

Onshore entrapment of sea water in coastal aquifers by rapid coastline progradation

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Abstract

We hypothesize that onshore saline groundwater in delta systems may have resulted from rapid shoreline progradation during the Holocene. To explore this hypothesis, we develop a model for the transport of saline groundwater in a shore-normal longitudinal cross-section of an evolving ocean margin. The transport model uses a control volume finite element model (CVFEM), where the mesh of node points evolves with the changing aquifer geometry while enforcing local mass balance around each node. The progradation of the shoreline and evolution of the aquifer geometry is represented by assuming the shoreline advances at a prescribed speed with fixed top and foreset slopes. The combined model of transport and progradation, is used to predict the transient trapping of saline water under an advancing shore-line across a range of realistic settings for shoreline velocity and aquifer hydraulic properties. For homogeneous aquifers, results indicate that the distance behind the shoreline, over which saline water can be detected, is controlled by the ratio of the shoreline progradation rate to the aquifer velocity and the Peclet number. The presence of confining units probably had the greatest impact in sequestering onshore seawater behind an advancing shoreline. Further support for the validity of the proposed model is provided by fitting model predictions to data from two field sites (Mississippi River and Bengal Deltas); the results illustrate consistent agreement between predicted and observed locations of fossil seawater.

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13 **Key Points:**

- 14 • We have developed a transient model of the transport of a saline groundwater in
15 an aquifer under a prograding sedimentary delta
16 • The predicted amount of fossil saline water trapped onshore depends on the ra-
17 tio of the shoreline advancement to the groundwater velocity
18 • Our model predictions are consistent with the entrapment of fossil seawater within
19 the Mississippi River and Bengal Deltas

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Abstract

We hypothesize that onshore saline groundwater in delta systems may have resulted from rapid shoreline progradation during the Holocene. To explore this hypothesis, we develop a model for the transport of saline groundwater in a shore-normal longitudinal cross-section of an evolving ocean margin. The transport model uses a control volume finite element model (CVFEM), where the mesh of node points evolves with the changing aquifer geometry while enforcing local mass balance around each node. The progradation of the shoreline and evolution of the aquifer geometry is represented by assuming the shoreline advances at a prescribed speed with fixed top and foreset slopes. The combined model of transport and progradation, is used to predict the transient trapping of saline water under an advancing shore-line across a range of realistic settings for shoreline velocity and aquifer hydraulic properties. For homogeneous aquifers, results indicate that the distance behind the shoreline, over which saline water can be detected, is controlled by the ratio of the shoreline progradation rate to the aquifer velocity and the Peclet number. The presence of confining units probably had the greatest impact in sequestering onshore seawater behind an advancing shoreline. Further support for the validity of the proposed model is provided by fitting model predictions to data from two field sites (Mississippi River and Bengal Deltas); the results illustrate consistent agreement between predicted and observed locations of fossil seawater.

Plain Language Summary

Saltwater intrusion in coastal aquifers is generally thought to be due to excessive pumping. Here we propose that the rapid advance of the delta front due to lateral sediment transport can entrap seawater onshore. We developed a cross-sectional mathematical model to understand the key controls on onshore seawater entrapment by sediment progradation. Using this model, we found that the ratio of the lateral coastline advance velocity over the groundwater velocity as well as the ratio of advective to dispersive solute transport plays a key role in the extent of seawater capture onshore. Additional analysis showed that the ratio of vertical advective to diffusive transport and the presence of low permeability confining units are also important in the trapping of onshore seawater. We applied our model to the Bengal and Mississippi River deltas using published estimates of shoreline progradation and salinity conditions. Our model is as able to reproduce observed onshore saline water consistent with our hypothesis.

1 Introduction

Over the past several decades, there has been growing concern regarding how onshore groundwater pumping has led to seawater intrusion within coastal aquifer systems (Barlow & Reichard, 2010; Han et al., 2015). More recently, the specter of sea level rise (Chui & Terry, 2013; Lee et al., 2016) and tsunami activity (Violette et al., 2009; K.G. Villholth & Neupane, 2011; Pauw et al., 2012) has also been shown to result in coastal groundwater salinization.

Within the Bengal delta aquifer system, onshore saline groundwater exists within both a deep confined and unconfined aquifer system at depth range between about 40m to 120m and extending 50km onshore (Figure 1a-1b). This onshore seawater appears to be unrelated to any of the above mechanisms. The Bengal Delta has experienced relatively high sediment fluxes resulting in the lateral migration of the coastline ocean-ward by over 100km have been deposited onshore (Kuehl et al., 2005). As a comparison, the Mississippi delta has a higher aquifer conductivity and thus lower onshore salinities. In the Mississippi River Delta brackish water extends about 60km inland (Figure 1c; Chamberlain et al. 2018).

68 We hypothesize that rapid deposition of sediments during the Holocene has resulted
 69 in entrapment of seawater onshore. In this study, we have developed a coupled sediment
 70 transport and groundwater flow/solute transport model to explore under what condi-
 71 tions, seawater can be trapped on shore. Below, we present a sensitivity study that con-
 72 sideres different ratios of sediment velocity to hydraulic conductivity that we believe con-
 73 trols the distribution of fossil seawater onshore. We also assess how the hydrodynamic
 74 dispersion/diffusion influences onshore seawater sequestration. Finally, We attempt to
 75 match field conditions within the Bengal Delta and the Gulf of Mexico using this model
 as a means of qualitatively providing ground truth for our hypothesis.

