Ensemble Calibration and Uncertainty Quantification of Precipitation Forecasts for a Risk-based UTM

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Abstract

Uncertainty on precipitation forecasts results in major high cancellation rate in Unmanned Aircraft Systems operations and reduces the benefits of BVLOS operations in terms of risk-based contingency planning. Hence, quantifying and reducing the uncertainty on precipitation forecasts will reduce mission uncertainties, avoid accidents and make the integration of UAS into the National Airspace System more efficient and reliable. To achieve this goal, the Member-By-Member post-processing technique is used to calibrate a probabilistic forecast composed of 20 members of precipitation rate over South Florida during summer period. The Continuous Ranked Probability Score (CRPS) of the ensemble is minimised to achieve the optimal regression between ensemble members without any assumption on the forecasted parameter. The radar data from the Multi-Radar/Multi-Sensor (MRMS) is used to correct ensemble spread every 10 min and reduce forecasting uncertainty. A multi-physics ensemble was used to generate high-resolution, convection resolving/allowing 48-hours forecasts. The calibration was obtained over a learning process over the simulated period over 3 years. The comparison between the raw and calibrated ensemble from unseen data is presented in terms of bias correction and ensemble reliability. The calibration was able to correct the bias found in raw probabilistic forecasts relative to MRMS data. The comparison with precipitation data from tipping buckets over four airports over South Florida revealed that the calibrated ensemble tends to overestimate the precipitation rates mainly because of the particles evaporation that is taking place under radar beam.

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5

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8 Aircraft Systems operations and reduces the benefits of BVLOS operations in terms of risk-
9 based contingency planning. Hence, quantifying and reducing the uncertainty on precipitation
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13 members of precipitation rate over South Florida during summer period. The Continuous Ranked
14 Probability Score (CRPS) of the ensemble is minimized to achieve the optimal regression
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18 resolution, convection resolving/allowing 48-hours forecasts. The calibration was obtained over
19 a learning process over the simulated period over 3 years. The comparison between the raw and
20 calibrated ensemble from unseen data is presented in terms of bias correction and ensemble
21 reliability. The calibration was able to correct the bias found in raw probabilistic forecasts
22 relative to MRMS data. The comparison with precipitation data from tipping buckets over four
23 airports over South Florida revealed that the calibrated ensemble tends to overestimate the
24 precipitation rates mainly because of the particles evaporation that is taking place under radar
25 beam.

26 **Plain Language Summary**

27 The uncertainty on precipitation forecasts is a very important information for contingency
28 planning within the framework of Beyond Visual Line Of Sight (BVLOS) Operations of
29 Unmanned Aircraft Systems (UAS) and UAS Traffic Management (UTM) systems. In this
30 article, forecasts uncertainty is reduced using ensemble calibration techniques using merged
31 radar data over South Florida. This technique optimizes regression coefficients by learning from
32 historical data and minimizing the difference between observations and forecasts and we show
33 that thanks to the calibration, the ensemble becomes more reliable and the bias of the calibrated
34 ensemble improved. The comparison between precipitation forecasts and ground-based data
35 over airports revealed an improvement the forecasts, as the calibration is very sensitive to the
36 used radar observations.
37

38 **Introduction**

39 Rain of different amplitudes accompanied by thunderstorms, reduced visibility and wind gusts
40 are non-negligible threat to small Unmanned Aircraft Systems (sUAS). These precipitations are
41 also a major cause of UAS flights cancellation as operators because flying during wet conditions
42 is still conservative, which pose a genuine challenge to the business model of multiple
43 companies relying on BVLOS operations (Campbell et al. 2017). Moreover, precipitations can
44 cause lost-link hazard which also make the BVLOS operations less efficient. In addition,
45 contingency planning related to lost-link hazards is highly impacted by deterministic assessment
46 of precipitation because it requires weather uncertainty information, uncertainty on precipitation
47 forecasts in particular. To solve this problem, Campbell et al. 2017 suggested two main
48 recommendations: 1) quantify forecasts uncertainty and 2) investigate new solutions to reduce
49 these uncertainties.

50 Within this risk-based planning approach, ensemble forecasting is widely used to provide more
51 accurate forecasts and uncertainty information (Gneiting & Katzfuss, 2014). In fact, the
52 ensemble mean is generally used as the forecast and the ensemble standard deviation or spread as
53 the forecast uncertainty. However, systematic errors make forecasts 'certainty and accuracy
54 strongly degrade and their reliability decreases as a function of lead times as the ensembles
55 become very overconfident (under-dispersive) as shown in Nicolis et al. 2009 and Leutbecher
56 and Palmer 2008.

57 Foretunately, these forecasting issues can be solved using ensemble post-processing and
58 calibration. Multiple studies used different calibration techniques to improve probabilistic
59 forecasts of vector or scalar variables (Pinson, 2012, (Vannitsem, 2009; Van Schaeybroeck and
60 Vannitsem, 2011, 2012).

61 Two approaches exist today to calibrate an ensemble of forecasts. The first method is 'statistical'
62 such as logistic distribution used in Wilks, 2009; Schmeits and Kok, 2010; Roulin and
63 Vannitsem, 2012 or Non-homogeneous Gaussian Regression used in Gneiting et al., 2005;
64 Hagedorn et al., 2008. However, these techniques are generally based on random sampling from
65 assumed predictive distributions and ignore spatial and temporal correlations and cross-
66 correlations as shown in Van Schaeybroeck and Vannitsem 2015. The second approach adopted
67 in this work is member by member (MBM) independent calibration by which every member is
68 individually calibrated in order to retain correlation correlations (Van Schaeybroeck and
69 Vannitsem 2015).

70 In the MBM approach, Different cost functions and fitting procedures exist: Bayesian Model
71 Averaging (BMA) used by Raftery et al. 2005; Sloughter et al. 2010. Other studies such as
72 Bröcker and Smith 2007 used likelihood maximization with the logarithm loss but showed that
73 this method fails to produce accurate calibrated members. However, the mentioned techniques
74 are mainly based on strong assumptions and do not offer strong guarantees on ensemble
75 improvement. The continuous ranked probability score (CRPS) is the squared difference between
76 the cumulative distribution functions of the ensemble forecast and the observation was used by
77 Thorey et al. 2018, Gneiting et al. 2005, Gebetsberger et al. 2017 as a cost function to minimize
78 and obtain calibrated forecasts as it does not need a theoretical assumption regarding parameters
79 distribution.

