

Ocean general circulation models simulate total ocean transport averaged over surface waves

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February 22, 2024

Abstract

We argue that ocean general circulation models and observations based on Ekman or geostrophic balance provide estimates of the Lagrangian-mean ocean velocity field averaged over surface waves — the total time-averaged velocity that advects oceanic tracers, particles, and water parcels. This interpretation contradicts an assumption often made in ocean transport studies that numerical models and observations based on dynamical balances estimate the Eulerian-mean velocity — the velocity time-averaged at a fixed position and only `_part_` of the total ocean velocity. Our argument uses the similarity between the wave-averaged Lagrangian-mean momentum equations appropriate at large oceanic scales, and the momentum equations solved by “wave-agnostic” general circulation models that neglect surface wave effects. We further our case by comparing a realistic, global, “wave-agnostic” general circulation ocean model to a wave-averaged Lagrangian-mean general circulation ocean model at eddy-permitting 1/4-degree resolution, and find that the wave-agnostic velocity field is almost identical to the wave-averaged Lagrangian-mean velocity.

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Key Points:

- General circulation models *without* surface wave effects simulate total Lagrangian-mean currents
- Observational transport estimates derived from Ekman or geostrophic balance are also Lagrangian-mean
- Don't add Stokes drift to model output or observations based on Ekman or geostrophic balance

Abstract

We argue that ocean general circulation models and observations based on Ekman or geostrophic balance provide estimates of the Lagrangian-mean ocean velocity field averaged over surface waves — the total time-averaged velocity that advects oceanic tracers, particles, and water parcels. This interpretation contradicts an assumption often made in ocean transport studies that numerical models and observations based on dynamical balances estimate the Eulerian-mean velocity — the velocity time-averaged at a fixed position and only *part* of the total ocean velocity. Our argument uses the similarity between the wave-averaged Lagrangian-mean momentum equations appropriate at large oceanic scales, and the momentum equations solved by “wave-agnostic” general circulation models that neglect surface wave effects. We further our case by comparing a realistic, global, “wave-agnostic” general circulation ocean model to a wave-averaged Lagrangian-mean general circulation ocean model at eddy-permitting $1/4^\circ$ resolution, and find that the wave-agnostic velocity field is almost identical to the wave-averaged Lagrangian-mean velocity.

Plain language summary

Physical oceanographers are taught that surface waves “induce” a time-averaged current called the Stokes drift. This notion motivates studies in which the total ocean surface transport of things like trash, oil, and kelp is estimated by the combined effect of “ocean currents” as simulated by an ocean model, or estimated from observations, and an *additional* “surface wave Stokes drift”. In this paper, we show that ocean models and observations actually estimate total ocean transport *including* Stokes drift. So, we usually shouldn't “add Stokes drift” to model output or certain kinds of observations.

1 Introduction

Ocean surface waves complicate observations and models of near-surface ocean transport. Surface waves are associated with significant, yet oscillatory fluid displacements that must be time-averaged away to reveal the underlying persistent circulation. But time-averaging over surface waves is not straightforward: the ocean velocity averaged at a fixed position — the

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“Eulerian-mean velocity” — is missing a component of the total transport called the “Stokes drift” (Stokes, 1847). The total mean velocity responsible for advecting tracers, particles, and water parcels is called the “Lagrangian-mean velocity”, because it can be obtained by time-averaging currents in a semi-Lagrangian reference frame that follows surface wave oscillations. These statements are summarized by the timeless formula

$$\mathbf{u}^L = \mathbf{u}^E + \mathbf{u}^S, \quad (1)$$

where $\mathbf{u}^L$ is the surface-wave-averaged Lagrangian-mean velocity, $\mathbf{u}^E$ is the surface-wave-averaged Eulerian-mean velocity, and $\mathbf{u}^S$ is the surface wave Stokes drift (Longuet-Higgins, 1969). On average, tracers, particles, and water parcels follow streamlines traced by Lagrangian-mean velocity $\mathbf{u}^L$. (Formulas analogous to (1) also apply to velocities averaged over longer time intervals, such as supermonthly timescales over mesoscale ocean turbulence, but we do not discuss “other” Lagrangian-mean velocities in this paper.)

Most general circulation models of ocean transport, and many observation-based estimates based on dynamical balances, neither resolve surface wave oscillations nor invoke an explicit dependence on the surface wave state. Such “wave-agnostic” estimates must be *interpreted* as somehow time-averaged over surface wave oscillations. Note that the expression “wave-agnostic” excludes observations based on explicit averaging, such as moored Eulerian velocity measurements, or fully Lagrangian drifter or tracer-based estimates (for in depth discussions and examples see Longuet-Higgins, 1969; Middleton & Loder, 1989; Smith, 2006), which lack the ambiguity inherent to wave-agnostic estimates. We ask: do wave-agnostic models and observations based on dynamical balances estimate the Eulerian-mean velocity, or the Lagrangian-mean velocity?

