Multi-pulse corona discharges in thunderclouds observed in optical and radio bands

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Abstract

How lightning initiates inside thunderclouds remains a major puzzle of atmospheric electricity. By monitoring optical emissions from thunderstorms, the Atmosphere-Space Interactions Monitor (ASIM) onboard the International Space Station is providing new clues about lightning initiation by detecting Blue LUminous Events (BLUEs), which are manifestations of an enigmatic type of electrical discharge that sometimes precedes lightning and is named "fast breakdown". Here we combine optical and radio observations from a thunderstorm near Malaysia to uncover a new type of event containing multiple optical and radio pulses. We find that the first optical pulse coincides with a strong radio signal in the form of a Narrow Bipolar Event (NBE) but subsequent optical pulses, delayed some milliseconds, have weaker radio signals, possibly because they emanate from a horizontally oriented fast breakdown which does not trigger full-fledged lightning. Our results cast light on the differences between isolated and lightning-initiating fast breakdown.

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Key Points:

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14	•	Optical multi-pulse corona discharges coincide with Narrow Bipolar Events and their
15		subsequent pulses.
16	•	Subsequent optical pulses are related to horizontally oriented fast breakdowns which
17		emitted faint radio signals.
18	•	The class of horizontally oriented fast breakdowns might play a significant role in the

initiation of the lightning leaders.

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20 Abstract

How lightning initiates inside thunderclouds remains a major puzzle of atmospheric electricity. 21 By monitoring optical emissions from thunderstorms, the Atmosphere-Space Interactions Moni-22 tor (ASIM) onboard the International Space Station is providing new clues about lightning initiation 23 by detecting Blue LUminous Events (BLUEs), which are manifestations of an enigmatic type of 24 electrical discharge that sometimes precedes lightning and is named "fast breakdown". Here we 25 combine optical and radio observations from a thunderstorm near Malaysia to uncover a new type of 26 event containing multiple optical and radio pulses. We find that the first optical pulse coincides with 27 a strong radio signal in the form of a Narrow Bipolar Event (NBE) but subsequent optical pulses, 28 delayed some milliseconds, have weaker radio signals, possibly because they emanate from a hori-29 zontally oriented fast breakdown which does not trigger full-fledged lightning. Our results cast light 30 on the differences between isolated and lightning-initiating fast breakdown. 31

32 Plain Language Summary

One of the biggest mysteries in the atmospheric sciences is to understand how lightning is 33 initiated inside thunderclouds. By combining observations in optical and radio bands, our work 34 uncovers a yet-unreported type of lightning process: multi-pulse corona discharges. For the first 35 time, we cast light on the differences between the isolated and lightning-initiating fast breakdown 36 (an enigmatic type of electrical discharge that is likely present in all lightning initiation events). Our 37 results indicate that there is an unexpected class of horizontally oriented fast breakdown discharges 38 between those that are fully isolated and those that initiate a leader. They have been ignored by all 39 the radio observations so far due to their faint radio signals. However, this would be the class of 40 breakdowns that play a significant role in the initiation of the lightning leaders. 41

42 **1 Introduction**

Narrow bipolar events (NBEs) are short, strong radio pulses emitted by thunderclouds (Smith 43 et al., 1999, 2004). Interferometric (Rison et al., 2016) as well as optical, space-based observations 44 (Soler et al., 2020; Li et al., 2021) indicate that their source, with an spatial extent of hundreds of 45 meters to a few kilometers and a duration of some tens of microseconds, is a poorly understood type 46 of electrical breakdown produced by the simultaneous propagation of 10^8 to 10^9 cold filamentary 47 discharges called streamers (Li et al., 2021; N. Liu et al., 2019; Nijdam et al., 2020). This type of 48 electrical discharge, called fast breakdown, is likely present in all lightning initiation events (Attana-49 sio et al., 2021; Sterpka et al., 2021) and even during flash development, although only under a still 50 undefined set of conditions it is sufficiently strong to manifest itself as an NBE. 51

NBEs normally occur in isolation (Rison et al., 2016; Kostinskiy et al., 2020) but a small frac-52 tion of them, named Initiation-type NBEs (INBEs) (Wu et al., 2014) are the initial event of a light-53 ning flash. Sometimes NBEs are followed by subsequent radio pulses associated with leaders (hot 54 lightning channels); these pulses, sometimes called Initial Breakdown Pulses (IBPs) (e.g., Kostin-55 skiy et al., 2020; Lyu et al., 2019) or Preliminary Breakdown pulses (PBs) (e.g., Kolmašová et al., 56 2018; Wu et al., 2015), precede by a few milliseconds an intracloud (IC) or cloud-to-ground (CG) 57 lightning discharge. Whereas isolated NBEs are strong emitters of Very High Frequency (VHF) ra-58 diation (3000 - 300 000 W) (Rison et al., 2016; Kostinskiy et al., 2020), initiation-type NBEs, even 59 with pulse widths similar to isolated NBEs, present smaller amplitudes and weaker VHF signals 60 (3 – 300 W) (Rison et al., 2016; Kostinskiy et al., 2020; Wu et al., 2014; Bandara et al., 2019). 61

