

Library of simulated gamma-ray glows and application to previous airborne observations

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Abstract

Gamma-Ray Glows (GRGs) are high energy radiation originating from thunderclouds, in the MeV energy regime, with typical duration of seconds to minutes, and sources extended over several to tens of square kilometers. GRGs have been observed from detectors placed on ground, inside aircraft and on balloons. In this paper, we present a general purpose Monte-Carlo model of GRG production and propagation. This model is first compared to a model from Zhou et al. (2016) relying on another Monte-Carlo framework, and small differences are observed. We then have built an extensive simulation library, made available to the community. This library is used to reproduce five previous gamma-ray glow observations, from five airborne campaigns: balloons from Eack et al. (1996b), Eack et al. (2000); and aircrafts from ADELE (Kelley et al., 2015), ILDAS (Kochkin et al., 2017) and ALOFT (Østgaard et al., 2019). Our simulation results confirm that fluxes of cosmic-ray secondary particles present in the background at a given altitude can be enhanced by several percent (MOS process), and up to several orders of magnitude (RREA process) due to the effect of thunderstorms' electric fields, and explain the five observations. While some GRG can be explained purely by the MOS process, E-fields significantly larger than E_{th} (the RREA threshold) are required to explain the strongest GRGs observed. Some of the observations also came with in-situ electric field measurements, that were always lower than E_{th} , but may not have been obtained from regions where the glows are produced. This study supports the claim that kilometer-scale E-fields magnitudes of at least the level of E_{th} must be present inside some thunderstorms.

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6 **Key Points:**

- 7 • A general-purpose Monte-Carlo model of gamma-ray glow production is presented.
- 8 • Plausible Gamma-ray Glow production conditions are provided for five previous
- 9 airborne observations.
- 10 • Some cases are explained by the MOS mechanism only while other require elec-
- 11 tric fields close to the threshold of the RREA process or above.

Abstract

Gamma-Ray Glows (GRGs) are high energy radiation originating from thunderclouds, in the MeV energy regime, with typical duration of seconds to minutes, and sources extended over several to tens of square kilometers. GRGs have been observed from detectors placed on ground, inside aircraft and on balloons. In this paper, we present a general purpose Monte-Carlo model of GRG production and propagation. This model is first compared to a model from Zhou et al. (2016) relying on another Monte-Carlo framework, and small differences are observed. We then have built an extensive simulation library, made available to the community. This library is used to reproduce five previous gamma-ray glow observations, from five airborne campaigns: balloons from Eack et al. (1996b), Eack et al. (2000); and aircrafts from ADELE (Kelley et al., 2015), ILDAS (Kochkin et al., 2017) and ALOFT (Østgaard et al., 2019). Our simulation results confirm that fluxes of cosmic-ray secondary particles present in the background at a given altitude can be enhanced by several percent (MOS process), and up to several orders of magnitude (RREA process) due to the effect of thunderstorms' electric fields, and explain the five observations. While some GRG can be explained purely by the MOS process, E-fields significantly larger than E_{th} are required to explain the strongest GRGs observed. Some of the observations also came with in-situ electric field measurements, that were always lower than E_{th} , but may not have been obtained from regions where the glows are produced. This study supports the claim that kilometer-scale E-fields magnitudes of at least the level of E_{th} must be present inside some thunderstorms.

Plain Language Summary

Gamma-Ray Glows (GRGs) are high energy radiation originating from thunderclouds, in the MeV energy regime, with typical duration of seconds to minutes, and sources extended over few to tens of square kilometers. In this study, we built a general purpose model of GRG production, including cosmic ray fluxes and enhancement by thunderstorm's electric field, propagation and instrumental response. We use this model to reproduce (simulate) and constrain five previously reported airborne GRG observations, two from balloons and three from aircraft. It is found that all the observations can be explained by one of the two expected regimes, one involving purely particle acceleration (MOS, Modification of Spectrum), and the other one involving also particle multiplication (RREA, Relativistic Runaway Electron Avalanche). According to our simulations, the required

44 large-scale (kilometer) thunderstorm electric fields compatible with the observations are
 45 generally larger than was measured previously.

46 1 Introduction

47 Gamma-Ray Glows (GRGs) are high energy photon radiation originating from thun-
 48 derclouds, with a typical time-scale of a second to minutes, and can extend over an area
 49 of tens of squared kilometers, i.e. the scale of thunderclouds. GRGs can also be referred
 50 as Thunderstorm Ground Enhancements (TGE) by some authors, but we choose to keep
 51 the former terminology for the rest of this article because we are focusing on airborne
 52 observations. A review of the GRG observations and other high energy atmospheric physics
 53 phenomena is provided in Dwyer et al. (2012). GRGs have been observed from detec-
 54 tors placed on ground (typically 0 to 4 km altitude), aircrafts and balloons (typically 4
 55 to 20 kilometers altitude). Ground observations of GRG were reported in Torii et al. (2002);
 56 Tsuchiya et al. (2007); Torii et al. (2009); Brunetti et al. (2000); Chubenko et al. (2000);
 57 Wada et al. (2018) (and references therein), sometimes associates with neutrons, elec-
 58 trons and positron signatures (Babich, 2003; Chilingarian et al., 2010; Gurevich et al.,
 59 2012; Tsuchiya et al., 2012; Chilingarian et al., 2012, 2013; Teruaki et al., 2017). Sev-
 60 eral aircraft-based observations of GRG were reported by Parks et al. (1981); McCarthy
 61 and Parks (1985); Kelley et al. (2015); Kochkin et al. (2017); Østgaard et al. (2019) (see
 62 also references therein). Several balloon-based observations of GRG were reported by
 63 (Eack et al., 1996a, 1996b, 2000). A GRG was also observed preceding a Terrestrial Gamma-
 64 ray Flash and it is proposed that they could be a necessary requirement for TGF pro-
 65 duction, as they can induce enough amplification of a Relativistic Runaway Electron Avalanche
 66 (Smith et al., 2018; Wada et al., 2019). When a leader is developed in a region that al-
 67 ready has the electric field above E_{th} , the leader field will add to it and potentially cre-
 68 ate conditions to produce a TGF.

69 The detected photon spectrum of a GRG is consistent with bremsstrahlung radi-
 70 ation from high energy electrons. Following the original idea of Wilson (1925), electrons
 71 can run away, i.e. get continuously accelerated by electric fields present in thunderclouds,
 72 as the field acceleration overcomes the friction force from the air. It requires appropri-
 73 ate electron energy ε and electric field magnitude E . Following the idea of Gurevich et
 74 al. (1992), the electron population can further grow by the effect of collisions knocking
 75 out other electrons from the medium. This results in a Relativistic Runaway Electron

76 Avalanche (RREA), that is also referred as runaway breakdown in the literature. RREA
 77 triggers with different probabilities for different (ε, E) values, and an evaluation of this
 78 probability distribution is presented in (Lehtinen, 2000; Chanrion et al., 2016; Sarria et
 79 al., 2018), using several models and methods. To be initiated, the RREA process requires
 80 electrons above a given energy threshold ε_c (that are called "seed electrons") and an elec-
 81 tric field above a threshold, the "RREA threshold" of $E_{th} = 284$ MV/km (that scales
 82 inverse proportionally with air density). In the case of GRGs, these seeds come from the
 83 background radiation, i.e. cosmic ray secondaries (extensive air showers). In addition
 84 to the RREA process, a Relativistic Feedback effect (RF) can contribute significantly
 85 to the electron multiplication if the electric field is increased further above E_{th} . The RF
 86 mechanism consists of the possibility for positrons and back-scattering x-rays to come
 87 back inside the avalanche region and consequently induce the production of more RREAs,
 88 that will increase the electron multiplication factor even more. In other words, there will
 89 be an "avalanche" of RREAs. The state of the feedback process is parameterized by a
 90 γ factor, that gives the rate at which the RREAs are multiplied. It has three states :

- 91 • if $\gamma \ll 1$, it just provides a small enhancement of the electron multiplication.
- 92 • if γ is large enough, but < 1 , it can increase the electron multiplication factor by
 93 several orders of magnitude, and reach a steady-state where relativistic electrons
 94 are continuously generated over a long period of time, until an external factor breaks
 95 it.
- 96 • if $\gamma > 1$, the system becomes limited by the number of RREAs that increases
 97 exponentially, and produce a macroscopic number of electrons (theoretically in-
 98 finitely), which produces a current flow that will discharge (partially or fully) the
 99 electric-field region. That is to say, the RREA space charge becomes significant
 100 enough to affect the external field (Dwyer, 2012).

