Long-Term Density Trend in the Mesosphere and Lower Thermosphere from Occultations of the Crab Nebula with X-Ray Astronomy Satellites

Satoru Katsuda¹, Teruaki Enoto², Andrea N Lommen³, Koji Mori⁴, Yuko Motizuki⁵, Motoki Nakajima⁶, Nathaniel C Ruhl³, Kosuke Sato¹, Gunter Stober⁷, Makoto S Tashiro¹, Yukikatsu Terada¹, and Kent S Wood⁸

¹Saitama University
²RIKEN
³Haverford College
⁴University of Miyazaki
⁵RIKEN Nishina Center
⁶Nihon University
⁷University of Bern
⁸Living in Colorado

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Abstract

We present long-term density trends of the Earth's upper atmosphere at altitudes between 71 and 116 km, based on atmospheric occultations of the Crab Nebula observed with X-ray astronomy satellites, ASCA, RXTE, Suzaku, NuSTAR, and Hitomi. The combination of the five satellites provides a time period of 28 yr from 1994 to 2022. To suppress seasonal and latitudinal variations, we concentrate on the data taken in autumn (49 < doy < 111) and spring (235 < doy < 297) in the northern hemisphere with latitudes of 0^* - 40^* . With this constraint, local times are automatically limited either around noon or midnight. We obtain four sets (two seasons × two local times) of density trends at each altitude layer. We take into account variations due to a linear trend and the 11-yr solar cycle using linear regression techniques. Because we do not see significant differences among the four trends, we combine them to provide a single vertical profile of trend slopes. We find a negative density trend of roughly -5%/decade at every altitude. This is in reasonable agreement with inferences from settling rate of the upper atmosphere. In the 100–110 km altitude, we found an exceptionally high density decline of about -12%/decade. This peak may be the first observational evidence for strong cooling due to water vapor and ozone near 110 km, which was first identified in a numerical simulation by Akmaev et al. (2006). Further observations and numerical simulations with suitable input parameters are needed to establish this feature.

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¹Graduate School of Science and Engineering, Saitama University, 255 Shimo-Ohkubo, Sakura, Saitama 338-8570, Japan

²RIKEN Cluster for Pioneering Research, Hirosawa 2-1, Wako 351-0198, Japan
 ³Haverford College, 370 Lancaster Ave., Haverford, PA 19041, USA
 ⁴Department of Applied Physics and Electronic Engineering, University of Miyazaki, 1-1, Gakuen

Kibanadai-nishi, Miyazaki 889-2192, Japan

⁵Institute of Space and Astronautical Science (ISAS), Japan Aerospace Exploration Agency (JAXA),

3-1-1 Yoshinodai, Chuo-ku, Sagamihara, Kanagawa, 252-5210, Japan ⁶RIKEN Nishina Center, Hirosawa 2-1, Wako 351-0198, Japan

⁷School of Dentistry at Matsudo, Nihon University, 2-870-1 Sakaecho-nishi, Matsudo, Chiba 101-8308, Japan

⁸Institute of Applied Physics & Oeschger Center for Climate Change Research, Microwave Physics, University of Bern, Bern, Switzerland ⁹P.O. Box 127, Nathrop, Colorado 81236, USA

Key Points:

- Time series of O+N densities are measured in the MLT, based on atmospheric occultations of the Crab Nebula using X-ray astronomy satellites.
- The density is decreasing everywhere, with a local minimum of -12%/decade near 105 km.
- The local minimum in density trends may be due to strong cooling by water vapor and ozone, as was first predicted by Akmaev et al. (2006).

Corresponding author: Satoru Katsuda, katsuda@mail.saitama-u.ac.jp

Abstract

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1 Introduction

Understanding the changes of the middle and upper atmosphere is important to our life, as was illustrated by the discovery of the stratospheric ozone depletion. The importance is increasing, as we utilize the space environment for many purposes such as telecommunications, navigation, space tourism, and scientific projects to explore the universe. There are several known drivers of middle and upper atmosphere climate change, including the increase in greenhouse gas (mainly, water vapour and carbon dioxide) concentrations, changes in ozone concentration, long-term solar and geomagnetic activity variations, and shifts in Earth's main magnetic field. Of these, the dominant cause of long-term trends in the upper atmosphere in recent decades is thought to be the increase of greenhouse gases (e.g., Akmaev et al., 2006; Qian et al., 2013; Cnossen, 2020).

The roles of greenhouse gases in the atmosphere are (1) heating the atmosphere in the troposphere (near surface) and (2) cooling the middle atmosphere above $\sim 20 \,\mathrm{km}$ altitude, which was first shown by computer simulations by Manabe and Wetherald (1967). Roble and Dickinson (1989) performed pioneering numerical simulations focusing on the middle and upper atmosphere above 60 km, followed by many researchers in both numerical simulations and observations (Laštovička, 2017; Danilov & Konstantinova, 2020, for recent reviews). Greenhouse gases, particularly CO_2 , cool the middle atmosphere, because the density in the middle atmosphere is so low that CO_2 molecules are optically thin to outgoing infrared radiation. In this condition, thermal energy transferred by collisions with ambient gas to the excited states of CO_2 is lost to space via its infrared radiation (e.g., Goessling & Bathiany, 2016, for a deeper understanding of CO₂-induced cooling). The combination of lower atmosphere heating and middle atmosphere cooling is demonstrated on Venus, whose atmospheric composition is dominated by CO₂. The "greenhouse cooling" in the middle atmosphere results in contraction of the middle atmosphere, leading to a downward displacement of constant pressure surfaces. Combined with the exponential density decrease with increasing altitude, a density at a fixed height decreases with time. The fact that stronger long-term trends have been predicted and confirmed in the middle atmosphere rather than the troposphere makes studies of the mesosphere and lower thermosphere (MLT) important in predicting climate changes.

The density trends in the thermosphere ($\sim 300 \text{ km}$ altitude and above) have been extensively studied from satellites' orbit drag. Various researchers came to the conclu-

sion that the density trend at ~400 km is negative at about a few %/decade with a possible solar-cycle dependence, ranging from -5%/decade for solar minimum conditions to -2%/decade for maximum conditions (e.g., Emmert et al., 2008, and references therein). This trend is in reasonable agreement with the state-of-the-art numerical simulations (e.g., Solomon et al., 2015; Cnossen, 2020).

The trend study in the MLT (80–110 km altitude) is also of great importance, especially because volume mixing ratio (VMR) of CO_2 rapidly falls off in this region due to molecular diffusive separation (as CO_2 is heavier than the mean molecular weight of the air) and photolysis. According to Whole Atmosphere Community Climate Model (WACCM) simulations (e.g., López-Puertas et al., 2017), the CO_2 VMR decreases from 380 ppmv below 80 km to 120 ppmv at 110 km altitude. Observationally, the CO_2 VMR is relatively difficult to be quantified in this region (Laštovička & Jelínek, 2019, for a review of observations). The most recent measurements are consistent with the model at the bottom of the MLT, but depart from the model with increasing altitude in the sense that the model underestimates the data (e.g., Garcia et al., 2016), posing challenges to our current understanding of dynamics, energetics, and photolysis in the MLT region. The long-term trend of the air density in the MLT region can be a new indicator of the trend of the CO_2 VMR trend.

Despite its importance, measurements of density trends in the MLT region are still scarce due to difficulty in in-situ observations. Snap-shot measurements were performed from solar/stellar occultations (e.g., Norton & Warnock, 1968; Determan et al., 2007) as well as in-situ measurements based on the falling sphere technique (e.g., Strelnikov et al., 2013, and references therein). Although these data provided precious opportunities to verify density models, they are not sufficient to explore long-term trends. There is only one indirect measurement of the long-term density trends in the MLT. This is based on meteor radar-echo observations which measure meteor peak flux altitudes and convert them to neutral air densities. The neutral density trend inferred by this method was $-5.8\pm1.1\%$ /decade at 91 km altitude (Stober et al., 2014). Because this is obtained at a single altitude, our knowledge of the long-term trend in the MLT region is obviously poor.

Here, we present the first direct measurements of long-term neutral density variations in the MLT (altitudes between 71 and 116 km), utilizing atmospheric occultations of the Crab Nebula observed with X-ray astronomy satellites. A pioneering work on Xray occultation sounding of the upper atmosphere was performed by Determan et al. (2007) who analyzed Earth's atmospheric occultations of the Crab Nebula obtained with the RXTE satellite. Historically, this paper was produced as a by-product of X-ray satellite navigation experiments; if the navigational state vector for the satellite is known with precision, then the horizon crossings can be used to extract diagnostic information about the state of the atmosphere. The history of the dual usage of X-ray horizon crossing transitions is summarized in Wood et al. (2020). Recently, Katsuda et al. (2021), hereafter Paper I, and Yu et al. (2022b, 2022a) applied the same technique to derive atmospheric vertical density profiles, using Japanese and Chinese X-ray astronomy satellites, respectively. In this paper, we analyze atmospheric occultation data of the Crab Nebula acquired with X-ray astronomy satellites, ASCA, RXTE, Suzaku, NuSTAR, and Hitomi to reveal long-term trend of the neutral density in the MLT region. The data were obtained between 1994 and 2022, providing a time span of 28 yr. This is longer than two solar cycles, enabling us to remove/suppress the possible influence of the 11-year solar cycle. This paper is organized as follows. In Section 2, we describe observations analyzed in this paper. In Section 3, we describe data analysis and results. In Section 4, we interpret the analysis results. Finally, we give conclusions of this paper in Section 5.

2 Observations and Data Reduction

We analyze X-ray data during Earth occultations of the Crab Nebula, which is a remnant of a supernova explosion occurred in 1054 AD, to obtain vertical density profiles of the MLT region. The essential requirements for the celestial source used for this technique are (1) that the source be either constant or not varying significantly during the time required for the atmospheric occultation (a minute or so) and (2) that it should be a point source or sufficiently point-like that the angular extent does not matter. It is known that the Crab Nebula is not a perfect standard candle (Wilson-Hodge et al., 2011). However, its degree of variability is not so rapid as to change the shapes of individual occultations, or affect the analysis. It is also well established that the Crab Nebula also has an angular extent of about an arcminute in X-rays around 1 keV and then decreases in angular extent with increasing X-ray energy. Given that the distance between the satellite and the tangent point is roughly 2000 km, this angular extent corresponds to a tangent altitude of ~ 0.6 km. This is comparable with the error due to the satellite position uncertainty from TLE+SGP4, as we will quantify later in this section. One could worry from these rough estimates that the angular size of the Crab Nebula, which is slightly asymmetric, should be in the error analysis, because it might be of the same order as the satellite position error. However, while there is potential for the total angular extent to be a problem, the flux is concentrated toward the center of the Nebula and the pulsar contributes as a point source near the centroid of the Nebular emission. Thus, it is reasonable to consider the Crab Nebula as effectively a point source.

Basic information about the X-ray occultation technique can be found in Paper I. Because most (if not all) X-ray astronomy satellites so far have used the Crab Nebula to perform their calibrations, there are numerous data sets for this standard candle on orbits. Here, we make use of them to reveal long-term trends of the air density. Specifically, we use data acquired with the X-ray astronomy satellites/instruments, ASCA/GIS (Tanaka et al., 1994; Ohashi et al., 1996), RXTE/PCA (Jahoda et al., 1996), Suzaku/XIS+PIN (Mitsuda et al., 2007; Koyama et al., 2007; Takahashi et al., 2007), NuSTAR/FPM (Harrison et al., 2013), and Hitomi/HXI (Takahashi et al., 2018; Nakazawa et al., 2018).

To remove possible seasonal biases, we concentrate on spring (± 30 days around the spring equinox) and autumn (± 30 days around the autumnal equinox), and analyze the two seasons separately. In fact, ASCA, Suzaku, and Hitomi observed the Crab Nebula only in these two seasons, whereas RXTE and NuSTAR observed it during the whole year. Given that the five X-ray satellites used in this paper are in the low Earth orbits with low inclination angles, and that the declination angle of the Crab Nebula is $+22^{\circ}$ above the celestial equator, the majority of the data are obtained in the northern hemisphere. To eliminate/suppress possible latitudinal dependences of atmospheric density, we analyze data obtained only in the northern hemisphere. Consequently, all the data are acquired in a latitude range between 0° and 40° in the northern hemisphere. It would be ideal to divide the data even more finely by latitude. However, the limited number of data does not allow us to do so.

In Table A1, we summarize basic information about all the data analyzed in this paper. The individual setting (or rising) occultations in the same observation sequences are combined together to improve the photon statistics. This merging process is reasonable, because these data are taken at the similar telescope tangent points (latitude and longitude) and local times with each other. The merged occultations are labeled with the same group number as shown in the last column of the table. We note that the photon statistics in the RXTE data are so rich that they need not be combined. From this table and Fig. 1, which illustrates local time vs. day of year for all the occultation scans analyzed, we can see that local times are approximately either midnight or noon for all of our data sets. Therefore, by analyzing the noon and midnight data separately, density variations caused by tidal waves with periods of 24 hr plus harmonics are removed naturally.