Most of this knowledge about NBEs and fast breakdown derives from radio observations but these have been recently complemented by optical detections from space. The Modular Multispectral Imaging Array (MMIA) instrument of the Atmosphere-Space Interactions Monitor (ASIM), operating since 2018 from the International Space Station (ISS), has detected a large number of Blue LUminous Events (BLUEs) globally (Soler et al., 2021), which are optical pulses with a strong 337 nm signal, associated with streamer discharges, but lacking the 777 nm emissions that would indicate the presence of a hot leader (Soler et al., 2020; Li et al., 2021; F. Liu, Lu, et al., 2021). 69 Combined radio and optical studies provide strong evidence that every NBE has a BLUE counterpart

(Soler et al., 2020; Li et al., 2021; F. Liu, Lu, et al., 2021). Hence BLUEs are another manifestation
 of fast breakdown.

Novel optical observations help to elucidate the context in which fast breakdown occurs. Soler 72 et al. (2020) found that a significative fraction of BLUEs contained more than one optical pulse 73 with a delay between pulses of a few milliseconds. Here we combine observations from MMIA 74 and from ground-based Very Low Frequency/Low Frequency (VLF/LF) radio sensors to investigate 75 a number of multi-pulse BLUEs from a thunderstorm near Malaysia. We find that in all these 76 77 events the first optical pulse has an unambiguous NBE counterpart. Remarkably, we also find that the subsequent optical pulses, even though they have optical amplitudes comparable to the leading 78 pulse, are accompanied by faint, sometimes undetectable, radio emissions. The implication is that 79 NBEs are frequently followed by a new type of event that has escaped detection until now. Our 80 observations are compatible with these events being horizontally directed fast breakdown which 81 does not initiate a leader. 82

2 Instruments and Observations

Since its commissioning in 2018, the Modular Multispectral Imaging Array (MMIA) of the 84 Atmosphere-Space Interactions Monitor (ASIM) has been observing Earth thunderstorms from space 85 in a nadir-viewing geometry from the International Space Station (ISS) (Chanrion et al., 2019; Neu-86 bert et al., 2019). MMIA contains three photometers with a sampling rate of 100 ksamples/s: one 87 photometer in the ultraviolet (UV) band at 180-230 nm, one in the near-UV at the strongest spectral 88 line of the nitrogen second positive system (337 nm) and one at the strongest lightning emission 89 band (777.4 nm). The last two photometers are complemented with cameras sensitive to the same 90 wavelengths. The spatial resolution of the cameras on the ground is around $400 \text{ m} \times 400 \text{ m}$ and they 91 have an integration time of 83.3 ms. 92

Our radio-frequency data comes from a broadband Very Low Frequency/Low Frequency (VLF/LF) magnetic sensor that operates at 400 Hz to 400 kHz and is located at Universiti Teknikal Malaysia Melaka (UTeM), Malacca, Malaysia (Zhang et al., 2016; Ahmad et al., 2017). To compare MMIA and VLF/LF data correcting for MMIA's time uncertainty we matched MMIA pulses with data from the GLD360 lightning detection network (Said & Murphy, 2016), obtaining a time shift for MMIA with respect to the ground-based VLF/LF measurements of (-15.00 ± 0.65) ms (see Figure S1 in Supplemental Material).

On the evening of April 30, 2020, there were 16 Blue LUminous Events (BLUEs) simultaneously observed by the 337 nm photometer and its filtered camera of MMIA, as well as the groundbased VLF/LF sensor near Malaysia (Ahmad et al., 2017), with absent or negligible signals in both the 180 - 230 nm photometer and in the 777.4 nm photometer and filtered camera. Among the events, there are 8 single-pulse BLUEs (Soler et al., 2020; Li et al., 2021) and 8 multiple-pulse BLUEs. We focus mainly on the multiple-pulse BLUEs.

