# The time scale of shallow convective self-aggregation in large-eddy simulations is sensitive to numerics

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#### Abstract

Numerical simulations of the tropical mesoscales often exhibit a self-reinforcing feedback between cumulus convection and shallow circulations, which leads to the self-aggregation of large cloud structures. We investigate whether this basic feedback can be adequately captured by large-eddy simulations (LESs). To do so, we simulate the non-precipitating, cumulus-topped boundary layer of the canonical 'BOMEX'; case over a range of numerical settings in two models. Since the energetic convective scales underpinning the self-aggregation are only slightly larger than typical LES grid spacings, aggregation timescales do not converge even at rather high resolutions (less than 100m). Therefore, high resolutions or improved unresolved scales models may be required to faithfully represent certain forms of trade-wind mesoscale cloud patterns and self-aggregating deep convection in large-eddy and cloud-resolving models, and to understand their significance relative to other processes that organise the tropical mesoscales.

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#### Key Points:

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10	• In large-eddy simulations, sub-kilometre scale cumulus convection self-organises
11	into mesoscale structures through shallow circulations
12	• The aggregation time-scale does not converge with model resolution for typical
13	discretisation choices.
14	• Numerical representations of the tropical mesoscales may require finer model res-
15	olutions than previously thought

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#### 16 Abstract

Numerical simulations of the tropical mesoscales often exhibit a self-reinforcing feedback 17 between cumulus convection and shallow circulations, which leads to the self-aggregation 18 of large cloud structures. We investigate whether this basic feedback can be adequately 19 captured by large-eddy simulations (LESs). To do so, we simulate the non-precipitating, 20 cumulus-topped boundary layer of the canonical 'BOMEX' case over a range of numer-21 ical settings in two models. Since the energetic convective scales underpinning the self-22 aggregation are only slightly larger than typical LES grid spacings, aggregation timescales 23 do not converge even at rather high resolutions (<100m). Therefore, high resolutions or 24 improved unresolved scales models may be required to faithfully represent certain forms 25 of trade-wind mesoscale cloud patterns and self-aggregating deep convection in large-eddy 26 and cloud-resolving models, and to understand their significance relative to other pro-27 cesses that organise the tropical mesoscales. 28

## <sup>29</sup> Plain Language Summary

The most detailed models of our atmosphere frequently have their clouds spontaneously 30 organise into large clusters. Small clouds (less than a kilometre in size) seem to play an 31 important role in such "self-aggregation". However, even in detailed models small clouds 32 are hard to adequately capture: Typically, they must resolve such clouds using less than 33 10 pixels, thus requiring additional, lower-accuracy "unresolved-scales" models for cloudy 34 motions smaller than this resolution. Here, we show that merely varying the resolution 35 of several state-of-the-art atmospheric models has an effect on how quickly they predict 36 the self-aggregation of clouds to occur, even when many complex, uncertain processes 37 are removed from the problem. We hypothesise that this is because several fundamen-38 tal assumptions of our unresolved scales models are commonly violated in simulations 39 of self-aggregating clouds. To help work out how important self-aggregation is in the real 40 world, models of the phenomenon may therefore require higher numerical resolutions than 41 previously thought. 42

#### 43 **1** Introduction

A striking feature of idealised simulations of the tropical atmosphere in radiative-44 convective equilibrium (RCE) is the spontaneous aggregation of their column-integrated 45 moisture and convection into large clusters (Bretherton et al., 2005; Muller & Held, 2012). 46 Many mechanisms have been proposed to explain this, including the collision and con-47 vective triggering of horizontally expanding and colliding cold pools of evaporated pre-48 cipitation (Tompkins, 2001; Böing, 2016; Haerter, 2019) and gravity wave-convection in-49 teractions (Yang, 2021). Yet, perhaps the strongest consensus is on the importance of 50 shallow circulations (Shamekh et al., 2020; Muller et al., 2022), configured to transport 51 moisture from dry to moist columns. 52

These circulations can be traced to differential, radiative cooling between moist re-53 gions, which trap outgoing longwave radiation in their moisture-rich lower atmosphere 54 and under high clouds, and dry regions, which more readily radiate their thermal energy 55 to space (Muller & Held, 2012). Such heating anomalies give rise to ascent in moist columns 56 and descent in dry columns, and may be framed as moisture-radiation instabilities (Emanuel 57 et al., 2014; Beucler & Cronin, 2016) with negative moist gross stability (Bretherton et 58 al., 2005; Raymond et al., 2009). However, the circulations may also be reinforced by tur-59 bulent mixing at cloud edges, which deposits moisture in the free troposphere and thus 60 raises the livelihood and vigour of any subsequent convection; differential convection may 61 then itself result in a net ascent of moist, convecting regions and descent in dry, non-convecting 62 regions (Grabowski & Moncrieff, 2004; Tompkins & Semie, 2017). Interactions between 63 these radiative and convective feedbacks appear important, and their relative significance 64 is debated (Beucler et al., 2018; Kuang, 2018). 65

Rooting deep convective self-aggregation in shallow circulations implicitly under-66 lines the importance of shallow convection in developing and maintaining them. Bretherton 67 et al. (2005); Muller and Held (2012) make this connection explicit; they show that shal-68 low convection in dry regions exports moist static energy, an appropriate energetic measure of the moisture, to moist, deep convective regions. If one removes cold-pool feed-70 backs, the shallow circulation is even more tightly coupled to the effects of shallow, non-71 precipitating convection. In such situations, self-aggregation occurs also on smaller do-72 mains (Jeevanjee & Romps, 2013) and without requiring radiative feedbacks (Muller & 73 Bony, 2015). 74

Interestingly, shallow cumulus convection under typical trade-wind conditions also 75 self-organises into clusters much larger than that of individual cumuli (e.g. Narenpitak 76 et al., 2021). Bretherton and Blossey (2017); Janssens et al. (2022) attribute such ag-77 gregation to the convective feedback: Shallow circulations driven by anomalous latent 78 heating in shallow cumulus transport moisture from dry to moist regions in the absence 79 of radiative or precipitating heterogeneity. If integrated over sufficiently long time pe-80 riods, simulations of this mechanism aggregate enough moisture into their moist regions 81 to transition into deep, organised convection (see also Vogel et al., 2016). These stud-82 ies likely describe the confluence of shallow convective instability and the deep convec-83 tive instabilities described by Jeevanjee and Romps (2013); Muller and Bony (2015), and 84 grounds the latter in the former. 85

These paragraphs serve to illustrate that an extensive body of work may rely rather strongly on how well the numerical models used to simulate convective self-aggregation represent shallow convection. To remain tractable when running on domains of O(1000)km, numerical simulations of self-organisation often employ rather coarse grid spacings (usually greater than 1 km). At such grid spacings, shallow convection, whose energetic scales themselves lie around 1 km, are at best barely resolved, and at worst parameterised.