Studies that discuss surface wave effects on ocean transport (Kubota, 1994; Tamura et al., 2012; Fraser et al., 2018; Iwasaki et al., 2017; Van den Bremer & Breivik, 2017; Dobler et al., 2019; Onink et al., 2019; Kerpen et al., 2020; Van Sebille et al., 2020; Bosi et al., 2021; Van Sebille et al., 2021; Durgadoo et al., 2021; Cunningham et al., 2022; Chassignet et al., 2021) often assume that the ocean velocity estimated by numerical models or observational products — in particular, those that neglect surface wave effects — is the Eulerian-mean velocity. We call this assumption the “Eulerian-mean hypothesis”. Within the context of the Eulerian-mean hypothesis, the total Lagrangian-mean transport is constructed by adding an estimate of the Stokes drift velocity (derived from an estimate of the surface wave state) to model output or observational products, according to (1).

In this paper we propose the alternative “Lagrangian-mean hypothesis”, which posits that wave-agnostic models and most dynamics-based observational products estimate the Lagrangian-mean velocity. We begin in section 2.1 by showing that the Eulerian-mean hypothesis is inconsistent: in the Eulerian-mean Boussinesq equation (Craig & Leibovich, 1976; Huang, 1979), surface wave terms cannot be neglected if the Stokes drift $\mathbf{u}^S$ is comparable to the Eulerian-mean velocity $\mathbf{u}^E$. Next, in section 2.2, we show that the alternative “Lagrangian-mean hypothesis” is consistent because, in the Lagrangian-mean Boussinesq equation, surface wave terms are negligible at ocean mesoscales and larger. Our scaling arguments apply both to general circulation models and observational products based on Ekman and geostrophic balance like GlobCurrent (Johannessen et al., 2016) and predict that wave-agnostic general circulation model output is *indistinguishable* from Lagrangian-mean general circulation model output.

In section 3, we demonstrate the similarity between wave-agnostic dynamics and Lagrangian-mean dynamics at ocean mesoscales by comparing output from a wave-agnostic “control” general circulation ocean model simulation that neglects surface wave effects on velocity and tracers with a “wave-averaged” general circulation ocean model simulation that explicitly includes surface waves. We find that the velocity in the wave-agnostic simulation is almost identical to the Lagrangian-mean velocity in the wave-averaged simulation.

Our results provide strong evidence that wave-agnostic models and dynamically-based observational products implicitly use a Lagrangian-mean formulation of the wave-averaged Boussinesq equations, and therefore estimate of the Lagrangian-mean transport directly. In consequence, ocean transport studies based on wave-agnostic model output or observations based on dynamical balances should not “add Stokes drift” to construct the total Lagrangian-mean transport. We conclude in section 4 by discussing the implications of our results for surface boundary layer parameterizations and the potential uses of wave-averaged general circulation models.

2 Wave-averaged and wave-agnostic dynamics

The wave-averaged Craik–Leibovich Boussinesq momentum equation (Craik & Leibovich, 1976; Huang, 1979) can be written either in terms of the Eulerian-mean velocity $\mathbf{u}^E$,

$$\partial_t \mathbf{u}^E + (\mathbf{u}^E \cdot \nabla) \mathbf{u}^E + f \hat{\mathbf{z}} \times (\mathbf{u}^E + \mathbf{u}^S) + \nabla (\bar{p} + \frac{1}{2} \mathbf{u}^S \cdot \mathbf{u}^S + \mathbf{u}^S \cdot \mathbf{u}^E) = \bar{b} \hat{\mathbf{z}} + \mathcal{X} + \mathbf{u}^S \times (\nabla \times \mathbf{u}^E), \quad (2)$$

or the Lagrangian mean velocity, $\mathbf{u}^L$,

$$\partial_t \mathbf{u}^L + (\mathbf{u}^L \cdot \nabla) \mathbf{u}^L + (f \hat{\mathbf{z}} - \nabla \times \mathbf{u}^S) \times \mathbf{u}^L + \nabla \bar{p} = \bar{b} \hat{\mathbf{z}} + \mathcal{X} + \partial_t \mathbf{u}^S. \quad (3)$$

In (2)–(3), $\bar{p}$ is the Eulerian-mean kinematic pressure (pressure scaled with ocean’s reference density), $\bar{b} \stackrel{\text{def}}{=} -g\rho'/\rho_0$ is the Eulerian-mean buoyancy defined in terms of gravitational acceleration g , reference density ρ_0 , and the Eulerian-mean density perturbation ρ' , f is the Coriolis parameter, and $\hat{\mathbf{z}}$ is the unit vector pointing up. $\mathcal{X}$ parametrizes subgrid momentum flux divergences associated with, for example, ocean surface boundary layer turbulence. We discuss $\mathcal{X}$ further in section 4. Equations (2)–(3) are related by (1) and standard vector identities. Physical interpretations for the green surface wave terms in equations (2)–(3) are discussed by Wagner et al. (2021) in their section 2.1, Bühler (2014) in their section 11.3.2, and by Suzuki and Fox-Kemper (2016).

The green surface wave terms in equations (2) and (3) depend *explicitly* on the Stokes drift $\mathbf{u}^S$ and therefore the surface wave state. The green terms distinguish equations (2)–(3) from the wave-agnostic Boussinesq momentum equation,

$$\partial_t \mathbf{u} + (\mathbf{u} \cdot \nabla) \mathbf{u} + f \hat{\mathbf{z}} \times \mathbf{u} + \nabla p = b \hat{\mathbf{z}} + \mathcal{X}, \quad (4)$$

solved by typical, wave-agnostic ocean general circulation models.