In Paper I, we did not use the satellite positions provided by the Suzaku and Hitomi housekeeping files, but rather recalculated their positions by using the two-line elements (TLEs) to improve accuracies of their positions and consequently tangent altitudes. In the mean time, we realized that the original positions provided by JAXA, which we received after publishing Paper I, are actually more accurate than the TLE data and are used in this paper. Suzaku's position accuracy is not available, but is a few hundred m, given that it is determined by radio ranging. This is an order of magnitude better than that for the TLE data, which will be evaluated later in this section. Because Hitomi carries a GPS receiver, its position accuracy is less than 1 m. The accuracy in the position of the RXTE satellite is less than \sim 450 m with 99% confidence (Jahoda et al., 2006). Such accurate positions are recorded every 60 sec. Unfortunately, this time resolution is insufficient for our analysis. Therefore, we interpolate the satellite positions by using a cubic spline interpolation method. The accuracy of the interpolated position becomes worse than the original precision, but is less than a few 100 m, which is sufficient for our following analysis.

As for ASCA and NuSTAR, no accurate satellite positions (with reasonable time intervals for ASCA) are available. Therefore, we calculate their positions based on TLE sets with the Simplified General Perturbations Satellite Orbit Model 4 (SGP4), using the skyfield software written in python. The uncertainty on the TLE-based satellite positions are estimated for the RXTE satellite by comparing the TLE-based positions and high precision orbit data provided by the RXTE team. For this comparison, we do not perform the cubic interpolation but use original data with a cadence of 60 sec to keep the original high precision. To increase the number of samples, we collect all occultation data of the Crab Nebula without constraints of the season and the latitude. As a result, we obtained a total of 140 occultations, most of which are not listed in Table A1. For each occultation, we calculate position differences between TLE and high-precision orbits for about 10 data points (~10 minutes) including the atmospheric occultation, and calculate their averages. The difference is calculated in altitude, latitude, and longitude directions, separately.

Figure 2 shows a cumulative fraction of the position differences in three directions, from which we derive the position uncertainties on the TLE as shown in Table 1. The fact that errors in the longitudinal direction are much large than than those in the other directions is reasonable, because TLEs tend to have larger errors in the in-track direction (Wang et al., 2009), which is close to the longitudinal direction for the RXTE with inclination angle of only 23°. In fact, the orbit errors associated with TLE+SGP4 measured for the CHAMP satellite (Xu & Xiong, 2018) are close to our measurement for the RXTE satellite. Thus, the errors in Table 1 seem typical for TLE-based positions for low-Earth-orbit satellites. In the next section, we will evaluate the impact of the spacecraft's position error to the measurement error on the air density.

3 Analysis and Results

We plot in Fig. 3 example occultation light curves taken with each of the six instruments used in this paper. The gradual increase/decrease of the X-ray intensity along with the tangent altitude clearly shows the effect of atmospheric absorption. Also, the characteristic rising/setting altitudes significantly vary from instrument to instrument. This is due to the different energy coverage of each instrument, as shown in Fig. 4 showing the effective area comparison for the six instruments. The higher the energy coverage of the instrument, the deeper the characteristic altitude. The altitude range to be analyzed for our spectral analysis is within dotted vertical lines in each panel, which is slightly different from instrument to instrument.

We derive vertical atmospheric density profiles for each data group defined in Table A1, following the same procedure as Paper I, with some modifications and improvements as described below. We extract X-ray spectra from an altitude layer between 71 km and 116 km, with a resolution of 6 km for each occultation data group. Every 6-km layer is overlapped with adjacent layers by half to provide an effective altitude resolution of 3 km. An exception is Suzaku/XIS for which the data were obtained in a special model, i.e., an exposure time of 0.1 sec with a cadence of 8 sec. As Suzaku moves in orbit, the tangent altitude increases/decreases at a speed of $\sim 2 \text{ km/sec}$ near a tangent altitude of 100 km. Thus, the altitude bin of the XIS data corresponds to $\sim 0.2 \text{ km}$ and the data are taken every $\sim 16 \text{ km}$ altitude. This is too sparse for binning by 6 km. On the other hand, thanks to the high throughput of the combined three co-aligned XISs, the exposure time of 0.1 sec (or 0.2 km altitude resolution) is sufficient for us to perform spectral analysis. Thus, we analyze the XIS spectra without binning.

Before measuring the atmospheric density, we fit unattenuated spectra from the Crab Nebula, i.e., the source spectrum at the top of the Earth's atmosphere, for each occultation data group. Then, we evaluate lower-altitude X-ray spectra with this spectral model, by taking into account the effect of the atmospheric absorption. The model is basically the same as in Paper I, but to be more appropriate, we add another absorption component, i.e., **cabs** in the XSPEC software (Arnaud, 1996), which takes into account the Compton scattering that could play an important role in the hard X-ray regime; a total photon cross section in carbon is dominated by the Compton scattering process in the photon energy range of $0.05-10 \, \text{MeV}$ (Hubbell et al., 1980). Therefore, our model is expressed as **vphabs** × **cabs** × TBabs × powerlaw, where **vphabs** and TBabs represent the photo-electric absorptions due to the Earth's atmosphere and the interstellar medium, respectively, and powerlaw is the intrinsic X-ray emission from the Crab Nebula.

We perform deadtime corrections for ASCA/GIS, Suzaku/PIN, and NuSTAR/FPM, for which deadtime fractions for the Crab Nebula exceed 10% at the top of the atmosphere. To calculate deadtime fractions, we utilize hxddtcor for Suzaku/PIN. As for the ASCA/GIS and NuSTAR/FPM, we calculated deadtime fractions from the detected count rates by using Fig. 18 (specifically, the theoretical prediction for FLF SP-ON) in Makishima et al. (1996) for ASCA/GIS or Fig. 2.7 in Bhalerao (2012) for NuSTAR/FPM, respectively.

We assume that the atmosphere consists purely of N, O, and Ar, as we did in Paper I. Their relative abundances are fixed to model values from NRLMSIS 2.0 (Emmert et al., 2021) for which we input typical parameters, i.e., noon on 2000-09-15, solar radio flux F10.7 = 100 solar flux unit (SFU, 1 SFU = 10^{-22} W m⁻² Hz⁻¹), geomagnetic index Ap = 5. The cabs component has a single parameter, i.e., the hydrogen column density, assuming that $N_{\rm H} \times 1.21 = N_{\rm e}$ expected for the solar abundance. This is usually good for cosmic plasmas but is not realistic for the air. To adapt cabs for the air composition, we compute the total number of protons in the air, i.e., $\Sigma Z_{\rm i} N_{\rm i}$ with i representing elements N, O, and Ar, Z being the atomic number, N being the column density. Then, we take it as an equivalent hydrogen column density for the input of the cabs model. In this calculation, we utilize the abundances of N, O, and Ar obtained from the vphabs component, so that the vphabs model becomes consistent with the cabs model.

All the spectra are well reproduced with this model. Figure 5 shows example spectra with the best-fit models for each of the six instruments. The only free parameter in this fitting procedure is the N column density in the atmospheric absorption component **vphabs**. The best-fit N column density and the assumed N/O ratio allow us to calculate a total N+O (molecules and atoms are combined) column density at each altitude layer.

We evaluate the uncertainties on the N(+O) column density caused by the TLE errors estimated in the previous section. To this end, we reanalyze the six occultations in Obs.ID 70018 obtained with RXTE. We artificially shift the satellite position by ± 1 -

 σ in three directions, based on Table 1. From the shifted satellite positions, we recalculate tangent altitudes for each occultation, and remeasure the vertical N+O column density. Thus-derived column density ratios between $+1\sigma$ and -1σ shifts are summarized in Table 2. The total uncertainties in the three directions amount to $\pm 6\%$, which are dominated by longitudinal errors as expected from the TLE errors in Table 1.

The O/N relative abundance in the air is known to vary with season, latitude, and geomagnetic activity (e.g., Meier et al., 2015). According to the NRLMSIS 2.0 model, the variation is as large as $\pm 10\%$ at 120 km altitude, and is almost negligible below 100 km. To check the maximum effect on the O/N variation, we artificially modify the O/N ratios by $\pm 10\%$, and perform the spectral fitting. As a result, the combined N+O column density in the air vary by only $\pm 1\%$. This is smaller than typical statistical uncertainties. We note that there is also a possibility of a long-term negative trend in the O/N₂ ratio (Pokhunkov et al., 2009). However, it is currently insignificant, and thus we do not consider the effect of long-term variability in this paper. In any case, the error caused by the incorrect N/O ratio should be smaller than statistical uncertainties, because the magnitude of possible long-term variation is comparable with the short-term variation.

We calculate the local number density at the tangent point by inverting the Abel integral equation (the column density) as we did in Paper I. As a result, we obtain vertical density profiles as a function of geometric altitude. In this inversion process, we arrange the irregular altitude binning for Suzaku/XIS, ~0.2-km bin every ~16 km, to become uniform 6-km bins. Then, we generate time series of the N+O density in the time period of 1994–2022 at each altitude. Figure 6 shows combined N+O density trends at each of altitude layers, where we concentrate on the data taken during Autumn-midnight. Note that the temporal coverages by the data are not exactly the same among the plots. This is partly because the sensitive altitudes are different from instrument to instrument (i.e., ASCA/GSI: 83–116 km; NuSTAR/FPM: 71–116 km; Suzaku/XIS: 101–116 km; Suzaku/PIN: 71–95 km; NuSTAR/FPM: 71–116 km; Hitomi/HXI: 71–116 km as shown in Fig. 3), and partly because we discard unreliable data with statistical errors of >20% as they do not help constrain long-term trends.

We then determine long-term trends and solar responses at all altitude layers, by using a multiple linear regression (MLR) model to the N+O density time series. Because we focus on two months around spring and autumn equinoxes, our data are inevitably de-seasonalized if we perform the MLR fitting for the two seasons separately. The effects of tidal waves (diurnal variations) can be also suppressed by analyzing the data taken around noon and midnight, separately (see Fig. 1 and Table A1). Thus, we have four time series of the air density at each altitude. The MLR model is expressed as:

 $n_{\rm MLR}(t) = a + b \times t + c \times F10.7(t),$

where $n_{\text{MLR}}(t)$ is the N+O density, t is the time (year) when the data were taken, and F10.7(t) is the solar radio flux which is daily averaged at each occultation date; the solar flux data are taken from https://lasp.colorado.edu/lisird/data/noaa_radio_flux and https://www.spaceweather.gc.ca/forecast-prevision/solar-solaire/solarflux/sx-5-en.php for old and recent data, respectively. The bottom panel in Fig. 6 shows the solar radio (10.7 cm) flux in solar flux unit (SFU). The constant a, long-term trend b, and the amplitude to the solar response c are obtained through least square fitting.

The best-fit long-term trends are summarized in Table 3, and some of the best-fit models are shown as the solid lines in Fig. 6. We note that some time series are too sparse (number of data points < 4) to derive robust/unbiased trends from the MLR fitting, for which we assign "not available (N.A.)". The density trends obtained are generally negative, which is at least qualitatively consistent with past observations (Stober et al., 2014; Bailey et al., 2021) and numerical simulations (Akmaev et al., 2006; Solomon et al., 2019). There are no obvious differences among the different seasons and local times. Therefore, we calculated error-weighted means at all altitude layers. Figure 7 left and right show

the mean values of the density trends and solar response terms, respectively. The longterm trend is about -5%/decade throughout the altitudes investigated, except for ~ 105 km altitude where the trend shows a local minimum of -12%/decade. On the other hand, the solar response term is positive everywhere at about 5%/100 SFU. The positive response to F10.7 is consistent with past observations of the temperature trends in the MLT (e.g., Zhang et al., 2016; Bailey et al., 2021).

To check the fitting quality, we calculate χ^2 values. In this process, we add TLEinduced 1- σ errors on the N+O density, i.e., $\pm 6\%$ as shown in Table 2. Because the TLEbased satellite's positions are used only for ASCA and NuSTAR, we introduce this error only for data taken with the two satellites. Table 4 lists the reduced χ^2 values, from which we can see that the fit quality is mostly satisfactory.

However, there are several poor quality fits, too. They might be improved by introducing additional terms in the MLR model. In fact, Laštovička (2017) summarized several possible drivers of long-term trends in addition to the greenhouse gases. These include secular changes in the geomagnetic activity (Ap) as well as dynamical variations such as Quasi-Biennial Oscillation (QBO), El Nino Southern Oscillation (ENSO), and Arctic Oscillation (AO). In addition, long-term trends in the atmospheric circulation and wave activity may be also important (Wilhelm et al., 2019). Although their effects are not well known, Bailey et al. (2021) tried to incorporate those effects by introducing interhemispheric and intra-hemispheric indices calculated from temperature data provided by the National Center for Environmental Prediction/National Center for Atmospheric Research.