101 Zhou et al. (2016); Bartoli et al. (2018) quantified the variations of both electron
 102 and positron background fluxes reaching a detector located at 4.3 km altitude, as a func-
 103 tion of the electric field of the thundercloud above the detector. The E-field is vertical
 104 with upward values in the -1000 V/cm to +1000 V/cm range (about $\pm 0.6E_{th}$). It was
 105 modeled for a specific geometrical configuration, in order to reproduce observations of
 106 background enhancements observed during thunderstorms by the ARGO-YBJ cosmic
 107 ray detector, located in Tibet. Since the involved electric fields are about 40% below the

108 RREA threshold (i.e. there is no, or marginal electron multiplication), the underlying
 109 mechanism explaining this flux increase (resp. decrease; depending on the sign of the field)
 110 is that the charged particles gain (resp. lose) kinetic energy from the thunderstorm's elec-
 111 tric field, and travel longer (resp. shorter) distances in the air. Therefore more (resp. fewer)
 112 background particles are able to reach the detector, compared to fair weather conditions.
 113 This effect is usually called the "Modification of the Spectrum" (MOS) mechanism (Chilingarian
 114 et al., 2010). Zhou et al. (2016) showed that, in their configuration (electric field set be-
 115 tween 4.3 and 6.3 km altitude), the electron number flux could increase up to a factor
 116 of 2.2 for an electric field of -1000 V/cm (applied potential of 200 MV), and the positron
 117 content could increase up to a factor of 1.8 for electric-field of +1000 V/cm (applied po-
 118 tential of -200 MV). However, the high energy photon content is only increased by fac-
 119 tors of about 1.2 and 1.1 for -1000 V/cm and +1000 V/cm respectively, because they
 120 represent about 92% of the background content (electrons typically 6% and positrons
 121 2%).

122 In section 2, we describe our Monte-Carlo model to simulate the enhancement of
 123 cosmic ray secondary photons, electrons and positrons by thunderstorms' electric fields.
 124 In section 3, we apply this model to independently reproduce the simulation results pre-
 125 sented by Zhou et al. (2016) at mountain altitude and with electric fields below the RREA
 126 threshold, and discuss how the two models compare. In section 4, we presents the re-
 127 sults of our model, when it is extended from 10 to 20 kilometers (aircraft and balloon
 128 altitudes), and to electric fields above the RREA threshold, in order to simulate several
 129 previous airborne gamma-ray glow observations. We discuss the results in section 5, and
 130 we conclude in section 6.

131 2 Monte-Carlo model description

132 We realized a computer model able to simulate and record the effect of thunder-
 133 storm electric fields on the fluxes of cosmic ray secondary particles. The code and final
 134 data products are made freely available on a public online repository, see the Open Re-
 135 search section. Our approach assumes that the glow is not evolving with time and has
 136 a fixed intensity for a given fixed parameter set (the parameters of the models are de-
 137 scribed below). Our model uses the GEANT4 toolkit (Agostinelli et al., 2003; Allison
 138 et al., 2006), version 10.07, that is freely available. It is coupled with the PARMA code
 139 (also freely available, see the Open Research section) that gives us the distributions of

140 cosmic ray secondaries: energy, altitude, and zenith angle, of photons, electrons, positrons,
 141 neutrons and protons (Sato et al., 2008; Sato, 2016). The cosmic ray particles can be sam-
 142 pled at a discrete altitude, or inside a given altitude range. We also integrated the NRLMSISE-
 143 00 model to simulate the atmosphere between 0 and 25 km altitude. GEANT4 is a pow-
 144 erful modular Monte-Carlo simulation toolkit developed by the European Organization
 145 for Nuclear Research (CERN) in association with a worldwide collaboration. It is used
 146 to simulate particle propagation through matter with or without electro-magnetic fields.
 147 The ability of GEANT4 to simulate particle propagation in the context of thunderstorms
 148 and high-energy atmospheric radiation was extensively tested against several custom mod-
 149 els used by the high-energy atmospheric physics community (Skeltved et al., 2014; Rut-
 150 jes et al., 2016; Sarria et al., 2018).

151 PARMA gives estimates of the cosmic-ray spectra of neutrons, protons, muons, elec-
 152 trons, positrons, photons and ions (helium and heavier). It is based on empirical ana-
 153 lytical formulas fitted on the results of runs of the Monte-Carlo code PHITS (Sato et al.,
 154 2008). The later requires quite large resources to run, and PARMA was produced to make
 155 it possible to rapidly compute cosmic radiation doses with a precision equivalent to that
 156 of PHITS. The accuracy of the data provided by PARMA was verified against different
 157 sets of experimental data, taken under various conditions, in a large range of altitudes
 158 (Sato et al., 2018). Later versions of the software extended its validity to higher altitudes
 159 and added angular distributions for the particles.

160 Figure 1 illustrates the geometrical configuration of our simulation. The param-
 161 eters of the model are :

- 162 • H_E : the altitude of the center of the electric field region.
- 163 • ΔH_E : the full (vertical) size of the electric field region, i.e. E is between $H_E -$
 164 $\Delta H_E/2$ and $H_E + \Delta H_E/2$.
- 165 • H_D : the altitude of particle detection (record).
- 166 • ΔU : the total potential difference applied on the electric field region. Positive ΔU
 167 means downward E , i.e. electrons are accelerated upward.

168 In some of the configurations we are using, the electric field may be either in the
 169 MOS regime, or larger than the RREA threshold E_{th} . When the RREA threshold is reached
 170 and exceeded, the Relativistic Feedback (RF) effect will increase its significance as the

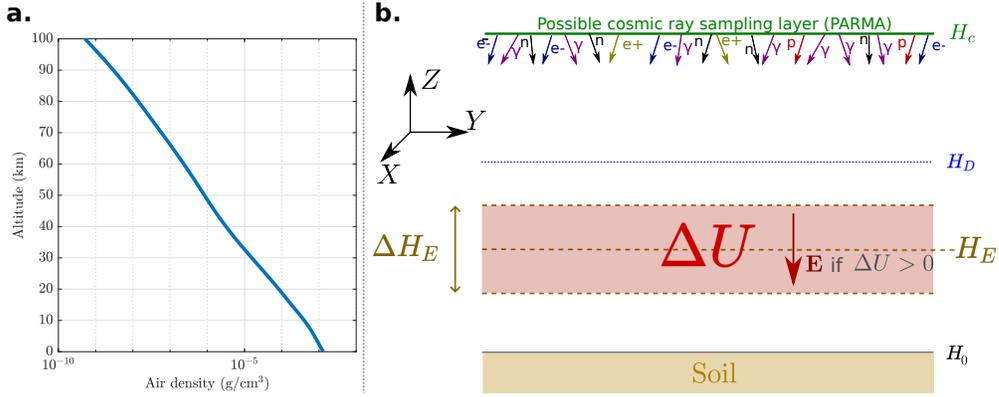


Figure 1. **a.** Altitude as function of atmospheric density given by the NRLMSISE-00 model. **b.** Geometrical configuration of the simulation based on the GEANT4, PARMA and NRLMSISE-00 codes. Initial cosmic rays are generated by the PARMA code at altitude H_C , the particle tracking is done with GEANT4, and the atmospheric densities are obtained from NRLMSISE-00. The electric field layer (in red) is centered at altitude H_E , and has a size ΔH_E that contains a potential difference ΔU (Positive ΔU means electrons accelerated upwards). The detection layer is located at altitude H_D , and is positioned above the electric field region for illustration, but can be set at any altitude between 0 and 25 km. The cosmic-ray sampling layer, represented in green, can also be positioned at any altitude.

