

Height-integrated conductance and field-aligned current magnitudes evolve differently during a substorm

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Abstract

We examine the average evolution of precipitation-induced height-integrated conductances, along with field-aligned currents, in the nightside sector of the polar cap over the course of a substorm. Conductances are estimated from the average energy flux and mean energies derived from auroral emission data. Data are binned using a superposed epoch analysis on a normalised time grid based on the time between onset and recovery phase (Δt) of each contributing substorm. We also examine conductances using a fixed time binning of width 0.25 hr. We split the data set by magnetic latitude of onset. We find that the highest conductances are observed for substorms with onsets that occur between 63 and 65 degrees magnetic latitude, peaking at around 11 mho (Hall) and 4.8 mho (Pedersen). Substorms with onsets at higher magnetic latitudes show lower conductances and less variability. Changes in conductance over the course of a substorm appear primarily driven by changes (about 40% at onset) in the average energy flux, rather than the average energy of the precipitation. Average energies increase after onset slower than energy flux, later these energies decrease slowly for the lowest latitude onsets. No clear expansion of the main region 1 and region 2 field-aligned currents is observed. However, we do see an ordering of the current magnitudes with magnetic latitude of onset, particularly for region 1 downwards FAC in the morning sector. Peak current magnitudes occur slightly after or before the start of the recovery phase for the normalised and fixed-time grids.

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Key Points:

- We track the progression of height-induced conductances, along with field-aligned currents, during substorms
- Low-latitude onsets exhibit the largest and longest-lived changes to height-integrated conductance
- Latitude of substorm onset has less control on field-aligned current magnitudes

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Abstract

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Plain Language Summary

Particles precipitate from Earth's magnetosphere into the upper ionosphere causing auroral emissions. A comparison of these auroral emissions, taken at different wavelengths, can be used to estimate the mean energy of the particles, as well as the flux, or number of precipitating particles in an area per unit time. From this mean energy and flux, we can estimate changes in the conductance of the ionosphere. Here, we examine how the conductance varies during the course of a substorm; when increased auroral emissions are seen suddenly on the nightside of the Earth. For this work we use imaging data from low-altitude spacecraft that give reasonable spatial coverage of the nightside ionosphere. We compare the changes in conductance over the course of an average substorm, to those seen in electrical currents that flow in the Earth's magnetosphere. The currents respond in a similar manner to the parameters derived from the auroral emissions.

1 Introduction

Deciphering the spatial and temporal variations in ionospheric conductances, under a variety of ambient conditions is of importance to the solar-terrestrial community (Denton et al., 2016). Knowledge of the conductance, is of particular importance, for example, when considering the coupling of component regions within magnetosphere and the thermosphere. Auroral imagers offer a method to estimate height-integrated conductances induced through particle precipitation simultaneously over large areas of the high-latitude polar cap region (Lam et al., 2019). There may be considerable differences between spatially precise, height-resolved conductances, and those presented in statistical maps (McGranaghan et al., 2015). However, statistical maps still have value as primers for global magnetospheric-ionospheric coupling models, particularly under extreme conditions (Mukhopadhyay et al., 2020). Parameterisation of height-integrated conductances at the dayside, under varying interplanetary magnetic field (IMF) and solar wind conditions, along with a simple parameterisation during an average substorm on the nightside, was presented in Carter et al. (2020). In this previous work, only the substorm phase relative to onset time was considered, using a superposed epoch analysis based on substorm onsets determined from the SuperMAG dataset (Newell & Gjerloev, 2011; Gjerloev, 2012). In this work we parameterise height-integrated conductances by substorm

65 phase and also by the magnetic latitude of substorm onset, as this is known to control
 66 substorm intensity (Milan et al., 2009). We also consider the evolution of these conduc-
 67 tances with respect to distributions of field-aligned currents (FACs), which are an inte-
 68 gral component of the magnetosphere-ionosphere coupled system.

69 Lester et al. (1996) examined Hall and Pedersen conductances during an individ-
 70 ual substorm using an incoherent scatter radar. They found that the implied mean en-
 71 ergy of the incoming precipitation varied during the progression of the substorm, which
 72 involved two expansion phases. At onset, the conductances were seen to increase to ex-
 73 ceptionally high values of approximately 77 mho and 26 mho for Hall and Pedersen con-
 74 ductances respectively, whereas the mean energy remained constant. The second expan-
 75 sion phase showed a marked increase in mean energy, which was then doubled during
 76 the recovery phase. The authors suggested that the variations in mean energy were due
 77 to changes in acceleration processes in the magnetotail during the phase of a substorm,
 78 although observational effects from the radar are not discounted.

79 FACs in the Earth’s magnetosphere respond to the substorm cycle in a variety of
 80 ways. The main region 1 and region 2 FAC distributions expand quickly to lower lat-
 81 itudes in the growth phase, and simultaneously increases are seen in both region 1 and
 82 region 2 current magnitudes, although the increase is larger for region 1 (Coxon et al.,
 83 2014). The FAC latitude and magnitudes recover within about 20 mins. Asymmetries
 84 in the response of the FACs at onset are observed associated with the sign of the IMF
 85 B_Y component (Milan et al., 2018).

86 This paper is laid out as follows. In Section 2 we describe the data sets used to de-
 87 rive Pedersen and Hall height-integrated conductance values from observations of auro-
 88 ral emissions, FACs, and the substorm list on which we based our superposed epoch anal-
 89 ysis. Here we also describe both a substorm-expansion phase binning and a fixed-time
 90 binning used for the superposed epoch analysis. We compare and discuss distributions
 91 of mean energy, mean energy flux, Pedersen and Hall height-integrated conductances in
 92 relation to the FACs during the progress of an average substorm in Section 3. We con-
 93 clude in Section 4.

94 2 Data

95 We use a superposed epoch analysis of substorm phase to parameterise the other
 96 datasets described below. This study uses a modified Substorm Onsets and Phases from
 97 Indices of the Electrojet (SOPHIE) list from (Forsyth et al., 2015) which had been con-
 98 structured from SuperMAG data and covers the years 2005 until 2019. This list is of those
 99 substorms with an expansion phase threshold with the SML index < -75 nT, where the
 100 SML indices originate from SuperMAG (Gjerloev, 2012). This modified SOPHIE list con-
 101 tained the start of the expansion and recovery phases, plus the MLT and magnetic lat-
 102 itude locations for each substorm onset. We take the start of the expansion phase as the
 103 onset time. For this analysis, we only include substorm onsets that occurred between 18h
 104 MLT and 06h MLT, which we parameterise by onset latitude. We only used isolated sub-
 105 storms, i.e. those onsets that were preceded by a growth phase and followed by a recov-
 106 ery phase. This is to avoid multiple intensifications without an interim recovery period,
 107 and although these occur rarely (1% of time) (Milan et al., 2021), their effects could be
 108 large. The onset latitude bin boundaries were chosen to give good coverage of at least
 109 several hundreds of onsets per bin for the statistical analysis, with bins with a width of
 110 2 degrees starting from 63° , apart from the bins at the extremes of the range. As in the
 111 study of Carter et al. (2020), substorm phases are taken at set intervals before and af-
 112 ter onset. We define δt as the time period between onset and the start of the recovery
 113 phase for each contributing substorm. The expansion and recovery phase starts are given
 114 in the supplementary material of Forsyth et al. (2015). The duration of each substorm
 115 is not defined in this list. We use a step size of $0.25 \delta t$ over the course of a substorm in

