

Dual State-Parameter Assimilation of SAR-derived Wet Surface Ratio for Improving Fluvial Flood Reanalysis

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November 21, 2022

Abstract

Flooding is one of the most devastating natural hazards to which our society worldwide must adapt, especially as its severity and occurrence tend to increase with climate changes. This research work focuses on the assimilation of 2D flood observations derived from remote-sensing images acquired during overflowing events. To do so, the resulting binary wet/dry maps are expressed in terms of wet surface ratios (WSR) over a number of floodplain subdomains. This ratio is assimilated jointly with in-situ water-level gauge observations to improve the flow dynamics within the floodplain. An Ensemble Kalman Filter with a dual state-parameter analysis approach is implemented on top of a TELEMAC-2D hydrodynamic model. The EnKF control vector is composed of spatially-distributed friction coefficients and a corrective parameter of the inflow discharge. It is extended with the hydraulic states within the floodplain subdomains. This data assimilation strategy was validated and evaluated over a reach of the Garonne river. The observation operator associated with the WSR observations, as well as the dual state-parameter sequential correction, was first validated in the context of Observing System Simulation Experiments. It was then applied to two real flood events that occurred in 2019 and 2021. The merits of assimilating SAR-derived WSR observations, in complement to the in-situ water-level observations, are shown in the parameter and observation spaces with assessment metrics computed over the entire flood events. It is also shown that the hydraulic state correction within the dual state-parameter analysis approach significantly improves the flood dynamics, especially during the flood recession.

1 **Dual State-Parameter Assimilation of SAR-derived**
2 **Wet Surface Ratio for Improving Fluvial Flood**
3 **Reanalysis**

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9 **Key Points:**

- 10 • An Ensemble Kalman Filter data assimilation designated to flood fluvial re-analysis,
11 built on top of a hydrodynamic TELEMAC-2D model;
- 12 • Advanced data assimilation approaches combining in-situ and SAR-derived WSR
13 observations are proposed and comprehensively evaluated;
- 14 • Dual state-parameter analysis treating model parameters and hydraulic states in
15 floodplain zones provides more accurate flood simulations.

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Abstract

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Flooding is one of the most devastating natural hazards to which our society world-wide must adapt, especially as its severity and occurrence tend to increase with climate changes. This research work focuses on the assimilation of 2D flood observations derived from remote-sensing images acquired during overflowing events. To do so, the resulting binary wet/dry maps are expressed in terms of wet surface ratios (WSR) over a number of floodplain subdomains. This ratio is assimilated jointly with in-situ water-level gauge observations to improve the flow dynamics within the floodplain. An Ensemble Kalman Filter with a dual state-parameter analysis approach is implemented on top of a TELEMAC-2D hydrodynamic model. The EnKF control vector is composed of spatially-distributed friction coefficients and a corrective parameter of the inflow discharge. It is extended with the hydraulic states within the floodplain subdomains. This data assimilation strategy was validated and evaluated over a reach of the Garonne river. The observation operator associated with the WSR observations, as well as the dual state-parameter sequential correction, was first validated in the context of Observing System Simulation Experiments. It was then applied to two real flood events that occurred in 2019 and 2021. The merits of assimilating SAR-derived WSR observations, in complement to the in-situ water-level observations, are shown in the parameter and observation spaces with assessment metrics computed over the entire flood events. It is also shown that the hydraulic state correction within the dual state-parameter analysis approach significantly improves the flood dynamics, especially during the flood recession.

1 Introduction**1.1 Flood monitoring and forecasting**

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Flooding is one of the most common, yet most severe and costliest natural disasters worldwide. According to figures provided by the United Nations Office for Disaster Risk Reduction, flooding accounted for 43.4% of all 7,255 disaster events recorded globally between 1998 and 2017¹. Flood forecasting systems rely on both monitoring and numerical modelling. Most modelling systems concatenate hydrologic rainfall-runoff models that represent the dynamics of the catchment with hydrodynamic models that simulate the dynamics of the river bed and the floodplain. River hydrodynamic models rely on solving the Shallow Water equations (SWE) which are depth-averaged Navier-Stokes equations. They are used to predict river water surface elevation (WSE) and discharge, thus allowing for flood risk assessment. However, these numerical models remain imperfect due to the uncertainties in the model itself and its inputs, e.g., friction and boundary conditions (BC), which translate into uncertainties in the model outputs, i.e. water level and discharge. A well-established method for reducing such uncertainties is to periodically adjust these models by assimilating various available observations. As a result, flood simulation and forecast capability have greatly improved thanks to the advances in data assimilation (DA) (Madsen & Skotner, 2005; Neal & Jeffrey, 2007; Neal et al., 2009). Continuous time-series of gauged water levels and/or discharges recorded at sparse locations have been used for model calibration and validation. DA strategies, namely EnKF, classically consist in combining these time-series measurements with numerical models to correct the hydraulic states and reduce the uncertainties in the model parameters, e.g., friction coefficients, upstream inflow (Neal & Jeffrey, 2007). EnKF relies on the stochastic computation of the forecast error covariance matrix amongst a limited number of perturbed simulations. Therefore, this approach depends strongly on the characteristics of the observing network, i.e., the density, the frequency and the statistics of errors of the observation (Mirouze et al., 2019). However, due to installation and

¹ <https://www.prevention-web.net/knowledgebase>

64 maintenance costs, limnometric in-situ gauge stations providing water levels are only avail-
65 able at a few locations within a catchment (Mason et al., 2012), and they are usually in-
66 stalled by the river. Such a spatial scarcity is a limitation for numerical model precision
67 in simulation and forecast, especially in the floodplain. This can be overcome by the use
68 of other data sources such as remote sensing (RS) flood maps that, despite low revisit
69 frequency, offer a 2D representation of the flow dynamics.

70 1.2 Assimilation of remote sensing flood-related data

71 Leveraging RS products in the context of flood risk management presents a great
72 opportunity to improve the ability of flood monitoring and forecasting (G. Schumann
73 et al., 2009). In the recent years, SAR systems have played a major role in operational
74 flood management, due to its reliability to collect day-and-night observations regardless
75 of weather conditions. Water bodies and flooded areas typically exhibit low backscat-
76 ter on SAR images since most of the incident radar pulses are specularly reflected away
77 upon arrival at the water surfaces. Therefore, the detection of flooded areas is straight-
78 forward on SAR images, with several exceptions, e.g. in urban environment, vegetated
79 areas, or when facing variability of water roughness and speckle. Indeed, mis-detection
80 of flooded vegetation areas (i.e. partially submerged vegetation) mainly occurs because
81 signals cannot reach the water surfaces beneath vegetation being caught in volume scat-
82 tering from the canopy, or due to multiple-bounce effects between the tree trunks and
83 the underneath water surfaces. It could also occur in urban areas due the complexity of
84 the landscape geometry (e.g. shadow, layover, highly reflective scatterers). Over the last
85 decades, the literature on DA into hydrodynamic models mainly focused on the assim-
86 ilation of in-situ or RS-derived WSE observations (Hostache et al., 2010), mostly because
87 this is a state variable in any hydraulic model, thereby rendering the DA more straight-
88 forward. Such methods involve retrieving WSE from the combination of RS-derived flood
89 extent maps with topography data. Yet, this relies on the use of precise and high-resolution
90 Digital Terrain Models (DTM) and still requires some further research to prevent po-
91 tential bias from such a usage (Cian et al., 2018). As a result, recent studies have been
92 carried out to directly assimilate flood extent maps in hydraulic models. Flood proba-
93 bility maps have also been estimated by a Bayesian approach applied to SAR images,
94 and subsequently assimilated into a particle filter-based data assimilation framework (Hostache
95 et al., 2018; Dasgupta, Hostache, Ramsankaran, Schumann, et al., 2021; Revilla-Romero
96 et al., 2016; Di Mauro et al., 2021). Cooper et al. (Cooper et al., 2019) proposed a new
97 observation operator that directly uses backscatter values from SAR images as obser-
98 vations in order to bypass the flood edge identification or flood probability estimation
99 processes. However, this approach has only been implemented with synthetic SAR im-
100 ages in the scope of a twin experiment. It relies on the hypothesis that SAR images must
101 yield distinct distributions of wet and dry backscatter values, which may not hold for
102 real SAR data due to aforementioned limitations.

103 The increasing availability of highly spatially distributed RS observations of flood
104 extent and water levels offer new opportunities for investigation and analysis (e.g., (Bates,
105 2004; G. Schumann et al., 2009)). The possibility of using SAR imagery data for the val-
106 idation and calibration of two-dimensional (2D) hydraulic models was first highlighted
107 by Jung et al. (Jung et al., 2012). Since then, the increasing amount of RS data and the
108 advances in Machine Learning algorithms dedicated to water detection have enabled a
109 great number of research work dedicated to hydrologic and hydraulic models calibration/validation
110 for real-time forecasting. The combination of RS data with local hydrodynamic mod-
111 els has thus been greatly studied in the literature as it allows to overcome the limita-
112 tions of both incomplete and uncertain sources of knowledge on the river and floodplain
113 dynamics. A comprehensive review by Grimaldi et al. (Grimaldi et al., 2016) provides
114 an analysis on the use of coarse-, medium- and high-resolution RS observations of flood
115 extent and water level to improve the accuracy of hydraulic models for flood forecast-
116 ing. It points out that RS data should be used as a complement data source—but not

117 as an alternative—to the in-situ data in order to calibrate, validate, and constraint the
118 hydraulic models. This stems from their low precision and acquisition frequency (Grimaldi
119 et al., 2016). Indeed, compared to in-situ data, RS data provide useful flood extent and
120 flood edge information at a large coverage, usually covering the whole considered catchment,
121 but they are much sparser in terms of frequency. In addition, uncertainty exists
122 in flood extent mapping from RS observations, e.g. SAR images, which originates from
123 both the input images and the classification algorithm itself. As a matter of fact, clas-
124 sification overall accuracy of flooded areas varies considerably and only in rare cases ex-
125 ceeds 90% (G. J.-P. Schumann et al., 2012). An updated review from Dasgupta et al.
126 (Dasgupta, Hostache, Ramsankaran, Grimaldi, et al., 2021) provides the state-of-the-art
127 on the assimilation of Earth Observation data with hydraulic models for the purpose of
128 improved flood inundation forecasting.

129 **1.3 Objective and Outline**

130 As the severity and occurrence of flood events tend to intensify with climate change,
131 the need for flood forecasting capability increases. In this regard, the Flood Detection,
132 Alert and rapid Mapping (FloodDAM) project (Kettig et al., 2021), funded by the Space
133 for Climate Observatory initiative, was set out to develop pre-operational numerical tools
134 to enable quick responses in various flood-prone areas while improving the resolution,
135 reactivity, and predictive capability. In our previous works (Nguyen et al., 2021, 2022),
136 flood extent maps were inferred from Sentinel-1 (S1) images by a Random Forest (RF)
137 developed in the framework of the FloodML project (Huang et al., 2020; Kettig et al.,
138 2021). In these works, in-situ water level time series at observing stations of the river
139 bed were assimilated in order to sequentially correct friction and inflow discharge. Ac-
140 cordingly, the hydrodynamic model results in re-analysis and forecast modes are improved.
141 S1-derived flood extent were then used as independent validation observations provid-
142 ing valuable information, especially in the floodplain. The EnKF algorithm was favored
143 and implemented as it allows to stochastically estimate the covariance matrices between
144 the model inputs/parameters and its outputs, without formulating the tangent linear of
145 the hydrodynamics model, under the assumption that the errors in the control vector
146 are properly described by a Gaussian probability density function. Taking further ad-
147 vantage of S1-derived flood extents, the DA of flood extent maps, expressed in terms of
148 wet surface ratios (WSR) computed as the ratio of wet pixels detected on S1-derived wa-
149 ter masks, over the total number of pixels in a subdomain of the floodplain, is here in-
150 vestigated. This strategy aims at reducing comprehensively the uncertainties in the model
151 parameters and forcing, and consequently improve the overall flood re-analysis and fore-
152 cast capability especially in the floodplain. This article presents a DA approach to ac-
153 commodate 2D WSR observations alongside with in-situ water level time-series within
154 an EnKF framework implemented on a 2D hydrodynamics model on the Garonne river.
155 A dual state-parameter DA strategy is implemented to reduce the uncertainties in fric-
156 tion coefficients, upstream forcing and hydraulic state (water level in selected floodplain
157 subdomains). The control vector is augmented with a water level state correction that
158 is uniform over a limited number of subdomains in the floodplain. This work is first car-
159 ried out in the context of Observing System Simulation Experiment (OSSE) where ob-
160 servations are generated from a reference simulation with chosen settings, considered as
161 the truth. Generated in-situ and WSR synthetical observations are then assimilated into
162 an ensemble DA with a priori (background) settings that differ from the true settings.
163 This strategy is common in DA studies as it allows to validate a DA algorithm and whether
164 its analysis manages to bring the resulting control vector closer to the truth’s settings,
165 as well as the resulting model state closer to the synthetical observations than the a pri-
166 ori state. The DA strategy is then tested for real flood events, assimilating both water
167 level data measured at in-situ gauge stations and WSR observations derived from S1 im-
168 ages. The DA results are validated with respect to independent data from Sentinel-2 (S2)
169 optical images and high water marks (HWM) that are available and relevant. The lat-

170 ter is a collaborative dataset of high water marks² contributed by occasional observers
171 in the floodplain is used as independent data for validation purposes.

172 The remainder of the paper is organized as follows. Section 2 gathers the material
173 and data used in this study. Subsection 2.1 presents the hydrodynamic numerical solver
174 TELEMAC-2D³ (T2D). Its implementation on the Garonne Marmandaise catchment for
175 the representation of flooding along with the associated sources of uncertainties are de-
176 scribed in subsection 2.2. The reference flood events and the in-situ and remote sens-
177 ing data that are used for assimilation and validation purposes are then described in sub-
178 section 2.3. The EnKF algorithm for dual state-parameter correction is presented in sec-
179 tion 3. The description of the control vector, the forecast and analysis steps are proposed
180 in subsection 3.1, subsection 3.2 and subsection 3.3, respectively. Section 4 provides a
181 thorough description of the experimental settings and assessment metrics for the DA strat-
182 egy. The experimental settings for DA cycling and observation errors are gathered along
183 with the metrics that are used to assess the performance of the DA simulations with re-
184 spect to assimilated and independent data. Experimental results are presented in Sec-
185 tion 5, first in the framework of OSSE (subsection 5.1), then for real events (subsection
186 5.2). The merits of assimilating RS data for simulation evaluation in the river bed and
187 the floodplain are highlighted in the control and the observation space for OSSE and real
188 experiments, especially at the flood peak and during the flood recess. Conclusions, lim-
189 itations, and perspectives are given in Section 6.