This is relevant, since convective self-aggregation is sensitive to numerical settings 92 and parameterisations in cloud-resolving simulations of deep convection (Muller & Held, 93 2012; Wing et al., 2020) and large-eddy simulations (LESs) of cold pool-driven pattern 94 formation in shallow convection (Seifert & Heus, 2013). One may therefore wonder if the 95 self-aggregation of non-precipitating cumulus is subject to similar sensitivities, whether 96 this matters when attempting to interpret numerical simulations of deep convective self-97 aggregation and ultimately how much the phenomenon bears on reality. This motivates 98 us to ask the question: Can we consistently represent convective self-aggregation in its 99 most basic form - shallow, non-precipitating cumulus convection - in LES? 100

Guided by this question, we revisit a classical case of non-precipitating shallow cu-101 mulus convection and simulate it on a mesoscale domain in several numerical configu-102 rations (section 2). We then summarise the feedback mechanism discussed by Bretherton 103 and Blossey (2017); Janssens et al. (2022) that drives the self-aggregation in these sim-104 ulations (section 3). Next, we demonstrate the multiscale nature of the feedback: Small, 105 cumulus-scale processes drive moisture variability at scales an order of magnitude larger 106 (section 4). This renders it sensitive to three choices that govern the effective resolution 107 of finite-volume-based LES: grid spacing, advection scheme and unresolved scales model 108 (section 5). We discuss the implications of these findings for modelling studies of shal-109 low and deep convective self-aggregation and their potential parameterisation in section 110 6, before summarising in section 7. 111

#### 112 2 Numerical Simulations

#### 2.1 Case study

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Our study concerns a set of numerical experiments of the "undisturbed period" during the Barbados Oceanographic and Meteorological Experiment (BOMEX), as introduced to the LES modelling community by Siebesma and Cuijpers (1995). We concen trate on BOMEX because it represents the simplest imaginable setting of shallow cu mulus convection, simulating only moist thermodynamics and boundary-layer turbulence.

Three assumptions made in the composition of our case deserve mention here. First, 119 in lieu of representing spatial and temporal variability in i) the large-scale subsidence, 120 ii) horizontal wind and iii) surface fluxes of heat and moisture, we parameterise such larger-121 scale and boundary forcings with profiles that vary only in height. Second, we do not 122 locally calculate radiative heating rates, instead approximating them with a slab-averaged 123 cooling. Third, we explicitly ignore the formation and impact of precipitation. We will 124 therefore suppress aggregation that is forced on our cloud-field by vertical motions of a 125 scale larger than our domain, such as those imposed in the simulations conducted by Narenpitak 126 et al. (2021) and observed by George et al. (2022), by radiation heterogeneity (Klinger 127 et al., 2017) and by cold-pool dynamics (e.g. Seifert & Heus, 2013; Seifert et al., 2015; 128 Anurose et al., 2020; Lamaakel & Matheou, 2022) respectively, all of which appear im-129 portant pathways to develop the mesoscale cumulus patterns observed in nature. 130

We justify the neglect of these processes by noting that they are not necessary for large, aggregated cumulus structures to develop (Bretherton & Blossey, 2017). Instead, they accelerate and modulate an internal mechanism that also occurs without them. This feedback is intrinsic to moist, shallow convection (Janssens et al., 2022), and its sensitivity to resolution is most clearly exposed by only studying this aspect. We will return briefly to this discussion in section 6.

#### 137 2.2 Numerical model

We perform simulations with two models: The Dutch Atmospheric Large Eddy Simulaton (DALES, Heus et al., 2010; Ouwersloot et al., 2017) and MicroHH (Van Heerwaarden et al., 2017). Both models attain a numerical representation of the atmospheric state on a staggered grid by solving filtered, finite difference approximations of the conservation equations of mass, momentum, and scalars in the anelastic approximation:

$$\frac{\partial}{\partial x_j} \left( \rho_0 u_j \right) = 0 \tag{1}$$

$$\frac{\partial u_i}{\partial t} = -\frac{1}{\rho_0} \frac{\partial}{\partial x_j} \left(\rho_0 u_i u_j\right) - \frac{\partial \pi'}{\partial x_i} + \frac{g}{\overline{\theta_v}} \left(\theta_v - \overline{\theta_v}\right) \delta_{i3} - \frac{\partial \tau_{ij}}{\partial x_j} + S_{u_i} \tag{2}$$

$$\frac{\partial \chi_i}{\partial t} = -\frac{1}{\rho_0} \frac{\partial}{\partial x_j} \left( \rho_0 u_j \chi_i \right) - \frac{\partial R_{u_j, \chi_i}}{\partial x_j} + S_{\chi_i},\tag{3}$$

In these equations,  $u_i \in \{u, v, w\}$  are the three (grid-filtered) components of velocity,  $\chi_i \in \{\theta_l, q_t\}$  is a generic scalar whose set contains at least the total specific humidity  $q_t$  and liquid-water potential temperature, approximated as

$$\theta_l \approx \theta - \frac{L_v}{c_p \Pi} q_l. \tag{4}$$

where  $\theta$  is the (dry) potential temperature,  $L_v$  is the latent heat of vaporisation,  $c_p$  is the specific heat of dry air at constant pressure,  $q_l$  is the liquid water specific humidity and

$$\Pi = \left(\frac{p}{p_0}\right)^{\frac{R_d}{c_p}} \tag{5}$$

is the Exner function, where  $R_d$  is the gas constant of dry air and p is the reference pressure profile. The corresponding reference density is  $\rho_0$ ,  $\pi'$  are fluctuations of modified

pressure around p, g is gravitational acceleration,  $\theta_v$  is the virtual potential temperature 151 whose slab-mean is represented by an overbar,  $S_{u_i}$  and  $S_{\chi_i}$  denote momentum and scalar 152 sources, and  $\tau_{ij}$  and  $R_{u_j,\chi_i}$  are the residual fluxes of momentum and scalars that result 153 from filtering the equations (the Sub-Filter Scale (SFS) fluxes). These fluxes are approx-154 imated with a traditional eddy viscosity model, which explicitly assumes the filtering to 155 take place at a scale where diffusion of the resolved flow approximates the net dissipa-156 tion of homogeneous, isotropic turbulence; it must be significantly smaller than the energy-157 containing scales of the simulation: 158

$$\tau_{ij} \approx -K_m \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \tag{6}$$

$$R_{u_j,\chi_i} \approx -K_h \frac{\partial \chi_i}{\partial x_j} \tag{7}$$

These approximations introduce modelling errors which can be expected to influence the large, resolved scales when their requirements are not met.

The main differences between DALES and MicroHH reside in their model for the eddy diffusivities  $K_m$  and  $K_h$ : DALES uses a one-equation closure for the turbulent kinetic energy e (Deardorff, 1973) subject to Deardorff (1980)'s stability correction; MicroHH employs a stability-corrected Lilly-Smagorinsky model (Lilly, 1968). Both models estimate  $K_m$  and  $K_h$  through a mixing length  $\lambda$  associated with the grid-scale filter:

$$\lambda = f\left(\Delta\right),\tag{8}$$

$$\Delta = \left(\Delta x \Delta y \Delta z\right)^{\frac{1}{3}},\tag{9}$$

where f subsumes the stability correction, which diminishes the eddy diffusivities in stably stratified grid cells, and where  $\Delta$  assumes the grid spacing is isotropic, which is an assumption we will violate. Note that  $\Delta$  also sets the discretisation error in the model's spatial gradients for a finite difference scheme of a given order; these errors will interact non-trivially with the modelling error made by the approximations above.

