# On the measurement of Sdiff splitting caused by lowermost mantle anisotropy

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December 7, 2022

#### Abstract

Seismic anisotropy has been detected at many depths of the Earth, including its upper layers, the lowermost mantle, and the inner core. While upper mantle seismic anisotropy is relatively straightforward to resolve, lowermost mantle anisotropy has proven to be more complicated to measure. Due to their long, horizontal raypaths along the core-mantle boundary, S waves diffracted along the core-mantle boundary (Sdiff) are potentially strongly influenced by lowermost mantle anisotropy. Sdiff waves can be recorded over a large epicentral distance range and thus sample the lowermost mantle everywhere around the globe. Sdiff therefore represents a promising phase for studying lowermost mantle anisotropy; however, previous studies have pointed out some difficulties with the interpretation of differential SHdiff-SVdiff travel times in terms of seismic anisotropy. Here, we provide a new, comprehensive assessment of the usability of Sdiff waves to infer lowermost mantle anisotropy. Using both axisymmetric and fully 3D global wavefield simulations, we show that there are cases in which Sdiff can reliably detect and characterize deep mantle anisotropy when measuring traditional splitting parameters (as opposed to differential travel times). First, we analyze isotropic effects on Sdiff polarizations, including the influence of realistic velocity structure (such as 3D velocity heterogeneity and ultra-low velocity zones), the character of the lowermost mantle velocity gradient, mantle attenuation structure, and Earth's Coriolis force. Second, we evaluate effects of seismic anisotropy in both the upper and the lowermost mantle on SHdiff waves. In particular, we investigate how SHdiff waves are split by seismic anisotropy in the upper mantle near the source and how this anisotropic signature propagates to the receiver for a variety of lowermost mantle models. We demonstrate that, in particular and predictable cases, anisotropy leads to Sdiff splitting that can be clearly distinguished from other waveform effects. These results enable us to lay out a strategy for the analysis of Sdiff splitting due to anisotropy at the base of the mantle, which includes steps to help avoid potential pitfalls, with attention paid to the initial polarization of Sdiff and the influence of source-side anisotropy. We demonstrate our Sdiff splitting method using three earthquakes that occurred beneath the Celebes Sea, measured at many Transportable Array (TA) stations at a suitable epicentral distance. We resolve consistent and well-constrained Sdiff splitting parameters due to lowermost mantle anisotropy beneath the northeastern Pacific Ocean.

# On the measurement of $S_{diff}$ splitting caused by lowermost mantle anisotropy

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#### 4 Abstract

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Preprint submitted to Geophysical Journal International

November 1, 2022

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#### 34 the northeastern Pacific Ocean.

Keywords: Planetary interiors, Numerical modelling, Computational seismology, Seismic anisotropy, Wave propagation

#### 35 1. Introduction

Seismic anisotropy, or the directional dependence of seismic wave speeds, typically results from deformation in the Earth (e.g., Long and Becker, 2010). Seismic anisotropy has been 37 identified in the crust (e.g., Barruol and Kern, 1996; Erdman et al., 2013), the upper mantle 38 (e.g., Silver, 1996; Chang et al., 2014), the mantle transition zone (e.g., Yuan and Beghein, 39 2014; Chang and Ferreira, 2019) and Earth's inner core (e.g., Romanowicz et al., 2016; 40 Frost et al., 2021). The bulk of the lower mantle is largely isotropic (e.g., Panning and 41 Romanowicz, 2006), but some studies have suggested seismic anisotropy in the uppermost 42 lower mantle, particularly in subduction zones (e.g., Foley and Long, 2011; Lynner and Long, 43 2015; Mohiuddin et al., 2015; Ferreira et al., 2019). Finally, the bottom 200-300 km of the 44 mantle, in the following synonymously referred to as D'', has been shown to be anisotropic 45 in many places (e.g., Lay et al., 1998; Garnero et al., 2004; Wookey et al., 2005; Nowacki et al., 2010; Creasy et al., 2017; Wolf et al., 2019; Lutz et al., 2020; Wolf and Long, 2022). 47 A main cause for seismic anisotropy is the preferential alignment of intrinsically anisotropic 48 minerals due to mantle flow (e.g., Nowacki et al., 2011; Karato et al., 2008). 49

As with the upper mantle, measurements of lowermost mantle anisotropy can poten-50 tially resolve deep mantle deformation and map patterns of flow at the base of the mantle. 51 In practice, however, such inferences remain challenging to make. These difficulties reflect 52 shortcomings or assumptions in commonly used measurements methods (e.g., Nowacki and 53 Wookey, 2016; Wolf et al., 2022a), limitations in data coverage (e.g., Ford et al., 2015; Creasy et al., 2017; Wolf et al., 2019), and/or uncertainties about realistic lowermost man-55 tle elasticity scenarios (e.g., Nowacki et al., 2011; Creasy et al., 2020). For instance, even with perfect knowledge about potential elastic tensors describing lowermost mantle mate-57 rials, seismic anisotropy must generally be measured from multiple directions to uniquely 58 constrain deformation and mineralogy (e.g., Nowacki et al., 2011; Creasy et al., 2019). The 59 deep mantle is likely dominantly composed of bridgmanite or its high-pressure polymorph 60 post-perovskite, along with ferropericlase; the single-crystal elasticity and dominant slip 61 systems of the minerals at the relevant pressure-temperature conditions are not precisely 62 known (e.g., Creasy et al., 2020). Therefore, it is not completely straightforward to in-63 fer deformation geometry from measured shear wave splitting parameters (fast polarization directions and delay times). One strategy is to assume a plausible lowermost mantle com-65 position based on the likely temperature conditions and seismic velocities of a certain region

67 and carry out forward modelling to make predictions that can be compared to observations

<sup>68</sup> (e.g., Nowacki et al., 2010; Ford et al., 2015; Creasy et al., 2021; Wolf and Long, 2022).

Recent progress in full-wave modelling of seismic anisotropy with arbitrary geometries in 69 the lowermost mantle has led to an improved understanding of the shortcomings inherent in 70 commonly used shear wave splitting measurement techniques (Nowacki and Wookey, 2016; 71 Tesoniero et al., 2020; Wolf et al., 2022a; 2022b), which are typically based on ray theory 72 (a high-frequency approximation to the wave equation). However, not all of the difficulties 73 have successfully been resolved, and challenges remain with commonly used measurement 74 methods such as differential S-ScS and SKS-SKKS splitting. Thus, it is important to ex-75 plore alternatives to the commonly used seismic phases for measuring D'' anisotropy, and 76 to validate them using full-wave simulations rather than relying solely on ray-theoretical 77 assumptions. A viable candidate phase for D'' anisotropy measurements is the  $S_{diff}$  phase, 78 because of its particularly long and horizontal raypaths along the CMB (Figure 1a), along 79 which it can accumulate splitting. However, extracting information about deep mantle an-80 isotropy from  $S_{diff}$  waveforms is non-trivial. This is partly because  $S_{diff}$  waves are generally 81 neither perfectly SH nor SV polarized in absence of anisotropy; furthermore,  $SH_{diff}$  and 82  $SV_{diff}$  can accumulate a time shift due to isotropic structure (e.g., Komatitsch et al., 2010; 83 Borgeaud et al.; 2016; Parisi et al., 2018), which can potentially be misinterpreted as shear 84 wave splitting. Further, it must be ensured that phase interference is not misinterpreted 85 as splitting (Komatitsch et al., 2010; Borgeaud et al.; 2016; Parisi et al., 2018). Another challenge is that the splitting signature of  $S_{\text{diff}}$  reflects the integrated effects of seismic an-87 isotropy along the raypath, including the source and receiver side upper mantle as well as 88 D″. 89

Despite these challenges, the interpretation of  $S_{\text{diff}}$  splitting in terms of lowermost mantle 90 anisotropy has a substantial history (e.g., Vinnik et al., 1989; 1995; 1998a; 1998b; Garnero 91 and Lay, 1997; Ritsema et al., 1998; Fouch et al., 2001). In some early papers, S<sub>diff</sub> splitting 92 was compared to the splitting of SK(K)S waves to assess the upper mantle anisotropy 93 contribution to the waveforms, often under the assumption that  $SV_{diff}$  should have died 94 off after travelling a certain epicentral distance, typically 110° (e.g., Vinnik et al., 1989). 95 Alternatively, some studies have focused on the time delay between  $SH_{diff}$  and  $SV_{diff}$  without explicitly measuring splitting parameters (e.g., Ritsema et al., 1998; Fouch et al., 2001). 97 While  $S_{diff}$  waves are in fact often primarily SH-polarized, recent work has shown that the 98 assumption that  $SV_{diff}$  has completely died off at 110° distance cannot always be made 99 (Komatitsch et al., 2010; Borgeaud et al., 2016). It has also been shown that the SH and 100 SV components of S and S<sub>diff</sub> (Komatitsch et al., 2010; Borgeaud et al., 2016; Parisi et al., 101 2018) can accumulate an apparent time-shift that can potentially mimic splitting, even 102

for isotropic Earth models. As a result, it has recently become less common to measure D'' seismic anisotropy using  $S_{diff}$ . A few exceptions (Cottaar and Romanowicz, 2013; Wolf and Long, 2022) have typically relied on specific arguments about likely initial polarizations of the waves under study.

In this study, we provide a new and comprehensive examination of the suitability of  $S_{diff}$ 107 splitting measurements to infer lowermost mantle anisotropy using global wavefield modeling 108 tools. We analyze potential pitfalls in  $S_{diff}$  splitting analysis, and develop strategies to 109 avoid them. For this purpose, we complement previous studies from Tesoniero et al. (2020) 110 and Wolf et al. (2022a,b), who have analyzed the accuracy of commonly used shear-wave 111 splitting techniques for D" anisotropy studies with a focus on SK(K)S and S/ScS. We also 112 complement a recent study by Creasy et al. (in review), who investigated the effects of the 113 Earth's Coriolis force on SK(K)S polarizations. We undertake a similar approach as in these 114 previous studies, using the AxiSEM3D (Leng et al., 2016, 2019) and SPECFEM3D\_GLOBE 115 (Komatitsch and Tromp, 2002a, 2002b) software to model global wave propagation. 116

In contrast to previous studies (Komatitsch et al., 2010; Borgeaud et al., 2016; Parisi 117 et al., 2018) that used global wavefield simulations to examine  $S_{diff}$  waveform behavior, we 118 do not explicitly investigate differential  $SH_{diff}$ -SV<sub>diff</sub> travel times. Rather, we analyze how 119  $S_{diff}$  phases can be used infer robust shear-wave splitting parameters (time delay, fast-axis 120 polarization direction, and splitting intensity) associated with lowermost mantle anisotropy. 121 Unlike the measurement of differential  $SH_{diff}$ - $SV_{diff}$  travel times, such an analysis includes 122 strict requirements for the shape of the waveform. Whenever we use the term  $S_{diff}$ -splitting 123 in the following, we refer to the explicit measurement of splitting parameters and not to the 124 analysis of time delays. 125

We conduct a suite of global wavefield simulations with increasing complexity to assess 126 the conditions under which  $S_{diff}$  waves are suitable for shear wave splitting measurements. 127 In the first set of simulations, we analyse the effects of realistic isotropic velocity struc-128 ture on  $S_{diff}$  polarizations. In particular, we analyze the assumptions and conditions when 129 SV<sub>diff</sub> and SH<sub>diff</sub> die off. While it has been shown that assumptions cannot always made 130 (Komatitsch et al., 2010), no study so far has assessed these assumptions comprehensively. 131 We continue with simulations investigating the effects of realistic 3D velocity structure and 132 Earth's Coriolis force on  $S_{diff}$  polarizations. In a second set of simulations, we investigate 133 the effect of seismic anisotropy on  $SH_{diff}$  waves in detail. We examine the conditions un-134 der which splitting caused by source-side anisotropy could potentially be misdiagnosed as 135 showing evidence for lowermost mantle anisotropy. Furthermore, we analyze the limits of 136 resolution for the cases in which  $S_{diff}$  splitting can indeed be reliably attributed to lower-137 most mantle anisotropy. This second set of simulations reveals how exactly D" anisotropy 138

expresses itself in  $S_{diff}$  waveforms, particularly for cases in which there is also an upper mantle contribution. Finally, we use the insights gained for our  $S_{diff}$ -wavefield simulations to outline a novel strategy for using  $S_{diff}$  splitting measurements to reliably infer deep mantle anisotropy. We use these insights to conduct a thorough splitting analysis for three deep earthquakes that occurred in the Celebes Sea in 2009 and 2010, for which  $S_{diff}$  waves, recorded at a large swath of stations across USArray, sample the lowermost mantle beneath the northeastern Pacific Ocean.