Therefore, we perform the MLR fitting by introducing additional terms of Ap (https://www.gfz-potsdam.eQBO (https://iridl.ldeo.columbia.edu/SOURCES/.Indices/.QBO/.QBO_realtime/), ENSO (https://psl.noaa.gov/enso/mei/), AO (https://www.daculaweather.com/4_ao_index.php), inter-hemispheric, and intra-hemispheric coupling indices. We take the inter- and intrahemispheric coupling indices from Bailey et al. (2021). To see their individual contributions, we perform the MLR fitting by adding each of Ap, QBO, ENSO, AO, and a combination of inter- and intra-hemispheric terms to the original model, i.e., linear and solar response terms. We realized that none of these additional parameters improve the fit quality. In some cases, the reduced- χ^2 becomes even worse due to the increased number of free parameters. Moreover, we check that the long-term trends and the magnitudes of the solar response remain consistent within the errors before and after introducing the additional terms, which assures the robustness of the result shown in Fig. 7. Thus, we conclude that the additional indices do not play an important in controlling the long-term variation of the neutral density in the MLT region.

There are several possibilities to explain the bad fits. One obvious cause is insufficient knowledge of atmospheric wave activities. For example, anomalous short-period gravity waves originating from the lower atmosphere could easily produce outliers in the density time series (e.g., Sato et al., 2018; Yasui et al., 2018). In addition, short-term variations owing to planetary waves, which are often removed by averaging a number of data in a month or two, are difficult to be suppressed in our sparse data sets; we have only a few data groups in one season. In particular, the semidiurnal tide shows a clear solar cycle dependence (Wilhelm et al., 2019). Another possibility associated with planetary waves is a stratospheric sudden warming (SSW), which is a sudden temperature increase by more than a few dozen degrees near north pole, caused by a rapid amplification of planetary waves propagating upward from the troposphere (e.g., Matsuno, 1971; Tomikawa et al., 2012). SSW signatures are very small for the latitude band considered here, because it is a primarily polar phenomenon. However, we may not fully rule out the possibility that our data are affected by SSWs. Given that SSWs occur typically in late December to January and early February, we searched for signatures in our data taken in spring. After all, we found no significant density differences between SSW and non-SSW springs, suggesting that SSWs do not play important roles in our data. Finally, we

note that the TLE error is another source that could produce outliers for ASCA and NuS-TAR.

4 Discussion

We obtained long-term trends of total number densities of N and O (both atoms and molecules are combined) in the MLT region, based on atmospheric occultations of the Crab Nebula observed with X-ray astronomy satellites, ASCA, RXTE, Suzaku, NuS-TAR, and Hitomi. In this section, we compare our results with past observations and numerical simulations.

As we described above, direct density measurements in the MLT region, in particular long-term trends in density, is scarce. As far as we know, the only long-term density trend has been measured for electron densities, which have been measured with sounding rockets for more than 80 years, providing us with long-term trends (e.g., Friedrich et al., 2017). In general, an increase in the electron density of the order of $\sim 1\%/yr$ was found in the MLT region. This, combined with the vertical increase upward in the electron density, suggests a downward shifts of the electron density profile. This is qualitatively consistent with the atmospheric contraction/descent due to the greenhouse cooling. However, quantitative evaluation of the trend in total density has not yet been obtained.

Except for the electron density, density trends in the MLT region have been inferred from measurements of atmospheric falling from a variety of methods. These include (1) the height of the E-layer's peak electron density (e.g., Bremer, 2008), (2) the mesopause height, i.e., the height at the local temperature minimum (e.g., Yuan et al., 2019), (3) the centroid height of the Na layer (e.g., Clemesha et al., 1997), (4) the meteor peak flux altitude (e.g., Stober et al., 2014), (5) the ionospheric reflection height in the low-frequency (LF) range (e.g., Peters & Entzian, 2015; Peters et al., 2017), (6) the pressure altitude measured by atmospheric occultations and Earth's limb emission (e.g., Bailey et al., 2021). In addition, there are other indirect observables to estimate the atmospheric falling, including the height of the turbopause (Pokhunkov et al., 2009; Hall et al., 2016) and the height of noctilucent clouds, also known as polar mesospheric clouds (e.g., Fiedler et al., 2017; Lübken et al., 2021). In this paper, we do not discuss them, because the turbopause heights are known to be problematic as discussed in Laštovička (2015, 2017) and the altitudes of noctilucent clouds depend not only on the density profile but also strongly depend on the temperature and the water vapor concentration in the atmosphere. Furthermore, there is evidence that space traffic has a strong influence on the interannual variability of the bright noctilucent clouds (Stevens et al., 2022).

The air density corresponds one-to-one to the altitude, given the locally hydrostatic balanced relationship: $d\rho \propto -\rho \, dh$. Therefore, we can convert the altitude to the density by using some atmospheric models. Consequently, we can convert the speed of atmospheric vertical shifts to the rate of density change. According to the NRLMSIS 2.0 model (Emmert et al., 2021), the air density decreases with increasing altitude at a rate of $16\pm1\%/\text{km}$ in the MLT region. To check possible systematic uncertainties on density models, we also examined another empirical atmospheric density model, Jacchia-Bowman 2008 (Bowman et al., 2008). This model gives a density gradient of ~17%/km at 90 km altitude, which is consistent with the NRLMSIS 2.0 model. Thus, we multiply an altitude trend by a value of $16\pm1\%/\text{km}$ to derive a density trend. The result is summarized in Table 5 and Fig. 6. We note that Stober et al. (2014) showed the density trend inferred from the meteor peak flux altitude, but did not explicitly give the altitude trend. Therefore, we calculated the altitude trend based on Fig. 4 in Stober et al. (2014), by performing the same MLR analysis as we did in the previous section. We can see that our measurements are generally consistent with past observations at every altitude. It should be noted, however, that our trend slopes in density are systematically steeper (albeit within error bars) than those inferred from past observations. Resolving this issue is beyond the scope of this paper, but one problem is that our conversion process from altitude trends to density trends for past observations may be too simple. We also note that the vertical trend profile exhibits a local minimum at ~ 105 km, with a decline rate of -12%/decade. In fact, past observations show the largest (negative maximum) trend near 100 km, which is at least qualitatively consistent with our measurement. Unfortunately, past observations do not cover the altitude range of 100-110 km. Therefore, revealing the density trend in this altitude range is left as an important future work.

As shown in Fig. 7 left, our results are also in reasonable agreement with the stateof-the-art numerical simulations using WACCMeXtended, in which trends are calculated from 5-year simulations for the years 1972–1976 and 2001–2005, which serves as a small ensemble of similar years and are averaged over each of the two ensembles (Solomon et al., 2019). This model takes into account all key trace constituents, i.e., CO_2 , CH_4 (a precursor of H_2O), H_2O , and O_3 . The model was computed for the solar maximum and minimum conditions, the results of which are illustrated in Fig. 7 left as the solid and dashed lines, respectively. We can see that the difference between the solar minimum and maximum conditions are small in the region of interest. It is interesting to note that numerical experiments exhibit a local maximum of a density decline just above 100 km (the local minimum is more evident in the original figure, Fig. 3 in Solomon et al. (2019), showing a wider altitude range). Akmaev et al. (2006) first pointed out that this peak is created by the effects of H₂O and O₃; the cooling effect on the density accumulates with altitude up to $\sim 110 \,\mathrm{km}$ where in situ H₂O and O₃ forcings disappear. The density trend obtained in this work shows a local (negative) maximum near 105 km altitude. This seems to be the first observational evidence for the local maximum in the density decline due to H_2O and O_3 .

There is about 20 yr time difference between the simulations by Solomon et al. (2019) and our data sets, which is subject to possible systematic errors, because temporal variations of greenhouse gas concentrations vary from period to period. The simulations took the increasing rates of CO₂, CH₄, and chlorofluorocarbon (sensitive to O₃) to be +4.5%/decade, +6.3%/decade, and +30%/decade, respectively. In the middle and upper stratosphere, H₂O is mainly formed by CH₄ oxidation process. According to Qian et al. (2013), the 6.3% increase in CH₄ concentration results in an increase of 2%/decade in H₂O concentration in the upper atmosphere. This H₂O increase seems to be incorporated in the simulations by Solomon et al. (2019), although it is difficult to evaluate the H₂O increasing rate quantitatively from their paper alone.

Realistic trends of greenhouse gases in the time period of our data (1994–2022) would be different from the values assumed in the simulations by Solomon et al. (2019). In particular, the O₃ trend changed from negative (ozone depletion) to none or positive around 1990 as a consequence of the Montreal protocol in 1987. Because O₃ is a strong absorber of the solar ultra-violet radiation, the temperature (and density) response to O₃ increase is opposite to that of the other major greenhouse gases. The O₃ increase has a heating effect on the MLT region via reduced solar heating, which was demonstrated by numerical simulations by Lübken et al. (2013). Given that O₃ is increasing in the recent three decades (Maillard Barras et al., 2020; Bernhard & Stierle, 2020), O₃ should work to expand the middle and upper atmosphere during the time period of our data sets. Therefore, a proper incorporation of the effect of O₃ in the numerical simulations would make the trend slope in density larger (closer to zero) to some extent.

As for the increasing rate of H₂O concentration, recent measurements of water vapor with the Sounding of the Atmosphere using Broadband Emission Radiometry (SABER) and the Aura Microwave Limb Sounder found a global increase of $3\pm1.5\%$ /decade near 80 km altitude (Yue et al., 2019). This is the same level as that assumed in the simulations (likely 2%/decade). Therefore, the simulation is realistic from the point of view of the H₂O concentration.

The CO₂ concentration in the upper atmosphere has been debated (Laštovička & Jelínek, 2019, for a review). However, the most recent result by Rezac et al. (2018) who re-analyzed SABER data between 2002 and 2016 came to a conclusion that CO₂ density trends below 90 km are consistent with the tropospheric value of 5.5%/decade, whereas above 90 km the trend becomes higher, reaching a maximum value of 8.2%/decade at ~105 km altitude for bimonthly time bins (or 10%/decade for monthly time bins). This is consistent with earlier results obtained from the solar occultation data with the Atmospheric Chemistry Experiment Fourier Transform Spectrometer (Emmert et al., 2012). In this context, it seems that the most reliable trend in the MLT is twice larger than the value used in the simulations by Solomon et al. (2019).

In this way, all of these input parameters including CO_2 , CH_4 , H_2O , and O_3 concentrations must be updated to be consistent with the observational data. Because the density response to the increasing greenhouse gases is nonlinear, it is necessary to perform numerical simulations, which use physical parameters that are consistent with observational data.

5 Conclusions

We obtained long-term density trends in the last 28 yr (1994–2022) of the Earth's upper atmosphere at geometric altitudes between 71 and 116 km with a resolution of 3 km, based on atmospheric occultations of the Crab Nebula observed with X-ray astronomy satellites, ASCA, RXTE, Suzaku, NuSTAR, and Hitomi. The data taken in different seasons (spring and autumn) and different local times (noon and midnight) are combined to provide a single vertical profile of trend slopes. The density trends are overall negative at roughly -5%/decade. This is roughly consistent with inferences from past measurements of the rates of settling atmosphere in the MLT region. In the 100-110 km altitude, we found an exceptionally high density decline of about -12%/decade. We believe that this peak is the first observational evidence for strong cooling due to water vapor and ozone near 110 km, which was first identified in a numerical simulation by Akmaev et al. (2006). However, this feature needs to be verified by further observations as well as numerical simulations, which use physical parameters that correspond to the time periods of observations.