#### **2.3 Experiments**

We base our analysis on 8 simulations of BOMEX that are set up in the configu-172 ration reported by Siebesma et al. (2003), except for their computational grid, integra-173 tion time and advection scheme. To support mesoscale fluctuations with little influence 174 from the finite domain size, the cases are run on domains with horizontal length L =175 102.4 km, a height of 10 km, for 36 hours. The vertical grid spacing  $\Delta z = 40$  m up to 176 6 km, and is stretched by 1.7% per level above this height. To investigate how the de-177 velopment of mesoscale fluctuations is sensitive to numerics, we vary the horizontal grid 178 spacing  $\Delta x = \Delta y \in [50, 100, 200]$  m. At their coarsest spacing, our grid cells attain 179 rather high aspect ratios. Such anisotropic grids are commonly used in large-domain LES 180 of shallow cumulus convection (e.g. Vogel et al., 2016; Klinger et al., 2017; Bretherton 181 & Blossey, 2017; Janssens et al., 2022), although the isotropic filter length scale  $\lambda$  con-182 sequently overestimates the vertical length scale required from the SFS model, and un-183 derestimates the horizontal length scale (de Roode et al., 2022). As will become clear 184 in section 5, we will be particularly concerned with the underestimation of the horizon-185 tal length scale. Therefore, we also run the DALES simulations at  $\Delta x = 200$  m with 186  $\Delta = 200 \text{ m}.$ 187

All cases are run with a variance-preserving, second order central difference scheme to represent advective transfer, while the coarsest two DALES simulations are additionally run using a fifth order, nearly monotonic scheme (Wicker & Skamarock, 2002). This

**Table 1.** Differences in numerical configurations of BOMEX simulations. e refers to the oneequation turbulence kinetic energy SFS model (Deardorff, 1973); SL refers to the Smagorinsky-Lilly model (Lilly, 1968). Advection schemes are either O(2) central differences (a2), or the O(5) scheme by Wicker and Skamarock (2002) (a5). 'fiso' refers to coarsening the filter as if it were isotropically increasing with the horizontal grid spacing, while 'nocorr' denotes a run with Deardorff (1980)'s stability correction turned off.

Abbreviation	Model	$\Delta x$	SFS model	Advection scheme	$\Delta$
D1	DALES	200	e	O(2) a2	117
D2	DALES	200	e	O(5) a5	117
D3	DALES	200	e	O(2) a2	200, fiso
D4	DALES	100	e	O(2) a2	73.7
D5	DALES	100	e	O(5) a5	73.7
D6	DALES	100	e	O(5) a2	73.7, nocorr
D7	DALES	50	e	O(2) a2	46.4
M1	MicroHH	200	$\operatorname{SL}$	O(2) a2	117
M2	MicroHH	100	$\operatorname{SL}$	O(2) a2	73.7
M3	MicroHH	50	$\operatorname{SL}$	O(2) a2	46.4

scheme is rather diffusive, consequently dampens the (co)variance contained in the smallest, resolved scales of the simulations we run (Heinze et al., 2015), and has an effective
resolution commensurate with the five grid-point stencil it requires (Bryan et al., 2003).

<sup>194</sup> These properties have significant consequences.

Finally, we test the effects of the stability correction on  $\lambda$  by running a single simulation where it is turned off.

We focus our analysis of the simulations on the period before their characteristic moisture length scales approach the domain size, as we wish to eliminate the finite-domain constraints posed by our doubly-periodic boundary conditions.

#### <sup>200</sup> 3 Conceptual model for self-aggregation

We will study the numerical sensitivity of the shallow convective self-aggregation using the conceptual model described by Janssens et al. (2022), which is a closed-form version of the theory introduced by Bretherton and Blossey (2017). The model is briefly summarised in this section; readers looking for a full derivation are encouraged to explore the above manuscripts.

206 **3.1 Definitions** 

In the following, self-aggregation of the convection in our simulations will be interpreted as growth in mesoscale fluctuations of vertically integrated moisture. To make this more precise, let us define mesoscale fluctuations in a generic scalar  $\chi$  by partitioning it into its slab-average  $\overline{\chi}$  and remaining fluctuation  $\chi'$ , before scale-separating  $\chi'$  into a mesoscale component  $\chi'_m$  and sub-mesoscale component  $\chi'_s$ :

$$\chi = \overline{\chi} + \chi' = \overline{\chi} + \chi'_m + \chi'_s. \tag{10}$$

 $\chi'_m$  is defined with a spectral low-pass filter at 12.5 km, i.e. fluctuations larger than this scale are considered mesoscale fluctuations. In our framework, self-aggregation is associated with the development of coherent, mesoscale moist, convecting regions, where  $q'_{t_m} > 0$ , and dry, non-convecting regions, where  $q'_{t_m} < 0$ . To identify these regions in our simulations, we use the density-weighted vertical average

$$\langle \chi \rangle = \frac{\int_0^{z_\infty} \rho_0 \chi dz}{\int_0^{z_\infty} \rho_0 dz},\tag{11}$$

where  $z_{\infty} = 10$  km, yielding the column-averaged, or bulk, moisture  $\langle q_t \rangle$ . Moist (dry), mesoscale regions as positions where  $\langle q'_{t_m} \rangle > 0$  ( $\langle q'_{t_m} \rangle < 0$ ).

With these definitions, we formulate a budget for  $\chi'_m$  by subtracting the slab-average of eq. 3 from itself, mesoscale-filtering the result, and rewriting several terms:

$$\frac{\partial \chi'_m}{\partial t} = \underbrace{-w'_m \Gamma_{\chi}}_{\text{Grad. prod.}} \underbrace{-\frac{\partial}{\partial x_{j_h}} (u_{j_h} \chi')_m}_{\text{Horizontal transport}} \underbrace{-\frac{1}{\rho_0} \frac{\partial}{\partial z} (\rho_0 F_{\chi'_m})}_{\text{Vertical transport}} \underbrace{-\overline{w_{ls}} \frac{\partial \chi'_m}{\partial z}}_{\text{Subsidence}} \underbrace{+\frac{\partial}{\partial x_j} (R_{u_j,\chi'_m})}_{\text{SFS diffusion}} \underbrace{+S'_{\chi_m}}_{\text{Source}}$$
(12)

In this relation, the slab-averaged vertical gradient  $\partial \overline{\chi} / \partial z = \Gamma_{\chi}$ , while  $F_{\chi'_m}$  is the anomalous mesoscale vertical flux of  $\chi'$  around the slab average

$$F_{\chi'_m} = (w'\chi')_m - \overline{w'\chi'}.$$
(13)

The conceptual model requires eq. 12 to be posed for measures of moisture and heat. To remain consistent with Bretherton and Blossey (2017); Janssens et al. (2022), we will use  $q_t$  as our moisture variable, and liquid-water virtual potential temperature, defined as

$$\theta_{lv} = \theta_l + 0.608\overline{\theta_l}q_t \equiv \theta_v - 7\overline{\theta_l}q_l, \tag{14}$$

as our heat variable (e.g. B. Stevens, 2007). Both  $q_t$  and  $\theta_{lv}$  are conserved under nonprecipitating shallow cumulus convection. Hence, in the absence of radiative heterogeneity, we immediately recognise that  $S'_{\chi_m} = 0$ . In the following, we will additionally assume that the direct effects of horizontal transport, subsidence and SFS diffusion on the  $\chi'_m$  budget are small.

