A decomposition of the atmospheric and surface contributions to the outgoing longwave radiation

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The outgoing longwave radiation (OLR), which consists of the thermal radiation from both the atmosphere and surface, is of critical importance to the Earth radiation energy budget. To understand the global OLR distribution, it is important to quantify the varying atmospheric and surface contributions. In this work, we present such a quantification using radiative transfer computations based on global reanalysis atmospheric data. By dissecting the OLR simulated following the radiative transfer equation, we quantitatively measure the layer-wise atmospheric contributions to OLR and compare it to the surface contribution in different spectral bands. One focus of this study is on the OLR in the far-infrared, for which new satellites are expected to provide unprecedented measurements. We find that around 45% of the global mean OLR is radiated in the far-infrared and in polar regions the far-infrared contribution can increase to 60%. Our vertical decomposition of OLR discloses that the enhanced far-infrared contribution in the polar regions mainly results from a stronger surface (as opposed to atmosphere) contribution. Our analysis also reveals that the tropopause layer makes a minimum contribution to the OLR, which may be a unique spectroscopic feature of the Earth atmosphere. Clouds are found to reduce the atmospheric contribution in the far-infrared while enhancing it in the mid-infrared.

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The outgoing longwave radiation (OLR), which consists of the thermal radiation from both the atmosphere and surface, is of critical importance to the Earth radiation energy budget. To understand the global OLR distribution, it is important to quantify the varying atmospheric and surface contributions. In this work, we present such a quantification using radiative transfer computations based on global reanalysis atmospheric data. By dissecting the OLR simulated following the radiative transfer equation, we quantitatively measure the layer-wise atmospheric contributions to OLR and compare it to the surface contribution in different spectral bands. One focus of this study is on the OLR in the far-infrared, for which new satellites are expected to provide unprecedented measurements. We find that around 45% of the global mean OLR is radiated in the far-infrared and in polar regions the far-infrared contribution can increase to 60%. Our vertical decomposition of OLR discloses that the enhanced far-infrared contribution in the polar regions mainly results from a stronger surface (as opposed to atmosphere) contribution. Our analysis also reveals that the tropopause layer makes a minimum contribution to the OLR, which may be a unique spectroscopic feature of the Earth atmosphere. Clouds are found to reduce the atmospheric contribution in the far-infrared while enhancing it in the mid-infrared.

(Plain Language Abstract)

OLR plays a fundamental role in Earth's energy budget. We quantify the layer-wise atmospheric contribution to OLR, with a focus on the radiation energy in the far-infrared. Combining the spectral, vertical and geographic perspectives, our analysis identifies the critical atmospheric layers that account for the OLR in different spectral ranges. Our results affirm the importance of far-infrared spectrum for the Earth radiation balance and reveal that the geographic variation of the OLR in far-infrared is mainly driven by a varying surface contribution.

Key Points

1. The higher FIR fraction of OLR in polar region is due to stronger surface contribution.
2. The atmospheric layer around the tropopause makes a minimum contribution to OLR.
3. Cloud radiative effect reduces the atmospheric contribution in FIR and increases it in MIR.

1. Introduction

The outgoing longwave radiation (OLR) at the top of the atmosphere (TOA) is an important component of the Earth's radiation energy budget. The balance between OLR and the net incoming solar radiation determines the energy gain or loss, and thus the thermal state, of the whole climate system. OLR consists of the atmospheric emission and the surface emission transmitted through the atmosphere, which many studies have tried to accurately quantify (Kiehl & Trenberth, 1997; Trenberth et al., 2009; Trenberth & Fasullo, 2012; Stephens et al., 2012; Wild et al., 2013). For example, a widely cited diagram of Kiehl and Trenberth (1997) quantified the surface emission transmitted through the mid-infrared atmospheric window to be 40 W m^{-2}, which was revised by Costa and Shine (2012) to be 22 W m^{-2} using an accurate radiative transfer model. However, this latter number is still subject to the uncertainties due to the use of annually averaged atmospheric profiles in the calculation.

In comparison to the surface contribution, the layer-by-layer atmospheric contribution to OLR has been rarely quantified, despite the foreseeable benefits. Quantifying the contribution of different vertical layers to OLR would help visualize the radiative transfer process in the atmosphere and understand how importantly different parts of the atmosphere influence the TOA radiation balance. Moreover, from the remote sensing point of view, the identification of critical layers where most OLR photons originate from would illuminate which part of the atmosphere the space measurement of OLR is sensitive to. This would elucidate the theoretical basis of passive satellite sounding of the atmosphere. Hence, in this paper, we are motivated to use the latest global reanalysis atmospheric data and accurate radiative transfer calculations to provide an assessment of the vertically decomposed atmospheric contributions, as well as surface contribution, to OLR.

As evidenced by many previous studies, spectrally decomposed OLR provides much richer information about the atmosphere. For example, OLR spectral measurements were found to afford a rigorous test of the simulations of global climate models (GCMs) and provide useful clues for identifying the causes of the model biases (Y. Huang et al., 2007a; Y. Huang & Ramaswamy, 2008; X. Huang et al., 2008; Feldman et al., 2014). The rich information in the OLR spectra also makes it possible to spectrally fingerprint the radiative forcings and feedbacks that drive and modulate the global climate change (Brindley & Bantges, 2016; Harries et al., 2008; Y. Huang et al., 2010a; Y. Huang et al., 2010b; Y. Huang & Ramaswamy, 2009; Y. Huang, 2013; Whitburn et al., 2021). Hence, in addition to the total OLR, we are motivated to analyze spectrally decomposed OLR and how it is contributed by different atmospheric layers. We are especially interested to analyze the OLR with longer wavelength, i.e., in the conventionally termed far-infrared (FIR) spectral region (Harries et al., 2008). The interest in the FIR is motivated by the fact that a large fraction of the OLR energy exists in this spectral region (Harries et al., 2008; X. Huang et al., 2008; Chen et al., 2014; Turner & Mlawer, 2010; Bellisario et al., 2019; Martinazzo et al., 2021) and that the OLR in FIR is especially sensitive to atmospheric water vapor and clouds and thus provides potentially improved means of retrieving their information (Sinha & Harries, 1995; Harries et al., 2008; Delamere et al., 2010; Cox et al., 2015; L. Palchetti et al., 2015; L. Palchetti et al., 2016; Magurno et al., 2020; Blanchet et al., 2011).

In recognition of the importance of FIR, several observational projects have recently gained momentum in their development and aimed to acquire unprecedented measurements in this spectral region. These projects include the Thin Ice Cloud in Far Infrared Experiment (TICFIRE, Blanchet et al., 2011) funded by the Canadian Space Agency, the Polar Radiant Energy in the

95 Far Infrared Experiment (PREFIRE) funded by U.S. NASA (L'Ecuyer et al., 2021), and the Far-
96 Infrared Outgoing Radiation Understanding and Monitoring (FORUM) project funded by the
97 European Space Agency (L Palchetti et al., 2020). Given that the worldwide observation data of
98 FIR is not available yet, we are motivated to use simulations to acquire prior knowledge of
99 climatological mean distribution of the OLR in FIR.
100   In summary, in this paper we aim to use a radiative transfer model to simulate the spectrally
101 decomposed OLR and dissect the atmospheric and surface contributions to the global mean OLR
102 as well as its geographic distributions. We are particularly interested to identify the critical
103 atmospheric layers that contribute most to the OLR in different spectral regions. The rest of the
104 paper is structured as: Section 2 describes the model and dataset used for analyses. Section 3
105 presents the results of layer-wise contributions to OLR and their geographical patterns. Section 4
106 summarizes the main conclusions of the paper.

109 **2. Method**

111 **2.1 Numerical model and data**

113   In this paper, we use the GCM version of the longwave rapid radiative transfer model
114 (RRTMG) (Mlawer et al., 1997) to simulate OLR. RRTMG has been extensively validated
115 against the benchmark line-by-line computations (Collins et al., 2006). It adopts the correlated-k
116 method, conducting the radiative transfer computation at 140 g-points (monochromatic spectral
117 nodes) to derive the OLR in 16 different spectral intervals ("bands") ranging from 10 cm^{-1} to
118 3250 cm^{-1}. Three of the RRTMG bands are located in the far-infrared (see Table S1). Taking
119 advantage of the RRTMG band configuration, we adopt a practical definition of the far-infrared
120 as the wavenumbers ranging from 10 to 630 cm^{-1} and designate the sum of the fluxes in the first
121 three RRTMG bands as the OLR in the far-infrared and denote it as *FIR*. In comparison, the sum
122 of the rest bands, which include the mid-infrared window regions, is referred to as *MIR* (mid-
123 infrared).
124   To separate the emission contribution from each atmospheric layer to the OLR at the TOA,
125 we use the model-generated radiative properties at each g-point, including optical depth,
126 blackbody emission, etc., to calculate the layer-wise contribution to spectral OLR (i.e., the
127 emission by a layer that reaches the TOA), following the discrete form of radiative transfer
128 equation (Goody & Young 1989):

130 $$I(\tau = 0) = B(\tau^*) \cdot e^{-\tau^*} + \sum_{i=1}^{n}[B(\tau_i) \cdot e^{-\tau_i} \cdot \Delta\tau_i] \qquad (1)$$

132 where *I* is the upwelling irradiance at the TOA in the units of W m^{-2} and can represent either
133 *total OLR*, *FIR* or *MIR*. τ is the optical depth, monotonically increasing from the TOA ($\tau = 0$) to
134 the surface (τ^*). τ_i is the optical depth between TOA and the ith atmospheric layer and $e^{-\tau_i}$
135 measures the transmittance between this layer and the TOA. $\Delta\tau_i$ is the optical depth difference
136 between the upper and lower boundaries of the ith layer and measures the emissivity of the layer.
137 $B(\tau_i)$ and $B(\tau^*)$ are the source functions, i.e., the blackbody emission by the ith atmospheric
138 layer and the surface, respectively, in the units of W m^{-2}. n is the number of the layers ($n + 1$
139 levels) in the atmosphere. Based on Equation (1), the contribution of the surface emission or an

140   arbitrary atmospheric layer to the OLR is $B(\tau^*)e^{-\tau^*}$ or $B(\tau_i)e^{-\tau_i}\Delta\tau_i$, respectively, which we
141   compute from the RRTMG-generated optical depths and source functions.
142   To accurately measure the OLR in reality, profiles required by RRTMG, such as
143   temperature, water vapor, ozone concentration, cloud fraction, cloud water path, etc., are taken
144   from the 6-hourly data of the fifth generation European Centre for Medium-Range Weather
145   Forecasts atmospheric reanalysis (ERA5) (Hersbach et al., 2020), with a horizontal resolution of
146   2.5 degree by 2.5 degree and 37 vertical levels. Five more layers of the U.S. standard profile are
147   patched above 1hPa to ensure the accuracy of the radiative flux. Other cloud properties, such as
148   cloud liquid droplet and ice crystal radii are taken from the synoptic TOA and surface fluxes and
149   clouds product of the Clouds and Earth's Radiant Energy System (CERES, Doelling et al., 2013)
150   at the same sampling time, interpolated from a horizontal resolution of 1 degree to the resolution
151   (2.5 degree) of the ERA5 data.
152   To account for the seasonal variations of the spectral OLR, we conduct a one-year
153   simulation in year 2013, a neutral year with no significant El niño or La niña anomalies (see
154   Figure S1), using the instantaneous profiles described above. Annual mean results are averaged
155   from all instantaneous radiative fluxes, i.e., $\frac{1}{365*4}\sum_{i=1}^{365*4} I_i$, where the index i indicates different
156   time steps, and used for all the analyses here. We will focus on the all-sky results in the
157   following, although clear-sky fluxes are also computed by excluding cloud condensates in the
158   RRTMG computation and are compared to the all-sky results in order to measure the cloud
159   effects.
160   The total OLR diagnosed based on Equation (1) is compared to the RRTMG directly
161   output values as shown in Figure S2, which confirms the validity of this decomposition. Figure
162   S2 also shows a comparison of total OLR between our simulation and the data provided by
163   ERA5, which are in good agreement and affirms the quality of the simulation data used in this
164   analysis.
165
166
167   **2.2 Diagnostic method**
168
169   From Equation (1), the contribution of a certain layer is controlled by two factors: the
170   source function (the Planck term B relevant to the atmospheric temperature) and the radiative
171   properties (the emissivity and transmission terms relevant to τ). To isolate the spectroscopic
172   effect relevant to τ from the temperature effect that affects B, here we define a *layer contribution*
173   *function:*
174
175     $f_i = B(\tau_i) \cdot e^{-\tau_i} \cdot \Delta\tau_i$ (2)
176
177   to distinguish from the often-used concept of *weighting function* (Goody & Yung, 1989):
178
179     $w_i = e^{-\tau_i} \cdot \Delta\tau_i$ (3)
180
181   Furthermore, we analyze these functions in their normalized forms:
182
183     $F_i = \frac{f_i}{OLR_{atm} \cdot \Delta p_i} \cdot 100hPa$ (4)
184