80   The goal of this paper is to show how ensemble-spread correction using CRPS minimization
81   relative to the Multi-Radar Multi-Sensor (MRMS) precipitation data over multiple years yield to
82   an improvement of the predictions and evaluate the performance of probabilistic forecasts of
83   precipitation by comparison to precipitation observations over airports. In this study, we start
84   with 20-members ensemble of precipitation forecasts and apply a MBM calibration approach
85   developed by Schaeybroeck et al. 2015 to improve the probabilistic forecasts of a precipitation
86   event in South Florida.

87

88   This paper is structured as follows: section 1 describes the calibration method. Section 2
89   discusses the simulated use case, the simulation setup and ensemble building, and the datasets
90   used in the calibration and evaluation. Section 3 explains the evaluation method. Section 4
91   discusses the results and evaluation findings.

92

93   **1. Ensemble Calibration**
94   **1.1. MBM post-processing method**

95   Following Schaeybroeck and Vannitsem 2015, the calibrated ensemble of M members at time n
96    $X_{C,n} = \left(X_{C,n}^m\right)_{1 \leq m \leq M}$ can be expressed as a function of the raw ensemble $X_n = (X_n^m)_{1 \leq m \leq M}$ as
97   shown in Equation 1where $\overline{X}_n$ is the ensemble-mean, α is the bias parameter, β represents the
98   ensemble-mean scale parameter. The parameter τ_n defined in Equation 2 is the spread tuner or
99   adjuster of the corrected ensemble while ϵ_n defined in equation 4 represents the deviation from
100   the mean of the uncorrected ensemble. $\langle . \rangle_m$ denotes the ensemble average. The standard
101   deviation of the corrected ensembles is used as a spread measure of the corrected forecasts to
102   quantify the uncertainty of the forecasts.

103

104                        $$X_{C,n} = \alpha + \beta \overline{X}_n + \tau_n \epsilon_n \qquad (1)$$

105                        $$\tau_n = \gamma_1 + \gamma_2 \delta_n^{-1} \qquad (2)$$

106                $$\delta_n = \left\langle \left\langle \left| X_n^{m_1} - X_n^{m_2} \right| \right\rangle_{m_1} \right\rangle_{m_2} \qquad (3)$$

107                        $$\epsilon_n = X_n - \overline{X}_n \qquad (4)$$

108   **1.2.CRPS minimization**

109

110   The parameters (α, β, γ1, γ2) are estimated through regression learning through the same time
111   over 3 years by the minimization of the associated Continuous Ranked Probability Score (CRPS)
112   which is the squared difference between the Cumulative Distribution Functions (CDFs) of the
113   ensemble forecasts and observations.

114 The loss function defined as the CRPS corresponding to the observations $X_{O,n}$ and the corrected-
115 forecast members $X_{C,n}^{m}$ can be written as shown in Equation 5 (Gneiting and Raftery, 2007). The
116 correction is used every 10 min during the two simulated summer days for 3 years: 2019, 2020
117 and 2021. The forecast ensemble used here covers three years 2019, 2020 and 2021 and the CDF
118 of the observations was based on the radar MRMS observations over the same years at the same
119 two days. Data from 2022 will be used as an independent test for the calibration. A short training
120 period was chosen in this work (48 hours). In fact, there is a trade-off in selecting the length of
121 the training period. Shorter training periods can be used to correct flow-dependent model biases
122 that have rapid variations while longer training periods aim at reducing the statistical variability
123 of different coefficients and hence the calibrated forecast.

124
$$CRPS\,(\alpha,\,\beta,\,\gamma_1,\,\gamma_2) \;=\; \left\langle \left\langle \left| X_{C,n}^{m} - X_{O,n} \right| \right\rangle_m - \frac{\delta_n}{2} \right\rangle_n \qquad (5)$$

125 **2. Materials and Methods**
126   **2.1. Use case description**

127 The simulated event is precipitation event that took place in South Florida that was visible in the
128 MRMS data with scales of 200 km and small scales of 1-50 km as shown Figures 1 and 3. These
129 events fall under Meso-β and Meso-γ features. In South Florida, particularly during the summer,
130 mesoscale weather features (e.g., land–sea breezes, thermal troughs, outflow boundaries, etc.)
131 have a significant impact on day-to-day weather forecasting, as they frequently represent the
132 primary forcing for convection. During the simulated period,

133 These mesoscale features necessitate the use of high-resolution, convection resolving forecast
134 tools in order to provide the detailed information needed to improve local forecasts and
135 warnings. Moreover, Florida has recently emerged as a leader in autonomous vehicles including
136 UAS through different investments in its Department of Transportation. Therefore, South Florida
137 is a suitable area to study precipitation forecasting and its impact on UAS contingency planning.

138 During the simulation summer period, precipitations were of different types: mainly convective
139 because sea breezes are often form on the west and east sides of Florida, and due to differences
140 in temperature between the land (which heats quickly) and the ocean (which heats up more
141 slowly) which enhance the convective lift and induce intense rainfall and thunderstorms.
142 Convective and tropical convective precipitation are often embedded in areas of warm stratiform
143 precipitation. Warm stratiform precipitations are also present in South Florida that result from
144 frontal systems where the growth of hydrometeor particles occurs.