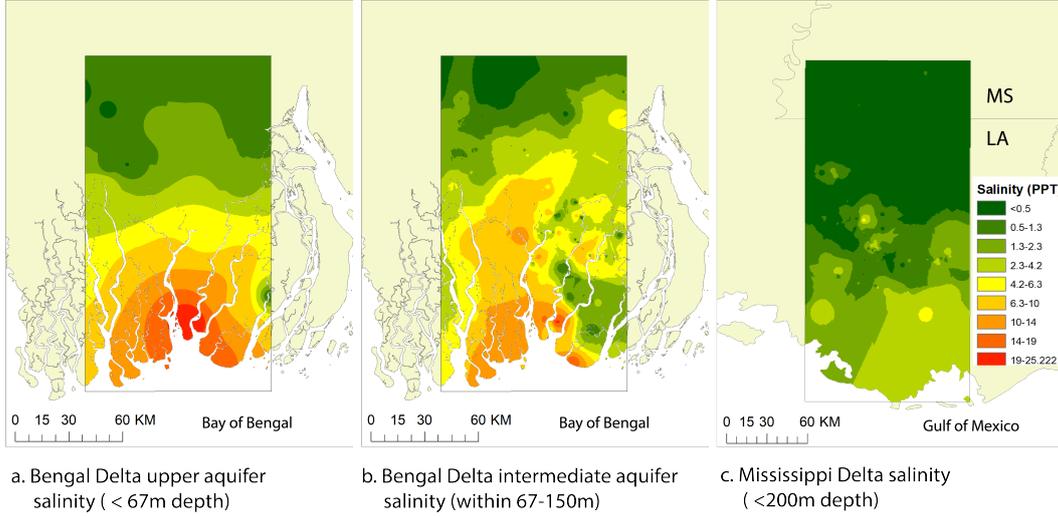


Figure 1. Interpolation maps of Bengal Delta (a & b) and Mississippi River Delta (c) showing planview salinity data (BWDB, 2013).

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77 2 Methods

78 Below we present the govern transport equations and numerical solution scheme
 79 used in this paper.

80 2.1 Governing Equations

Our governing variable-density groundwater flow equations uses freshwater heads (Post et al., 2007) given by

$$h = \frac{p}{\rho_w g} + y \quad (1)$$

where p [Pa] is pressure, g [m/s^2] is gravity, y [m] is elevation, and ρ_w is the freshwater density (1000 kg/m^3). The governing equation for the conservation of fresh and saline water in an aquifer can be written as (Fahs et al., 2016)

$$S_s \frac{\partial h}{\partial t} = \frac{\partial}{\partial x} \left[K_x \left(\frac{\partial h}{\partial x} \right) \right] + \frac{\partial}{\partial y} \left[K_y \left(\frac{\partial h}{\partial y} + C(\rho_{rel} - 1) \right) \right], \quad (2)$$

Here, K_x, K_y [m/s] are the isotropic hydraulic conductivity tensor components (variations with saline concentrations have been neglected), S_s [1/m] is the specific storage, ρ_{rel} [-] is the ratio of the density of saturated saline to fresh water, and C [-] is the salt concentration ($C = 1$ corresponding to the saturated condition). Note we can write eq.

(2) in the condensed form as

$$S_s \frac{\partial h}{\partial t} = \frac{\partial}{\partial x} [-q_x] + \frac{\partial}{\partial y} [-q_y], \quad (3)$$

where the discharge components are defined as

$$q_x = -K_x \left(\frac{\partial h}{\partial x} \right), \quad q_y = -K_y \left(\frac{\partial h}{\partial y} + C(\rho_{rel} - 1) \right), \quad (4)$$

The associated governing equation for the conservation of solute (salt) is (Fahs et al., 2016)

$$\begin{aligned} \phi \frac{\partial C}{\partial t} = & \frac{\partial}{\partial x} \left[-q_x C + D_{xx} \left(\frac{\partial C}{\partial x} \right) + D_{xy} \left(\frac{\partial C}{\partial y} \right) \right] \\ & + \frac{\partial}{\partial y} \left[-q_y C + D_{xy} \left(\frac{\partial C}{\partial x} \right) + D_{yy} \left(\frac{\partial C}{\partial y} \right) \right], \end{aligned} \quad (5)$$

where the dispersion tensor is defined as (Bear, 1972)

$$D_{xx} = \alpha_L \frac{q_x^2}{|\vec{q}|} + \alpha_T \frac{q_y^2}{|\vec{q}|} + \phi D_{mol}, \quad (6a)$$

$$D_{yy} = \alpha_T \frac{q_x^2}{|\vec{q}|} + \alpha_L \frac{q_y^2}{|\vec{q}|} + \phi D_{mol}, \quad (6b)$$

$$D_{xy} = (\alpha_L - \alpha_T) \frac{q_x q_y}{|\vec{q}|}, \quad (6c)$$

ϕ is porosity, α_L and α_T [1/m] are the longitudinal and transverse dispersivity coefficients, and D_{mol} [m²/s] is the molecular diffusion of salt in water. Again, on defining the solute fluxes as

$$q_x^C = q_x C - D_{xx} \left(\frac{\partial C}{\partial x} \right) - D_{xy} \left(\frac{\partial C}{\partial y} \right) \quad (7a)$$

$$q_y^C = q_y C - D_{xy} \left(\frac{\partial C}{\partial x} \right) - D_{yy} \left(\frac{\partial C}{\partial y} \right) \quad (7b)$$

we can write this conservation equation in the condensed form as

$$\phi \frac{\partial C}{\partial t} = \frac{\partial}{\partial x} [-q_x^C] + \frac{\partial}{\partial y} [-q_y^C], \quad (8)$$

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2.2 The solution domain

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Figure 2 shows the finite element mesh and solution domain for our model. At a given time $t > 0$, the aquifer domain consists of land and sea-bed components, comprising a subaerial, fluvial topset and submarine foreset and seafloor. The elevations of the seafloor (B) and sea-level (SL) are assumed constant. If the water table is at or close to the land surface, the boundary condition on of this domain are as follows

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- The domain bottom and sides are no-flow boundaries.
- On the topset ($\eta(x) \geq SL$) the solute concentration is set to $C = 0$ and the head is set as $h = \eta(x)$, where $\eta(x)$ is the current land surface elevation at seaward distance $0 \leq x \leq L$.
- On the seabed (foreset and seafloor, $\eta(x) < SL$) the solute concentration is set to the seawater concentration, $C = 1$ and the head is set to the equivalent freshwater value $h = \eta(x) + (SL - \eta(x))\rho_{rel}$, where $\eta(x)$ is now the elevation of the seabed.