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Direction	1- σ C.L. (km)	90 % C.L. (km)
Longitude	± 1.1	± 1.4
Latitude	± 0.22	± 0.35
Altitude	± 0.13	± 0.21

Table 1.TLE errors for the RXTE satellite

Table 2. N+O column density errors caused by 1- σ TLE errors

Data group	Ratio	Total difference		
	Longitude	Latitude	Altitude	
	$\frac{N_{\rm N+O}({\rm Sat.pos.}-1.1{\rm km})}{N_{\rm N+O}({\rm Sat.pos.}+1.1{\rm km})}$	$\frac{N_{\rm N+O}({\rm Sat.pos.}-0.17{\rm km})}{N_{\rm N+O}({\rm Sat.pos.}+0.17{\rm km})}$	$\frac{N_{\rm N+O}({\rm Sat.pos.}-0.1\rm km)}{N_{\rm N+O}({\rm Sat.pos.}+0.1\rm km)}$	
7	1.12	0.98	0.96	$\pm 6\%$
8	1.13	0.99	0.96	$\pm 7\%$
9	1.11	0.99	0.96	$\pm 6\%$
10	0.89	0.99	0.97	$\pm 6\%$
11	0.89	0.99	0.96	$\pm 6\%$
12	0.88	0.99	0.95	$\pm 7\%$

 Table 3.
 Density trend at each altitude layer

Altitude	Autumn-noon	Autumn-midnight	Spring-noon	Spring-midnight	Mean
(km)	(%/decade)	(%/decade)	(%/decade)	(%/decade)	(%/decade)
71-77	-8.5 ± 5.2	$+5.5 \pm 7.6$	-8.2 ± 8.1	-5.9 ± 9.0	-5.1 ± 3.5
74 - 80	-7.2 ± 4.1	-0.1 ± 5.5	-6.7 ± 6.6	-3.6 ± 6.7	-4.8 ± 2.7
77 - 83	-4.0 ± 3.5	$+0.2 \pm 4.3$	$+0.8\pm6.1$	-4.7 ± 5.5	-2.3 ± 2.3
80 - 86	-3.8 ± 3.7	-2.7 ± 4.0	$+3.9\pm7.3$	-5.9 ± 5.1	-3.1 ± 2.3
83 - 89	-4.6 ± 2.8	-2.9 ± 3.0	N.A.	N.A.	-3.8 ± 2.0
86 - 92	-6.1 ± 2.0	-3.0 ± 2.7	N.A.	N.A.	-4.9 ± 1.6
89 - 95	-7.4 ± 2.0	-7.1 ± 3.5	N.A.	N.A.	-7.4 ± 1.8
92 - 98	-7.8 ± 2.2	-5.7 ± 3.5	$+1.1\pm8.5$	-3.9 ± 13.9	-6.7 ± 1.8
95 - 101	-7.9 ± 2.6	-6.6 ± 3.6	-1.0 ± 9.9	-6.9 ± 15.9	-7.2 ± 2.0
98 - 104	-8.3 ± 2.9	-10.2 ± 3.4	-4.6 ± 10.9	-12.7 ± 16.7	-9.0 ± 2.2
101 - 107	-9.3 ± 3.4	-14.0 ± 2.7	-6.5 ± 10.9	-1.3 ± 17.6	-11.9 ± 2.0
104 - 110	-6.3 ± 3.0	-13.4 ± 2.4	$+2.6\pm10.0$	-11.3 ± 16.9	-10.1 ± 1.8
107 - 113	$+2.0 \pm 4.1$	-14.2 ± 3.4	N.A.	$+23.1\pm14.0$	-6.5 ± 2.6
110 - 116	$+4.2\pm5.5$	-21.3 ± 6.7	N.A.	N.A.	-6.2 ± 4.3

N.A. stands for not available.

Altitude (km)	Reduced chi-squares					
	Autumn-noon	Autumn-midnight	Spring-noon	Spring-midnight		
71–77	1.705	3.842	0.939	2.364		
74 - 80	1.296	1.157	0.844	0.879		
77 - 83	1.352	1.088	1.226	0.538		
80-86	1.493	0.967	1.433	0.544		
83-89	1.277	0.817	N.A.	N.A.		
86-92	1.131	1.417	N.A.	N.A.		
89 - 95	1.618	5.682	N.A.	N.A.		
92 - 98	1.699	5.710	2.719	2.351		
95 - 101	1.311	3.729	3.112	2.582		
98 - 104	1.228	1.956	2.352	1.745		
101 - 107	1.083	1.075	1.168	1.293		
104 - 110	0.745	0.598	0.610	0.683		
107 - 113	0.755	0.647	N.A.	0.488		
110 - 116	0.641	1.367	N.A.	N.A.		

 Table 4.
 Goodness of MLR fittings

N.A. stands for not available.

 $\textbf{Table 5.} \quad \text{Altitude} \rightarrow \text{density trends in the MLT region}$

Target	Altitude	Obs. Period	Altitude trend	Density trend ^{a}	Reference
(Method)	(km)	(yr)	$(\mathrm{km/decade})$	(%/decade)	
E -layer $n_{\rm e}$ peak height	110	1957 - 2005	-0.029 ± 0.020	$-4.6 \pm 3.2 \pm 0.03$	Bremer (2008)
(Ionosonde)					
High mesopause height	100	1990 - 2018	$-0.45 {\pm} 0.09$	$-7.2\pm1.4\pm0.5$	Yuan et al. (2019)
(Na lidar)					
Meteor peak flux altitude	92	2002 - 2014	$-0.58 {\pm} 0.01$	-5.8 ± 1.1	Stober et al. (2014
(Specular meteor echo)					
Na layer height	92	1972 - 1994	$-0.37 {\pm} 0.09$	$-6.2\pm1.4\pm0.4$	Clemesha et al. (199
(Na lidar)					
Low mesopause height	85	1990 - 2018	$-0.13 {\pm} 0.16$	$-2.1\pm2.6\pm0.1$	Yuan et al. (2019)
(Na lidar)					
Radio reflection height	82	1959 - 2009	$-0.114{\pm}0.078$	$-1.8 \pm 1.2 \pm 0.01$	Peters et al. (2017)
(Phase-height experiment)					
Pressure altitude	50 - 91	1991 - 2020	$-0.15 {\pm} 0.05$	$-2.4 \pm 0.8 \pm 0.02$	Bailey et al. (2021)
(Satellites' remote sensing)					

^aThe first and second error-terms represent intrinsic measurement errors and possible errors on density gradients $(\pm 1\%/\text{km})$ in the empirical models, respectively.

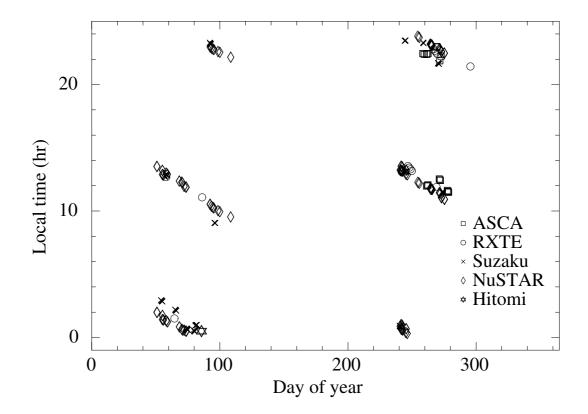


Figure 1. Local time at an altitude of $100 \, \mathrm{km}$ for each occultation against the day of year.

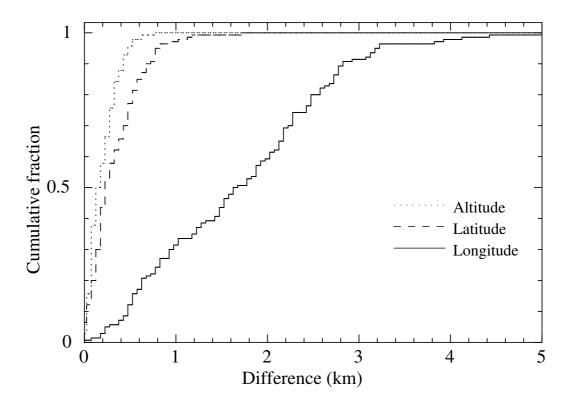


Figure 2. Cumulative fraction of the TLE errors in three directions. The TLE errors are defined as the difference between the RXTE position given in the orbit file (less than \sim 450-m at 99% confidence level) and that estimated from the TLE.

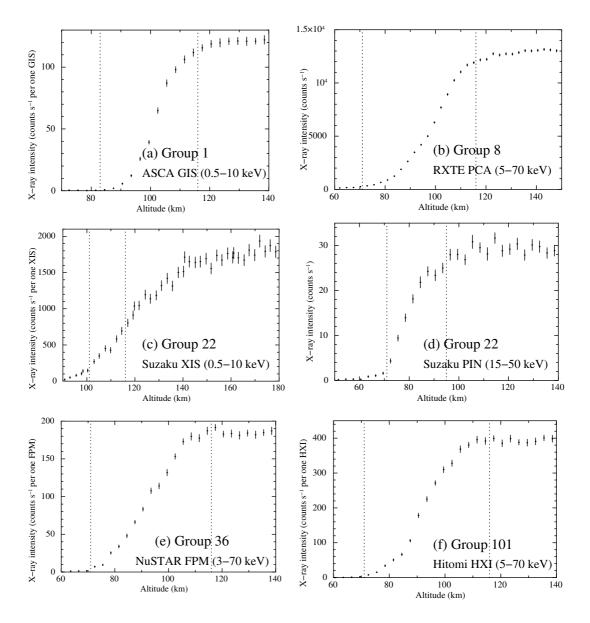


Figure 3. (a) Example occultation light curves for ASCA/GIS. Ten individual occultations in group 1 (five occultations for GIS2 and GIS3) are merged to improve the photon statistics. The deadtime correction is not performed for this light curve. The altitude range used for our spectral analysis is within dotted vertical lines in each panel. (b)–(f) Same as (a) but for RXTE/PCA, Suzaku/XIS, Suzaku/PIN, NuSTAR/FPM, and Hitomi/HXI. Note that rounded shapes of the light curves are due to gradual changes of the neutral column density as a function of altitude. Also, the altitudes where most of the photons are absorbed vary significantly. This is because energy coverages are different among instruments; photons with higher energies can penetrate more deeply into the atmosphere.

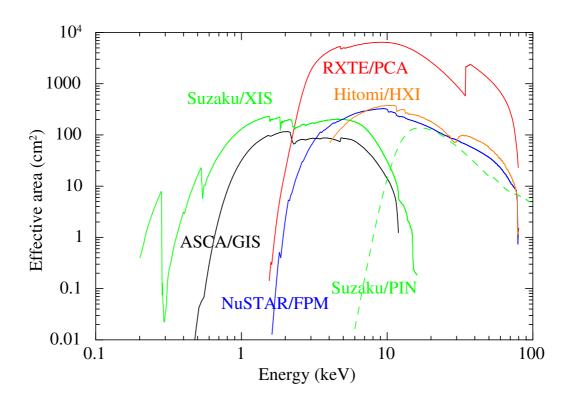


Figure 4. Comparison of the effective areas for the six instruments analyzed in this paper.

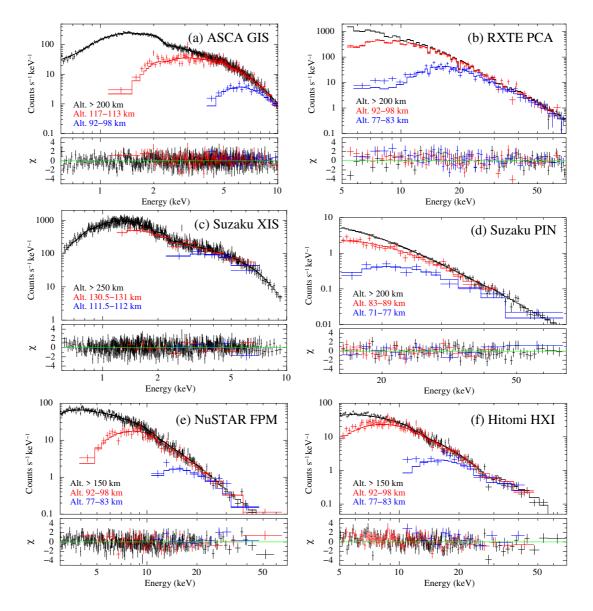


Figure 5. (a) Example X-ray spectra obtained with the ASCA/GIS. The occultations used are the same as Fig. 3 (a). Data in black, red, and blue are taken at different altitude layers. It is clear that the X-ray intensity decreases from the low-energy band, as the layer goes deeper. The data in black are fitted with TBabs \times powerlaw, and those in red and blue are fitted with vphabs \times cabs \times TBabs \times powerlaw (see text for details). (b)-(f) Same as (a) but for RXTE/PCA, Suzaku/XIS, Suzaku/PIN, NuSTAR/FPM, and Hitomi/HXI.

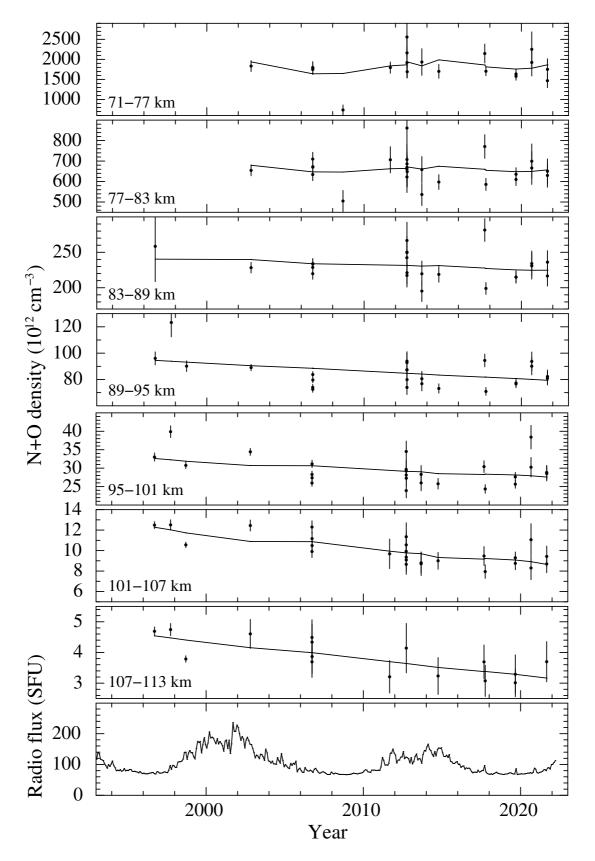


Figure 6. Combined N+O density trends at altitude layers indicated in the lower-left corner of each panel. We concentrate on the data taken at Autumn-midnight. The solid lines represent the best-fit model obtained by the multiple linear regression analysis. The bottom panel shows the solar radio (10.7 cm) flux in solar flux unit (SFU).