#### 3.2 Model

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The main features of the conceptual model are captured by fig. 1. Its central panel shows a vertical cross-section of simulation D1 after 16 hours of simulation time, coloured by  $q_t$ . Clouds are drawn on top of the  $q_t$  field as small, black contour lines. They form preferentially on an anomalously moist, mesoscale patch in the cloud layer (smooth, black contour line, delineating the boundary where  $q'_{t_m} = 0$ ); convection and clouds have selfaggregated into mesoscale structures in this panel.

To explain why, we begin at fig. 1 a), which shows a progressing contrast in  $q'_{t_m}$  between moist (blue) and dry (red) regions near the inversion base. Upon vertically averaging eq. 12, it can be shown that the resulting increase in  $\langle q'_{t_m} \rangle$  is due primarily to the "gradient production" term, i.e.

$$\frac{\partial \langle q'_{t_m} \rangle}{\partial t} \approx -\langle w'_m \Gamma_{q_t} \rangle \tag{15}$$



Figure 1. Overview over the circulation-driven self-aggregation mechanism in simulation D1 after 16 hours. Central panel: Example x-z cross-section depicting clouds (small, jagged black contours), which form favourably on a moist, mesoscale region (coloured contours; large, smooth, black contour), in turn driven by a mesoscale circulation (streamlines). Horizontal lines indicate the cloud and inversion bases. a) Vertical profiles of  $q'_{tm}$  and  $w'_m$ , averaged over moist (blue) and dry (red) regions, evolving in time (increasing opacity). b) WTG approximation eq. 17 (maroon) of  $w'_m$  compared to LES-diagnosed ground-truth (black). c) Mesoscale heat flux anomaly  $F'_{\theta_{lvm}}$  (maroon, using eq. 13) and its liquid water flux approximation (blue, using eq. 20). d) As in central panel, but coloured by relative humidity and overlaid by contours of  $7\overline{\theta_l} (w'q'_l)_m$ .

This term expresses transport along the mean, negative moisture gradient with mesoscale vertical velocity anomalies  $w'_m$ , which in fig. 1 a) grow increasingly positive (negative) in the moist (dry), cloud layer.  $w'_m$  embodies the ascending and descending branches of a shallow circulation (drawn as in-plane streamlines in the central panel of fig. 1), which converges in the moist regions' subcloud layer, transports mixed-layer moisture into the corresponding, moist cloud layer, and diverges near the trade-inversion base into dry regions, where it subsides.

The shallow circulations  $(w'_m)$  may be understood as a direct result from heat flux differences between moist and dry mesoscale regions. To show this, consider fig. 1 b). It plots  $w'_m$ , averaged over the moist, mesoscale region as i) diagnosed by the LES model, and ii) as predicted by reducing eq. 12 for  $\theta_{lv}$  to a diagnostic relation:

$$\frac{\partial \theta_{lv_m}'}{\partial t} \approx -w'_m \Gamma_{\theta_{lv}} - \frac{1}{\rho_0} \frac{\partial}{\partial z} \left( \rho_0 F'_{\theta_{lv_m}} \right) \approx 0 \tag{16}$$

$$w'_m \approx -\frac{1}{\rho_0} \frac{\partial}{\partial z} \left( \rho_0 F'_{\theta_{lvm}} \right) / \Gamma_{\theta_{lv}}. \tag{17}$$

Eq. 17 essentially amounts to posing the Weak Temperature Gradient (WTG) as-255 sumption (e.g. Held & Hoskins, 1985; Sobel et al., 2001), as often successfully employed 256 in models of self-aggregating deep convection (e.g. Emanuel et al., 2014; Chikira, 2014; 257 Beucler et al., 2018; Ahmed & Neelin, 2019). Fig. 1 b) justifies making this assumption 258 for our shallow convective self-aggregation too. Combining eqs. 15 and 17, integrating 259 by parts and ignoring surface flux feedbacks (which are zero by definition in our config-260 uration with homogeneous surface fluxes) then yields a model for  $\langle q'_{tm} \rangle$  which finds its 261 energetic support solely in the heat flux anomaly  $F'_{\theta_{lvm}}$ , appropriately scaled by the ver-262 tical structure of the slab-averaged, thermodynamic state: 263

$$\frac{\partial \langle q'_{t_m} \rangle}{\partial t} \approx - \left\langle F'_{\theta_{lv_m}} \frac{\partial}{\partial z} \left( \frac{\Gamma_{q_t}}{\Gamma_{\theta_{lv}}} \right) \right\rangle \tag{18}$$

To discover why  $F'_{\theta_{lvm}}$  develops, let us multiply eq. 14 by w', which decomposes the heat fluxes into flux measures of buoyancy and liquid water:

$$w'\theta'_{lv} \equiv w'\theta'_v - 7\overline{\theta_l}w'q'_l. \tag{19}$$

Fig. 1 c) attributes the primary contribution in this decomposition to liquid water flux anomalies, i.e.

$$F'_{\theta_{lvm}} \approx -7\overline{\theta_l}F'_{q_{lm}}.$$
(20)

In turn, the divergence of  $F'_{q_{l_m}}$  stems directly from mesoscale anomalies in the condensation  $\mathcal{C}'_m$ . Put differently, latent heating in clouds underpins the mesoscale circulation.

Finally, as indicated in fig. 1 d), convective plumes rising into a cloud layer that is moister than the slab mean will condense and later reevaporate more water vapour than average, closing a feedback loop in  $q'_{t_m}$ . We express this feedback mathematically by assuming  $F'_{q_{l_m}}$  can be written in terms of  $q'_{t_m}$  through a poor-man's mass flux approximation:

$$F'_{q_{l_m}} \approx C' w^* q'_{l_m} \approx C w^* q'_{t_m} \tag{21}$$

In combination, eqs. 18, 20 and 21 give a linear instability model for the moistureconvection feedback with time scale  $\tau_{q'_{tm}}$ :

$$\frac{\partial \langle q'_{t_m} \rangle}{\partial t} \approx \frac{\langle q_{t'_m} \rangle}{\tau_{q'_{t_m}}},\tag{22}$$

$$\tau_{q'_{t_m}} = \frac{1}{C\overline{\theta}_l w^* \frac{\partial}{\partial z} \left(\frac{\Gamma_{q_t}}{\Gamma_{\theta_{l_m}}}\right)}.$$
(23)

This minimal model is rather accurate for describing the evolution of  $\langle q'_{t_m} \rangle$  in simulation D1 (Janssens et al., 2022), and suffices to illustrate how the mechanism is sensitive to discretisation and modelling error.

#### <sup>281</sup> 4 Dependence on sub-mesoscale dynamics

If all assumptions made in deriving eq. 23 hold, it relies on only two variables: A convective velocity scale  $w^*$  and the gradient of the ratio of slab averaged lapse rates of heat and moisture, i.e. the vertical structure of the mean environment. Janssens et al. (2022) show that the development of  $\partial/\partial z (\Gamma_{q_t}/\Gamma_{\theta_{lv}})$  relies only on slab-averaged heat and moisture fluxes; so does  $w^* \langle q'_{t_m} \rangle$  through eqs. 20 and 21. Therefore, we pause for a moment to analyse which scales of motion control these fluxes.