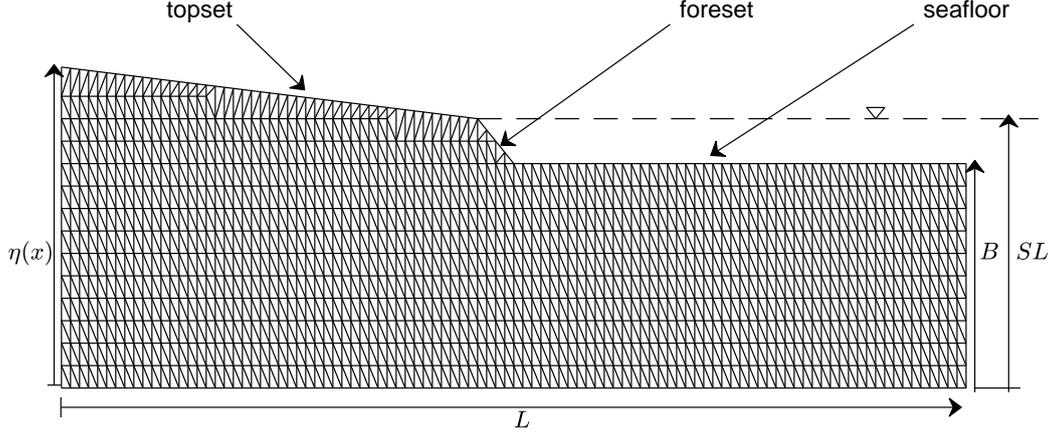


Figure 2. The solution domain and finite element discretization, at time $t > 0$. (Height to Length aspect ratio is 25).

95 A key part of the proposed model is that the domain evolves through time. At the
 96 initial time, $t = 0$, the highest point in the domain is at the sea-level (see top left schematic
 97 in Fig. 3), comprising just the submerged foreset and seafloor. At this initial time, the
 98 following conditions are imposed:

- 99 • The shoreline (beach) is at $x = 0$.
- 100 • The toe of the foreset (the point of intersection between the foreset and seafloor
 101 is at $x_{toe} = (SL - B)/S_f$, where S_f is the slope of the foreset.
- 102 • The entire aquifer contains fully saturated saline water, $C = 1$ (seawater).

103 On appealing to the successful models of sedimentary basin evolution, based on purely
 104 geometric constructs (e.g., see Voller et al., 2020; Reynolds et al., 1991; Kim et al., 2006;
 105 Lorenzo-Trueba et al., 2009), we evolve the domain in time, by assuming that the flu-
 106 vial topset S_t and foreset S_f slopes retain constant values. Then, by simply translating
 107 the toe of the foreset at a prescribed seaward velocity (v_{toe}), we can produce a physi-
 108 cally realistic model for the advance of a shoreline, with a characteristic clinoform, over
 109 an ocean seafloor, see schematics in Fig. 3.

110 2.3 Control Volume Finite Element Model (CVFEM)

At a given time step $t > 0$, a mesh of linear triangular finite elements are used
 to discretize the domain. Each element e is associated with three linear shape functions,
 $N_i^e(x, y)$, $i = 1, 2, 3$ (Zienkiewicz et al., 2005), each function taking a value of unity at
 a specified vertex (node=1,2,3) and linearly reducing to zero on the element side oppo-
 site the node. In this way, we can provide a linear approximation for a dependent vari-
 able $u = h$ or C , over the element e , as

$$u^e(x, y) = N_1 u_1 + N_2 u_2 + N_3 u_3 \quad (9)$$

To move forward with the approximation afforded by the finite element discretiza-
 tion we note that our governing head eq.(3) and concentration eq.(8) equations can be
 written in the generic form

$$\mu \frac{\partial u}{\partial t} = \frac{\partial}{\partial x} [-q_x^u] + \frac{\partial}{\partial y} [-q_y^u], \quad (10)$$

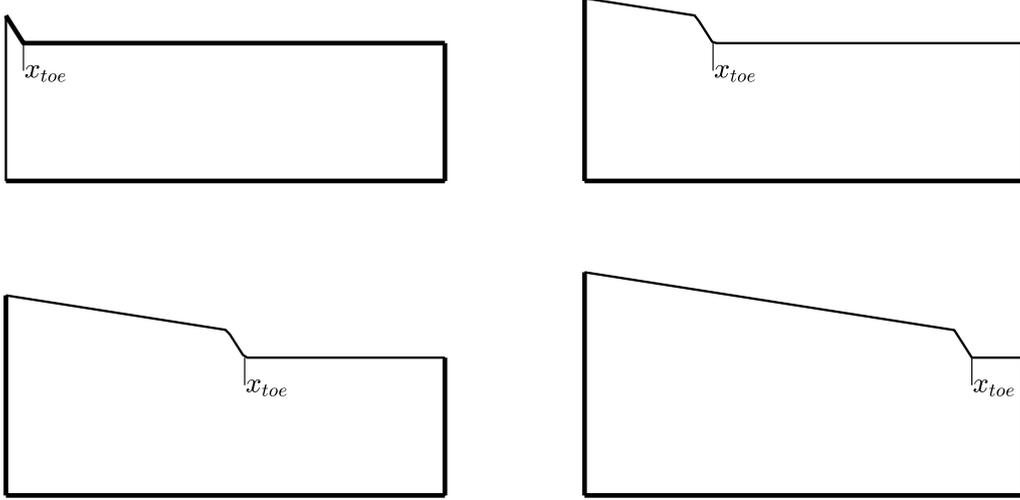


Figure 3. Schematic diagram denoting the model geometry changes in time. The initial domain (top left) only involves the submarine foreset and seafloor. As time increase, the toe (the intersection of the foreset with the seafloor) advances with a prescribed velocity, leading to the appearance of a subaerial topslope. This geomorphology develops in time, under the conditions of constant top- and fore- set slopes, until the model termination (bottom right) when the toe is 95% across the domain L .

111 For the head calculation, $u = h$, $\mu = S_s$, and the the flux components q_x^u and q_y^u are
 112 defined by eq.(4), in the concentration calculation $u = C$, $\mu = \phi$, and the flux compo-
 113 nents are defined by eq.(7).

On integrating the generic conservation equation, over a closed fixed control volume Ω , with surface Γ , followed by an application of the divergence theorem we arrive at

$$\frac{d}{dt} \int_{\Omega} \mu u \, dV = - \int_{\Gamma} q_x^u n_x + q_y^u n_y \, dS \quad (11)$$

114 where $n = (n_x, n_y)$ is the outward pointing normal on Γ .