#### 146 2. Methods

#### 147 2.1. Full-wave simulations

AxiSEM3D and SPECFEM3D\_GLOBE are two commonly used tools to conduct global 148 wavefield simulations. In this work, we primarily use AxiSEM3D due to its computational 149 efficiency, which allows us to calculate synthetic seismograms down to periods that are 150 commonly used for shear wave splitting measurements  $(\sim 5 s)$ . For these calculations, we 151 extend the work of Tesoniero et al. (2020) and Wolf et al. (2022a,b), who have established 152 AxiSEM3D as a suitable tool to conduct full-wave simulations for models that include 153 anisotropy of arbitrary symmetry. To investigate the effects of Earth's Coriolis force, we 154 calculate seismograms down to  $\sim 9 \,\mathrm{s}$  using SPECFEM3D\_GLOBE, extending work from 155 Creasy et al. (in review). The Coriolis force effect on body waves is frequency dependent, 156 but because the period we are using in our SPECFEM3D\_GLOBE simulations (9s) is much 157 smaller than the period of Earth's rotation, the results would be unaffected if we were to 158 calculate synthetics for lower periods (Snieder et al., 2016). SPECFEM3D\_GLOBE gives 159 the user the option to calculate synthetics with and without considering Earth's rotation. 160

The initial input model for our numerical simulations with AxiSEM3D and SPECFEM3D\_GLOBE 161 is isotropic PREM (Dziewonski and Anderson, 1981). All simulations include attenuation 162 and ellipticity. Building on this simple scenario, we move towards increasingly complex 163 models in our AxiSEM3D simulations. To do so, we replace the initial PREM input model 164 at certain depths with different or more complex structure. Specifically, we first replace low-165 ermost mantle properties (e.g, velocity, velocity-gradient,  $Q_{\mu}$ ) in the context of an isotropic 166 Earth to investigate the influence of various factors on how SH and SV amplitudes die off as 167 a function of distance for diffracted waves. We also run simulations for a model that replaces 168 PREM with 3D tomographic models to assess the influence of 3D velocity heterogeneity on 169  $S_{diff}$  polarizations. Next, we shift our attention to simulations that include seismic aniso-170 tropy, in particular source-side and lowermost mantle anisotropy, for background models 171 based on both PREM and PREM+3D tomographic model. 172

To identify the effects of Earth's rotation on  $S_{diff}$  polarizations, we conduct simulations 173 with SPECFEM3D\_GLOBE. In this solver, the globe is divided into six chunks; we apply 480 174 spectral elements along one side of each chunk at the surface, resolving down to a minimum 175 period of  $\sim 9$  s during simulations. We conduct two simulations including gravity (Cowling 176 approximation) and the ocean load (Komatitsch and Tromp, 2002b), one including Earth's 177 rotation and the other excluding it. The source, at 616 km depth, is selected from the Global 178 Centroid-Moment-Tensor catalogue (Ekström et al., 2012; event name: 201004112208A), 179 but we change the source location to  $25^{\circ}$ S and  $66^{\circ}$ W. This event is selected so that the 180 north-south propagation directions are far from the nodal planes of the source, to amplify 181 the rotation effect (Creasy et al., in review). More than 1,000 pseudo receivers are placed 182 across the global mesh with  $8^{\circ}$  - spacing. Waveforms from the simulations are bandpass 183 filtered to retain energy between 10 - 50 s before processing. 184

An example of a typical source-receiver configuration used for our synthetic simulations 185 with AxiSEM3D is shown in Figure 1b. Here, we place our source and receivers along the 186 equator. The source is chosen to be at longitude  $-90^{\circ}$  and the receivers are placed along 187 the equator at epicentral distances between  $103 - 130^{\circ}$ . For this scenario, we choose a focal 188 depth of 500 km and a moment tensor whose only non-zero component is  $M_{tp}$  for perfect 189 initial SH polarization. The same is done for perfect initial SV polarization (keeping  $M_{tt}$  as 190 the only non-zero component). The details of the moment tensor are only relevant insofar 191 as they affect the initial polarization of the wave; we choose these simple moment tensor 192 scenarios because they are straightforward to understand and interpret. An additional 193 source-receiver configuration that we use is an equivalent scenario along the zero meridian 194 with the source at the north pole and a focal depth of  $0 \,\mathrm{km}$ . These two configurations 195 are arbitrary, but they allow us to build on results from an initial benchmarking exercise 196 without having to rerun computationally expensive simulations for another source-receiver 197 setup. We use the first configuration (shown in Figure 1b) for all the isotropic AxiSEM3D 198 simulations (Section 3) and the alternative configuration for all simulations that include 199 lowermost mantle anisotropy (Section 4). 200

For simulations that include anisotropy near the source, we incorporate a 200 km thick 201 layer with horizontally transversely isotropic (HTI) symmetry. We calculate appropriate 202 elastic tensors using MSAT (Walker and Wookey, 2012), creating an elastic tensor at each 203 depth increment whose isotropic average matches isotropic PREM velocities. We tune the 204 elastic tensor using MSAT to have an anisotropic strength of either 2% or 4%. We incorpo-205 rate a source-side anisotropy layer at a depth range of  $30 - 230 \,\mathrm{km}$  for simulations with a 206 source depth of 0 km, and at a depth range of 500 - 700 km for a focal depth of 500 km. In 207 both cases the raypath through the layer is sufficiently vertical that the effects of focal depth 208

and anisotropic layer depth on the observed splitting are minor. Whenever we include upper 209 mantle anisotropy, we make sure that the HTI tensor is rotated such that its fast direction 210 is at an angle of  $45^{\circ}$  with respect to the polarization of the wave, which maximizes splitting. 211 For the lowermost mantle, we use an elastic tensor based on textured post-perovskite 212 (Ppv) from the elastic tensor library of Creasy et al. (2020), for simple shear with 100% 213 strain. This tensor incorporates estimates of single-crystal elasticity from Stackhouse et al. 214 (2005) and is based on a model of texture development using a visco-plastic self-consistent 215 modeling approach (Creasy et al., 2020). We rotate this tensor appropriately to obtain 216 strong  $S_{diff}$  splitting, following Wolf et al. (2022b). For the cases for which we measure 217 splitting intensities (Section 4), we mix this Ppv tensor with its isotropic equivalent (using 218 MSAT) to obtain an anisotropic strength that is only 1/3 of the original tensor. This allows 219 us to obtain more realistic splitting intensities ( $\sim$ 1; Section 2.2) at the receiver when using 220 a global, uniform layer of anisotropy. In the real Earth, of course, some regions of D'' may 221 be strongly anisotropic while others are isotropic. We emphasize that while we focus on a 222 Ppv anisotropy scenario in these simulations, our conclusions are more general and do not 223 depend on the details a certain elasticity scenario. Unless specified otherwise, the thickness 224 of the anisotropic basal mantle layer that we incorporate into our simulations is 150 km, 225 following previous work (Wolf et al., 2022a; 2022b). 226

#### 227 2.2. Shear wave splitting measurements

A shear wave travelling through an anisotropic medium will split into two quasi-S wave 228 components, one fast and one slow (e.g., Silver and Chan, 1991). These quasi-S waves will 229 thus accumulate a time delay with respect to each other, usually referred to as  $\delta t$ . The fast 230 direction of the anisotropic material is inferred by measuring the fast polarization direction 231 of the wave, called  $\phi$ . The fast polarization direction,  $\phi$ , is usually measured as a (clockwise) 232 azimuth from the north. In this study, we also use  $\phi'$ , which denotes the fast polarization 233 direction measured clockwise from the backazimuthal direction (meaning that  $\phi$  is identical 234 to  $\phi'$  if the backazimuth is 0°; Nowacki et al., 2010). Another quantity that is very useful for 235 studies of seismic anisotropy (in part due to its robustness in case of noise or weak splitting) 236 is the splitting intensity, in the following abbreviated as SI (Chevrot, 2000). The typical 237 definition of SI (for initially SV polarized waves) is 238

$$SI_{SV} = -2\frac{T(t)R'(t)}{|R'(t)|^2} \approx \delta t \sin(2(\alpha - \phi)) ,$$
 (1)

with T(t) denoting the transverse component, R'(t) the time derivative of the radial component,  $\delta t$  the time lag between the fast and slow travelling quasi S-waves, and  $\alpha$  the polarization direction of the incoming wave (equivalent to the backazimuth for SKS waves following their exit from the core). Thus, SI values are large if the transverse component resembles the radial component time derivative (which is true in the case of splitting; Silver and Chan, 1991; Chevrot, 2000) and has a high amplitude. The definition in Equation (1) is usually used because splitting measurements are often made on \*KS phases that are initially SV polarized due to the P-to-SV conversion at the CMB. For SH<sub>diff</sub> waves, we will use an alternate definition of SI:

$$SI_{SH} = -2\frac{R(t)T'(t)}{|T'(t)|^2} , \qquad (2)$$

where T'(t) denotes the transverse component time derivative. For these waves, when SH<sub>diff</sub> undergoes splitting and some energy is partitioned into SV<sub>diff</sub>, the transverse component time derivative will have the shape of the radial component.

We bandpass-filter our synthetic and real data before measuring splitting, typically re-251 taining periods between 8-25 s (for the assessment of Coriolis effects we instead use 10-25 s). 252 We conduct our splitting measurements on both synthetic and real data using a modified 253 version of the MATLAB-based graphical user interface SplitRacer (Reiss and Rümpker, 254 2017; Reiss et al., 2019). This version of SplitRacer retrieves the splitting parameters ( $\phi$ , 255  $\delta t$ ) using the transverse energy minimization approach (Silver and Chan, 1991), paired with 256 the corrected error determination of Walsh et al. (2013); additionally, this version measures 257 the splitting intensity. We modified SplitRacer slightly for this study, measuring  $\phi'$  instead 258 of  $\phi$ , thus transforming  $\phi$  into the ray reference frame. We also switched the transverse 259 and radial components to estimate  $S_{diff}$  splitting. We call the fast polarization direction 260 obtained this way  $\phi''$ , which equals  $90^\circ - \phi'$ . This direction  $\phi''$  appears on many figures but 261 will also always be translated into the  $\phi'$  coordinate frame. 262

#### $_{263}$ 3. Isotropic effects on $S_{diff}$ waveforms

#### $_{264}$ 3.1. Influence of various lowermost mantle properties on $S_{diff}$ amplitudes

First, we investigate the influence that different isotropic lowermost mantle properties 265 have on  $S_{diff}$  amplitudes, specifically on how  $S_{diff}$  amplitudes decrease as a function of dis-266 tance in an isotropic Earth. Doornbos and Mondt (1979) and Komatitsch et al. (2010) 26 have previously shown how  $S_{diff}$  amplitudes decrease with distance, and that the relative 268 SV/SH amplitude ratio decrease depends on lowermost mantle properties. Here, we extend 269 this work and systematically examine the influence of a realistic range of lowermost mantle 270 properties on the amplitude decay with distance of  $SH_{diff}$  and  $SV_{diff}$ . Our motivation is to 271 identify whether it can be assumed, for different lowermost mantle structure and epicentral 272 distance ranges, that  $SV_{diff}$  has died off while  $SH_{diff}$  has not. This assumption is important 273

for Sdiff splitting analyses, as many studies presume that  $SH_{diff}$  polarization energy dominates the Sdiff signal, due to the assumed die-off of  $SV_{diff}$  polarization energy by a particular distance (e.g., Vinnik et al., 1989). While this assumption has been shown to be inadequate in some cases (Komatitsch et al., 2010; Borgeaud et al., 2016), it may be justified for some combinations of lowermost mantle conditions, which we interrogate here.