185     $W_i = \frac{w_i}{(\sum w_i) \cdot \Delta p_i} \cdot 100 hPa$ (5)

186

187   Here f_i and w_i are the layer contribution functions and weighting functions of the ith layer,
188   respectively. Δp_i is the pressure thickness of the layer, in the units of hPa. OLR_{atm} is the total
189   atmospheric contribution to OLR and $\sum w_i$ is the sum of the weighting functions of all the
190   atmospheric layers (excluding the surface), as the focus here is to dissect the atmospheric
191   contribution. F_i measures the overall relative contribution of each 100hPa-thick atmospheric
192   layer; in comparison, W_i measures the relative contribution governed by absorber distribution,
193   i.e., the contribution that an isothermal atmosphere would have. Note that both functions, F_i and
194   W_i, are defined here with respect to unit layer thickness measured in hPa and thus the latter
195   differs from the weighting function $(\frac{de^{-\tau_i}}{dz})$ that is often used in remote sensing analyses and
196   defined with respect to unit thickness in km.
197   Although the contribution function F_i can be evaluated from the band fluxes readily
198   available from RRTMG, it would be inappropriate to simply average the RRTMG-computed
199   transmission functions to obtain a broadband weighting function W_i, because such a
200   straightforward average would not account for the strong variation of the radiance intensity with
201   frequency (a feature of Planck function). Alternatively, we adopt a diagnostic approach to infer a
202   band-representative optical depth using the flux profiles generated from RRTMG. Assuming a n-
203   layer ($n+1$ levels) atmosphere with an increasing index from TOA to the surface, the flux
204   coming into and out of the boundaries of ith layer can be expressed as:

205

206     $F_i^{up} = e^{-\Delta \tilde{\tau}_i} \cdot F_{i+1}^{up} + (1 - e^{-\Delta \tilde{\tau}_i}) \cdot \tilde{B}_i$ (6)

207

208     $F_{i+1}^{down} = e^{-\Delta \tilde{\tau}_i} \cdot F_i^{down} + (1 - e^{-\Delta \tilde{\tau}_i}) \cdot \tilde{B}_i$ (7)

209

210   Here F_i^{up} and F_i^{down} are the upward and downward fluxes, respectively, at the upper boundary
211   of the ith layer in the units of W m[-2]. Similarly, F_{i+1}^{up} and F_{i+1}^{down} are the fluxes at the lower
212   boundary of the ith layer. $\Delta \tilde{\tau}_i$ and $\tilde{B}_i$ are the diagnostic optical depth and source function of the
213   i[th] layer, which can be solved from the two equations given all the fluxes available from
214   RRTMG. We denote these diagnostic variables with a tilde to distinguish them from those
215   directly generated by RRTMG.
216   From Equations (6) and (7), $\Delta \tilde{\tau}_i$ can be derived as:

217

218     $\Delta \tilde{\tau}_i = log(\frac{F_i^{down} - F_{i+1}^{up}}{F_{i+1}^{down} - F_i^{up}})$ (8)

219

220   Equation (8) provides a simple method to derive the optical depth throughout the atmospheric
221   column. For instance, the accumulated optical depth of all layers above the ith level can be
222   computed as: $\tilde{\tau}_i = \sum_1^i \Delta \tilde{\tau}_j$. For readers interested in this topic, we show the geographic
223   distribution of the derived broadband optical depth in the Supplementary Figure S3 and, as an
224   example, compare the transmission profile based on the optical depth derived for one band and
225   that averaged from the RRTMG-computed transmission functions at the g-points in Figure S4.
226   The comparison shows that the diagnostic results can well depict the RRTMG-computed results,
227   which we remind are not necessarily a better measure for the analysis here because they do not

228 account for the spectral variance of the radiance. See the Supplementary Information for further
229 discussion of the calculation of the weighting function in different vertical coordinates (Figure
230 S5).
231   The above formulation can be easily adapted to the analysis of either broadband or
232 spectral OLR. For example, to obtain the weighting function appropriate to *FIR*, we use the
233 RRTMG-simulated far-infrared fluxes (sum of the first three bands) to derive a FIR-appropriate
234 optical depth profile following Equation (8) and then derive the weighting function following
235 Equations (3) and (5). All the following results associated with broadband optical depth,
236 transmittance or weighting function are obtained based on this method if not otherwise stated.
237
238
239 **3. Results**
240
241   In this section, we first present the geographic distribution of the *OLR* and *FIR* to provide
242 a comparison of their global patterns. Following the methods introduced in Section 2, we then
243 decompose the TOA fluxes into contributions from the different atmospheric layers and the
244 surface. Finally, the cloud radiative effect is measured as the difference between all-sky and
245 clear-sky results, to identify the cloud influence on the atmospheric layer-wise contributions to
246 OLR. Our aim is to dissect the OLR distribution from a combined spectral, vertical and
247 geographic perspective. Although the presentation below is focused on *OLR* and *FIR,* interested
248 readers can find complementary *MIR* results in the Supplementary Information.
249
250 **3.1 Geographic distribution of total OLR and FIR**
251
252   Figure 1 shows the geographic distributions of the annual zonal mean OLR. There is a
253 prominent meridional gradient of total OLR from the equator to the poles, with the maximum
254 values in the tropics being about two times that at the South pole. In contrast, *FIR* displays a
255 much more uniform pattern, showing little variations with latitudes (Figure 1a), although in both
256 cases (total OLR and *FIR*), regional minima exist where high convective clouds (e.g., in the
257 Intertropical Convergence Zone, ITCZ) or high topography (e.g., Tibet and Antarctic plateaus)
258 result in colder radiating temperatures (Figure 1c and d).
259   It is interesting to notice that the fraction of the FIR flux relative to the total OLR increases
260 with the latitude (Figure 1b), amounting to over 50% in North Pole and nearly 60% in South
261 Pole. This is due to the shift of the peak of Planck function to lower wavenumbers at lower
262 temperatures according to the Wien's displacement law. This emphasizes the predominant
263 importance of FIR in the cold regions. This is in accordance with the previous studies; for
264 example, Harries et al. (2008) noted a 45% FIR contribution to OLR.
265   The breakdown of the TOA FIR into atmospheric and surface contributions in Figure 1b
266 discloses that the atmospheric fractional contribution (about 45%) is almost constant across the
267 latitudes and the higher FIR fraction at the polar regions is mainly due to enhanced contributions
268 from the surface, which is typically less than 1% in the lower latitudes (Table 1) due to the
269 strong water vapor absorption but can amount to nearly 20% at South Pole where the atmosphere
270 is thin and dry (Figure 1b). This indicates the opening of the atmospheric window in the far-
271 infrared in the high latitude and high altitude regions, which makes the FIR measurements there
272 especially useful for sounding both the atmosphere and possibly the surface (e.g., Feldman et al.,
273 2014). A similar decomposition in MIR can be found in the Supplementary Figure S6.
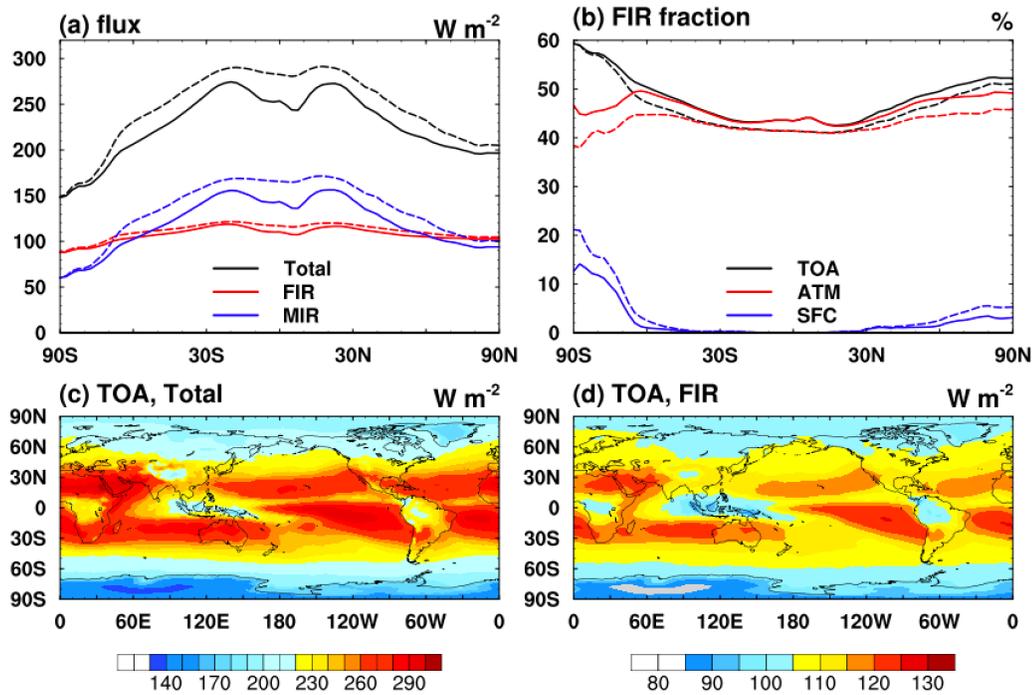
Figure 1. Annual mean distribution of OLR. (a) Zonal mean total OLR, FIR and MIR, units: W m^{-2}. (b) Zonal mean FIR fraction with respect to local total OLR, decomposed into contributions from the atmosphere and surface, units: %. (c, d) Geographic distributions of total OLR and FIR, units: W m^{-2}. Note that red and blue lines in (a, b) add up to the black lines. Solid lines in (a, b) represent the results in all sky and dash lines in clear sky.

(a)

W m^{-2} (%)		FIR	MIR	Total
TOA		110.51 (45.53%)	132.20 (54.47%)	242.72 (100.00%)
SFC		1.80 (0.74%)	39.56 (16.30%)	41.36 (17.04%)
ATM	whole	108.71 (44.79%)	92.64 (38.17%)	201.35 (82.96%)
	troposphere	99.61 (41.04%)	78.27 (32.25%)	177.88 (73.29%)
	stratosphere	9.11 (3.75%)	14.36 (5.92%)	23.47 (9.67%)

(b)

W m^{-2} (%)		FIR	MIR	Total
TOA		115.16 (43.48%)	149.68 (56.52%)	264.84 (100%)
SFC		2.86 (1.08%)	65.74 (24.82%)	68.59 (25.90%)
ATM	whole	112.30 (42.40%)	83.94 (31.70%)	196.25 (74.10%)
	troposphere	103.53 (39.09%)	69.73 (26.33%)	173.25 (65.42%)
	stratosphere	8.78 (3.31%)	14.22 (5.37%)	22.99 (8.68%)

(c)

W m^{-2}	FIR	MIR	Total
TOA	-4.65	-17.47	-22.12

SFC		-1.06	-26.17	-27.23
ATM	whole	-3.59	8.70	5.11
	troposphere	-3.92	8.55	4.63
	stratosphere	0.33	0.15	0.48

Table 1. Annual global mean contributions from the atmosphere and surface in the FIR and MIR to the total OLR in (a) all sky, (b) clear sky and (c) the cloud radiative effects (the difference of flux between all sky and clear sky). The contribution from troposphere and stratosphere is divided based on the definition of the tropopause of the World Meteorological Organization.