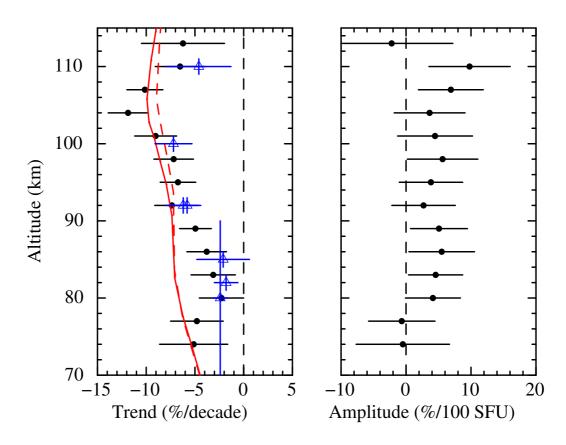


Figure 7. Left: Linear trends in N+O density as a function of geometric altitude. The solid and dashed lines represent numerical simulations computed for the solar maximum and minimum conditions, respectively (Solomon et al., 2019). The triangle data in blue show density trends inferred from past measurements of atmospheric falling. Right: N+O density amplitude to the radio solar flux as a function of geometric altitude.

Appendix A Summary of Atmospheric Occultations Analyzed

All the data analyzed in this paper are listed in Table A1. For ASCA and NuS-TAR, we recalculated satellites' positions to improve the accuracy, using the skyfield package into which we gave orbital elements taken from NORAD TLEs (http://celestrak.com/NORAD/archive with the SGP4 propagator algorithm. We use original positions for the other satellites, which are provided by the teams. These satellite positions are the most important ingredients to determine tangent altitudes and tangent points. We collected data taken in spring (± 30 days around the equinox) and autumn (± 30 days around the equinox). We also limit the data taken in the nothern hemisphere. The last column denotes the data group. We merge the data in the same group for our spectral analysis.

Instrument	UT^a	Tangent point ^{b}	Local time ^{c}	Type	Group
(Obs.ID)	(HH:MM:SS)	Long, Lat $(^{\circ})$	(HH:MM:SS)	~ .	
	1994-09-28, 05:24:41	106.9204, 41.9572	12:32:21		1
ASCA/GIS	1994-09-28, 14:59:35	322.4569, 41.5094	12:29:24	0	1
(10010180)	$1994-09-29,\ 00:34:29$	177.9692, 41.0303	12:26:21		1
(10010100)					1
		1994-09-29, 02:10:18 $153.8861, 40.9471$ $12:25:50$ Setting $1994-09-29, 05:21:56$ $105.7188, 40.7777$ $12:24:47$ Setting $1994-10-04, 13:07:13$ $337.7223, 30.8591$ $11:38:05$ Setting $1994-10-04, 22:42:08$ $193.0689, 29.9003$ $11:34:23$ Setting $1994-10-05, 00:17:58$ $168.9556, 29.7475$ $11:33:47$ Setting $1994-10-05, 01:53:47$ $144.8492, 29.5808$ $11:33:10$ Setting $1994-10-05, 03:29:36$ $120.7376, 29.4155$ $11:30:02$ Setting $1994-10-05, 09:52:53$ $24.2916, 28.7546$ $11:30:02$ Setting $1994-10-05, 11:28:42$ $0.1818, 28.5844$ $11:29:25$ Setting $1994-10-05, 13:04:31$ $336.0716, 28.4137$ $11:28:48$ Setting $1996-09-17, 09:23:55$ $38.5445, 6.2673$ $11:58:05$ Setting $1996-09-17, 09:54:07$ $187.4372, 41.5528$ $22:23:51$ Rising $1996-09-17, 10:59:44$ $14.6868, 6.6670$ $11:58:27$ Setting $1996-09-17, 10:59:44$ $14.6868, 6.6670$ $11:58:27$ Setting $1996-09-17, 23:46:12$ $183.7813, 9.6564$ $12:01:18$ Setting $1997-09-26, 07:45:40$ $228.6920, 8.1441$ $23:00:25$ Rising $1997-09-26, 15:44:06$ $108.2979, 9.2428$ $22:57:16$ Rising $1997-09-26, 15:44:06$ $108.2979, 9.2428$ $22:57:16$ Rising $1998-09-15, 10:12:57$ $183.6161, 43.5114$ $22:27:24$ Rising $1998-09-15, 11:48:28$ $159.6453, 43.5447$ $22:27:02$ Rising<	1		
	,			Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Rising Setting Rising Rising Rising Rising Rising Rising Rising Rising Rising Rising Setting Setting Setting Setting Setting Setting Rising	2
					2
	,				2
ASCA/GIS	·	·			2
(10010190)					2
				0	2
				0	2
				0	2
					3
		2		0	4
ASCA/GIS	<i>,</i>	2		0	3
(10403000)					4
					3
	1996-09-17, 23:46:12	183.7813, 9.6564	12:01:18	Setting	4
ASCA/GIS	1997-09-26, 07:45:40	228.6920, 8.1441	23:00:25	Rising	5
(11501000)	1997-09-26, 09:21:21	204.6166, 8.3629		Rising	5
(11501000)	1997-09-26, 15:44:06	108.2979, 9.2428	22:57:16	Rising	5
	1998-09-15, 10:12:57	183.6161, 43.5114	22:27:24	Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Rising Setting Rising Rising Rising Rising Rising Rising Rising Rising Rising Rising Rising Rising Rising Setting	6
ASCA/CIS	1998-09-15, 11:48:28	159.6453, 43.5447	22:27:02	Rising	6
,	1998-09-15, 13:24:00	135.7008, 43.5384	22:26:48	Rising	6
(11002000)	1998-09-16, 11:41:20	160.3667, 43.6404	22:22:47	Rising	6
	1998-09-16, 14:52:23	112.4787, 43.6316	22:22:17	Rising	6
	2002-03-05, 14:05:26	171.2213, 27.0653	01:30:19	Setting	7
	2002-08-29, 22:14:21	222.8523, 1.4405	13:05:44	Setting	8
RXTE/PCA	2002-09-26, 02:04:09	147.4954, 22.0718	11:54:06	Setting	9
(70018)	2002-10-22, 14:23:43	105.4934, 3.7893	21:25:41	Rising	10
	2003-02-27, 04:33:13	122.0489, 16.4205	12:41:23		11
	2003-03-27, 03:39:21	111.3536, 8.4639	11:04:45		12
	2006-09-03, 21:09:40	245.9062, 27.8003	13:33:16	-	13
	2006-09-04, 20:43:57	250.4656, 26.0700	13:25:47	0	14
,	2006-09-05, 20:18:14	254.9570, 24.1404	13:18:02	Setting	15

Table A1: Atmospheric occultations of the Crab Nebula analyzed in this paper.

 $^a \rm Universal time when the line-of-sight tangential altitude becomes <math display="inline">100\,\rm km.$

 $^b {\rm Latitude}$ and longitude of the tangent point at 100 km altitude.

Instrument	UT^a	Tangent point ^{b}	Local time ^{c}	Type	Group
(Obs.ID)	(HH:MM:SS)	Long, Lat $(^{\circ})$	(HH:MM:SS)		
	2006-09-06, 19:52:32	259.3940, 22.0419	13:10:05	Setting	16
	2006-09-23, 21:05:07	25.7248, 21.7392	22:48:00	Rising	17
	2006-09-24, 20:39:22	30.1601, 23.8829	22:40:00	Rising	18
	2006-09-25, 20:13:36	34.6437, 25.8576	22:32:09	Rising	19
	2006-09-26, 19:47:50	39.1949, 27.6340	22:24:36	Rising	20
Suzaku/XIS+PIN	2005-09-15, 15:47:27	112.9348, 21.6094	23:19:10	Rising	21
Suzaku/XIS+PIN	2005-09-15, 17:23:23	88.7894, 21.8078	23:18:32	Rising	21
(100023010)	2005-09-15, 18:59:19	64.6462, 22.0065	23:17:53	Rising	21
PIN only	2005-09-15, 14:11:30	117.5 154.0	23:19:50	Rising	21
Suzaku/XIS+PIN	2005-09-15, 20:35:15	40.5040, 22.2049	23:17:15	Rising	21
(100023020)	2005-09-16, 01:23:04	328.0701, 22.7902	23:15:20		21
()	2007-03-20, 11:03:59	203.0962, 28.9984	00:36:21	-	22
	2007-03-20, 19:03:28	82.4316, 28.1415	00:33:11		22
	2007-03-20, 20:39:21	58.3004, 27.9608	00:32:32	0	22
	2007-03-20, 22:15:15	34.1662, 27.7856	00:31:54	0	$\frac{-}{22}$
	2007-03-20, 23:51:09	10.0323, 27.6087	00:31:15	0	$\frac{12}{22}$
Suzaku/XIS+PIN	2007-03-21, 01:27:03	345.9020, 27.4311	00:30:38		22
(102019010)	2007-03-21, 03:02:56	321.7692, 27.2496	00:30:00		22
	2007-03-21, 04:38:50	297.6363, 27.0733	00:29:21		22
	2007-03-21, 06:14:44	273.5048, 26.8952	00:28:45	0	22
	2007-03-21, 07:50:38	249.3681, 26.7177	00:28:05	0	22
	2007-03-21, 09:26:31	245.5001, 20.1111 225.2351, 26.5324	00:27:27		$\frac{22}{22}$
	$-\frac{2007-03-21}{2007-03-20}, 12:39:53$	$\frac{223.2331, 20.3324}{178.9600, 28.8299}$	$-\frac{00.21.21}{00.35.43}$	88Setting00Setting11Setting15Setting15Setting16Setting17Setting18Setting19Setting11Setting15Rising	$-\frac{22}{22}$
	2007-03-20, 12:35:35	154.8306, 28.6595	00:35:05		$\frac{22}{22}$
	2007-03-20, 14:15:47 2007-03-20, 15:51:40	134.8300, 28.0393 130.6976, 28.4824	00:33:03 00:34:27	0	$\frac{22}{22}$
PIN only			00:33:48	0	$\frac{22}{22}$
	2007-03-20, 17:27:34	106.5661, 28.3117	00:35:48 00:26:49		$\frac{22}{22}$
	2007-03-21, 11:02:25	201.1047, 26.3490			
	2007-03-21, 12:38:19	176.9683, 26.1683	00:26:11	0	22
	2008-08-27, 08:53:45	240.7545, 8.8327	00:56:45	Setting Rising Rising Rising Rising Rising Rising Rising Rising Rising Rising Rising Setting Rising Rising Rising Rising Rising Rising Setting	23
	2008-08-27, 10:29:38	216.6275, 9.0504	00:56:08		23
	2008-08-27, 12:05:31	192.5022, 9.2686	00:55:31	-	23
~	2008-08-27, 13:41:25	168.3694, 9.4947	00:54:52		23
Suzaku/XIS+PIN	2008-08-27, 15:17:18	144.2389, 9.7116	00:54:15		23
(103007010)	2008-08-27, 16:53:11	120.1106, 9.9297	00:53:36		23
	2008-08-27, 18:29:05	95.9780, 10.1570	00:52:59		23
	2008-08-27, 20:04:58	71.8479, 10.3754	00:52:21		23
	2008-08-27, 21:40:51	47.7197, 10.5942	00:51:42		23
	2008-08-28, 04:04:24	311.2021, 11.4750	00:49:11	15Setting 38 Setting 00 Setting 21 Setting 21 Setting 45 Setting 05 Setting 27 Setting 43 Setting 27 Setting 31 Setting 31 Rising 31 Rising 52 Rising 36 Rising 36 Rising 21 Rising 42 Rising 31 Rising	23
	2009-04-02, 02:28:52	312.5537, 15.8190	23:19:04	RisingRisingRisingRisingSettingRisingRisingRisingRisingRisingRisingRisingRisingRisingRisingRisingSetting <tr< td=""><td>24</td></tr<>	24
	2009-04-02, 05:40:37	264.3008, 15.3940	23:17:48	Setting	24
	2009-04-02, 07:16:29	240.1773, 15.1828	23:17:11	Setting	24
	2009-04-02, 08:52:22	216.0431, 14.9684	23:16:32	Setting	24
Suzaku/PIN (only)	2009-04-02, 10:28:15	191.9123, 14.7529	23:15:52	Setting	24
/ ()	2009-04-02, 12:04:08	167.7842, 14.5363	23:15:15	Setting	24
(104001010)	2009-04-02, 13:40:00	143.6593, 14.3257	23:14:38	Setting	24
	2009-04-02, 15:15:53	119.5299, 14.1091	23:13:59	Setting	24
	2009-04-02, 16:51:45	95.4068, 13.8977	23:13:22		24
	2009-04-02, 18:27:38	71.2755, 13.6801	23:12:43		24
	2009-04-02, 20:03:31	47.1460, 13.4604	23:12:06	Setting	24

 $^a \mathrm{Universal}$ time when the line-of-sight tangential altitude becomes $100\,\mathrm{km}.$

 $^b\mathrm{Latitude}$ and longitude of the tangent point at 100 km altitude.