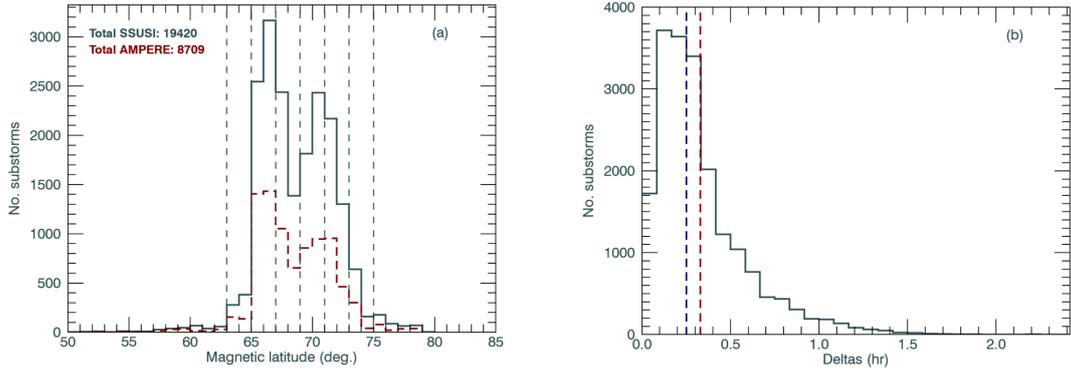


Figure 1. Statistics of the substorm onsets used in this analysis. Plot (a): A histogram of substorm onset latitudes from the (Forsyth et al., 2015) during the SSUSI (gray) and the shorter, but superimposed AMPERE (red) data periods. Dashed vertical lines indicate the boundaries used for the latitude selection in this analysis. Plot (b): A histogram of all δt , defined as the interval between the start of the substorm expansion and recovery phase (E-R) from the (Forsyth et al., 2015) list. The mean and median δt values are marked by the red and blue vertical dashed lines, respectively.

116 our analysis below. We also examine the behavior over an average substorm by using
 117 a time bin of a fixed width of 0.25 hrs.

118 In Fig. 1 we plot a histogram of substorm onset latitudes used in this study, along
 119 with a histogram of the δt intervals. Histograms for onset magnetic latitudes occurring
 120 during both the SSUSI (gray line) and AMPERE (red dashed line) data ranges are shown
 121 in plot (a), and a histogram of δt is shown in plot (b). The mean δt value is 0.32 hr, or
 122 19.8 min. The minimum δt used in this analysis was 2 min.

123 Later in this paper we present Pedersen and Hall height-integrated conductances
 124 derived from auroral emissions data obtained by the Special Sensor Ultraviolet Spectro-
 125 graphic Imager (SSUSI) (Paxton & Anderson, 1992; Paxton & Zhang, 2016) on board
 126 three Defense Meteorological Satellite Programme (DMSP) spacecraft. We calculate the
 127 conductances from data products produced by the SSUSI team, and we describe these
 128 calculations and data products fully in Carter et al. (2020). However in summary, the
 129 conductances are calculated from the mean energy and mean energy flux of the incom-
 130 ing precipitating particles, which are assumed to be electrons, derived from Lyman-Birge-
 131 Hopfield (LBH) long (165-180 nm) and short band (140-150 nm) radiances. We use SSUSI
 132 data from the Southern Hemisphere in this paper, as we have good coverage of the mid-
 133 night local time sectors for all three DMSP spacecraft. The data originates from all avail-
 134 able SSUSI files in the time period from 1 January 2005 to 31 December 2016 for F16,
 135 from 11 December 2006 to 4 August 2017 for F17, and from 17 November 2009 to 31 De-
 136 cember 2017 for F18.

137 The calculation proceeded as follows. From the mean energy (E_0 , in units of keV)
 138 and mean energy flux (Q , in units of $\text{erg cm}^{-2} \text{s}^{-1}$), the height-integrated Pedersen (Σ_P)
 139 and Hall (Σ_H) conductances can be calculated per pixel, via the empirical expressions
 140 found in Robinson et al. (1987), and as shown in equations 1 and 2.

$$141 \quad \Sigma_P = \frac{40E_0}{16 + E_0^2} \sqrt{Q} \quad (1)$$

$$\Sigma_H = 0.45(E_0^{0.85})\Sigma_P \quad (2)$$

To make a set of conductance maps, at each UT-stamped pixel at a given projected magnetic local time and magnetic latitude, the value of E_0 and Q are considered separately from each contributing DMSP satellite, and used to calculate the Hall and Pedersen height-integrated conductances for that particular pixel. The conductances are then averaged at a given pixel to provide a series of images showing the average nightside spatial distribution of conductance at each substorm time step, whether fixed or related to δt , and for each latitude bin.

In this work we use SSUSI data products of mean energy and mean energy flux. These have been calculated based on the assumption of a Gaussian profile for the incoming particle precipitation energy distribution. Maxwellian and Gaussian distributions will have the same characteristic energy, but different mean energies (Robinson et al., 1987). Applying Eqn. 1 to an average energy flux of $5.2 \text{ erg cm}^{-2} \text{ s}^{-1}$ and an average mean energy of 5.8 keV over the entire SSUSI data set used in this work, the Gaussian assumption would overestimate the height-integrated conductance at 10.7 mho compared to 7.0 mho for a Maxwellian distribution, see Fig. 2. Parity between distributions occurs for a characteristic energy of 2.85 keV , below which the Maxwellian assumption would overestimate the height-integrated conductance as compared to the Gaussian assumption. We present the calculated conductances as well as the behavior of E_0 and Q in Section ??.

The auroral-derived products are accompanied by patterns of FACs, obtained from the Active Magnetosphere and Planetary Electrodynamics Response Experiment (AMPERE) (Anderson et al., 2000; Waters et al., 2001). The FACs have been organised with respect to substorm latitude and substorm phase in the same way as the spatial distributions of E_0 , Q , and conductance as described above. Contributing AMPERE data spans the period 1 January 2010 to 31 December 2016, which was available at the time of processing. Only current densities over $0.1 \mu\text{A m}^{-2}$ are included to avoid including spurious low current density values that result from the AMPERE data processing technique, similar to the threshold used in Clausen et al. (2012).

3 Results and Discussion

In Fig. 3, we plot an example series of images showing the nightside spatial distribution of height-integrated Pedersen conductance (purple color scale), ordered by substorm phase along with contours of the FAC distribution at each phase. We overplot contours of upwards and downwards FAC distributions, colored red and blue respectively, at intervals of $0.05 \mu\text{A m}^{-2}$. This figure is plotted for the example magnetic latitude substorm onset bin of 63° to 65° degrees. In Fig. 4, in a similar format as the previous figure and again for the example magnetic latitude substorm onset bin of 63° to 65° degrees, we plot a set of differences image (purple-green color scale) showing the change in the conductance from the previous phase time step, expressed as a percentage. In these figures, the conductance begins to increase at onset at latitudes above 70 degrees and in MLT sectors just after local midnight. By $0.5 \delta t$, increases in conductance occur across many MLT and magnetic latitudes. Conductances begin to reduce at lower latitudes at $0.75 \delta t$, before starting to reduce at higher latitudes from $1.00 \delta t$. By $1.25 \delta t$, i.e. into the early part of the recovery phase, changes in conductance are seen at the edges of the main auroral oval, suggesting that dramatic differences in conductances here may be due to rapid changes to the auroral oval resulting in large percentage changes, or possibly artifacts of the averaging technique involving low numbers of contributing pixels, or less likely due to transient auroral events such as transpolar arcs which have not been screened for here. Clearer evidence of increased conductance at onset was observed when the magnetic latitude of substorm onset was not examined, as in Fig. 5 of Carter et al. (2020).