We show synthetic seismograms for the three scenarios shown in Figure 2. Scenario 1 incorporates isotropic PREM and for scenarios 2 and 3, lowermost mantle velocities are decreased or increased, respectively. In the Supplementary Information, we additionally show some scenarios with different lowermost mantle velocity gradients (Figure S1) and a changed lowermost mantle shear wave attenuation (Figure S2).

The results for scenario 1 (isotropic PREM) are shown in Figure 3 for different initial 284 polarizations of the  $S_{diff}$  waves. We focus, in particular, on how radial and transverse am-285 plitudes decrease as a function of distance. We observe little or no interfering energy from 286 other phases in the transverse component record sections for the entire distance range, al-287 though for SV there is some non-S<sub>diff</sub> energy for larger distances. While this SV energy does 288 not correspond to any standard phase, we speculate that it comes from reflecting energy in 289 the upper layers of the PREM input model, a phenomenon that has been observed before 290 for ScS (Wolf et al., 2022b). Both SV and SH amplitudes are significant at distances of 291  $130^{\circ}$ , although SV<sub>diff</sub> appears to die off slightly faster than SH<sub>diff</sub>. This simple simulation 292 reinforces previous findings (Komatitsch et al., 2010; Borgeaud et al., 2016) that it is gener-293 ally incorrect to assume that for an  $S_{diff}$  wave with arbitrary initial polarization, the initial 294  $SV_{diff}$  energy has died off at a particular distance, while  $SH_{diff}$  has not. We next extend 295 on this scenario and examine how particular aspects of lowermost mantle structure affect 296 SH<sub>diff</sub> and SV<sub>diff</sub> amplitudes. 297

We investigate the influence of reasonable velocity deviations (e.g., Simmons et al., 2010; 298 French and Romanowicz, 2014) from PREM-like velocities, still in the context of 1D velocity 299 profiles. We assume typical deviations of  $\sim\pm\,2\,\%$  for LLVP regions and regions with higher 300 velocities dominated by slab remnants, respectively. To have maximum radial and transverse 301 amplitudes for visualization, we conduct two different end-member simulations, for initially 302 solely SH and solely SV polarized  $S_{diff}$  waves, respectively. The waveforms for simulations 303 that incorporate such a change in lowermost mantle velocity are displayed in record sections 304 in Figure 4, which uses similar plotting conventions as Figure 3. When velocities are higher 305 than PREM,  $SH_{diff}$  and  $SV_{diff}$  amplitudes decrease similarly as a function of distance as 306 for PREM. When velocities are lower than PREM, amplitudes decrease more slowly. While 307 this is a general trend for both  $SH_{diff}$  and  $SV_{diff}$ , we find that  $SV_{diff}$  energy dies off faster 308 than SH<sub>diff</sub> for higher velocities, but behaves similarly as a function of distance for lower 309

velocities (Figure 4). This implies that the assumption that initial  $SV_{diff}$  energy has died off 310 at any particular distance, while SH<sub>diff</sub> has not, will be more suitable (but still not perfect) 311 for faster than average regions in the lowermost mantle. The details of how  $SH_{diff}$  and 312  $SV_{diff}$  die off, however, do not only depend on absolute lowermost mantle velocities but also 313 on the velocity gradient (Supplementary Figure S1). In Figure S1, we compare scenarios 314 that incorporate a velocity jump with linear velocity gradients at the base of the mantle. 315 For higher and lower velocities than average at the base of the mantle, a linear velocity 316 gradient will lead to a sharper amplitude decrease with distance than a velocity jump. 317

We next show that the mantle shear quality factor can have an influence on the amplitude 318 decrease of SH- and SV<sub>diff</sub> waves.  $Q_{\mu}$  is usually assumed to have a value between 200 and 319 400 in radially symmetric models (e.g., Dziewonski and Anderson, 1981; Lawrence and 320 Wysession, 2006), although there may be a substantial lateral variability (e.g., Romanowicz 321 and Mitchell, 2007). To account for this, we test two relatively extreme cases with different 322  $Q_{\mu}$  values ( $Q_{\mu} = 75$  and  $Q_{\mu} = 1000$ ), leaving  $Q_{\kappa}$  unchanged. The results for both cases 323 are shown in Supplementary Figure S2. Changing  $Q_{\mu}$  appears to have a larger influence on 324  $SV_{diff}$  than  $SH_{diff}$ . While the details likely reflect the specific details of the implemented 325  $Q_{\mu}$  model, in general this implies that the propagation of initial SV<sub>diff</sub> energy will not only 326 depend on the details of the lowermost mantle velocity and velocity gradient, but also on 327  $Q_{\mu}$ . This agrees with results from Borgeaud et al. (2016), who investigated the dependence 328 of apparent  $SH_{diff}$  -SV<sub>diff</sub> differential times on lowermost mantle  $Q_{\mu}$  structure in detail. 329

These simulations show that, although  $SV_{diff}$  dies off faster than  $SH_{diff}$  in most cases, 330 a blanket assumption that  $SV_{diff}$  dies off at a specific epicentral distance is unwarranted. 331 This is important because if SV energy is present for  $S_{\text{diff}}$  in absence of anisotropy, then 332 isotropic waveform effects can potentially be mistaken for splitting, even for isotropic Earth 333 models. For instance, Komatitsch et al. (2010), Borgeaud et al. (2016) and Parisi et al. 334 (2018) showed that isotropic structure can lead to a relative time-shift between SH<sub>diff</sub> and 335  $SV_{diff}$  components (although the authors did not explicitly measure splitting). Our results 336 imply that S<sub>diff</sub> waves can be used for shear wave splitting measurements only if it can 337 be established that, for a given event and raypath and in absence of lowermost mantle 338 anisotropy, the SV<sub>diff</sub> component is expected to be negligible. This means that whether a 339 given measurement is usable will depend on the initial polarization of the wave as well as the 340 lowermost mantle structure. This criterion can be evaluated through synthetic modelling. 341 In practice, many  $S_{diff}$  waves will in fact be suitable for splitting analysis. Therefore, direct 342 S and ScS become asymptotic as they eventually become the same wave at the diffraction 343 distance. Their SV polarities, however, are opposite, resulting in destructive interference; 344 depending on the velocity structure, this can result in a rapidly diminishing  $SV_{diff}$  amplitude 345

346 with distance.

# $_{347}$ 3.2. Influence of realistic 3D velocity structure on the polarizations of $S_{diff}$ waves

We have shown that  $S_{diff}$  waves with a significant initial SV component (that is, SV 348 energy that does not result from splitting) cannot be reliably used for shear wave splitting 349 measurements (Section 3.1). Therefore, from here on we will focus our attention on purely 350 SH-polarized S<sub>diff</sub> waves. In particular, we next investigate whether initially SH polarized 351 waves can be influenced by effects other than anisotropy, such that some energy is partitioned 352 into SV on the radial component, potentially mimicking splitting. We first investigate 353 the effects of realistic 3D heterogeneity on  $S_{diff}$  polarizations. We do so by using the 3D 354 tomography model GyPSuM (Simmons et al., 2010) in the mantle instead of our initial 355 isotropic PREM input model; we retain PREM structure for the crust and the core. We 356 place a source with a focal depth of  $0 \,\mathrm{km}$  at the north pole and the receivers every  $20^{\circ}$  along 357 a specific longitude. We repeat this every  $20^{\circ}$  of longitude, starting at the zero meridian, for 358 distances  $103 - 130^{\circ}$ . These waveforms are shown in Figure 5a for a representative example 359 along longitude  $60^{\circ}$ . We see that almost no energy arrives on the radial component and 360 the measured splitting intensities are null or very close to it (|SI| < 0.3), consistent with 361 a lack of splitting, for all measurements (Figure 5c). Receivers at other longitudes yield 362 similar results. These simulations confirm that we cannot expect a significant redistribution 363 of energy from the transverse to radial components (potentially mimicking splitting) when 364 incorporating a realistic representative 3D tomographic model into our simulations. We 365 repeat this exercise using the 3D tomography model S40RTS (Ritsema et al., 2011), which 366 yields similar results in terms of shear wave polarizations (Figure S3). 367

We additionally conduct slightly more complicated simulations using the same GvPSuM-368 based input model and also including a global 20 km thick basal mantle layer of reduced 369 shear velocities, approximating a global ultra-low velocity zone (ULVZ). ULVZs are thin 370 features at the base of the mantle that are characterized by shear wave velocities that 371 are reduced by some tens of per cent compared to the surrounding mantle (e.g., Yu and 372 Garnero, 2018). A global ULVZ has not been observed; this simplified scenario may, however, 373 be a good approximation for zones with widespread ULVZs. We implement S velocity 374 reductions of 30% compared to PREM (decreasing P velocities by 10% and keeping density 375 constant) and conduct simulations for an initially SH polarized  $S_{diff}$  wave with stations 376 placed along the zero meridian. Waveforms are shown in Figure 5b as a function of distance 377 and the corresponding splitting intensities are displayed in Figure 5d. We find that SI-378 values (representing the amount of radial component energy) are null (|SI| < |0.3|) for all 379 distances. 380

 $_{381}$  We conclude that, while  $SH_{diff}$  and  $SV_{diff}$  waves may indeed accumulate a relative time

<sup>382</sup> shift in isotropic structure (Komatitsch et al., 2010; Borgeaud et al., 2016; Parisi et al., 2018), <sup>383</sup> no substantial redistribution of energy from initially SH-polarized  $S_{diff}$  waves to  $SV_{diff}$  can be <sup>384</sup> expected in realistic 3D tomographic models or through the influence of ULVZs. In cases for <sup>385</sup> which a slight energy redistribution happens, the waveforms will be strongly distorted from <sup>386</sup> the pulse shape predicted for shear wave splitting and, in practice, would not be mistaken <sup>387</sup> for true splitting.

## 338 3.3. Polarization anomalies caused by Earth's Coriolis effect

We next evaluate the influence of Earth's Coriolis effect on S<sub>diff</sub> waveforms using SPECFEM3D\_GLOBE. 389 The Earth's Coriolis effect influences all seismic wave propagation, but it has the most no-390 ticeable effect on normal modes (Backus and Gilbert, 1961; Masters et al., 1983; Dahlen and 391 Tromp, 1998) and surface waves (e.g., Park and Gilbert, 1986; Tromp, 1994; Snieder and 392 Sens-Schönfelder, 2021). Body waves, particularly shear waves, can be modestly affected 393 (Schoenberg and Censor, 1973; Snieder et al., 2016). As a shear wave propagates through 394 a rotating body, there is a slow rotation of the polarization of shear waves; in contrast, the 395 orientation of wavefronts is not affected by Earth's rotation. The exact change in the polar-396 ization of a shear wave will depend on travel time duration, event location, and the raypath 397 relative to Earth's rotation axis, as outlined by Snieder et al. (2016). Here, we determine 398 the deviations of  $S_{\text{diff}}$  from its initial polarization due to the Coriolis effect by comparing 399 two simulations with the same event-receiver setup, for which one simulation excludes and 400 the other includes Earth's rotation (Figure 6). 401

We find that  $S_{diff}$  polarization anomalies follow the expected pattern of polarization 402 change due to the Coriolis effect, in which a shear wave's polarization follows a negative 403 cosine curve (Snieder et al., 2016; Creasy et al., in review). Sdiff waves propagating along 404 Earth's rotation axis (north-south) from the event show waveform changes, mainly on the 405 radial component (Figure 6c). S<sub>diff</sub> waves propagating nearly east-west (that is, perpen-406 dicular to Earth's rotation axis) produce waveforms for both simulations (rotating and 407 non-rotating) that are completely identical (Figure 6d). Overall, the differences in wave-408 form shapes between the two simulations for the north-south path is small (the amplitudes 409 of the radial component must be doubled to visualize the effect; Figure 6). The polarization 410 change due to Earth's rotation is only  $1-3^{\circ}$  for S<sub>diff</sub> waves, which is generally insignif-411 icant considering that error estimates on fast polarization directions are usually at least 412  $\pm(10-15^{\circ})$  for splitting measurements (e.g., Long and Silver, 2009). Furthermore, the 413 pattern of polarization anomalies can be easily predicted using a raytracing approach and 414 the effect of Coriolis-induced polarization anomalies can be corrected. Other waves such as 415 direct S are more strongly affected by Earth's rotation, with polarization anomalies up to 416 almost  $7^{\circ}$  (Creasy et al., in review). 417

# 418 4. Anisotropic effects on SH<sub>diff</sub> waveforms

#### 419 4.1. Influence of lowermost mantle anisotropy on $S_{diff}$ amplitudes

We now focus on the influence that lowermost mantle anisotropy has on  $SH_{diff}$  and  $SV_{diff}$ amplitudes for initially SH-polarized  $S_{diff}$  waves. To do so, we run simulations for a model that replaces the bottom 150 km of the mantle of our initial isotropic PREM input model with Ppv anisotropy, as described in Section 2.1, initially using a global layer of anisotropy. The raypath of  $S_{diff}$  along the CMB can be very long; therefore, we also investigate how the anisotropic signature is influenced by laterally heterogeneous seismic anisotropy, by running models with finite anisotropic regions.