190 2 Methodology

191 2.1 Hydrodynamic model

The non-conservative form of the SWE are written in terms of water level (denoted
by H [m]) and horizontal components of velocity (denoted by u and v [$\text{m}\cdot\text{s}^{-1}$]). They ex-
press mass and momentum conservation averaged in the vertical dimension, assuming
that (i) vertical pressure gradients are hydrostatic, (ii) horizontal pressure gradients are
due to displacement of the free surface, and that (iii) horizontal length scale is signif-
icantly greater than the vertical scale. The SWE read:

$$\frac{\partial H}{\partial t} + \frac{\partial}{\partial x} (Hu) + \frac{\partial}{\partial y} (Hv) = 0 \quad (1)$$

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -g \frac{\partial Z}{\partial x} + F_x + \frac{1}{H} \text{div} \left(H \nu_e \overrightarrow{\text{grad}}(u) \right) \quad (2)$$

$$\frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = -g \frac{\partial Z}{\partial y} + F_y + \frac{1}{H} \text{div} \left(H \nu_e \overrightarrow{\text{grad}}(v) \right) \quad (3)$$

192 where Z [m NGF69] is the water surface elevation and ν_e [$\text{m}^2\cdot\text{s}^{-1}$] is the water diffusion
193 coefficient. The water level $H = Z - Z_b$ is computed from Z with Z_b [m NGF69] the
194 bottom elevation. In the following, the water surface elevation is shortened as WSE and
195 the water level as WL. t stands for time and g is the gravitational acceleration constant.
196 div and $\overrightarrow{\text{grad}}$ are respectively the divergence and gradient operators.

In addition, F_x and F_y [$\text{m}\cdot\text{s}^{-2}$] are the horizontal components of external forces (fric-
tion, wind and atmospheric forces), defined as follows:

$$F_x = -\frac{g}{K_s^2} \frac{u\sqrt{u^2+v^2}}{H^{4/3}} - \frac{1}{\rho_w} \frac{\partial P_{atm}}{\partial x} + \frac{1}{H} \frac{\rho_{air}}{\rho_w} C_d U_{w,x} \sqrt{U_{w,x}^2 + U_{w,y}^2} \quad (4)$$

$$F_y = -\frac{g}{K_s^2} \frac{v\sqrt{u^2+v^2}}{H^{4/3}} - \frac{1}{\rho_w} \frac{\partial P_{atm}}{\partial y} + \frac{1}{H} \frac{\rho_{air}}{\rho_w} C_d U_{w,y} \sqrt{U_{w,x}^2 + U_{w,y}^2} \quad (5)$$

² <https://www.reperesdecrues.developpement-durable.gouv.fr/>

³ www.opentelemac.org

197 where ρ_w/ρ_{air} [$\text{kg}\cdot\text{m}^{-3}$] is the water/air density ratio, P_{atm} [Pa] is the atmospheric
 198 pressure, $U_{w,x}$ and $U_{w,y}$ [$\text{m}\cdot\text{s}^{-1}$] are the horizontal wind velocity components, C_d [-] is the
 199 wind drag coefficient that relates the free surface wind to the shear stress, and lastly, K_s
 200 [$\text{m}^{1/3}\cdot\text{s}^{-1}$] is the river bed and floodplain friction coefficient, using the Strickler formu-
 201 lation (Gaukler, 1867).

202 In order to solve Eq. (1)-(3), initial conditions $\{H(x, y, t = 0) = H_0(x, y); u(x, y, t =$
 203 $0) = u_0(x, y); v(x, y, t = 0) = v_0(x, y)\}$ are provided, and boundary conditions (BC)
 204 are described with a time-varying hydrogram upstream and a rating curve downstream.
 205 The Strickler coefficient is prescribed uniformly over defined subdomains, and calibrated
 206 according to the observing network. The hydrodynamic numerical model T2D is used
 207 to simulate and predict WSE and velocity from which the flood risk can be assessed. T2D
 208 solves the SWE derived from Navier-Stokes equations with an explicit first-order time
 209 integration scheme, a finite-element scheme and an iterative conjugate gradient method
 210 (Hervouet, 2007). The results are obtained at each point of the mesh mapped onto the
 211 catchment topography.

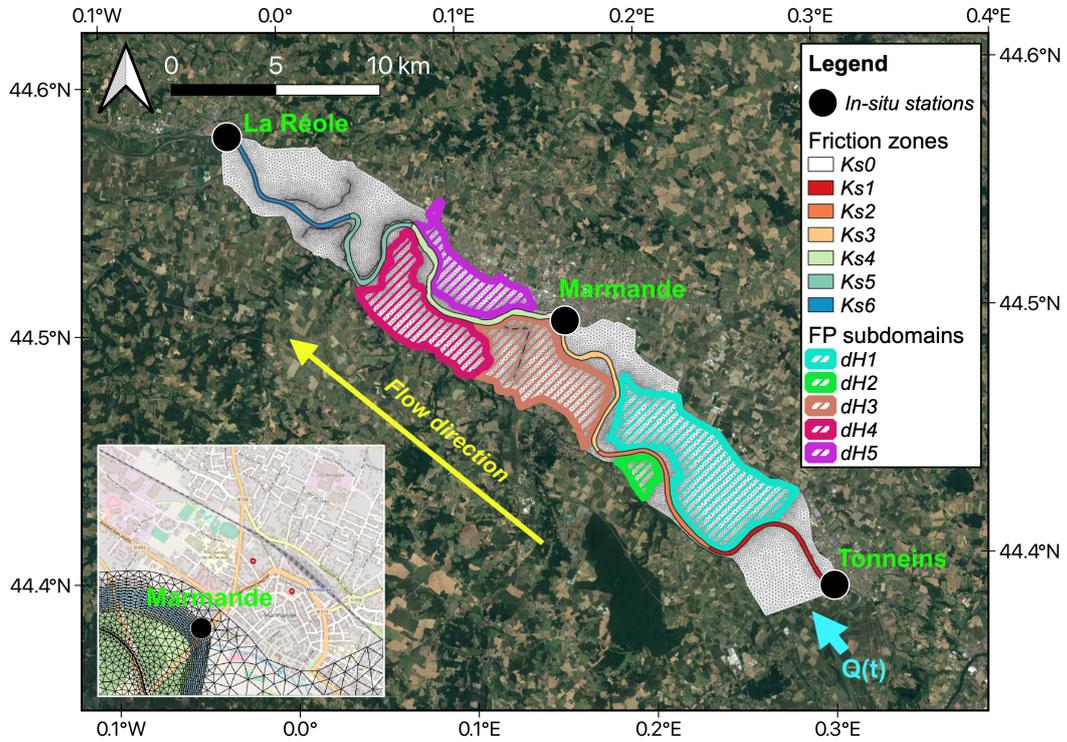


Figure 1: T2D Garonne Marmandaise domain. The VigiCrue observing stations are indicated as black circles. The different river friction zones are indicated as colored segments of the river bed. The floodplain is divided into five subdomains that are hatched in different colors. The inset figure at the bottom left corner magnifies the urban area of Marmande nearby its namesake gauging station.

2.2 Study area and description of the uncertainties

213 The study area is the Garonne Marmandaise catchment (southwest of France) which
 214 extends over a 50-km reach of the Garonne River between Tonneins and La Réole (Fig-
 215 ure 1). Since the 19th century, it has been equipped with infrastructures. As such, a sys-
 216 tem of dykes and weirs had been progressively built to protect floodplains from flood-

217 ing events, such as the historic flood of 1875, and to manage submersion and flood re-
 218 tention areas. Observing stations operated by the VigiCrue network⁴ are located at Ton-
 219 neins, Marmande, and La Réole (indicated as black circles in Figure 1, providing water-
 220 level measurements every 15 minutes.

221 A T2D model was developed and calibrated over this catchment, which was built
 222 on a mesh of 41,000 nodes using bathymetric cross-sectional profiles and topographic data
 223 (Besnard & Goutal, 2011). The topography of the catchment was generated using IGN
 224 (French National Mapping Agency) maps as well as aerial photographs for photogram-
 225 metric reconstruction (Besnard & Goutal, 2011). A local rating curve at Tonneins is used
 226 to translate the observed WL into a discharge time-series. Discharge time-series $Q(t)$ are
 227 then applied as forcing over the whole upstream interface (cyan arrow in Figure 1), in-
 228 cluding both river bed and floodplain boundary cells. This modeling strategy was im-
 229 plemented to allow for a cold start of the model with any inflow value. However, it prompts
 230 an over-flooding of the upstream first meander, until the water returns to the river bed.
 231 The downstream BC at La Réole is described with a local rating curve. In the follow-
 232 ing, both upstream and downstream areas are excluded from the computation of assess-
 233 ment metrics to limit the impact of the choice of the BC strategy and topographic er-
 234 rors on the results. Over the simulation domain, the friction coefficient is defined over
 235 seven zones, including six segments from K_{s_1} to K_{s_6} for the river bed and one K_{s_0} for
 236 the entire floodplain, as illustrated in Figure 1 with solid colored segments of the river
 237 bed and white background color for the floodplain. A priori values for friction in the river
 238 bed are set from a calibration process using in-situ WL observations at Tonneins, Mar-
 239 mande and La Réole for selected set of past flood events, summarized by Table 1. The
 240 description of the friction coefficients is highly prone to uncertainties related to the zon-
 241 ing assumption, the calibration procedure, and the set of calibration events. In the fol-
 242 lowing, these coefficients are considered as random variables with a gaussian Probabil-
 243 ity Density Function (PDF) with mean \mathbf{x}_0 and standard deviation $\sigma_{\mathbf{x}}$ estimated from
 244 the calibration process (Table 1). The a priori values are further improved with the DA
 245 strategy. The uncertainty in the upstream BC is also taken into account. Indeed, the
 246 limited number of in-situ observations yields errors in the formulation of the rating curve
 247 that is used to translate the observed WL into discharge, especially for high flow. Thus,
 248 a multiplicative factor μ on the time-dependent discharge time-series is considered as a
 249 random variable with a gaussian PDF centered at 1. Lastly, in order to account for the
 250 evapotranspiration, ground infiltration and rainfall processes that are lacking in the T2D
 251 Garonne model, a state correction is implemented in the floodplain. The floodplain is
 252 divided in five subdomains based on the description of the storage areas (Besnard & Goutal,
 253 2011) and the dyke system of the catchment. A uniform WL correction δH_k with $k \in$
 254 $[1, 5]$ over each subdomain is added to the control vector. Each δH_k is considered as a
 255 random variable with a zero-mean Gaussian with a standard deviation set to 0.25 [m].
 256 The calibrated friction coefficient values, and the default values of 1 for μ and 0 for δH_k
 257 are used as setting for the free run experiment further denoted as FR.

258 2.3 Flood events and Observations

259 Two significant flood events having occurred in December 2019 and January-February
 260 2021 are studied in this research work. In-situ WL measured every 15 minutes at Ton-
 261 neins, Marmande and La Réole are shown in Figure 2a and Figure 2b, respectively. A
 262 simulation period of 25 days was selected around the flood peak for each event in order
 263 to properly capture the flood and the recess periods. All of the time-varying plots in this
 264 article are made in local time (UTC +01:00).

⁴ <https://www.vigicrues.gouv.fr/>

Table 1: Characteristics of the Gaussian PDF for friction coefficients, multiplicative coefficient for inflow and water level correction in the subdomain of the floodplain.

Variable	Unit	Calibrated/ default values \mathbf{x}_0	Standard deviation $\sigma_{\mathbf{x}}$	95% confidence interval
K_{s_0}	$\text{m}^{1/3} \cdot \text{s}^{-1}$	17	0.85	17 ± 1.67
K_{s_1}	$\text{m}^{1/3} \cdot \text{s}^{-1}$	45	2.25	45 ± 4.41
K_{s_2}, K_{s_3}	$\text{m}^{1/3} \cdot \text{s}^{-1}$	38	1.9	38 ± 3.72
$K_{s_4}, K_{s_5}, K_{s_6}$	$\text{m}^{1/3} \cdot \text{s}^{-1}$	40	2.0	40 ± 3.92
μ	-	1	0.06	1 ± 0.0136
δH_k ($k \in [1, 5]$)	m	0	0.25	0 ± 0.0566

Table 2: General information on the studied flood events.

Event	First date	Last date	Nb of S1 images	Nb of usable S2 images	Nb of HWM
2019	2019-12-08	2020-01-02	11	2	120
2021	2021-01-16	2021-02-10	12	0	178

265 Sentinel-1 (S1) is the first satellite series of the Copernicus program (Torres et al.,
266 2012). This SAR system works at C-band, with a central frequency of 5.405 GHz. The
267 Interferometric Wide (IW) mode with 250-km-wide swath used in this study offers a ground
268 resolution of approximately 20×22 m; this product is then resampled, reprojected and
269 distributed at 10×10 m for the Ground Range Detected (GRD) products. In order to
270 improve the revisit time, Sentinel-1 works as a constellation of two polar-orbiting iden-
271 tical satellites Sentinel-1A launched on 2014-04-03 and Sentinel-1B on 2016-04-26, al-
272 lowing a six-day revisit time. The S1 GRD IW products are leveraged as the predom-
273 inant data source to produce binary water maps using Machine Learning algorithms de-
274 veloped by CNES and CLS in the framework of the FloodML project (Huang et al., 2020;
275 Kettig et al., 2021). The specifications of the flood extent mapping method applied to
276 S1 images are detailed in (Nguyen et al., 2022).

277 Similarly, Sentinel-2 (S2) mission comprises a constellation of two multispectral in-
278 strument satellites, Sentinel-2A launched on 2015-06-23 and Sentinel-2B on 2017-03-07.
279 They are placed in the same sun-synchronous orbit, phased at 180 degrees to each other.
280 They provide 290-km swath width and a high revisit time (10 days at the equator with
281 one satellite, and 5 days with 2 satellites under cloud-free conditions which might result
282 in 2-3 days revisit at mid-latitudes due to orbit overlapping). In order to perform the
283 flood extent mapping on S2 images, an extraction of features based on the Normalized
284 Difference Vegetation Index (NDVI) (Huang et al., 2021) and the Modified Normalized
285 Difference Water Index (MNDWI) (Xu, 2006) was carried out. They are then used as
286 the inputs for the implemented RF classifier (Kettig et al., 2021).

287 The double-peak flood event in 2019 was observed by eleven S1 SAR images, provid-
288 ed by the constellation of S1-A and S1-B ascending and descending orbits, and two
289 S2 images with acceptable cloud cover condition. The 2021 flood event is composed of
290 a single peak (but with a stronger flow than that of 2019) and was observed by 12 S1
291 images. The flood peak was reached on 2021-02-04 and it exceeded the highest thresh-
292 old level for flood risk at Marmande, set out by the French national flood forecasting cen-
293 ter (SCHAPI) in collaboration with the departmental prefect (see Figure 2b). It should

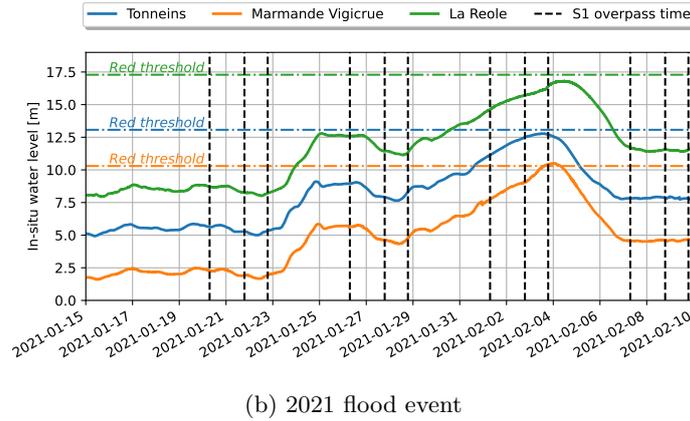
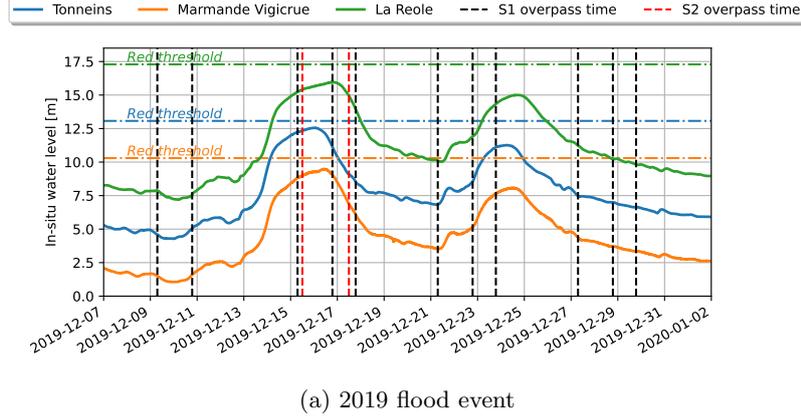


Figure 2: Water level H time-series for (a) 2019 flood event, and (b) 2021 flood event, at Tonneins (blue), Marmande (orange) and La Réole (green). S1 and S2 overpass times are indicated as vertical dashed lines, respectively in black and in red. The red thresholds for the WL associated with the highest level of flooding risk at each observing stations are shown as horizontal dash-dotted lines with the same color.