2.1 The Eulerian-mean hypothesis is inconsistent

The Eulerian-mean hypothesis posits that velocities $\mathbf{u}$ that solve equation (4) are identical or similar to $\mathbf{u}^E$ in (2) at ocean mesoscales and larger. The Eulerian-mean hypothesis therefore requires that (4) is a good approximation to (2) when $\mathbf{u}^S \sim \mathbf{u}^E$.

The central flaw in the Eulerian-mean hypothesis is that Stokes-Coriolis term $f \hat{\mathbf{z}} \times \mathbf{u}^S$ in (2) is the same magnitude as the “Eulerian-mean component of the Coriolis force”, $f \hat{\mathbf{z}} \times \mathbf{u}^E$. Thus for dynamics close to geostrophic and Ekman balance, (2) is not a good approximation to (4) because it does not represent the *total* Coriolis force $f \hat{\mathbf{z}} \times \mathbf{u}^L$. A similar argument applies to tracer advection by $\mathbf{u}^L$.

The failure of the Eulerian-mean hypothesis to account for both tracer advection and the total Coriolis force is sufficient motivation to pursue the Lagrangian-mean hypothesis, and convinced readers may skip to section 2.2. The remainder of this section shows that the “vortex force” $\mathbf{u}^S \times (\nabla \times \mathbf{u}^E)$ and “Stokes-Bernoulli” terms aside the pressure in (2) are $O(\text{Ro})$, where

$$\text{Ro} \stackrel{\text{def}}{=} \frac{U}{fL}, \quad (5)$$

is the Rossby number for flows with velocity scale $|\mathbf{u}^L| \sim |\mathbf{u}^S| \sim |\mathbf{u}^E| \sim U$ and horizontal scales $L \sim U/|\nabla_h \mathbf{u}|$. Ro is typically less than unity for oceanic motion at mesoscales and larger.

Under slowly-modulated surface waves, the ratio

$$\frac{|\nabla_h \mathbf{u}^S|}{|\partial_z \mathbf{u}^S|} \sim \frac{H}{L}, \quad (6)$$

is small, where H is the vertical decay scale of the Stokes drift. The approximation (6) simplifies the vortex force in (2) to

$$\mathbf{u}^S \times (\nabla \times \mathbf{u}^E) \approx v^S (\partial_x v^E - \partial_y u^E) \hat{\mathbf{x}} - u^S (\partial_x v^E - \partial_y u^E) \hat{\mathbf{y}} - (u^S \partial_z u^E + v^S \partial_z v^E) \hat{\mathbf{z}}, \quad (7)$$

where $\hat{\mathbf{x}}$ and $\hat{\mathbf{y}}$ are unit vectors in horizontal directions.

We simplify the scaling analysis by reusing H and L in (6) for vertical and horizontal near-surface velocity scales. For the x -component of (7) we find

$$\frac{\partial_x (\frac{1}{2} \mathbf{u}^S \cdot \mathbf{u}^S + \mathbf{u}^S \cdot \mathbf{u}^E)}{f v^E} \sim \frac{(\partial_x v^E - \partial_y u^E) v^S}{f v^E} \sim \frac{U^2/L}{f U} = \text{Ro}. \quad (8)$$

A similar result holds for the y -component of (7). Compared to the geostrophic pressure gradient $\partial_z \bar{p} \sim fUL/H$, we find that the vertical component of (7) scales with

$$\frac{u^S \partial_z u^E + v^S \partial_z v^E}{\partial_z \bar{p}} \sim \frac{U^2/H}{fUL/H} = \text{Ro}. \quad (9)$$

In summary, in nearly geostrophic mesoscale flows, the Stokes–Coriolis term in (2) is $O(1)$ and non-negligible, which means that (2) is a poor approximation to (4) and casts doubt on the Eulerian-mean hypothesis. The other surface wave terms in (2) are $O(\text{Ro})$ and are thus negligible for $\text{Ro} \ll 1$.

2.2 The Lagrangian-mean hypothesis is consistent

The “Lagrangian-mean hypothesis” posits that velocities $\mathbf{u}$ that solve (4) are similar to Lagrangian-mean velocities $\mathbf{u}^L$ that solve (3) at ocean mesoscale and larger. We argue that the Lagrangian-mean hypothesis is consistent with a scaling analysis that suggests the green terms in (3) are negligible at ocean mesoscales and larger.

Using (6) we simplify the surface wave term in (3),

$$(\nabla \times \mathbf{u}^S) \times \mathbf{u}^L \approx w^L \partial_z u^S \hat{\mathbf{x}} + w^L \partial_z v^S \hat{\mathbf{y}} - (u^L \partial_z u^S + v^L \partial_z v^S) \hat{\mathbf{z}}. \quad (10)$$

The term in (10) has the same form as the “non-traditional” component of the Coriolis force associated with the horizontal components of planetary vorticity (which have been neglected *a priori* from (3)). Thus the terms in (10) are small for the same reason we make the traditional approximation for Coriolis forces: because of the dominance of hydrostatic balance, and because geostrophic vertical velocities scale with

$$w^L \sim \text{Ro} \frac{H}{L} U, \quad (11)$$

and are therefore miniscule at ocean mesoscales and larger where both Ro and especially H/L are much smaller than unity. Specifically, the same arguments leading to (8) conclude that the horizontal components of (10) scale with Ro^2 — much smaller than $O(1)$ and smaller even than the $O(\text{Ro})$ terms in (8). The vertical component of (10) shares the same scaling with (9): $O(\text{Ro})$ and therefore negligible at ocean mesoscales and larger.

