatial and temporal properties of the background 561 noise (atmosphere and errors in orbit estimations). 562

As shown in Section 4.3, the relatively small patch size that we use in our model is 563 not an obstacle to detection of much longer wavelength deformation. In fact, using the 564 sliding window technique for processing large areas has proven to be advantageous because 565 anomalous intervals can be flagged by multiple patch locations (see Figure 8), or if missed 566 in one patch, can be flagged in others. This could be improved for processing large areas of 567 data by the development of a voting ensemble (machine learning model that combines the 568 predictions from multiple models) instead of taking a simple union for gathering the epoch 569 intervals. 570

The types of deformation detectable with our method are also strongly dependent on the resolution of the input dataset. LiCSAR processing is optimised for scientific study of very long wavelength, low magnitude interseismic signals, using multi-looking and some filtering to clean up the interferograms at the expense of spatial resolution (Morishita et al., 2020). They are therefore less appropriate for the detection of small-scale displacements such as anthropogenic or some volcanic signals.

577 5.3 Directions for new development

We found that the addition of synthetic training datasets did not significantly improve 578 the performance of our model. Initially, it was challenging to train similar network archi-579 tectures on synthetic data. The problem of model over-fitting very early in training time 580 hindered its learning. The network architectures are designed to cater for raw unwrapped 581 interferograms, the phase values of which varied across a wide range (for example from -300582 rad to 15 rad). However, the range of values in our synthetic dataset are smaller, and not 583 diverse as compared to raw data. This was a consequence of the estimation of parameters 584 using least square inversion and residual interferograms as explained in Section 3. In ad-585 dition, noise was not separately simulated and added in the data, resulting in lower data 586 diversity. A better approach may be to incorporate data augmentation techniques (Taylor 587 & Nitschke, 2018), instead of solely depending on synthetic training data. This would in-588 crease the number of data samples and also add diversity to the training set. For example, 589 descending frames could be augmented (as it also a variant of data that captures similar region but with different look angle) or synthetic data could be augmented with real data 591 to create one training set. 592

The key to a diverse and well-fitted model is generally hidden in its training data. A diverse dataset can lead to a model that could be re-used to be applied on wrapped or geocoded data through transfer learning. Once fully trained, the weights of the model can be re-used to initiate training on various data types. For example, we incorporated transfer learning and utilized the weights of ALADDIn (Shakeel et al., 2022) to train a Temporal self-attention model. Similarly, it could be fine-tuned on different data types to create a generalized model. Also, while preparing the data, introducing regions or temporal stamps with extreme atmospheric conditions would be helpful and reduce false positives. For example, it could be advantageous to use interferograms with winter images or snow in them or including regions near sea, river or lake.

The model developed in this study can be used further to build weakly supervised methods (Campanella et al., 2019). Such methods incorporate constrained and indirect sources of supervision to devise labels for large volumes of unlabelled data. The residuals created by the model predictions can be used as weak pixel-wise labels/masks for anomalies. This can lead to supervised anomalous instance segmentation by creating a global labelled dataset.

609 6 Conclusions

This work addresses two limitations of our previous prototype anomaly-detector for 610 InSAR data: (1) temporal inconsistency and (2) limited patch size. The development of 611 new architecture that incorporates temporal self-attention improves the performance of our 612 model so that it flags deformation of peak magnitude of a few cm and wavelength of a 613 few hundred metres with an overall accuracy of 80-90 %. We demonstrate that our model, 614 although trained on data in northern Turkey is successful in flagging displacements at an 615 Argentinian volcano, and that it is capable of detecting both transient (earthquake) and 616 persistent (volcano) deformation. We have shown that the architecture developed here has 617 important potential for anomaly detection, and believe that fruitful future developments to 618 improve its performance could include development of more diverse, realistic training data, 619 and testing against a wider variety of volcano-tectonic and other deformation sources. 620

⁶²¹ 7 Acknowledgments

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⁶²⁹ 8 Open Research

Sentinel-1 interferograms are used for training and evaluations of the models. Un-630 wrapped interferograms, including all of those used in this study, were processed auto-631 matically and can be downloaded from the open access LiCSAR hub (Lazecký et al., 2020) 632 https://comet.nerc.ac.uk/comet-lics-portal/. The deep learning models (ALADDIn 633 and Temporal self-attention (Anza Shakeel, 2022)) developed and tested in this study are 634 available at GitHub: https://github.com/AnzaShakeel/Deep-Learning-for-InSAR.git 635 via DOI: https://doi.org/10.5281/zenodo.7326911 .The machine learning platforms 636 used to develop the models presented here are Keras (Chollet et al., 2015) with Tensor-637 Flow (Abadi et al., 2015) as backend. 638

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