294 be noted that for the S1 images from the ascending orbit 132, a small part of the down-
 295 stream area (including La Réole) is a no-data area as it is out of range from the acqui-
 296 sition. As aforementioned, two S2 optical images are available for 2019 near the first flood
 297 peak at 2019-12-15 12:05 and 2019-12-17 11:54 thus providing independent data for valida-
 298 tion, with a cloud cover percentage of 40.58% and 11.28%, respectively. Due to high
 299 cloud cover, none of the S2 images acquired during the 2021 provides reliable observa-
 300 tions. The SAR S1 image acquired on 2021-02-02 18:55 and the derived flood extent map
 301 by FloodML for the same date are shown respectively in Figure 3a with grayscale (from
 302 dark to bright) indicating the backscatter values (from low to high), and in Figure 3b
 303 where wet pixels are indicated in white. The simulated flood extent for the free run (FR)
 304 introduced in Sect. 2.2 using the calibrated and default parameter values (Table 1) is shown
 305 in green in Figure 3b. The ratio between the number of wet pixels and the total num-
 306 ber of pixels, named WSR, is formulated for each of the five subdomains of the flood-
 307 plain indicated in hatched colored areas in Fig 1. WSR is further considered as the ob-
 308 servation for the DA strategy. In order to account for mis-detection of wet pixels in veg-
 309 etated regions, exclusion layers were identified from four land cover classes (deciduous
 310 and coniferous forests, orchards, and diffused built-up areas) of the IOTA2 land cover

311 map (Inglada et al., 2017) produced on the French territory. These highly vegetated areas shown in red in Figure 3b were excluded from the comparison between the model
 312 flood extent and the RS-derived observation, as well as from the WSR and further as-
 313 sessment computation. A zoomed-in view of Figure 3c over the zones 1, 2 and 3 of the
 314 floodplain is provided in Figure 3b with the same color code. Figure 3d complements the
 315 zoomed-in view with the effective areas (color-coded according to Figure 1) for the com-
 316 putation of WSR, taking into account the excluded pixels (in red). Lastly, as aforemen-
 317 tioned, there are 120 HWM observations available for the 2019 flood event whereas 178
 318 observations were collected in the aftermath of the 2021 event (as it was more severe).
 319

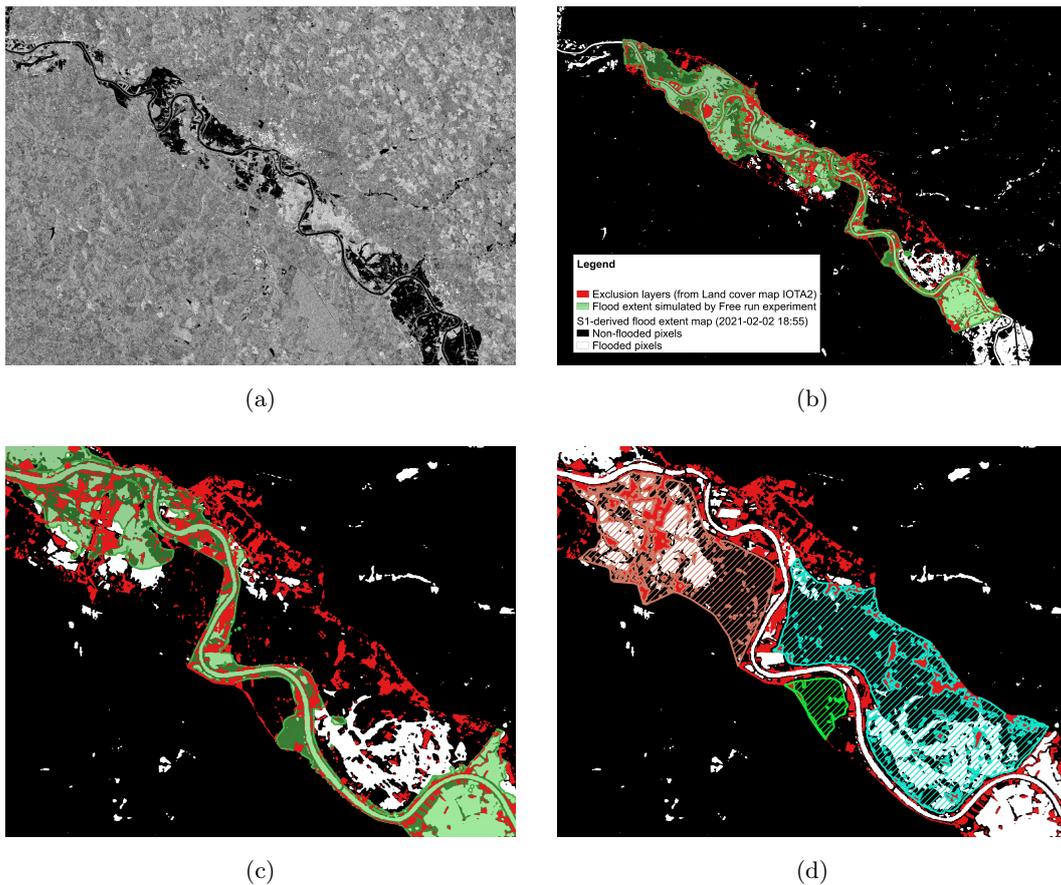


Figure 3: 2D flood extent observation derived from S1 data. (a) SAR S1 (VV polarization) image acquired on 2021-02-02 18:55:00, (b) the S1-derived flood extent binary map with red regions representing the areas to be excluded from the comparison between flood extents, green outline: the free run using calibrated and default parameter values, (c) zoomed-in view of sub-figure 3b and (d) zoomed-in view of the effective areas for the computation of WSR on the zones 1-3 taking into account exclusion layers, overlaid on the flood extent map.

3 Data Assimilation

3.1 Description of the control vector

The implemented DA algorithm consists in a cycled stochastic EnKF, where the control vector \mathbf{x} is composed of the seven friction coefficients K_{s_k} with $k \in [0, 6]$, one multiplicative parameter μ to modify the time-varying upstream BC $Q(t)$, and five state corrective variables δH_k with $k \in [1, 5]$ over the floodplain zones. Altogether these $n = 13$ parameters are assumed to be constant over a DA cycle, yet their evolution in time is made possible by DA between cycles. The DA cycle c covers a time window, denoted by $W_c = [t_{start}, t_{end}]$ of length $T = 18$ hours over which $n_{obs,c}$ observations are assimilated. The cycling of the DA algorithms consists in sliding the time window of a period $T_{shift} = 6$ hours so that the cycles c and $c + 1$ overlap over 12 hours.

It could be argued that the DA algorithm is more a smoother than a filter as it operates over a sliding time window. Yet, as the control vector is composed of model parameters and corrections that are assumed constant over the assimilation window (as opposed to the model state), the smoothing resumes to a filtering. The EnKF algorithm relies on the propagation of N_e members with perturbed values of \mathbf{x} , denoted by \mathbf{x}^i . The forecast values of \mathbf{x}^i are denoted by $\mathbf{x}_c^{f,i}$ (superscript index f stands for “forecast”), where $i \in [1, N_e]$ is the ensemble member counter.

3.2 Description of the EnKF forecast step

The EnKF forecast step consists in the propagation in time, over W_c , of the control and model state vectors. The EnKF is applied to model parameters that, by definition, do not evolve in time over the cycle c . The absence of propagation model for the control vector implies that the forecast for the control vector at cycle c should remain equal to its analysis at cycle $c - 1$. Yet, in order to avoid ensemble collapse, artificial dispersion is introduced with the addition of perturbations $\boldsymbol{\theta}$ to a global value $\mathbf{x}_{c-1}^{a,glo}$ issued from the previous cycle. For the friction coefficients K_{s_k} with $k \in [0, 6]$, and the forcing parameter μ , $\mathbf{x}_{c-1}^{a,glo}$ is chosen as the mean of the analysis from the previous cycle $\bar{\mathbf{x}}_{c-1}^a$ (superscript index a stands for “analysis” and $\bar{\bullet}$ stands for the average over the ensemble). For the floodplain state corrections δH_k with $k \in [1, 5]$, $\mathbf{x}_{c-1}^{a,glo}$ is set to 0. The forecast step thus reads:

$$\mathbf{x}_c^{f,i} = \begin{cases} \mathbf{x}_0 + \boldsymbol{\theta}_1^i & \text{if } c = 1 \\ \mathbf{x}_{c-1}^{a,glo} + \boldsymbol{\theta}_c^i & \text{if } c > 1 \end{cases} \quad (6)$$

with

$$\mathbf{x}_{c-1}^{a,glo} = \left[\overline{(K_{s_k})^a}_{c-1} \text{ with } k \in [0, 6], \overline{\mu^a}_{c-1}, 0 \text{ for each } \delta H_k \text{ with } k \in [1, 5] \right], \quad (7)$$

and

$$\boldsymbol{\theta}_c^i \sim \mathcal{N}\left(\mathbf{0}, (\sigma_c^i)^2\right), \quad (8)$$

where

$$\sigma_c^i = \begin{cases} \sigma_{\mathbf{x}} & \text{if } c = 1, \\ \lambda \sqrt{\frac{1}{N_e-1} \sum_{i=1}^{N_e} (\mathbf{x}_{c-1}^{a,i} - \bar{\mathbf{x}}_{c-1}^a)^2} + (1 - \lambda)\sigma_{\mathbf{x}} & \text{if } c > 1. \end{cases} \quad (9)$$

For the first cycle, the perturbed friction, upstream forcing coefficient values and floodplain state perturbations are drawn within the PDFs described in Table 1. For the next cycles, the set of coefficients issued from the mean analysis at the previous cycle $c - 1$ is further dispersed by additive perturbations $\boldsymbol{\theta}$ (Eq. (8)) drawn from the Gaussian distribution with zero mean and a standard deviation obtained from the linear combination of the standard deviation of the analysis at $c - 1$ and $\sigma_{\mathbf{x}}$ described in Table 1.

356 The two terms are weighted by the hyperparameter λ (Eq. (9)). This technique is an ad-
 357 vanced alternative to anomalies inflation for avoiding the well-known ensemble collapse,
 358 better suited for heterogeneous control of parameters. The combined update of the vari-
 359 ance for the re-sampling of the parameters allows to preserve part of the information from
 360 the background statistical description that may differ amongst the parameters and over
 361 time while also inheriting analyzed variance from the previous cycle. In the following im-
 362 plementation, λ is set to 0.3. This tuning was chosen after the analysis of the ensemble
 363 spread in the control space along the DA cycles.

The background hydraulic state, associated with each member of the ensemble of
 inputs, denoted by $\mathbf{s}_c^{f,i}$, results from the integration of the hydrodynamic model $\mathcal{M}_c: \mathbb{R}^n \rightarrow$
 \mathbb{R}^m from the control space to the model state (of dimension m) over W_c :

$$\mathbf{s}_c^{f,i} = \mathcal{M}_c(\mathbf{s}_{c-1}^{a,i}, \mathbf{x}_c^{f,i}). \quad (10)$$

364 The initial condition for \mathcal{M}_c at t_{start} is provided by a user-defined restart file for
 365 the first cycle. For the following cycles, it takes in a full restart $\mathbf{s}_{c-1}^{a,i}$ saved from the anal-
 366 ysis run of the previous cycle $\mathbf{s}_{c-1}^{a,i}$ at time $t_{start} + T_{shift}$. Note that in order to avoid
 367 inconsistencies between the state and the analysed set of parameters at t_{start} , a short
 368 spin-up integration is run on the 3 hours preceding t_{start} . It should be noted that the
 369 perturbations δH_k ($k \in [1, 5]$) (Eq. 6) are evenly distributed on the time steps in $[t_{start} -$
 370 $3h, t_{start} + T_{shift}]$ and added to the simulated WL field, while enforcing that the result-
 371 ing WL at each pixel remains non-negative.

The control vector equivalent in the observation space for each member, denoted
 by $\mathbf{y}_c^{f,i}$, stems from:

$$\mathbf{y}_c^{f,i} = \mathcal{H}_c(\mathbf{s}_c^{f,i}) \quad (11)$$

where $\mathcal{H}_c: \mathbb{R}^m \rightarrow \mathbb{R}^{n_{obs}}$ is the observation operator from the model state space to the
 observation space (of dimension n_{obs}) that selects, extracts and eventually interpolates
 model outputs at times and locations of the observation vector \mathbf{y}_c^o over W_c . The obser-
 vation vector here gathers observations of different types (in-situ WL and WSR), at dif-
 ferent times over W_c . The observation operator \mathcal{H}_c is thus composed of two operations
 that are applied separately to the T2D hydraulic state. On the one hand, a selection op-
 erator that extracts the WL at time and locations of the in-situ observations. On the
 other hand, a flood mask generator that applies a threshold of 5 cm on the WL simu-
 lated field at S1 overpass times, in order to identify the wet/dry pixel mask, then com-
 puts WSR observations by counting the number of wet pixels in each subdomain of the
 floodplain. It should be noted that, in the following, the observation operator regard-
 ing the in-situ observations, also includes a bias removal step to take into account a sys-
 tematic model error. Eq. (11) thus reads

$$\mathbf{y}_c^{f,i} = \mathcal{H}_c(\mathbf{s}_c^{f,i}) - \mathbf{y}^{bias} \quad (12)$$

372 where \mathbf{y}^{bias} is an a priori knowledge of the model-observation bias. Such a bias was di-
 373 agnosed and estimated during the 24-hour quasi-stationary non-overflowing period of 2021-
 374 01-15. This yields $\mathbf{y}_{Tonneins}^{bias} = 0.72$, $\mathbf{y}_{Marmande}^{bias} = 0.40$, and $\mathbf{y}_{LaR  ole}^{bias} = -0.24$ m (Nguyen
 375 et al., 2021, 2022).