Table 1 summarizes the global mean contribution from each component to the total OLR in all sky. The global annual mean total OLR of 2013 is computed to be about 243 W m^{-2}, slightly higher than the value (239 W m^{-2}) reported in Trenberth et al. (2009) and that (240 W m^{-2}) in Loeb et al. (2018) but within the uncertainty range given by Stephens et al. (2012). From the global mean perspective, around 83% of the OLR is originated from the atmosphere and 45% (111 W m^{-2}) comes from FIR. The spatial variability (measured by the standard deviation of the local annual mean values across the globe as depicted in Figure 1c and d) of the total OLR is 30.86 W m^{-2} and that of FIR is 7.17 W m^{-2}, in accordance with the more uniform FIR pattern noted above. For the surface contribution, the global mean surface contribution is about 41 W m^{-2}, with the majority coming from the MIR. This number is close to the result of Kiehl and Trenberth (1997) and Trenberth et al. (2009), who reported that the transmitted surface emission is 40 W m^{-2}. In comparison, Costa and Shine (2012) measured the direct transmitted surface emission to be 22 W m^{-2}. The discrepancies between these numbers warrant some discussions. First, Kiehl and Trenberth (1997) particularly noted their number as transmission through the mid-infrared atmospheric window. If integrated from 820 to 1390 cm^{-1} (based on the RRTMG band partition), our calculation shows that the sum of OLR in this spectral range is 84.73 W m^{-2}, to which the surface contributes 33.29 W m^{-2}, showing significant atmospheric contribution even in these window bands as noted by Costa and Shine (2012). Secondly, the temporal and spatial resolution of profiles used in the computation can also lead to the differences. The result of Kiehl and Trenberth (1997) was presented for a single global mean profile and Costa and Shine (2012) used annual mean profiles, including that of clouds, in their radiative transfer calculation. In contrast, our simulation here uses 6-hourly instantaneous profiles at every location across the globe, minimizing the bias due to spatiotemporal sampling and nonlinear dependence of radiation on the atmospheric state variables. Although our simulation is also subject to certain limitations, for instance, the ignorance of cloud scattering of the infrared radiation, from the published assessments (e.g., Chen et al. 2014) this effect typically makes a difference of about 1 W m^{-2} in OLR and thus a small (<1%) fractional uncertainty in our results.

To summarize, the results above disclose that the atmosphere makes a dominant contribution to OLR, especially in the far-infrared. The higher far-infrared fraction of OLR in the polar regions is caused by a stronger surface contribution as the atmospheric window opens in these dry regions. Given the importance of the atmospheric contribution, which critical layer of the atmosphere dominates the atmospheric contribution? Does the critical layer vary with the spectrum? We will address these questions in the following subsection.

329
330 **3.2 Layer-wise contribution to total OLR and FIR**

331
332 **a) Global mean**

333
334   First, we show a globally averaged spectral and vertical decomposition of OLR in Figure
335 2, which discloses that the critical layer that contributes most to OLR strongly varies in height in
336 different spectral bands. In the far-infrared (wavenumber less than 630 cm^{-1}), the atmospheric
337 contributions are mainly emitted from the middle and upper portions of the troposphere, with a
338 maximum located at around 500hPa and 500 cm^{-1} (Figure 2a), due to the strong absorption of
339 water vapor in this band blocking the emission from the lower troposphere and the surface. In the
340 CO_2 absorption band (from 630 cm^{-1} to 700 cm^{-1}), the strong absorption of CO_2 masks almost all
341 emissions below the stratosphere and leads to a contribution peak in the stratosphere. In the
342 window region (700-980 cm^{-1}and 1080-1180 cm^{-1}), the atmosphere contribution is located in the
343 lower troposphere where the relatively weaker water vapor continuum absorption mainly
344 accounts for the atmospheric absorption and emission, and this allows the transmitted surface
345 emission to make significant contribution to OLR (Figure 2c). The maximum in the stratosphere
346 in the 980-1080 cm^{-1} band results from the absorption of stratospheric O_3. It is interesting to note
347 that Figure 2a, despite its much lower spectral resolution, well resembles the pattern of the
348 sensitivity of spectral OLR to atmospheric perturbations (Huang et al., 2007b). This affirms that
349 the critical layers that significantly contributing to OLR are also the vertical locations where the
350 space OLR measurements are most sensitive to.
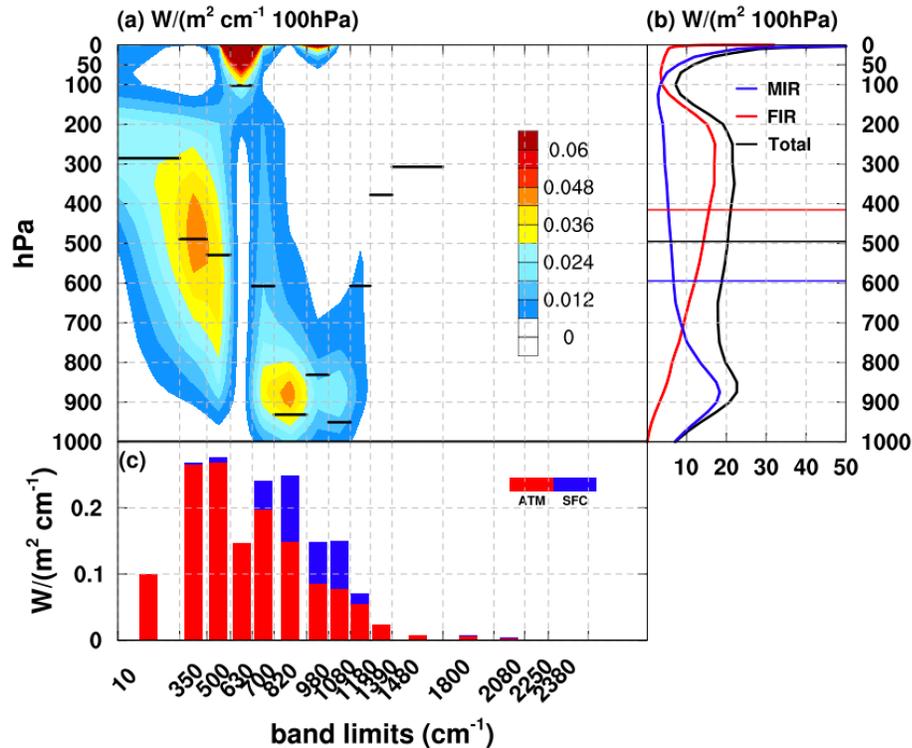

351
352   Figure 2. All-sky global annual mean spectral and vertical decomposition of OLR. (a)
353 Layer-wise atmospheric contribution to the OLR irradiance flux in each of the 16 RRTMG
354 bands, units: W/(m^2 cm^{-1} 100hPa). (b) Spectrally integrated layer-wise contribution, units:
355 W/(m^2 100hPa). (c) Vertical integrated atmospheric contribution, in comparison with the surface

356 contribution, units: W/(m^2 cm^{-1}). The horizontal lines in (a) and (b) are the inferred $\tau=1$ level
357 using the diagnostic method described in Section 2. Note that the results in (a) and (b) are
358 smoothed in the vertical direction using a 3-point running average to eliminate the artifacts
359 caused by the non-uniform vertical resolution of the EAR5 atmospheric profiles; the same
360 procedure is applied to the other vertical plots.
361
362   Despite the height variations of the critical layers from band to band, the broadband
363 atmospheric contribution is rather vertically uniform throughout most of the troposphere (from
364 900hPa to 200hPa) (Figure 2b). This, however, is smoothed from the contrasting behaviors of
365 FIR and MIR, to which the atmospheric contribution peaks in the upper and lower troposphere,
366 respectively. The comparison to the clear-sky decomposition (Figure S7) shows that the local
367 maxima near 900hPa and 200hPa are partially attributable to the significant cloud occurrence at
368 these levels (see Figure S1e).
369   A remarkable finding revealed by Figure 2 is that the tropopause layer around 100hPa
370 makes a minimum contribution to OLR. The atmospheric contribution here is about three times
371 less than the surrounding vertical layers (Figure 2b). From Equation (1), is this due to the
372 temperature minimum at the tropopause (the source function B_i) or the vertical distribution of the
373 atmospheric absorbers and their spectroscopic features, which leads to a minimum of the
374 weighting function value here? Figure 3 shows the comparison of F_i and W_i of total OLR and
375 FIR, which shows that the contribution function is largely controlled by the shape of weighting
376 function, with the temperature effect playing a modulating role. Specifically, in the troposphere
377 below 600 hPa where the air temperature is relatively higher than the upper layers, the
378 atmospheric contribution is nearly doubled by the temperature effect (in Figure 3a, the areas
379 subtended by the two lines below 600hPa are 42.73% and 23.67%, respectively). The situation is
380 opposite in the upper troposphere. However, at the tropopause around 100 hPa, the two lines
381 coincide with each other, suggesting that the minimum contribution here is largely explained by
382 the weighting function (atmospheric spectroscopy). The minimum contribution at the tropopause
383 also indicates that it is generally more difficult to retrieve the atmospheric conditions near this
384 level by using space measurements.
385   It is worth noting that the peaks of the weighting functions here (the black lines in Figure
386 3) differ from the often cited $\tau=1$ level (e.g., see the derivation of Huang & Bani Shahabadi
387 2014) as shown in Figure 2b. As Jeevanjee and Fueglistaler (2020) noted, the $\tau=1$ law depends
388 on the choice of vertical coordinate and normally corresponds to the level where $\frac{de^{-\tau}}{dz}$ peaks, as
389 opposed to where $\frac{de^{-\tau}}{dP}$ (the weighting function defined here) peaks.
390
391
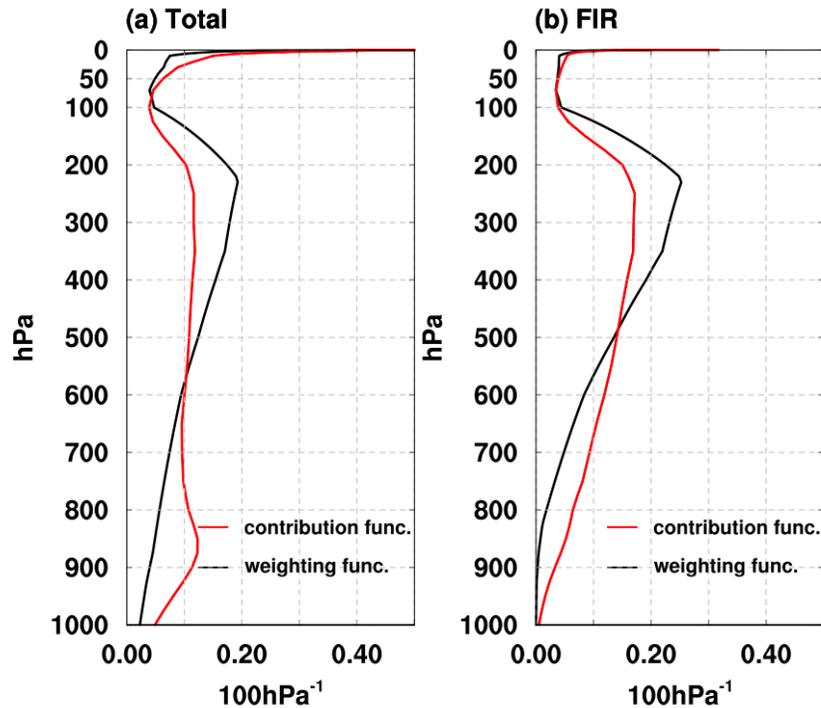
Figure 3. All-sky annual mean global mean contribution functions and weighting functions for (a) the total OLR, and (b) FIR.