Eq. 20 argues that  $F'_{\theta_{lvm}}$  is facilitated by cumulus clouds, whose energetic scales follow the depth of the boundary layer, of O(1000) m. Hence, the fluctuations in vertical velocity, heat and liquid water that construct  $F_{q'_{lm}}$  and  $F_{\theta'_{lvm}}$  generally are of a scale much smaller than  $q'_{tm}$ , which by definition is larger than 12.5 km. It is therefore not trivial that  $F_{\theta'_{lvm}}$  should be controlled by  $q'_{tm}$  as directly as eqs. 20 and 21 suggest.

To illustrate this, consider fig. 2, which shows how the saturation excess  $q_t - q_s$ 293 varies over a vertical cross-section of our domain ( $q_s$  is the specific humidity at satura-294 tion). The white-to-blue contour lines identify a moist, mesoscale patch, with  $q'_{t_m}$  up to 295 0.003 kg/kg near the inversion base at 1500m, which coincides with a region of high  $q_t$ -296  $q_s$ , and upon which most of the clouds at these levels consequently form. However, the 297 structure of these clouds, indicated by black contour lines, still varies horizontally with 298 small fluctuations in  $q_t - q_s$ , on a scale commensurate with the cumulus convection it-299 self. As a result,  $F_{q'_l}$ ,  $F_{\theta'_{lv}}$  and their mesoscale-filtered counterparts  $F_{q'_{lm}}$  and  $F_{\theta'_{lvm}}$ , plotted over the dashed line at 1500m in the top panel, also remain dominated by sub-mesoscale 301 variation in heat, moisture and vertical velocity. Hence, one might view the mesoscale 302 moisture fluctuations as preconditioners that raise the relative humidity over large re-303 gions of the local cumulus layer, while the resulting condensation and diabatic heating 304 in that layer remains governed by sub-mesoscale, cloudy updrafts that carry sub-mesoscale 305 fluctuations of water vapour  $(q'_{t_0})$  into it. 306

As a result, almost the entire basis of our mesoscale circulation is found in projections of *sub*-mesoscale scalar fluxes onto the mesoscale. More formally, for  $\chi' \in \{q'_t, \theta'_{lv}, q'_l\}$ , one can scale-decompose a mesoscale-filtered vertical scalar flux as

$$(w'\chi')_m = (w'_m\chi'_m)_m + (w'_m\chi'_s)_m + (w'_s\chi'_m)_m + (w'_s\chi'_s)_m$$
(24)

and write the approximation

$$(w'\chi')_m \approx (w'_s\chi'_s)_m \tag{25}$$



Figure 2. Bottom: Cross-section over the same x-z plane as the extraction plotted in the central panel of fig. 1, coloured by filled contours of relative humidity (yellow to blue) and overlaid by contour lines of i)  $q'_{t_m}$  (blue to white lines) and ii) clouds (black lines). Top: Spatial variation of  $F_{\theta'_{lv}}$ , its mesoscale-filtered counterpart  $F_{\theta'_{lvm}}$ , and their respective liquid-water contributions  $-7\overline{\theta_l}F_{q'_l}$  and  $-7\overline{\theta_l}F_{q'_{lm}}$ , over the dashed line at inversion base.



Figure 3. Grid-resolved  $(w'\chi')_m$ , for  $\chi \in \{\theta_{lv}, q_l\}$ ,  $(q_l$  fluxes are scaled by  $-7\overline{\theta_l})$ , scale-decomposed into pure mesoscale contributions  $(w'_m\chi'_m)_m$ , cross-scale contributions  $(w'_m\chi'_s)_m + (w'_s\chi'_m)_m$  and pure sub-mesoscale contributions  $(w'_s\chi'_s)_m$ , averaged over 14-16 hours in simulation D1, in moist (left) and dry (right) regions.

to very good accuracy, as shown for both  $(w'\theta'_{lv})_m$  and  $(w'q'_l)_m$  in fig. 3. Hence, for eq. 23 to successfully explain the evolution of mesoscale moisture anomalies, it is crucial to get the sub-mesoscale fluctuations of w,  $\theta_{lv}$  and  $q_l$  that form them right.

### <sup>314</sup> 5 Sensitivity to resolution

At  $\Delta x = 200$  m, our coarsest simulations barely resolve the energy containing scales of the shallow convection. While the impact of such assumptions may be limited in short simulations on small domains (Siebesma et al., 2003; Blossey et al., 2013), one might imagine simulations of mesoscale structures on large domains, at coarse resolutions and over long integration times to be more sensitive.

Fig. 4 presents the time evolution of vertically integrated mesoscale moisture fluctuations,  $\langle q'_{t_m} \rangle$  and the timescale  $\tau_{q'_{t_m}}$  estimated from eq. 22 for the numerical model configurations in tab. 1. It shows that repeated grid refinement in the horizontal dimension more than doubles  $\tau_{q'_{t_m}}$  in DALES, and quadruples it in MicroHH. The models do not



Figure 4. Time-evolution of  $\langle q'_{t_m} \rangle$ , averaged over moist (blue) and dry (red) mesoscale regions, for numerical configurations indicated by the line styles, in simulations run by DALES (dark colours) and MicroHH (light colours). Abbreviations "fiso", "a5" and "nocorr" follow the definitions from tab. 1.

agree even at  $\Delta x = 50$  m. Similar results are obtained for numerical setups that dissipate resolved fluctuations more strongly (simulations D2, D3 and D5). In fact, switching from a second-order advection scheme to a fifth-order scheme (simulations D2 vs. D1 and D5 vs. D4) slows the growth of  $\langle q'_{t_m} \rangle$  to the point that it is barely perceptible. In all numerical configurations, the scale growth mechanism eq. 18 holds almost exactly (see fig. S1). Hence, while the form of the circulation-driven mechanism is rather resolutioninvariant, its ingredients,  $w^*$  and  $\Gamma_{q_t}/\Gamma_{\theta_{tv}}$ , are not.

To investigate this in more detail, we will focus on how the DALES simulations run-331 ning at  $\Delta x = 200$  m (D1 and D3) and with fifth order advection (D5) and no stabil-332 ity correction (D6) differ from that running at  $\Delta x = 100$  m (D4). Since our length scale 333 growth model is state-dependent, such differences are best studied by tracing the tem-334 poral divergence between experiments that start from an identical state after the model 335 spinup. We choose that state to be simulation D4's solution after 12 hours, when mesoscale 336 fluctuations are small. For simulations D1 and D3, this solution is first coarse-grained 337 onto a grid with  $\Delta x = 200$  m using a top-hat filter. We then run the cases on for 12 338 hours with all other settings kept identical to simulations D1, D3, D5 and D6. 339

Fig. 5 shows how profiles of the ingredients to eq. 18 evolve in these simulations in the first six hours after they have been relaunched. Their  $q'_{t_m}$  fields are initially identical, as is  $\Gamma_{q_t}/\Gamma_{\theta_{lv}}$ . However, this state immediately elicits a response in the coarser simulations'  $F_{\theta'_{lvm}}$ . It increase in strength, amplifying  $w'_m\Gamma_{q_t}$ . As a result,  $q'_{t_m}$  begins growing more quickly in these simulations, supplying additional fuel that  $F_{\theta'_{lvm}}$  can feed on; the mechanism and divergence between the simulations intensifies over time.