376 3.3 Description of the EnKF analysis step

The EnKF analysis step stands in the update of the control and model state vec-
 tors. When applying a stochastic EnKF (Asch et al., 2016), the observation vector $\mathbf{y}^{o,i}$
 is perturbed, and an ensemble of observations $\mathbf{y}_c^{o,i}$ ($i \in [1, N_e]$) is generated:

$$\mathbf{y}_c^{o,i} = \mathbf{y}_c^o + \boldsymbol{\epsilon}_c \text{ with } \boldsymbol{\epsilon}_c \sim \mathcal{N}(\mathbf{0}, \mathbf{R}_c). \quad (13)$$

377 $\mathbf{R}_c = \sigma_{obs}^2 \mathbf{I}_{n_{obs}}$ is the observation error covariance matrix ($\mathbf{I}_{n_{obs}}$ is the $n_{obs} \times n_{obs}$ identity
 378 matrix). \mathbf{R}_c is assumed to be diagonal, of standard deviation σ_{obs} , as the observa-
 379 tion errors are assumed to be uncorrelated, Gaussian with a standard deviation propor-
 380 tional to the observation $\sigma_{obs,c} = \tau \mathbf{y}_c^o$. This stochastic perturbation was not set up for
 381 the WSR observations in $\mathbf{y}_c^{o,i}$ in order to avoid values beyond the physical range $[0, 1]$
 382 for the ratio.

The innovation vector over W_c is the difference between the perturbed observation
 vector $\mathbf{y}_c^{o,i}$ and the model equivalent $\mathbf{y}_c^{f,i}$ from Eq. (11) and Eq. (13). It is weighted by
 the Kalman gain matrix \mathbf{K}_c and then added as a correction to the background control
 vector $\mathbf{x}_c^{f,i}$, so that the analysis control vector $\mathbf{x}_c^{a,i}$ reads:

$$\mathbf{x}_c^{a,i} = \mathbf{x}_c^{f,i} + \mathbf{K}_c (\mathbf{y}_c^{o,i} - \mathbf{y}_c^{f,i}), \quad (14)$$

with

$$\mathbf{x}_c^{a,i} = [(K_{s_k})_c^{a,i} \text{ with } k \in [0, 6], \mu_c^{a,i}, (\delta H_k)_c^{a,i} \text{ with } k \in [1, 5]]. \quad (15)$$

The Kalman gain reads:

$$\mathbf{K}_c = \mathbf{P}_c^{\mathbf{x},\mathbf{y}} [\mathbf{P}_c^{\mathbf{y},\mathbf{y}} + \mathbf{R}_c]^{-1}. \quad (16)$$

$\mathbf{P}_c^{\mathbf{y},\mathbf{y}}$ is the covariance matrix of the error in the background state equivalent in the ob-
 servation space \mathbf{y}_c^f . $\mathbf{P}_c^{\mathbf{x},\mathbf{y}}$ is the covariance matrix between the error in the control vec-
 tor and the error in \mathbf{y}_c^f . Both matrices are stochastically estimated within the ensem-
 ble:

$$\mathbf{P}_c^{\mathbf{x},\mathbf{y}} = \frac{1}{N_e} \mathbf{X}_c^T \mathbf{Y}_c \in \mathbb{R}^{n \times n_{obs}} \quad (17)$$

$$\mathbf{P}_c^{\mathbf{y},\mathbf{y}} = \frac{1}{N_e} \mathbf{Y}_c^T \mathbf{Y}_c \in \mathbb{R}^{n_{obs} \times n_{obs}} \quad (18)$$

with:

$$\mathbf{X}_c = [\mathbf{x}_c^{f,1} - \overline{\mathbf{x}_c^f}, \dots, \mathbf{x}_c^{f,N_e} - \overline{\mathbf{x}_c^f}] \in \mathbb{R}^{n \times N_e} \quad (19)$$

$$\mathbf{Y}_c = [\mathbf{y}_c^{f,1} - \overline{\mathbf{y}_c^f}, \dots, \mathbf{y}_c^{f,N_e} - \overline{\mathbf{y}_c^f}] \in \mathbb{R}^{n_{obs} \times N_e} \quad (20)$$

and

$$\overline{\mathbf{x}_c^f} = \frac{1}{N_e} \sum_{i=1}^{N_e} \mathbf{x}_c^{f,i} \in \mathbb{R}^n \quad (21)$$

$$\overline{\mathbf{y}_c^f} = \frac{1}{N_e} \sum_{i=1}^{N_e} \mathbf{y}_c^{f,i} \in \mathbb{R}^{n_{obs}}. \quad (22)$$

383 It should be noted that a localization on $\mathbf{P}_c^{\mathbf{x},\mathbf{y}}$ was implemented so that only the WSR
 384 observations are used to account for errors in the floodplain state through the estima-
 385 tion of $\delta H_k^{a,i}$. Consequently, the correction of the hydraulic state in the floodplain is only
 386 activated when WSR are available over the assimilation window. This prevents from equi-
 387 finality issues due to the size of the ensemble. Indeed, the stochastic approximation in
 388 Eq. (17) and Eq. (18) could infer some artificial sensitivity of the hydraulic state in the
 389 floodplain with respect to the friction coefficients in the river bed.

The analyzed hydrodynamic state, associated with each analyzed control vector $\mathbf{x}_c^{a,i}$
 is denoted by $\mathbf{s}_c^{a,i}$. It results from the integration of the hydrodynamic model \mathcal{M}_c with
 the updated friction coefficients $(K_{s_k})_c^{a,i}$, the upstream forcing Q_{up} using $\mu_c^{a,i}$ and the
 state correction in the floodplain $\delta H_k^{a,i}$ over W_c , starting from the same initial condi-
 tion as each background simulation within the ensemble. In order to preserve a smooth
 WL field, the mean of the analysis for $\overline{\delta H_k^a}$ computed within the ensemble is considered
 (Eq. (25)).

$$\mathbf{s}_c^{a,i} = \mathcal{M}_c(\mathbf{s}_{c-1}^{a,i}, \tilde{\mathbf{x}}_c^{a,i}), \quad (23)$$

with

$$\tilde{\mathbf{x}}_c^{a,i} = \left[(K_{s_k})_c^{a,i} \text{ with } k \in [0, 6], \mu_c^{a,i}, \overline{(\delta H_k)_c^a} \text{ with } k \in [1, 5] \right], \quad (24)$$

and

$$\overline{(\delta H_k)_c^a} = \frac{1}{N_e} \sum_{i=1}^{N_e} (\delta H_k)_c^{a,i} \text{ with } k \in [1, 5]. \quad (25)$$

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4 Experimental settings

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4.1 Specifications of Observing System Simulation Experiments

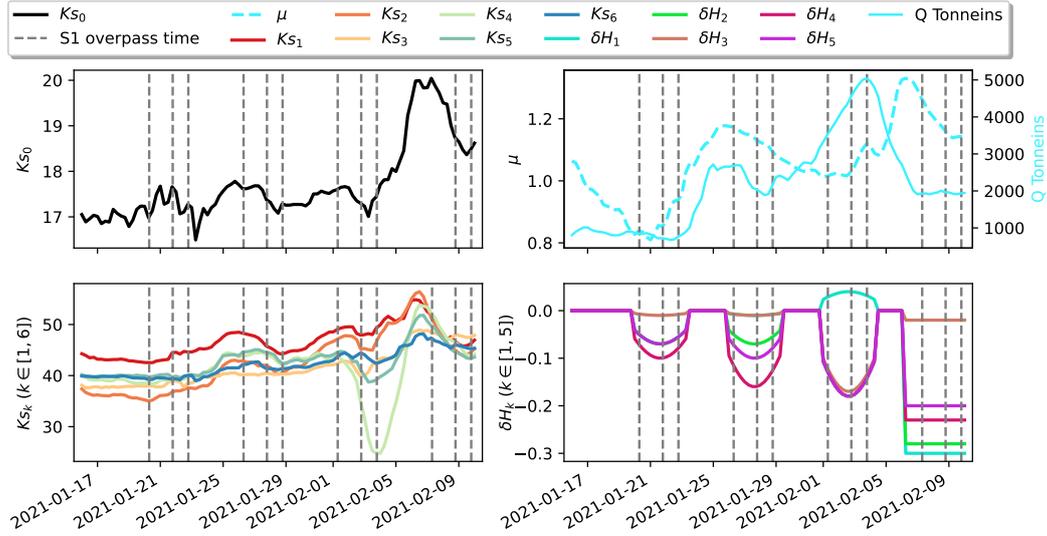


Figure 4: True values of the control vector for the reference simulation over the synthetic 2021 event in OSSE. Top left: K_{s_0} , bottom left: K_{s_k} with $k \in [1, 6]$, top right: μ (left y-axis, dashed cyan curve) and $Q(t)$ (right y-axis, solid cyan curve), bottom right: δH_k with $k \in [1, 5]$. These color codes are identical to those of Figure 1. The S1 overpass times are indicated as vertical black dashed lines.

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The framework of an OSSE is based on a deterministic simulation with a selected set of time-varying parameters over the flood event, as shown in Figure 4. This reference simulation is further denoted as true. In the present work, the true friction parameter K_{s_k} with $k \in [0, 6]$, are set from the results of a previous DA experiments on the real 2021 flood event. In Figure 4, the true friction coefficient for the floodplain K_{s_0} is plotted in black on the top left panel and the true friction coefficients K_{s_k} with $k \in [1, 6]$ for the river bed are plotted on the bottom left panel. The time-series discharge for the 2021 event is used as the upstream BC for the OSSE experiment. The true multiplicative correcting factor μ for the inflow is also issued from a previous DA analysis, and is added a cosine function as perturbation. It is plotted as a dashed cyan curve on the top right panel in Figure 4 (left y-axis) along with the inflow BC at Tonneins, represented by a solid cyan curve (right y-axis). The state correction true values were set up with negative cosine curves for the three first groups of S1 observations (from the beginning of the event until the flood peak), and a constant water removal of -18 cm over the flood recession period. They are shown on the bottom right panel in Figure 4. For the sake of consistency, the color codes for K_{s_k} with $k \in [1, 6]$ and for δH_k with $k \in [1, 5]$ are identical to their effective areas depicted in Figure 1.

409 The true simulation is used to provide synthetic observations using the observa-
 410 tion operator \mathcal{H}_c from Eq. (11) applied at the in-situ and S1 observation times from the
 411 real 2021 event. This stands in the extraction of the true simulated WL values at all ob-
 412 servation times and locations, first to generate synthetical in-situ observations, and sec-
 413 ond to extract the wet/dry pixels for WSR computation. Thus this experiment is fur-
 414 ther denoted as *synthetical 2021 event*. These synthetical in-situ and WSR observations
 415 are then assimilated in a DA experiment, with a priori settings that differ from the truth.
 416 The OSSE experiments aim at assessing the performance of the DA method involving
 417 both types of observations (in-situ and WSR), especially its capacity to retrieve the true
 418 parameters (forcing data, friction coefficients and state correction).

419 4.2 Experimental setup and assessment metrics

420 In both OSSE and real event experiments, one free run FR (without assimilation),
 421 and three DA experiments were carried out with different configurations regarding the
 422 types of observations that are assimilated and the active components of the control vec-
 423 tor, as detailed in Table 3. Two types of observations are considered: (i) in-situ WL ob-
 424 servations at the three VigiCrue stations Tonneins, Marmande and La Réole every 15
 425 minutes, (ii) WSR values computed over the five floodplain zones at S1 overpass times.
 426 Then, two options of control vector are involved, one with all six friction coefficients and
 427 the inflow multiplicative coefficient, whereas the other one is extended with the water
 428 state correction in the floodplain. With these configurations, three experiments are called
 429 IDA, IWDA and IHDA. IDA experiment only assimilates in-situ WL observations (syn-
 430 thetical observations in the context of OSSE) and the control vector is limited to fric-
 431 tion coefficients K_{s_k} with $k \in [0, 6]$ and the inflow multiplicative coefficient μ . IWDA
 432 experiment assimilates in-situ WL and WSR observations (synthetical in the context of
 433 OSSE) with the same control vector as IDA. IHDA has an extended control vector that
 434 also includes δH_k with $k \in [1, 5]$, it assimilates the same in-situ WL and WSR obser-
 435 vations (synthetical in the context of OSSE) as IWDA. For the DA experiments, the pro-
 436 portionality coefficient used to specify the observation error τ (cf. subsection 3.3) for in-
 437 situ data is fixed to 15%, meaning that σ_{obs} amounts to 15% of the observation value,
 438 whereas the value of τ for WSR data varies from 10% to 20% depending on how early
 439 the observation time is within the 18-hour assimilation window. All DA experiments were
 440 carried out using $N_e = 75$ members. In the following, the subscript *OSSE* is used in
 441 the experiment name to distinguish the OSSE from the real modes.

442 The metrics employed for 1D and 2D assessment are formulated with respect to
 443 the observations that are synthetical in the context of OSSE, or with respect to the real
 444 observations from the VigiCrue gauge stations (for the in-situ WL) and from S1/S2 im-
 445 ages (for 2D flood extent maps and derived WSR).

Table 3: Summary of the Free Run and DA experiment settings.

Exp. name	DA	Assimilated observations	Nb of members N_e	Control variables
FR	No	-	1	-
IDA _(OSSE) /IDA	Yes	In-situ WL	75	$K_{s[0:6]}, \mu$
IWDA _(OSSE) /IWDA	Yes	In-situ WL and WSR	75	$K_{s[0:6]}, \mu$
IHDA _(OSSE) /IHDA	Yes	In-situ WL and WSR	75	$K_{s[0:6]}, \mu, \delta H_{[1:5]}$

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4.2.1 1D metrics for water level time-series assessment

The quality of the simulated WL, noted H^m , is assessed with respect to in-situ observed WL, noted H^o , computing the root-mean-square error (RMSE) between the simulated and the observed WL time-series, sampled at observation times, along the assimilation windows for the entire flood event:

$$\text{RMSE} = \sqrt{\frac{1}{n_{obs}} \sum_{i=1}^{n_{obs}} (H_i^m - H_i^o)^2} \quad (26)$$

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In the case of OSSE, the RMSE is also formulated with respect to the control parameters, computing the difference between their true value and the DA analysis.

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4.2.2 2D metrics for flood extent assessment

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The simulated flood extent maps are generated from the T2D simulated WL 2D field, by applying a threshold of 5 cm below which the pixel is considered as dry and above which it is considered as wet. The T2D WL output field is first projected onto the regular grid of the S1 image (ground sampling distance: 10×10 m) so as to allow for a straightforward comparison between observed and simulated flood extent. In the case of OSSE, the water flood maps from the reference simulation are used instead of the observed flood extent maps from S1 images.

The metrics to compare the simulated and the observed flood extents are the Critical Success Index (CSI) and Cohen's kappa index (κ). CSI considers the FloodML flood extent maps as the reference observed flood maps (ground truth) based on which the T2D simulated flood extent maps are evaluated, whereas the objective of κ index is used to measure the agreement between the two flood extent estimators. The formulation of these indices relies on the count of pixels following one of four outcomes that constitute a contingency map: True Positives (TP) and True Negatives (TN), respectively, are the number of pixels correctly predicted as flooded and correctly identified as non-flooded, False Positives (FP) or *over-prediction* is the number of non-flooded pixels incorrectly predicted as flooded, and False Negatives (FN) or *under-prediction* is the number of missed flooded pixels. Based on these counts, the CSI and κ indices are computed as follows:

$$\text{CSI} = \frac{TP}{TP + FP + FN}, \quad (27)$$

$$\kappa = \frac{p_o - p_e}{1 - p_e} \quad (28)$$

where p_o is the observed proportionate agreement and p_e is the probability of a random agreement, defined as follows:

$$p_o = \frac{TP + TN}{TP + FP + FN + TN},$$

$$p_e = \frac{TP + FN}{TP + FP + FN + TN} \times \frac{TP + FP}{TP + FP + FN + TN}.$$

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These two metrics range from 0% when there is no common area (i.e. no agreement) between the simulated and the observed flood extents, and reach their highest value of 100% when the prediction provides a perfect fit to the observed flood extents. While CSI is conventionally the most widely used metric for this comparison, Cohen's kappa index provides a better overall metric with TN pixels also being taken into account. Lastly, it should be noted that the magnitude and the size of the flood (and consequently the number of pixels used for the computation) were shown by (Stephens et al., 2014) to have a significant influence on these indices; thus limiting their use for different event and different catchment comparison. This limitations has no impact here, as CSI and κ indices are used to compare different numerical experiments on a single catchment and on the same event.