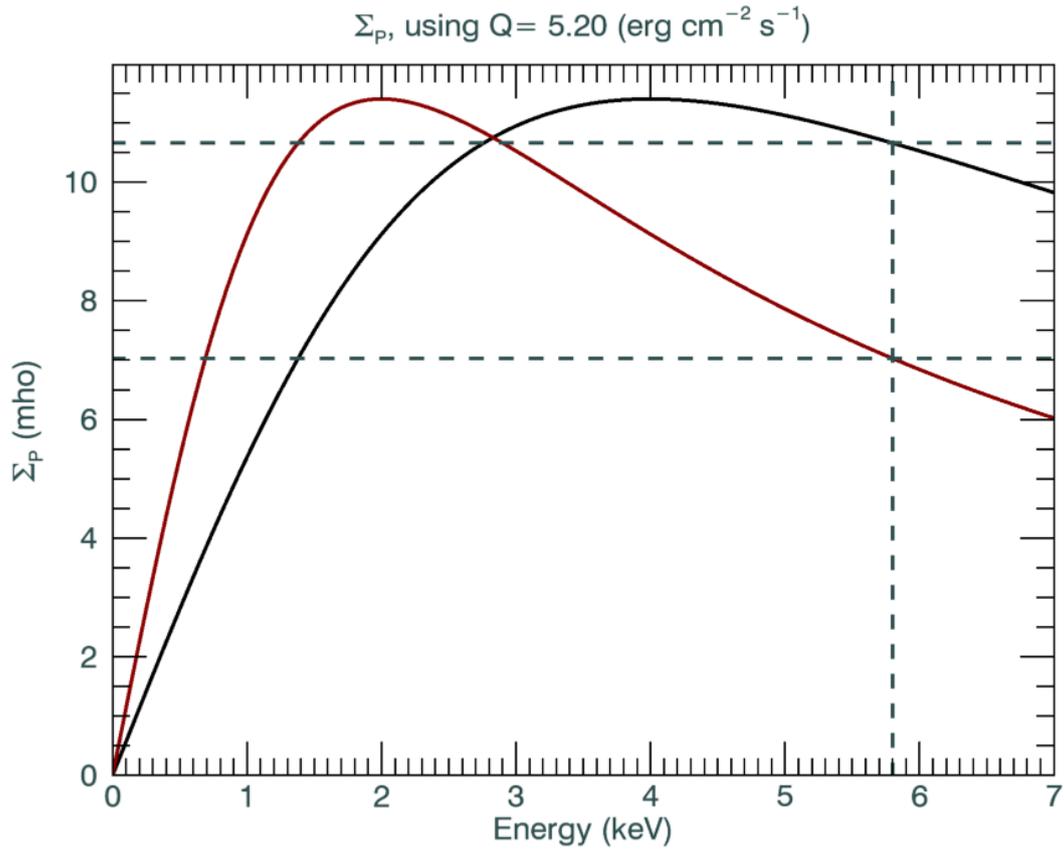


Figure 2. Height-integrated Pedersen conductances calculated using Eqn. 1 by assumed characteristic energy of the incoming particle precipitation, using the average mean energy flux of the SSUSI data set used in this work. This is calculated for a Maxwellian (red) or Gaussian (gray) distribution. Dashed lines indicate the average mean energy of the SSUSI data set.

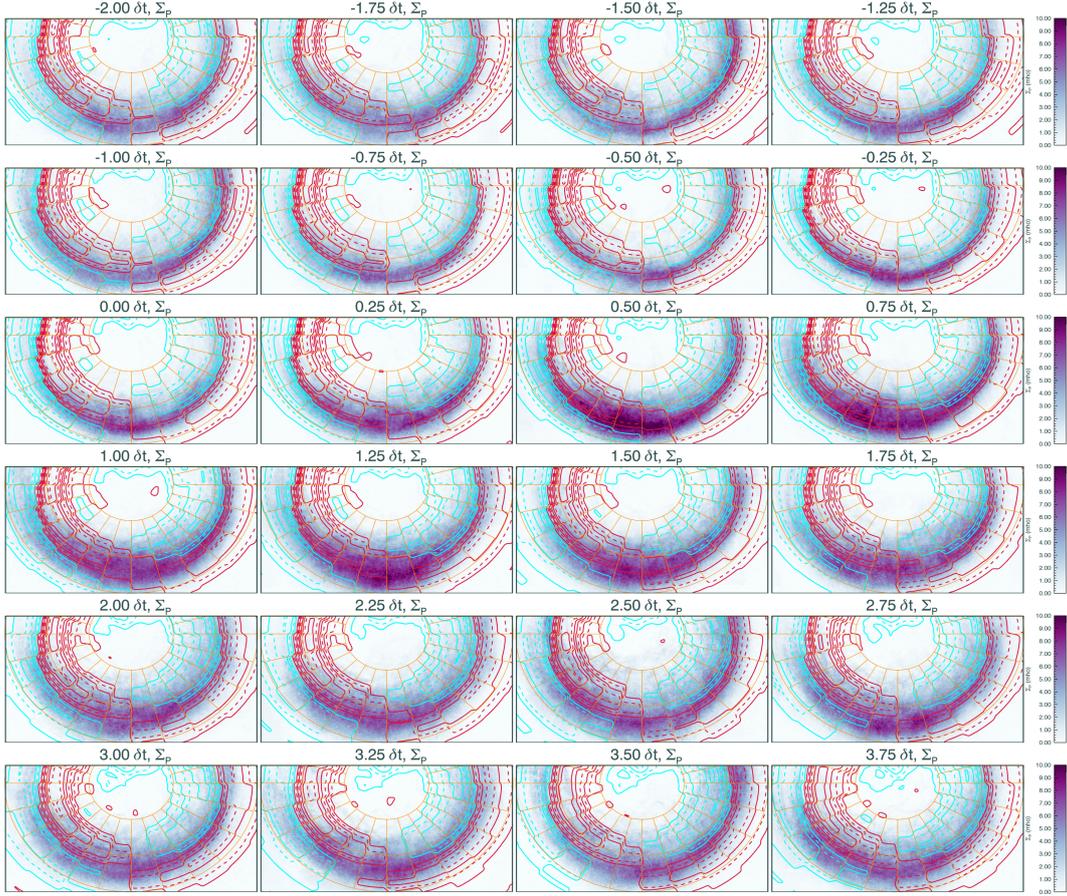


Figure 3. A series of images showing the nightside spatial distribution of height-integrated Pedersen conductance by substorm phase, for substorm onsets that occur between 63° to 65° degrees magnetic latitude. Each image is plotted on a magnetic-latitude, magnetic local time grid, with midnight to the bottom of each panel. On each panel we plot contours of the accompanying FAC distributions. Red contours are for upwards currents and blue contours are for downwards currents. Contours are plotted at intervals of $0.05 \mu\text{A m}^{-2}$.