We perform simulations for three different cases. First, we incorporate a global layer 427 of Ppv anisotropy at the base of the mantle (first row in Figure 7); then, we incorporate 428 Ppv anisotropy in the lowermost mantle up to a distance of  $65^{\circ}$  from the source (second 429 row); third, we incorporate Ppv anisotropy for epicentral distances greater than  $65^{\circ}$  from 430 the source (third row). For the first case (Figure 7, first row), for which the anisotropic 431 layer is global,  $SH_{diff}$  is clearly split, with  $SV_{diff}$  energy for the whole distance range. We 432 also observe that for this first case,  $SH_{diff}$  and  $SV_{diff}$  amplitudes decrease similarly as a 433 function of distance, meaning that the relative amount of energy split to  $SV_{diff}$  will reflect 434 the lowermost mantle anisotropy, independent of the size of the anisotropic region. In the 435 second case (Figure 7, second row), we observe splitting (with some energy partitioned 436 to  $SV_{diff}$ ) at closer distances (< 115°), because lowermost mantle anisotropy is only being 437 sampled at the beginning of the raypath along the CMB. SV<sub>diff</sub> energy then decreases quickly 438 as a function of distance and has largely died off at an epicentral distance of  $130^{\circ}$ , relative 439 to  $SH_{diff}$ . For the third scenario (Figure 7, third row), at close distances  $S_{diff}$  waves do not 440 sample seismic anisotropy along the CMB but do sample anisotropy after they leave the 441 CMB on their (long) path through the D" layer. At slightly larger distances ( $\sim 115^{\circ}$ ), they 442 start sampling the anisotropy along the CMB, leading to significant splitting. 443

These results have some important implications regarding SH<sub>diff</sub> splitting measurements performed on real data. In the absence of upper mantle anisotropy, our simulations demonstrate the following:

• Seismic anisotropy in the lowermost mantle generally leads to splitting of energy from SH to SV for initially SH-polarized  $S_{diff}$  waves. (For the real Earth, recognizing splitting in record sections will not be as straightforward as in Figure 7 because  $SV_{diff}$ energy may not have originated from splitting, but may instead be due to the initial source polarization, as discussed in Section 3).

Relatedly, if waveforms similar to those predicted for cases one and two (Figure 7; with
 D" anisotropy sampled in the beginning of the raypath, or along the whole raypath)

were observed in real data, radial energy could not directly be attributed to splitting due to lowermost mantle anisotropy without considering the source mechanism. The possibility of SV<sub>diff</sub> energy due to effects other than anisotropy can only be excluded if the focal mechanism, and therefore the amount of initial SV energy, is known.

Assuming that it can be shown (via knowledge of the focal mechanism and/or wavefield simulations) that observations of significant SV energy would not be expected in the absence of lowermost mantle anisotropy, deep mantle anisotropy must be present. S<sub>diff</sub>
 splitting serves as a straightforward diagnostic of lowermost mantle anisotropy in this case. However, it will likely be challenging to infer exactly where along the raypath lowermost mantle anisotropy is present or what the lateral extent of the anisotropic region is.

• Only for the case shown in the third row of Figure 7, for which  $S_{diff}$  waves are not 465 sampling D" anisotropy at close distances, and therefore there is an increase in  $SV_{diff}$ 466 amplitudes as a function of distance, can lowermost mantle anisotropy be diagnosed 467 without knowledge of the focal mechanism. An increase of radial amplitudes as a 468 function of distance while transverse amplitudes are decreasing (without any enigmatic 469 waveform effects) almost certainly reflects the presence of lowermost mantle anisotropy 470 (see waveform behavior in Section 3). Additionally, for this case, it should also be 471 possible to localize the anisotropy by identifying which S<sub>diff</sub> raypaths are are associated 472 with an increase of  $SV_{diff}$  amplitudes as a function of distance. 473

In addition to isotropic PREM, we also incorporate the 3D tomography model GyPSuM in the mantle (replacing PREM at those depths) and repeat the simulations described above, incorporating lowermost mantle anisotropy. The results are shown in Supplementary Figure S4. Apart from the arrival times of the  $S_{diff}$  waves and some minor effects to the waveforms, the general amplitude trends are the same as in as in Figure 7, so our conclusions do not depend on the details of long-wavelength mantle heterogeneity.

#### $_{480}$ 4.2. Influence of source-side anisotropy on $SH_{diff}$ splitting estimates

We have already shown that, if there is a non-negligible initial  $SV_{diff}$  component,  $SV_{diff}$ energy could potentially mimic splitting, even if no anisotropy is present. However, even if the focal mechanism is known and it can be shown that  $S_{diff}$  should be (almost) fully SH polarized,  $S_{diff}$  may sample seismic anisotropy in the upper- or mid-mantle on the source side, leading to more SV energy than would be expected for the isotropic case. Here, we investigate how anisotropy near the seismic source can affect estimates of splitting due to lowermost mantle anisotropy.

We first incorporate a 200 km thick anisotropic layer in the upper mantle just beneath the 488 source, with no anisotropy in the lowermost mantle, and investigate the cases of moderate 489 (2% anisotropic strength) and relatively strong (4%) upper mantle source-side anisotropy. 490 For the case of strong HTI upper mantle anisotropy on the source side (and no anisotropy on 491 the receiver side), direct S waves accumulate a time delay of  $\sim 1.8$  s for an epicentral distance 492 of  $60^{\circ}$ , which we determined by running synthetic simulations and measuring the resulting 493 shear wave splitting. The time delay is about half as large for the moderate splitting case. (In general, we would expect splitting of  $S_{diff}$  waves to be weaker than for S, because SV 495 energy will be lost to the core upon diffraction of these waves.) In order to characterize 496 and quantify splitting of  $S_{diff}$  waves due to source-side anisotropy, we calculate synthetic 497 seismograms using AxiSEM3D for the range of (isotropic) lowermost mantle properties that 498 were investigated in Section 3.1, and also incorporate the GyPSuM tomography model for 499 the mantle into our simulations. Then, we measure the splitting intensity due to source-side 500 anisotropy using SplitRacer. 501

Figure 8 shows the synthetic splitting intensities as a function of epicentral distance for 502 a moderate strength of upper mantle source-side anisotropy (200 km thick layer, 2% HTI). 503 We see that, largely independent of lowermost mantle properties, the contribution of source-504 side anisotropy to  $S_{diff}$  splitting is quite modest and would thus unlikely be misdiagnosed as 505 strong lowermost mantle splitting (Figure 7). We do see absolute SI-values that are in some 506 cases (slightly) larger than 0.3 for distances that are smaller than  $115^{\circ}$ ; in particular, for 507 the GyPSuM and the linear gradient scenario with a lowermost mantle velocity of 7.5  $\frac{\mathrm{km}}{\mathrm{s}}$ , 508 the absolute SI-values exceed 0.3 in a few cases. In general, however, moderate source-509 side anisotropy would not be enough to produce significant splitting in S<sub>diff</sub> seismograms. 510 Therefore, it is not likely be mistaken for lowermost mantle anisotropy. 511

For the strong source-side anisotropy case, the results are more complicated, as shown 512 in Supplementary Figure S5: For the case of low  $Q_{\mu}$  (= 75) and for lowermost mantle 513 velocities that are lower than PREM (-2%), the splitting contribution from the source side 514 can propagate through to the receiver and potentially be mistaken for lowermost mantle 515 splitting; for all other investigated scenarios, absolute source-side splitting intensities are 516 mostly lower than 0.3. Another general observation is that the influence of source-side 517 anisotropy tends to decrease with increasing distance (because  $SV_{diff}$  dies off faster than 518  $\mathrm{SH}_{\mathrm{diff}}$ ). Despite this, however, our results indicate that for regions with strong source-519 side anisotropy, S<sub>diff</sub> waves should be corrected for this contribution to reliably measure 520 lowermost mantle splitting. The source-side contribution can, for example, be investigated 521 using other waves such as direct S (e.g., Russo et al., 2010; Foley and Long, 2011; Mohiuddin 522 et al., 2015). 523

Our observation that strong source-side anisotropy can cause  $S_{diff}$  splitting if lowermost 524 mantle velocities are lower than PREM (Figure 8b) poses the question of whether ULVZs can 525 potentially have an even larger effect. In order to investigate their effects, we incorporate a 526 global 20 km thick layer of reduced velocities into our input model. Because we expect results 527 to depend on how much the shear-wave velocity is reduced, we conduct multiple simulations 528 for different S wave velocity reductions. Because the results are generally very similar 529 for different shear velocity reductions, we show the two endmembers with  $2\,\%$  and  $20\,\%$ 530 velocity reduction in Figure 9. (We reduce P velocities by 1/3 of the value for S velocities 531 and keep density unchanged.) Trade-offs between velocity reduction and thickness of the 532 anisotropic layer likely exist, but are not explicitly explored here. We find that only a couple 533 of measurements at small distances are (slightly) split, while all other measurements are null, 534 indicating that source-side upper mantle anisotropy would not generally be mistaken for a 535 lowermost mantle contribution if thin low velocity anomalies are present at the CMB. We 536 conducted similar simulations for different velocity reduction percentages, which confirm 537 this impression (Figure S6). 538

# $_{539}$ 4.3. Influence of lowermost mantle anisotropy on $SH_{diff}$ splitting measurements

We have shown in Section 4.1 how SV amplitudes behave as a function of distance in 540 the presence of lowermost mantle anisotropy. Further, we have shown that strong source-541 side anisotropy can potentially cause  $S_{diff}$  splitting and can thus potentially be mistaken 542 for a lowermost mantle anisotropy contribution in some cases if not properly accounted for 543 (Section 4.2). Here, we go one step further and explicitly measure shear wave splitting 544 (via the splitting intensity) for scenarios that include lowermost mantle anisotropy. We 545 also investigate whether and how the presence of source-side anisotropy affects estimates of 546 splitting parameters due to lowermost mantle anisotropy. 547

For this purpose, we compute synthetic seismograms for multiple scenarios. As in Sec-548 tion 4.1, we investigate how splitting measurements on initially SH-polarized S<sub>diff</sub> waves 549 are influenced by anisotropy located at different regions along the raypath. We incorporate 550 Ppv lowermost mantle anisotropy in the mantle either for a global anisotropic layer in the 551 lowermost mantle, for epicentral distances larger than  $65^{\circ}$  (measured from the source), or 552 less than  $65^{\circ}$ . In order to achieve realistic splitting intensity values for these models, the 553 anisotropic strength of the Ppv elastic tensor for the deep mantle is reduced, as described 554 in Section 2.1. We use two different background models for these synthetics: a) isotropic 555 PREM or b) isotropic PREM, but with the mantle structure replaced by the GyPSuM to-556 mography model. For each of these cases, we investigate how the addition of upper mantle 557 anisotropy influences the shear wave splitting measurements. 558

<sup>559</sup> We show results for moderately strong HTI anisotropy in the upper mantle in Figure 10.