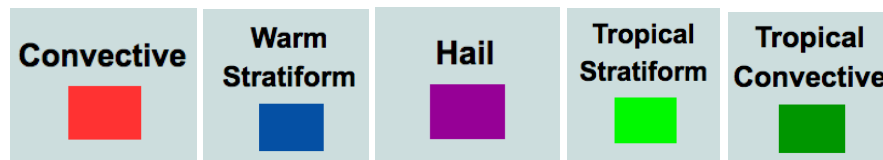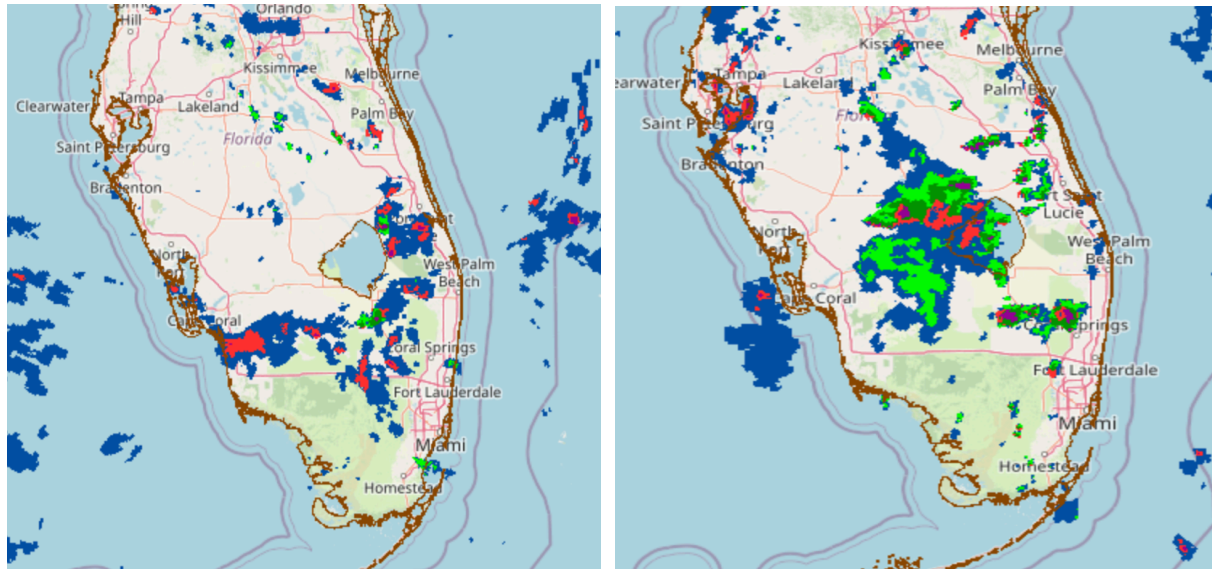| **Convective**	**Warm Stratiform**	**Hail**	**Tropical Stratiform**	**Tropical Convective**
🟥	🟦	🟪	🟩	🟩

Figure 1: MRMS Precipitation type over South Florida on July 16th at 5:40pm (left panel) and on July 17th at 6:44 pm (right panel (https://mrms.nssl.noaa.gov/qvs/product_viewer/) .

2.2. Ensemble Forecasts

2.2.1.   Simulations Setup

WRF (Sharmarock et al. 2005) was widely used in both academic research and industry (Chrit et al. 2022, Chrit et al. 2018, Chrit et al. 2017). The fully compressible and non-hydrostatic dynamic framework is used in the ARW module. The simulated domains D1 and D2 shown in Figure 2 represent the outermost and innermost domains respectively. The horizontal resolutions of D1, D2 are 3-km and 1-km. Vertically, 80 vertical levels are used with 30 vertical levels used below 1-km. The central point of the two domains is 80.74332 ºW, 26.40334 ºN.

The outermost D1 and innermost D2 domains have 560 x 720 and 460 x 400 grid points respectively in the south-north and east-west directions. In order to guarantee the numerical stability of the WRF model, the adaptive time stepping is used. The configuration and the physical parameterizations used in the simulations over D1 and D2 are shown in Table [1] of Appendix A.
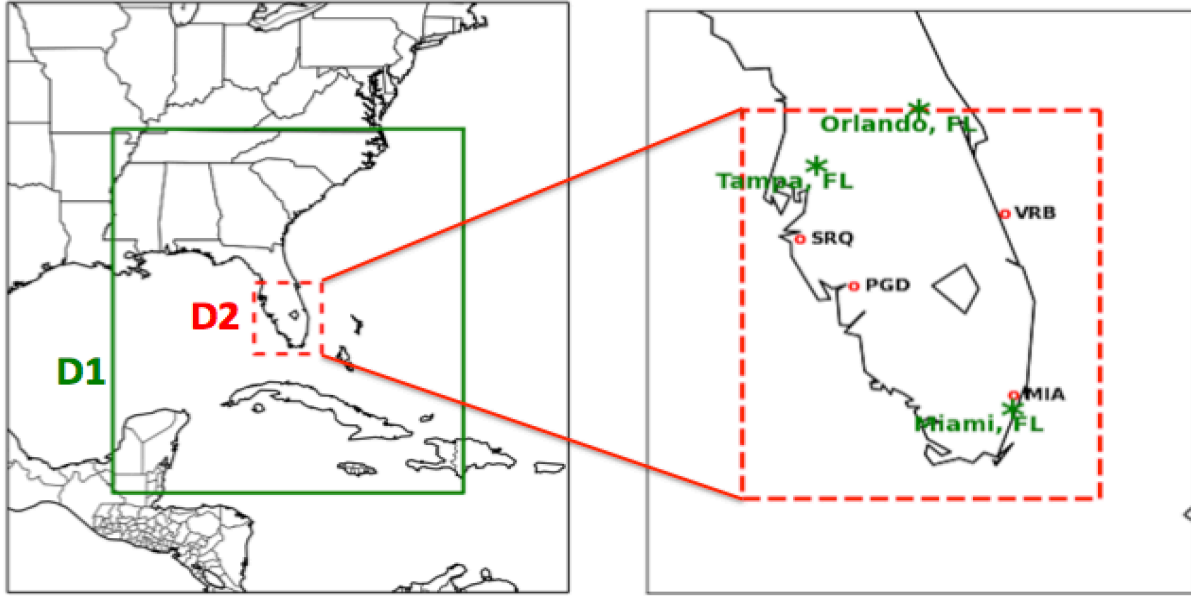
Figure 2: Left panel: Map of the simulated outermost and nested domains D1 and D2 delimited with green solid and red dashed rectangles, respectively. Right panel: Simulation domain is delimited with red dashed rectangle with the four ASOS stations used for evaluation shown with red points. The Three major cities in Florida (Miami, Orlando and Tampa) are shown in green stars.