Instrument	UT^a	Tangent $point^b$	Local time ^{c}	Type	Group
(Obs.ID)	(HH:MM:SS)	Long, Lat $(^{\circ})$	(HH:MM:SS)		
	2009-04-02, 21:39:24	23.0145, 13.2414	23:11:26	Setting	24
	2009-04-02, 23:15:16	358.8897, 13.0297	23:10:49	Setting	24
	2009-04-03, 00:51:09	334.7635, 12.8104	23:10:12	Setting	24
	2010-02-23, 01:07:24	27.5234, 44.5019	02:57:29	Setting	25
	2010-02-23, 02:43:15	3.4639, 44.4581	02:57:06	Setting	25
	2010-02-23, 04:19:07	339.4214, 44.4512	02:56:48		25
Suzaku/XIS+PIN	2010-02-23, 05:54:58	315.3504, 44.4045	02:56:21		25
	2010-02-23, 13:54:14	195.0371, 44.2031	02:54:21	0	25
	2010-02-23, 15:30:05	170.9671, 44.1518	02:53:57	0	25
	2010-02-23, 17:05:56	146.8931, 44.0990	02:53:30	0	25
(104001070)	2010-02-23, 18:41:48	122.8454, 44.0821	02:53:09	0	25
(101001010)	2010-02-23, 20:17:39	98.7736, 44.0294	02:52:44	0	$\frac{-0}{25}$
	2010-02-23, 21:53:30	74.6982, 43.9783	02:52:17		$\frac{20}{25}$
	2010-02-23, 23:29:21	50.6253, 43.9263	02:51:51	0	$\frac{20}{25}$
	2010-02-23, 25:25:21 2010-02-24, 01:05:12	26.5563, 43.8720	02:51:24	0	$\frac{25}{25}$
	2010-02-24, 01:05:12 2010-02-24, 02:41:03	2.4805, 43.8172	02:50:57	0	$\frac{25}{25}$
Suzaku/XIS+PIN (105002010)	2010-02-24, 02:41:03 2010-02-24, 04:16:54	338.4038, 43.7578	02:50:37 02:50:30		$\frac{25}{25}$
			02:30:30	~	$\frac{23}{26}$
	2010-04-06, 00:13:27	132.5794, 44.7686	09:03:40	5) Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Rising Rising Rising Rising Rising Rising Rising Rising Rising Rising Setti	$\frac{20}{26}$
	2010-04-06, 01:49:18	108.5461, 44.7772		0	
Suzaku/XIS+PIN	2010-04-06, 03:25:10	84.5450, 44.7403	09:03:20	0	26
(105002010)	2010-04-06, 05:01:02	60.5457, 44.6994	09:03:11	0	26
· · · ·	2010-04-06, 06:36:54	36.5486, 44.6582	09:03:05	0	26
	2010-04-06, 08:12:45	12.5208, 44.6633	09:02:48		26
	2010-04-06, 09:48:37	348.5188, 44.6257	09:02:40		26
	2010-04-05, 16:14:09	252.6709, 44.8427	09:04:50		26
	2010-04-05, 17:50:00	228.6303, 44.8519	09:04:31		26
PIN only	2010-04-05, 19:25:52	204.6280, 44.8210	09:04:22		26
	2010-04-05, 21:01:43	180.5906, 44.8324	09:04:04		26
	2010-04-05, 22:37:35	156.5839, 44.8016	09:03:55	9Setting2Setting2Setting3Setting4Setting5Setting6Setting7Setting9Setting9Setting9Setting9Setting9Setting1Setting1Setting1Setting1Setting1Setting1Setting1Setting1Setting1Setting1Setting1Rising1Rising1Rising1Rising1Rising1Rising1Rising1Rising2Rising3Setting3Setting4Setting5Setting6Setting7Setting8Setting9 <td< td=""><td>26</td></td<>	26
	2011-03-21, 19:41:41	78.7092, 39.2653	00:56:30	Setting	27
	2011-03-21, 21:17:33	54.7942, 39.4346	00:56:43	Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Setting Rising Rising Rising Rising Rising Rising Rising Rising Rising Setting	27
	2011-03-21, 22:53:25	30.8867, 39.6003	00:56:57	Setting	27
	2011-03-22, 00:29:18	7.0040, 39.8187	00:57:17	Setting	27
	2011-03-22, 02:05:10	343.0985, 39.9859	00:57:33	Setting	27
	2011-03-22, 03:41:02	319.1887, 40.1518	00:57:47	Setting	27
	2011-03-22, 05:16:54	295.2737, 40.3134	00:57:59	Setting	27
	2011-03-22, 10:04:30	223.5321, 40.7892	00:58:36	Setting	27
Suzaku/XIS+PIN	2011-03-22, 11:40:22	199.6170, 40.9492	00:58:50	Setting	27
	2011-03-22, 13:16:13	175.6760, 41.0566	00:58:54		27
× /	2011-03-22, 14:52:05	151.7591, 41.2150	00:59:07		27
	2011-03-22, 16:27:57	127.8495, 41.3677	00:59:20		27
	2011-03-22, 18:03:48	103.9000, 41.4732	00:59:23		$\overline{27}$
	2011-03-22, 19:39:40	79.9866, 41.6262	00:59:35		27
	2011-03-22, 21:15:32	56.0717, 41.7799	00:59:48		27
	2011-03-22, 22:51:23	32.1257, 41.8849	00:59:53		27
	2011-03-23, 00:27:15	8.2138, 42.0381	01:00:06		$27 \\ 27$
	2011-03-23, 02:03:06	344.2684, 42.1442	01:00:10		$\frac{21}{27}$
	2011-03-23, 02:03:00	$\frac{544.2084, 42.1442}{252.0472, 42.5591}$	23:27:38	0	$\frac{21}{28}$
Suzaku/XIS+PIN (105029010) Suzaku/XIS+PIN					
(106012010)	2011-09-01, 07:45:03	79.6606, 5.5418	13:03:41		29 28
(105029010) Suzaku/XIS+PIN	2011-09-01, 08:15:17	228.0969, 42.4752	23:27:39	Rising	28

 b Latitude and longitude of the tangent point at 100 km altitude.

Instrument	UT^a	Tangent point ^{b}	Local time ^{c}	Type	Grou
(Obs.ID)	(HH:MM:SS)	Long, Lat $(^{\circ})$	(HH:MM:SS)		
	2011-09-01, 09:51:07	204.1749, 42.3442	23:27:47	Rising	28
	2011-09-01, 10:56:49	31.8986, 6.3004	13:04:23	Setting	29
	2011-09-01, 11:26:56	180.2215, 42.2622	23:27:48	Rising	28
	2011-09-01, 13:02:46	156.3045, 42.1316	23:27:59		28
	2011-09-01, 14:38:36	132.3875, 41.9985	23:28:08		28
	2011-09-01, 16:14:26	108.4658, 41.8605	23:28:17		28
	2011-09-01, 17:50:15	84.5215, 41.7703	23:28:19		28
	2011-09-01, 19:26:05	60.6072, 41.6296	23:28:30		28
	2011-09-01, 20:32:07	248.6250, 8.5945	13:06:37		29
	2011-09-01, 21:01:55	36.6872, 41.4873	23:28:38		$\frac{1}{28}$
	2011-09-01, 22:08:00	224.7420, 8.9729	13:06:57		29
	2011-09-01, 22:37:45	12.7723, 41.3508	23:28:50		$\frac{20}{28}$
	2011-09-01, 22:91:49	200.8643, 9.3497	13:07:19		20 29
	2011-09-02, 00:13:35	348.8518, 41.2116	23:28:59	0	$\frac{23}{28}$
	2011-09-02, 01:19:46	176.9834, 9.7286	13:07:41		20 29
			13:08:08	0	$\frac{29}{29}$
	2011-09-02, 02:55:40 2011-09-02, 04:31:33	$153.1248, 10.1580 \\129.2479, 10.5358$	13:08:31		$\frac{29}{29}$
					29 29
	2011-09-02, 06:07:26	$\frac{105.3699, 10.9140}{248.0472, 21.5102}$	13:08:53	~	$\frac{29}{30}$
	2012-03-14, 01:27:52	348.9473, 21.5192	00:43:39		
	2012-03-14, 03:03:35	324.8601, 21.3204	00:43:00		30
	2012-03-14, 04:39:18	300.7737, 21.1207	00:42:23		30
	2012-03-14, 06:15:01	276.6836, 20.9213	00:41:44	0	30
	2012-03-14, 07:50:44	252.5936, 20.7208	00:41:06	0	30
	2012-03-14, 09:26:27	228.5048, 20.5185	00:40:27		30
1	2012-03-14, 11:02:10	204.4156, 20.3156	00:39:48		30
(106014010)	2012-03-14, 12:37:53	180.3265, 20.1133	00:39:11		30
	2012-03-14, 14:13:36	156.2397, 19.9099	00:38:32		30
	2012-03-14, 15:49:19	132.1504, 19.7072	00:37:54		30
	2012-03-14, 17:25:02	108.0625, 19.5037	00:37:15		30
	2012-03-14, 19:00:45	83.9744, 19.2992	00:36:38		30
Suzaku/XIS+PIN (106014010)	2012-03-14, 20:36:28	59.8841, 19.0937	00:36:00	Setting	30
	2012-03-14, 22:12:11	35.7953, 18.8861	00:35:21	Setting	30
	2012-09-26, 06:38:44	225.9450, 43.6655	21:42:29	Rising	31
	2012-09-26, 08:14:24	201.9427, 43.6907	21:42:10	Setting Rising Rising Rising Rising Rising Rising Rising Setting Rising Setting Rising R	31
	2012-09-26, 09:50:03	177.9161, 43.7499	21:41:42	Rising	31
	2012-09-26, 11:25:42	153.8869, 43.8101	21:41:13	Rising	31
	2012-09-26, 13:01:22	129.8874, 43.8355	21:40:54	Rising	31
Suzaku/XIS+PIN	2012-09-26, 14:37:01	105.8578, 43.8916	21:40:26	Rising	31
(107011010)	2012-09-26, 16:12:40	81.8353, 43.9488	21:40:00	Rising	31
	2012-09-26, 17:48:19	57.8115, 44.0017	21:39:33	Rising	31
	2012-09-26, 19:23:59	33.8157, 44.0155	21:39:14	Rising	31
	2012-09-26, 20:59:38	9.7952, 44.0657	21:38:48	0	31
	2012-09-26, 22:35:17	345.7727, 44.1193	21:38:21		31
	2012-09-27, 04:57:55	249.7428, 44.2478	21:36:52		31
	2013-02-27, 01:09:14	176.7227, 6.7619	12:56:07	· · ·	32
	2013-02-27, 02:44:51	152.6637, 6.9839	12:55:30		32
Suzaku/XIS+PIN	2013-02-27, 04:20:28	128.6018, 7.2055	12:54:51		32
	2013-02-27, 05:56:05	104.5407, 7.4277	12:54:14		32
(10,012010)	2013-02-27, 07:31:42	80.4816, 7.6515	12:53:36		32 32
	2013-02-27, 09:07:19	56.4198, 7.8743	12:53:50 12:52:59		32 32
(106014010) Suzaku/XIS+PIN	2010-02-21, 03.01.13	50.4150, 1.0145	12.02.03	Tusing	04

^bLatitude and longitude of the tangent point at 100 km altitude.