171 electric field and so the feedback factor γ increases. We expect 3 simulation states, purely
 172 driven by the high energy Monte-Carlo simulation, i.e. not accounting for disturbances
 173 in the charge structure of the thundercloud that could be due to the production of large
 174 amounts of charged particles. The 3 states are:

- 175 • (i) MOS dominated : the E-field $E < E_{\text{th}}$, gives an increase of path length and
 176 energies of electrons (or positrons for opposite field polarity) that increases their
 177 amounts locally and makes electrons (or positrons) produce more Bremsstrahlung
 178 radiation (but there is no significant multiplication). The expected photon fluence
 179 increase in this case is about several percent to about 20% above background.
- 180 • (ii) RREA dominated: $E \gtrsim E_{\text{th}}$, exponential increase of electrons as function of
 181 time. The multiplication of particles is dominated by the RREA process, and the
 182 increase due to the MOS effect only becomes negligible. Some level of feedback
 183 is also possible but does not dominate the multiplication (i.e. there can be some
 184 positrons or x-rays scattering backwards in the electric field region and produc-
 185 ing extra electrons multiplication). This regime is able to produce photon flux in-
 186 creases from a factor 10 to about several 1000s above background (this is before
 187 absorption that happens between the production region and the detector).
- 188 • (iii) Feedback dominated: $E > E_{\text{th}}$. In this case $\gamma > 1$ and the particle increase
 189 is expected to be able to reach 10^6 or more. This produces an exponential increase
 190 and can be maintained for unlimited time in the simulation (not taking into ac-
 191 count space charges). For this study we fixed a maximum time limit of about 6
 192 avalanche times (estimated from previous knowledge of avalanche rates for given
 193 uniform field E). Note that for significant feedback to occur it is not enough to
 194 have $E > E_{\text{th}}$: one also must satisfy requirements on the volume occupied by the
 195 field (Dwyer, 2012). This regime was not properly explored in this study because
 196 it produces computational problems with our approach, and another approach,
 197 time-driven, is needed (see Skeltved et al. (2014) for an implementation of such
 198 approach)

199 Firstly, a cut-off energy of $\varepsilon_c = 100$ keV was set (this means that particles with
 200 lower energies are discarded), similar to what is used by Zhou et al. (2016), whose model
 201 is compared to our own in the next section. We then used a lower ε_c of 8 keV, because
 202 it is the minimum required electron kinetic energy at which RREA can trigger for E-fields

203 below E_c ($=26$ MV/m at sea level), the critical electric field magnitude for which low-
 204 energy thermal electrons can run away: tracking particles below this ε_c would not change
 205 our simulation results. With electric fields lower than the RREA threshold (that is the
 206 case for the comparison we present in section 3) both 8 keV and 100 keV energy thresh-
 207 olds were tested, and presented similar results. However, when the simulation is extended
 208 to E-fields above the RREA threshold, it can produce a significant change in the results,
 209 as any electrons above $\varepsilon_c = 8$ keV is a potential seed for the RREA process (Sarria et
 210 al., 2018). The value of ε_c is actually dependent on the E-field magnitude, but rather
 211 than using a variable value, it was easier for us to use a single, conservative, lower limit
 212 for ε_c of 8 keV for all our simulations.

213 3 Comparison to previous modeling

214 The first step of this study was to compare our model with results from previous
 215 modeling effort presented in Zhou et al. (2016) and Bartoli et al. (2018). They quanti-
 216 fied, for the first time (to our knowledge), the variations of both electron and positron
 217 background fluxes reaching a detector, as function of the electric field of the thunder-
 218 cloud, located on top of the detector, this last being located on a mountain at 4.3 kilo-
 219 meter altitude. They used a different modeling strategy than us. Their method is fully
 220 based on the CORSIKA code, and starts by sampling high energy cosmic protons at high
 221 altitude, to calculate the distribution of secondary particles by comprehensively simu-
 222 lating the particle showers in the atmosphere. In our model, this part was pre-calculated
 223 by the PARMA based on the PHITS code (see previous section), and we start from lower
 224 altitude sources of photons, electrons, positrons, neutrons and protons, and the track-
 225 ing and interactions of particles is processed by GEANT4. We use the definition that
 226 a positive potential difference ΔU implies a positive electric field pointing downwards,
 227 and therefore electrons accelerated upwards.

228 The configuration used by Zhou et al. (2016) for studying the ARGO-YBJ detec-
 229 tor results, can be reproduced by our model by setting $H_E = 5.3$ km, $\Delta H_E = 2$ km,
 230 $H_D = 4.3$ km. They applied an electric field from -1000 V/cm to 1000 V/cm ($=100$ kV/m),
 231 that is equivalent in our modeling by setting a potential ΔU between -200 and +200 MV
 232 inside the E-field layer, which is about 60% of the RREA threshold for $H_E = 5.3$ km.

233 Figure 2 shows the variation fluxes of electrons and positrons as function of the ap-
 234 plied electric field obtained by Zhou et al. (2016), compared to our model. The bottom
 235 panel shows the relative difference in electron and positron fluxes between the two mod-
 236 els.

237 We can first discuss the flux variations of electrons and positrons. For positive (resp.
 238 negative) electric fields, the electrons (resp. positrons) traveling in the direction of the
 239 detector are decelerated, therefore the detected number of particles is decreasing, down
 240 to about -20% for $E = +100$ kV/m (resp. $E = -100$ kV/m). In this case, the two mod-
 241 els show a very good agreement with less than 5% differences. For negative (resp. pos-
 242 itive) electric fields, the electrons (resp. positrons) traveling in the direction of the de-
 243 tector are accelerated. Therefore the detected number of particles is increasing, up to
 244 about 100% for positrons when $E = +100$ kV/m, and up to 140% for electrons when
 245 $E = -100$ kV/m. The two models show a very good agreement (less than 5% differ-
 246 ence) for $|E| < 60$ kV/m. For larger $|E|$ the models show a larger discrepancy: the dif-
 247 ference goes up to 20% for positrons at $E = +100$ kV/m, and goes up to about 33%
 248 for electrons when $E = -100$ kV/m; our model presenting systematically larger vari-
 249 ations.

250 These differences cannot be attributed to an effect of the cut-off energy ε_c , as we
 251 tested both 100 keV and 8 keV for our model, that lead to similar results. However this
 252 low energy limit is expected to be more significant for larger electric fields, at which the
 253 minimum runaway electron energy drops below the simulation cut-off energy (see sec-
 254 tion 4). It is still unclear to us how the above differences between the two models could
 255 be explained. They are completely independently built: key elements that differ between
 256 them include the physics implementation (GEANT4 and CORSIKA) and cross-sections
 257 for both electro-magnetic and hadronic processes, the atmospheric models, the particle
 258 propagator in the E-fields and to get precise particle records. Both models are valid, within
 259 the uncertainties of their building elements, thus the difference in their results should
 260 be interpreted as the estimate of the level of uncertainty considering the cumulative ef-
 261 fect of all the possible small differences in each of the building elements.

262 In addition of the electron and positron fluxes, our model also provides the vari-
 263 ation of photons fluxes, presented in Figure 2 (black dots), that was not provided by Zhou
 264 et al. (2016). The increases are up to 20% for a $E=-100$ kV/m and up to 10% for $E=+100$ kV/m.