5 Results and Discussions

Quantitative performance assessments are carried out in the control and in the observational spaces by comparing (i) the parameters yielded by the different DA analysis, including a comparison to the true parameters in OSSE, (ii) the different analyzed WL time-series with synthetical or real in-situ observations, (iii) the different analyzed WSR with real or synthetical WSR observations in the floodplain, and (iv) the contingency maps and the overall CSI and Cohen's kappa index computed for the different analyzed flood extent maps, with respect to the synthetical or real observed flood extent maps. First, these comparisons in OSSE mode (subsection 5.1) allow to assess the benefits of assimilating spatially distributed RS-derived observations, with an augmented control vector, in order to represent the floodplain dynamics, and advocates for this strategy in real experiment mode. Then, subsection 5.2 presents all these quantitative assessments concerning the two real flood events, 2019 and 2021.

5.1 Results for OSSE experiments

5.1.1 Results in the control space for OSSE

Figure 5 shows the analyzed parameters from the different DA experiments, with blue lines for IDA, green lines for IWDA and red lines for IHDA for the synthetical 2021 flood event. The true parameter values are plotted in black and the calibrated or default values \mathbf{x}_0 are indicated by horizontal dashed lines. The overpass times of S1 over the 2021 event are depicted by vertical dashed lines. The analyzed values for K_{s_k} (with $k \in [0, 6]$) are shown on the left column, while that of the inflow correction μ is in the top panel of the right column. The reference and the analyzed values in IHDA experiment for δH_k^a with $k \in [1, 5]$ are shown on the other panels of the right column, respectively in black and in red (0 for the default value). The bottom right panel displays the upstream forcing for reference purposes.

For the synthetical 2021 event, it appears that all three DA analyses succeed in retrieving the true friction coefficients in the river bed, with a lesser success on the 5th and 6th river segments (i.e. K_{s_5} and K_{s_6}). This is most likely due to equifinality issues, as the downstream part of the flow is also influenced by the friction in the middle part of the river near Marmande (corresponding to the 3rd and 4th river segments controlled by K_{s_3} and K_{s_4}). Also due to the equifinality issues, the analysis for the floodplain friction K_{s_0} probably compensates for the analysis of K_{s_3} at the beginning of the event during low flow. As the water begins to occupy the floodplain, this equifinality issue lessens and the analysis on the floodplain friction becomes more efficient, and converges to the true value. It should be noted that despite these equifinality issues, all analyzed friction coefficients remain within physical ranges (both for the ones in the river bed and the one in the floodplain) and closer to the true value than to the default value, especially near the flood peak. It is also worth-noting that, as expected, the assimilation of in-situ observations at Marmande (located in the 4th river segment) allows for an excellent analysis on K_{s_4} for IDA, and no additional information from the floodplain is necessary to constrain the friction in this segment. The analysis for the multiplicative factor μ is very noteworthy for all 3 DA experiments, even with a small underestimation as water recession starts. Given the localization step in the EnKF algorithm, the analysis for the state correction in the floodplain δH_k ($k \in [1, 5]$) only activates when WSR observations are present over the 18-hour assimilation window. Hence, the analysis for the WL correction (IHDA in red) is zero most of the time, including in between two S1 overpass times (in this catchment there is a minimum of 24 hours between two S1 observations from different orbits). For the assimilation windows that include WSR observations, the IHDA analysis succeeds in retrieving the values that are close to the true values for all subdomains of the floodplain and over the entire event.

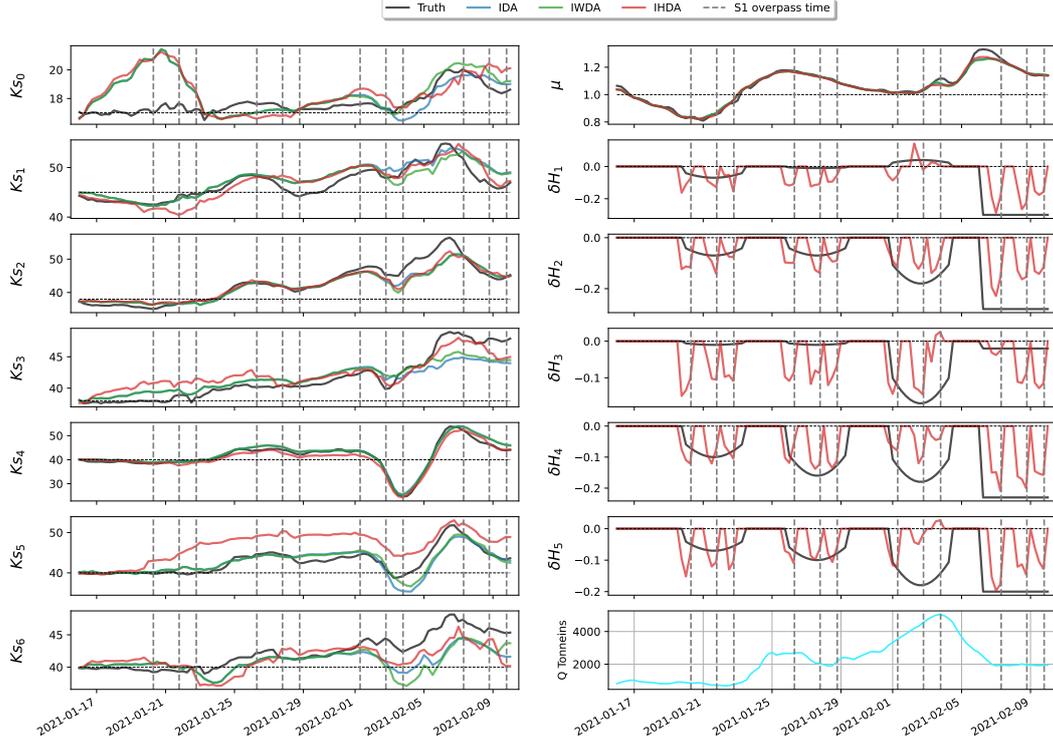


Figure 5: Analyzed values of the control vector for IDA (blue), IWDA (green), and IHDA (red) in OSSE. The default values are represented with horizontal dashed lines, whereas the S1 overpass times are shown with vertical dashed lines. Left column: friction coefficients in the floodplain K_{s_0} , and in the river bed K_{s_k} (with $k \in [1, 6]$). Right column, from top to bottom: multiplicative correction to the inflow μ , state correction δH_k (with $k \in [1, 5]$), and upstream forcing $Q(t)$.

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5.1.2 Results in the observation space: Water levels at observing stations for OSSE

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The RMSE (Eq. (26)) computed over the entire event, for the WL from FR simulation, as well as from IDA, IWDA and IHDA analyses, with respect to the reference WL at Tonneins, Marmande, and La Réole are presented in Table 4. For each observing station, the lowest RMSE values are underlined. Table 4 shows that all DA experiments succeed in significantly reducing the WL errors, compared to that of FR. The reduction in RMSE with respect to FR amounts to 79%, 89%, and 91%, respectively, at Tonneins, Marmande, and La Réole, with very close values for IDA, IWDA and IHDA. The RMSE at observing stations remains under 5.5 cm for all DA experiments. This level of precision is expected in OSSE, in coherence with the prescribed observation error. It validates the performance of the implemented EnKF solution. These results illustrate that the correction of the hydraulic state in the river bed can be properly achieved assimilating WL at observing stations only, and that the complementary assimilation of WSR is of greater interest when assessing the dynamics of the floodplain.

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5.1.3 Results in the observation space: WSR in the floodplain for OSSE

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The WSR in the five floodplain zones for the simulated WL in FR and the analyzed WL in the three DA experiments are compared to the WSR computed from the

Table 4: Water level RMSE w.r.t. reference water levels at VigiCrue observing stations, for 2021 synthetical event, in OSSE.

Exp. name	Root-Mean-Square Error [m]		
	Tonneins	Marmande	La Réole
FR	0.260	0.397	0.578
IDA	0.052	<u>0.042</u>	0.053
IWDA	0.055	0.044	0.054
IHDA	<u>0.052</u>	0.045	<u>0.050</u>

536 reference simulation in Figure 6. The WSR values are shown in Figure 6a and the mis-
537 fit between the reference and simulation WSR values (i.e. observed WSR - simulated WSR)
538 are shown in 6b. The WSR for the truth are plotted in black, whereas the WSR for FR
539 are in orange. The color code for the DA experiments is the same as in Figure 5: IDA
540 in blue, IWDA in green, and IHDA in red. From the beginning of the event to the flood
541 rising limb (around 2021-02-01), the impact of assimilating WSR is insignificant as the
542 water has not overflowed to the floodplain. The WSR values in the reference and the ex-
543 periment are thus null or close to zero.

544 Near the flood peak, FR underestimates flooding in most of the zones, with the ex-
545 ception of zone 5. Both IDA and IHDA present improved results with greater WSR val-
546 ues than FR. The merits of IHDA (red) versus IWDA (green) is clearly visible during
547 the flood recess (after 2021-02-03) in all zones when the T2D model alone in FR fails to
548 evacuate the water. The WSR values in IHDA are brought significantly close to the ref-
549 erence WSR values, while WSR values for IDA and IWDA are not better than those of
550 FR. This illustrates how the augmented control vector with δH_k (with $k \in [1, 5]$) al-
551 lows for an efficient assimilation of the information in the floodplain expressed as WSR
552 measurements, and an associated correction of the floodplain dynamics. This shows that
553 IHDA is the most efficient DA strategy to represent the floodplain, thus advocates for
554 its application in real event mode.

555 **5.1.4 2D validation with contingency maps, CSI and κ indices for OSSE**

556 Figure 7 displays the resulting contingency maps for FR and DA experiments for-
557 mulated for the T2D simulated flood extent maps with respect to those of the reference
558 simulation in OSSE. The correctly predicted pixels are represented in light blue when
559 non flooded, and in dark blue when flooded in the (synthetical) observations. The in-
560 correctly predicted non-flood and flooded pixels (respectively, underprediction and over-
561 prediction) are represented in yellow and in red. Contingency maps are shown for the
562 synthetical 2021 event at the time of the flood peak (top panel) and during water recess
563 (bottom panel). The resulted CSI (Eq. (27)) and the κ indices (Eq. (28)) are also indi-
564 cated. At the flood peak, FR significantly underestimates flooding over several subdo-
565 mains of the floodplain. While the assimilation of in-situ data in IDA and the joint as-
566 similation of WSR in IWDA bring some improvements, the most significant improvement
567 comes from the extended control vector involving the hydraulic state associated with the
568 assimilation of WSR in IHDA. During the water recess, IDA and IWDA fail to bring any
569 improvement with respect to FR. Yet, the correction of the hydraulic state in the sub-
570 domains of the floodplain associated with the assimilation of WSR in IHDA leads to an
571 effective drying of the floodplain that is in good agreement with the synthetical obser-
572 vation.

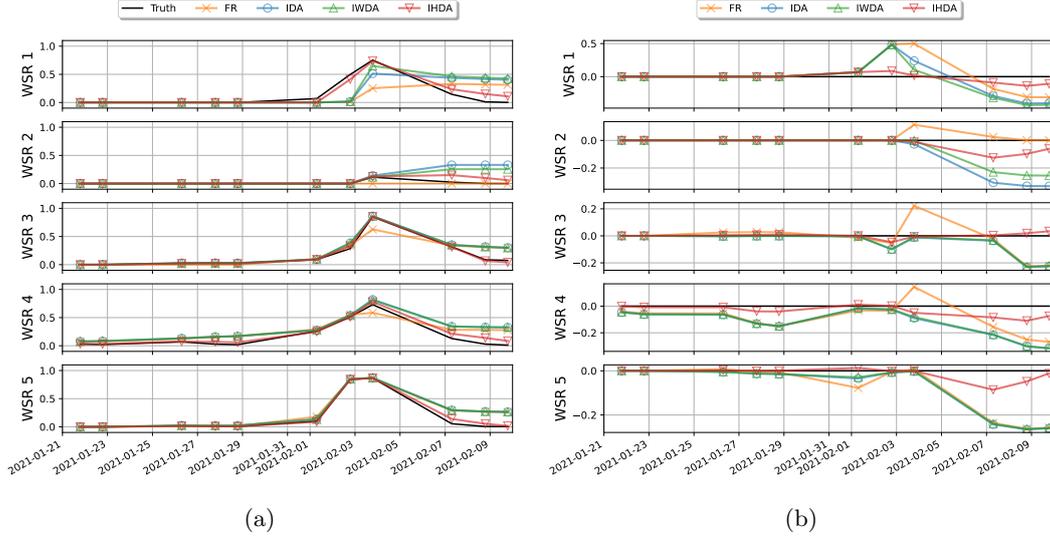


Figure 6: (a) WSR values computed in OSSE for the reference run (black), FR (orange), IDA (blue), IWDA (green), and IHDA (red) over the five subdomains of the floodplain. (b) Misfit between the reference WSR and the simulated WSR values in the five floodplain zones.

573 Figure 8a (respectively, Figure 8b) depicts the CSI (respectively, the κ index) yielded
 574 by FR and DA experiments at all S1 overpass times. Within the OSSE framework, all
 575 DA experiments result in flood extent maps that are in relative agreement with the refer-
 576 ence flood maps. Indeed, IDA, IWDA and IDA allow for a significant improvement with
 577 respect to FR near the flood peak (2021-02-03 19:00). Yet, IHDA outperforms both IDA
 578 and IWDA, especially during the flood recess. IHDA leads to a CSI above 68% at every
 579 time steps (and above 88% before water recession period). During the flood recess
 580 (last three timesteps), IDA and IWDA have a CSI varying between 38-63% while IHDA
 581 has a CSI above 68% at all 3 timesteps. The results on the κ index, while also involv-
 582 ing the TN counts (cf. subsection 4.2.1), provide the same conclusions. The analysis of
 583 the contingency maps as well as the CSI and κ indices demonstrate the merits of the as-
 584 similation of the WSR observations, together with the correction of the hydraulic state
 585 in subdomains of the floodplain. This strategy is thus applied in real event mode in the
 586 following subsection.