To illustrate the thunderstorm context of the BLUEs, figure 1 shows the distribution of intr-106 acloud (IC)/cloud-to-ground (CG) lightning with the 8 multi-pulsed BLUEs superimposed on the 107 cloud Top Blackbody Brightness Temperature (TBB, given in Kelvin) provided by the Himawari-8 108 satellite (Bessho et al., 2016) in ten-minute intervals starting at 17:40:00 UTC, 17:50:00 UTC and 109 18:00:00 UTC. Because GLD360 only captured 3 events, we determine the locations of multiple-110 pulse BLUEs by projecting the brightest pixel of the of 337-nm camera images into geo-coordinates 111 (latitude and longitude). We also show the GLD360-detected lightning flashes surrounding our 112 events, including their classification as positive or negative, CG or IC. The BLUEs, which occurred 113 in the time period from 17:50:00 to 17:51:00 UTC, are accompanied by the highest concentration of 114 IC and CG lightning with an apparent decrease of the negative CG flash rate. 115

The detailed features of all multiple-pulse BLUEs are listed in Table 1. As an example, the multiple-pulse BLUE with ID 1 is presented in Figure 2, with other cases given in Figure S2-S9 in the Supplemental Material. The multiple-pulse BLUEs include one primary BLUE pulse and one or several subsequent BLUE pulses within 1 ms to 9 ms. In most cases, both rise time and time duration of the subsequent BLUE pulses are found to be similar or somewhat shorter than those corresponding to the primary BLUEs; the irradiances of the primary BLUEs are higher than those of the subsequent BLUEs pulses by about a factor of two. All the BLUEs are isolated from other IC or CG lightning discharges detected by either GLD360 or the 777.4 nm photometer and filtered camera of MMIA within at least 100 ms. That means that they do not initiate any leader activity and therefore would be classified as isolated NBEs.

126 3 Results

As shown in Figure 2 and Figures S2-S9 in the Supplemental Material, all the multiple-pulse BLUEs are associated with an isolated positive NBE sometimes accompanied by faint subsequent radio pulse trains. Figure 3 demonstrate the correlation of the horizontal *B* fields ($B_{\rm EW}$ and $B_{\rm NS}$) for both the positive NBE and its subsequent pulses for event 1 (See Figures S11-S19 in Supplemental Materials for other cases).

As shown in figure 3(d), the NBE pulses exhibit a tight linear relationship of the horizontal 132 B fields, something that is expected for the horizontally propagating ground wave of a vertical dis-133 charge. However, in the subsequent pulses the horizontal components of the field trace elliptical 134 curves (see Figure 3(h)). As this is a projection into the horizontal plane of the trajectory of the 135 magnetic field in the plane perpendicular to the wave propagation, the implication is that the wave 136 is elliptically polarized. One explanation for this behaviour is that the electric current responsible 137 for the subsequent pulses is oriented horizontally: in that case the ground wave is absent and the 138 first signal to reach the detector is the wave reflected in the ionosphere. Due to the anisotropy intro-139 duced by the geomagnetic field, different components of the wave electromagnetic fields propagate 140 differently in the magnetized plasma of the lower ionosphere, introducing a phase shift between dif-141 ferent components. This would explain both the weak amplitude and the elliptical polarization of 142 the observed signal. 143

We tested this hypothesis by means of a Full Wave Method (FWM) electromagnetic model 144 (Lehtinen & Inan, 2008, 2009) (see Methodology in Supplemental Material for further details). 145 We simulated the signals produced by both vertical and horizontal dipole current sources imitating 146 the event-detector geometry of our observations. The results, shown in figure 3, reproduce the 147 qualitative features of the waveform measured by the ground-based VLF/LF. For the case of NBE, 148 both ground wave and its first and second reflected sky waves can be clearly seen in figure 3(a, c) 149 with a linear relationship between the magnetic field components B_x and B_y (see figure 3(b, d)). For 150 the subsequent pulse trains, the ground wave is absent and the magnetic field components B_x and 151 $B_{\rm y}$ of the first and second sky waves trace elliptical curves (see figure 3(e,f,g,h)). These simulations 152 support our hypothesis of a horizontal discharge triggered by the primary, vertical fast breakdown 153 that generates the NBE. 154

To better understand the multiple-pulse BLUEs, we simulated the propagation of their opti-155 cal emissions within the thundercloud with both an analytical diffusion model and a Monte Carlo 156 model (Li et al., 2020) (see Methodology in Supplemental Material for further details). Table 2 157 lists the inferred parameters of the multiple-pulse BLUEs. The estimated depths L (relative to the 158 cloud top) of the BLUEs are derived by the analytical diffusion model based on the 337-nm pho-159 tometer signals of MMIA, assuming a cloud particle radius $r = 20 \,\mu m$ and droplet number density 160 $N_d = 10^8 \text{ m}^{-3} to3 \times 10^8 \text{ m}^{-3}$. The altitudes H of the NBEs are evaluated based on the ground-based 161 VLF/LF radio signals by using the simplified ray-theory method (Smith et al., 1999, 2004), which 162 involves an uncertainty of about ± 1 km (Li et al., 2020). 163