We observe that splitting intensities are relatively constant as a function of distance for a 560 full global anisotropic layer, while they either increase or decrease with epicentral distance 561 for the two other cases. The incorporation of (isotropic) 3D heterogeneity via the GyPSuM 562 tomography model has only a slight influence on the measured splitting intensities compared 563 to isotropic PREM. Also, we find that moderate source-side anisotropy does not strongly 564 affect the measured splitting. This is generally also true for strong source-side anisotropy 565 (Supplementary Figure S7), although the strong upper mantle anisotropy has a slightly 566 larger influence, as expected (see Section 4.2). Compared to a moderate upper mantle 567 anisotropy strength, the 95% confidence intervals of the splitting measurements tend to 568 become larger for strong upper mantle anisotropy. 569

From the simulations that include lowermost mantle anisotropy, we infer that even strong source-side anisotropy likely only has minor effects on the measured overall splitting if the lowermost mantle anisotropy is sufficiently strong. Because it is difficult to ensure that this condition is met, however, we nevertheless recommend only using data that does not sample strong anisotropy in the source side upper mantle, which can be assured using data from phases other than S<sub>diff</sub>. Moreover, we have demonstrated that including realistic 3D heterogeneity does not have a large effect on the measured S<sub>diff</sub> splitting parameters.

#### 577 5. Discussion

#### 578 5.1. Strategy for $S_{diff}$ splitting measurements

We have argued that in order to avoid introducing large uncertainties, splitting should 579 only be measured on  $S_{diff}$  waves that have a negligible initial  $SV_{diff}$  component. We have 580 shown in Section 3.1 that the assumption that  $SV_{diff}$  has died off at any particular distance, 581 and therefore that all SV energy is due to splitting, cannot be made universally. However, 582 there are some examples for which this assumption is indeed appropriate. Specifically, 583 when S<sub>diff</sub> waves sample regions in which the lowermost mantle velocity is greater than 584 average and for certain attenuation structures,  $SV_{diff}$  waves are predicted to die off quickly 585 compared to SH<sub>diff</sub>. There is, however, substantial uncertainty regarding lowermost mantle 586 properties, which makes it difficult to ensure that these conditions are met for any source-587 receiver pair. If isotropic lowermost mantle conditions and  $S_{diff}$  initial polarization are 588 known perfectly, seismic anisotropy could be characterized if  $S_{diff}$  has a mixed  $SH_{diff}$  versus 589  $SV_{diff}$  initial polarization, for example through a waveform modeling approach. However, 590 in practice, there is significant uncertainty about the detailed properties of the lowermost 591 mantle. Therefore, we suggest to ensure that  $S_{\text{diff}}$  is primarily SH polarized via knowledge 592 593 of the focal mechanism. Before measuring  $S_{diff}$  splitting, it should be verified that for the selected source-receiver configuration, little or no  $SV_{diff}$  energy can be expected to arrive at 594

the receiver in an isotropic Earth. This evaluation can be done by using full-wave simulations (by incorporating the known moment tensor), as we do here, or by calculating the initial polarization based on the moment tensor. These simulations can and should consider a priori information about the velocity and attenuation structure of the particular region. It may not be sufficient to rely on isotropic PREM to investigate whether negligible  $SV_{diff}$ energy can be expected, particularly if raypaths sample structures such as LLVPs or regions with higher than average velocities.

We have also shown in Section 4 that, even for cases in which S<sub>diff</sub> would be primarily 602 SH polarized in an isotropic Earth, splitting can occur in the upper mantle on the source 603 side, which can potentially be misinterpreted as evidence of lowermost mantle anisotropy if 604 one does not account for this possibility. Events associated with regions of strong source-605 side anisotropy can be avoided by explicitly measuring source-side splitting using direct 606 S or by focusing on particularly deep events (i.e.,  $> 400 \,\mathrm{km}$ ). While the uppermost lower 607 mantle and the transition zone have been shown to be anisotropic in some cases, particularly 608 in subduction zone settings, they generally produce splitting with delay times < 1 s (e.g., 609 Foley and Long, 2011; Lynner and Long, 2015; Mohiuddin et al., 2015). This means that 610 deep events (> 400 km) can generally be used for  $S_{\text{diff}}$  splitting measurements because only 611 relatively weak source-side splitting ( $\delta t < 1 \, \text{s}$ ) can be expected for them. In any case, it 612 must be ensured in  $S_{diff}$  splitting analyses that candidate  $SH_{diff}$  waves sample only weak to 613 moderate source-side anisotropy. 614

Apart from potentially sampling source-side and lowermost mantle anisotropy, S<sub>diff</sub> waves 615 will generally also be affected by anisotropy in the receiver-side upper mantle (and perhaps 616 the crust), just like other waves used to study the deep mantle. A feasible approach to 617 characterize upper mantle anisotropy beneath stations is to measure SKS splitting over a 618 range of backazimuths, as SKS waves generally reflect contributions from the upper mantle 619 beneath the receiver in most cases (e.g., Becker et al., 2015). S<sub>diff</sub> waves can then be 620 explicitly corrected for this contribution before measuring D"-associated splitting. Such an 621 approach has been shown to accurately retrieve the fast polarization direction,  $\phi$ , for direct 622 source side S splitting; uncertainties of  $\delta t$  measurements are large, however (Wolf et al., 623 2022a). While explicit receiver side corrections are the most straightforward way to account 624 for account for upper mantle anisotropy beneath the receiver, there may also be alternative 625 strategies, particularly in cases where array data are available. (We will discuss alternatives 626 in Section 5.3.) In any case, it should be demonstrated that any measured  $S_{\text{diff}}$  splitting 627 signature cannot be explained by receiver side upper mantle anisotropy, and explicit receiver 628 side corrections are often appropriate. In some cases, it may only be possible to demonstrate 629 that  $S_{diff}$  is affected by lowermost mantle anisotropy, without the ability to explicitly measure 630

the lowermost mantle associated splitting parameters (due to uncertainties associated withreceiver-side corrections).

After measuring the lowermost mantle-associated splitting parameters, it should be con-633 sidered that there is significant uncertainty regarding where along the  $S_{\text{diff}}$  raypath splitting 634 has occurred. In general, anisotropy sampled earlier along the D'' portion of the ray's path 635 will affect the measured splitting parameters at the station less than anisotropy that is 636 sampled later on the raypath (Section 4.1), due to full-wave effects. A single measurement, 637 however, does not suffice to show where exactly seismic anisotropy is present in the low-638 ermost mantle. Inferences on the likely distribution of anisotropy may be possible when 639 multiple measurements from dense seismic arrays are interpreted together; furthermore, an-640 isotropy may be localized by taking advantage of crossing raypaths (e.g., Nowacki et al., 641 2010; Ford et al., 2015; Creasy et al., 2021). We also point out that the measured splitting 642 at the receiver will be affected by a large D'' volume, as the sensitivity kernels for  $S_{diff}$  waves 643 at the base of the mantle are broad. 644

To summarize, our suggested workflow for  $S_{diff}$  splitting measurements to detect lowermost mantle anisotropy includes the following steps:

- <sup>647</sup> 1. Ensure that  $S_{diff}$  can be expected to be almost fully  $SH_{diff}$  polarized in an isotropic <sup>648</sup> Earth for the raypaths under study. This can, for example, be done via full-wave <sup>649</sup> simulations.
- Exclude a substantial source-side upper mantle contribution, either by characterizing
   the source-side anisotropy through other phases (e.g., direct S) or by focusing on deep
   earthquakes (> 400 km).
- $_{653}$  3. Measure S<sub>diff</sub> splitting parameters using standard techniques.

4. If necessary, explicitly correct for receiver side upper mantle anisotropy.

5. Interpret S<sub>diff</sub> splitting measurements in terms of lowermost mantle anisotropy, con sidering that it is often unclear where exactly along the raypath lowermost mantle
 anisotropy was sampled.

#### $_{558}$ 5.2. $S_{diff}$ splitting strategy in light of previous work

Previous work investigated apparent time delays between  $SH_{diff}$  and  $SV_{diff}$  for simple Earth models (Komatitsch et al., 2010), different mantle attenuation structure (Borgeaud et al., 2016), and realistic 3D velocity structure (Parisi et al., 2018). In these studies, events were chosen such that  $S_{diff}$  waves are partially SH and partially SV polarized, with both components generally having a similar amplitude. The radial energy that produced differential  $SH_{diff}$ -SV<sub>diff</sub> travel times in absence of seismic anisotropy in previous studies (Komatitsch

et al., 2010; Borgeaud et al., 2016; Parisi et al., 2018) was mostly due to initial SV energy 665 propagating along the CMB. In practice, however, S<sub>diff</sub> phases are often primarily SH polar-666 ized. We have suggested in this study that  $S_{diff}$  waves can be used for splitting measurements 667 for cases in which  $SH_{diff}$  can be expected to be much larger than  $SV_{diff}$ , thereby excluding 668 effects similar to those reported in previous papers. Additionally, instead of focusing on 669 differential SH<sub>diff</sub>-SV<sub>diff</sub> travel times which often result from waveform distortions, we have 670 explicitly measured splitting parameters ( $\phi$ ,  $\delta t$ ; SI) in our study. This approach helps avoid 671 the misinterpretation of SV<sub>diff</sub> energy that results from isotropic structure (for example, 672 due to the presence of ULVZs or phase interference) as splitting. The reason for this is that 673 well-constrained splitting parameters will only be obtained (for an initially SH-polarized 674  $S_{diff}$  phase) if the radial component has a similar shape as the transverse component time 675 derivative. To summarize, previous studies have analyzed differential  $SH_{diff}$ -SV<sub>diff</sub> travel 676 times from partially SH and SV-polarized  $S_{diff}$  waves. We measure splitting parameters for 677  $S_{diff}$  waves that can be assumed to initially be SH-polarized, a different approach than that 678 taken in this work. The results from this study, including our suggested splitting strategy, 679 are fully consistent with the previous findings of Komatitsch et al. (2010), Borgeaud et al. 680 (2016) and Parisi et al. (2018). 681

#### 682 5.3. Real data example

In order to illustrate our suggested  $S_{diff}$  splitting strategy, we present a real data example 683 using EarthScope USArray data from North America. We focus on a source-receiver geome-684 try for which S<sub>diff</sub> splitting has been identified previously (Wolf and Long, 2022) but expand 685 our analysis to consider additional earthquakes. We use three events that occurred in 2009 686 and 2010 beneath the Celebes Sea; at this time, a large number of USArray Transportable 687 Array stations were deployed at an epicentral distance range of  $101^{\circ}$  to  $120^{\circ}$ . Figure 11a 688 illustrates our source-receiver geometry sampling the lowermost mantle beneath the north-689 ern Pacific Ocean, where we highlight the sections of the raypath along the CMB. The 690 station selection for all three events is very similar (but not identical, because we discard 691 low-quality data from some stations and because the events occurred at different times). 692 The substantial overlap also means that the raypaths are similar for all three events. 693

#### 694 Step 1: Initial polarization of $S_{diff}$

As a first step, following the strategy laid out in Section 5.1, we investigate the expected S<sub>diff</sub> polarizations for each event. We obtain the focal mechanisms of all three events from the USGS database and conduct synthetic simulations using AxiSEM3D (for the same sourcereceiver configurations as for the real data). The background velocity model that we use is isotropic PREM, but we replace the velocities in the lowermost mantle with velocities

from a (isotropic) local 3-D shear wave velocity model beneath the northern Pacific Ocean 700 (Suzuki et al., 2021) to approximate the local velocity structure. We incorporate the Suzuki 701 et al. (2021) model rather than a global model here because it represents smaller scale 702 velocity heterogeneity in the lowermost mantle of our study region. We do not incorporate 703 ULVZs because we have shown before that SV energy due to ULVZs is unlikely to mimic 704 splitting (Section 3.2), and because no ULVZs have been unambiguously identified in our 705 region of interest (Yu and Garnero, 2018). The synthetic radial and transverse component 706 seismograms for three simulations are shown in Figure 11c-e. Fortunately, for all three 707 events, little or no SV<sub>diff</sub> energy would be expected in an isotropic Earth, although predicted 708  $SV_{diff}$  amplitudes for event 2009-10-07 are slightly larger than for the other two events. 709 Despite that, these modeling results indicate that  $S_{diff}$  splitting analyses can be conducted 710 for all three events, as any significant SV energy can be attributed to splitting behavior and 711 not isotropic structure. 712

#### 713 Step 2: Influence of source-side anisotropy

Second, we investigate the possibility of source-side anisotropy contributions to our waveforms. All the three events used in this study occurred at depths greater than 580 km. As argued in Section 4.3 and Section 5.1, significant source-side anisotropy (with delay times > 1 s) is unlikely for such deep events (e.g., Foley and Long, 2011; Lynner and Long, 2015). This was also explicitly shown by Mohiuddin et al. (2015) for the Celebes Sea, where the three earthquakes under study occurred.