b) Geographic variations

Figure 2 shows that the layer-wise atmospheric contributions with respect to the global mean OLR. How do the atmospheric contributions geographically vary? Figure 4 shows the zonal mean atmospheric contributions, in comparison with surface contribution. With regard to the total OLR, the atmospheric contribution shows a pattern that corresponds to the distribution of clouds. For instance, the maxima at 200hPa in the tropics, 400hPa in the mid-latitudes and 900hPa in the southern latitudes all coincide with the high cloud occurrence in these regions (Figure S1e). The comparison to the clear-sky result (Figure S8) further affirms that these maximum contribution layers are caused by the clouds (see further analysis in the following section).
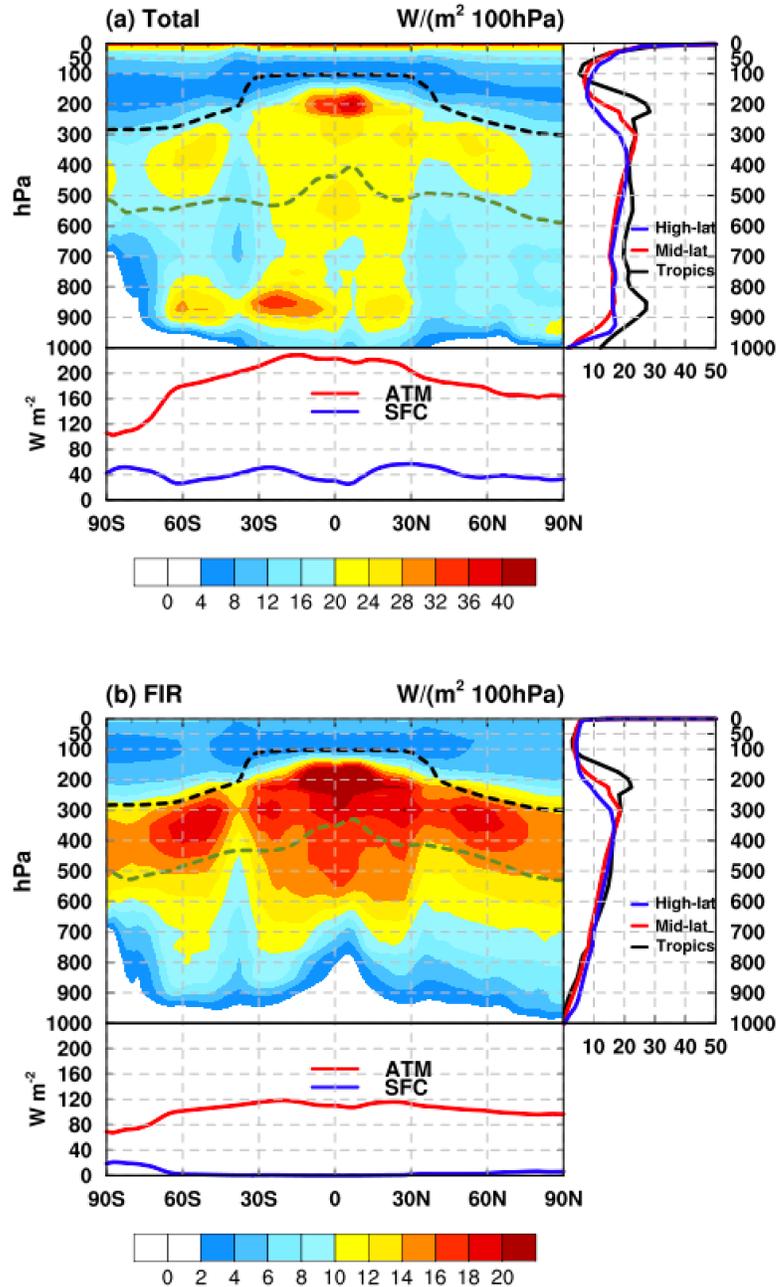
Figure 4. Annual mean and zonal mean flux intensity in all sky (a) in total OLR, (b) in FIR, units: W/(m² 100hPa). The bottom line plots show the vertically integrated atmospheric contribution and surface contribution, units: W m⁻². The right line plots are the regional averaged profiles, with Tropics representing the tropics (from 30N to 30S) and Mid-lat representing the northern mid-latitude region (60N-30N) and High-lat representing northern high-latitude region (90N-60N). The black dash line in contour plots represents the tropopause based on the definition of World Meteorological Organization and dark green dash line is the inferred $\tau = 1$ level using the method described in Section 2.

Comparing the overall atmospheric contribution to *OLR* to that of the surface, we find that interestingly the surface contribution is rather invariant with the latitude, showing a value of

420 about 40 W m^{-2}, although the atmospheric contribution peaks in the lower latitudes due to the
421 higher emitting temperatures and greater atmospheric opacity there. The right line plot in Figure
422 4a contrasts the contribution functions between the northern-hemisphere low-, mid- and high-
423 latitudes, which shows the local maximum in the upper troposphere descending from 200hPa in
424 the low latitudes to in the 400hPa latitudes, reflecting the lowering of the tropopause which caps
425 the atmospheric emitters such as clouds and water vapor within the troposphere. It is interesting
426 to note that the aforementioned minimum contribution layer around the tropopause persists at all
427 the latitudes, indicating that this feature is robust and prominent at all locations.
428   In comparison to the total OLR, the atmospheric contribution to *FIR* at all latitudes has a
429 prominent maximum located right below the tropopause (around 200hPa to 400hPa). This is
430 because the strong absorption in the water vapor rotational band in the far-infrared masks the
431 emission from the lower troposphere and surface (blank regions in Figure 4b). This figure shows
432 that only near the poles the near-surface atmospheric layers and the surface are visible to the
433 space in the far-infrared.
434
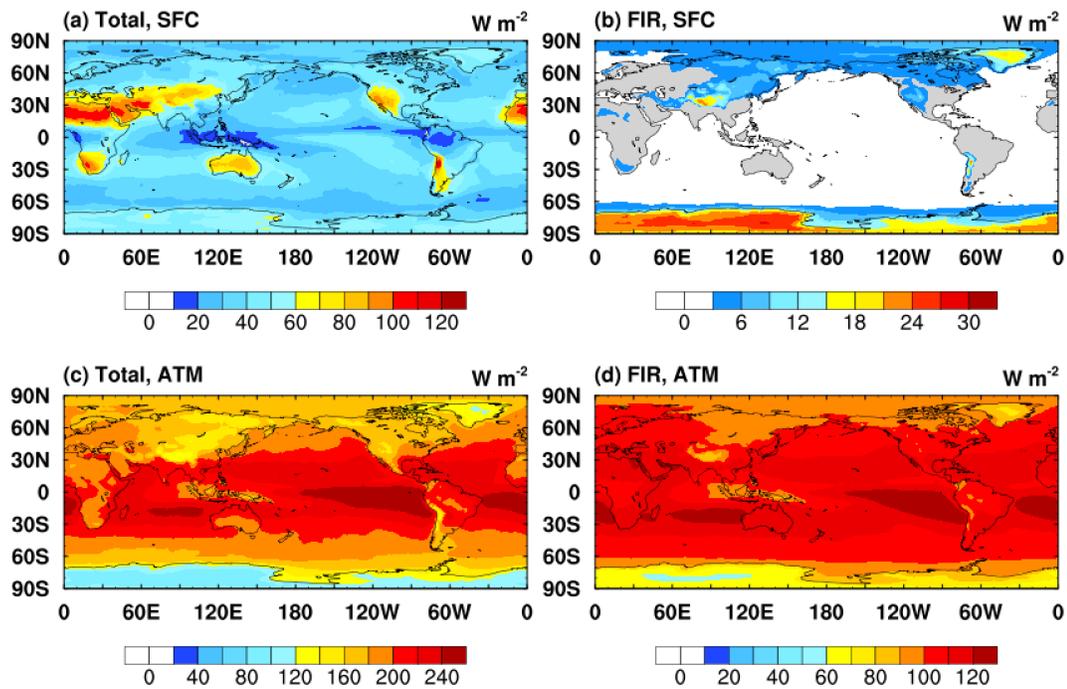
435
436   Figure 5. All-sky annual mean (a, b) surface and (c, d) atmospheric contributions to total
437 OLR and FIR, units: W m^{-2} (See further decomposition of troposphere and stratosphere in Figure
438 S9).
439
440   Figure 5 further discloses the geographic distribution of the surface and atmospheric
441 contributions. The surface contribution to the total OLR is rather uniform across the globe at a
442 value around 40 W m^{-2}, except in dry or high-elevation regions (e.g., Sahara, Tibet Plateau,
443 Australia, Rocky Mountains and Andes) where the contribution can exceed 100 W m^{-2}, and in
444 very moist regions such as the ITCZ where the surface contribution is lower than 20 W m^{-2}. Due
445 to strong absorption in the water vapor rotational band, the surface contribution to FIR is visible
446 only in polar regions and in regions of high topography (thin atmosphere).