191 FAC contours show little change in position throughout the substorm. The tech-
 192 nique employed here has smeared out the subtle approximately 1-degree latitudinal changes
 193 seen in FAC distributions in magnetic latitude, that are seen on a case to case basis (Coxon
 194 et al., 2014). However, evolution of the FACs over the course of a substorm are observed
 195 here, which we present later in this section.

196 In Fig. 5 we plot average E_0 and Q by MLT sector for a selection of MLTs, r the
 197 course of a substorm, for both the variable δt binning (top row), and a fixed time grid
 198 (bottom row). We observe the largest parameter values in all cases for the MLT = 23 hr
 199 sector ($\approx 4.3 \text{ keV}$, and $\approx 6.8 \text{ ergs cm}^{-2} \text{ s}^{-1}$). The lowest peak values for each variable are
 200 found at the extreme east and west edges of the selected MLTs, which peak below 4 keV
 201 and below $4 \text{ ergs cm}^{-2} \text{ s}^{-1}$, consistent with the literature, e.g. Walach et al. (2017). Al-
 202 most all E_0 increase simultaneously after onset, with a slight delay to the east and west.
 203 We do not see a clear faster change in E_0 eastwards, towards MLT = 02 hr, as compared
 204 to a slower expansion westwards to MLT = 21 hr, as implied by the work of Gjerloev et
 205 al. (2007). The mean energy flux Q rises sharply at onset for the fixed time binning, for
 206 all MLT sectors, whereas this is somewhat smeared out for the δt based grid. Q in the

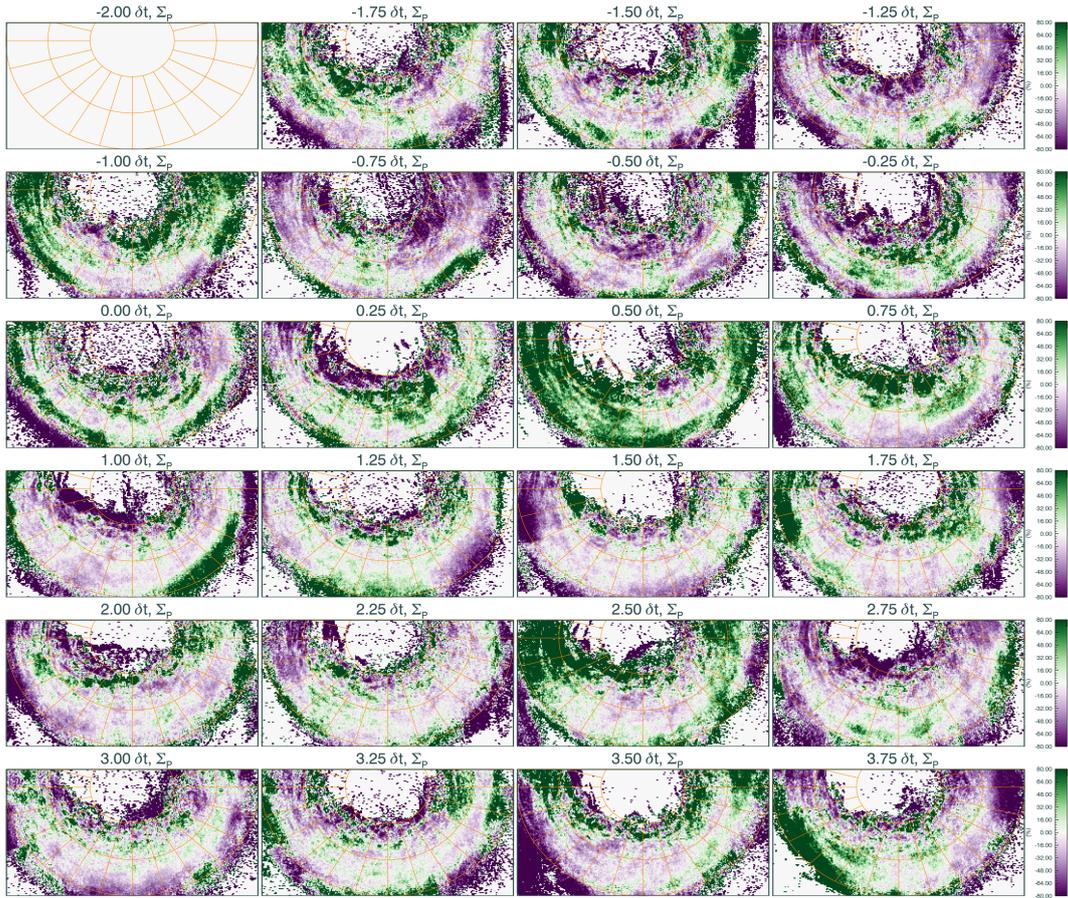


Figure 4. A series of images showing the percentage difference in Pedersen conductance from the previous normalised-time step, for substorm onsets that occur between 63° to 65° degrees magnetic latitude. The orientation and organisation of the plots is as in Fig. 3

207 MLT = 23 hr and MLT = 00 hr show a rapid reduction to levels similar to the other MLT
208 sectors by $2 \delta t$ or by 1.5 hr after onset.

209 We now explore the behavior of various parameters over the course of an average
210 substorm, at all substorm onset magnetic latitude bins. In Fig. 6 we plot a set of time
211 series with each step a multiple of δt as defined in Section 2. Each latitude bin is col-
212 ored according to the legend given in the plot. Parameters from the SSUSI stacked data
213 have been averaged over a wedge shape, within a MLT range of 21 hrs to 02 hrs and at
214 co-latitudes less than 30° to encompass the auroral bulge. We plot a time series of the
215 mean energy (E_0), energy flux (Q), and ratio between Q and E_0 , the mean height-integrated
216 Hall then Pedersen conductance, and then the mean Pedersen conductance offset from
217 the mean conductance in the time period from $-2 \delta t$ to $-0.5 \delta t$, i.e. prior to onset. We also
218 plot the mean up and down FAC densities, taken from all contributing individual val-
219 ues in a given spatial wedge shape. These values are averaged over all latitudes, but taken
220 in a narrow MLT sector between 4 hr and 5 hr MLT to encompass the maxima of the
221 region 2 FACs in the post midnight sector. The spatial selection applied here extracts
222 region 2 upwards FAC and region 1 downwards FAC.