We save the discussion of $\partial_t \mathbf{u}^S$ for last. Only the horizontal components of $\mathbf{u}^S$ are significant (Vanneste & Young, 2022). $\partial_t \mathbf{u}^S$ is primarily associated with wave growth beneath

atmospheric storms and thus effectively represents the small part of the total parameterized air-sea momentum transfer that is *depth-distributed* rather than fluxed at or just below the surface (Wagner et al., 2021). We could therefore interpret $\partial_t \mathbf{u}^S$ as accounted for implicitly in wave-agnostic models by bulk formulae for air-sea momentum transfer. Even so, we consider a scaling argument by introducing an average $\langle \cdot \rangle$ over a time-scale T much longer than a day, and therefore much larger than f^{-1} . We find that

$$\frac{\langle \partial_t u^S \rangle}{|f v^L|} \sim \frac{|\mathbf{u}^S|}{f T |\mathbf{u}^L|} \ll 1. \quad (12)$$

We conclude that the Lagrangian-mean hypothesis is consistent since all terms in (3) that explicitly involve surface waves are at least $O(\text{Ro})$ or smaller.

3 Ocean general circulation simulations with and without explicit surface wave effects

We pursue empirical validation of the scaling arguments and conclusions in section 2 by describing a novel wave-averaged general circulation model, and comparing simulated surface velocity fields between a realistic, typical “control” global ocean simulation and a wave-averaged simulation. The comparison shows that typical general circulation models — which do not depend explicitly on the ocean surface wave state — simulate and output Lagrangian-mean currents. Both the control and wave-averaged general circulation simulations use models based on the Modular Ocean Model 6 (MOM6) following the Geophysical Fluid Dynamics Laboratory (GFDL)’s OM4 configuration (Adcroft et al., 2019).

3.1 Control general circulation model based on MOM6

Our control MOM6-based general circulation model (GCM) is called “Ocean Model 4”, or OM4. OM4 is a typical GCM that discretizes and time-integrates the horizontal components of the wave-agnostic, implicitly-averaged Boussinesq momentum equation (4), with hydrostatic balance

$$\partial_z p = b, \quad (13)$$

approximating the vertical component of (4).

3.2 A wave-averaged MOM6

Our wave-averaged GCM, dubbed “OM4-CL” (CL after Craik & Leibovich, 1976) discretizes and time-integrates the horizontal components of the wave-averaged Craik–Leibovich Boussinesq momentum equation (3). OM4-CL replaces the vertical component of equation (3) with “wavy hydrostatic balance” (Suzuki & Fox-Kemper, 2016)

$$\partial_z \bar{p} = \bar{b} - (\mathbf{u}^L \partial_z \mathbf{u}^S + \mathbf{v}^L \partial_z \mathbf{v}^S). \quad (14)$$

In OM4-CL, tracers are advected by $\mathbf{u}^L$, and mass conservation is enforced by requiring that $\mathbf{u}^L$ is divergence-free.

3.3 Coupled sea ice–ocean model simulations

Both the control OM4 and the wave-averaged OM4-CL simulations follow the approach for coupled ocean and sea-ice model initialization and forcing laid out by Adcroft et al. (2019). Prescribed atmospheric and land forcing fields in these simulations are obtained from the JRA55-do reanalysis product (Tsujino et al., 2018), following recommendations from the second Ocean Model Intercomparison Project protocol (OMIP2, see Griffies et al., 2016; Tsujino et al., 2020). Simulations are performed with a nominal lateral resolution of $1/4^\circ$ that partially resolves mesoscale eddies. Our configuration is similar to OM4p25 described by Adcroft et al. (2019). We conduct simulations using forcing from 1958–2017 and analyze