We see in Table 2 that the positive NBEs are located at relatively high altitudes with H = 165 16 km*to*18 km, which are above the median heights of the majority of positive NBEs (about 13 km) reported in the literature (Smith et al., 2004; Wu et al., 2014; F. Liu, Zhu, et al., 2021). This suggests that the occurrence of multi-pulsed BLUE events may be related to the rare occurrence of highaltitude positive NBEs (Wu et al., 2014). As shown in Table 2, our modeling indicates that the subsequent BLUE pulses are located at similar or slightly higher altitudes than the primary BLUEs, with a depth of L = 1 kmto3 km measured from the cloud top. This low depth explains why MMIA not only detects the primary BLUEs but also their subsequent BLUE pluses. The optical energy in the 337-nm band emitted by fast breakdown of the primary NBE is about 10³ J, which involves around 10⁸ streamer branching events evaluated as discussed by Li et al. (2021). The ratio of the irradiances and the streamer branches is expected to have a roughly linear relationship, thus the secondary BLUEs involve about 5 × 10⁷ streamer breaching events.

We can shed some light into what differentiates multiple-pulse from single-pulse BLUEs by 176 looking at the electrical currents of the fast breakdown where they originate. We estimated the 177 current moments (M_i) of all the 16 BLUEs with sufficient data in the investigated thunderstorm, 178 including the 8 multiple-pulse BLUEs and the 8 single-pulse BLUEs. Starting from the azimuthal 179 magnetic field component, B_{ϕ} , we solved the inverse convolution problem using the Uman's equa-180 tion (Uman et al., 1975) shown in (see Methodology and Figure S10 in the Supplemental Material 181 for further details). Figure 4 shows a linear relationship between the amplitude of the azimuthal 182 magnetic field component B_{ϕ} and the estimated current moment M_i . Despite one outlier far from the 183 other multiple-pulse BLUEs with ID 7, all the single-pulse and multiple-pulse BLUEs are well separated into two clusters. The primary BLUEs of the multiple-pulse BLUEs have relatively weaker 185 current moments and amplitudes than those corresponding to the single-pulse BLUEs. This is rem-186 iniscent of initiation-type NBEs, which also have weaker source currents. We emphasize however 187 that all the multiple-pulse NBEs that we analyzed are isolated NBEs, separated from any IC or CG 188 lightning discharges detected by either GLD360 or the 777.4-nm band of MMIA within at least 189 100 ms. They are also located at relatively high altitudes nearby cloud tops, unlike the INBEs nor-190 mally located deeply inside the thundercloud (Smith et al., 2004; Wu et al., 2014). 191

¹⁹² 4 Discussion and conclusions

Our results suggest that a fraction of so-called isolated NBEs, which do not initiate leader activity and are therefore not the starting event of a lightning flash, nevertheless trigger subsequent fast breakdown activity. We now discuss some implications of these findings.

Turning first to the thunderstorm environment that surrounds the analyzed multiple-pulse BLUEs, we notice from the lightning distribution in Figure 1 that the rate of negative CGs exceeds that of positive ones by about a factor three, which suggests that the thunderstorm has a dipole-like electrical structure with the positive charge above the negative charge (Wilson, 1956). However, the charge structures can be more complex in the convective region of the thunderstorm (Stolzenburg et al., 1998). Both IC and CG flash rates vary dramatically during the time interval when the BLUEs occurred.

The negative CG rate decreases sharply as the rate of the positive ICs increases, and later the 203 rates of all ICs and CGs start to increase. The dramatic change of the lightning rates suggests that the 204 lightning discharges are produced inside a thunderstorm with deep convective updrafts (Wiens et al., 205 2005; Petersen & Rutledge, 1998). The ring structures shown in Figure S5 and S7 further illustrate 206 that there is a cloud turret extending above the cloud top surface during the occurrence interval of 207 the BLUEs (Luque et al., 2020). One hypothesis for this is that the positive NBEs are produced 208 between the positive charge lifted to relatively high altitude by the strong updraft and the negative 209 screening charge layer which lies close to the overshooting region of the cloud (MacGorman et al., 210 2017). 211

Our results are connected to the problem of lightning initiation and the nature of fast breakdown. If our interpretation is correct, there is an intermediate class of fast breakdown discharges between those that are fully isolated and those that initiate a leader. This would be the class of breakdowns that trigger subsequent discharges which do not promote to leaders. It is unclear whether these discharges, with a primarily horizontal orientation and associated with faint radio pulses, are similar to the primarily vertical fast breakdown events described previously in the literature (Rison et al., 2016; Tilles et al., 2019; Lyu et al., 2019; N. Y. Liu & Dwyer, 2020; Huang et al., 2021). It is also unknown whether NBE-initiated leaders are initiated by horizontal fast breakdown. These questions should be addressed by future research.