587 5.2 Results for real experiments

588 In this subsection, the quantitative assessments are carried out in two real flood
 589 events, 2019 and 2021.

590 5.2.1 Results in the control space

591 Similarly to Figure 5, the analyzed parameters from the different DA experiments
 592 in real mode for 2019 event (respectively, 2021 event) are shown in Figure 9a (respec-
 593 tively, in Figure 9b), where horizontal black dashed lines stand for the default values \mathbf{x}_0 ,
 594 blue curves for IDA, green curves for IWDA, and red curves for IHDA. The analyzed val-
 595 ues for K_{s_k} (with $k \in [0, 6]$) over the flood events are shown on the left column of each
 596 figure. The analysis for the inflow correction μ is shown in the top panel of the right col-
 597 umn. The analyzed values for δH_k^a (with $k \in [1, 5]$) by IHDA are shown on the other

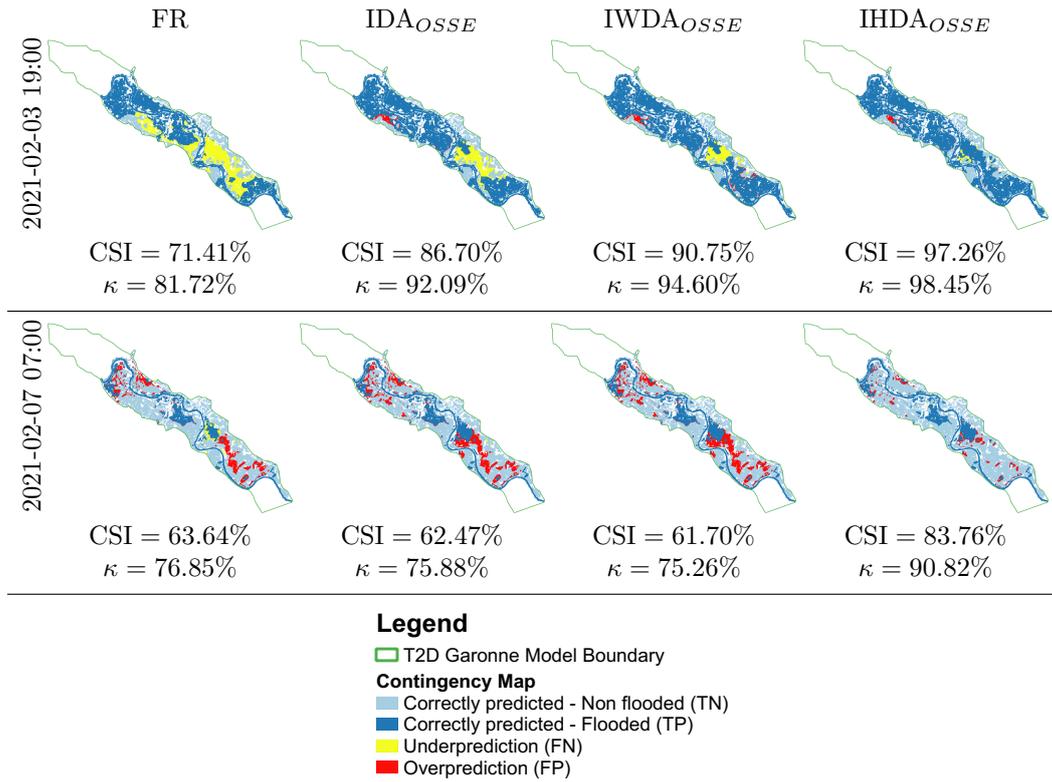


Figure 7: Contingency maps computed between simulated flood extent (from left to right: FR, IDA, IWDA and IHDA) with respect to the synthetic flood extent maps from the reference simulation in OSSE. First row: flood peak on 2021-02-03 18:48; Second row: flood recess on 2021-02-07 07:06.

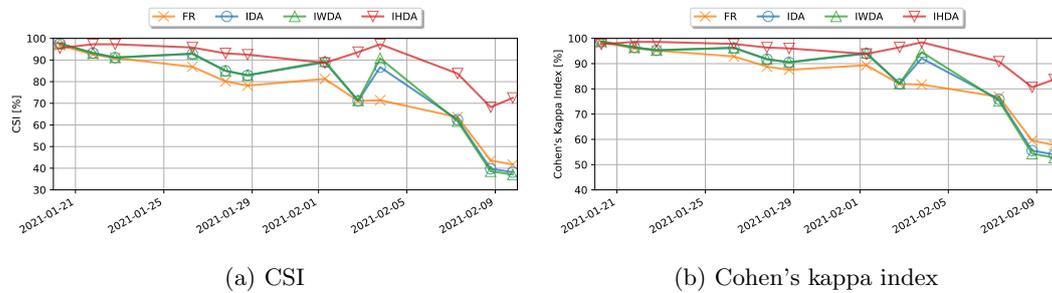


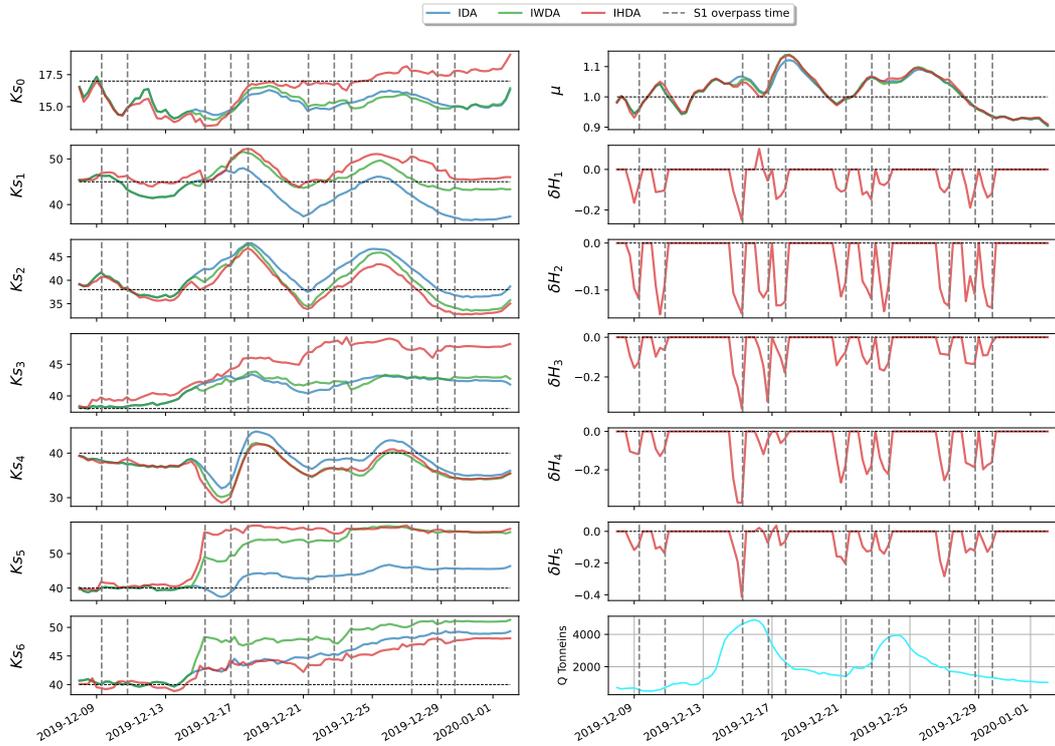
Figure 8: (a) CSI and (b) κ indices computed for the FR and DA experiments with respect to the synthetic flood extent from the reference simulation in OSSE, at S1 overpass times.

598 panels of the right column. The bottom panel of the right column displays the upstream
 599 forcing for reference purposes.

600 For all DA experiments and for both 2019 and 2021 events, the analysis values for
 601 the friction coefficients in the river bed and the floodplain remain within physical ranges,
 602 including the ones in the river bed and the one in the floodplain. The increment are larger

603 during the flood event, as the misfit between the background run and the observations
 604 increases. The analysis for IHDA are closer to that of IWDA, compared to IDA, as in
 605 both experiments the control vector is extended with the hydraulic state. The analysis
 606 is quite far from the calibrated values for the friction of the 5th and 6th river segments
 607 (i.e. K_{s_5} and K_{s_6}), which is most likely due to the poor quality of the model topogra-
 608 phy in the downstream part of the domain, and the large misfit between the in-situ and
 609 the simulated WLs at La Réole. As previously remarked in OSSE mode, the analysis in
 610 the 4th friction segment (i.e. K_{s_4}), that includes Marmande, is similar for IDA, IWDA
 611 and IHDA, showing that the assimilation of in-situ WLs suffices to account for friction
 612 errors in this area. Over the other friction zones, IDA is often closer to the default val-
 613 ues. The analyses on μ are similar for IDA, IWDA, and IHDA for both events. This sug-
 614 gests that the in-situ WLs observed at Tonneins are enough to constraint the multiplica-
 615 tive correction to the inflow and that the use of additional data in the floodplain is not
 616 necessary. Concerning IHDA, the mostly negative correction on all δH values increases
 617 (i.e. more water is removed in the corresponding floodplain zones) as the flood rises, es-
 618 pecially at the flood peak and during recess in order to account for the T2D model's lim-
 619 itation in physical process. During the recess period, the correction of the hydraulic state
 620 contributes in evacuating the water in the floodplain.

621 The results of IDA, IWDA and IHDA on the 2019 event show a greater dispersion
 622 than on the 2021 event. This may be due to the more complex flood dynamic of the 2019
 623 event with two peaks and thus results in a degraded representation between the first rec-
 624 cess and the second flood peak. As opposed to the assessment carried out in OSSE mode
 625 (subsection 5.1.1), the evaluation of the DA experiment results in the control space does
 626 not allow to quantitatively assess which DA strategy provides the best performance due
 627 to unknown true values of controlled parameters, thus further validations in the obser-
 628 vation space are necessary.



(a) 2019 flood event

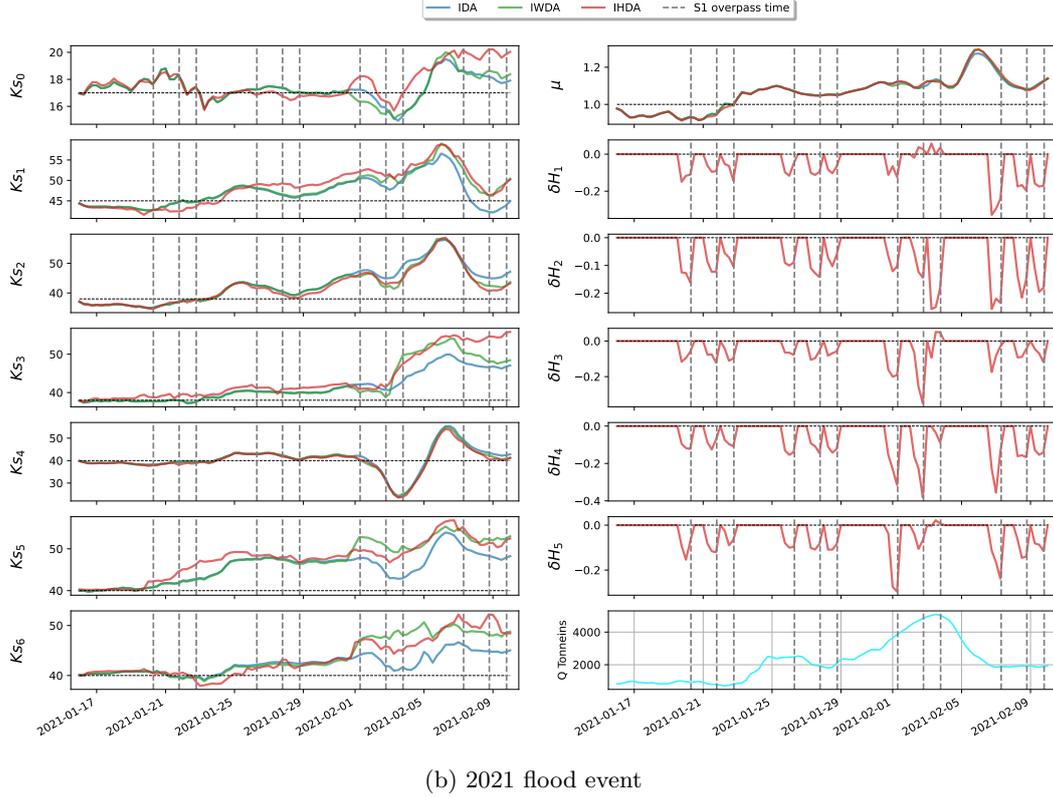


Figure 9: Analyzed values of the control vector for IDA (blue), IWDA (green), and IHDA (red), for (a) 2019 and (b) 2021 real events. The default values are represented by horizontal dashed lines, whereas the S1 overpass times are shown as vertical dashed lines. Left column: friction coefficients in the floodplain K_{s_0} , and in the river bed K_{s_k} (with $k \in [1, 6]$). Right column, from top to bottom: multiplicative correction to the inflow μ , state correction δH_k (with $k \in [1, 5]$), upstream forcing $Q(t)$.

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5.2.2 Results in the observation space: Water levels at observing stations

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The RMSEs computed over time for the 2019 event (respectively, 2021 event), for the WLs from the FR, IDA, IWDA and IHDA, with respect to the observed WLs at Tonneins, Marmande, and La Réole are summarized in Table 5a (respectively, in Table 5b). For each observing station, the lowest RMSE values are underlined. Table 5 shows that all DA experiments succeed in significantly reducing the WL errors compared to those of FR, even though such reductions are less significant than in OSSE (Table 4).

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For the 2019 event, the reductions in RMSE with respect to FR amount to 50%, 77%, and 57%, respectively, at Tonneins, Marmande, and La Réole, with close values between IDA, IWDA, and IHDA. For the 2021 event, those reductions are 34%, 80%, and 84%, respectively, at Tonneins, Marmande, and La Réole. For both event, the RMSEs at Tonneins and Marmande remain under 8 cm for all DA experiments, whereas it is under 14 cm at La Réole. While the RMSEs at Tonneins remain similar between the two events, a trade-off between Marmande and La Réole can be remarked for the 2019 and the 2021 events. These indicates that the model struggles to represent the dynamics at La Réole, most likely due to errors in topography in the downstream part of the domain,

646 to errors in the rating curve used as downstream BC or to the presence of non-modeled
647 tributaries that might play a significant role for high flows.

Table 5: Water level RMSE w.r.t. in-situ water levels at VigiCrue observing stations. The lowest RMSE is underlined.

(a) 2019 flood event				(b) 2021 flood event			
Exp. name	Root-Mean-Square Error [m]			Exp. name	Root-Mean-Square Error [m]		
	Tonneins	Marmande	La Réole		Tonneins	Marmande	La Réole
FR	0.129	0.220	0.318	FR	0.106	0.392	0.536
IDA	<u>0.060</u>	<u>0.045</u>	<u>0.125</u>	IDA	<u>0.062</u>	<u>0.071</u>	0.081
IWDA	0.064	0.049	0.128	IWDA	0.069	0.077	0.081
IHDA	0.064	0.051	0.138	IHDA	0.065	0.073	<u>0.079</u>

648 It should be noted that the best DA strategy according to in-situ WL RMSE is IDA
649 (although ever so slightly). The assimilation of WSR in the floodplain (in IWDA and
650 IHDA) leads to a smaller WL improvement from FR at observing stations than IDA does.
651 This is because the dynamics of the T2D model may be consistent with the real dynam-
652 ics within the river bed, but not coherent with real dynamics in the floodplain. Indeed,
653 while in OSSE mode (subsection 5.1), the observations in both the river bed and the flood-
654 plain were obtained from the same set of reference parameters which results in IHDA
655 achieving the lowest RMSEs, it is highly probable that, for the real events, no set of model
656 parameters allows to represent simultaneously a realistic and consistent dynamics in the
657 river bed and in the floodplain. Therefore, a more complex hydrodynamic model should
658 be considered to overcome these limitations, for instance, by considering a finer zoning
659 of friction in the river bed and the floodplain, an addition of lateral tributaries that mainly
660 carry a large volume of water for high flows, a more precise description of the topogra-
661 phy in the floodplain, or an addition of physical processes in the SWE solver such as rain
662 and evapotranspiration. A preliminary conclusion here is that the assimilation of data
663 in the floodplain is shown to under-perform the assimilation of (in-situ) WL data in the
664 river bed, especially when the performance is only assessed through the metrics in the
665 river bed.