223 In Fig. 6 (a)-(b) and (d)-(e), we observe that E_0 , and Q , and the conductances are
224 broadly ordered by magnetic latitude of onset. The peak parameter values are for the
225 second to lowest magnetic latitude substorms occurring between 63° to 65° . Hall and
226 Pedersen conductances peak at nearly 11 mho and 5 mho, respectively, for the 63° to
227 65° bin. All parameter values decrease with increasing magnetic latitude, although the
228 highest latitude bins over 71° are almost indistinct from one another. E_0 increases af-
229 ter onset, reaching a maximum of ≈ 3.5 keV within $1.25 \delta t$ after onset, with the excep-
230 tion of the lowest latitude substorms of 50° to 63° , which is slower to ramp up and peaks
231 at $1.75 \delta t$ at 3.2 keV. At the majority of these energies, the Gaussian assumption used
232 in the SSUSI data set gives lower Pedersen conductances as compared to the Maxwellian
233 assumption. An increase in Q is observed by $1 \delta t$ after onset, peaking at $4.3 \text{ erg cm}^{-2} \text{ s}^{-1}$.
234 The 63° to 65° substorms parameter values remain elevated after onset for the whole normalised-
235 time period shown ($4 \delta t$). To a lesser extent, this slow delay in recovery to pre-substorm
236 values is also seen in magnetic latitude bins 50° to 63° and 65° to 67° . Changes in E_0 ,
237 and Q are largest and slower to recover for the lowest magnetic latitude bins, which is
238 consistent with Grocott et al. (2009) and Milan et al. (2009) who showed that lower-latitude
239 onset substorms, with onsets at magnetic latitudes less than 65° , produced brighter auro-
240 ra that also persisted for longer. Following a detailed study of a substorm using pre-
241 cise but spatially constrained incoherent scatter radar measurements, Lester et al. (1996)
242 inferred an increase in precipitating particle energy to more than 10 keV during the sub-
243 storm recovery phase, or post $1 \delta t$ in comparison to the time series here, whereas they
244 observed that the expansion phase mean energy remained fairly constant at approximately
245 2.5 keV. This was for one substorm, detected by a set of magnetometers between 63.6°
246 and 67.3° magnetic latitude, and the mean energy here is slightly lower than 2 keV prior
247 to onset for magnetic latitudes between 65° to 67° . Here, we see an increase in precip-
248 itating energy before the recovery phase starts at $1 \delta t$, but a peak in energy after $1 \delta t$
249 to more modest mean energies up to a maximum of 3.6 keV, although here we average
250 over a wide range of magnetic local times.

251 Fig. 6 (c) shows the mean ratio between Q and E_0 during a substorm. This ratio
252 gives an indication of the number of precipitating particles. Most magnetic latitude bins,
253 exhibit a slight rise in the ratio from substorm onset at about $1.3 \text{ erg cm}^{-2} \text{ s}^{-1} \text{ keV}^{-1}$
254 to a maximum of $1.8 \text{ erg cm}^{-2} \text{ s}^{-1} \text{ keV}^{-1}$, an increase of approximately 40%, which lasts
255 until approximately $1.25 \delta t$ interval post onset. The highest latitude bin, for onsets above
256 73° , only sees an increase $0.5 \delta t$ after onset, but then shows a large variation in the ra-
257 tio. Similarly, the lowest latitude bin 50° and 63° , shows large variations in the ratio from
258 $1.75 \delta t$. Both these bins have the lowest number of contributing substorm onsets, and may
259 show the largest variation in substorm duration. Given the flatter changes in E_0 as com-

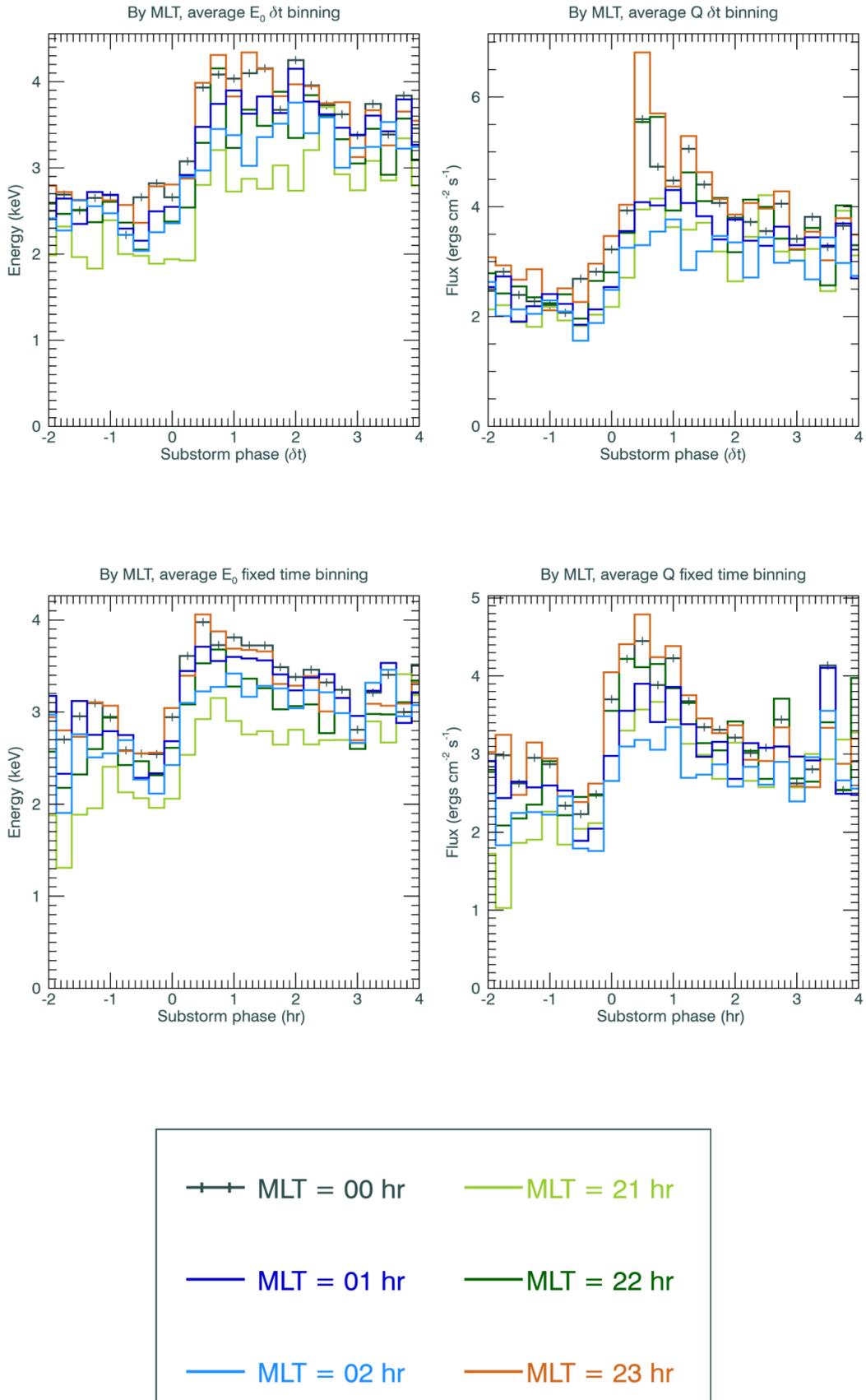


Figure 5. E_0 and Q over the course of a substorm by MLT, for substorms with onsets that occur between 63° to 65° degrees magnetic latitude. The top row is for the δt -defined time grid, and the bottom row for the fixed time binning.