The key construction in the Control Volume Finite Element Method (CVFEM) is to add an additional component to the mesh. By joining the mid point of each element to the mid point of each element side, see Fig. 4, we create a tessellation of closed control volumes around each node (element vertex) in the domain. We can associated each of these control volumes with the control volume of the integral equation in eq.(11). Then, following the detail in (Voller, 2009), we can used the geometric properties of the elements and the finite element approximations eq.(9), to numerical approximate the integrals in eq.(11) in terms of the nodal values of the dependent variables. This step produces the following point-wise, time implicit, update, for each node i in the domain mesh

$$\mu V_i u_i = \mu V_i^{old} u_i^{old} + \Delta t \left[\sum_{j=nb} a_j u_j - a_i u_i \right] \quad (12)$$

115 where V_i is the volume (area) of the control volume, the superscript *old* refers to the pre-
 116 vious time step value, the summation is over the neighboring nodes to i , i.e, the nodes
 117 that share a common element edge with node i , the a 's are known coefficients, and Δt
 118 is the time step. In arriving at the coefficients for the concentration equation ($u = C$)

119 an upwind approximation is used (Patankar, 1980), i.e., the concentration in the advective
 120 contribution is associated with the nodal value of the control volume from which the
 121 discharge emerges.

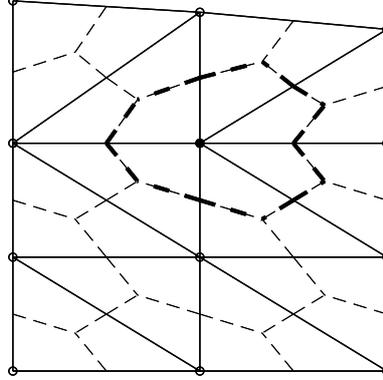


Figure 4. A section of the mesh showing nodes (circles), finite elements (solid lines) and control volumes (dashed lines). The control volume associated with node denoted by the filled circle is shown as a bolded dashed line.

122 The derivation of discrete update in eq.(12), naturally accounts for no flow bound-
 123 aries. At fixed value domain boundary nodes, the update is replaced by an update that
 124 imposes the required value for u_i . Each node i on the the domain boundary, has a control
 125 volume surface area, A_{bi} , coincident with the domain boundary. In this way, at a
 126 node i on a domain boundary with a prescribed water flux, q_{in} [m^3/s], the additional
 127 contribution $\Delta t q_{in} A_{bi}$ is added to right-hand side of eq.(12) when updating the head.

128 A separate equation in the form of eq.(12) is solved for both the head and the con-
 129 centration. In a time step, the head is updated and groundwater discharges determined,
 130 before solving for the concentrations. In the head update, the q_y discharge component
 131 (see second term of eq.(4)) is evaluated using the previous time values of C . A point-
 132 wise Jacobi iterative scheme is used in the update; a scheme well suited for vectoriza-
 133 tion and one that avoids the directional ('skewing') errors that can be induced with Gauss-
 134 Seidel iteration. Convergence is declared when the largest value of $|u_i - u_i^{old}|$, $i = 1, 2, \dots, N$
 135 (total nodes in the domain), between iterations, falls below a prescribed tolerance $tol \sim$
 136 $10^{-8} - 10^{-6}$.

137 2.4 Mesh evolution and motion

138 In our calculations, to account for the evolving shoreline, the finite element mesh
 139 changes with each time step, a schematic of the evolution of the mesh is shown in Fig.
 140 5. In the mesh there is a fixed number n_{cols} of vertical grid lines (columns), at equally
 141 spaced locations $x_j = j\Delta x$, $j = 0, 1, \dots, n_{cols}$, where $\Delta x = L/(n_{cols} - 1)$. Within each
 142 time step, starting from the bottom of each column, node points are arranged with a fixed
 143 vertical spacing Δ , at locations $y_i = i\Delta$, $i = 0, 1, \dots, top-1$. The fixed spacing is over-
 144 ridden, in placing the last node with index top . This node, assuming a purely deposit-
 145 ing system, tracks the movement of the land/seabed surface, i.e., $y_{top} = \eta(x_j, t)$. To
 146 reduce grid distortion, at the point where the spacing between the top node in a column
 147 and the node blow, exceeds 1.5Δ , i.e., $y(t)_{top} - top\Delta > 1.5\Delta$, the node index of the
 148 top node is advanced $top^{new} = top+1$ and a new fixed position node, with index $ins =$
 149 top , is inserted on the column, at position $y_{ins} = ins\Delta$. Values of the dependent vari-

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ables h_{ins} and C_{ins} at the inserted node are found by linear interpolation between the values at nodes top and $ins - 1$.

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We note that, the advance of the top surface nodes in each column and, when required, the addition of the new nodes below the advancing surface, will cause the control volumes associated with top surface nodes to change shape and size within a time step, Fig. 5. To simplify the calculation, we assume, that any conserved quantity added or subtracted, as a result of changes in control volume size, does not change the average value in the control volume. Essentially, this means that we can associate previous time nodal values with the current time control volume, i.e., in our iterative scheme, eq.(12), we can set $V_i^{old} = V_i$. We expect that any limitations in this approximation will be exposed in a mesh size /time step dependence study.