It is worth noting that the main sinks in the  $q'_{t_m}$  and  $\theta'_{lv_m}$  budgets, the horizontal advection terms, barely respond to the changes in grid spacing (see fig. S1 and S2). The faster growth of  $q'_{t_m}$  in our coarse simulations is then not because mesoscale fluctuations are horizontally redistributed or dissipated down to the sub-mesoscale less efficiently, but due to an enhancement of  $F_{\theta'_{lv_m}}$ -driven production at a given  $q'_{t_m}$ . Put differently, it is the proportionality in eqs. 20 and 21 that is not grid-converged.

Why is the development of  $F_{\theta'_{lv_{pl}}}$  resolution-sensitive? The spectra plotted in fig. 6 offer a suggestion. In the first hour after the coarse-resolution simulation D1 has been



**Figure 5.** Vertical profiles of  $q'_{t_m}$ ,  $F_{\theta'_{l_{v_m}}}$ ,  $\Gamma_{q_t}/\Gamma_{\theta_{l_v}}$  and  $w'_m\Gamma_{q_t}$  (columns left to right), in moist and dry regions (blue and red lines), averaged over 2-hour intervals (top to bottom rows) after launching the cases D1, D3, D5 and D6 from the case D4 (different line styles).

relaunched from the finer-resolution simulation D4, it contains slightly less variance in its smallest scales of  $q_t$ , w and  $\theta_{lv}$  in the sub-cloud layer (figs. 6 a-c). But in the cloud layer, where our instability resides, fluctuations in  $q_t$ , w and  $\theta_{lv}$  are more energetic at their smallest, resolved scales (figs. 6 d-f) in simulation D1 than in D4. At the inversion base, where  $F_{\theta'_{lvm}}$  reaches its maximum, the small-scale fluctuations in the coarse simulation are more energetic still (figs. 6 g-i).

The excess variance in inversion-layer  $q_t$  is initially almost ephemeral: Fig. 6 g) shows 360 that the inversion-layer moisture field is dominated by its largest scales (wavenumbers 361 smaller than  $k_m$ ), which remain unaffected by the restart. In contrast, the variance in 362 both w and  $\theta_{lv}$  peaks at wavenumbers commensurate with the boundary layer height of 363 O(1000) m, and retains a non-negligible contribution from a long range of scales smaller 364 than that, especially in the cloud and inversion layers. In our coarse simulations, it is 365 the excess small-scale w' and  $\theta'_{lv}$  in these two layers that through eq. 25 provide the vari-366 ance that underpins the stronger  $F_{\theta'_{t_{n_m}}}$  and subsequent development of  $q'_{t_m}$ . 367

The spectral variance plateau at the smallest, resolved scales at z = 1500 m persists even when  $\Delta x = 100$  m, explaining why simulations D7 and M3 ( $\Delta x = 50$  m) self-aggregate over an even longer time scale than simulations D4 and M2 ( $\Delta x = 100$ m). In fact, the plateau even persists in the inversion layer at  $\Delta x = 50$  m (see fig. S3), raising questions as to whether the self-aggregation even in those simulations would be



**Figure 6.** Radial power spectral density of  $q_t (k \hat{q}_t^2)^2$ , a, d, g)  $\theta_{lv} (k \hat{\theta}_{lv}^2)^2$ , b, e, h) and  $w (k \hat{w'}^2)^2$ , c, f, i) for our 100m simulation (D4) and 200m simulation (D1) restarted from D4, averaged over the first hour after the restart, over x-y cross-sections at 250m (a-c, in middle of sub-cloud layer), 750m (d-f, in cloud layer) and 1500m (g-i, at inversion base).  $k_m$  indicates the wavenumber that separates the mesoscales from the sub-mesoscales, according to eq. 10.

grid-independent. Simulations with stronger diffusion (D3, D5 nad D6, see fig. S4) dampen the spectral plateau, and consequently reduce  $F_{\theta'_{lym}}$  compared to simulation D1 (see fig. 5).

So which, if any, of the results above can we trust? It is impossible to answer this 375 question completely in the absence of observations. However, we believe we may elim-376 inate some ambiguity by testing the degree to which the simulations hold up to the fun-377 damental LES assumption that our quantities of interest should be independent of SFS 378 effects. The SFS models employed in DALES and MicroHH assume these effects can rea-379 sonably be modelled by diffusion with diffusivity  $K_m \sim u'' l''$ , where u'' and l'' are typ-380 ical velocity and length scales of the unresolved motions in the flow. This approxima-381 tion can be rationalised if  $l'' \sim \Delta$  resides in the inertial subrange of homogeneous, isotropic 382 turbulence. In the inertial subrange, the mean rate of transfer of turbulent kinetic en-383 ergy e from any scale to a smaller one is scale-independent, and equal to the rate at which 384 it is eventually dissipated by molecular diffusion at much smaller scales,  $\varepsilon$  (e.g. Wyn-385 gaard, 2010). Therefore, we are satisfied with resolving the larger, energy-containing ed-386 dies, characterised by velocity and length scales U and L, respectively, inserting  $\Delta$  in the 387 inertial subrange, and employing a diffusive SFS model that we only ask to model  $\varepsilon$  cor-388 rectly. If it does, a necessary requirement is that  $\varepsilon$  is independent of  $\Delta$ , and thus of our 389 grid spacing (Sullivan & Patton, 2011). Fig. 7 shows that this is not the case; our coarse-390 mesh simulations underestimate  $\varepsilon$  with respect to our fine-mesh simulations throughout 391 the cloud layer, and this underdissipation accelerates the observed length scale growth 392 (fig. S5 paints the same picture for our MicroHH simulations). We are either making mis-393 takes within our model for  $\varepsilon$  at  $\Delta x \in [100, 200]$  m, or must concede that these grid spac-394 ings are simply too coarse to reside in the inertial subrange. 395



Figure 7. Profiles of dissipation  $\varepsilon$  of resolved turbulent kinetic energy e, averaged between 12-14 hr, for numerical configurations indicated by the line styles, in simulations run by DALES.

Several pieces of evidence assign a high likelihood to the second of these options 396 holding some truth. First, let us attempt to account for our anisotropic grid, which makes 397 us underestimate  $\Delta$  in the horizontal direction. It is in principle possible that the insuf-398 ficient dissipation we observe stems from our abuse of this length scale. However, set-399 ting  $\Delta = \Delta x$  according to Deardorff (1980)'s original proposition (simulation D3) still 400 underestimates the dissipation with respect to higher-resolution simulations, even though 401 it strongly overestimates the vertical component of this length scale relative to the ver-402 tical grid spacing. It is thus unlikely that our grid anisotropy alone is responsible for un-403 derestimating  $\varepsilon$ . Second, our empirical stability corrections might over-ambitiously di-404 minish the eddy diffusivities in stratified regions. This too could explain the excess small-405 scale variance, as it rises as the stratification increases through the cloud and inversion 406 layers. Yet, switching off the stability correction entirely (simulation D6) only slightly 407 reduces the small-scale variance, and does not measurably influence the evolution. There-408 fore, it is also unlikely that stability corrections are at the root of the problem. Third, 409 the underestimation of dissipation is consistent across two independent LES codes with 410 different thermodynamics and SFS models, and is thus unlikely related to individual model 411 details. Finally, we remark that our resolutions may simply be too low to allow a proper 412 turbulent flow to develop on the resolved scales. If we had such a flow, its large-eddy Reynolds 413 number  $\operatorname{Re}_L \gg 1$ . Following Wyngaard (1984), 414