#### 720 Step 3: $S_{diff}$ splitting due to lowermost mantle anisotropy

Next, we investigate whether the  $S_{diff}$  waves from our three events show any evidence 721 of lowermost mantle anisotropy. We focus on a subset of the data that shows convincing 722 evidence for  $SV_{diff}$  energy due to D"-associated splitting at azimuths > 43° and distances 723  $> 110^{\circ}$  for all three events (Figure 12), building upon work from Wolf and Long (2022). 724 In Wolf and Long (2022), a similar subset of  $S_{diff}$  data for event 2010-10-07 was analyzed, 725 in combination with measurements of differential SKS-SKKS splitting. In that previous 726 work, we mainly based our interpretation in that work on SKS-SKKS differential splitting 727 results. With the results presented in this paper, we can now be fully confident that the 728 observed  $SV_{diff}$  energy indeed reflects splitting due to deep mantle anisotropy. Here, we 729 extend our analysis to two additional events and measure  $S_{diff}$  splitting due to lowermost 730 mantle anisotropy for all three earthquakes. 731

#### 732 Step 4: Receiver-side anisotropy contribution

Figure 12 shows S<sub>diff</sub> waveforms for all three events aligned via cross-correlation of the transverse components. Energy is clearly split to the radial component for all events; in fact,

the stacked waveforms (black lines; Figure 12) look very similar for all three earthquakes. 735 Figure 13a-c is similar to Figure 12 (for the same source-receiver pairs) but for SKS waves. 736 Figure 13 demonstrates that the splitting of energy from the transverse to the radial compo-737 nent of  $S_{diff}$  for these events cannot be explained by the presence of upper mantle anisotropy 738 beneath the receiver only. This conclusion can be made because no strong, coherent splitting 739 of energy from the radial to the transverse components can be observed for SKS, suggesting 740 that the upper mantle anisotropy beneath the receivers generally causes relatively weak and 741 incoherent splitting for this event. This in turn implies that differences in splitting between 742  $S_{diff}$  and SKS originate from contributions to  $S_{diff}$  splitting from anisotropy along the por-743 tion of the raypath through the lowermost mantle. This result is not entirely surprising, 744 considering that the upper mantle splitting pattern from the IRIS splitting database (IRIS 745 DMC, 2012) shows relatively weak and variable splitting across the array (Figure 13d). We 746 infer from this exercise that for the  $S_{diff}$  waves (measured and stacked across the same set 747 of stations as SKS) the receiver side upper mantle contribution can be expected to largely 748 average out as well. 749

We next quantitatively investigate the degree to which the waveforms are influenced by lowermost vs. upper mantle anisotropy by measuring SKS and  $S_{diff}$  splitting intensities for all individual seismograms from our three events (recorded at the stations shown in Figure 11). We compare these two phases because differences between SKS and  $S_{diff}$  splitting likely reflect a contribution from D", as argued above. Furthermore, we have previously shown that for this source-receiver geometry, SKS is likely primarily influenced by receiver side upper mantle anisotropy (Wolf and Long, 2022).

Our measurements of SKS and  $S_{diff}$  splitting intensities for individual seismograms are 757 shown in Figure 14 as a function of epicentral distance from the source. We find that 758 while SKS splitting intensities tend to decrease as a function of distance and scatter around 759 zero for distances that are larger than  $110^{\circ}$ ,  $S_{diff}$  waves for all three events, in contrast, 760 consistently show a pronounced increase in splitting intensities at an epicentral distance 761 of approximately 110°. This increase occurs at slightly larger distances for event 2009-10-762 07; this event occurred slightly farther away from the USArray stations than the other two 763 events (Figure 11a).  $S_{diff}$  splitting intensities plateau for distances > 110° (Figure 14). Thus, 764 the anisotropic signature apparently does not change as a function of distance, indicating 765 that S<sub>diff</sub> is likely sampling a large, uniformly anisotropic region at the base of the mantle. 766 This is also supported by the observation of coherent and uniform  $S_{diff}$  splitting in the 767 record sections that show the waveforms for these distances (Figure 12). The observation 768 that SKS splitting intensities scatter around zero for distances from  $110^{\circ}$  to  $120^{\circ}$  indicates 769 the presence of generally fairly weak upper mantle anisotropy that varies laterally across 770

<sup>771</sup> the area in which the receivers are positioned. This is consistent with previously published <sup>772</sup> estimates of SKS splitting at these stations (Figure 13d). In contrast to SKS splitting, <sup>773</sup>  $S_{diff}$  splitting is consistently very strong at epicentral distances larger than 110°, showing a <sup>774</sup> distinctly different pattern than SKS. This indicates a considerable influence of lowermost <sup>775</sup> mantle anisotropy on  $S_{diff}$  waves.

We emphasize that the approach we have taken here, which relies on visual inspection of 776 record sections and measurements of splitting intensity as a function of distance, can only 777 be used if S<sub>diff</sub> waves from one event are recorded across a large seismic array. Without such 778 a favorable source-receiver configuration, patterns of splitting intensity with distance could 779 not be resolved well; furthermore, if  $S_{diff}$  waves are too noisy or stations are too sparse, it 780 may not be possible to reliably resolve trends of the splitting intensity. Additionally, this 781 particular dataset allows us to measure splitting from single station  $S_{diff}$  data without ex-782 plicitly correcting for the upper mantle contribution, as discussed below; for other datasets, 783 explicit receiver-side upper mantle corrections will generally be needed. 784

#### <sup>785</sup> Step 5: Interpretation of $S_{diff}$ splitting parameters in terms of deep mantle anisotropy

Our next step is to measure the lowermost mantle associated splitting parameters. To do 786 this, we again focus on the subset of stations for which Wolf and Long (2022) demonstrated a 787 strong lowermost mantle anisotropy contribution for event 2009-10-07. Specifically, we focus 788 on the distances  $> 110^{\circ}$  and azimuths  $< 43^{\circ}$  and take an approach that involves stacking our 789 data. We note that data should only be stacked over a distance and azimuth range for which 790 a uniform lowermost mantle signature can be inferred based on the waveform behavior. In 791 our case, the waveforms in Figure 12 indicate that splitting is uniform. Additionally, we 792 measure  $S_{diff}$  splitting parameters of the single station  $S_{diff}$  seismograms, which yields similar 793  $(\phi', \delta t)$  measurements over the whole distance/azimuth range of interest (Figures S8-S10), 794 indicating that the influence of lowermost anisotropy is more dominant than the (weak) 795 upper mantle receiver side anisotropy (Figure 13d). 796

We now focus on the  $S_{\text{diff}}$  waveforms for the epicentral distance (> 110°) and azimuth 797  $(< 43^{\circ})$  ranges for which a lowermost mantle contribution to splitting has been observed 798 (and for which the corresponding SKS stack splitting is null). We align the S<sub>diff</sub> waveforms 799 by cross-correlation of the transverse components as shown in Figure 15a-b. For all three 800 events, we observe a strong and coherent splitting signal, expressed in  $S_{\text{diff}}$  amplitudes, 801 caused by the contribution of lowermost mantle anisotropy. In order to increase SNR and 802 thus confidence in our measurements, in addition to measuring splitting intensities for in-803 dividual seismograms (Figure 11), we also stack the  $S_{diff}$  waveforms across the array and 804 measure splitting parameters ( $\phi$ ,  $\delta t$ ) from these S<sub>diff</sub> stacks. Results for one event are shown 805 in Figure 15, which shows the splitting diagnostic plots for event 2010-10-04. We do not 806

<sup>807</sup> implement an explicit correction for the effect of the Coriolis force because we have shown that these effects are generally negligible (Section 3.3). We find that the splitting parameters measured for each of the three events agree extremely well (see Supplementary Figures S11 and S12 for events 2010-10-07 and 2010-07-29), with a maximum difference of 3° for  $\phi$ and 0.1 s for  $\delta t$  (the average values are  $\phi \approx 134^{\circ}$  and  $\delta t \approx 1.5$  s). The splitting measurements from the stacks agree with the single station splitting measurements for this dataset (Supplementary Figures S8-S10) but are more robust.

As a final step,  $S_{diff}$  splitting measurements can be interpreted in terms of lowermost 814 mantle deformation and flow directions. This is best accomplished via a forward modeling 815 approach; in particular, we can carry out global wavefield simulations for different lowermost 816 mantle anisotropy scenarios and compare predictions to data. We have previously applied 817 such an approach for event 2010-10-07 in our dataset, which was modeled simultaneously 818 with observations of D"-associated splitting of SKKS waves (Wolf and Long, 2022). Our 819 previous study showed that  $S_{diff}$  splitting for the source-receiver pairs examined in this study 820 can be explained with a model that invokes lattice-preferred orientation of Ppv resulting 821 from slab-driven flow in the lowermost mantle beneath the northeastern Pacific Ocean. 822 Although we used only one event from that study to conduct  $S_{\text{diff}}$  splitting measurements, 823 the results from all three events examined here are highly consistent with the results from 824 Wolf and Long (2022). Thus, the three measurements can also be explained by the same 825 deformation scenario. 826

# $_{227}$ 5.4. $S_{diff}$ splitting analyses on single-station data: Limitations and ways forward

One main advantage with the array data used in Section 5.3 is that the upper mantle 828 splitting contribution is such that explicit anisotropy corrections for the upper mantle on 829 the receiver side are not needed. In many or most cases, however, explicit corrections for 830 upper mantle anisotropy may need to be applied. Even in such cases, however, it may be 831 useful to stack data to improve signal-to-noise ratios. Apart from the approach used here, 832 there are various other strategies to account for the influence of receiver side anisotropy on 833 S<sub>diff</sub> waves. A common approach is to measure SKS splitting for every station, preferably 834 using multiple events from different backazimuths (e.g., Lynner and Long, 2014; Lynner and 835 Long, 2015). S<sub>diff</sub> waveforms can then be corrected for the upper mantle associated splitting 836 parameters obtained this way. We would advise against measuring SKS splitting for a few 837 backazimuths only because splitting beneath any particular station may be complex, and 838 any single SKS splitting measurement may potentially be influenced by lowermost mantle 839 anisotropy (e.g., Wolf et al., 2022a). Alternatively, a strategy to account for the S<sub>diff</sub> upper 840 mantle contribution can be to correct S<sub>diff</sub> for the SKS/SKKS splitting parameters for 841 the same source receiver configuration, if SKS and SKKS are split similarly. (If they are 842

not, at least one of the phases is likely influenced by lowermost mantle anisotropy and 843 both measurements cannot be assumed to be due to upper mantle anisotropy only.) A 84 major disadvantage of this strategy is that well-constrained SKS, SKKS and Sdiff splitting 845 parameters would be required for the same source-receiver configuration. Finding data for 846 which it is possible to obtain such good splitting measurements from three phases in one 847 seismogram may be challenging. A special case of this approach is if SKS and SKKS splitting 848 are null for the raypath under study. In this case,  $S_{\text{diff}}$  splitting could be interpreted to be 849 due to lowermost mantle anisotropy, and no corrections would need to be applied. 850