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231 Open Research

The Modular Multispectral Imaging Array (MMIA) level 1 data is proprietary and not cur-232 rently available for public release. Interested parties should direct their request to the ASIM Facility 233 Science Team (FST). ASIM data request can be submitted through: https://asdc.space.dtu.dk by 234 sending a message to the electronic address asdc@space.dtu.dk. The Himawari-8 gridded data in 235 this study is public to the registered users and supplied by the P-Tree System, Japan Aerospace Ex-236 ploration Agency (JAXA)/Earth Observation Research Center (EORC) (https://www.eorc.jaxa 237 . jp/ptree/). The data that support the findings of this study are openly available in https:// 238 doi.org/10.5281/zenodo.6123813. The Cloudscat Monte Carlo simulation code (Luque et al., 239 2020) is available at https://github.com/aluque/CloudScat.jl. The stanford Full-Wave 240 Method (StanfordFWM) code (Lehtinen & Inan, 2008, 2009) is available at https://gitlab 241 .com/nleht/stanfordfwm/. 242

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Table list 366

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17:50:55.181

ID	MMIA UTC time (source)	Primary BLUE			S	Time difference		
		Irradiance $(\mu W/m^2)$	Rise time ^a (ms)	Total time duration ^b (ms)	Irradiance $(\mu W/m^2)$	Rise time ^a (ms)	Total time duration ^b (ms)	(ms)
1	17:50:08.246	4.54	0.18	1.25	2.5	0.05	0.86	3.1
2	17:50:09.645	5.57	0.30	2.25	2.76 ^c	0.58 ^c	1.66 ^c	6.0
3	17:50:19.447	12.42	0.17	1.53	6.08	0.14	1.61	1.7
4	17:50:24.704	10.28	0.79	6.50	3.52	0.14	3.37	9.4
5	17:50:35.617	4.54	0.59	2.45	4.54	0.68	2.64	3.3
6	17:50:43.238	8.69	0.79	3.60	4.54	0.79	3.75	2.6
7	17:50:46 157	10.81	0.06	1 93	3.01	0.22	1 15	73

3.01°

0.41^c

2 559

14

Table 1. The detailed features of the multiple-pulse BLUEs. The detection times of MMIA have been corrected to the source time with respect to the BLUE locations.

^a Rise time is the time taken for the amplitude of a MMIA photometer signal to rise from 10% to 90%.

0.12

3.01

^b Time duration is the time interval for the amplitude of a MMIA photometer signal to rise from 10 % and fall to 10%.

1.19

^c The first subsequent BLUE pulse is used to evaluate the rise time and time duration since the photometer signal includes multiple pulses (see Figure S3 and S9 in Supplemental Material for details).

Table 2. The inferred features of the multiple-pulse BLUEs. The altitudes (H) are estimated using the simplified ray-theory method proposed by (Smith et al., 1999, 2004) based on the ground-based VLF/LF sferics. The depths (L) relative to cloud top boundary are evaluated by using the analytical diffusion model in equation (2) in Supplemental Material based on the 337-nm photometer signals of MMIA.

ID	Parameters				Subsequent pulses			
10	Distance d (km)	$\binom{N_d}{(m^{-3})}$	<i>R</i> (μm)	337-nm optical energy (J)	Streamer branching events	Altitude H (km)	Depth L (km)	Depth L (km)
1	495	3×10^{8}	20	1.3×10^{3}	1.0×10^{8}	17.68	0.96	0.66
2	494	2×10^8	20	3.7×10^{3}	2.9×10^{8}	16.67	1.50	1.74 ^a
3	489	1×10^8	20	6.4×10^{3}	5.0×10^{8}	17.03	1.85	1.45
4 ^b	486	-	-	-	-	15.55	-	-
5 ^b	486	-	-	-	-	15.55	-	-
6 ^b	480	-	-	-	-	15.87	-	-
7	482	1×10^8	20	3.8×10^{3}	3.0×10^{8}	17.95	1.30	2.79
8°	477	-	-	-	-	17.33	-	-

^a The first subsequent BLUE pulse is used to obtain the fitting parameters since the photometer signal includes multiple subsequent BLUE pulses (see Figure S3 in Supplemental Material for details).