Instrument	UT^a	Tangent $point^b$	Local time ^{c}	Type	Group
(Obs.ID)	(HH:MM:SS)	Long, Lat $(^{\circ})$	(HH:MM:SS)		
	2013-02-27, 17:05:23	296.1170, 8.9776	12:49:50	Rising	32
	2013-02-27, 18:41:00	272.0577, 9.2017	12:49:13	Rising	32
	2013-02-27, 20:16:37	247.9946, 9.4233	12:48:34	Rising	32
PIN only	2013-02-27, 21:52:14	223.9340, 9.6449	12:47:57	Rising	32
istrument Dbs.ID) PĪN only Suzaku/XIS+PIN (108011010) PĪN only PĪN only Suzaku/XIS+PIN (108012010) NuSTAR/FPM (10013021002) NuSTAR/FPM (10013024002) NuSTAR/FPM	2013-09-30, 11:41:53	357.3104, 19.7266	11:31:06	Setting	33
	2013-09-30, 13:17:25	333.2719, 19.5224	11:30:29	Setting	33
	2013-09-30, 14:52:57	309.2295, 19.3195	11:29:52	Setting	33
	2013-09-30, 16:28:29	285.1842, 19.1169	11:29:12	Setting	33
	2013-09-30, 18:04:01	261.1428, 18.9115	11:28:35	Setting	33
	2013-09-30, 19:39:34	237.0956, 18.7033	11:27:56	Setting	33
Suzaku/XIS+PIN	2013-09-30, 21:15:06	213.0517, 18.4971	11:27:18	Setting	33
(108011010)	2013-09-30, 22:50:38	189.0108, 18.2901	11:26:39	Setting	33
	2013-10-01, 00:26:10	164.9684, 18.0839	11:26:02	Setting	33
	2013-10-01, 02:01:42	140.9276, 17.8767	11:25:23	Setting	33
	2013-10-01, 03:37:15	116.8792, 17.6673	11:24:46	Setting	33
	2013-10-01, 05:12:47	92.8361, 17.4602	11:24:06	Setting	33
	2013-10-01, 06:48:19	68.7952, 17.2506	11:23:29	Setting	33
	2013-10-01, 08:23:51	44.7519, 17.0404	11:22:50	Setting	33
PIN only	2013-10-01, 09:59:23	20.7104, 16.8293	11:22:13	Setting	-33
	2014-03-06, 01:51:23	5.2762, 44.0279	02:12:29	:29Setting:02Setting:40Setting:38Setting	34
	2014-03-06, 03:26:48	341.3101, 43.9703	02:12:02	Setting	34
	2014-03-06, 05:02:14	317.3638, 43.9483	02:11:40	Setting	34
	2014-03-06, 12:59:21	197.5711, 43.7266	02:09:38	Setting	34
	2014-03-06, 14:34:46	173.6008, 43.6648	02:09:10	Setting	34
	2014-03-06, 16:10:11	149.6319, 43.5993	02:08:42	Setting	34
(108012010)	2014-03-06, 17:45:37	125.6839, 43.5707	02:08:21	Setting	34
	2014-03-06, 19:21:02	101.7124, 43.5079	02:07:51	Setting	34
	2014-03-06, 20:56:28	77.7640, 43.4797	02:07:31	Setting	34
	2014-03-06, 22:31:53	53.7919, 43.4175	02:07:03	Setting	34
(108011010) <u>PIN only</u> Suzaku/XIS+PIN (108012010) NuSTAR/FPM (10013021002) NuSTAR/FPM	2014-03-07, 00:07:18	29.8190, 43.3556	02:06:33	Setting	34
	2012-09-20, 03:14:44	299.2689, 15.5307	23:11:48	Rising	35
NuSTAR/FPM	2012-09-20, 04:16:38	112.4618, 5.5680	11:46:27	Setting	36
,	2012-09-20, 04:51:46	274.9422, 15.5296	23:11:31	Rising	35
Suzaku/XIS+PIN (108012010) NuSTAR/FPM	2012-09-20, 05:53:41	88.1595, 5.6261	11:46:18	Setting	36
	2012-09-20, 11:19:56	177.6637, 15.4670	23:10:35	Rising	37
NuSTAR/FPM	2012-09-20, 12:21:52	350.9328, 5.8355	11:45:34	Setting	38
	2012-09-20, 12:56:58	153.3413, 15.4654	23:10:18	Rising	37
(10010021002)	2012-09-20, 13:58:54	326.6212, 5.8660	11:45:23	Setting	38
	2012-09-20, 19:25:08	$\frac{520.0212, 0.0000}{55.7379, 15.3000}$	23:08:04	Rising	39
NuSTAR/FDM	2012-09-20, 19:25:08	229.0669, 6.1742	11:43:21	Setting	40
(10013022002)	2012-09-20, 20:27:03 2012-09-20, 21:02:10	31.4155, 15.2962	23:07:49	Rising	$\frac{40}{39}$
(10013022002)	2012-09-20, 21:02:10 2012-09-20, 22:04:08	204.7604, 6.2364		Setting	$\frac{39}{40}$
	,	$\frac{204.7604, 0.2304}{294.4665, 15.3093}$	$\frac{11:43:09}{23:08:11}$	-	
NUCTAD /EDM	2012-09-21, 03:30:20	,	23:08:11	Rising	41 42
NuSTAR/FPM	2012-09-21, 04:32:19	107.8726, 6.3589	11:43:48	Setting	42
(10013022004)	2012-09-21, 05:07:22	270.1443, 15.3033	23:07:55	Rising	41
	2012-09-21, 06:09:22	83.5663, 6.4222	11:43:36	Setting	42
NuSTAR/FPM	2012-09-21, 16:26:39	99.9226, 15.1632	23:06:20	Rising	43
(10013022006)	2012-09-21, 18:03:42	75.6101, 15.1242	23:06:07	Rising	43
	2013-03-09, 07:46:38	68.9599, 2.5936	12:22:27	Rising	44

 $^b\mathrm{Latitude}$ and longitude of the tangent point at 100 km altitude.

Instrument	UT^a	Tangent point ^{b}	Local time ^{c}	Type	Group
(Obs.ID)	(HH:MM:SS)	Long, Lat ($^{\circ}$)	(HH:MM:SS)		
	2013-03-09, 08:48:05	240.6845, 14.6767	00:50:48	Setting	45
NuSTAR/FPM	2013-03-09, 09:23:38	44.6454, 2.5835	12:22:11	Rising	44
	2013-03-09, 10:25:05	216.3539, 14.6495	00:50:29	Setting	45
(80001022002)	2013-03-09, 11:00:39	20.3403, 2.5505	12:22:00	Rising	44
	2013-03-09, 12:02:05	192.0277, 14.6201	00:50:11	Setting	45
	2013-04-03, 09:09:49	18.2802, 15.0293	10:22:55	Rising	46
NuSTAR/FPM	2013-04-03, 10:11:17	190.2760, 2.8922	22:52:23	Setting	47
(10013037002)	2013-04-03, 10:46:49	353.9586, 15.0456	10:22:38	Rising	46
NuSTAR/FPM (80001022002) NuSTAR/FPM (10013037002) NuSTAR/FPM (10013037004) NuSTAR/FPM (10013037006) NuSTAR/FPM (10013038002) NuSTAR/FPM (10013038004) NuSTAR/FPM (10013037008) NuSTAR/FPM (10013037008) NuSTAR/FPM (10002001002) NuSTAR/FPM (10002001004)	2013-04-03, 11:48:17	165.9694, 2.9140	22:52:09	Setting	47
	2013-04-04, 11:01:45	349.1032, 15.3330	10:18:09	Rising	48
NuSTAR/FPM	2013-04-04, 12:03:17	161.3774, 3.2953	22:48:47		49
,	2013-04-04, 12:38:45	324.7830, 15.3422	10:17:52		48
()	2013-04-04, 13:40:17	137.0754, 3.3221	22:48:34		49
	2013-04-05, 06:25:42	57.2489, 15.4965	10:14:40		50
NuSTAR/FPM	2013-04-05, 07:27:18	229.7341, 3.6801	22:46:14		51
	2013-04-05, 08:02:42	32.9296, 15.5003	10:14:25		50
(10010001000)	2013-04-05, 09:04:18	205.4322, 3.7116	22:46:00		51
	2013-04-08, 12:01:33	330.1119, 15.4659	10:01:59		52
NuSTAR/FPM	2013-04-08, 13:03:25	143.3684, 5.7677	22:36:52		53
	2013-04-08, 13:38:33	305.8007, 15.4487	10:01:45		50
(1001000002)	2013-04-08, 14:40:25	119.0723, 5.8124	22:36:42		53
	2013-04-09, 21:58:31	$\frac{110.0120, 0.0121}{179.6391, 15.0960}$	09:57:03		54
NuSTAR/FPM	2013-04-09, 23:00:29	353.1661, 6.8803	22:33:07		$54 \\ 55$
,	2013-04-09, 23:35:31	155.3323, 15.0710	09:56:49		$55 \\ 54$
(10013030004)	2013-04-10, 00:37:29	328.8659, 6.9306	22:32:56		$54 \\ 55$
	2013-04-18, 09:40:41	$\frac{323.8033, 0.3300}{357.8577, 9.2175}$	09:32:06		56
NuSTAR/FPM	2013-04-18, 10:42:49	171.7134, 13.7309	22:09:39		$50 \\ 57$
	2013-04-18, 10:42:43	333.5635, 9.1638	09:31:55		57
(10013037008)	2013-04-18, 12:19:49	147.4151, 13.7684	22:09:28		$50 \\ 57$
	2013-09-02, 04:29:03	$\frac{147.4151, 15.7084}{298.6616, 15.4632}$	00:23:40	-	58
N. CTAD /EDM	2013-09-02, 04:29:03		12:55:10		$\frac{58}{59}$
,	· · · · · · · · · · · · · · · · · · ·	111.1456, 3.6867			
(10002001002)	2013-09-02, 06:06:01	274.3493, 15.4756	00:23:24		58 50
	2013-09-02, 07:07:35	86.8473, 3.7114	12:54:57	-	<u>59</u>
(10013037002) NuSTAR/FPM (10013037004) NuSTAR/FPM (10013037006) NuSTAR/FPM (10013038002) NuSTAR/FPM (10013037008) NuSTAR/FPM (10002001002) NuSTAR/FPM	2013-09-03, 06:20:32	269.6793, 15.5823	00:19:14	0	60 61
	2013-09-03, 07:22:11	82.4347, 4.2782	12:51:55	-	61 60
(10002001004)	2013-09-03, 07:57:30	245.3676, 15.5876	00:18:57		60
	2013-09-03, 08:59:09	58.1361, 4.3083	12:51:41	-	61
	2014-10-02, 03:23:18	286.5470, 13.8173	22:29:29	RisingSettingRisingRisingRisingRisingRisingRisingRisingRisingRisingRisingRisingRisingRisingRisingRisingRisingRisingRisin	62
	2014-10-02, 04:24:24	97.8869, 2.3433	10:55:55		63
	2014-10-02, 05:00:08	262.2535, 13.8614	22:29:08		62
,	2014-10-02, 06:01:15	73.6147, 2.3598	10:55:41	0	63
(10002001008)	2014-10-02, 06:36:58	237.9601, 13.9053	22:28:48		62
	2014-10-02, 07:38:05	49.3375, 2.3531	10:55:26		63
	2014-10-02, 08:13:49	213.6728, 13.9254	22:28:30	0	62
	2014-10-02, 09:14:56	25.0655, 2.3706	10:55:10		63
	2016-04-01, 07:20:28	47.9118, 13.9393	10:32:06		64
NuSTAR/FPM	2016-04-01, 08:21:27	219.3273, 2.3173	22:58:45	Setting	65
(10002001009)	2016-04-01, 08:57:09	23.6581, 13.9778	10:31:45	Rising	64
(10002001000)	2016-04-01, 09:58:08	195.0895, 2.3163	22:58:28	Setting	65

 $^b\mathrm{Latitude}$ and longitude of the tangent point at 100 km altitude.