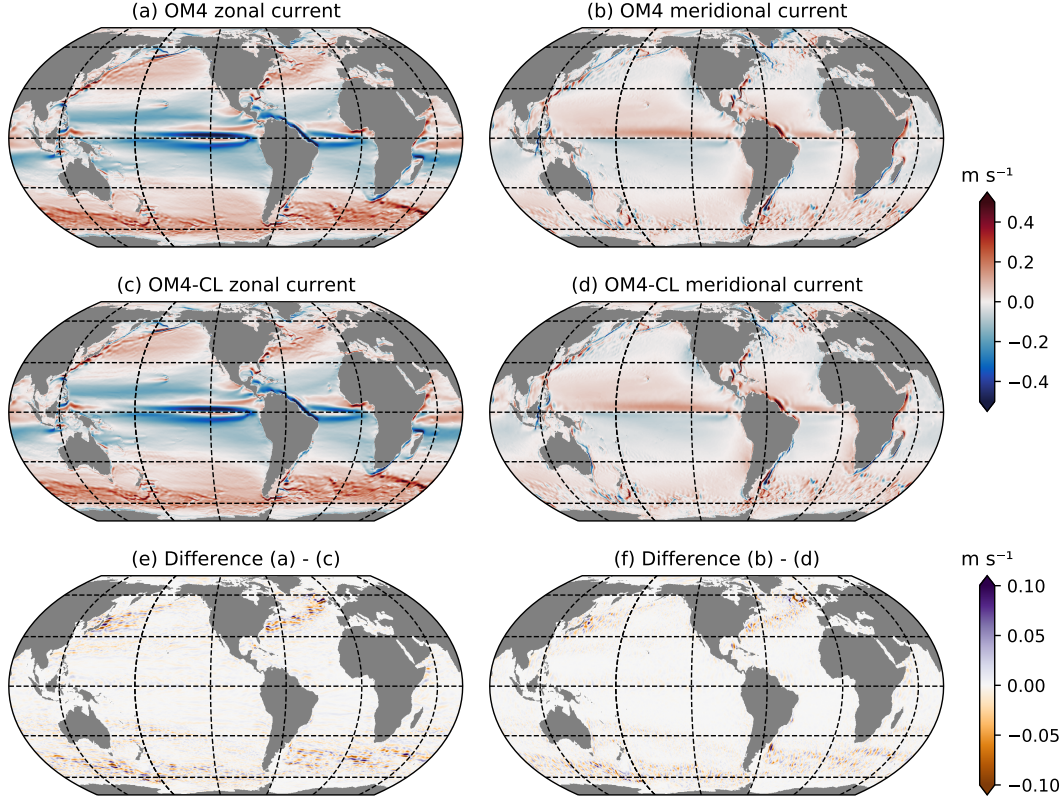


Figure 1: (Upper) OM4 zonal and meridional surface currents ($\mathbf{u}$ in (4)) averaged between 1998-2017, (middle) time-averaged OM4-CL zonal and meridional currents ($\mathbf{u}^L$ in (3)), and (bottom) differences between the upper two rows. Note the different color scales between panels (a)-(d) and the bottom two panels.

model output from the last 20 years (1998-2017). For the wave-averaged simulations, global Stokes drift velocities are taken from an offline WAVEWATCH-III v6.07 simulation (The WAVEWATCH III Development Group (WW3DG), 2016), following a similar procedure to that by Reichl and Deike (2020). Both OM4 and OM4-CL use the same wave-dependent surface boundary layer vertical mixing parameterization (Reichl & Li, 2019) with the same Stokes drift input.

Note that the same winds — not the same wind stress — force both OM4 and OM4-CL, and that OM4-CL includes the Stokes tendency term $\partial_t \mathbf{u}^S$ in equation (3). As a result, OM4 and OM4-CL have slightly different column-integrated momentum budgets (Fan et al., 2009; Wagner et al., 2021). Nevertheless, figures 1 and 2 show that these discrepancies are not important.

3.4 Wave-agnostic currents are almost identical to Lagrangian-mean currents simulated by the wave-averaged model

Figure 1 compares surface currents between the control OM4 and the wave-averaged OM4-CL. OM4 simulates “implicitly-averaged” currents with no explicit surface wave dependence, while OM4-CL explicitly simulates Lagrangian-mean surface currents. Currents output from both OM4 and OM4-CL are further averaged over the time period 1998-2017. The similarity of figure 1a-b, which show zonal and meridional components of $\mathbf{u}$ from OM4, and figure 1c-d, which show the zonal and meridional components of the Lagrangian-mean $\mathbf{u}^L$