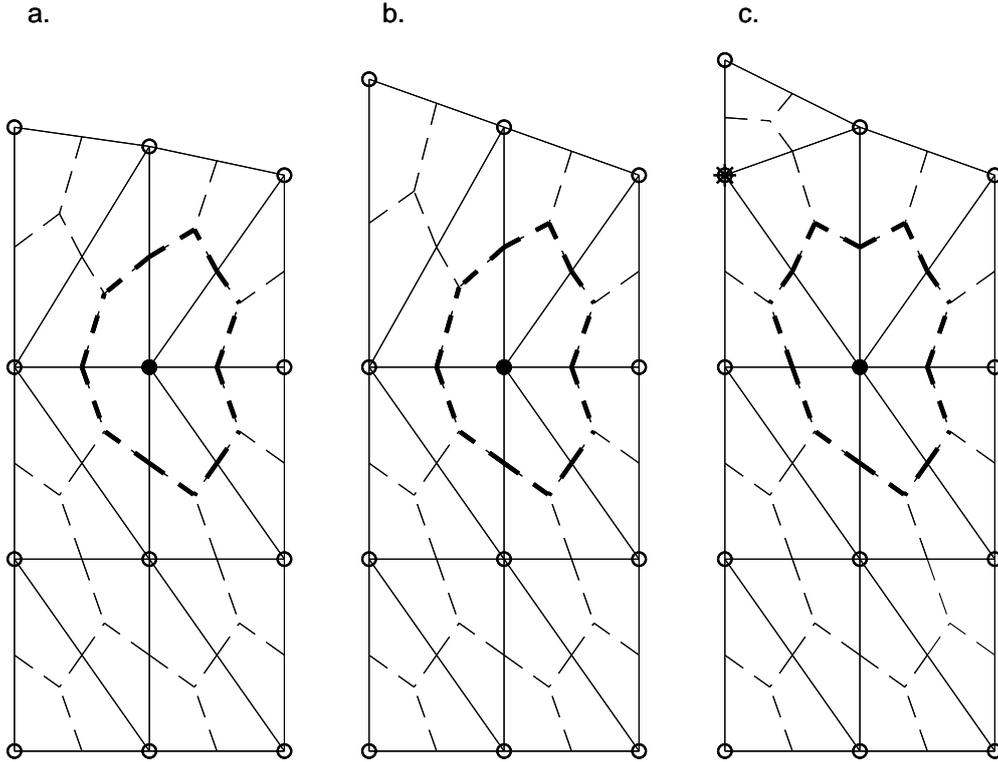


Figure 5. Mesh motion. a. The non-top nodes in each mesh column have fixed location and spacing Δ . b. The top nodes move with the land/sea-bed surface. If a top node reaches a vertical position that is more than 1.5Δ above the node below a new node (indicated by the asterisk) is inserted to maintain the Δ spacing.

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2.5 Code verification

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The code was verified by repeating ‘Test Case 2’ in (Fahs et al., 2016), where a semi-analytical steady-state solution for the Henry problem is presented. The two-dimensional rectangular problem domain is $1 \times 3(L)m$. The physical properties of the aquifer are $\alpha_L = 0.1$ m, $\alpha_T = 0.01$ m, $D_{mol} = 9.43 \cdot 10^{-8}$ m²/s, $K_x = K_y = 0.01$ m/s, $\rho_{rel} = 1.025$, $\phi = 0.25$, and $S_s = 0$ m⁻¹. The boundary conditions for the head are, top and bottom no flow boundaries, a fixed fresh water flux $q_{in} = 6.6 \cdot 10^{-5}$ m³/m²-s on the left, and an equivalent fresh water head $h = y + (1 - y)\rho_{rel}$ on the right. The boundary conditions

169 on the solute are, no flow boundaries, top and bottom, and fixed concentration values
 170 on the left ($C = 0$) and right ($C = 1$).

171 The linear finite element mesh is created through a Delaunay triangulation on a
 172 grid of 81×241 equally spaced nodes. To approach steady state, 60,000 time steps of
 173 0.5 seconds are used, a tolerance of $tol = 10^{-8}$ is used to determine convergence.

174 Figure 6 shows plots for steady state predictions for the 10%, 50%, and 90% con-
 175 tours of salt concentration. The 50% contour is directly compared (at $y = 0.2, 0.4, 0.6, 0.8,$
 176 and 1) with steady state values abstracted from Fig. 5 in (Fahs et al., 2016).

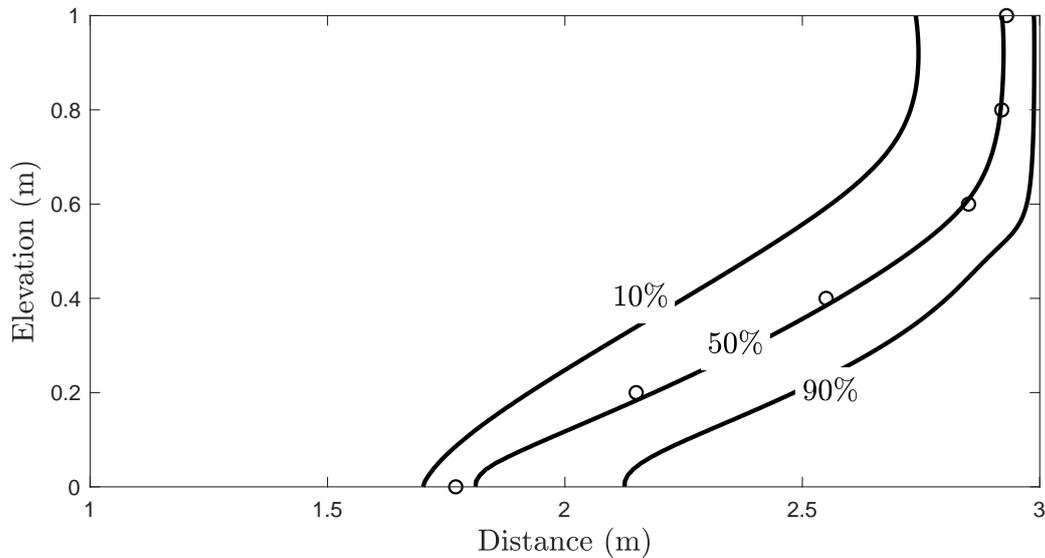


Figure 6. Predictions of contours of salt concentration. The open circles are values for the 50% contour abstracted from the semi-analytical solution in Fig. 5 of (Fahs et al., 2016). Note. the scale of this verification test problem 1×3 m, is much smaller than typical field scales

177 2.6 Model simplifications

178 The main purposes of our model is to demonstrated that saline water can be trapped
 179 under the land mass as the shoreline progrades and to identify the key system param-
 180 eters that control the level of seawater trapping. Our basic model for this demonstra-
 181 tion assumes a simplified constant slope geometry for the domain, a homogeneous aquifer
 182 material with constant conductivity, porosity, and storage, and a fixed relative sea-level
 183 change. We recognize that relaxing these settings in our model will affect the details of
 184 our predictions but expect that they will not undermine the observed general behavior.
 185 Thus, we posit that the simplifications in our basic treatment are appropriate for the mod-
 186 eling task at hand, broad prediction of the pattern of saline water as a shoreline advances.
 187 Note, however, following presentation of results with our basic model we do make ad-
 188 ditional runs where we consider confining units—rectangular regions in the aquifer with
 189 different conductivity and porosity values.