2.2.2. Ensemble design

The ensemble used in the present study is a multi-physics ensemble with forecasts initialized with different initial and boundary conditions. In fact, multi-physics schemes have been very successful in generating reliable probabilistic forecasts, particularly for mesoscale prediction systems. Although obtaining these forecasts is computationally intensive, the ensemble results in members with physical interpretation comparing to members generated with perturbed initial conditions that poses difficulties for physical interpretation. On the other hand, precipitation forecasting is sensitive to the simulation setup namely the cumulus convection scheme (Vitart et al. 2001; Biswas et al. 2014), microphysics scheme (Liu et al. 2020), boundary layer parameterization (Taraphdar and Pauluis 2021) and radiations schemes (Li et al. 2014).

In this work, 20 distinct combinations of physics packages for parameterizing the microphysics (MP scheme), cumulus (C), Short Waves (SW) and Long Waves (LW) parameterization, planetary boundary layer (PBL), and land-surface models, (Table 1) are used to build four ensembles: three ensembles simulating the same 48 hours plus 12 hours as spin-up period (from July 15th, 2018 at 12 pm UTC to July 18th, 2021 at 12 am UTC) but over 2019, 2020, 2021 for the training and the fourth for testing simulating the same 48 hours during 2022. To maximize ensemble diversity, different boundary and initial conditions were used based on four models: the North American Model (NAM), RApid Refresh (RAP), North American Regional Reanalysis (NARR) and Global Forecast System (GFS). A total of 20 WRF simulations were performed to build the ensemble for each year.

6

189 Two MP parameterizations used are Microphysics schemes used are Thompson (Thom.;
190 Thompson et al. 2008), WRF single-moment 6-class (WSM6; Hong and Lim . 2006). The C
191 schemes used here are: Kain–Fritsch (Kain and Fritsch, 1993) cumulus parameterization, and
192 Betts–Miller–Janjic cumulus parameterization (Betts & Miller, 1993). Two PBL
193 parameterizations were used: Mellor–Yamada–Janjic (MYJ; Janjic 1994), Yonsei University
194 (YSU; Noh et al. 2003). Two Land-Surface models were used: Rapid Update Cycle (RUC;
195 Benjamin et al. 2004) or NOAH (NCEP–Oregon State University–Air Force–NWS Office of
196 Hydrology; Ek et al. 2003). The SW parameterizations are Goddard (Tao et al. 2003) and Dudhia
197 (Dudhia 1989), the LW radiations schemes are RRTM (Mlawer et al. 1997) and GFDL (Fels and
198 Schwarzkopf 1981).

Member number	ICs and LBCs	MP scheme (Thom and WSM6)	PBL parameterization (MYJ and YSU)	Land-Surface model (NOAH and RUC)	SW parameterization (GFDL and DUDHIA)	LW parameterization (GFDL and RRTM)	C parameterization (KAIN FRTISCH and BMJ)
1	NAM	Thom	MYJ	NOAH	DUDHIA	RRTM	Kain
2	NAM	WSM6	MYJ	NOAH	DUDHIA	RRTM	Kain
3	NAM	Thom	YSU	NOAH	DUDHIA	RRTM	Kain
4	NAM	Thom	MYJ	RUC	DUDHIA	RRTM	Kain
5	NAM	Thom	MYJ	NOAH	GFDL	RRTM	Kain
6	NAM	Thom	MYJ	NOAH	DUDHIA	GFDL	Kain
7	NAM	Thom	MYJ	NOAH	DUDHIA	RRTM	BMJ
8	NAM	Thom	YSU	RUC	DUDHIA	RRTM	Kain
9	NAM	Thom	YSU	RUC	GFDL	RRTM	Kain
10	NAM	WSM6	YSU	RUC	DUDHIA	GFDL	BMJ
11	RAP	WSM6	YSU	RUC	DUDHIA	RRTM	Kain
12	NARR	Thom	MYJ	NOAH	DUDHIA	RRTM	Kain
13	GFS	Thom	MYJ	NOAH	DUDHIA	RRTM	Kain
14	NARR	Thom	MYJ	NOAH	DUDHIA	RRTM	Kain
15	RAP	Thom	MYJ	NOAH	DUDHIA	RRTM	Kain
16	RAP	Thom	YSU	RUC	GFDL	RRTM	Kain
17	NAM	WSM6	YSU	RUC	DUDHIA	GFDL	Kain
18	RAP	Thom	MYJ	RUC	DUDHIA	RRTM	Kain
19	GFS	Thom	MYJ	RUC	DUDHIA	RRTM	Kain
20	GFS	WSM6	MYJ	NOAH	DUDHIA	GFDL	Kain

199 Table 1: Physics packages for multi-physics ensemble: Parameterizations and schemes used for
200 every ensemble member.

201

202 ### 2.2.3. MRMS radar data

203 The Multi-Radar/Multi-Sensor (MRMS) system was created by the NOAA National Severe
204 Storms Laboratory (NSSL) to produce severe weather and precipitation products for decision-
205 making capabilities to improve severe weather forecasts and warnings, hydrology, aviation, and
206 Numerical Weather Prediction. It currently integrates about 180 operational radars and creates a
207 seamless 3D radar mosaic across the CONtiguous United States (CONUS) and southern Canada
208 at very high spatial (1 km) and temporal (2 min) resolution.

209 The performance of the MRMS system over single radar-based Quantitative Precipitation
210 Estimates (QPE) across CONUS was reasonable (Zhang et al., 2016). Chen et al. (2020)
211 evaluated the MRMS and Global Precipitation Measurement Mission (GPM) products at 1-hr
212 temporal resolution across Harris County and Spring Basin Texas. Their results showed that
213 remote sensing technologies could detect and estimate the unprecedented extreme rainfall
214 associated with Hurricane Harvey. Among the remote sensing products they used in their study,
215 MRMS had the best agreement with the network rain gauge observations.