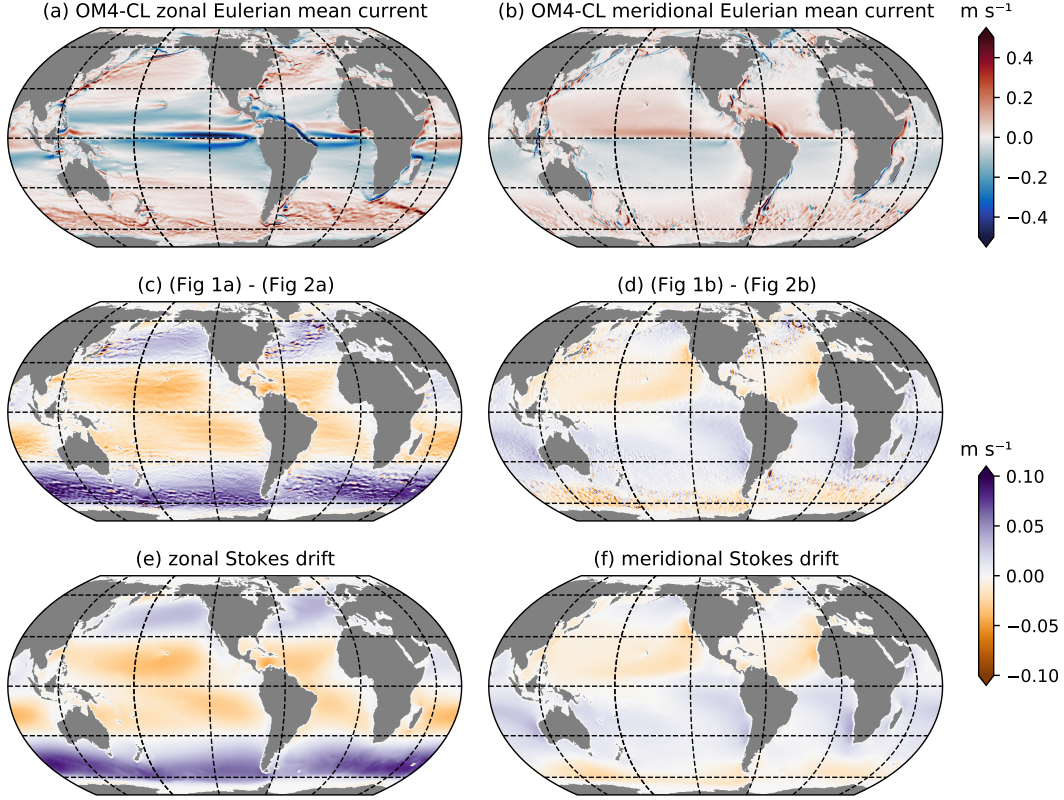


Figure 2: (Upper) Mean OM4-CL zonal and meridional Eulerian-mean surface currents (1998-2017), (middle) difference between OM4-CL Eulerian mean currents and OM4 currents, and (bottom) mean surface Stokes drift.

from OM4-CL, demonstrate that the surface circulation in OM4 and the Lagrangian-mean surface circulation in OM4-CL are almost identical. The differences between the zonal and meridional components of $\mathbf{u}$ and $\mathbf{u}^L$, shown in the bottom row of figure 1, are small and associated with turbulent mesoscale perturbations.

Next, we entertain the Eulerian-mean hypothesis. The Eulerian-mean velocity is calculated from OM4-CL output by subtracting the Stokes drift from the simulated velocity $\mathbf{u}^L$ according to (1). The Eulerian-mean hypothesis posits that the mean velocity in the control OM4 simulation is close or identical to Eulerian-mean velocity from the OM4-CL simulation. However, the middle row of figure 2 reveals a systematic and significant difference between the Eulerian-mean velocity from OM4-CL and the wave-agnostic velocity from OM4 which is much larger than the differences exhibited in the bottom row of figure 1. Furthermore, the difference between the currents from the control simulation and the Eulerian-mean currents from the wave-averaged simulation (middle row of figure 2) turns out to be almost identical to the mean surface Stokes drift currents (bottom row of figure 2). We thus do not find evidence to support the Eulerian-mean hypothesis. Instead, the current simulated by the wave-agnostic OM4 is close to the Lagrangian-mean current simulated by OM4-CL, as predicted by the Lagrangian-mean hypothesis.

4 Discussion

By inspecting the wave-averaged equations of motion, and comparing the output from wave-neglecting control simulation and an explicitly wave-averaged simulation, we come to two conclusions: (i) typical GCMs simulate the Lagrangian-mean velocity field; and (ii) resolved (not parameterized) surface wave effects are negligible at the large oceanic scales.

4.1 Boundary layer parameterization in general circulation models

Because general circulation models solve the Lagrangian-mean equations, their parameterizations are formulated in terms of $\mathbf{u}^L$. For example, the K -profile parameterization (Large et al., 1994) models the turbulent vertical flux of horizontal momentum with

$$\mathcal{X} \approx \partial_z (K \partial_z \mathbf{u}^L), \quad (15)$$

where the turbulent vertical diffusivity K is a nonlinear function of mean buoyancy $\bar{b}$, mean velocity $\mathbf{u}^L$, surface boundary conditions, and depth z . We emphasize that the parameterization in equation (15) is sensible, as it dissipates mean kinetic energy $\frac{1}{2}|\mathbf{u}^L|^2$ (Wagner et al., 2021) and is consistent with large eddy simulation results. For example, Reichl et al. (2016) find momentum fluxes aligned with $\partial_z \mathbf{u}^L$ in large eddy simulations of hurricane-forced boundary layer turbulence, and Pearson (2018) observe that turbulent mixing beneath surface waves tends to homogenize $\mathbf{u}^L$.

4.2 Future applications of wave-averaged general circulation models

Figures 1 and 2 show that resolved surface wave effects are negligible at $1/4^\circ$ degree resolution. However, we expect that resolved surface wave effects become more relevant at finer resolutions and higher Rossby numbers, when the term $(\nabla \times \mathbf{u}^S) \times \mathbf{u}^L$ in (3) is no longer negligible. The question remains: “At what resolution do wave effects matter for mesoscale or submesoscale dynamics?” Surface wave effects are known to be important at the $O(1\text{ m})$ scales of ocean surface boundary layer large eddy simulations (McWilliams et al., 1997), but the effects of surface wave on motions with scales between $O(1\text{ m})$ and $1/4^\circ$ remains relatively unexplored.