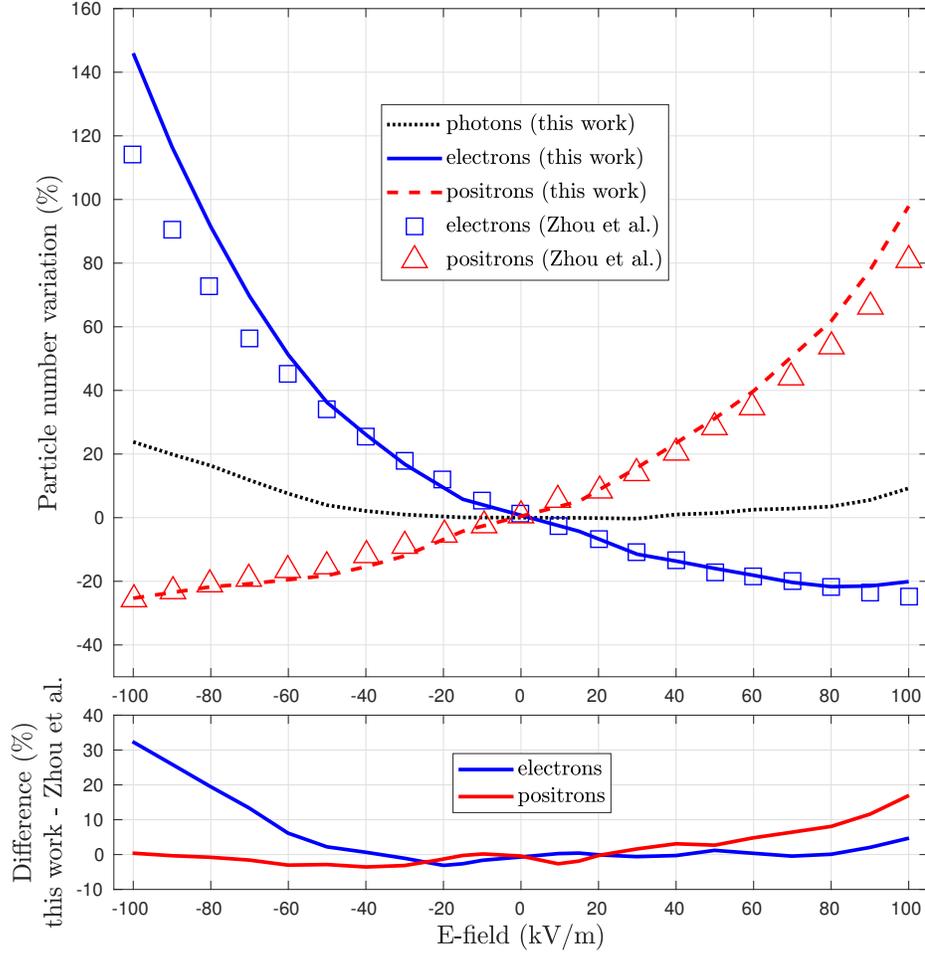


Figure 2. Top panel: fluxes of photons, electrons and positrons at 4.3 kilometers altitude, as function of the applied electric field (E), relatively to the case where no electric-field is present (i.e. background). The maximum electric field tested here, of ± 100 kV/m, corresponds to about 60% of the RREA threshold. The electric field is located between 4.3 and 6.3 km altitude. The results of the model developed for this study are compared with previous results extracted from Zhou et al. (2016). The bottom panel is the relative difference between the two models, for electrons and positrons. Photon flux variations are also shown.

265 In practice, these photons are more important than electrons as they will propagate much
 266 larger distances and are expected to produce the main contribution on GRG when they
 267 are detected by instruments that could be located several kilometers away.

268 4 Application to previous Gamma-Ray Glow (GRG) airborne obser- 269 vations

270 4.1 Simulation of GRGs and instruments

271 Using the model described in the section 2, we built a library of GRG simulations.
 272 It is meant to be used for a large set of observational contexts (ground, aircraft, balloon).
 273 This library is made publicly available, see the data availability section. The library cov-
 274 ers a wide range of parameters:

- 275 • the center of the electric field region located between $H_E = 4$ km and $H_E = 16$ km
 276 altitude. The used altitude grid is [4, 6, 8, 10, 12, 14, 15, 16] (in km)
- 277 • different values of ΔU so that the magnitude of the electric field is tested from 0
 278 to 220 MV, with both polarities. The used potential grid is [$\pm 220, \pm 210, \pm 175, \pm 150,$
 279 $\pm 120, \pm 80, \pm 50, \pm 40, \pm 30, \pm 20, \pm 10, 0$] (in MV).
- 280 • an extension of the E-field region fixed to $\Delta H_E = 2$ km (full length). We could
 281 not test other E-field region lengths because of limited computation time/power
 282 availability.
- 283 • for each case, the particles are recorded in a set of distances from the center of the
 284 electric field region, as a multiplication factor m of $\Delta H_E/2$, so that the detection
 285 altitude is $H_D = H_E + m \Delta H_E/2$. ($\Delta H_E/2$ is always equal to 1 km in this work).
 286 Values of m tested are [0, -1, 1, -2, 2, -3, 3, -4, 4, -5, 5, -6, 6, -7, 7, -8, 8], but
 287 any H_D value below 4 km or above 20 km was not considered.

288 Figure 3 shows a simulation result to illustrate what is contained in the simulation
 289 library. In this case, the E-field center altitude H_E is set to 14 km and all the particles
 290 are recorded at $H_D = 15$ km altitude. Figure 3.a. shows the multiplication factors of pho-
 291 tons, electrons and positrons as function of the applied potential. In this case the pho-
 292 tons can increase by a factor of 260 (compared to background) when the potential reaches
 293 the largest tested value of 220 MV (that is above the RREA theshold of about 125 MV
 294 at this altitude) and a factor of 14 with a potential of -220 MV. At a potential of +125
 295 MV, corresponding to the RREA theshold, the photon background is increased by a fac-

296 tor ≈ 1.7 , the electrons by a factor ≈ 16 , and the positrons are actually reduced by $\approx 20\%$
 297 compared to background (multiplication factor of 0.80), as the electric field make them
 298 gain momentum downwards, away from the detector.

299 In Figure 3.a, for positive potentials (electrons accelerated upwards), the number
 300 of recorded electrons is first due to the MOS mechanism (when $E < E_{\text{th}}$) and then to
 301 the RREA process (when $E > E_{\text{th}}$). Note that a change in the slope of the blue curve
 302 is observed around E_{th} : this is all the more important since the figure shows the vari-
 303 ation in the number of particles on a logarithmic scale. The photon number follows the
 304 increase of electrons due to the bremsstrahlung process. The increase of the number of
 305 positron is due to the pair production mechanism by these created bremsstrahlung (en-
 306 ergetic) photons.

307 In Figure 3.a, for negative potentials (positrons accelerated upwards), the observed
 308 increase of recorded positron number is mostly due to the MOS process on background
 309 positrons (increased kinetic energy and path length). The observed increase of photons
 310 is due to bremsstrahlung by the enhanced positrons. The new photons can produce Comp-
 311 ton electrons, and electron-positron pairs by pair production, that explain the observed
 312 increases.

313 Figure 3 b., c., d., e., f. and g. show, respectively, the photon, electron and positron
 314 spectra for different tested potentials between -220 and +220 MV. When the potential
 315 are increased from 0 to 220 MV, the photon and electron energy spectra evolve towards
 316 a characteristic RREA spectrum, namely power laws with an exponential cut-off. The
 317 number of positrons is increased due to pair production by high energy photons. These
 318 extra positrons have a different, softer, spectrum compared to background positrons, which
 319 are produced by a very different population of energetic photons.

320 When the potential is negative, from -220 to 0 MV, meaning that the electric field
 321 is pointing upwards, RREA is produced downwards and only the back-scattered RREA
 322 photons and their secondaries are detected. This implies the following for large negative
 323 potential (≤ -190 MV) : 1. a harder photon spectrum, i.e. with less pronounced RREA
 324 cut-off 2. a similar electron spectrum, but with a lower intensity for the same absolute
 325 value of potential 3. a positron spectrum much harder, as positrons have gained energy
 326 with the electric field but cannot produce more positrons (unlike electrons) and, like elec-
 327 trons, produce energetic electrons by inelastic scattering (also referred as Møller scat-

328 tering in the literature). To be used at a later stage, these values of particle variations
 329 should be weighted with their amounts in the background: generally about 92% photon,
 330 6% electrons and 2% positrons, which changes with altitude.

331 The measured enhancements above background presented above are also heavily
 332 affected by the characteristics of the instruments detecting them (actually, the final recorded
 333 particles are photons for most of the simulated cases). To be able to compare these sim-
 334 ulation results to real data, the response of the considered instrument must also be taken
 335 into account. In this study we investigated five different observation made with four very
 336 different detectors. For ILDAS and ALOFT missions, the mass models of the instruments
 337 (plus environment) were built closely with the relevant teams during previous studies
 338 (Kochkin et al., 2018; Østgaard et al., 2019). For the balloon observations of Eack et al.,
 339 an approximative GEANT4-based model as been built by us for this study, using infor-
 340 mation provided in Eack (1996); Eack et al. (1996b, 1996a) and Eack et al. (2000). The
 341 GEANT4-based geometrical model takes into account 5 cm diameter by 2 mm thick NaI
 342 scintillation crystal with a 1 mm thick aluminum entrance window, the detector window
 343 foam insulation (2.5 cm), the outer shield, a crude model of the PMT, the helium bal-
 344 loon, the sonde and the electric field meter. In Eack (1996) the NaI crystal is sensitive
 345 from 30 to 120 keV. It is important to understand that this corresponds to deposited en-
 346 ergy into the crystal, but an incident photon with larger energies can also be detected.
 347 Eack et al. (2000) uses essentially the same gamma-ray spectrometer but with a thicker
 348 NaI cristal than increases the sensitivity range to 60-300 keV. In the paper, it is not spec-
 349 ified how much thicker it was, and we assumed it was about twice thicker. A mass model
 350 of the ADELE instrument (and surrounding material) was provided by D.M. Smith (pri-
 351 vate communication), including an approximate model of the Gulfstream-V jet aircraft,
 352 upper/lower NaI and Plastic scintillators, and the lead shielding in-between. Note that
 353 for the ADELE campaign, only the plastic scintillators detected the GRGs since the NaI
 354 detectors operated in trigger mode and did not trigger for GRG observations (but trig-
 355 gered for TGF observations).