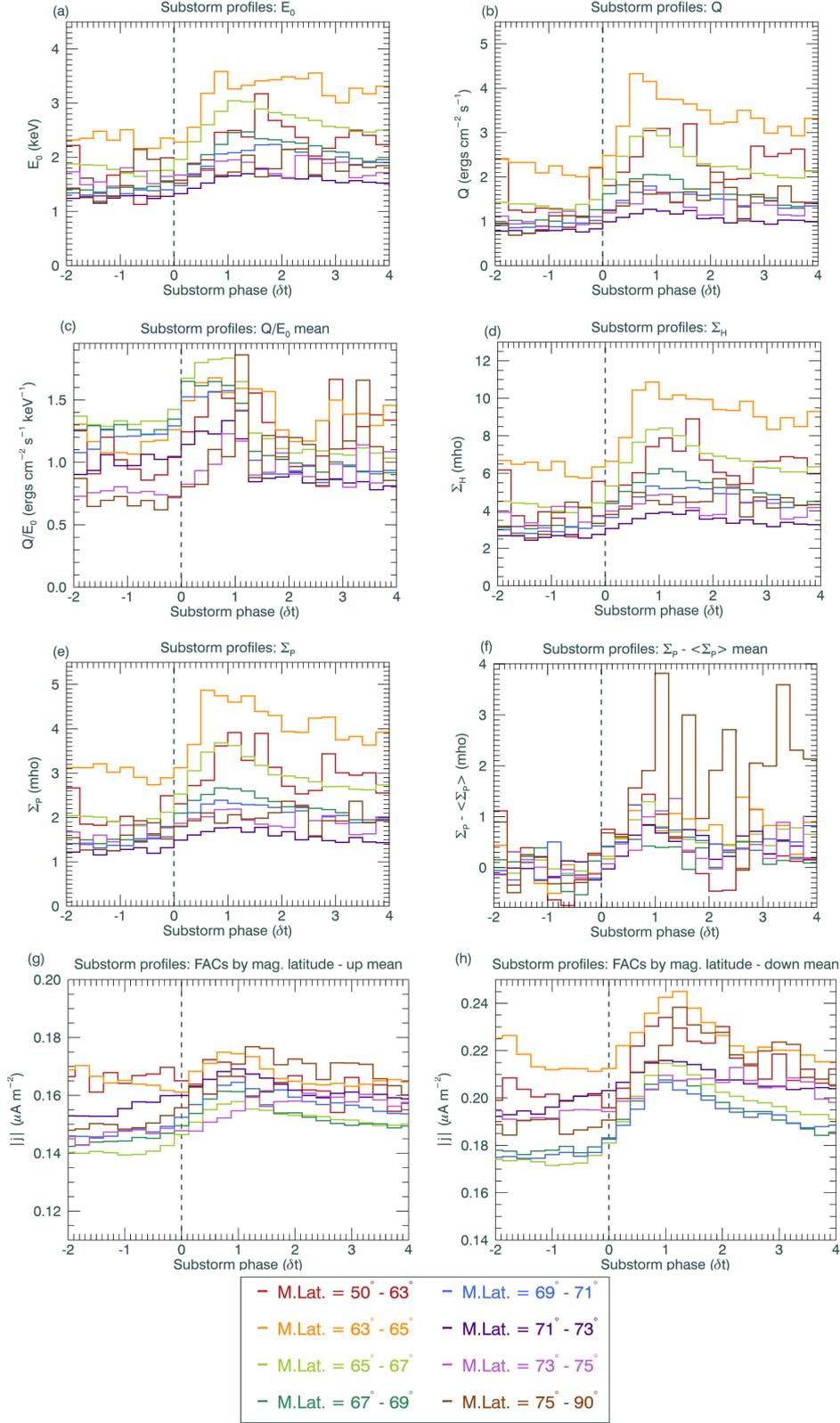


Figure 6. Adjusted time series of various quantities versus the δt defined step of an average substorm, by magnetic latitude bin, averaged over a restricted 21 hrs to 02 hrs MLT sector and down to latitudes of 30° . Panels (a) - (c): E_0 , then Q , and the ratio between them. Panels (d) - (f): Hall, and Pedersen mean height-integrated conductances, followed by the Pedersen conductance adjusted by the mean from $2\delta t$ to $0.5\delta t$ prior to onset. Panels (g) and (h): timeseries for average up, and then down FACs in a narrow MLT wedge, parameterised by magnetic latitude as the other parameters, over the course of an average substorm. A key to the color scheme is shown bottom right. Dashed vertical lines mark onset.

260 compared to Q , it appears that increases in mean energy flux Q at substorm onset is driv-
 261 ing changes after the recovery phase at $1 \delta t$, rather than any marked difference in the
 262 mean energy of the precipitating particles. We explore this issue in our discussion be-
 263 low.

264 In Fig. 6 (f), shows the Pedersen conductance offset from the average Pedersen con-
 265 ductance between $2 \delta t$ and $0.5 \delta t$ prior to onset. This plot reduces any biases in the data
 266 that may exist as the result of geomagnetic storms whereby large conductances prior to
 267 onset may influence our results. However, as we see no magnetic latitudinal dependence
 268 here, large geomagnetic storms do not appear to be causing any biases in the previous
 269 panels. The SOPHIE list uses the SuperMAG SML index in finding onsets. In the event
 270 of a large geomagnetic storm resulting in a long period decrease in the SML index, the
 271 SOPHIE technique is unlikely to find multiple instances of substorms occurring within
 272 an overall downward trend in SML. The highest latitude bin over 75° shows elevated val-
 273 ues above the mean after onset, and is likely to reflect weaker storms with a larger vari-
 274 ety of durations. Substorms within lower-latitudinal ranges are likely to have a longer
 275 duration. Milan et al. (2019, and references therein) explored convection braking for sub-
 276 storm with low-latitude onsets, and they quote a threshold of 65° magnetic latitude, above
 277 which convection braking is unlikely to occur. Onsets which start below 65° magnetic
 278 latitude are likely to have a more intense auroral response, leading to enhanced conduc-
 279 tance (e.g. in panel (e)) in the auroral bulge, which arrests the convection flow. We make
 280 no selection based on a minimum time between substorm onsets in our processing steps,
 281 and so our data set may include sawtooth events whereby a substorm-like signature is
 282 seen to repeat approximately every 3 hours (Borovsky et al., 1993), although these are
 283 rare phenomena occurring during enhanced geomagnetic activity (Walach & Milan, 2015).

284 In Fig. 6 (g) and (h), the upwards FACs show less clear behavior over the course
 285 of a substorm than the downwards FACs. We note a slow increase in the magnitude of
 286 the average upwards current building up to a maximum at $1 \delta t$, for the majority of the
 287 magnetic latitude bins. The largest current magnitudes are seen for the 63° to 65° and
 288 75° to 90° magnetic latitude bin. One exception occurs for the lowest bin of onsets, from
 289 50° to 63° which shows elevated average upwards current magnitudes prior to onset, which
 290 decrease after onset. Also, the bin from 73° to 75° shows a delayed and a very slow ramp
 291 up to the peak in the average upwards current magnitudes after more than $2 \delta t$. The up-
 292 wards FAC in the narrow MLT sector used for this time series represent region 2 FACs.
 293 Region 1 FACs have been shown to have higher current magnitudes compared to region
 294 2 FACs by about 20 % within 1 hour of onset on average (Coxon et al., 2014). We see
 295 in excess of 20 % greater FAC current magnitude between region 2 and region 1 (down-
 296 wards) FACs here.

297 The downwards, or region 1, FACs, do show a clearer ordering by magnetic lati-
 298 tude into two regimes, with the exception of the highest latitude onsets above 75° . Those
 299 for the lowest latitude bins, ranging from 50° to 65° magnitudes show much large av-
 300 erage downwards currents magnitudes than the other magnetic latitude bins, which in
 301 turn, show very little dependence on latitude above 65° . All magnetic latitude bins show
 302 an increase in current magnitude after onset, peaking in the main around $1 \delta t$. The cur-
 303 rent magnitudes recover similarly, and slowly between latitude bins after onset.