Even $1/4^\circ$ -resolution GCMs benefit from knowledge of the surface wave state when their boundary layer turbulence parameterizations depend on the surface wave state (Li et al., 2019). This is also true for air-sea flux parameterizations (Reichl & Deike, 2020) and potentially other parameterizations, such as those for wave-ice interaction.

Open Research

The MOM6 source code including modifications for MOM6-CL is available at <https://github.com/mom-ocean/MOM6>. WAVEWATCH III source code is available from <https://github.com/NOAA-EMC/WW3>. Code and model output used for generating figures are available at <https://github.com/breichl/MOM6CL-Figures> (and will be linked to Zenodo upon acceptance).

Acknowledgments

Without implying endorsement, we gratefully acknowledge discussions and even material assistance from Alistair Adcroft, Brandon Allen, Keaton Burns, Raffaele Ferrari, Glenn Flierl, Baylor Fox-Kemper, Stephen Griffies, Andy Hogg, Adele Morrison, Callum Shakespeare, William Young, and many others — not least of all the late Sean Haney. Be careful, Sean. G.L.W. is supported by the generosity of Eric and Wendy Schmidt by recommendation of the Schmidt Futures program, and by the National Science Foundation under grant AGS-6939393. N.C.C. is supported by the Australian Research Council DECRA Fellowship DE210100749.

We extend additional thanks to Zoom Video Communications for allowing collaboration during the difficult times of the COVID-19 pandemic.

References

- Adcroft, A., Anderson, W., Balaji, V., Blanton, C., Bushuk, M., Dufour, C. O., ... Zhang, R. (2019). The GFDL global ocean and sea ice model OM4.0: Model description and simulation features. *J. Adv. Model Earth Sy.* doi: 10.1029/2019MS001726
- Bosi, S., Broström, G., & Roquet, F. (2021). The role of Stokes drift in the dispersal of North Atlantic surface marine debris. *Frontiers in Marine Science*, 8, 697430. doi: 10.3389/fmars.2021.697430
- Bühler, O. (2014). *Waves and mean flows*. Cambridge University Press.
- Chassignet, E. P., Xu, X., & Zavala-Romero, O. (2021). Tracking marine litter with a global ocean model: Where does it go? Where does it come from? *Frontiers in Marine Science*, 8, 697430. doi: 10.3389/fmars.2021.667591
- Craik, A. D. D., & Leibovich, S. (1976). A rational model for Langmuir circulations. *Journal of Fluid Mechanics*, 73(3), 401–426.
- Cunningham, H. J., Higgins, C., & van den Bremer, T. S. (2022). The role of the unsteady surface wave-driven Ekman–Stokes flow in the accumulation of floating marine litter. *Journal of Geophysical Research: Oceans*, 127(6), e2021JC018106.
- Dobler, D., Huck, T., Maes, C., Grima, N., Blanke, B., Martinez, E., & Arduin, F. (2019). Large impact of Stokes drift on the fate of surface floating debris in the South Indian basin. *Marine Pollution Bulletin*, 148, 202–209.
- Durgadoo, J. V., Biastoch, A., New, A. L., Rühls, S., Nurser, A. J., Drillet, Y., & Bidlot, J.-R. (2021). Strategies for simulating the drift of marine debris. *Journal of Operational Oceanography*, 14(1), 1–12.
- Fan, Y., Ginis, I., & Hara, T. (2009). The effect of wind–wave–current interaction on air–sea momentum fluxes and ocean response in tropical cyclones. *Journal of Physical Oceanography*, 39(4), 1019–1034.
- Fraser, C. I., Morrison, A. K., Hogg, A. M., Macaya, E. C., van Sebille, E., Ryan, P. G., ... Waters, J. M. (2018). Antarctica’s ecological isolation will be broken by storm-driven dispersal and warming. *Nature Climate Change*, 8(8), 704–708.
- Griffies, S. M., Danabasoglu, G., Durack, P. J., Adcroft, A. J., Balaji, V., Böning, C. W., ... Yeager, S. (2016). OMIP contribution to CMIP6: experimental and diagnostic protocol for the physical component of the Ocean Model Intercomparison Project. *Geoscientific Model Development*, 9, 3231–3296. doi: 10.5194/gmd-9-3231-2016
- Huang, N. E. (1979). On surface drift currents in the ocean. *Journal of Fluid Mechanics*, 91(1), 191–208.
- Iwasaki, S., Isobe, A., Kako, S., Uchida, K., & Tokai, T. (2017). Fate of microplastics and mesoplastics carried by surface currents and wind waves: A numerical model approach in the Sea of Japan. *Marine Pollution Bulletin*, 121(1-2), 85–96.
- Johannessen, J., Chapron, B., Collard, F., Rio, M., Piollé, J., Gaultier, L., ... others (2016). GlobCurrent: Multisensor synergy for surface current estimation..
- Kerpen, N. B., Schlurmann, T., Schendel, A., Gundlach, J., Marquard, D., & Hüpgen, M. (2020). Wave-induced distribution of microplastic in the surf zone. *Frontiers in Marine Science*, 7, 590565.
- Kubota, M. (1994). A mechanism for the accumulation of floating marine debris north of Hawaii. *Journal of Physical Oceanography*, 24(5), 1059–1064.
- Large, W. G., McWilliams, J. C., & Doney, S. C. (1994). Oceanic vertical mixing: A review and a model with a nonlocal boundary layer parameterization. *Reviews of Geophysics*, 32(4), 363–403.
- Li, Q., Reichl, B. G., Fox-Kemper, B., Adcroft, A. J., Belcher, S. E., Danabasoglu, G., ... Zheng, Z. (2019). Comparing ocean surface boundary vertical mixing schemes including Langmuir turbulence. *Journal of Advances in Modeling Earth Systems*, 11(11), 3545–3592. doi: 10.1029/2019MS001810