The investigation of S<sub>diff</sub> waves recorded across a dense, large-aperture array makes 851 patterns of splitting more obvious than they would be for single station measurements 852 (for example, the opposite trends of SKS and  $S_{diff}$  splitting intensities that is shown in 853 Figure 14). Applying our observational strategy to an  $S_{diff}$  dataset from a relatively large 854 array is also helpful in localizing the anisotropy. In our case, for example, we know that the 855  $S_{diff}$  waves show a particularly strong signature of lowermost mantle anisotropy for distances 856  $> 110^{\circ}$ . With this knowledge, the dimensions of the anisotropic region in the lowermost 857 mantle can be (partially) inferred. In contrast, for a single S<sub>diff</sub> splitting measurement it 858 would not possible to infer where the anisotropy is localized along the  $S_{diff}$  raypath. Some 859 caution is also warranted when stacking waveforms across a large array (and thus averaging 860 anisotropy across a relatively large portion of the lowermost mantle). For our dataset this 861 approach is justified, because splitting is coherent for the  $S_{diff}$  waves sampling the D" region 862 under study (Figure 11a and Supplementary Figures S8-S10). In other cases, however, 863 anisotropy could potentially vary laterally, yielding variability in splitting. In general, only 864 those waveforms that show coherent splitting should be stacked, which may mean focusing 865 on smaller distance/azimuth intervals. 866

#### 867 6. Conclusion

In this work, we have investigated isotropic and anisotropic effects on  $S_{diff}$  polarizations 868 in order to understand whether and how the splitting of  $S_{diff}$  waves can be used to infer low-869 ermost mantle anisotropy. We have used full-wave simulations to demonstrate, for a range 870 of isotropic mantle models, that SV<sub>diff</sub> amplitudes do not necessarily decrease substantially 871 faster as function of distance than  $SH_{diff}$  amplitudes. Thus, only  $S_{diff}$  waves with a negligible 872 initial SV component should be used to conduct D'' shear wave splitting measurements, and 873 care must be taken to select suitable events for analysis. In order to evaluate the effects 874 of upper and mid-mantle anisotropy on  $S_{diff}$  splitting, we tested models with anisotropy 875 near the source and found that weak or moderate source-side splitting ( $\delta t_{source} < 1 \, \text{s}$ ) has 876 minimal effects on  $S_{diff}$  waves in most models. However, strong source-side anisotropy can 877

cause  $S_{diff}$  splitting and should be avoided in lowermost mantle anisotropy studies. We have 878 further shown that lowermost mantle anisotropy can be recognized by strong splitting of 87 energy from SH<sub>diff</sub> to SV<sub>diff</sub> (for initially SH-polarized S<sub>diff</sub> waves), while realistic isotropic 880 Earth structure does not mimic such a behavior. Our simulations have demonstrated that 881 S<sub>diff</sub> waves can, indeed, be used to infer lowermost mantle anisotropy under many condi-882 tions. These insights have helped us formulate a strategy for carrying out measurements of 883  $S_{diff}$  splitting due to D" anisotropy. Important considerations include showing that the  $S_{diff}$ waves of interest would be almost completely SH polarized in an isotropic Earth and are 885 not influenced by strong source-side anisotropy ( $\delta t_{source} < 1 \, \text{s}$ ). To illustrate our proposed 886 splitting strategy, we conducted a systematic  $S_{diff}$  splitting analysis for real waveforms for 887 western Pacific earthquakes measured at USArray stations, revealing evidence for strong, 888 coherent anisotropy in the lowermost mantle beneath the northeastern Pacific. 889

# 890 Acknowledgements

This work was funded by Yale University and by the U.S. National Science Foundation 891 via grant EAR-2026917 to MDL, grant EAR-1855206 to NC, and grant EAR-1853911 to EG. 892 We thank the Yale Center for Research Computing for providing the research computing 893 infrastructure for this study. We are also grateful to the Extreme Science and Engineer-894 ing Discovery Environment (XSEDE) Texas Advanced Computing Center (TACC) at The 895 University of Texas at Austin through allocation TG-EES200011 using XSEDE resources 896 (Towns et al., 2014). We acknowledge the Yale seismology group for helpful discussions. 897 The Generic Mapping Tools (Wessel and Smith, 1998), ObsPy (Beyreuther et al., 2010), 898 MSAT (Walker and Wookey, 2012) and SplitRacer (Reiss and Rümpker, 2017) were used in 899 this research. We are grateful to the editor, Ana Ferreira, and an anonymous reviewer for 900 their constructive comments that helped us improve the manuscript. 901

#### 902 Data availability

<sup>903</sup> The synthetic seismograms for this study were computed using AxiSEM3D and SPECFEM3D\_GLOBE,

 ${\tt which are publicly available at {\tt https://github.com/AxiSEMunity} and {\tt https://geodynamics.}}$ 

<sup>905</sup> org/cig/software/specfem3d\_globe. All USArray data (IRIS Transportable Array, 2003)

were downloaded through IRIS (https://service.iris.edu/).

# 907 Figures:



Figure 1: Schematic illustration of a typical source-receiver configuration in our numerical simulations. The  $S_{diff}$  raypath is shown by a solid purple line. (a) Cross-section through Earth. Stations are represented as red triangles and the source as a yellow star.  $S_{diff}$  potentially travels through upper mantle anisotropy at source and receiver side (green), and lowermost mantle anisotropy (blue). (b) Map view of the source, located at the equator (at longitude  $-90^{\circ}$ ), and the  $S_{diff}$  raypath to stations located in a distance of  $103^{\circ}$  and  $130^{\circ}$  at the equator.



Figure 2: 1D models velocity models used in our simulations. Scenario 1: Isotropic PREM (Dziewonski and Anderson, 1981); scenario 2: Isotropic PREM, with 2% lower velocities in the lowermost 150 km of the mantle; scenario 3: Isotropic PREM, with 2% increased velocities in the lowermost 150 km of the mantle.



Figure 3: Displacement synthetic seismograms for simulations using PREM (Dziewonski and Anderson, 1981) as an input model (scenario 1 in Figure 2), calculated for a focal depth of 0 km. We show transverse (first column, dark blue) and radial (second column, teal)  $S_{diff}$  waveforms and corresponding transverse (third column, dark blue) and radial (fourth column, teal) amplitudes as a function of epicentral distance. The amplitudes are plotted relative to the transverse (row 1 and 3) and radial  $S_{diff}$  (row 2) amplitudes at the lowest distance and measured as the maximum absolute values in a time window of from the predicted  $S_{diff}$  arrival to 30 s after it. Three simulations are shown for SH (top row), SV (middle row) and mixed SH-SV initial polarizations (bottom row). Seismograms are shown from 20 s before the predicted  $S_{diff}$  arrival time until 60 s after. Predicted arrival times are calculated using TauP (Crotwell et al., 1999) for the PREM model (red dashed lines). Waveforms are shown after applying a 10 – 50 s bandpass filter.



Figure 4: Transverse and radial  $S_{diff}$  displacement waveforms and amplitudes for 2% lower (scenario 2, top row) and 2% higher (scenario 3, bottom row) shear wave velocities than PREM (Dziewonski and Anderson, 1981) in the lowermost 150 km of the mantle, calculated using a focal depth of 0 km. The amplitudes are plotted relative to the  $SH_{diff}$  (column 1) and  $SV_{diff}$  (column 3) amplitudes at the closest distance. Simulations are conducted for initially fully SH (first/second column) and SV (third/fourth column) polarized  $S_{diff}$  waves. Waveforms are shown in columns 1 and 3; amplitudes are shown in columns 2 and 4. In contrast to Figure 3, only those panels are shown for which  $S_{diff}$  amplitudes are non-null. Other plotting conventions are the same as in Figure 3.



Figure 5: Results from simulations investigating isotropic effects on polarizations of (initially SH polarized)  $S_{diff}$  waves. (a) Transverse (left panel, dark blue) and radial (right panel, teal) waveforms as a function of distance for a simulation using the 3D tomography model GyPSuM (Simmons et al., 2010) for the mantle and isotropic PREM (Dziewonski and Anderson, 1981) elsewhere, calculated for a focal depth of 0 km. The amplitudes are plotted relative to the transverse  $S_{diff}$  amplitude at the lowest distance. For this simulation, the source was placed at the north pole and the the receivers were positioned along 60° longitude. While a clear arrival is visible on the transverse component, almost no energy arrives on the radial. Red dashed lines indicate predicted arrival times according to PREM. Waveforms are shown after applying a bandpass filter between 10 – 50 s. (b) Splitting intensities, measured using SplitRacer (Reiss and Rümpker, 2017), as a function of distance for analogue source-receiver configurations as in (a), along different longitudes (with a spacing of 20°; see legend). All splitting intensity measurements are null (|SI| < -0.3; indicated by black dashed lines). (c) Results for scenarios that include a global 20 km thick basal layer with largely reduced shear velocities (see legend) are shown. S wave velocity reductions are chosen to be 30% and P wave velocity reduction to be 10% compared to PREM (see legend), which is similar to the velocity reduction expected for ULVZs. (d) Splitting intensities for the scenario shown in c, measured as in panel b.



Figure 6: Results for simulations with and without Earth's rotation. (a) Angular deviations of  $S_{diff}$  polarization from the transverse component for a single, realistic event for isotropic PREM (depth = 616 km), where one simulation includes Earth's rotation (blue) and without (red) using SPECFEM3D\_GLOBE. (b) The difference in angular deviations for a simulation including Earth's rotation and one without as determined from (a), where each point is colored by arc distance. The event's moment tensor is included at upper right. (c) A small selection of Sdiff waveforms (for azimuths traversing north with an azimuth range of 340°-360°) from both simulations for the transverse (left) and radial (right) components (Note: radial waveforms are doubled relative to the transverse component to highlight the difference in waveform shape). Red waveforms represent simulations without Earth's rotation, while blue waveforms include rotation. Predicted PREM arrival times of SKS (light blue), SKKS (orange), and  $S_{diff}$  (green) are displayed as well. Waveforms are bandpass filtered (10 s-50 s). (d) Another selection of  $S_{diff}$  waveforms from the same event for azimuths  $100^\circ-130^\circ$ , plotted with same conventions as (c).



Figure 7: Results from synthetic calculations that use an isotropic PREM (Dziewonski and Anderson, 1981) input model, for which the bottom 150 km of the mantle were replaced by Ppv anisotropy, calculated for a focal depth of 500 km. The initial source polarization is SH for all simulations. (The reason for the difference in waveform shape compared to the previous figures is that we use a slightly different source-receiver configuration here, see Section 2.1). Transverse and radial  $S_{diff}$  waveforms (columns 1, 2) and corresponding amplitudes (columns 3, 4) are shown for three different cases. The amplitudes are plotted relative to the transverse  $S_{diff}$  amplitude at the lowest distance. These cases are schematically illustrated in the right column, showing raypaths (violet) from source (yellow star) to receiver (red triangle) for an epicentral distance of 130°, and the location of the lowermost mantle anisotropy (light blue). Upper row: full global layer of Ppv anisotropy (represented by light blue color in right column); middle row: lowermost mantle anisotropy, incorporated in the deep mantle up to an epicentral distance of 65° measured from the source (see right column); bottom row: lowermost mantle anisotropy from an epicentral distance of 65° from the source (see right column). Other plotting conventions are similar to Figure 3.



Figure 8: Results from simulations that incorporate only moderate source-side upper mantle anisotropy and no lowermost mantle anisotropy (200 km thick layer, 2% anisotropic strength for an HTI elastic tensor), plotted as  $SH_{diff}$  splitting intensities as a function of distance, calculated for a focal depth of 500 km. *SI* was measured using SplitRacer (Reiss and Rümpker, 2017). 95% confidence intervals are indicated by error bars. Simulations were conducted for all lowermost mantle properties tested in Section 3.1 (see legend). Simulations for which the lowermost mantle velocity was modified are shown in the top panel. These include an input model for which the mantle in PREM has been replaced by the GyPSuM tomographic model (Simmons et al., 2010; see legend). The middle panel shows results for different lowermost mantle velocity gradients, in particular, linear and flat gradients were tested (see legend). The bottom row presents results for two endmember Q-values. The shaded gray area indicates *SI*-values between -0.3 and 0.3, which would usually be defined as null. Results for simulations that include strong source-side anisotropy and are identical otherwise are shown in Supplementary Figure S5.