356 Table 1 summarizes the five observations that were simulated, including the detec-
 357 tor energy range, the geometrical area of the detectors, and the amount of material sur-
 358 rounding the detector, the altitude of the observation, the observed range of the GRG
 359 maximum increase above background, and the associated reference paper. Each of the
 360 five campaigns' associated papers reported several GRG observation. Table 1 also in-

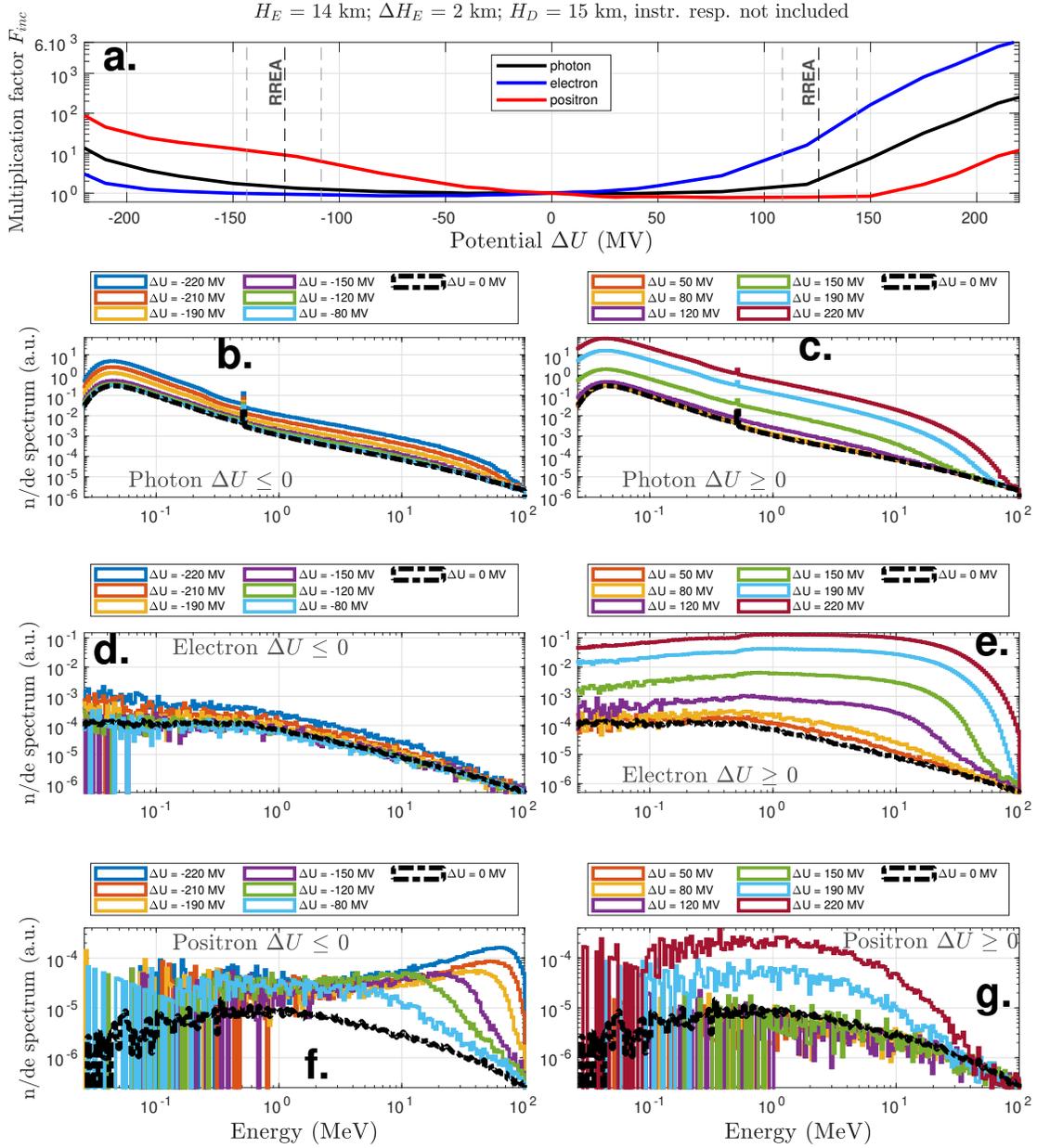


Figure 3. Example of content of the GRG simulation library. The E-field center altitude is set to 14 km, full length (in altitude) is 2 km and the all the particles are recorded at 15 km altitude. **a.** Increase factors of photons electrons and positrons as function of the applied potential. **b. c.** Photon energy spectrum for all the potentials. **d. e.** Electron energy spectrum for all the potentials. **f. g.** Positron energy spectrum for all the potentials. For the spectra, the y-units are arbitrary, but the relative scales between all the spectra and particle types are respected. For potentials close to 0 MV, the spectra are consistent with the ones given by PARMA/EXPACS (Sato et al., 2008). When the potential are increased from 0 to 220 MV, the energy spectra evolves towards a characteristic RREA spectrum that is a power law with an exponential cut-off (E_{th} is for 126 MV for $H_E=14$ km). When the potential evolves in the negative, RREA is produced downwards and only the back-scattered RREA is detected. In addition, the positrons are accelerated

Table 1. Main parameters of the five Gamma-ray Glow observations that were simulated.

Campaign	Detector energy range, MeV	Effective area, cm ²	Altitude, km	Flux increase factor F_{inc}	Surrounding material
Eack-1996 ^a	0.03-0.12	78	15	3-50	light ^f
Eack-2000 ^b	0.06-0.3	156	14	1.6-3	light ^f
ADELE ^c	0.05-5	161.3	14-15	1.2-10	heavy ^g
ILDAS ^d	0.1-10	23	12	3-20	heavy ^h
ALOFT ^e	0.3-30	225	20	1.2-1.45	heavy ⁱ

^aEack et al. (1996b). ^bEack et al. (2000). ^cKelley et al. (2015).

^dKochkin et al. (2017). ^eØstgaard et al. (2019).

^f foam close to NaI crystal, electronics, shielding, covering, balloon and electric field meters (far way).

^gGulfstream-V aircraft. ^hA340 aircraft. ⁱER-2 aircraft.

361 dicates the amount of material around each detector: it is very important in the sim-
362 ulation to take that into account, at least approximately. Indeed, more material means:
363 1. more absorption of the x/gamma-rays. 2. more interactions for the energetic electrons
364 and positrons (above several MeV) therefore producing more bremsstrahlung radiation.
365 3. more positrons being stopped therefore more 511 keV photons being produced by positron
366 annihilation.

367 Note that there is an additional GRG observation by Eack et al. (1996a) that we
368 did not consider in this work. It reported a GRG detected at 4 km altitude with an in-
369 crease above background of about a factor 100. This was completely out-of-scope of what
370 our model was able to produce in the tested potential range (-220 to +220 MV). It would
371 have required extremely high potential, largely above the RREA threshold.

372 Using GEANT4, we calculated effective areas, or equivalently detection efficiencies
373 as function of energy, for photons, electrons and positrons; that is only what is needed,
374 as we will work with relative increases over background only. The used instrumental re-
375 sponses for the five detectors, in the form of effective area curves, for vertically incident
376 photons, electrons and positrons, are provided in the supplementary material. For sim-
377 plicity, we did not consider responses as a function of the incoming angle, and assumed
378 always vertical. It is important to note that, for most cases, the detected particles are

379 overwhelmingly photons, as they are able to propagate long enough distances and/or pen-
 380 etrate shielding material (plane structure, detector shielding).

381 The response functions are used together with the simulated photons, electron and
 382 positron spectra resulting from the (described above) GRG simulation library, and a rel-
 383 ative increase of detector counts with respect to background (noted F_{inc}) is determined.
 384 If there is no increase over background, $F_{\text{inc}} = 1$. The values of F_{inc} were calculated
 385 at each altitude-potential grid point (see previous section), and values in-between were
 386 obtained using bi-linear interpolation on $\log(F_{\text{inc}})$.