^b There is a small pulse on the rising edge of light-curve that distorted the fit process (See Figure S5, S6 and S7 in Supplemental Material for details).

^c The photometer signal is too noisy to be fitted (See Figure S9 in Supplemental Material for details).

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Figure 1. Distribution of the intracloud (IC)/cloud-to-ground (CG) lightning with 8 multiple-pulse BLUEs superimposed on the cloud Top Blackbody Brightness temperature (TBB, given in K) in the region of interest and the zoomed-in rectangular region, indicated with the dotted black line, per 10 minutes at time 17:40:00 UTC (a,d), 17:50:00 UTC (b,e), and 18:00:00 UTC (c,f). Numbers of different types of lightning events are shown in (g): positive CGs (+CGs), negative CGs (-CGs), positive ICs (+ICs) and negative ICs (-ICs). The multiple-pulse BLUEs occurred in the time period from 17:50:00 to 17:51:00 UTC marked in blue shaded region in (g). The ground-based VLF/LF sensor at Malaysia is shown as a black triangle in panels (a, b, c). The footprints of ASIM are shown with a black dashed line.



Figure 2. Comparison between MMIA photometer irradiance (blue: 337 nm, yellow: 180-230 nm and red: 777.4 nm) and the modeling results of the analytical diffusion model (black) and Cloudscat model (green) on a linear (a) and logarithmic (b) scale, shown together with the North-south and East-west magnetic field components B_{NS} and B_{EW} (c) and its norm $|B| = \sqrt{B_{NS}^2 + B_{EW}^2}$ (d), recorded at the ground-based VLF/LF sensor nearby Malaysia for event 1. Also shown: the image detected by the 337-nm filtered camera of MMIA (e) and the simulated image of the Cloudscat model (f). The start time (corrected to the source time with respect to the locations) for NBE and its subsequent pulses is marked with the dashed black line, within the time difference 3.1 ms with ±0.65 ms uncertainty (gray shadowed region).



Figure 3. Comparison of normalized magnetic field components between the simulation and observation corresponding to the NBE(a,b,c,d) and the subsequent pulses (e,f,g,h) of multiple-pulse BLUE for event 1 (see the black rectangle with the NBE and subsequent pulses labels marked in the figure 2(c)). The magnetic field components of B_x and B_y are calculated by the FWM modeling and the North-South and East-West magnetic field components of B_{EW} and B_{NS} are measured by the ground-based VLF/LF sensor at Malaysia. The correlation between the different components of the simulated magnetic field (B_x and B_y) and the measured magnetic field components (B_{EW} and B_{NS}) for both NBE (b,d) and the subsequent pulses (f,h) are also shown in the figure. The ground wave and two ionospheric reflected sky waves marked as G, 1S, and 2S.



Figure 4. Correlation between the amplitude of the azimuthal magnetic field component B_{ϕ} and the inferred current moment M_i for all the detected BLUEs (8 single-pulse BLUEs (blue dots) and 8 multiple-pulse BLUEs analyzed in the paper (red dots)). The outlier of the multiple-pulse BLUEs corresponds to the event with ID 7 in Figure S8 in Supplemental Materials.

Supplemental Material for "Multi-pulse corona discharges in thunderclouds observed in optical and radio bands"

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10 Contents of this file

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Text S1: Methodology

MMIA observation simulation

In the simulation, we assumed the optical BLUE sources are impulsive and localized point sources inside a homogeneous isotropic cloud. The scattering and absorption processes of the photons propagating through the cloud are evaluated based on two different approaches including an analytical diffusion model and a Monte Carlo simulation (Luque et al., 2020).

¹⁸ We first fit the 337-nm photometer signal of MMIA to infer the depth (relative to the cloud ¹⁹ top) *L* of point-like optical sources inside a homogeneous and infinite cloud. To simplify the ²⁰ simulation, we neglect Rayleigh scattering and background absorption by adopting a homoge-²¹ neous collision rate $v = cN_dQ_{ext}\pi R^2$, where N_d is a droplet number density with particle radius ²² *R*.