304 In Fig. 7 we show histograms of all the contributing or calculated values from the
 305 SSUSI and AMPERE data sets; for E_0 , Q , Hall and Pedersen conductances, and the FACs
 306 split into up, red, and down, blue, currents. The FACs are given for the whole data set,
 307 regardless of substorm onset latitude. E_0 is limited to 20 keV through the SSUSI data
 308 processing procedures, and the distribution by energy is not dependent on the magnetic
 309 latitude of onset. The Q values show a separation by substorm onset magnetic latitude,
 310 whereby the 63° to 65° magnetic latitude bin exhibits the highest values of Q , and across
 311 all Q this latitude bin has a larger number of contributing points. Therefore we postu-
 312 late that enhanced conductances for substorms occurring between magnetic latitudes of

313 63° to 65° appear driven by increased flux, rather than an increase in the energy of pre-
 314 cipitating particles. Individual Hall and Pedersen conductances, calculated from indi-
 315 vidual pixel measurements, can peak at over 200 mho or 60 mho respectively.

316 In Fig. 8 we plot a similar set of panels as for Fig. 6, but instead of using the δt
 317 time step, calculated for each contributing substorm individually, we use a simple fixed
 318 time step of 0.25 hours to perform the superposed epoch analysis.

319 The fixed binning time series shows similar behavior to that based on δt . The mag-
 320 netic latitude bin with the largest values of E_0 and Q at substorm onset is 63° to 65°,
 321 as before for the δt grid. The lowest magnetic latitude bin, for 50° to 63° is the most
 322 erratic. The large values at the beginning and end of the substorm period around 2 hr
 323 prior or beyond 3 hr after onset may indicate that after this time it is likely that a sec-
 324 ond substorm had occurred so that at the extremes of the time series overlapping sub-
 325 storms are being detected. The remaining bins are ordered by magnetic latitude, whereby
 326 the largest parameter values seen for the lowest magnetic latitude onsets, as seen pre-
 327 viously. As before, parameters peak before 1 hour after onset. FAC magnitudes for these
 328 fixed bins are strongest for the lowest three latitude bins, as seen previously, and again
 329 this is most apparent for the downwards (region 1) FACs. Here, the 63° to 65° current
 330 magnitudes are largest by some margin, for both upwards and downwards FACs.

331 The normalisation of the substorms to δt , defined as the duration of the expansion
 332 phase, that we used in this work may still hide features of the progression of a substorm.
 333 In this paper, we normalise the time series to multiples of δt . The modal δt value is shown
 334 in Fig. 1 to between 0.10 and 0.20 hr, or 6 to 12 minutes. Walach et al. (2017) made a
 335 statistical study of substorms using images of ultraviolet aurora, and saw the expansion
 336 phase typically lasting from 10 to 20 minutes after onset of the electron aurora, so there-
 337 fore we justify the use of the independently calculated δt for binning of the conductances,
 338 derived from auroral data, in this paper. It is not necessarily the case that a longer total-
 339 duration substorm will have a longer expansion phase, nor is it true that conversely, shorter
 340 total-duration substorms have shorter expansion phases. The end of the recovery phase,
 341 when the auroral electrojet lower envelope boundary returns to a quiescent state and which
 342 would enable the calculation of the overall duration of each substorm, is not stored in
 343 the Forsyth et al. (2015) list. Walach et al. (2017) observed the recovery phase to oc-
 344 cur by 50 minutes post onset for the electron aurora, which for a modal δt of 0.15 hr equates
 345 to 1.25 δt . We see a peak in parameter values starting before 1 δt , but a slow recovery
 346 to values prior to onset. Smearing of the data will inevitably occur over either the δt or
 347 fixed-time grid. Even so, the binning used in this paper is able to order the height-integrated
 348 conductances, E_0 , Q , and region 1 downwards FACs by magnetic latitude of onset.

349 The dominance of high-parameter values for substorms with onsets that occur be-
 350 tween 63° to 65° magnetic latitude is still to be determined. The influence of the ring
 351 current modulating tail reconnection and arresting substorm onset may play a part (Milan
 352 et al., 2021). We leave this to future investigation.

353 4 Conclusions

354 We have examined the behavior of mean energy, mean energy flux, and height-integrated
 355 conductances over the course of a substorm, using a superposed epoch analysis of au-
 356 roral emissions derived parameters. We examined the behavior on both an artificial, normalised-
 357 time grid based on the duration of the expansion phase, and a fixed time grid. Average
 358 substorm timeseries are found for a set separated by the magnetic latitude of substorm
 359 onset into broad bins of different widths between 50° to approximately 80°. For both
 360 normalised and fixed time grids, the maximum parameter values were observed for on-
 361 sets that occur between 63° to 65° magnetic latitude. Why this latitude bin shows larger
 362 parameter values is still to be determined. Changes in the mean energy flux shortly af-