387 4.2 Results

388 Figures 4, 5, 6, and 7 summarizes our final simulation results for glow observations
 389 by Eack 1996 and 2000 (Eack et al., 1996b, 2000), ADELE (Kelley et al., 2015), ILDAS
 390 (Kochkin et al., 2017). The case of ALOFT is shown in Østgaard et al. (2019), Figure
 391 9, that was obtained with an earlier version of the same models used here (GRG pro-
 392 duction/propagation, and detector response). Figures 4, 5, 6, and 7 show level curve plots
 393 of F_{inc} , as function of the center-altitude of the E-field region (H_E), and the applied po-
 394 tential (ΔU). As indicated previously, the E-field region has a 2 kilometers full length
 395 (ΔH_E) for any center-altitude. The red line is the detection altitude of the given obser-
 396 vation (where the response of the given instrument is applied). The blue curves indicate
 397 the RREA threshold E_{th} that is function of H_E and ΔU : a large increase of F_{inc} is ex-
 398 pected above it. The green area is where the flux increase is within the ranges of val-
 399 ues are given in Table 1. A gray area indicates excluded part of the parameter space due
 400 to the approximation location of the cloud top.

401 Figure 4 shows the simulation result corresponding to conditions of the observa-
 402 tions presented in Eack et al. (1996b). For this observation at 15 km altitude, the bal-
 403 loon was above the thunderstorm, therefore compatible configurations for higher altitudes
 404 can be ignored. Our simulation shows that both positive and negative potentials above
 405 $|E_{\text{th}}|$ can explain the observed count increase above background, and there are compat-
 406 ible configurations for any H_E above 12.5 km, with the appropriate potential. For an
 407 electric field region closer to the detection altitude, it is easier to have a large F_{inc} . The
 408 lowest required configuration to have F_{inc} of 3 is an electric field located between 13 and
 409 15 km altitude ($H_E = 14$ km) with a potential of about +120 MV inside, that is slightly

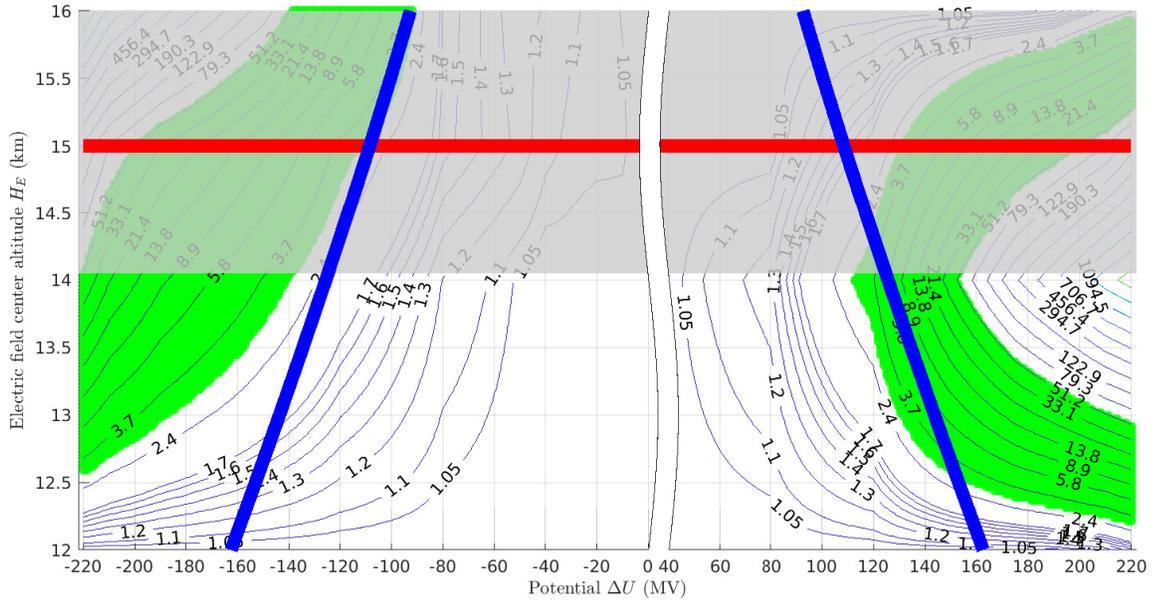
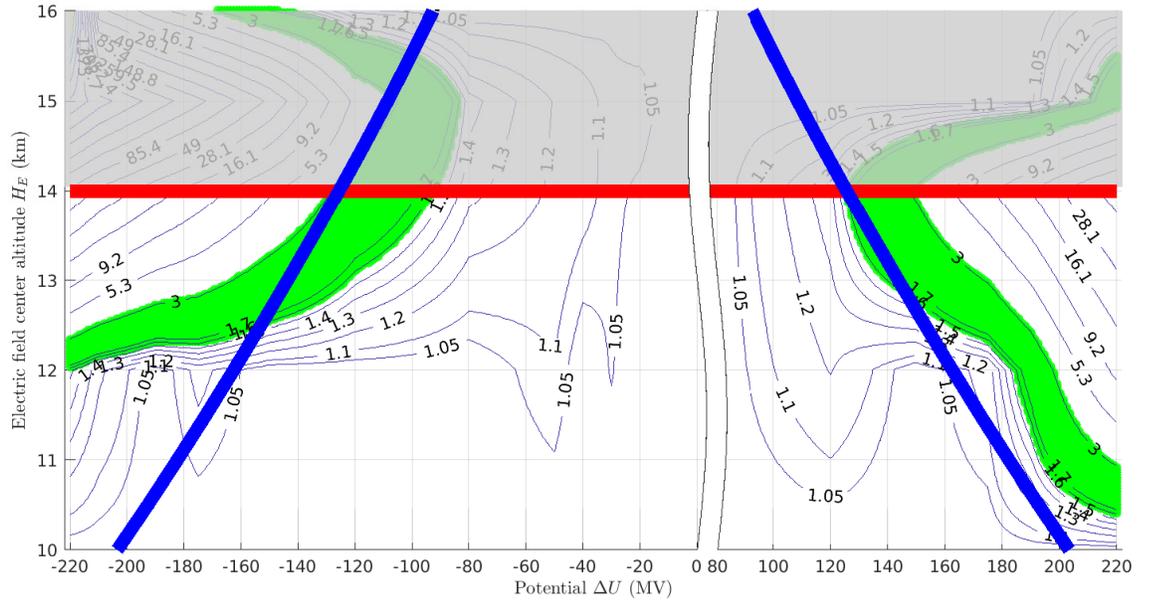


Figure 4. Level curves of detector counts multiplication factors (F_{inc}) as function of E-field center altitude and applied potential for results of the Eack 1996 campaign (Eack et al., 1996b). The extension of the electric field region (ΔH_E) is always 2 km. The red line is the detection altitude of the given observation. The blue curves indicate the RREA threshold E_{th} . The green area indicates where the observed flux increase is compatible with the observation. The gray area indicates a part of the parameter space than can be excluded.



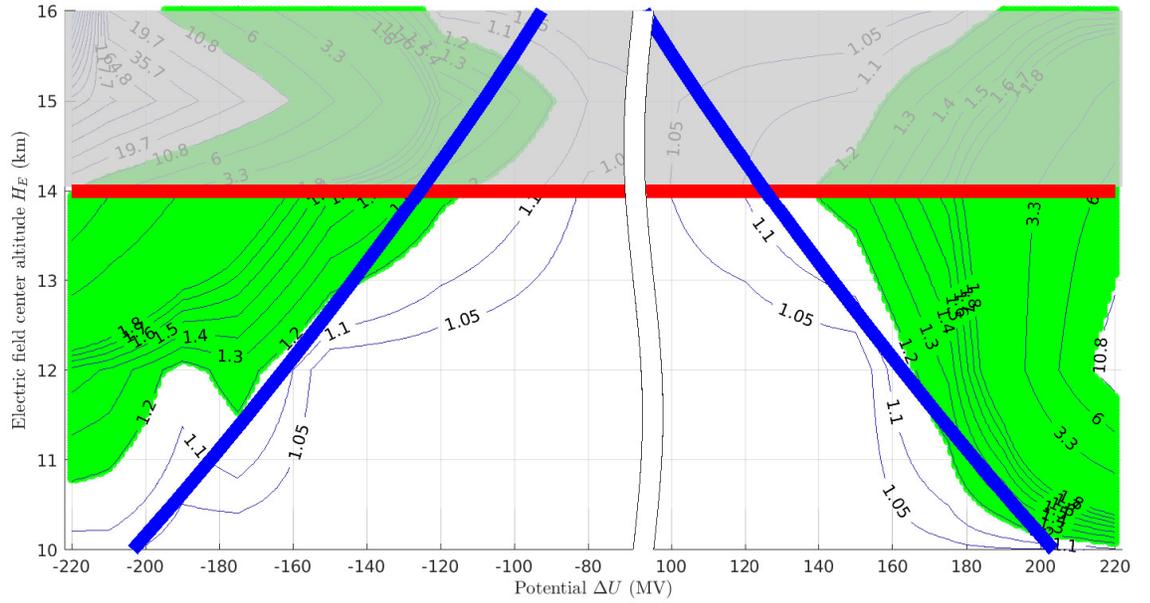


Figure 6. Level curves of detector counts multiplication factors (F_{inc}) as function of E-field center altitude and applied potential for results of the ADELE campaign (Kelley et al., 2015). The extension of the electric field region (ΔH_E) is always 2 km. The red line is the detection altitude of the given observation. The blue curves indicate the RREA threshold E_{th} . The green area indicates where F_{inc} is compatible with the observation. The gray area indicates a part of the parameter space than can be excluded.