216 The MRMS surface precipitation rate used in this paper is currently calculated using multiple R–
217 Z relationships. Polarimetric variables are not used because various polarimetric radar QPE
218 schemes are still under evaluation across CONUS and an optimal approach for all seasons and all
219 geographic regions has yet to be developed. The following empirical R–Z relationships are used
220 in MRMS to compute surface precipitation rate for each precipitation type: convective rain, hail,
221 warm and cold stratiform rain, snow and tropical stratiform mixed rain. More information about
222 the MRMS system can be found at NSSL's MRMS webpage (ASOS user guide), the MRMS
223 Fact Sheet (https://www.nssl.noaa.gov/news/factsheets/MRMS_2015.March.16.pdf), and
224 Kirstetter et al., 2012. The MRMS data for the two simulated days were re-gridded to the same
225 WRF grid over D2 with a 1-km resolution for every year of the learning and testing years.

226 ### 2.2.4.   ASOS data

227 The Automated Surface Observing System (ASOS) network provides most of the basic
228 hydrometeorological observations at different airports, including 1-hour accumulated
229 precipitation. The data is reported every 5 min in the majority of the stations. One hour
230 precipitation for the period from the observation time to the time of the previous hourly
231 precipitation reset. The precipitation accumulation algorithm obtains precipitation accumulation
232 data from the Heated Tipping Bucket (HTB) precipitation gauge once each minute (ASOS user
233 guide). The trace reports are considered as 0.1 mm. The detection threshold specified for the
234 ASOS HTB is 0.01 inch per hour (0.254 mm per hour), and the precipitation rate accuracy is the
235 larger of 10 percent or 0.01 inches per hour (0.254 mm per hour).

236 For this study, four METAR observation sites located over South Florida were used for the
237 evaluation of the different forecasts, and these sites are shown in Figure 1. Table [1] of Appendix
238 B shows the characteristics of the four stations that will be used for comparison and evaluation.
239 Additional stations are available, but either no precipitation is recorded, or most data is missing.

240 ### 3. Evaluation method

241 The probabilistic evaluation will be based on the rank histogram score and the reliability
242 diagram. The rank-histogram score δ defined in Equation (6) is a tool used to measure the spread
243 and hence the reliability of the ensemble.

244
$$\delta = \frac{N+1}{N\,M} \sum_{j=0}^{N}(r_j - \bar{r})^2 \qquad (6)$$

245
$$\bar{r} = \frac{M}{N+1} \qquad (7)$$

246 The rank-histogram score measures the deviation from a perfect and flat rank histogram
247 (Talagrand et al., 1999; Candille and Talagrand, 2005). In Equation (6), N is the number of
248 ensemble members, M is the number of observations, r_j the number of observations of rank j,
249 and $\bar{r}$ is the expectation of r_j defined in Equation (7). The optimal ensemble with a flat rank
250 histogram has a score of 1. A score lower than 1 would indicate overconfidence in the results.

251 Reliability is also assessed with the reliability diagram. This diagram provides a probabilistic
252 interpretation in terms of frequency of occurrence of precipitation events. The x-axis represents
253 the predicted probability of occurrence (p) of an event in a time when the y-axis represents the
254 relative frequency which is defined as the proportion of the observed event that really occurred
255 among events with a predicted probability of p. A reliability curve overlaying the first bisector
256 shows a perfectly reliable ensemble.

257 The statistical evaluation of the forecasted PR against the ASOS data uses classical skill metrics
258 namely the simulated mean ($\bar{s}$), the Root Mean Square Error (RMSE), the correlation coefficient
259 (R) and the Mean Bias Error (MBE). These scores are defined in Table 1 in Appendix D.

4. Results and discussions
4.1. Performance evaluation

262 In this section, we evaluate the two ensembles: the "Raw Ensemble" and the "Calibrated
263 Ensemble" during the two simulated days of 2022 against the corresponding MRMS
264 observations.   Figure 3 compares the PR measured by MRMS data and the simulated data using
265 the Raw and calibrated ensembles on July 16th , 2022 at 10 pm.
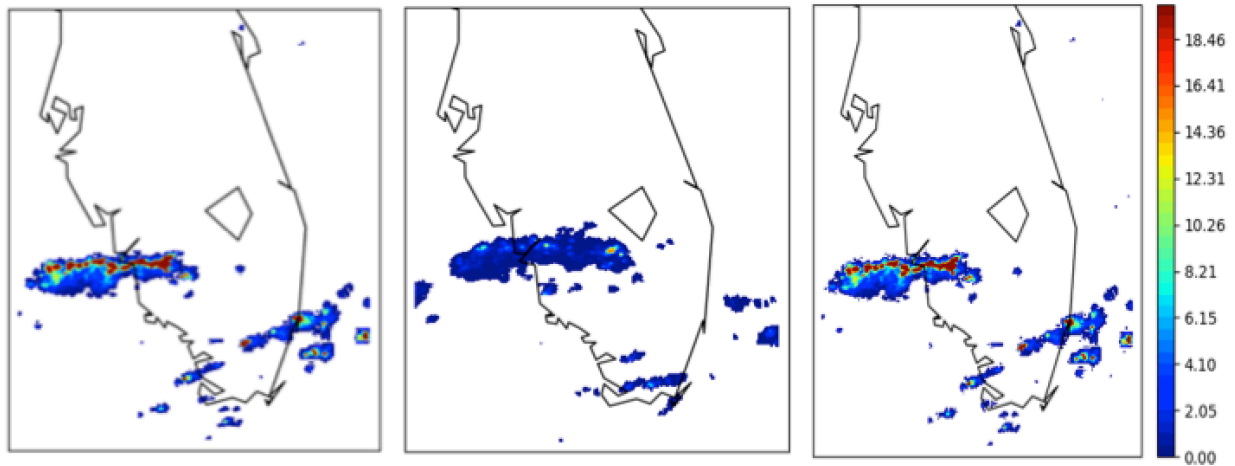

266
267 Figure 3: Left panel: PR from MRMS data on July 16th at 10 pm. Middle panel: Simulated PR

268   with Raw Ensemble mean at the same time and date as the left panel. Right panel: Simulated PR
269   with Calibrated Ensemble mean at the same time and date as the left panel. The white area
270   represents areas with zero PR.