Figure 9: Simulation results, expressed as measured splitting intensities, for initially SH-polarized  $S_{diff}$  waves for two different velocity reductions at the base of the mantle, in presence of moderately strong source-side upper mantle anisotropy (200 km thick layer, 4% anisotropic strength for an HTI elastic tensor), calculated for a focal depth of 500 km. Plotting conventions are similar to Figure 8. Synthetics were computed for a 20 km thick low velocity layer at the base of the mantle. P wave velocity reductions are 1/3 of the S wave velocity reductions (see legend). 95% confidence intervals are shown by error bars. Almost all of the measurements are null (gray area). Results for other velocity reductions than those shown here are presented in Supplementary Figure S6.



Figure 10: Results for similar scenarios of anisotropy in the lowermost mantle as shown in Figure 7, with similar plotting conventions as in Figure 8. Lowermost mantle anisotropy is incorporated for a full global layer of Ppv anisotropy, up to an epicentral distance of  $65^{\circ}$  (from the source) or from an epicentral distance of  $65^{\circ}$  (see legend). All simulations that use an isotropic PREM (Dziewonski and Anderson, 1981) without GyPSuM (Simmons et al., 2010) include lowermost mantle anisotropy only (see legend). Simulations with GyPSuM tomography in the mantle (replacing PREM velocity structure) include source and receiver side anisotropy (see legend). Results are shown for a moderately strongly anisotropic layer (as defined in the caption of Figure 8). Results for simulations that include strong source-side anisotropy and are otherwise identical are shown in Supplementary Figure S5.



Figure 11: (a) Raypath and station distribution for the  $S_{diff}$  waves used in our real data example. Events are shown as orange stars, stations as black dots.  $S_{diff}$  raypaths for all three events are shown as solid gray lines. The path length along the CMB (pink) and through the lowermost mantle on the receiver side (blue) are emphasized. (b-d) Synthetic displacement seismograms calculated using an isotropic PREM (Dziewonski and Anderson, 1981) input model, for which lowermost mantle velocities have been replaced with an (isotropic) local 3-D velocity model for the lowermost mantle beneath the northern Pacific (Suzuki et al., 2021). Synthetic seismograms are bandpass-filtered, retaining periods between 8 – 25 s. Transverse components (dark blue) are presented in the top row and radial components (teal) in the bottom row. Predicted S<sub>diff</sub> arrival times according to PREM are indicated by red dashed lines. For all three events S<sub>diff</sub> is almost fully SH polarized.



Figure 12: Transverse (top row) and radial (bottom row) component waveforms for the  $S_{diff}$  waves of all three events (left column: 2009-10-04; middle column: 2009-10-07; right column: 2010-07-29), recorded at a distance > 110° and an azimuth < 43° (see text). Waveforms are aligned and normalized with respect to the maximum radial  $S_{diff}$  amplitudes. Only every 10th trace is plotted without transparency to better visualize the individual waveforms. Red dashed lines represent approximate  $S_{diff}$  arrival times. Linearly stacked traces are plotted in black color on the corresponding panel.



Figure 13: (a-c) SKS waveforms for the same selection of stations and events as in Figure 12. The same plotting conventions as in Figure 12 are used. (d) Zoom-in to the stations (black dots) used for event 2009-10-04. Splitting parameters from the IRIS splitting database (IRIS DMC, 2012) are shown as pink sticks. The orientation of the sticks indicates the fast polarization direction and their length is proportional to the delay time (see legend). Note that the station selection for the two other events is very similar but not identical (e.g., due to different timings of events).



Figure 14: Measurement of splitting intensities for individual seismograms for three events, showing SKS (left column) and  $S_{diff}$  (right column). Top row: for event 2009-10-04; middle row: event 2009-10-07; bottom row: event 2010-07-29. Left column: SKS splitting intensities as a function of distance, measured using SplitRacer (Reiss and Rümpker, 2017). Null results (defined as |SI| < 0.3) are plotted in black and split results in red. Error bars indicate 95% confidence intervals. Only high-quality measurements are retained (defined by a 95% confidence interval that is smaller than  $\pm 0.5$ ). Right column: Sdiff splitting intensities as a function of distance using the same plotting conventions as for the left row. The area with tan shading indicates the distance range for which particularly strong  $S_{diff}$  splitting can be observed for each event.



Figure 15:  $S_{diff}$  waveforms and splitting diagnostic plots from SplitRacer (Reiss and Rümpker, 2017) for event 2009-10-04. Similar plots for the other two events are shown in Supplementary Figures S11 and S12. In the waveform plots, approximate  $S_{diff}$  arrival times as are shown as a red dashed lines. (a) Transverse component waveforms recorded at a distance > 110° and an azimuth < 43° (see text). Waveforms were aligned and normalized with respect to the maximum transverse  $S_{diff}$  amplitudes. (b) Similar representation of the corresponding radial  $S_{diff}$  waveforms. Only every 10th trace is plotted without transparency to better visualize the individual waveforms. (c) Waveforms of the  $S_{diff}$  stack (radial, top trace; transverse, bottom trace) are shown as black solid lines and the start/end of the 50 randomly chosen measurement windows as pink lines. (d) The upper diagram shows the particle motion for the original stack, the lower diagrams for the waveforms that were corrected for splitting. The red lines in the diagrams indicate the backazimuthal direction. (e) The best fitting splitting parameters are shown in the  $\phi'' - \delta t$ -plane, with black color indicating the 95% confidence region. For an explanation of the splitting parameters  $\phi''$  and  $\phi'$  see Section 2.2.

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- <sup>1</sup> Supplementary Information On the measurement of  $S_{diff}$  splitting caused by
- <sup>2</sup> lowermost mantle anisotropy



Figure S1: Representation of the transverse (left column, dark blue) and radial (third column, teal)  $S_{diff}$  waveforms as a function of epicentral distance. Transverse (second column, dark blue) and radial (fourth column, teal) amplitudes are also shown.  $S_{diff}$  arrival times predicted by PREM are represented as red dashed lines. Waveforms are shown for four cases that all use isotropic PREM as their background model. Top row: 40 km thick layer at the base of the mantle with shear wave speeds of 7.0  $\frac{\text{km}}{\text{s}}$  (right column); second row: velocity of 7.0  $\frac{\text{km}}{\text{s}}$  at the base of the mantle and a linear gradient to PREM-like velocities 40 km above the CMB (right column); third row: 150 km thick layer at the base of the mantle with shear at the base of the mantle and a linear gradient gradient to PREM-like velocities 150 km above the CMB (see right column);



Figure S2: Transverse and radial  $S_{diff}$  waveforms and amplitudes for shear quality factor values  $Q_{\mu}$  (throughout this work called Q) of 1000 (upper and third row) and 75 (second and bottom row) in the lowermost mantle. Waveforms were bandpass-filtered, retaining frequencies between 10 - 50 s. Plotting conventions are the same as in Figure S1.



Figure S3: Splitting intensities as a function of distance for analogue source-receiver configurations along different longitudes (with a spacing of 20°; see legend). All splitting intensity measurements are null (|SI| < -0.3; indicated by black dashed lines). This figure is similar to Figure 5b of the main manuscript. The only difference is that S40RTS was used instead of GyPSuM.



Figure S4: Similar to Figure 6 of the main manuscript using the GyPSuM tomography model for the mantle. Transverse and radial  $S_{diff}$  waveforms (columns 1, 2) and corresponding amplitudes (columns 3, 4) are shown for three different scenarios. These different scenarios are schematically illustrated in the right column, that shows raypaths (violet) from source (yellow star) to receiver (red triangle), and the location of the lowermost mantle anisotropy (light blue). Upper row: for a full global layer of Ppv anisotropy (represented by light blue color in right column); middle row: Lowermost mantle anisotropy, incorporated in the deep mantle up to an epicentral distance of 65° measured from the source (see right column); bottom row: from an epicentral distance of 65° from the source (see right column).



Figure S5: Results from similar simulations as those shown in Figure 8 of the main manuscript but for strong upper mantle anisotropy, plotted as  $SH_{diff}$  splitting intensities as a function of distance, calculated for a focal depth of 500 km. *SI* was measured using SplitRacer. 95% confidence intervals are indicated by error bars. Simulations for which the lowermost mantle velocity was modified are shown in the top panel. These include an input model for which the mantle in PREM has been replaced by the GyPSuM tomographic model (see legend). The middle panel shows results for different lowermost mantle velocity gradients, in particular, linear and flat gradients were tested (see legend). The bottom row presents results for two endmember Q-values. The shaded gray area indicates *SI*-values between -0.3 and 0.3, which would usually be defined as null.



Figure S6: Similar to Figure 9 of the main manuscript for strong upper mantle anisotropy. Simulation results, expressed as measured splitting intensities, for initially SH-polarized  $S_{diff}$  waves for two different velocity reductions at the base of the mantle, calculated for a focal depth of 500 km. Plotting conventions are similar to Figure S9. Synthetics were computed for a 20 km thick low velocity at the base of the mantle. P wave velocity reductions are 1/3 of the S wave velocity reductions (see legend). 95% confidence intervals are shown by error bars. Almost all of the measurements are null. Results for other velocity reductions than those shown here are presented in Supplementary Figure S5.



Figure S7: Similar to Figure 10 of the main manuscript for strong upper mantle anisotropy. Lowermost mantle anisotropy is incorporated for a full global layer of Ppv anisotropy, up to an epicentral distance of 65° (from the source) or from an epicentral distance of 65° (see legend). All simulations that use an isotropic PREM without GyPSuM include lowermost mantle anisotropy only (see legend). Simulations with GyPSuM tomography in the mantle (replacing PREM velocity structure) include source and receiver side anisotropy (see legend).



Figure S8: Well-constrained single station splitting parameters ( $\phi'$ ,  $\delta t$ ) for event 2009-10-04. (a-b)  $\phi'$  as a function of (a) distance and (b) azimuth. Red markers show best fitting fast polarization directions determined using SplitRacer; 95% confidence intervals are presented as error bars. The blue line shows the best fitting fast polarization direction measured from the stacked S<sub>diff</sub> waveform from this event. Light blue shading indicates distances > 110° and azimuths < 43°, for which S<sub>diff</sub> splitting was determined from stacks. (c-d) are analogous to (a-b) but for  $\delta t$ .



Figure S9: Like Figure S8 but for event 2009-10-07.



Figure S10: Like Figure S8 but for event 2010-10-24.



Figure S11:  $S_{diff}$  waveforms and splitting diagnostic plots from SplitRacer for event 2009-10-07. In the waveform plots, approximate  $S_{diff}$  arrival times are shown as a red dashed lines. (a) Transverse component waveforms recorded at a distance > 110° and an azimuth < 43° (see text). Waveforms were aligned and normalized with respect to the maximum transverse  $S_{diff}$  amplitudes. (b) Similar representation of the corresponding radial  $S_{diff}$  waveforms. Only every 10th trace is plotted without transparency to better visualize the individual waveforms. (c) Waveforms of the  $S_{diff}$  stack (radial, top trace; transverse, bottom trace) are shown as black solid lines and the start/end of the 50 randomly chosen measurement windows as pink lines. (d) The upper diagram shows the particle motion for the original stack, the lower diagrams for the waveforms that were corrected for splitting. The red lines in the diagrams indicate the backazimuthal direction. (e) The best fitting splitting parameters are shown in the  $\phi'' - \delta t$ -plane, with black color indicating the 95% confidence region. For an explanation of the splitting parameters  $\phi''$  and  $\phi'$  see Section 2.2 of the main manuscript.



Figure S12: Same plotting conventions as in Figure S11 but here for event 2010-07-29.