Soler et al. (2020) proposed a simplified analytical expression based on the diffusion approx-23 imation proposed by Koshak et al. (1994), named first-hitting-time model, to infer the depth 24 (relative to the cloud top) of the point-like optical sources located deep inside the cloud. How-25 ever, here we add more details by using equation (27) of Luque et al. (2020) to include Mie 26 scattering. Mie scattering corresponding to the wavelength of 337 nm is characterized by three 27 parameters: the scattering asymmetry parameter g = 0.88, the respective extinction coefficient 28 Q_{ext} = 2.06 and the single-scattering albedo ω_0 = 0.99 which is close to unity and describes 29 the probability that a photon re-emits after a scattering event. These parameters are obtained 30 by solving the Mie problem with the open source MieScatter.jl code (Wilkman, 2013; Li et al., 31 2020). 32

The total flux per unit time of single-pulse BLUEs $F_{single}(t)$ for the analytical diffusion model is (see more details in (Luque et al., 2020)):

39

$$F_{\text{single}}(t) = \frac{e^{-t/\tau_A - \tau_D/t}}{\sqrt{\pi}\tau_D} (t/\tau_D)^{-3/2}$$
(1)

where the photon absorption time $\tau_A = \frac{1}{\nu(1-\omega_0)}$ and the characteristic time $\tau_D(t) = \frac{L^2}{4D}$ with the depth *L* and the diffusion coefficient $D = \frac{c^2}{\nu(1-\omega_0)}$.

The equation for multiple-pulse BLUEs, denoted as $F_{\text{multiple}}(t)$, is a sum of $F_{\text{single}}(t)$ as follows:

$$F_{\text{multiple}}(t) = \sum_{i=1}^{M} F_{\text{single}}(t)$$
(2)

where M is the number of the BLUE pulses used in the fitting process.

We further simulate the 337-nm photometer signal and the corresponding camera image detected by MMIA using a Monte Carlo code CloudScat.jl (Luque et al., 2020) by considering a localized optical point source inside a homogeneous cloud at an altitude that spans from 7 km to the cloud top boundary. The depth *L* of the optical source is derived from the analytical diffusion model with the scattering parameters listed in Table 2.

FWM simulation

We simulate the radio waveform of both NBEs and the subsequent pulse trains of the multiplepulse BLUEs using the Stanford Full Wave Method (StanfordFWM) code of Lehtinen & Inan (2008, 2009). The source is assumed to be a vertical dipole for the NBEs and a horizontal dipole for the subsequent pluse trains with the current moment of 1 A m located at an altitude of 10 km (selected for simplicity, neglecting the small differences with the estimated source altitudes) emitting at frequencies between 10 kHz*to*100 kHz. The waveform of the current moment is assumed to be the bi-Gaussian function:

$$I(t) = I_0(e^{-t^2/\tau_1^2} - e^{-t^2/\tau_2^2}),$$
(3)

where the rise time τ_1 and the fall time τ_2 . The electric current moment for the NBEs is 54 $I_0 = [0, 0, 1]$ corresponding to a vertical dipole along z-axis. The electric current moment 55 for subsequent pulse trains is $I_0 = [\sqrt{2}/2, \sqrt{2}/2, 0]$, i.e., represents a horizontal dipole with an 56 angle of 45° with respect to the positive x-axis. Note that the angle of 45° here only represent an 57 example of the cases since we don't know the exact angle of the horizontally oriented sources. 58 The ionosphere is assumed to be horizontally stratified at altitudes between 0 km to 100 km and 59 treated as a magnetized plasma. In order to reflect the real propagation geometry, we assumed 60 the propagation in positive x-direction corresponding to the north component of the geomag-61 netic field. According to the International Geomagnetic Reference Field (IGRF) model (Alken 62 et al., 2021), the geomagnetic field in our case has the total intensity about 42 000 nT along the 63 positive y-axis. In the simulation, we only consider the electrons since the effect of the ions 64 can be neglected in the lower ionosphere in the frequency range of interest. The electron den-65 sity profile is obtained using the International Reference Ionosphere (IRI) model (Bilitza et al., 66 2014) at the location of the BLUEs at 17:50:00 UTC on April 30, 2020. The ground is assumed 67 to be perfectly conducting without considering the effect of the ground conductivity due to the 68 BLUEs occurred over the ocean. By following the geometry of the observation, the observed 69 sensor at Malaysia is located at about 500 km away from the BLUEs (see figure 1(b)). After 70 the results of the FWM modeling at different frequencies are obtained, we applied the inverse 71 Fourier transform to calculate the time-domain waveforms of the x and y components of the 72

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magnetic field at the observation point. The comparison between the StanfordFWM results and
 the observation are shown in figure 3.