271

272   Figure 3 shows clear discrepancies between the means of the Raw and Calibrated Ensembles.
273   The Raw Ensemble was able to predict the location and timing of the meso-β precipitation
274   system but was not able to reproduce the meso-γ precipitation systems over the south-eastern
275   part of the simulation domain. However, the raw prediction of the PR is underestimated by a
276   factor of 2. In fact, 75 % of the raw ensemble members underestimate the PR mainly because
277   75% of the simulated members use the Thompson microphysical scheme that produces less
278   liquid condensate which results is lower precipitation amount. Similar results were found by Guo
279   et al. 2019 by comparing four MP parameterizations over Eastern China over a six-year summer
280   period (2009-2014). They concluded that the Thompson scheme creates more snow articles than
281   other schemes which produces less graupel and precipitations during warm times. The prediction
282   of PR using the calibrated ensemble substantially improved the PR forecasts as the predicted
283   mean is closer to the MRMS observations and the predicted mean increased from 1 with the raw
284   mean to 19 mm.h^{-1} with the calibrated mean. Furthermore, the calibration improved the timing
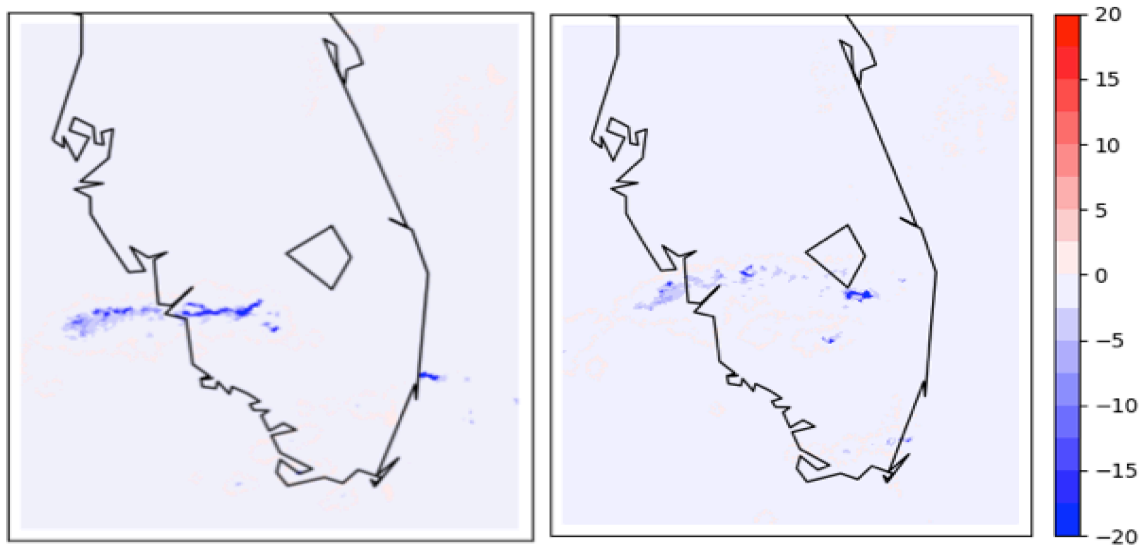285   and the location of this simulated precipitation event and the meso-γ precipitations.

286

287   Figure 4: Left panel: Absolute difference (mm.h^{-1}) between the CRPS of the raw ensemble and
288   the calibrated ensemble on July 16 at 10pm. Right panel: Similar to the left panel on July 17th at
289   00 am.

290   Figure 4 shows the impact of the calibration of the CRPS of the PR forecasts. The calibration
291   was successful in reducing the CRPS of the calibrated ensemble by a 90 % approximately over
292   the high PR areas, hence improving accuracy relative to MRMS observations. This improvement
293   was guaranteed by the MBM method as it was based on learning the minimization of the CRPS.

294 This is indicative that the weighting coefficients were able to accurately learn temporal features
295 during the two simulated days and correct the raw forecasts.

296 Figure 5 shows the bias of the means of the Raw and Calibrated Ensembles relative to the
297 MRMS data at two different times. The mean of the raw ensemble has a high bias significant
298 over the precipitation areas that can be as high as 20% against the MRMS data. Figure 5 shows
299 also the impact of ensemble calibration on bias and CRPS of the probabilistic forecasts. The
300 calibration had a significant impact over the forecasted PR as the bias of the calibrated mean
301 decreased by 20% relative to the MRMS observed PR.

302

303 Figure 5: Top left panel: Bias error (mm.h^{-1}) of the Raw Ensemble mean at July 16th 2022 at
304 10pm . Top right panel: Absolute difference between Bias errors of the Calibrated and Raw
305 ensemble means at 8pm. Bottom left panel: Similar to top left panel at July 17th 00pm . Bottom
306 right panel: Similar to top right panel at July 17th at 00 am.

307

308 The reliability diagram of the Raw and Calibrated ensembles are shown in Figure 6. Raw PR
309 forecasts tend to over-forecast both high and low probability events. When considering the
310 calibrated ensemble, the reliability increased for both low and high frequency events. In addition,
311 there is a better reliability for low frequency precipitation events, but the calibrated ensemble is
312 still over forecasting the high-frequency precipitation events. The calibrated ensemble was not
313 able to reproduce the high-frequency event because of biases related to the location and spatial
314 extent of the precipitation events of different scales. The rank-histogram scores of the raw and
315 calibrated ensembles are 15.9 and 4.1   respectively. The rank-histogram score decreased but still
316 more than the optimal score confirming that the calibration improved the spread of the ensemble
317 but still do not have optimal spread in our ensemble. Training on more years such as a decade,
318 although very resource-intensive may further improve the reliability of the calibrated ensemble.
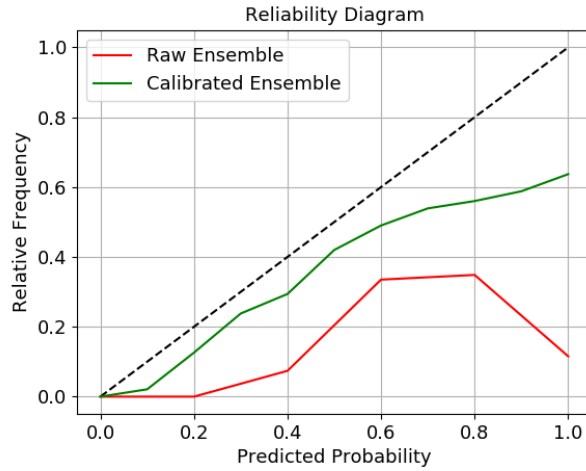
319

321 Figure 6: Reliability diagram of the Raw and Calibrated ensembles over the simulated time and
322   over the precipitation areas of the D2 domain.