666 **5.2.3 Results in the observation space: WSR in the floodplain**

667 The WSR in the five floodplain subdomains for the simulated WL in FR and the
668 analyzed WL in the three DA experiments with a threshold of 5 cm are compared to the
669 WSR computed from the observed S1-derived flood extent maps, and shown in Figure 10
670 and Figure 11, respectively for the 2019 and 2021 events. For the 2019 event (respec-
671 tively, 2021 event), the WSR values are shown in Figure 10a (respectively, Figure 11a)
672 and the misfit between simulation and observation WSR values (i.e. observed WSR - sim-
673 ulated WSR) are shown in Figure 10b (respectively, Figure 11b). The color codes for the
674 experiments are the same as in previous figures, i.e. FR in orange, IDA in blue, IWDA
675 in green, and IHDA in red.

676 As previously noted in OSSE, the impact of assimilation WSR is not significant
677 until the floodplain is active. In most subdomains, when the floodplain is active, the model
678 (FR and all DA experiments) tend to overflow, especially during flood recess period.
679 First, it should be noted that the analysis for IDA and IWDA does not bring much im-
680 provement with respect to FR in the 2019 flood event. The improvement is much more

681 evident for IHDA, in both events, especially at the flood peak and during the recess pe-
 682 riod. For the 2019 event, IHDA brings a significant improvement for the subdomains 3,
 683 4 and 5 as the misfits in subdomains 1 and 2 have already been small for FR (hence the
 684 contributions from IHDA are less obvious). Such an improvement over all subdomains
 685 is much more evident in the 2021 event. A significant overprediction at the timestep right
 686 before the first peak (2019-12-15 07:00) in subdomain 4 and 5 can be observed. This could
 687 stem from the characteristics of SAR backscatter which intensifies as the soil moisture
 688 increases due to rainfalls while the area has not been flooded. The correction of the hy-
 689 draulic state in the floodplain for IHDA, during the recess of the first peak (between 2019-
 690 12-17 and 2019-12-21), allows for a better simulation of the second flood peak than in
 691 FR. For both events, the assimilation of WSR by IHDA with the hydraulic state correc-
 692 tions brings an improvement is all subdomains and the floodplain is efficiently emptied
 693 after the flood peak.

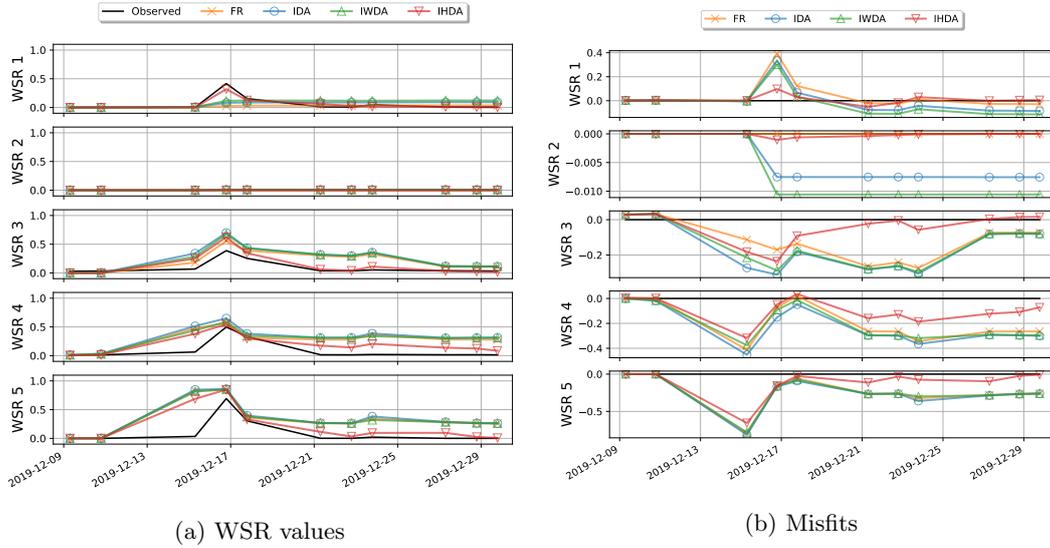


Figure 10: 2019 flood event - (a) WSR values computed for the S1-derived flood extent (black), FR (orange), IDA (blue), IWDA (green), and IHDA (red) over the five floodplain zones. (b) Misfit between the observed WSR and the simulated WSR values in the five floodplain zones.

694 **5.2.4 2D validation with contingency maps, CSI and κ indices**

695 Similarly to the OSSE, 2D validations are carried out by evaluating contingency
 696 maps comparing T2D water masks with S1- or S2-derived flood maps at their overpass
 697 times, and by quantitatively assessing the resulting CSI and the κ index scores. How-
 698 ever, since the flood dynamic is quite different and even more complex in the 2019 flood
 699 event, let us start with the 2D validation on this event. Figure 12 depicts the contingency
 700 maps based on the comparison of the T2D simulated flood extent maps from FR and
 701 DA experiments with respect to those derived from S1 or S2 images during the 2019 flood
 702 event. The contingency maps are shown from top to bottom, at satellite overpass time
 703 right before the first flood peak by S2 (2019-12-15 12:00), at flood peak by S1 (2019-12-
 704 16 19:00), during the flood falling limb by S2 (2019-12-17 12:00) and by S1 (2019-12-17
 705 19:00), and at the beginning of the second flood peak (2019-12-23 19:00) for S1. It should
 706 be stressed that, in this work, S2 imagery data are not assimilated and only are used for

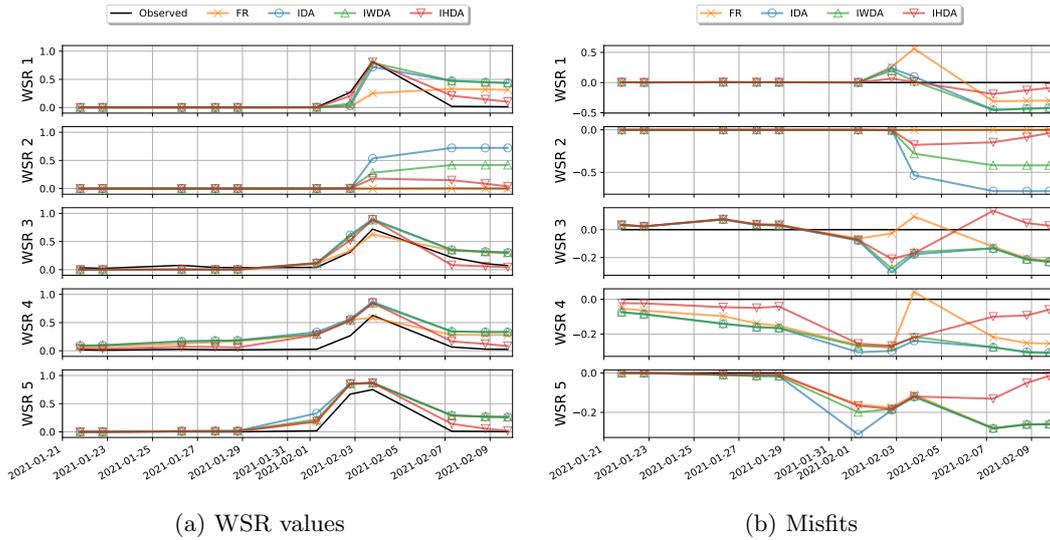


Figure 11: 2021 flood event - (a) WSR values computed for the S1-derived flood extent (black), FR (orange), IDA (blue), IWDA (green), and IHDA (red) over the five floodplain zones. (b) Misfit between the observed WSR and the simulated WSR values in the five floodplain zones.

707 validation as independent data. The associated CSI and the κ indices are indicated on
 708 each contingency map.

709 For 2019 flood event, IHDA brings noticeable improvements with respect to FR,
 710 IDA and IWDA before the flood peak (first row in Figure 12), with better predictions
 711 of the flooded pixels, mostly in subdomain 1 and 3. A relatively significant overpredic-
 712 tion on subdomain 4 and 5 from all experiments can be observed on these first-row fig-
 713 ures. It is coherent with the remark made on the WSR validation (subsection 5.2.3). At
 714 the first flood peak observed by S1 image (second row in Figure 12), IHDA allows bet-
 715 ter predictions of the flooded pixels, mostly in subdomain 1. During the first flood rec-
 716 cess (third and fourth row in Figure 12), the improvement brought by IHDA is not as
 717 visible as at the flood peak (second row). The added validation of the S2 image at 2019-
 718 12-17 12:00 provides an interesting remark. Indeed, the observed flood extent detected
 719 on this image is more similar to the one captured by the S1 image at 2019-12-16 19:00
 720 (or 17 hours backward) than the one right afterward at 2019-12-17 19:00 (or 5 hours for-
 721 ward). Such a situation, taking into account the fact that these three images in particu-
 722 lar were acquired in the span of 24 hours during the start of the falling limb, shows the
 723 different tendencies between the in-situ WL and the floodplain dynamics. This empha-
 724 sizes the complexity of the flood dynamics in the floodplain, and advocates for the fur-
 725 ther addition of the S2-derived flood observations in the DA. Such a remark of S1 and
 726 S2 incoherence is rarely possible due to the unavailability of S2 images during a flood
 727 event because of cloud cover problem. Lastly, the fifth row of Figure 12 shows an over-
 728 all improvement spread out over the five subdomains. This is also thanks to the state
 729 corrections applied at the timesteps between the two flood peaks.

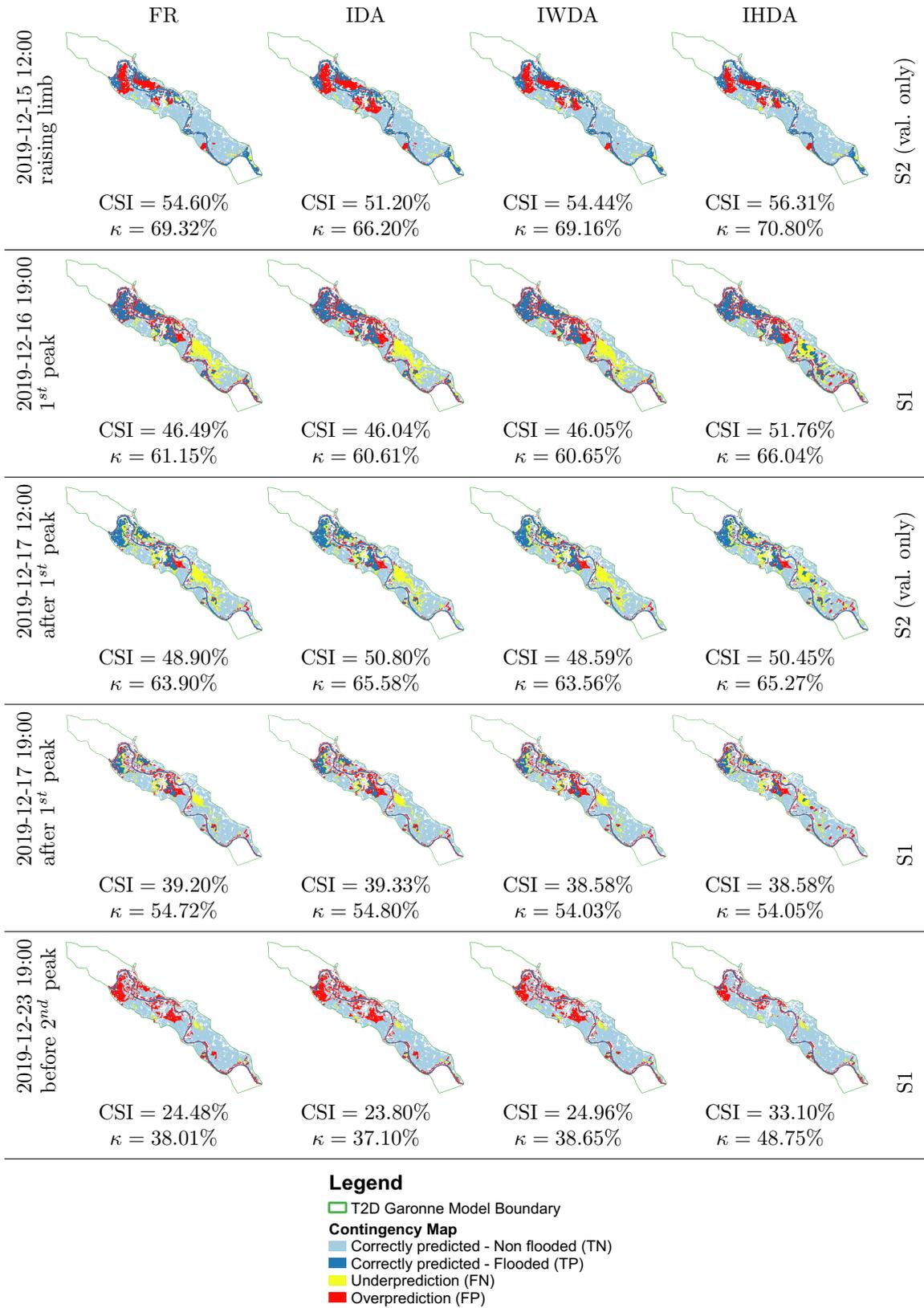


Figure 12: 2019 flood event - Contingency maps computed between simulated flood extent (from left to right: FR, IDA, IWDA and IHDA) with respect to S1-derived flood extent (row 2, 4 and 5) and S2-derived flood extent (rows 1 and 3).

730 Figure 13 displays the contingency map for the 2021 flood event (flood peak observed at 2021-02-03 19:00 and recess 2021-02-07 07:00), with metrics computed with respect to S1 derived flood extent as no S2 data were available. For 2021, the assimilation of WSR data brings a significant improvement at the flood peak (first row in Figure 13) in all subdomains in terms of the correctly predicted flood pixels. The recess period (second row in Figure 13) simulated by IHDA is also better than that of IDA and IWDA, yet, some residual flooded pixels remain, leading to still over-predicted areas. Figure 14 depicts the CSI (left column) and the κ index (right column) yielded by FR and DA experiments at all S1 overpass times, for 2019 event (top panels) and 2021 event (bottom panels), with the same color code used previously. These confirm the merits of the DA strategy in IHDA, especially for flood recess.