190 **2.7 Dimensionless groups controlling onshore seawater entrapment**

191 Here we present some heuristic arguments toward identifying the dimensionless groups
 192 that control the level of aquifer seawater trapping under a shoreline advances. We have
 193 identified two process that control seawater trapping.

The first process is the competition between the rate of advance of the shoreline, dimensions $[LT^{-1}]$, and the flow velocity of the freshwater recharge $[LT^{-1}]$. If the shoreline advance is more rapid than the lateral groundwater velocity we should expect the seawater trapping to increase. In our geometric sedimentation model, the rate of the shoreline advance is directly given by the prescribed foreset toe velocity v_{toe} . On noting that the driving head gradient, for onshore groundwater flow, is the fluvial topslope, we can characterize the flow velocity of the freshwater recharge as $K_x S_t / \phi$. In this way we see that dimensionless group

$$G_v = \frac{v_{toe}\phi}{K_x S_t} \quad (13)$$

194 accounts for the competition between shoreline toe advance and freshwater recharge; when
 195 G_v is large we expect the shoreline advance to outrun the recharge and promote seawater
 196 trapping.

197 The second process that controls seawater trapping is the level of mixing between
 198 fresh and saline water. Typically, in advection-dispersion systems, mixing is controlled
 199 by a Peclet number. We can construct an appropriate Peclet number for our system by
 200 considering the ratio of the product of a length scale $[L]$ and a characteristic discharge
 201 value \tilde{q} $[LT^{-1}]$, to a characteristic dispersivity \tilde{D} $[L^2 T^{-1}]$. In our system, choosing the
 202 length scale as the system depth SL and setting the characteristic dispersivity as $\tilde{D} =$
 203 $\alpha_L \tilde{q}$, arrives at the Peclet number

$$P_e = \frac{SL\tilde{q}}{\alpha_L \tilde{q}} = G_m = \frac{SL}{\alpha_L} \quad (14)$$

204 When the group G_m is large we would expect the mixing between fresh and salt water
 205 to be reduced, leading to an increase in seawater trapping.

So taken together, we propose that the effects of shoreline velocity to recharge and mixing, on seawater trapping is controlled by the dimensionless group

$$G_T = G_v G_m = \left[\frac{v_{toe}\phi}{K_x S_t} \right] \left[\frac{SL}{\alpha_L} \right] \quad (15)$$

206 **3 Results**

207 In order to explore the effects of changing hydrogeologic properties and solute mixing,
 208 we conducted a sensitivity analysis in which we varied the hydraulic conductivity
 209 of the sediments and the longitudinal/transverse dispersivity (Table 1). Because the water
 210 table gradient is fixed by the landward topographic slope, hydraulic conductivity serves
 211 as a proxy for groundwater velocity. Simulation parameters that were not varied in the
 212 sensitivity study are listed in Table 2. In three simulations (8-10), we included a relatively
 213 low-permeability, semi-confining unit 100m thick.

214 For all model runs, we used a domain 300km in length with 101 nodal columns spaced
 215 3 km apart and a maximum sediment thickness of 400 m. The vertical nodal spacing used
 216 was 37.5m. The model was run for 16,370 years using a fixed time step size of 100 days.
 217 Over the simulation, the shoreline migrated about 220km. At the end of the simulation,
 218 the grid was composed of 1017 nodes and 1195 elements. We present ten simulations in
 219 our sensitivity study. One simulation (run 1) we termed the “base case” (Table 1). This
 220 simulation used a hydraulic conductivity (K_x) of 5 m/day and a longitudinal dispersivity
 221 (α_L) of 50m. Figure 6 depicts changes in salinity through time for the base case. Note

Table 1. Parameters varied in sensitivity study.

| Run | Aquifer Kx (m/day) | α_L | G_T | Confining Unit Kx (m/day) | Figure |
|-----|--------------------------|------------|-------|---------------------------------|--------|
| 1 | 5 | 50 | 33.6 | - | 6-14 |
| 2 | 10 | 50 | 16.8 | - | 10-11 |
| 3 | 50 | 50 | 3.36 | - | 10-11 |
| 4 | 150 | 50 | 1.12 | - | 10-11 |
| 5 | 5 | 40 | 42 | - | 8-9 |
| 6 | 5 | 30 | 56 | - | 8-9 |
| 7 | 5 | 20 | 84 | - | 8-9 |
| 8 | 5 | 40 | 21 | 0.5 | 12-14 |
| 9 | 5 | 30 | 14 | 0.05 | 12-14 |
| 10 | 5 | 20 | 14 | 0.005 | 12-14 |
| 11 | 20 | 70 | 5.14 | 0.005 | 16b |
| 12 | 50 | 30 | 29.3 | - | 16c |

Table 2. Properties held constant.

| Parameter | Definition | Value | Units |
|------------|------------------------------|---------------|----------------|
| K_x/K_y | anisotropy | 100 | dimensionless |
| D_d | solute diffusion coefficient | 10^{-5} | $m^2 day^{-1}$ |
| | top slope | 0.005 | dimensionless |
| | fore slope | 0.05 | dimensionless |
| | toe velocity | 0.04 | $mday^{-1}$ |
| S_s | specific storage | 10^{-3} | m^{-1} |
| Δt | time step size | 100 | Days |
| α_T | transverse dispersivity | $0.1\alpha_L$ | m |

222 that a normalized concentration of 1 is equivalent to seawater and has a fluid density of
 223 1025 kg/m³.