323

324   **4.2.Comparison with ASOS data**

325 The calibration is evaluated against the measured PR over the four ASOS stations shown in
326 Figure 7. Table 2 shows the statistical scores of both raw and calibrated means. Tables 1, 2, 3
327 and 4 in Appendix C show the statistical evaluation of PR over the stations PGD, MIA, SRQ and
328 VRB respectively.

329

330
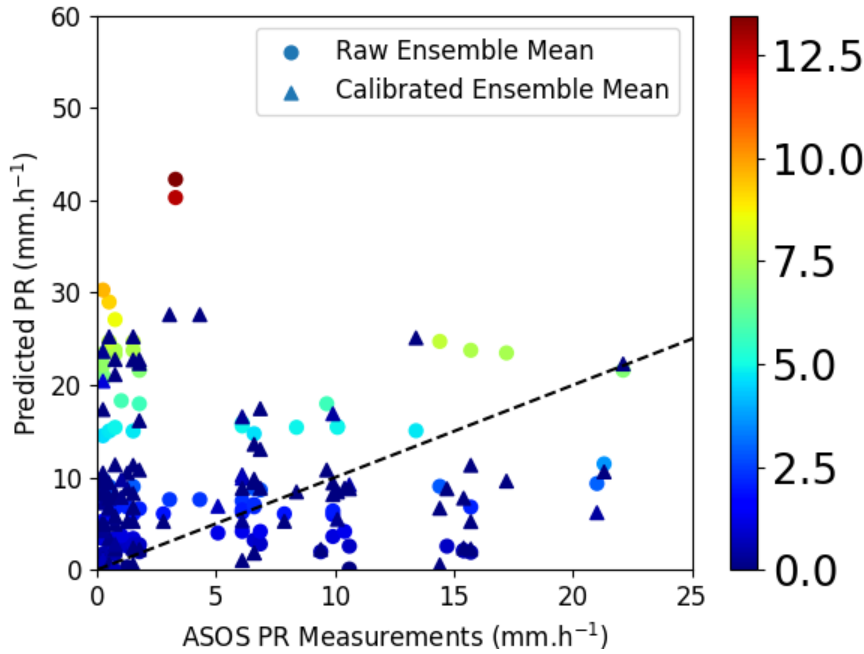
Figure 7: Scatter plot of the simulated PR using the means Raw and Calibrated
ensembles. The colors are the uncertainty of the forecasts.

$\overline{o}$= 4.82 mm.h^{-1}	$\overline{s}$ (mm.h^{-1})	RMSE (mm.h^{-1})	R (%)	MBE (%)
Raw Ensemble Mean	19.07	31.60	16.70	1807.09
Calibrated Ensemble Mean	10.31	11.07	23.15	615.91

Table 2: Statistics of the means of the Raw and Calibrated ensembles against data over the four
ASOS.

The scatter plot in Figure 5 shows that both raw and calibrated means overestimate the observed
PR over the four ASOS stations with a simulated means of 19.07 and 10.31 mm.h^{-1} for raw and
calibrated ensemble respectively against 4.82 mm.h^{-1} .The slopes of the lines of best fit are 3.87
and 1.57 for the raw and calibrated means respectively. The calibration improved the forecasts as
the RMSE decreased from 31.60 mm.h^{-1} to 11.07 mm.h^{-1} and the MBE decreased from
1807.09% to 615.91 %. Besides, the uncertainty of the forecasted PR was reduced because of the
calibration as the uncertainty of the calibrated mean decreased from 14 to 4 mm.h^{-1}.

The calibrated ensemble still has high bias and significantly overestimates the PR by a factor of
2. This overestimation may be due to the overestimation of PR during summertime by the
MRMS data compared to ground based ASOS data because of the evaporation process occurring
under the radar beam. In fact, both raw and calibrated PR forecasts overestimate the light
precipitation (particularly PR less than 2 mm.h^{-1} because the MRMS data also overestimates the

13

349 light precipitations. Similar result was found by Gao et al. 2018 by evaluating the MRMS data
350 against the NEXt generation weather RADar (NEXRAD) data over TEXAS, USA and a dense
351 rain gauge network covering Harris County, Texas, USA. Santer and Grams 2020 evaluated the
352 MRMS Quantitative precipitation estimation (QPE) and PR during 18-months period against rain
353 gauges from the National Centers for Environmental Prediction Meteorological Assimilation
354 Data Ingest System (MADIS) over CONUS and showed that, during warm times, an important
355 systematic overestimation exist because of sub-radar beam evaporation. They also quantified the
356 uncertainty of a MRMS radar measurement based on distance from the radar and partial radar
357 beam blockage

358

359 **Conclusion**

360 In this study, we have applied the MBM calibration technique by minimizing CRPS in order to
361 improve the probabilistic forecasting of precipitation as part of a risk-based approach to integrate
362 UAS into the NAS. The algorithm does not depend on any assumptions on distributions such as
363 gaussianity or uniformity and comes with theoretical guarantee of performance.

364 The case study examined the impact of ensemble calibration on precipitation forecasts accuracy
365 and uncertainty over South Florida. The MRMS radar data was used to calibrate a 20-members
366 ensemble that was underestimating the PR. This paper showed that CRPS minimization brings
367 improvement on classical scores for the ensemble mean and probabilistic diagnostic tools.
368 Indeed, the forecasting capability measured by classical scores (RMSE, MBE and bias) are
369 improved by the algorithm used during the two simulated summer days. Besides, this spread
370 correction provides a bias correction, improved the reliability of the ensemble and reduced
371 forecasts' uncertainty although the comparison with ASOS data shows a persistent
372 overestimation because of the inherent bias of the MRMS data.