- Longuet-Higgins, M. (1969). On the transport of mass by time-varying ocean currents. In *Deep Sea Research and Oceanographic Abstracts* (Vol. 16, pp. 431–447).
- McWilliams, J. C., Sullivan, P. P., & Moeng, C.-H. (1997). Langmuir turbulence in the ocean. *Journal of Fluid Mechanics*, 334, 1–30.
- Middleton, J. F., & Loder, J. W. (1989). Skew fluxes in polarized wave fields. *Journal of Physical Oceanography*, 19(1), 68–76. doi: 10.1175/1520-0485(1989)019<0068:SFIPWF>2.0.CO;2
- Onink, V., Wichmann, D., Delandmeter, P., & Van Sebille, E. (2019). The role of Ekman currents, geostrophy, and Stokes drift in the accumulation of floating microplastic. *Journal of Geophysical Research: Oceans*, 124(3), 1474–1490.
- Pearson, B. (2018). Turbulence-induced anti-Stokes flow and the resulting limitations of large-eddy simulation. *Journal of Physical Oceanography*, 48(1), 117–122.
- Reichl, B. G., & Deike, L. (2020). Contribution of sea-state dependent bubbles to air-sea carbon dioxide fluxes. *Geophysical Research Letters*, 47(9), e2020GL087267. doi: 10.1029/2020GL087267
- Reichl, B. G., & Li, Q. (2019). A parameterization with a constrained potential energy conversion rate of vertical mixing due to Langmuir turbulence. *Journal of Physical Oceanography*, 49(11), 2935–2959.
- Reichl, B. G., Wang, D., Hara, T., Ginis, I., & Kukulka, T. (2016). Langmuir turbulence parameterization in tropical cyclone conditions. *Journal of Physical Oceanography*, 46(3), 863–886.
- Smith, J. A. (2006). Observed variability of ocean wave Stokes drift, and the Eulerian response to passing groups. *Journal of Physical Oceanography*, 36(7), 1381–1402. doi: 10.1175/JPO2910.1
- Stokes, G. G. (1847). On the theory of oscillatory waves. *Trans. Camb. Phil. Soc.*, 8, 411–455.
- Suzuki, N., & Fox-Kemper, B. (2016). Understanding Stokes forces in the wave-averaged equations. *Journal of Geophysical Research: Oceans*, 121(5), 3579–3596.
- Tamura, H., Miyazawa, Y., & Oey, L.-Y. (2012). The Stokes drift and wave induced-mass flux in the North Pacific. *Journal of Geophysical Research: Oceans*, 117(C8).
- The WAVEWATCH III Development Group (WW3DG). (2016). *User manual and system documentation of WAVEWATCH III version 5.16*. (Tech. Rep. No. 329). NOAA/NWS/NCEP/MMAB.
- Tsujino, H., Urakawa, L. S., Griffies, S. M., Danabasoglu, G., Adcroft, A. J., Amaral, A. E., ... Yu, Z. (2020). Evaluation of global ocean-sea-ice model simulations based on the experimental protocols of the Ocean Model Intercomparison Project phase 2 (OMIP-2). *Geoscientific Model Development*, 13(8), 3643–3708. doi: 10.5194/gmd-13-3643-2020
- Tsujino, H., Urakawa, S., Nakano, H., Small, R. J., Kim, W. M., Yeager, S. G., ... Yamazaki, D. (2018). JRA-55 based surface dataset for driving ocean - sea-ice models (JRA55-do). *Ocean Modelling*, 130, 79–139.
- Van den Bremer, T. S., & Breivik, Ø. (2017). Stokes drift. *Philosophical Transactions of the Royal Society A: Mathematical, Physical and Engineering Sciences*, 376(2111), 20170104.
- Vanneste, J., & Young, W. R. (2022). Stokes drift and its discontents. *Philosophical Transactions of the Royal Society A*, 380(2225), 20210032.
- Van Sebille, E., Aliani, S., Law, K. L., Maximenko, N., Alsina, J. M., Bagaev, A., ... others (2020). The physical oceanography of the transport of floating marine debris. *Environmental Research Letters*, 15(2), 023003.
- Van Sebille, E., Zettler, E., Wienders, N., Amaral-Zettler, L., Elipot, S., & Lumpkin, R. (2021). Dispersion of surface drifters in the tropical Atlantic. *Frontiers in Marine Science*, 7, 607426.
- Wagner, G. L., Chini, G. P., Ramadhan, A., Gallet, B., & Ferrari, R. (2021). Near-inertial waves and turbulence driven by the growth of swell. *Journal of Physical Oceanography*, 51(5), 1337–1351.