447   Interestingly, the atmospheric contribution in the ITCZ also appears a local minimum
448 within the tropics, while the maxima locate in the subtropical regions where it is less cloudy and
449 thus more lower tropospheric emission at higher temperatures can reach the space.
450   In summary, this section investigates the layer-wise atmospheric contributions to total
451 OLR and FIR, as controlled by both temperature and spectroscopic effects, and compare the
452 atmospheric contribution to the surface contribution. We find that OLR, as well as its geographic
453 variation, is largely contributed by the atmosphere, although there are also noticeable regional
454 differences in the surface contribution, especially for the FIR. The vertical decomposition of the
455 atmospheric contribution clearly signifies the effects of clouds, which we will further analyze in
456 the following subsection.
457
458
459 **3.3 Cloud radiative effect**
460
461   Here, we use the difference in flux contribution between the all-sky and clear-sky to define
462 the cloud radiative effect (CRE). Figure 6a shows how clouds modify the global mean
463 atmospheric and surface contributions to the total OLR. Generally speaking, the atmospheric
464 contribution is enhanced at the locations of high cloud occurrence, e.g., at levels near 200hPa
465 and 900hPa (Figure S1e) as they enhance the atmospheric emissivity. At the same time, the
466 clouds decrease the transmission from layers below and reduce their contributions to OLR.
467   Figure 6b shows that interestingly the cloud effect in the far-infrared is to reduce the
468 overall atmospheric contribution (as indicated by a larger area of negative values subtended by
469 the red line) while the cloud effect in the mid-infrared is to increase the atmospheric
470 contribution, which, however, is at the price of reduced surface contribution. These effects lead
471 to a reduced OLR value in the all sky (243 W m^{-2}, as shown in Table 1) compared to clear sky
472 (265 W m^{-2}).
473   Figure 6c displays the spectral decomposition of the CRE and how it is decomposed into
474 atmospheric and surface contributions. As noted by many previous studies (e.g., Kiehl &
475 Trenberth 1997), the CRE mainly arises from the mid-infrared window. Overall, the cloud
476 effects increase the atmospheric contribution by 5.11 W m^{-2} and decrease that by the surface by -
477 27.23 W m^{-2} (Table 1b), leading to a total CRE at the TOA of 22.12 W m^{-2}. These numbers lie
478 within the range of values reported by others. For example, L'Ecuyer et al. (2008) measured the
479 total CRE to be 21.6W m^{-2} using the CloudSat dataset, CERES Energy Balanced and Field Ed
480 4.1 Data Quality Summary reported 26 W m^{-2} in the CERES Ed 4.1 dataset, and Allan (2011)
481 reported 27.2 W m^{-2}, with atmosphere and surface contributions of 5.5 m^{-2} and -32.7 m^{-2}
482 respectively.
483
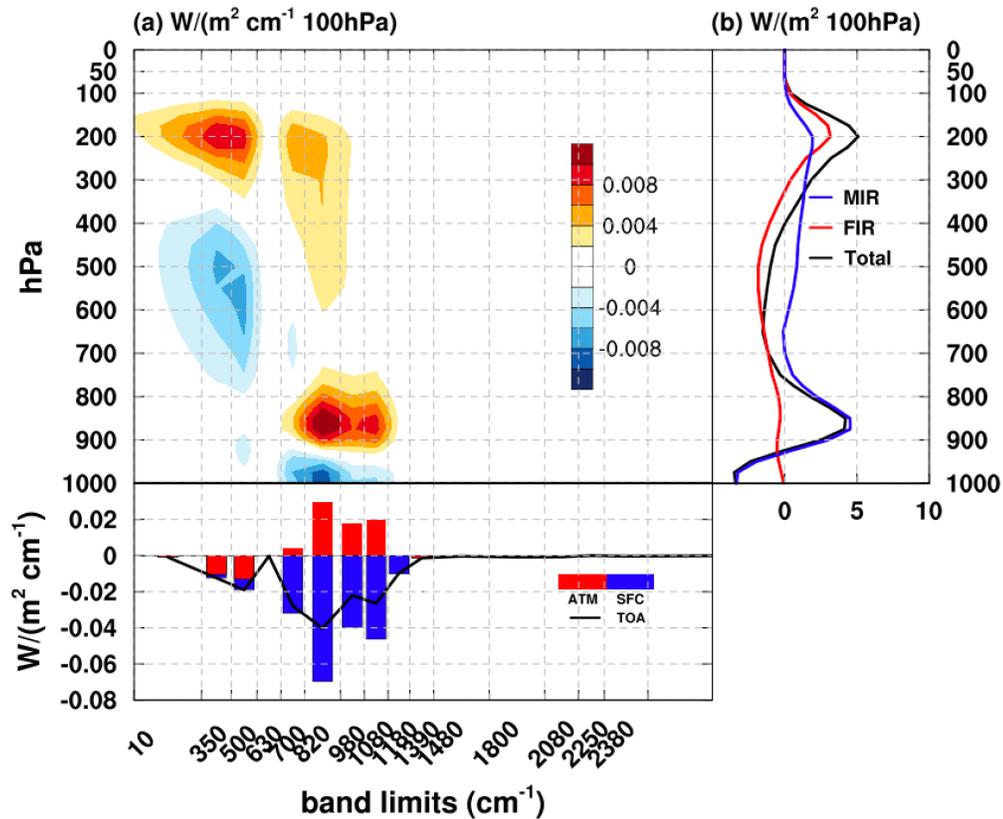
484
485   Figure 6. Similar to Figure 2 but for the cloud radiative effect.
486
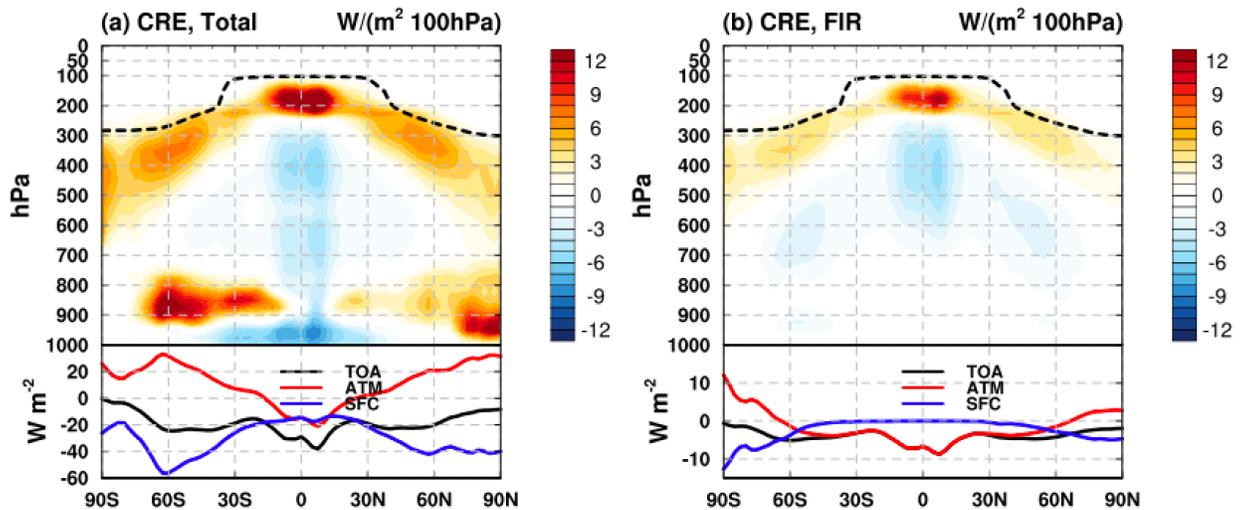
487
488   Figure 7. All-sky annual zonal mean cloud radiative effect on the atmospheric and surface
489   contributions to (a) the total OLR, and (b) FIR, units: W/(m^2 100hPa). Line plots show the
490   vertically integrated atmospheric contribution and surface contribution, units: W m^{-2}. The black
491   dash line in contour plots represents the tropopause (See results in MIR in Figure S10).
492

Figure 7 discloses the zonal mean pattern of the CRE, with respect to vertically decomposed atmospheric contribution in terms of both total OLR and FIR. It is interesting to notice that the cloud blocking of the surface contribution more strongly exists in the extratropics, while for the atmospheric contribution, the CRE changes sign from low- to high-latitudes.
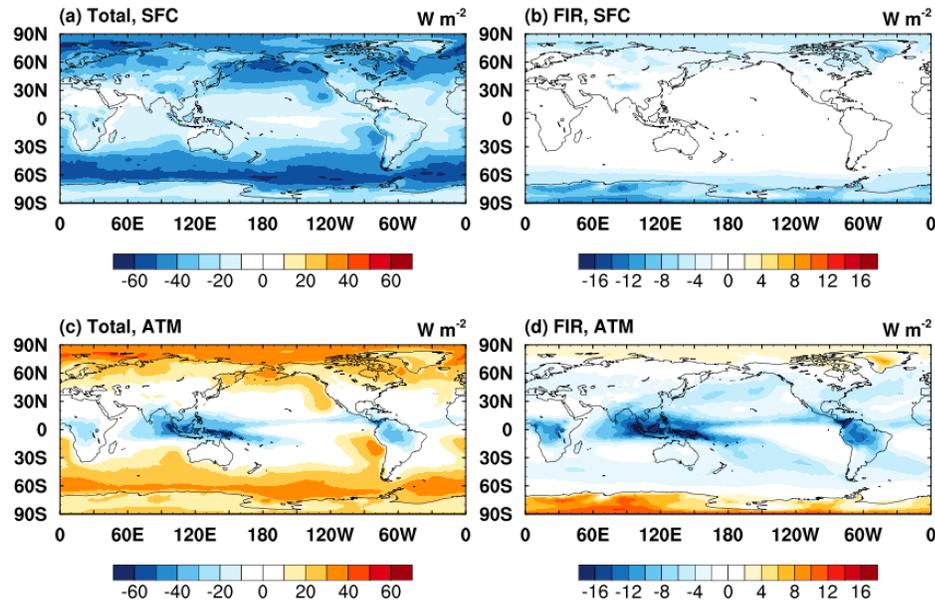

Figure 8. Annual mean cloud radiative effect on the surface and atmospheric contributions to (a, c) the total OLR and (b, d) FIR, units: W m^{-2}.

Figure 8 further shows the geographic distributions of the CRE. Clouds greatly decrease the transmission of the surface emission through the atmosphere and this effect is more significant in mid-to-high latitudes where the water vapor concentration is relatively lower compared with the tropics. With respect to the atmospheric contribution, the CRE is characterised by strong negative values at the ITCZ and positive values in the extratropics. The CRE in the atmosphere at different levels can be of opposite sign due to the compensation of enhanced emission at cloud layers and weakened transmission from cloud layers below (See more details in Figure S11 and Table S2).

In summary, clouds result in a decrease of the surface contribution to OLR and an increase of the atmospheric contribution to the TOA. The atmospheric contribution is especially enhanced at the locations of cloud occurrence.

4. Conclusions and discussions

In this paper, we use a radiative transfer model to simulate the spectrally resolved OLR and decompose it into the contributions from the surface and atmosphere. This analysis dissects OLR from a combined spectral, vertical and geographic perspective, identifying the critical atmospheric layers contributing most strongly to the OLR in different spectral bands and how the contributions vary geographically. A notable strength of this assessment is that it is based on a

522 whole year's instantaneous atmospheric profiles from an observationally constrained global
523 dataset, ERA5.
524   One focus of this analysis is the global distribution of the OLR in the far-infrared, which
525 is expected to be monitored by several new satellites under development. This study presents a
526 preview of the observation based on simulated radiation fields. Our calculations affirm that a
527 significant portion of the Earth thermal radiation to space, i.e., the total OLR, is radiated in the
528 far-infrared. The far-infrared contribution is about 45% in terms of the global mean OLR and at
529 colder polar regions this contribution can increase to about 60% (Table 1). The vertical
530 decomposition discloses that the enhanced far-infrared contribution at the polar regions mainly
531 results from the surface (as opposed to atmosphere) contribution (Figure 1b).
532   It has been a long-standing interest to quantify the surface contribution to OLR, for which
533 previous studies reported differing values. We find that, from a global mean perspective, the
534 surface contributes about 17% of OLR (Table 1). The distribution of zonally averaged surface
535 contribution is relatively uniform across the globe with a strength of around 40 W m^{-2}, although
536 the geographic distribution is modulated by the atmospheric thickness and moisture content
537 (Figure 5). The surface contribution mainly comes from the mid-infrared, while in the far-
538 infrared the surface is only visible in the polar regions where the far-infrared surface contribution
539 can amount to 20% of the total OLR (compared to 1% or less at other latitudes).
540   Our analysis further resolves the atmospheric contributions to different vertical layers
541 from TOA to surface and identifies the critical contribution layers in different spectral bands. We
542 find the critical layers strongly vary in height in different spectral bands, with the critical layer in
543 far-infrared being located in the upper troposphere while that in the mid-infrared in the lower
544 troposphere (Figure 2). From a globally averaged and spectrally integrated point of view, the
545 contribution to the broadband OLR is vertically uniform throughout most of the troposphere
546 (Figure 2b). However, an interesting and remarkable feature revealed in this analysis is that the
547 atmosphere around the tropopause makes minimum contribution to OLR and this is found to be a
548 robust feature geographically at different latitudes (Figure 4a). By comparing the vertical
549 contribution functions to the weighting functions obtained via a diagnostic technique developed
550 here (Equation (4)), we find that the feature of minimum tropopause layer contribution is mainly
551 due to the spectroscopic feature of the Earth atmosphere and to a smaller extent due to the
552 temperature minimum around this level (Figure 3). Specifically, as shown in Figure 2a, the
553 absorption strength of the major gas absorption bands is such that the Earth-escaping photons of
554 OLR either emerges from the stratosphere (e.g., in the CO_2 band centered at 667 cm^{-1}) or from
555 the troposphere (e.g., in the H_2O band in the far-infrared), making the tropopause layer a
556 minimum contribution layer. It is for this reason that it is difficult to sound the tropopause layer
557 by satellite observation of OLR from the space.
558   The cloud radiative effect on OLR primarily comes from the reduction of surface
559 contribution (Table 1). In contrast, the cloud layers enhance the atmospheric contributions,
560 especially at the location of the cloud layers. The cloud effect is much stronger in the mid-
561 infrared than in the far-infrared, due to the existence of the mid-infrared atmospheric window
562 (800-1200 cm^{-1}) that is sensitive to the cloud masking effect (Figure 6).
563   In summary, our work provides a systematical assessment of the layer-wise contributions
564 to OLR, pinpointing the critical atmospheric contributing layers in each spectral band and
565 quantitatively comparing the atmospheric and surface contributions. Our simulation provides a
566 modeling reference of spectrally decomposed global distribution of OLR and dissection of its
567 spatial variability, which can be validated by future OLR observations that include the critical

568 far-infrared spectrum. This will provide insights into the radiation budget as well as model
569 biases. While a climatologic mean distribution is presented here, the temporal variability of the
570 OLR and how it results from varying atmospheric and surface contributions warrant further
571 studies to elucidate.
572
573
579
580 **Data Availability Statement**
581
582   The ERA5 datasets can be accessed through the ECMWF website
583 (https://cds.climate.copernicus.eu/#!/search?text=ERA5&type=dataset). The RRTM code can be
584 downloaded at http://rtweb.aer.com/rrtm_frame.html. The data used in this work can be accessed
585 from http://dx.doi.org/10.17632/2d95dztpxn.1.
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1   Supplementary information for

2   **A decomposition of the atmospheric and surface contributions to the outgoing**
3   **longwave radiation**