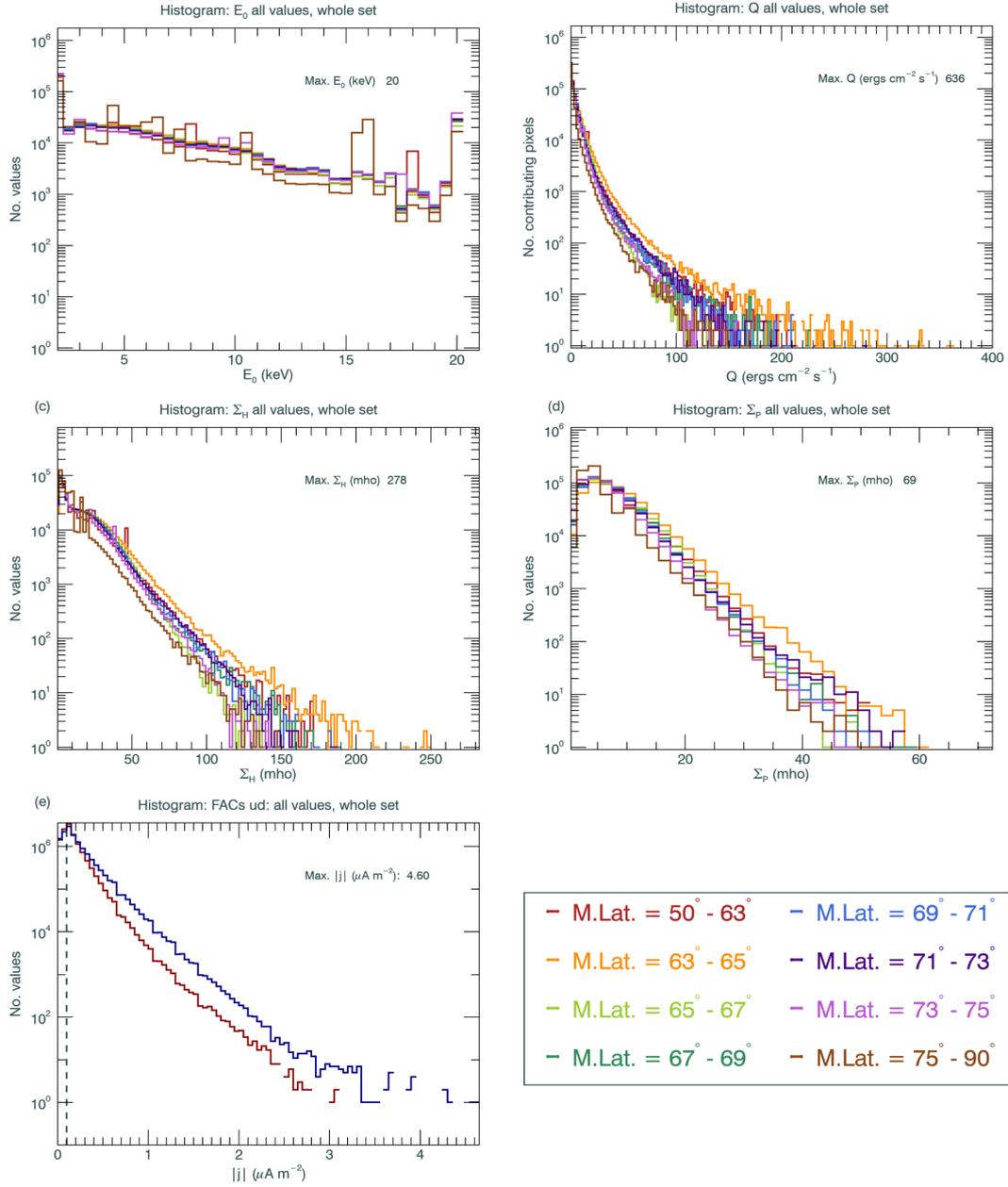


Figure 7. A set of histograms showing the distribution of all contributing data parameters for E_0 , Q , Hall and Pedersen conductances, and the FACs split into up, red, and down, blue, currents. The Q panel has a restricted x-axis range to better show differences between magnetic latitude bins. The dashed line in (e) shows the threshold current density applied to the AMPERE data set.

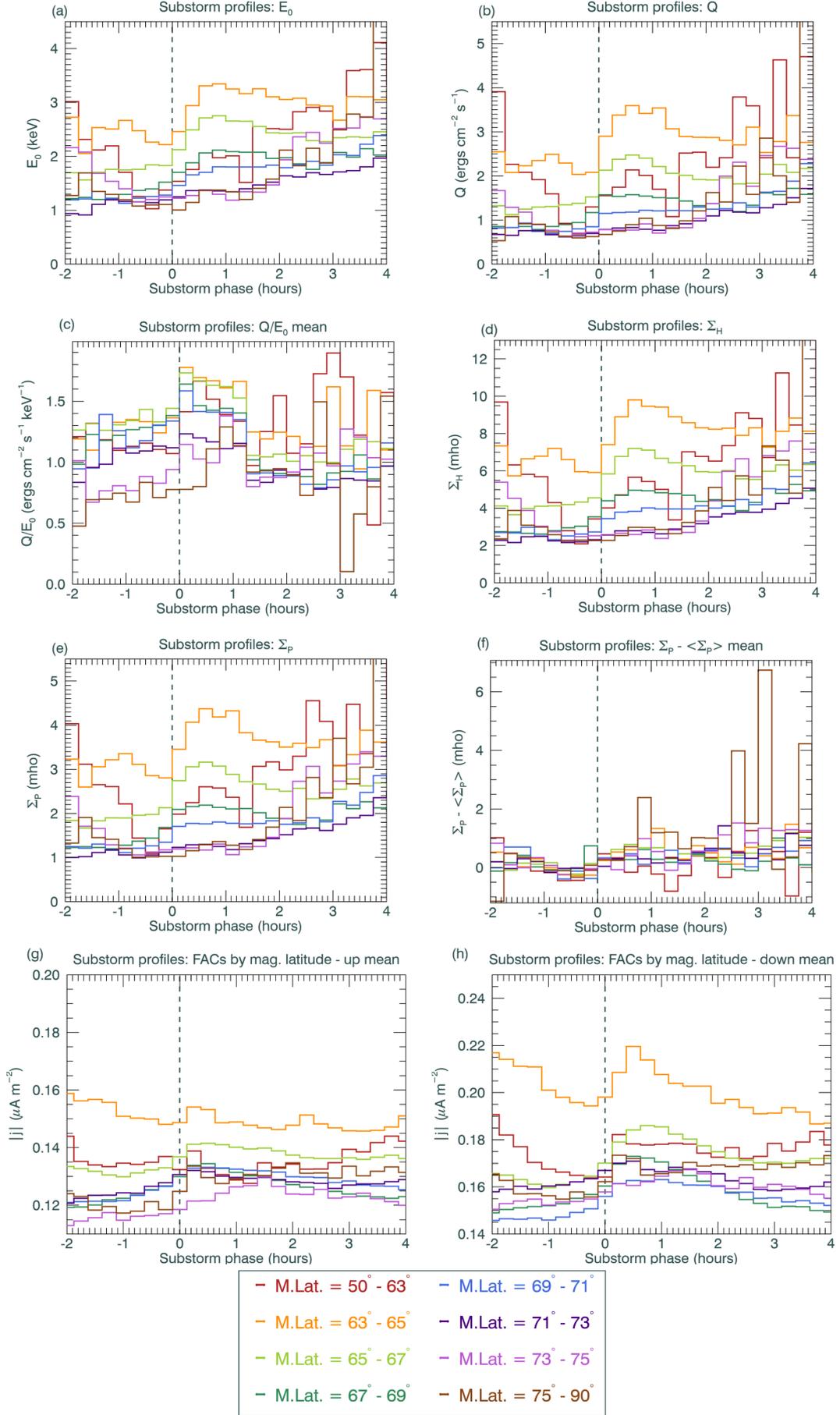


Figure 8. A set of time series in the same layout as Fig. 6, but using a fixed time step of 0.25 h for the superposed epoch analysis.

363 ter substorm onset are greater than changes in the mean energy of the precipitation. Higher
 364 magnetic latitude onsets exhibit lower values, throughout an entire substorm. For the
 365 normalised time binning, magnetic latitude onsets behave similarly over the course of
 366 a substorm, with values peaking by the start of the recovery phase, and decaying after-
 367 wards. Lower latitude onset parameters decay slower to their pre-onset values than high
 368 latitude onsets. The fixed time binning series are likely to include several overlapping
 369 substorms, which affects the lowest magnetic latitude bin the most. FACs respond to a
 370 substorm in a similar manner to the auroral parameters, and this is most apparent in
 371 the downwards current magnitudes. FAC current magnitudes are also ordered by mag-
 372 netic latitude, so that the lower magnitude latitude onsets exhibit the highest current
 373 magnitudes.

374 This work uses auroral emissions that are obtained by low-altitude spacecraft ob-
 375 serving the ionosphere from above, with the advantage of observing large areas of the
 376 polar cap over short durations. Future work will involve comparing the wide-field aurora-
 377 derived parameters with those obtained incoherent radar data taken from ground-based
 378 facilities to verify the technique in a spatially constrained region.

379 5 Open Research

380 The DMSP/SSUSI file type EDR-AUR data were obtained from <http://ssusi.jhuapl.edu>
 381 (data version 0106, software version 7.0.0, calibration period version E0018). AMPERE
 382 data were obtained from <http://ampere.jhuapl.edu>. The AMPERE-derived region 1 re-
 383 gion 2 FAC radii are stored at <https://doi.org/10.25392/leicester.data.11294861.v1>. Su-
 384 perMAG data can be found via the portal at <http://supermag.jhuapl.edu>.

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