VLF/LF sferic simulation

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We estimate the current moment $M_i(t)$ for the primary BLUE pulse of the multiple-pulse 75 BLUEs based on the azimuthal magnetic field component B_{ϕ} measured by the ground-based 76 very low frequency/low frequency (VLF/LF) sensor nearby Malaysia. In the calculation, we 77 assumed the source as a vertical dipole located at an altitude of H away from the sensor at 78 a distance of d (see Table 2). The ground is assumed to be perfectly conducting because the 79 VLF waves propagation from the BLUEs occurred over the ocean. We calculate the azimuthal 80 magnetic field component B_{ϕ} by using Uman's equation (Uman et al., 1975) and compare it with 81 the observation. The source current moments can be inferred by solving the inverse convolution 82 problem (Cummer & Inan, 2000; Cummer, 2003): 83

$$B(t) = \int_{-\infty}^{\infty} M_i(t)h(t-\tau)d(\tau),$$
(4)

where *B* is the measured magnetic field waveform, M_i is the source current moment and h(t)is the propagation response evaluated from the modeling results of Uman's equation. In the modeling, the waveform of the source current is also assumed to be the bi-Gaussian function in equation (3). The inferred current moments M_i and the cumulative charge moments M_q of all multiple-pulse BLUEs are presented in Figure S10.



Figure S1. The systematic time shift of MMIA with respect to the ground-based VLF/LF radio signals calculated by using 16 BLUEs (8 single-pulse BLUEs (black dots) and 8 multiple-pulse BLUEs analyzed in the paper (red dots)) simultaneously detected by the 337-nm photometer and its filtered camera of MMIA and the ground-based VLF/LF sensor nearby Malaysia. The mean value of the MMIA time shift is about -15 ms with the standard deviation ± 0.65 ms.



Figure S2. Comparison between MMIA photometer irradiance (blue: 337 nm, yellow: 180-230 nm and red: 777.4 nm) and the modeling results of the analytical diffusion model (black) and Cloudscat model (green) on a linear (a) and logarithmic (b) scale along with the North-south and East-west magnetic field components B_{NS} and B_{EW} (c), and their sum of the square $B_{NS^2+EW^2}$ (d) from the ground-based VLF/LF sensor nearby Malaysia for event 1. The image detected by 337-nm filtered camera of MMIA (e) and the simulated image of Cloudscat model(f). The start time (refer to source) for NBE and its subsequent pulse is marked in dashed black line within the time difference 3.1 ms with ±0.65 ms uncertainty (gray shadowed region). The inset zoom figures for both primary NBE and its subsequent pulse trains are also given in the figure.



Figure S3. Similar to Figure S2, but for event 2.



Figure S4. Similar to Figure S2, but for event 3.



Figure S5. Photometer irradiance (blue: 337 nm, yellow: 180-230 nm and red: 777.4 nm) of MMIA on a linear (a) and logarithmic (b) scale along with the magnetic field components B_{NS} , B_{EW} (c) and their sum of the square $B_{NS^2+EW^2}$ (d) detected from the ground-based VLF/LF sensor nearby Malaysia for event 4. The image detected by 337-nm filtered cameras of MMIA (e). The start time (refer to source) for NBE and its subsequent pulse is marked in dashed black line with ±0.65 ms uncertainty (gray shadowed region). The inset zoom figures for both primary NBE and its subsequent pulse trains are also given in the figure.



Figure S6. Similar to Figure S5, but for event 5.



Figure S7. Similar to Figure S5, but for event 6.



Figure S8. Similar to Figure S2, but for event 7.



Figure S9. Similar to Figure S5, but for event 8. Note that the zoom-in of the first and second subsequent pulses trains within time difference 1.4 ms and 4.4 ms are also shown in the figure.



Figure S10. The evaluated current moments M_i and charge moments M_q for the primary BLUE pulse of eight multiple-pulse BLUEs listed in Table 1 based on the azimuthal magnetic field component B_{ϕ} measured by the ground-based very low frequency/how frequency (VLF/LF) sensor nearby Malaysia..



Figure S11. The waveform of the North-south and East-west magnetic field component (B_{NS} and B_{EW}) and the correlation between them for both NBE (a,b) and its subsequent pulse trains (c,d) of the multiple-pulse BLUE for event 1.



Figure S12. Similar to Figure S11, but for event 2.



Figure S13. Similar to Figure S11, but for event 3.



Figure S14. Similar to Figure S11, but for event 4.



Figure S15. Similar to Figure S11, but for event 5.



Figure S16. Similar to Figure S11, but for event 6. Note that, as shown in (d), the subsequent pulses trains show a similar linear-like pattern comparing with NBE pulses. It is due to the subsequent pulse trains for the event 6 seems like a negative NBE, however, it is too noisy to identify it through the radio signals (see (c)).



Figure S17. Similar to Figure S11, but for event 7.



Figure S18. Similar to Figure S11, but for both NBE and its first subsequent pulse for event 8.



Figure S19. Similar to Figure S11, but for both NBE and its second subsequent pulse for event 8.

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