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Band	Wavenumber (cm^{-1})	Number of g-points	Influential gases
1	10 - 350	10	H_2O, N_2
2	350 - 500	12	H_2O
3	500 - 630	16	H_2O, CO_2, N_2O
4	630 - 700	14	H_2O, CO_2, O_3
5	700 - 820	16	H_2O, CO_2, O_3, CCl_4
6	820 - 980	8	H_2O, CO_2, CFC_{11}, CFC_{12}
7	980 - 1080	12	H_2O, O_3, CO_2
8	1080 - 1180	8	H_2O, CO_2, O_3, N_2O, CFC_{12}, CFC_{22}
9	1180 - 1390	12	H_2O, CH_4, N_2O
10	1390 - 1480	6	H_2O
11	1480 - 1800	8	H_2O, O_2
12	1800 - 2080	8	H_2O, CO_2
13	2080 - 2250	4	H_2O, N_2O, CO_2, CO, O_3
14	2250 - 2380	2	CO_2
15	2380 - 2600	2	N_2O, CO_2, H_2O, N_2,
16	2600 - 3250	2	H_2O, CH_4

Table 1. RRTMG bands and influential gases (from RRTMG LW instructions, http://rtweb.aer.com/rrtm_frame.html).
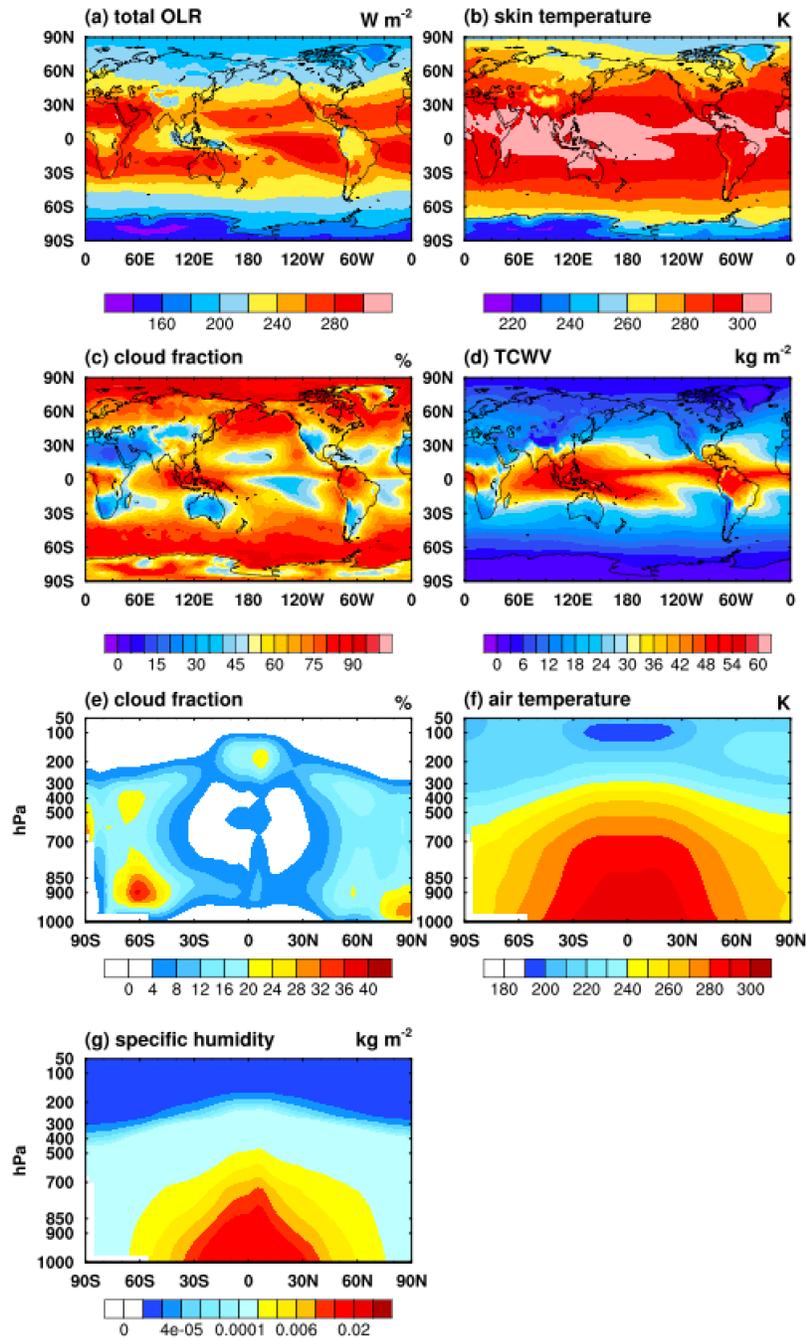
Figure S1. Annual mean (a) total OLR, units: W m^{-2}, (b) skin temperature, units: K, (c) cloud fraction, units: %, (d) total column water vapor (TCWV), units: kg m^{-2}, (e) zonal mean vertical distribution of cloud fraction, units: %, (f) zonal mean vertical distribution of air temperature, units: K, (g) zonal mean vertical distribution of specific humidity, units: kg m^{-2}, in 2013 of ERA5. The global mean values of total OLR and skin temperature in 2013 are 242.03 W m^{-2} and 288.36 K, respectively. In comparison, the multi-year (2013 to 2018) average (as well as the interannual standard deviation) of total OLR and skin temperature are 242.15 W m^{-2} (0.14 W m^{-2}) and 288.54 K (0.14 K), which shows that 2013 is a "normal" year.
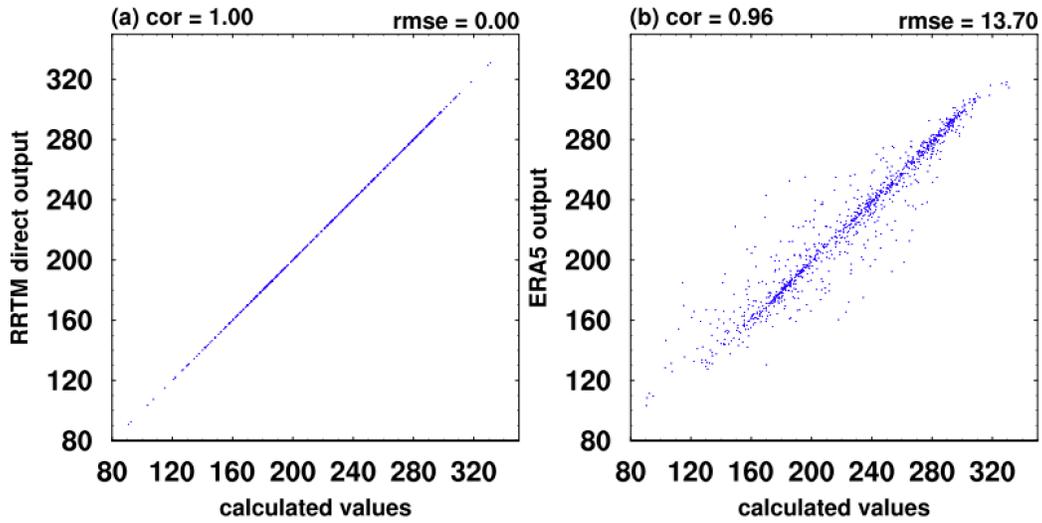
48
49 Figure S2. Validations of total OLR over the whole globe in all sky between (a) calculated
50 values using Equation 1 and direct output from RRTMG, (b) RRTKG-simulated results and
51 direct output from ERA5 at one time slice, units: W m^{-2}. *cor* is the correlation between two
52 series and *rmse* is the root-mean-square-error. The results here confirm the validity of both the
53 decomposition method described in Section 2.1 and the RRTMG simulations.
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(a) τ =1 level in all sky
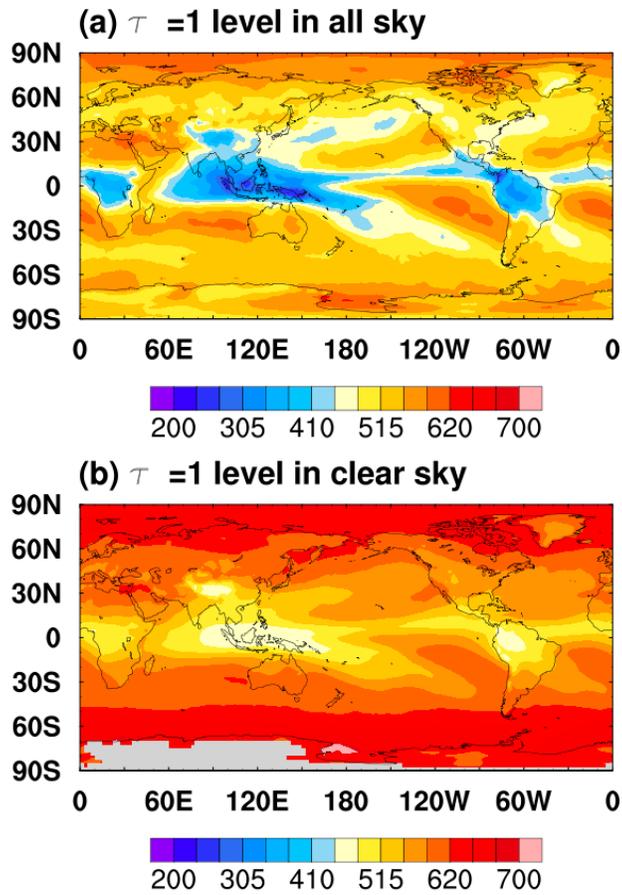
(b) τ =1 level in clear sky

Figure S3. Annual mean pressure of the τ=1 level in (a) all sky, and (b) clear sky. The plots are based on the broadband optical depth values derived using Equation (8). The missing value (grey region in (b)) indicates the total atmospheric optical depth is smaller than 1.
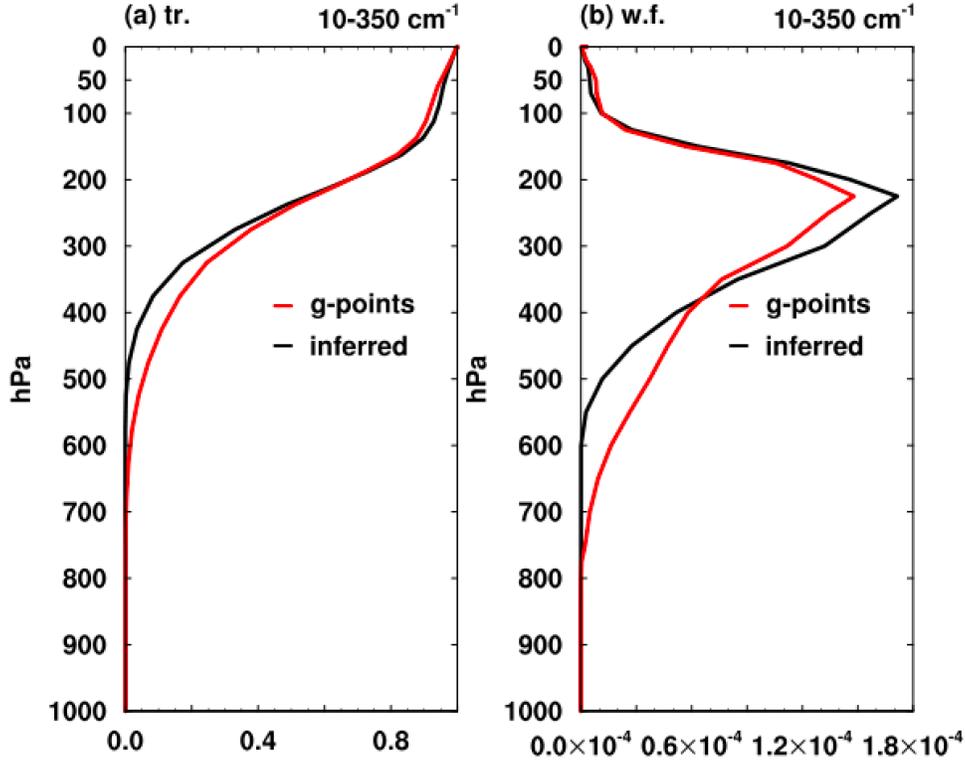
Figure S4. Comparison of (a) transmittance and (b) weighting functions between the inferred method (Equation (4)) and the averaged values from the g-points in the 10-350 cm^{-1} band at a random location (15N, 100E) in clear-sky.