$$\operatorname{Re}_{L} = \frac{UL}{K_{m}} \sim \frac{UL}{u''\Delta} \sim \frac{UL}{\varepsilon^{\frac{1}{3}}\Delta^{\frac{4}{3}}} \sim \left(\frac{L}{\Delta}\right)^{\frac{3}{3}},\tag{26}$$

if  $\varepsilon \sim U^3/L \sim u''^3/\Delta$ , which holds if  $\Delta$  resides in the inertial subrange (Tennekes & 415 Lumley, 1972). In our simulations,  $L \sim 1000$  m, and we attain Re<sub>L</sub>  $\sim 10$  for  $\Delta x \in$ 416 [100, 200] m; this number is even lower for simulations with the O(5) advection scheme, 417 whose effective resolution is approximately  $6\Delta x$  (Bryan et al., 2003). Simulations of or-418 ganised, deep convection indicate that  $\text{Re}_L \sim 10^2$  may be necessary for the flow to en-419 ter a regime where its statistics no longer scale with  $\operatorname{Re}_{L}$  (Bryan et al., 2003); the same 420 seems necessary for certain shallow cumulus cases (D. E. Stevens et al., 2002). Thus, grid 421 spacings at the lower end of what we test here, or even finer, may be required to sim-422 ulate organising shallow cumulus in LES, and any subsequent transition to deep, organ-423 ised convection, unless SFS models are employed that do not rely on  $\Delta$  residing in the 424 inertial subrange. 425

#### 426 6 Discussion

We find that the numerical representation of fluctuations in buoyancy and vertical velocity in shallow cumuli at scales smaller than 1 km have the potential to propagate into significant differences in the moisture field at scales up to the 100 km domain
 sizes simulated here. We draw attention to a few implications for the modelling of trop ical convection.

First, it is worthwhile to place these results in the context of early LES model in-432 tercomparisons. In the BOMEX intercomparison (Siebesma et al., 2003), small-domain 433 LES models agreed well with each other at the resolutions considered here. It proved much 434 harder to achieve similar agreement for shallow cumulus under strong inversions, such 435 as those that develop in conditions sampled during the Atlantic Tradewind Experiment 436 437 (ATEX) (B. Stevens et al., 2001). It is precisely in the inversion, where the energy-containing turbulent length scales shrink below the boundary layer's depth (e.g. Mellado et al., 2014, 438 2017), that we find both the key to circulation-driven self-aggregation, and our SFS mod-439 els lacking. Given the tight coupling between the fluxes that grow the cumulus layer (B. Stevens, 440 2007) and those that lead to its self-aggregation (Janssens et al., 2022), we wonder whether 441 our results simply give the historical context of the ATEX intercomparison a new per-442 spective: It is perhaps simply too ambitious to simulate large-scale cloud structures that 443 depend so strongly on inversion-layer dynamics at resolutions tractable for large-eddy 444 simulations. 445

In particular, our results suggest why the structures termed "flowers" by B. Stevens 446 et al. (2020) are inadequately captured in simulations of even coarser resolution than con-447 sidered here (Schulz, 2021): They may just run an overly dissipative combination of ad-448 vection scheme and unresolved scales model. The results also indicate that small-scales 449 driven development of mesoscale scalar variance poses a fitting and challenging test case 450 for the development of better parameterisations in the convective gray zone, such as those 451 discussed in (Honnert et al., 2020), and ultimately to the development of the next gen-452 eration of cumulus parameterisations in global models, which are unable to adequately 453 estimate the contribution from the trades towards the equilibrium climate sensitivity (Myers 454 et al., 2021; Cesana & Del Genio, 2021). At minimum, our results suggest that it is pru-455 dent for modelling studies of the spontaneous development of mesoscale shallow cloud 456 patterns to incorporate an assessment of their degree of grid convergence. Concretely, 457 we recommend to always assess the resolution sensitivity of one's quantities of interest, 458 e.g.  $\langle q'_{t_m} \rangle$ , and of our indicators of mesoscale variance production, e.g.  $F'_{\theta_{lv_m}}$  or  $\tau_{q'_{t_m}}$ . If 459 such sensitivities are found, inversion-layer w or heat spectra may offer insight into the 460 sensitivity's origins. 461

We pose our recommendations on the basis of simulations with minimal physics. 462 Therefore, it may not be immediately obvious why our results should be of interest to 463 situations where radiation, precipitation or strong boundary forcings prevail over the moist 464 convection. Yet, simulations of such situations often first appear to require non-precipitating 465 cumulus to aggregate sufficient amounts of moisture into moist mesoscale regions before 466 developing stratiform cloud layers and cold pools (Bretherton & Blossey, 2017; Naren-467 pitak et al., 2021), which may then modulate the mesoscale dynamics (Vogel et al., 2016; 468 Anurose et al., 2020). Additionally, the microphysical parameterisations upon which such 469 precipitation-driven mechanisms rely typically exhibit even larger model biases than the 470 turbulence-parameterisations discussed here (e.g. van Zanten et al., 2011). If such pa-471 rameterisations are not even driven by the right model dynamics, they can also not be 472 expected to return realistic precipitation and cold pools. Exactly how large error prop-473 agation from dynamics-to-physics modules is for self-organising cumulus convection re-474 mains largely unquantified; appraising and amending such estimates is therefore a worth-475 while topic of future research. 476

Finally, we return to the matter of self-aggregation in simulations of radiative-convective equilibrium discussed in the introduction. Our coarsest two simulations (D1 and M1) develop deep convective clouds on top of their mesoscale moist regions, displaying some form of radiation- and precipitation-less, deep convective self-aggregation. We do not argue that these clouds are physical. Yet, their development does open a potential path



Figure 8. Power-spectral densities of  $\langle q_t \rangle$  (a) and  $w_{500}$  (vertical velocity at 500 hPa, b) of five participating models in the RCE Model Intercomparison Project (RCEMIP), in the RCE-large configuration detailed by Wing et al. (2018), over a sea surface at 300K and averaged over the last 50 days of simulation. Simulations with more energetic small-scale vertical velocity fluctuations contain more variance in their largest scales of moisture.

between the convective feedback in the shallow convection discussed here and the shal-482 low circulations that underlie deep convective self-aggregation. Therefore, our results may 483 contribute to explain why numerical models set up on the same numerical domain, but 484 with different advection schemes and SFS models, self-aggregate so differently in RCE 485 (Wing et al., 2020). Running with grid spacings exceeding 1 km - i.e. a factor five greater 486 than the coarsest grids used here - these simulations may simply dissipate energy from 487 their oft-parameterised shallow convection at different rates and thus support highly vari-488 able circulation strengths and self-aggregation time scales (Shamekh et al., 2020). The 489 spectra of vertically integrated water vapour and vertical velocity of several simulations 490 that participate in Wing et al. (2020) bear these hallmarks (fig. 8). More study of choices 491 in discretisation and unresolved scales schemes, and the resulting interaction of numer-492 ical and modelling errors with the resolved dynamics in cloud-resolving models of RCE 493 is warranted. 494