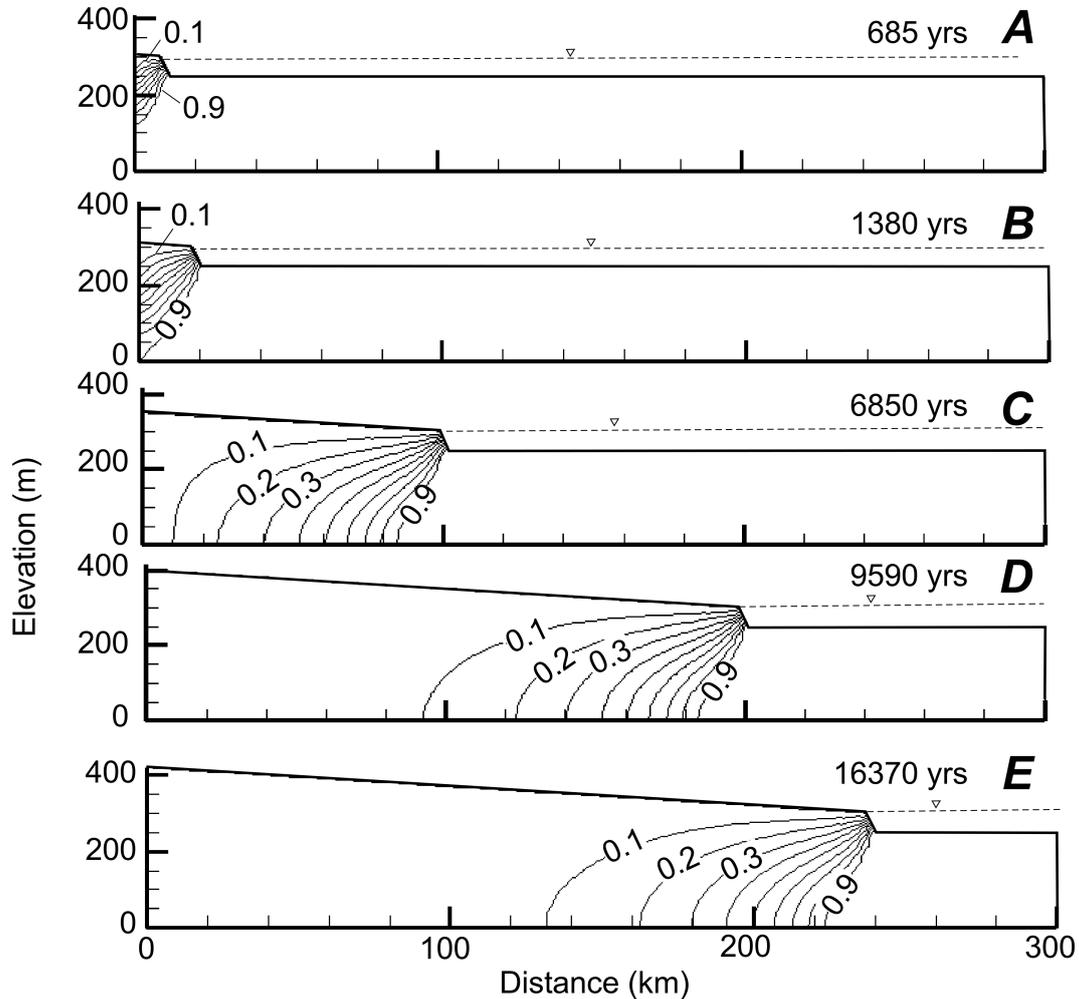


Figure 7. Salinity evolution through time during shoreline progradation for the base case.

224 During early times, onshore freshwater propagates downward towards the bottom
 225 of the model domain (Fig. 7a-7b). This is because connate seawater must first be dis-
 226 placed by freshwater before lateral flushing can take place. During this time period, there
 227 are significant changes in the magnitude of groundwater flux vertically (Fig. 8a-8c). The
 228 lateral migration of the solute front is negligible. Once the toe of the freshwater-saltwater
 229 mixing zone attaches to the bottom of the domain (Fig. 7c-7e) it migrates laterally, lag-
 230 ging behind the shoreline toe. At early times, fluxes are highest near the land surface.

231 Longitudinal and transverse dispersivities strongly influences the downward rate
 232 of propagation of the solute front. The lower the dispersivity, the longer it takes for the
 233 freshwater to reach the base of the model domain and begins to migrate laterally. The
 234 final distribution of salinity at the end of each model run is shown in Figure 9 for lon-
 235 gitudinal dispersivities between 50m to 20m. Recall that transverse dispersivities are set
 236 to be an order of magnitude lower (Table 2). More seawater is “trapped” on shore be-
 237 cause of the higher lag times for the freshwater interface to reach the base of the model
 238 domain with lower dispersivities. The relative positions of the shoreline toe and the toe
 239 of the freshwater-seawater mixing zone (normalized concentration of 0.05) through time