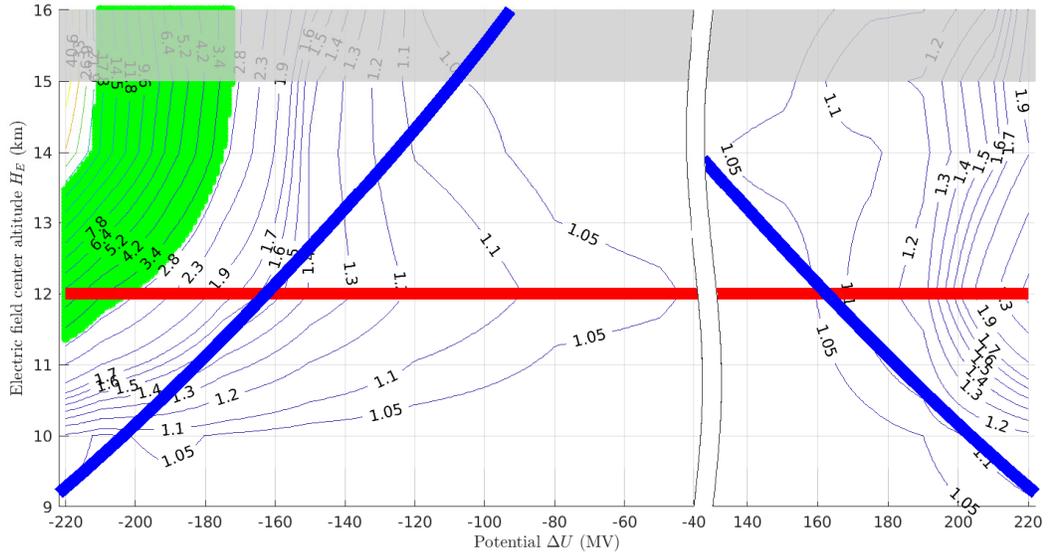


Figure 7. Level curves of detector counts multiplication factors (F_{inc}) as function of E-field center altitude and applied potential for results of the ILDAS campaign (Kochkin et al., 2017). The extension of the electric field region (ΔH_E) is always 2 km. The red line is the detection altitude of the given observation. The blue curves indicate the RREA threshold E_{th} . The green area indicates where F_{inc} is compatible with the observation. The gray area indicates a part of the parameter space than can be excluded.

410 below E_{th} . This configuration is the most favorable for glow production, as the electrons
 411 get a 2 km long acceleration region and are recorded exactly at the end of it. In order
 412 to produce an increase that has the same magnitude as the strongest glow observed in
 413 the paper ($F_{\text{inc}} \approx 50$), a potential of 160 MV is required, that is 1.3 times the RREA
 414 threshold (E_{th}) at 14 km altitude, and increases to 220 MV ($1.6 E_{\text{th}}$) just 1 km below.
 415 Eack et al. (1996b) also reports a measurement of the electric field magnitude, that shows
 416 an electric field always far below E_{th} , and mostly located between 2 and 11 km altitude,
 417 that is out of range of the E-field location required by our simulations.

418 Figure 5 shows the simulation result concerning the observations presented in Eack
 419 et al. (2000). For this case, the balloon is at 14 km altitude, most likely above the thun-
 420 dercloud region (and electric field) therefore the compatible configurations for altitudes
 421 above it can be ignored. H_E located between 10.5 and 14 km altitude can produce a com-
 422 patible F_{inc} between 1.6 and 3, as observed. The minimal required ΔU is also 120 MV
 423 for H_E at the same altitude level as the detector, and a potential up to 200 MV is re-
 424 quired for $H_E = 11$ km. For lower altitudes, very large un-tested potential are required
 425 ($|\Delta U| > 220\text{MV}$). In this case, the MOS mechanism (E-field below E_{th}) can explain
 426 all the observed fluxes for negative potentials, assuming the balloon is inside, or very close
 427 to the E-field region. The largest flux increase can be explained for ΔU corresponding
 428 to 1.3 times the RREA threshold (E_{th}) at a center altitude of 12 km. Both Eack et al.
 429 (2000) and Eack et al. (1996b) observations were made above continental US (Kansas,
 430 Oklahoma), and therefore E-field regions above 14 km altitude are unlikely.

431 Figure 6 shows the simulation result concerning the observations by the ADELE
 432 instrument presented in Kelley et al. (2015) by the plastic detectors on-board a Gulfstream-
 433 V aircraft. In this case the observed glows, with F_{inc} between 1.2 and 10 can also be ex-
 434 plained with a large interval of H_E between 10 to 16 km, above, below or at the level of
 435 the aircraft. As for the previous cases, compatible F_{inc} can be obtained when the E-field
 436 is close to E_{th} . For F_{inc} to increase from 1.2 to 10, a raise of 80% of ΔU is necessary,
 437 meaning an electric field significantly above E_{th} . The reported observations were also
 438 obtained above continental US (Colorado and Florida) and radar data indicating a cloud
 439 top close to 14 km altitude is mentioned for one even.

440 Figure 7 shows the simulation result concerning the observations by the ILDAS LaBr₃-
 441 based X/gamma-ray detector located inside an A340 aircraft, presented in Kochkin et

442 al. (2017). The article indicates that the cloud top height is close to 15 km altitude, so
 443 values above this can be ignored. In this case, we see that compatible values of F_{inc} can
 444 be only produced using negative potentials. With negative potentials, the electrons are
 445 accelerated downwards and therefore the E-field region (and its center altitude H_E) should
 446 be above the aircraft (located at about 12 km altitude). Compared to previous obser-
 447 vations, the minimal potential condition to reproduce the observed F_{inc} of 3 is to have
 448 a potential of $< -170\text{MV}$ at 14 km altitude, that is 25% above the RREA threshold
 449 (E_{th}). To reproduce the maximum observed F_{inc} of about 20, a potential $< -210\text{ MV}$
 450 is required, that is very large ($1.75 E_{\text{th}}$).

451 The case of ALOFT is shown in Østgaard et al. (2019), that was obtained using
 452 an earlier version of the models presented here (glow generation, propagation and instru-
 453 ment response). This campaign contained BGO detectors inside the pod of a ER-2 air-
 454 craft flying at 20 km altitude. The figure shows simulation results of a GRG detected
 455 at 20 km altitude with a source H_E between 9 and 12 km altitude. In this case ΔH_E
 456 was also 2 km. It was showed that only negative ΔU (electrons accelerated upwards) gave
 457 possible solutions as positive ΔU could lead to a background increase larger than the sim-
 458 ulation noise level. Note that we inverted the polarity definition here, compared to Østgaard
 459 et al. (2019)). Possible solutions have H_E between 9 and 12 km due to constraints com-
 460 ing from other measurements (see description in Østgaard et al. (2019)), and higher al-
 461 titudes were not tested as they are incompatible with the measured cloud top. In this
 462 altitude range, it was shown that the required potential to produce a glow with a F_{inc}
 463 between 1.1 and 1.45 is about 20% to 25% above the RREA threshold. This study also
 464 included spectral analysis, but the biggest constraint on H_E and ΔU was actually ob-
 465 tained from F_{inc} only, as compatible energy spectra were contained inside a fairly large
 466 parameter area.

467 5 Discussion

468 In the previous section, we showed that some glow observations can be explained
 469 by electric-fields only in the MOS regime, while some other observations require E to
 470 be at least at the level of the RREA threshold E_{th} . The latter corresponds to large elec-
 471 tric field magnitude, that were never observed, to our knowledge. Eack et al. (1996b) could
 472 measure the electric field magnitude when the balloon was moving upwards inside, or
 473 around the thunderstorm. The on-board E-field meter measured an electric field of about

474 50 kV/m at 9 km altitude (see Figure 1 of Eack et al. (1996b)), that corresponds to a
 475 potential of 50 MV in our case (assuming a total E-field length of 2 km), that is about
 476 44% of the RREA threshold. However, this is a point measurement, limited to a specific
 477 narrow region of the cloud, while the balloon was climbing in altitude. There is no ev-
 478 idence that larger electric fields could not be present somewhere else inside the cloud.