### 495 7 Summary

In pursuit of understanding why and when idealised models of tropical convection 496 self-aggregate, we have studied the sensitivity to numerical settings of self-aggregating 497 shallow cumulus convection. In idealised large-eddy simulations with a homogeneous sur-498 face forcing and no radiation or precipitation models, spontaneous aggregation is facil-499 itated by a pure, convective instability: Small fluctuations in latent heating in shallow 500 cumulus clouds prompt mesoscale circulations which transport moisture from dry to moist 501 columns, resulting in aggregated patches of cumulus clouds which release more latent 502 heat and strengthen the circulations. 503

The instability represents a pathway for sub-mesoscale, turbulent fluxes of heat and moisture in kilometre-scale cumulus clouds to control the moisture variability at scales up to two orders of magnitude larger. Therefore, modellers must take great care when trying to represent the underlying, turbulent dynamics in LES or cloud-resolving models: We find that the time scale of the instability is highly sensitive to differences in grid spacing and advection scheme, over a range of rather conventional choices for LES mod-

elling of shallow cumulus (fig. 4); even at  $\Delta x = 50$  m grid spacings, we find two LES 510 codes with different SFS models to aggregate at rather different time scales. Given the 511 potential role played by shallow convection in developing and maintaining deep convec-512 tive self-aggregation, we wonder whether similar differences in how cloud-resolving mod-513 els represent the effects of shallow convection matter in explaining the abundance of ag-514 gregation varieties observed in simulations of deep convection in RCE. 515

Our results call for a thorough analysis of the degree to which models of shallow 516 convective self-aggregation match reality, a question which has remained elusive for stud-517 ies of their deep-convective counterparts (Muller et al., 2022). A good start in this di-518 rection is offered by simulations of the EUREC<sup>4</sup>A field campaign (Narenpitak et al., 2021; 519 Saffin et al., 2022), which exhibit circulation-driven moisture aggregation in more real-520 istic settings, and which compare favourably to the campaign's observations. In fact, these 521 observations include sufficiently detailed observations of mesoscale circulations (George 522 et al., 2021) that the data required to reconcile models and nature may be in hand, bod-523 ing well for our understanding of self-aggregating convection. 524

#### 8 Open Research 525

Frozen images of the versions of DALES and MicroHH used in this study have been 526 stored at https://doi.org/10.5281/zenodo.6545655 and https://doi.org/10.5281/ 527 zenodo.822842 respectively. The numerical settings, routines and post-processed sim-528 ulation data used to generate the figures presented in the manuscript are available at https:// 529 doi.org/10.5281/zenodo.6772483. Living repositories for DALES, MicroHH and the 530 postprocessing scripts are available at https://github.com/dalesteam/dales, https:// 531 github.com/microhh/microhh and https://github.com/martinjanssens/ppagg, re-532 spectively. Both DALES and MicroHH are released under the GNU General Public Li-533 cense v3.0. The standardized RCEMIP data is hosted by the German Climate Comput-534 ing Center (DKRZ) and is publicly available at https://www.wdc-climate.de/ui/info 535 ?site=RCEMIP\_DS. 536

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Figure 1.



Figure 2.



Figure 3.



Figure 4.



Figure 5.



Figure 6.



Figure 7.





Figure 8.



# Supporting Information for "The time scale of shallow convective self-aggregation in large-eddy simulations is sensitive to numerics"

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## Contents of this file

1. Figures S1 to S5

# Introduction

In this supplement, we present five figures that support the section "sensitivity to resolution" in the main text. Figs. S1 and S2 show how the three most important terms in the budgets for mesoscale fluctuaions of liquid-water virtual potential temperature  $(\theta'_{lv_m})$  and total water specific humidity  $(q'_{t_m})$  are affected by changing the numerical resolution of our simulations. Figs. S3 and S4 display power spectral densities of the three most important variables underlying our simulations' self-aggregation in different numerical configurations run by MicroHH and DALES, respectively. Finally, fig. S5 indicates how dissipation of resolved turbulent kinetic energy is affected by resolution in MicroHH.

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Figure S1. Vertical profiles of gradient production (left), vertical transport (centre) and horizontal transport (right) of  $\theta'_{lv_m}$  evolving in time (rows) after simulations D1, D3, D5 and D6 have been launched from simulation D4 at t = 12 hr. The gradient production of  $\theta'_{lv_m}$  is almost exactly balanced (up to ensemble averaging deficiencies) by its vertical flux divergence, while horizontal transport remains negligible. Put differently, the weak temperature gradient assumption holds well for all simulations. The upshot is that the numerical sensitivity in gradient production of  $q'_{t_m}$ , plotted in fig. S2 and discussed in the main test, can be traced to the increased vigour of the heat flux divergence in coarser simulations, plotted here.



Figure S2. Vertical profiles of gradient production (left), vertical transport (centre) and horizontal transport (right) of  $q'_{t_m}$  evolving in time (rows) after simulations D1, D3, D5 and D6 have been launched from simulation D4 at t = 12 hr. Both the gradient production (which comes about through heat flux divergence, see fig. S1) and the vertical flux divergence intensify in coarser simulations, with exception of D5, which runs with a diffusive advection scheme that slows the growth. Horizontal moisture advection is small and unaffected by resolution change, i.e. quicker  $q'_{t_m}$  growth in coarser simulations is not because they mix moisture variance horizontally and to smaller scales less efficiently, but because they produce it more efficiently.



Figure S3. Radial power spectral density of  $q_t (k \hat{q}_t^2, a, d, g) \theta_{lv} (k \hat{\theta}_{lv}^2, b, e, h)$  and  $w (k \hat{w'}^2, c, f, i)$  for simulations M1-M3, i.e. at increasingly fine grid spacing, over x-y cross-sections at 250m (a-c, in middle of sub-cloud layer), 750m (d-f, in cloud layer) and 1500m (g-i, at inversion base).  $k_m$  indicates the wavenumber that separates the mesoscales from the sub-mesoscales. The spectra are plotted after 12 hours of simulation without restart, i.e. these spectra subsume historical information of their self-generated state, such that the excess variance predicted for the coarsest simulation (M1) is in part due to its advanced, self-reinforcing scale growth. Note, however, the same spectral variance plateaus at all three simulations' smallest, resolved scales at their inversion base, though it shifts to increasingly small, quiescent and thus inconsequential scales.



Figure S4. As fig. S3, for the three DALES simulations D1, D3 and D5 restarted from simulation D4, averaged over the first hour after the restart. The more diffusive simulations (D3 and D5) possess a reduced variance plateau at their smallest, resolved scales with respect to D1, slowing their self-aggregation. Simulation D5 appears to compensate for a lack of variability in its smallest scales - at  $\Delta x = 100$ m any variance < 500 m is controlled by free parameters of the numerical scheme (Bryan et al., 2003) - by shifting variance to larger scales, perhaps following the mechanism suggested by de Roode et al. (2022). Note that its overall variance in the submesoscales remains smaller than that of its 2nd order advective counterpart D4, especially in the cloud layer.)



Figure S5. Profiles of dissipation  $\varepsilon$  of resolved turbulent kinetic energy e, averaged between 3-5 hr, for numerical configurations indicated by the line styles, in simulations run by MicroHH, i.e. before any of the simulations have self-aggregated appreciably.  $\varepsilon$  is much smaller in simulation M1 than in M2 and M3, consistent with this simulation being underdissipated and self-aggregating much more rapidly than its finer counterparts. Encouragingly, M2 and M3 differ less, though M2 remains underdissipated, especially at inversion base where scale growth is maximised.