Instrument	UT^a	Tangent point ^{b}	Local time ^{c}	Type	Group
(Obs.ID)	(HH:MM:SS)	Long, Lat $(^{\circ})$	(HH:MM:SS)		
`	2016-04-01, 10:33:50	359.4044, 14.0159	10:31:27	Rising	64
	2016-04-01, 11:34:50	170.8569, 2.3396	22:58:14	Setting	65
	2016-04-01, 12:10:32	335.1568, 14.0299	10:31:09	Rising	64
	2016-04-01, 13:11:31	146.6191, 2.3395	22:57:59	Setting	65
	2017-02-19, 19:49:00	92.6967, 14.5072	01:59:47	Setting	66
NuSTAR/FPM	2017-02-19, 21:25:40	68.4563, 14.4823	01:59:29		66
	2017-02-19, 23:02:20	44.2117, 14.4588	01:59:09	0	66
NuSTAR/FPM (10202001006) NuSTAR/FPM (10302001002) NuSTAR/FPM (10302001004) NuSTAR/FPM (10402001004)	2017-02-20, 00:39:00	19.9671, 14.4348	01:58:51		66
	2017-09-02, 07:37:03	256.2480, 4.2871	00:42:02	~	67
	2017-09-02, 08:38:20	69.0233, 15.4090	13:14:25		68
	2017-09-02, 09:13:43	232.0362, 4.2403	00:41:51		67
NuSTAR/FPM	2017-09-02, 10:15:00	44.7982, 15.4209	13:14:11	0	68
	2017-09-02, 10:50:23	207.8203, 4.1923	00:41:39	0	67
(1000-00100-)	2017-09-02, 11:51:39	20.5630, 15.4056	13:13:54	-	68
	2017-09-02, 12:27:03	183.6087, 4.1462	00:41:29	0	60
	2017-09-02, 13:28:19	356.3337, 15.4183	13:13:38		68
	2017-09-29, 18:29:01	62.0202, 14.2942	22:37:05	RisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSettingRisingSetting	69
	2017-09-29, 19:30:02	233.6046, 2.3753	11:04:27	Setting Setting Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising Setting Rising	70
	2017-09-29, 20:05:40	37.7792, 14.3291	22:36:47		69
	2017-09-29, 21:06:41	209.3772, 2.3787	11:04:10	-	70
	2017-09-29, 21:42:20	13.5400, 14.3374	22:36:29		69
NUSTAD /FDM	2017-09-29, 21:42:20	13.5400, 14.5574 185.1551, 2.4071	11:03:57		09 70
/				0	70 69
(10302001004)	2017-09-29, 23:18:59	349.2991, 14.3715	22:36:10	-	09 70
	2017-09-30, 00:20:00	160.9278, 2.4113	11:03:42		70 69
	2017-09-30, 00:55:38	325.0540, 14.4036	22:35:49		09 70
	2017-09-30, 01:56:40	136.7058, 2.4407	11:03:29		
	2017-09-30, 02:32:17	300.8132, 14.4371	22:35:31		69 70
	2017-09-30, 03:33:19	112.4785, 2.4457	11:03:12	~	70
	2018-03-13, 00:18:24	174.8090, 9.5597	11:57:38		71
	2018-03-13, 01:20:06	348.7072, 13.2345	00:34:54		72
	2018-03-13, 01:55:04	150.6043, 9.4813	11:57:29		71
(10402001004)	2018-03-13, 02:56:45	324.4931, 13.2702	00:34:42		72
	2018-03-13, 03:31:43	126.3984, 9.4373	11:57:18		71
	2018-03-13, 04:33:25	300.2886, 13.3366	00:34:33	RisingSetting	72
	2018-03-14, 11:44:51	2.2749, 8.2658	11:53:56		73
	2018-03-14, 12:46:29	176.0298, 14.1074	00:30:36	0	74
	2018-03-14, 13:21:30	338.0655, 8.2195	11:53:44	Rising	73
	2018-03-14, 14:23:08	151.8128, 14.1372	00:30:23	Setting	74
NuSTAR/FPM	2018-03-14, 14:58:10	313.8656, 8.1428	11:53:36	Rising	73
(10402001008)	2018-03-14, 15:59:47	127.5960, 14.1665	00:30:10	Setting	74
	2018-03-14, 16:34:49	289.6562, 8.0966	11:53:26	Rising	73
	2018-03-14, 17:36:27	103.3889, 14.2259	00:30:00	Setting	74
	2018-03-14, 18:11:29	265.4564, 8.0200	11:53:17	Rising	73
	2018-03-14, 19:13:06	79.1722, 14.2544	00:29:47	Setting	74
	2019-03-11, 05:34:03	100.7470, 2.6298	12:17:2	Rising	75
	2019-03-11, 06:34:41	271.1959, 11.1829	00:39:28	Setting	76
NuSTAR/FPM	2019-03-11, 07:10:41	76.5135, 2.6532	12:16:44	Rising	75
,				Setting	76
(10502001006)	2019-03-11, 08:11:19	246.9517, 11.1325	00:39:06	Setting	(0

 $^b\mathrm{Latitude}$ and longitude of the tangent point at 100 km altitude.

Instrument	UT^a	Tangent $point^b$	Local time ^{c}	Type	Grou
(Obs.ID)	(HH:MM:SS)	Long, Lat $(^{\circ})$	(HH:MM:SS)		
	2019-03-11, 09:47:57	222.7075, 11.0821	00:38:45	Setting	76
$\frac{NuSTAR/FPM}{(10502001008)}$	2019-03-11, 18:27:08	266.5429, 2.7104	12:13:18	Rising	77
	2019-03-11, 19:27:45	76.8998, 10.8750	00:35:20	Setting	78
	2019-03-11, 20:03:46	242.3092, 2.7370	12:13:00	Rising	77
	2019-03-11, 21:04:23	52.6511, 10.8252	00:34:59	Setting	78
NuSTAR/FPM (10502001013)	2019-08-29, 10:10:21	217.6229, 15.3713	00:40:50	Rising	79
	2019-08-29, 11:11:40	30.3802, 4.3013	13:13:10	Setting	80
	2019-08-29, 11:46:59	193.3996, 15.3712	00:40:33	Rising	79
	2019-08-29, 12:48:18	6.1695, 4.3354	13:12:57	Setting	80
	2019-08-29, 13:23:37	169.1763, 15.3705	00:40:18	Rising	79
	2019-08-29, 14:24:56	341.9589, 4.3697	13:12:46	Setting	80
	2019-08-29, 15:00:15	144.9487, 15.3677	00:40:01	Rising	79
	2019-08-29, 16:01:35	317.7577, 4.4317	13:12:36	Setting	80
	2019-08-29, 16:36:53	120.7253, 15.3661	00:39:47	Rising	79
	2019-08-29, 17:38:13	293.5470, 4.4667	13:12:24	Setting	80
	2019-08-29, 18:13:31	96.5019, 15.3640	00:39:30	Rising	79
	2019-08-29, 19:14:51	269.3362, 4.5021	13:12:11	Setting	80
	2019-08-29, 19:50:09	72.2785, 15.3615	00:39:15	Rising	79
	2019-08-29, 20:51:30	245.1349, 4.5651	13:12:02	Setting	80
	2019-08-30, 08:43:13	238.4968, 15.3279	00:37:12	Rising	81
	2019-08-30, 09:44:37	51.4801, 4.9439	13:10:32	Setting	82
	2019-08-30, 10:19:51	214.2773, 15.3231	00:36:56	Rising	81
	2019-08-30, 11:21:15	27.2690, 4.9821	13:10:18	Setting	82
NuSTAR/FPM (10502001015)	2019-08-30, 11:56:30	190.0638, 15.2882	00:36:45	Rising	81
	2019-08-30, 12:57:53	3.0620, 5.0188	13:10:06	Setting	82
	2019-08-30, 13:33:08	165.8400, 15.2806	00:36:29	Rising	81
	2019-08-30, 14:34:32	338.8603, 5.0855	13:09:57	Setting	82
(2019-08-30, 15:09:46	141.6205, 15.2742	00:36:14	Rising	81
	2019-08-30, 16:11:10	314.6490, 5.1244	13:09:44	Setting	82
	2019-08-30, 16:46:24	117.4009, 15.2674	00:36:0	Rising	81
	2019-08-30, 17:47:48	290.4419, 5.1619	13:9:33	Setting	82
	2019-08-30, 18:23:02	93.1771, 15.2584	00:35:44	Rising	81
	2019-08-30, 19:24:27	266.2401, 5.2296	13:09:24	Setting	82
	2020-02-27, 01:52:08	$\frac{200.2101, 0.2200}{166.8508, 5.6676}$	12:59:31	Rising	83
	2020-02-27, 02:52:38	336.6918, 6.6537	01:19:23	Setting	84
NuSTAR/FPM	2020-02-27, 03:28:45	142.6076, 5.7239	12:59:09	Rising	83
(10602002002)	2020-02-27, 03:28:49	312.4440, 6.5964	01:19:00	Setting	84
	2020-02-27, 04:25:15	118.3693, 5.7626	12:58:50	Rising	83
	2020-02-27, 05:05:23	288.2054, 6.5555	01:18:42	Setting	84
NuSTAR/FPM (10602002004)	2020-02-27, 00:05:55	$\frac{288.2054, 0.3555}{187.4582, 6.3583}$	12:54:41	Rising	85
	2020-02-28, 00:24:32	357.2962, 5.9578	01:14:32	Setting	86
	2020-02-28, 01:25:22 2020-02-28, 02:01:29			Rising	
		163.2149, 6.4171	$\begin{array}{c} 12{:}54{:}20\\ 01{:}14{:}11 \end{array}$		85 86
	2020-02-28, 03:01:59	333.0528, 5.9013 138.0766 6.4582		Setting Rising	86 85
	2020-02-28, 03:38:07	138.9766, 6.4582	12:54:01		85 86
	$\frac{2020-02-28,\ 04:38:37}{2020,\ 08,\ 28,\ 00:25:02}$	308.8104, 5.8645	01:13:50	Setting	86
$\operatorname{NuSTAR/FPM}(10602002006)$	2020-08-28, 09:35:02	231.5389, 3.8916	01:01:10	Rising	87
	2020-08-28, 10:36:17	44.1504, 15.3800	13:32:53	Setting	88
	2020-08-28, 11:11:39	207.3275, 3.8718	01:00:56	Rising	87
	2020-08-28, 12:12:54	19.9219, 15.3664	13:32:35	Setting	88
	2020-08-28, 12:48:17	183.1217, 3.8242	01:00:46	Rising	87

 b Latitude and longitude of the tangent point at 100 km altitude.

^cLocal time of the tangent point at 100 km altitude.

Instrument	UT^a	Tangent $point^b$	Local time ^{c}	Type	Grou
(Obs.ID)	(HH:MM:SS)	Long, Lat (°)	(HH:MM:SS)	01	-
· · · ·	2020-08-28, 13:49:31	355.6977, 15.3505	13:32:17	Setting	88
NuSTAR/FPM (10602002008)	2020-08-29, 04:54:34	301.0417, 3.4484	00:58:42	Rising	89
	2020-08-29, 05:55:45	113.4503, 15.2920	13:29:32	Setting	90
	2020-08-29, 06:31:11	276.8268, 3.4309	00:58:28	Rising	89
	2020-08-29, 07:32:22	89.2221, 15.2732	13:29:15	Setting	90
	2020-08-29, 08:07:49	252.6215, 3.3880	00:58:18	Rising	89
	2020-08-29, 09:09:00	64.9998, 15.2813	13:28:59	Setting	90
NuSTAR/FPM (10702303002)	2021-02-24, 02:02:25	162.7668, 15.4134	12:53:29	Rising	91
	2021-02-24, 03:03:38	335.4311, 3.9672	01:25:21	Setting	92
	2021-02-24, 03:39:02	138.5451, 15.4127	12:53:12	Rising	91
	2021-02-24, 04:40:16	311.2310, 4.0295	01:25:10	Setting	92
	2021-02-24, 05:15:39	114.3234, 15.4115	12:52:55	Rising	91
	2021-02-24, 06:16:53	287.0255, 4.0638	01:24:59	Setting	92
NuSTAR/FPM (10702303004)	2021-02-24, 19:45:11	256.3431, 15.4164	12:50:32	Rising	93
	2021-02-24, 20:46:28	69.1889, 4.4436	01:23:12	Setting	94
	2021-02-24, 21:21:48	232.1256, 15.4122	12:50:17	Rising	93
	2021-02-24, 22:23:05	44.9830, 4.4811	01:22:59	Setting	94
	2021-02-24, 22:58:24	207.9022, 15.4366	12:49:59	Rising	93
	2021-02-24, 23:59:42	20.7811, 4.5173	01:22:49	Setting	94
NuSTAR/FPM	2021-08-28, 15:50:19	135.8574, 8.4183	00:53:44	Rising	95
	2021-08-28, 16:50:49	305.8260, 4.1961	13:14:07	Setting	96
	2021-08-28, 17:26:55	111.6184, 8.4748	00:53:22	Rising	95
(10702303006)	2021-08-28, 18:27:25	281.5903, 4.1548	13:13:45	Setting	96
(2021-08-28, 19:03:31	87.3795, 8.5313	00:53:02	Rising	95
	2021-08-28, 20:04:01	257.3587, 4.1121	13:13:27	Setting	96
	2021-08-29, 07:56:20	253.4673, 8.9665	00:50:12	Rising	97
	2021-08-29, 08:56:51	63.5047, 3.8224	13:10:51	Setting	98
NuSTAR/FPM	2021-08-29, 09:32:56	229.2247, 9.0214	00:49:49	Rising	97
(10702303008)	2021-08-29, 10:33:27	39.2736, 3.7825	13:10:32	Setting	98
	2021-08-29, 11:09:32	204.9864, 9.0780	00:49:27	Rising	97
	2021-08-29, 12:10:03	15.0386, 3.7447	13:10:11	Setting	98
	2022-02-24, 02:33:19	160.0056, 4.0911	13:13:19	Rising	99
	2022-02-24, 03:34:33	332.6630, 15.2855	01:45:11	Setting	100
NuSTAR/FPM	2022-02-24, 04:09:54	135.8067, 4.0655	13:13:06	Rising	99
(10802303002)	2022-02-24, 05:11:08	308.4491, 15.2763	01:44:54	Setting	100
	2022-02-24, 05:46:30	111.6091, 4.0102	13:12:56	Rising	99
	2022-02-24, 06:47:43	284.2311, 15.2684	01:44:38	Setting	100
Hitomi/HXI	2016-03-25, 14:52:43	144.4674, 36.2736	00:30:34	Setting	101

 $^b\mathrm{Latitude}$ and longitude of the tangent point at 100 km altitude.