479 Both Eack et al. (2000) and Eack et al. (1996b) observations were made above con-
 480 tinental US (Kansas, Oklahoma), and therefore E-field regions above 14 km altitude are
 481 highly unlikely. The highest possible E-field region could be between the upper positive
 482 charge region and a negative screening layer; or inverted for an anomalous charge sys-
 483 tem. In Østgaard et al. (2019), the reported glow observation was also made over con-
 484 tinental US (Colorado) the upper cloud layer was reported to be at about 13 km alti-
 485 tude by the on-board Cloud Physics Lidar instrument. Therefore, for Eack et al. (2000)
 486 and Eack et al. (1996b) observations, scenarios with H_E around 12 km and E-fields above
 487 the RREA threshold are the most likely.

488 In Østgaard et al. (2019), extensive electric field and lightning activity measure-
 489 ment from ground and front the airplane were available. It was shown that the cloud po-
 490 larity is most probably anomalous (positive), that means a large-scale electric field ac-
 491 celerating electrons downwards, that seems incompatible with the simulated GRG pro-
 492 duction scenario inside the cloud (as the detector was located above the cloud at 20 km
 493 altitude). We see two possible solutions to this issue: 1. even if the main thunderstorm
 494 structure is inverted (anomalous), the whole structure could be more complex and have
 495 somewhere a sub-charge structure with the correct polarity and a strong enough poten-
 496 tial difference. 2. Østgaard et al. (2019) presents an alternative glow production scenario
 497 where the glow is produced by a large-scale electric field between the cloud top and the
 498 ionosphere. The problem with this scenario is that the electric field measurements from
 499 the onboard instrument did not report a strong enough E-field.

500 As written in the previous section, for the ADELE and ILDAS observations, large
 501 potential values of $1.75 E_{th}$ to $1.8 E_{th}$ are necessary to explain largest F_{inc} observed. Such
 502 values are quite challenging to explain for real thunderstorm conditions, as it is not clear
 503 if such high potential can be reached before it dropping due to the movement of charges
 504 and ions. In addition, as already mentioned in section 4, there is an additional GRG ob-
 505 servation by Eack et al. (1996a) that we were not able to reproduce in this work. The

506 glow was detected at 4 km altitude with an increase above background of about a fac-
 507 tor 100. This is completely outside of what our model is able to produce as it probably
 508 requires extremely high potential, largely above the RREA threshold that we could not
 509 test, due to limitations of our simulation code in its current version. This case would be
 510 in the simulation state (iii), as described in section 2. In this state, the relativistic feed-
 511 back dominates the contribution to F_{inc} , and our simulation would require a more so-
 512 phisticated management of a time step and limit in order to work properly. As discussed
 513 above, it is important to stress that the existence, in real life, of such high potential con-
 514 ditions (i.e. larger than the RREA threshold) is questionable, but remains an open ques-
 515 tion. For a discussion of maximum possible E-fields in thunderstorms, see Dwyer (2003).
 516 For a review of measurements see Stolzenburg and Marshall (2008), that always reports
 517 the E-fields at the edge or below the RREA threshold E_{th} .

518 For the cases requiring potentials more than 2 times the RREA threshold, another
 519 production mechanism could be responsible for the GRG production. It is possible that
 520 the mechanism presented here, purely based on thunderstorms' E-fields affecting the cosmic-
 521 ray background, can explain all the high altitude GRG observations (i.e. above 10 km
 522 altitude); but lower altitude glow, like in Eack et al. (1996a) at 4 km altitude, and some
 523 ground observations, may require another mechanism. This mechanism could be based
 524 on the afterglow of X/gamma-ray produced by radioactive isotopes disintegration (Teruaki
 525 et al., 2017; Bowers et al., 2017; Babich, 2017; Rutjes et al., 2017; Wada et al., 2020);
 526 where the isotopes could be a consequence of a Terrestrial Gamma-ray Flash. In this sce-
 527 nario, glow durations of several tens of minutes were shown possible according to sim-
 528 ulations by Diniz et al. (2021), using RREA seeding from β^+ decay particles. This in-
 529 volves that the observation from Eack et al. (1996a) at 4 km altitude could have been
 530 preceded by a TGF, that was not reported (while the opposite, a TGF produced at the
 531 termination/end of a GRG, was reported in Wada et al. (2019)).

532 6 Conclusions and future work

533 We presented a general Monte-Carlo GEANT4-based model of Gamma-ray Glow
 534 (GRG) production. This model was compared to another, completely independent, model
 535 from Zhou et al. (2016) relying on another Monte-Carlo framework and small differences
 536 were observed. By running our model, we build an extensive simulation library made avail-
 537 able to the community (see the Open Research section). This library was used, together

538 with several instrumental responses, to simulate (reproduce) five previous gamma-ray
 539 glow airborne observations. These observations are from five campaigns: balloons from
 540 Eack et al. (1996b), Eack et al. (2000); and aircrafts from ADELE (Kelley et al., 2015),
 541 ILDAS (Kochkin et al., 2017) and ALOFT (Østgaard et al., 2019).

542 We confirmed that fluxes of cosmic-ray secondary photons, electrons and positrons
 543 at a given altitude can be multiplied by several tens of percent to orders of magnitude
 544 due to thunderstorms' electric fields (if available potential differences are large enough),
 545 and therefore explain the GRG observations mentioned above. We showed that some GRG
 546 can be explained purely by the MOS process, while E-fields significantly larger than E_{th}
 547 are required to explain the strongest ones. Some of the observation also came with par-
 548 tial electric field measurements, that reported measurements always much lower than the
 549 RREA threshold. These measurements were sparse, and there is no guarantee that they
 550 measured the region of the thundercloud with the highest E-fields, where the GRGs are
 551 produced. This study shows evidence that there must be E-fields with magnitude equal
 552 or larger than E_{th} inside thunderstorms. To find them, more observations are required,
 553 possibly with an array of several balloons and/or aircraft, and ground electric field and
 554 radio measurements, in order to get a complete picture of a thundercloud system pro-
 555 ducing a GRG.

556 In the literature, two quite different GRG observations were reported, described
 557 as positron events, showing glows with a strong enhancement of the 511 keV line (Dwyer
 558 et al., 2015; Kochkin et al., 2018). It is possible to investigate these two cases using the
 559 same modeling strategy as presented here. However they will require a deeper investi-
 560 gation by looking closely at the recorded energy spectra (after applying instrumental re-
 561 sponse) for an excess of the 511 keV annihilation line. Thankfully, both ADELE and IL-
 562 DAS could measure spectra with several energy bins. This will be the subject of a future
 563 work.

564 In this work, we focused on airborne observations, but many GRGs were observed
 565 from ground (see introduction). Our model could be used in order to try to reproduce
 566 and explain these observations as well. Even if some measurements are at sea level (e.g.
 567 Wada et al. (2019)), some are also from mountain altitudes. The provided simulation
 568 library uses a ground at sea level, and therefore would not be able to be used for moun-
 569 tain observations (e.g. Tsuchiya et al. (2007); Chilingarian et al. (2010)) as it is, and would

570 require a more specific simulation set-up (including back scattering from particles hit-
571 ting the ground).

572 **Open Research**

573 The model presented in section 2 is available in the following repository: [https://](https://doi.org/10.5281/zenodo.7129586)
574 doi.org/10.5281/zenodo.7129586. There is no specific documentation, so we suggest
575 the reader to read the documentations of GEANT4 and PARMA, and to contact David
576 Sarria (david.sarria@uib.no) for more information. Note that the code uses the PARMA
577 fortran code that is available here: <https://phits.jaea.go.jp/expacs/>, with the as-
578 sociated documentation.

579 The glow simulation library is provided in the following repository: [https://doi](https://doi.org/10.5281/zenodo.7129650)
580 [.org/10.5281/zenodo.7129650](https://doi.org/10.5281/zenodo.7129650), and comes with documentation in order to be usable
581 by other researchers.

582 All the data directly presented in this article, together with the used instrumen-
583 tal responses, can be obtained in the following repository: [https://doi.org/10.5281/](https://doi.org/10.5281/zenodo.7129672)
584 [zenodo.7129672](https://doi.org/10.5281/zenodo.7129672).

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