373 In addition, the selection of more predictors such as relative humidity, cloud cover and vertical
374 wind velocity may further enhance the skill of probabilistic post-processing for near-real-time
375 precipitation estimates. Besides, using satellite data along with radar data as used here may also
376 improve the evaluation against ground-based validation. The use of deep learning methods such
377 as distributional regression network, Bernstein Quantile Network and Histogram Estimation
378 Network is a promising as demonstrated in Schulz and Lerch 2022.

379 Future work should investigate the validation of the impact of the calibration and weights on
380 other use cases and the assessment of the performance of the calibrated ensemble over longer
381 lead times and different testing periods. The validation against denser rain gauges network is also
382 necessary as it will show the accuracy of the calibration over off-airport areas which is important
383 for weather-risk assessment and contingency planning during BVLOS operations.

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543

544

545 **Appendix**

546

547 **Appendix A**

548

Model parameter	Used configuration
Model and domains	
Model version	ARWv4.0 (Skarmarock et al. 2008)
Time step	Adaptative time step (36 s for D1)
Map projection	Lambert
Pressure top	50 hPa
Vertical levels	80 (*)
Time integration scheme	Third order Runge-Kutta scheme
Time integration scheme for acoustic and gravity-wave modes	Second order scheme

Horizontal/vertical advection	Fifth order upwind
Scalar advection	Positive definite
Upper-level damping (for vertical propagating gravity waves)	Rayleigh damping
Computational horizontal diffusion	6th-order numerical diffusion
Forecast period	60 h (from July 15th, 2018 at 12 pm UTC to July 18th, 2021 at 12 am UTC)

*Table [1]: WRF model configuration and input physics parameterizations. * η levels are 1,*
0.99938147, 0.9918859506, 0.9860143, 0.9835575, 0.97480931, 0.9691238, 0.95061912,
0.938789424, 0.91847208, 0.89114445, 0.87771024, 0.8344125, 0.807124586, 0.76820505,
0.71652851, 0.6848121, 0.615978875, 0.5720332, 0.5472062, 0.5233661, 0.5004734,
0.4784906, 0.4573815, 0.4371113, 0.4176468, 0.3989559, 0.3810079, 0.3637731, 0.3472234,
0.3313315, 0.316071, 0.3014172, 0.2873457, 0.2738335, 0.2608584, 0.2483989,
0.2364347, 0.2249459, 0.2139138, 0.2033201, 0.1931475, 0.1833792, 0.173999, 0.1649918,
0.1563425, 0.1480369, 0.1400615, 0.132403, 0.1250489, 0.1179871, 0.111206, 0.1046944,
0.09844154, 0.09243726, 0.08667168, 0.08113512, 0.07581868, 0.07071351, 0.06581128,
0.06110381, 0.0565835, 0.05224282, 0.04807468, 0.04407217, 0.04022875, 0.0365381,
0.03299413, 0.02959097, 0.02632311, 0.0231851, 0.02017184, 0.01727832, 0.0144998,
0.01183172, 0.00926967, 0.006809457, 0.004447003, 0.002178475, 0.

Appendix B

Station ID	Latitude(ºN)	Longitude(ºW)	Height ASL (m)
VRB	27.6556	80.4179	8.00
PGD	26.9172	81.9914	8.00
MIA	25.7880	80.3169	4.00
SRQ	27.4014	82.5586	9.00

Table 1: List of the four ASOS stations in South Florida and their corresponding latitude, longitude and above sea-level (ASL) height.

Appendix C

$\bar{o}$=5.02 mm.h^{-1}	$\bar{s}$ (mm.h^{-1})	RMSE (mm.h^{-1})	R (%)	MBE (%)
Raw Ensemble Mean	29.71	53.92	14.49	2469.24

Calibrated Ensemble Mean	10.77	14.24		20.81	575.37

Table 1: Statistics of the raw and calibrated means over the PGD ASOS station

$\bar{o}$= 4.34 mm.h^{-1}	$\bar{s}$ (mm.h^{-1})	RMSE (mm.h^{-1})	R (%)	MBE (%)
Raw Ensemble Mean	14.57	16.91	4.96	1023,87
Calibrated Ensemble Mean	13.79	15.09	8.39	940.71

Table 2: Statistics of the raw and calibrated means over the MIA ASOS station

$\bar{o}$= 2.54 mm.h^{-1}	$\bar{s}$ (mm.h^{-1})	RMSE (mm.h^{-1})	R (%)	MBE (%)
Raw Ensemble Mean	15.57	17.07	8.30	1302.87
Calibrated Ensemble Mean	8.60	9.77	29.36	605.77

Table 3: Statistics of the raw and calibrated means over the SRQ ASOS station

=7.39 mm.h^{-1}	$\bar{s}$(mm.h^{-1})	RMSE (mm.h^{-1})	R (%)	MBE (%)
Raw Ensemble Mean	16.43	15.61	19.72	904.30
Calibrated Ensemble Mean	8.06	7.04	30.06	30.06

Table 4: Statistics of the raw and calibrated means over the VRB ASOS station

Appendix D

Statistical indicator	Definition
$\bar{s}$	$\sqrt{\dfrac{1}{n}\sum_{i=1}^{n} s_i}$
$\bar{o}$	$\sqrt{\dfrac{1}{n}\sum_{i=1}^{n} o_i}$
RMSE	$\sqrt{\dfrac{1}{n}\sum_{i=1}^{n} (c_i - o_i)^2}$

21

Correlation	$$\frac{\sum_{i=1}^{n} (s_i - \bar{s})(o_i - \bar{o})}{\sqrt{\sum_{i=1}^{n} (s_i - \bar{s})^2} \sqrt{\sum_{i=1}^{n} (o_i - \bar{o})^2}}$$
MBE	$$\frac{1}{n}\sum_{i=1}^{n}(c_i - o_i)$$

577   Table 1: Definition of the statistics used in this work. o_i and s_i are the observed and simulated wind
578   speeds at time i. n is the number of data.

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