Here we provide more descriptions of the inference method for the atmospheric transmission and derived weighting functions. Based on Equation (6) and (7), the inferred transmittance of a layer can be written as:

$$\Delta \tilde{tr}_i = \frac{F_i^{down} - F_{i+1}^{up}}{F_{i+1}^{down} - F_i^{up}} \quad (S1)$$

Here $\Delta \tilde{tr}_i$ is the inferred transmittance in the ith layer and hence the transmittance between the the ith layer and the TOA is $\tilde{tr}_i = \prod_1^i \Delta \tilde{tr}_j$. In theory, the transmittance at any given level should be positive and no bigger than unity. However, the derived transmittance based on Equation (S1) may violate the physical expectation due to anomalous flux profiles. We find that negative transmittance may occur when the optical depth is very high, e.g., in strong absorption bands, which decouples the incident and transmitted radiance in either upward or downward direction. To fix this, we correct the inferred transmittance value to 0. Inferred transmittance greater than 1 occurs less frequently and usually happens when there is a temperature inversion. In this circumstance, we set the inferred value to 1 and the corresponding optical depth in that layer to a representative value of 10^{-4}. All results in this work are corrected using this method.

As mentioned in the main text, the choice of vertical coordinate affects the shape of weighting function, here we further show a comparison of weighting functions defined as $\frac{dtr}{dp}$ and $\frac{dtr}{dz}$ after the corrections mentioned above in Figure S5.
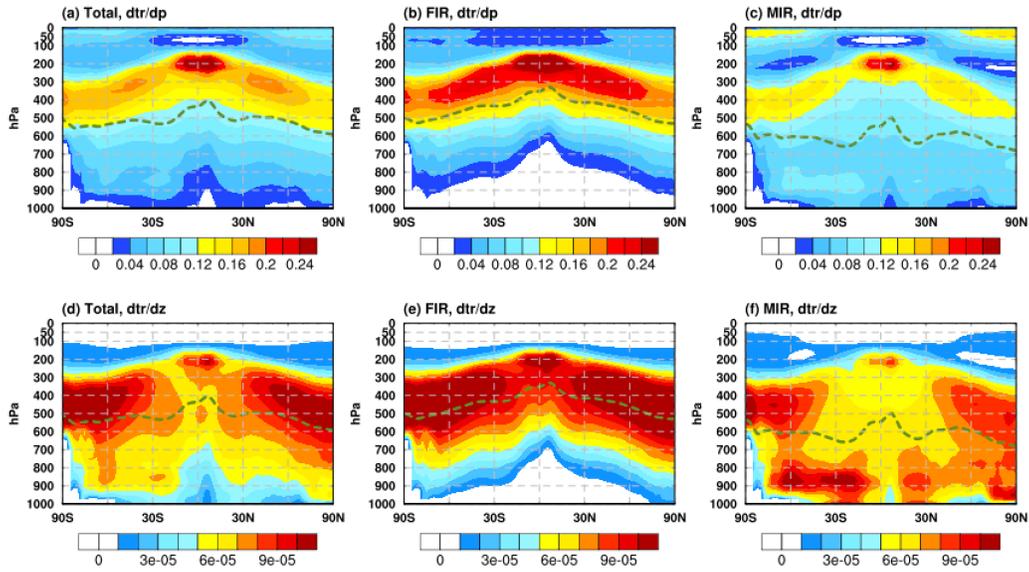
Figure S5. Annual mean derived weighting function in all sky defined as (a, b, c) $\frac{dtr}{dp}$ and (d, e, f) $\frac{dtr}{dz}$. The dashed dark green line is the inferred $\tau = 1$ level. The difference between the $\frac{dtr}{dp}$ and $\frac{dtr}{dz}$ comes from the density (ρ) effect ($\frac{dp}{dz} = -\rho g$), which takes larger values and thus suppresses the value of $\frac{dtr}{dp}$ in the lower layers. In comparison, we see $\frac{dtr}{dz}$ better corresponds to the location of cloud layers (e.g., Figure S5f). Moreover, as expected, the level of maximum values of $\frac{dtr}{dz}$ (panels d-f) better corresponds with the $\tau = 1$ level.

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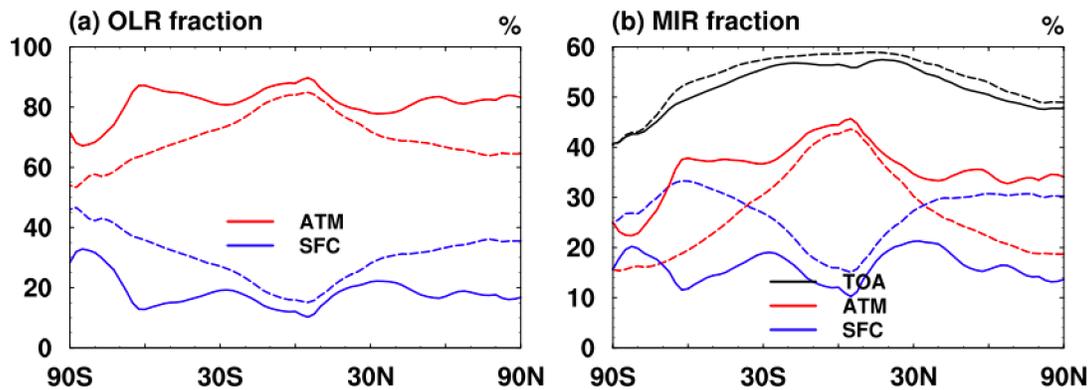
Figure S6. Annual mean (a) atmospheric and surface fractional contribution to the total OLR at the TOA, units: %. (b) zonal mean MIR fraction with respect to local total OLR, decomposed into contributions from the atmosphere and surface, units: %. Solid lines represent the results in all sky and dash lines in clear sky.

In total OLR, the atmosphere makes a major contribution to total OLR (panel a) at each latitude. The MIR fraction at the TOA decreases from the tropics at 60% to about 40% at the poles. The variation of the atmospheric and surface contribution with latitudes are opposite in both total OLR and MIR, as the decrease of water vapor concentration with latitudes weakens the local emission in the atmosphere and allows more surface emission to reach the TOA.

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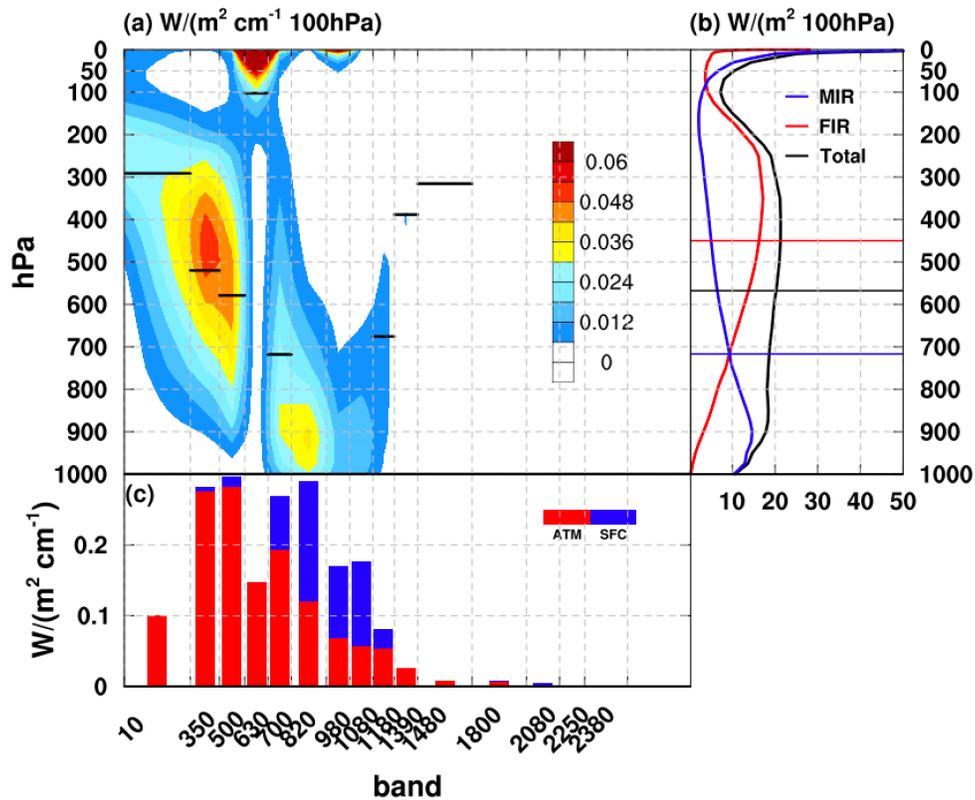
Figure S7. Clear-sky global annual mean spectral and vertical decomposition of OLR. (a) Layer-wise atmospheric contribution to the OLR irradiance flux in each of the 16 RRTMG bands, units: W/(m^2 cm^{-1} 100hPa). (b) Spectrally integrated layer-wise contribution, units: W/(m^2 100hPa). (c) Vertical integrated atmospheric contribution, in comparison with the surface contribution, units: W/(m^2 cm^{-1}). The horizontal lines in (a) and (b) are the inferred $\tau{=}1$ level using the diagnostic method described in Section 2.

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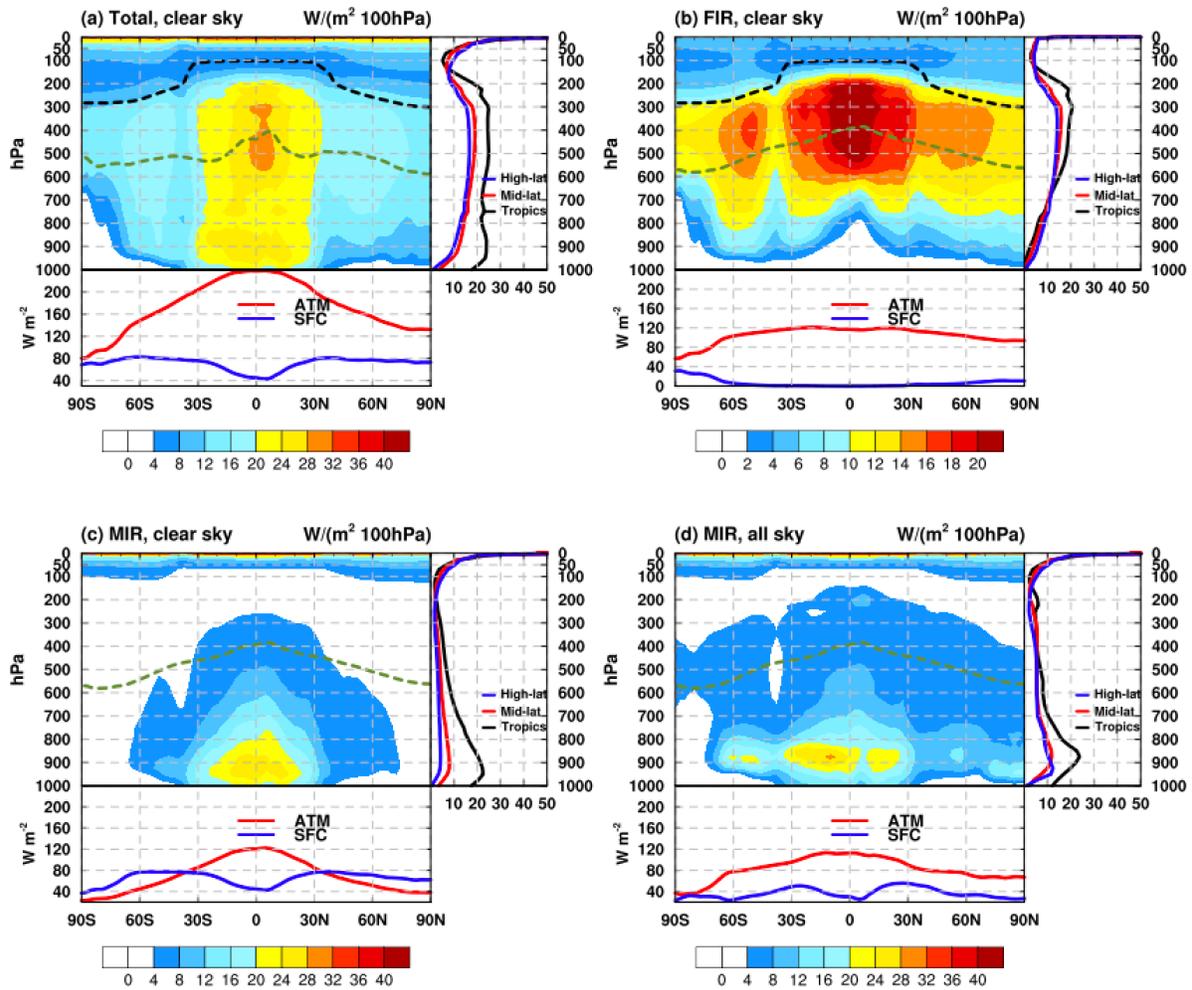
Figure S8. Same as Figure 4, but for the annual and zonal mean OLR fluxes in (a) total OLR, (b) FIR, (c) MIR in clear sky, and (d) MIR in all sky.