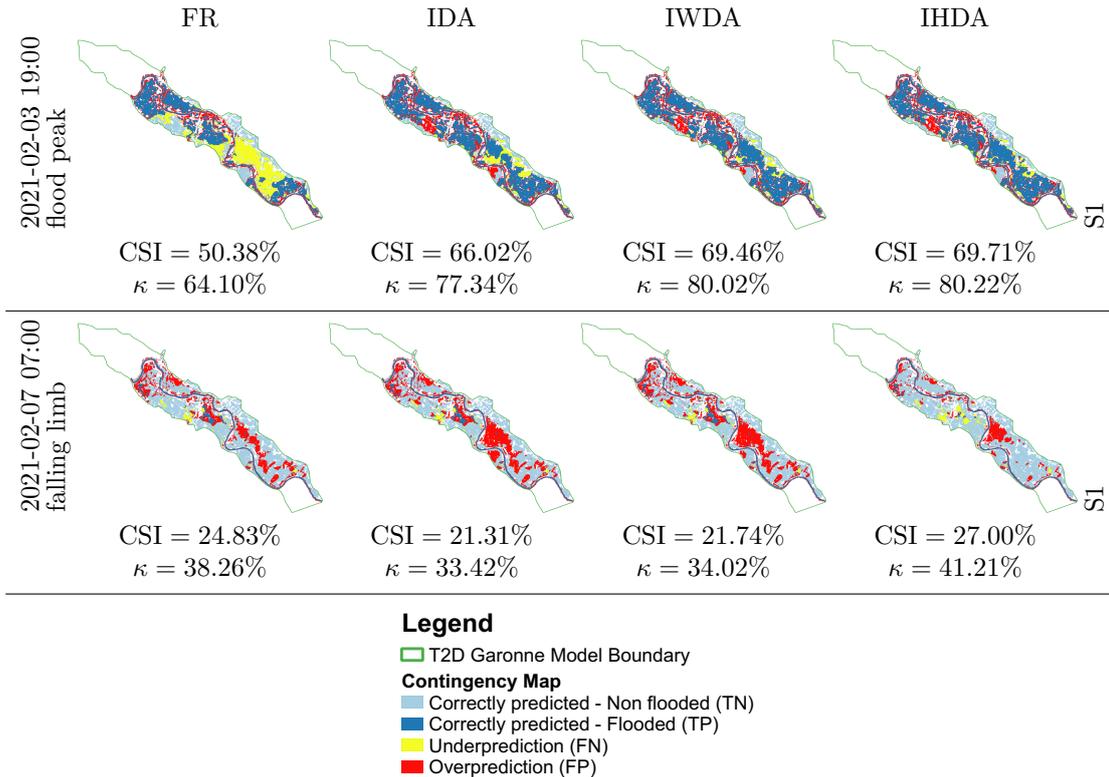


Figure 13: 2021 flood event - Contingency maps computed between simulated flood extent (from left to right: FR, IDA, IWDA and IHDA) with respect to S1-derived flood extent.

741 **5.2.5 Post-event measure validation with HWM observations**

742 Figure 15a and 15b illustrate the validations leveraging the collective public datasets
 743 of HWM for the 2019 and the 2021 flood events. They allow us to evaluate the spatially
 744 distributed observed highest WL at various points on the river banks or within the flood-
 745 plain, as opposed to the remote sensing-derived 2D flood extents that lack WL informa-
 746 tion. However, for the sake of conciseness, only the comparisons between FR and IHDA
 747 experiments are shown. First, since the flood 2019 event is of a smaller scale compared
 748 to the 2021 event, fewer HWM observations were collected. The HWM errors between
 749 the simulated WL and the observed WL are classified into four range, taking ± 1 meter
 750 as a baseline for small errors While an agreement between the errors is not available

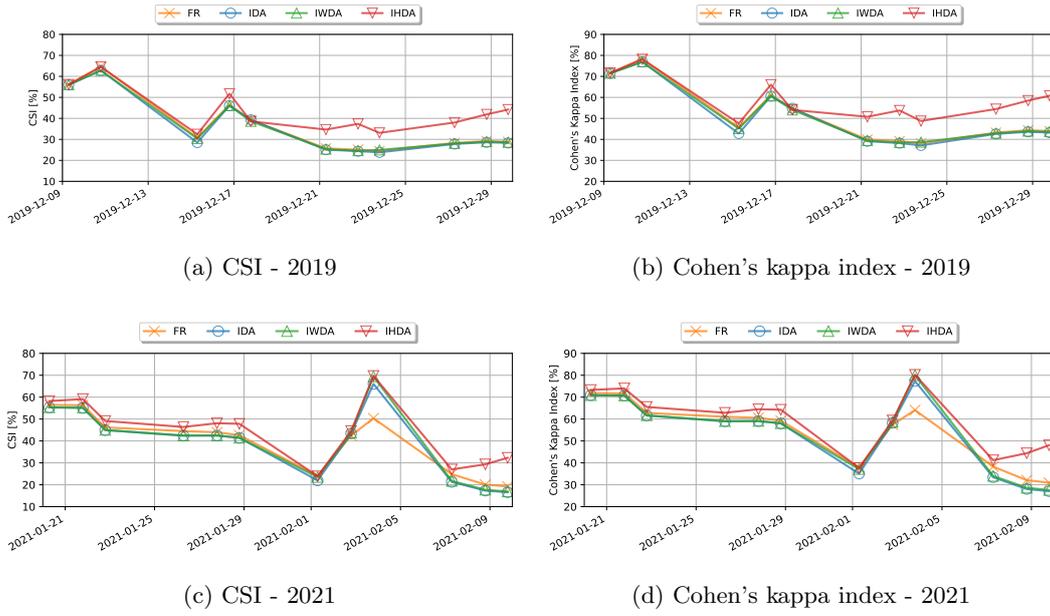
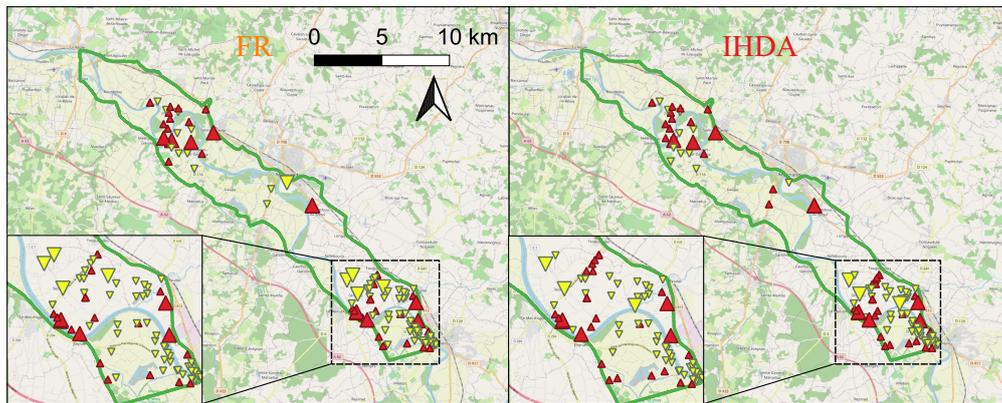


Figure 14: CSI (left column) and κ (right column) index computed for the FR (orange), IDA (blue), IHDA (green), and IWDA (red) experiments with respect to the S1-derived observed flood extent, for the 2019 flood event (top) and 2021 flood event (bottom).

751 in the 2019 flood event, an unanimous improvement by IHDA compared to FR at various
 752 points can be noted, from strong to weak underprediction (visually, from big yellow
 753 triangles to small yellow ones). Similar results are found between IDA, IWDA, and
 754 IHDA. Since this validation only concerns the highest WL after an event, the relevance
 755 of IHDA demonstrated strongly over the flood recess becomes unseen.

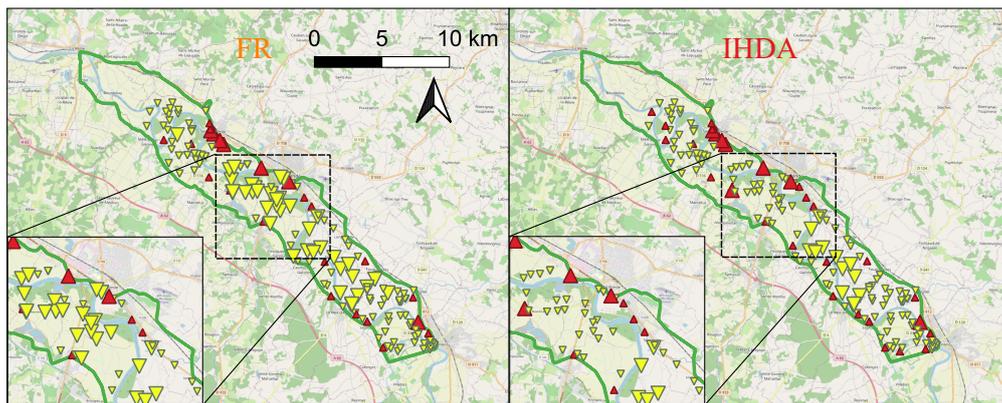


2019 flood event

Legend

- T2D Garonne Model Boundary
- Max Simulated WL - Observed HWM [m]**
- ▲ greater than 1
- ▲ between 0 and 1
- ▼ between -1 and 0
- ▼ less than -1

(a) HWM validation - 2019



2021 flood event

Legend

- T2D Garonne Model Boundary
- Max Simulated WL - Observed HWM [m]**
- ▲ greater than 1
- ▲ between 0 and 1
- ▼ between -1 and 0
- ▼ less than -1

(b) HWM validation - 2021

Figure 15: Post-event HWM validations over the (a) 2019 and (b) 2021 flood events. A negative value indicates an underprediction (yellow triangles) by the simulation whereas a positive value indicates an overprediction (red triangles).

6 Conclusions and Perspectives

This study presents the merits of assimilating 2D flood extent observations derived from remote sensing Sentinel-1 SAR images with an Ensemble Kalman Filter implemented on the 2D hydrodynamics model TELEMAC-2D. The flood extent information is expressed in terms of Wet Surface Ratio computed over defined sensitive subdomains of the floodplain. The WSR is assimilated jointly with in-situ water level observations. The study was carried out over the Garonne Marmandaise catchment, focusing on two flooding events in 2019 and 2021. Four experiments were realized; one in free run mode and three in DA mode. The control vector gathers friction and forcing correction, and is augmented with correction of the hydraulic state in subdomains of the floodplains (IHDA experiment) that constitute the innovative strategy of this work. All of the DA experiments were implemented by a cycled EnKF with an 18-hour assimilation window sliding with 6-hour overlapping. The DA strategy was first assessed in OSSE that mimics the 2021 flood event, then applied in re-analysis mode to both real events. The simulation results were comprehensively assessed with 1D and 2D metrics with respect to assimilated data as well as with respect to independent flood extent, derived from Sentinel-2 optical imagery data or High Water Mark collective public observations when they are available.

The first DA experiment (IDA) involves only in-situ observations whereas the second one (IWDA) assimilates both in-situ observations and WSR observations derived from 2D flood extent maps. These two experiments focus on the sequential correction of friction coefficients and inflow discharge. In OSSE, they demonstrated effectiveness in retrieving the true parameters and providing relevant assessment results. The spotlight of the article is the IHDA experiment, which not only assimilates both types of observations (similar to IWDA), but also handles a dual state-parameter estimation within the EnKF, by treating inflow discharge and friction coefficients as well as the hydraulic state variable in five particular floodplain subdomains, representing evapotranspiration and/or ground infiltration processes that are unavailable in the T2D model.

We have shown that the assimilation of in-situ data in IDA improves the simulation in the river bed, yet, the dynamics in the floodplain remains incorrect with a significant underestimation of the flood (both events). Indeed, the in-situ observations located in the river bed, do not bring information on the dynamics in the floodplain. The assimilation of WSR data in the floodplain, in IWDA, brings additional improvements, that remains limited as the dynamics of the river bed and that of the floodplain are not sensitive to model parameters that are accounted for in the control vector. The correction of the augmented control vector in IHDA allows to better represent the flood peak and to efficiently dry out the floodplain during the recess period. In OSSE mode, IHDA results in simulated WLRs and WSRs that are very close to the synthetic observations, and yields better estimates of true friction and discharge parameters than IDA and IWDA. In real event mode, from FR to IHDA, the RMSE computed with respect to in-situ data in the river bed is reduced by up to 77-80% at Marmande, whereas the CSI computed with respect to remote-sensing flood extent maps is improved by up to 19.33 percentage points for the 2021 flood event (and 5.27 percentage points for the 2019 flood event). This study confirms the assertion that a densification of the observing network, especially in the floodplain, with remote sensing data and advanced DA strategy, allows to improve the representation of the dynamics of the flow in the floodplains.

This work rely on the implementation of an advanced DA strategy for TELEMAC-2D, especially the development of the observation operator dedicated to WSR, as well as the definition of the associated augmented control vector. Yet, it should be noted that the definition of the subdomains in the floodplain over which the hydraulic state is uniformly corrected, requires a deep understanding of the dynamics of the flood, and is thus not straightforward. This aspect could be further investigated, for instance based on a global sensitivity analysis with respect to the hydraulic state but also to other sources of uncertainty such as topography, especially in the downstream area. Indeed, the same

809 dual state-parameter estimation approach could be applied to correct the bathymetry
 810 and topography provided that the size of the uncertainties is reduced, for instance work-
 811 ing with a spatially uniform correction or a correction that is only projected onto a lim-
 812 ited number of principal components of the errors. In this perspective, we aim to con-
 813 sider using high- and very-high-resolution topography as additional inputs to the model.
 814 The use of other imagery datasets (e.g. Landsat-8 and Landsat-9) can also be investi-
 815 gated. In the present work, the combination between remote-sensing data with regards
 816 to S1 and S2 data requires further investigation as it seems that the improvements made
 817 using S1-derived flood extent maps does not necessarily lead to an improvement with
 818 regards to S2-derived flood extents. This could stem from the differences between the
 819 S1 and S2 measurement, and the flood extent mapping algorithm. In addition, the iden-
 820 tification of S1 or S2 exclusion maps should also be considered taking into account the
 821 limitations of each data source. Finally, an major perspective of this work stands in the
 822 potential non-gaussianity of the WSR observations. This limitation can amount to a loss
 823 of optimality of the EnKF which relies on the assumption that the observational error
 824 follows a gaussian distribution. On going work, based on a rich literature based on a change
 825 of variable to transform the non-gaussian error into gaussian errors (widely known as Gaus-
 826 sian anamorphosis) is on going and yield promising early results.

827 **Acronyms**

828	BC Boundary condition
829	CSI Critical Success Index
830	DA Data Assimilation
831	EnKF Ensemble Kalman Filter
832	FloodML Flood Machine Learning
833	FR Free Run
834	HWM High Water Marks
835	IDA In-situ (only) DA Experiment
836	IWDA In-situ and WSR DA experiment
837	IHDA In-situ and WSR DA experiment with extended control vector
838	OSSE Observing System Simulation Experiment
839	PDF Probability Density Function
840	RMSE Root-Mean-Square Error
841	RS Remote Sensing
842	SAR Synthetic Aperture Radar
843	SWE Shallow Water Equations
844	S1 Sentinel-1
845	S2 Sentinel-2
846	T2D TELEMAC-2D
847	WL Water Level
848	WSE Water Surface Elevation
849	WSR Wet Surface Ratio

850 **Acknowledgments**

851 This work was supported in part by the Centre National d'Etudes Spatiales (CNES)
 852 and in part by the Centre Européen de Recherche et de Formation Avancée en Calcul
 853 Scientifique (CERFACS) within the framework of the Space for Climate Observatory (SCO).
 854 The authors gratefully thank the Electricité de France (EDF) for providing the Telemac2D
 855 model on the Garonne Downstream catchment, the SCHAPI, and the Garonne-Tarn-

856 Lot and Gironde-Adour-Dordogne SPCs for providing in-situ data. They also would like
 857 to thank S. El Garroussi and M. De Lozzo for former developments on the Telemac Sys-
 858 tem with API dedicated to data-driven simulations.

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