The vertical distribution in clear sky is more uniform in total OLR, compared with results in all sky. Different from FIR, the atmospheric contribution in MIR is maximized at the lower atmosphere. In both total OLR and MIR in clear sky, the surface contribution shows a local minimum in the tropics due to the high water vapor concentration and shows little variation in the extratropics. The relatively weaker surface contribution in southern polar region in MIR in clear sky is due to the local lower surface temperature.
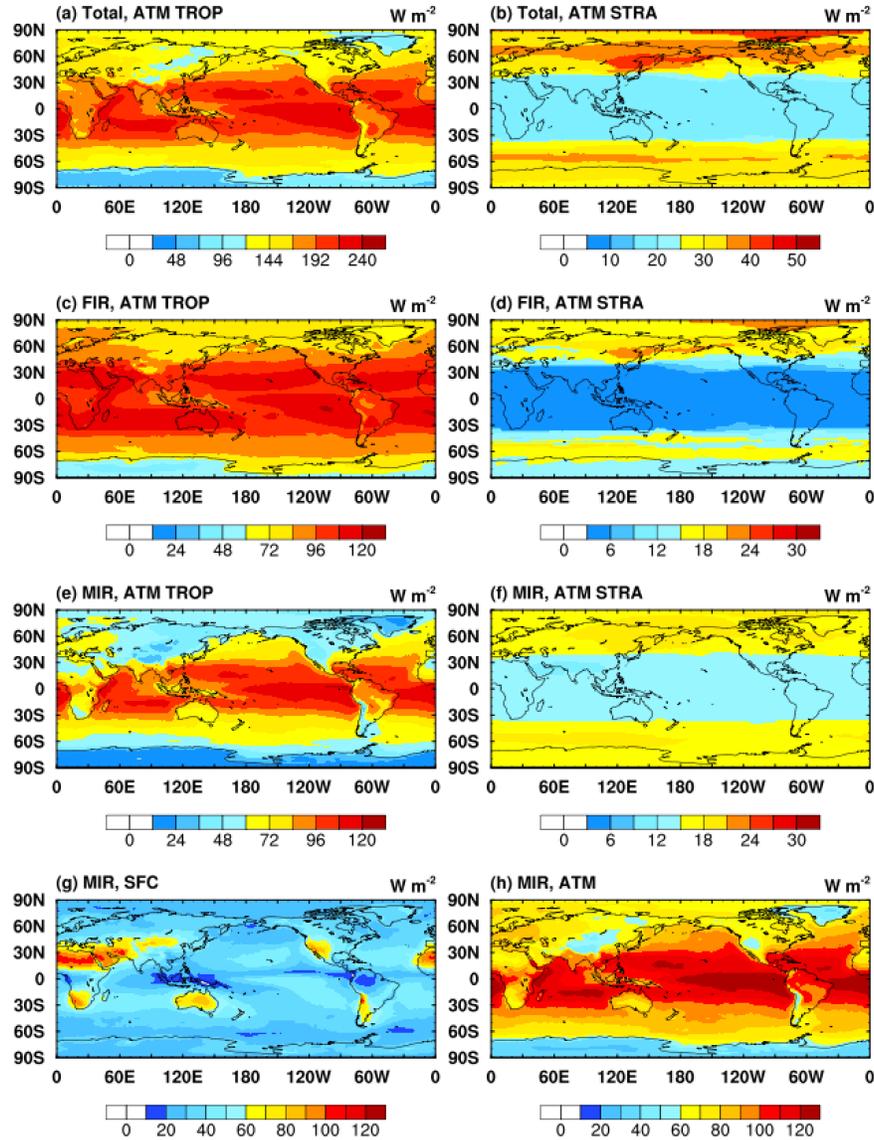
Figure S9. (a-f) Annual mean tropospheric and stratospheric contributions to the total OLR, FIR and MIR in all sky, (g) annual mean surface contribution in MIR, (h) annual mean total column atmospheric contribution in MIR (the sum of (e) and (f)). The troposphere and stratosphere are divided based on the tropopause in Figure 4.

The total OLR and MIR in the troposphere show noticeable gradients from the equator to the poles while FIR is more uniform. All the three plots (Figure S9 a, c, e) show a local minimum contribution in the ITCZ region. In the stratosphere, the contribution is much more uniform than in the troposphere, with a clear contrast between the tropics and extratropics; the weaker contributions in the tropics are due to higher tropopause and lower stratospheric temperature.
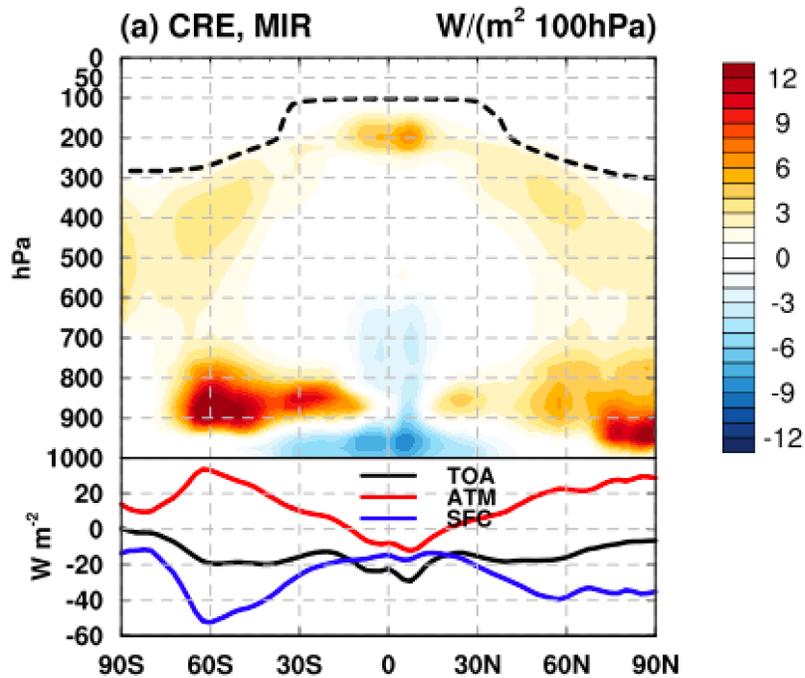
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147 Figure S10. Annual mean and zonal mean cloud radiative effect intensity in MIR, units: W/(m²
148 100hPa). Line plots show the vertically integrated atmospheric contribution and surface
149 contribution, units: W m⁻². The black dash line in contour plots represents the tropopause.
150
151 The CRE in MIR in the tropics comes from both the reduction of transmission in the lower
152 atmosphere and the increase of emission at about 200hPa, while in the extratropics, it is more
153 from the enhanced emission at the cloud layers (e.g., 900hPa in the southern mid-latitude).
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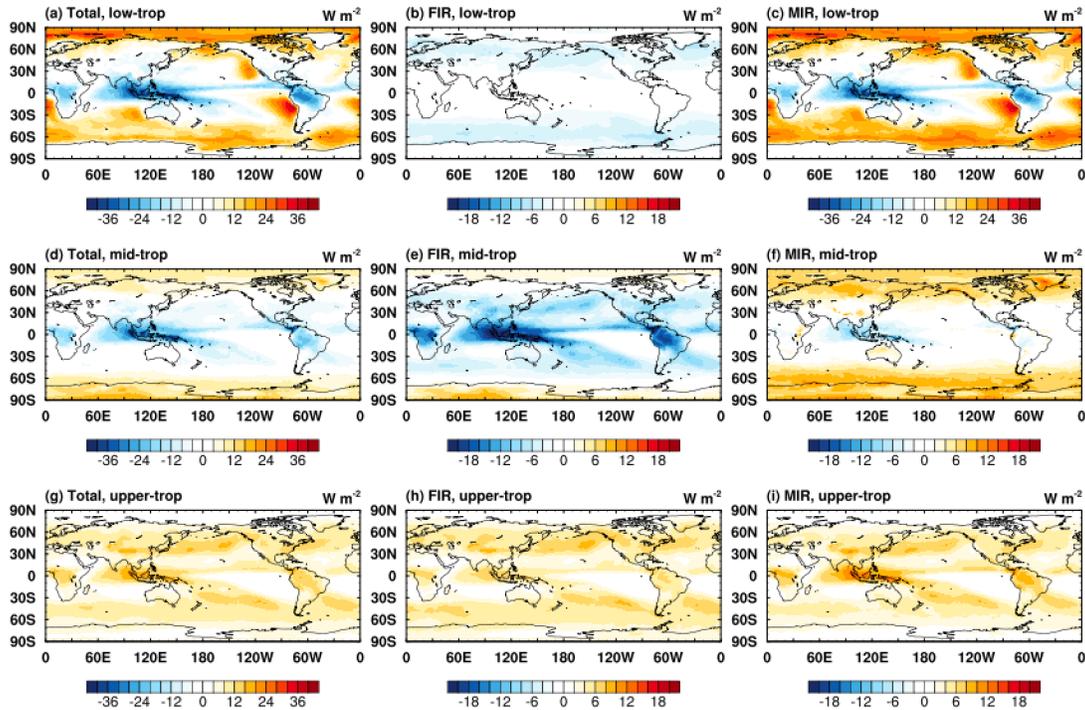
Figure S11. Annual mean cloud radiative effect in the atmosphere of different layers, units: W m^{-2}. Low-trop represents contribution from 1000hPa to 700hPa and mid-trop of 700hPa-400hPa, upper-trop of 400hPa -100hPa.

In the lower-troposphere (first row), CRE is negative in the tropics and positive in the extratropics with regard to the total OLR (panel a), which largely results from the cloud effect in MIR (panel b), where high clouds reduce the atmospheric transmission from this level (lower-troposphere) to TOA in the tropics and low clouds enhance atmospheric emissivity and thus lower-tropospheric contribution to OLR in the extratropics; in contrast, in FIR, due to the strong water vapor absorption, the OLR is insensitive to clouds and the CRE is negligible in the tropics. In the mid-troposphere (second row), the dampened transmission due to higher clouds affects both the total OLR and FIR, while in MIR the change in the tropics is weak and CRE is noticeably more in the mid-to-high latitudes. In the upper-troposphere (third row), the atmospheric contributions all increases due to the increase of atmospheric emissivity caused by the clouds.

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W m^{-2}	all sky		clear sky		CRE (all sky – clear sky)	
	total	FIR	total	FIR	total	FIR
Lower-trop	66.39	18.51	65.80	20.72	0.59	-2.21
Mid-trop	63.75	43.67	67.31	49.07	-3.57	-5.40
Upper-trop	55.04	42.41	46.95	38.39	8.08	4.02
Strato	16.18	4.13	16.18	4.13	0.00	0.00

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179   Table S2. Annual mean and global mean atmospheric contributions in different layers. The cloud
180   radiative effect (CRE) is the difference between the all-sky and clear-sky values, units: W m^{-2}.
181   Lower-troposphere represents contribution from surface (~1000hPa) to 700hPa, mid-troposphere
182   from 700hPa to 400hPa, upper-troposphere from 400hPa to100hPa, and stratosphere from
183   100hPa to TOA. Note that here the definition of stratosphere is different from that in Table 1 The
184   difference between the values roughly measures the contribution in the extratropical lower-most
185   stratosphere (between the tropopause and the 100hPa level).

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