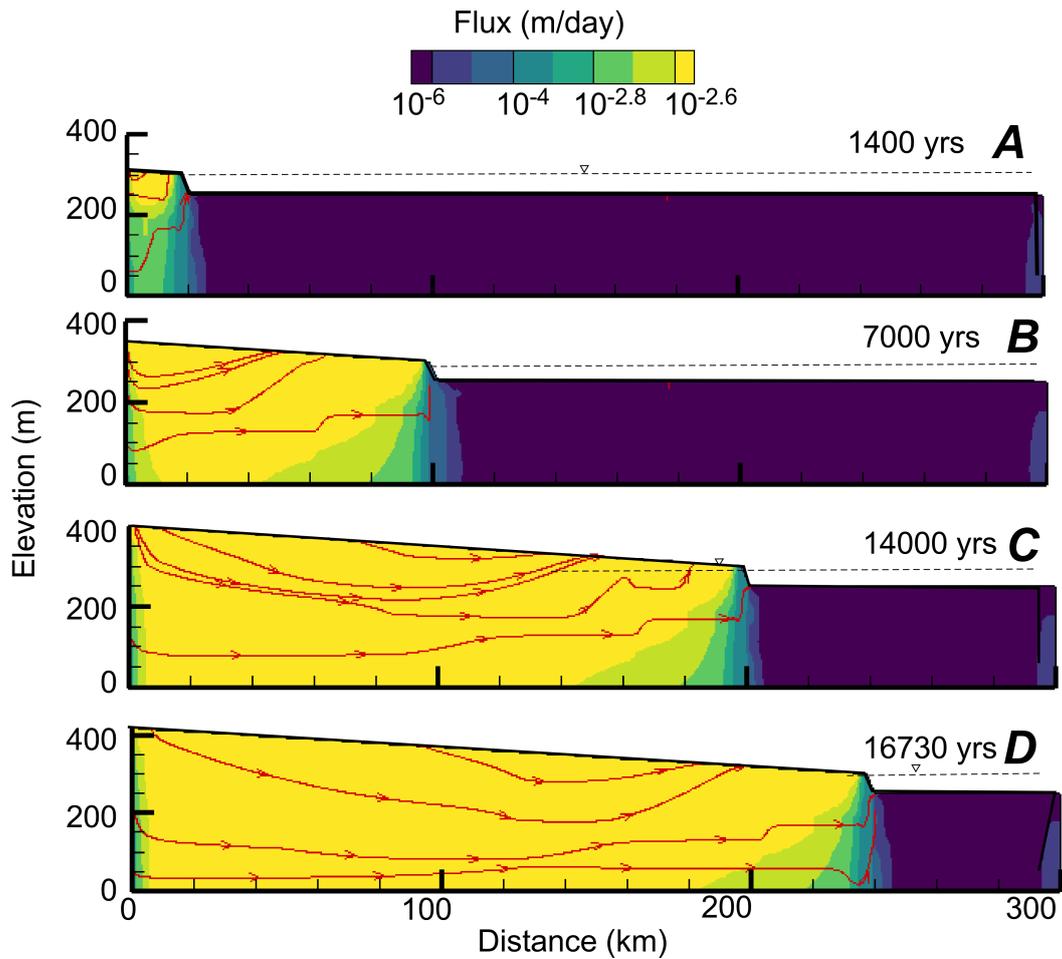


Figure 8. Groundwater flux evolution during shoreline progradation for the base case model run.

240 for the dispersivity model runs 1, 5-8 are shown in Figure 10. The toe of the interface
 241 lines do not begin at time equal zero because the freshwater toe has not reached the bot-
 242 tom the interface at early time is near the upper boundary. The portions of these lines
 243 that have curvature represent early time behavior when the freshwater-saltwater mix-
 244 ing zone is just reaching the base of the solution domain. Linear behavior occurs when
 245 the magnitude of the lateral velocity field becomes stationary. For the lowest dispersiv-
 246 ity ($\alpha_L = 10\text{m}$), the lateral velocity field is never reached.

247 Changes in hydraulic conductivity also influences the rate of lateral propagation
 248 of the solute front (Figure 11). Higher hydraulic conductivity results in a linear increase
 249 in groundwater flow rates because the onshore water table slope is fixed at the land sur-
 250 face elevation. The higher the groundwater flow rates, the closer the freshwater-seawater
 251 mixing zone is to the shoreline. This can also be seen by plotting the relative positions
 252 of the shore line and mixing zone toes (Figure 12). The distances between the mixing
 253 zone position and the shoreline appear to be unchanged during basin evolution.

254 We conclude our sensitivity study by considering the presence of a discontinuous
 255 confining unit on trapping seawater onshore. The onshore hydrogeology of Bangladesh
 256 (Bengal delta) has both confined and unconfined aquifers separated by discontinuous clay

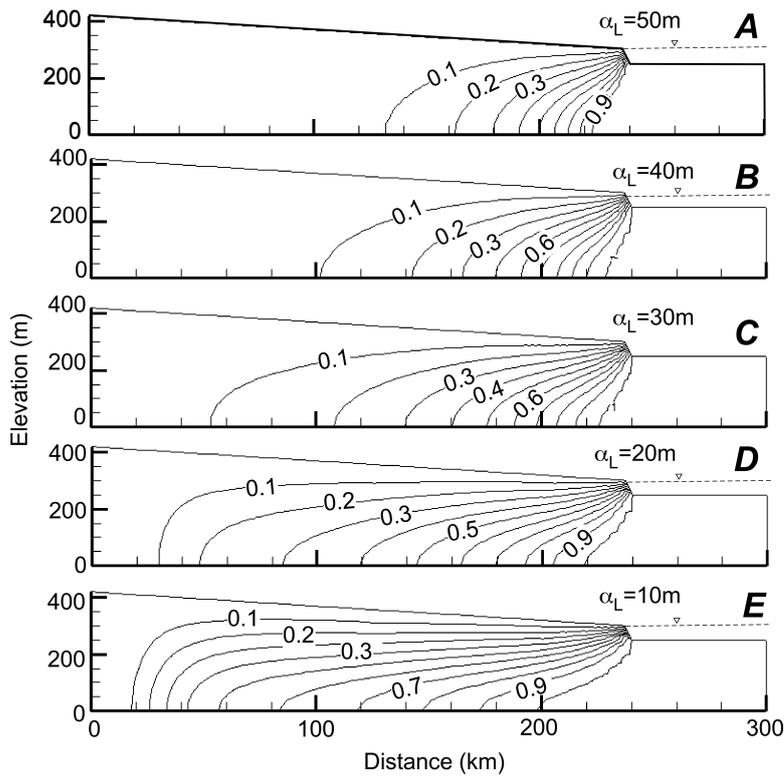


Figure 9. Effect of longitudinal dispersivity on salinity distribution. Parameters are listed in Table 1. Simulation results are at 16,370 years.

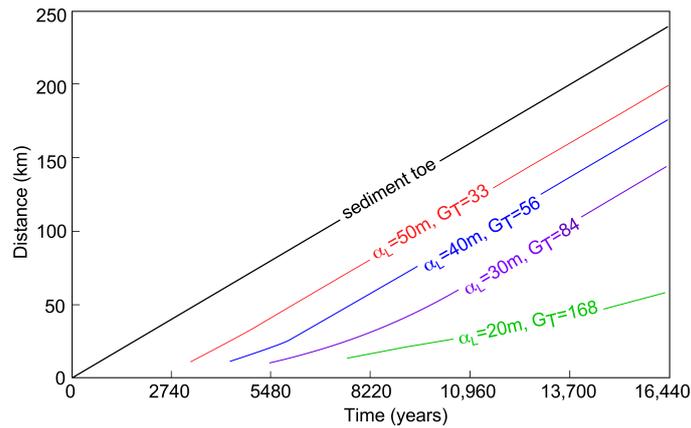


Figure 10. Computed toe of the shoreline (black line) and the toe of the saltwater-freshwater interface ($c=0.05$) and for the dispersivity simulations shown in Figure 8. The values of longitudinal dispersivity and the dimensionless number GT are listed with each line.

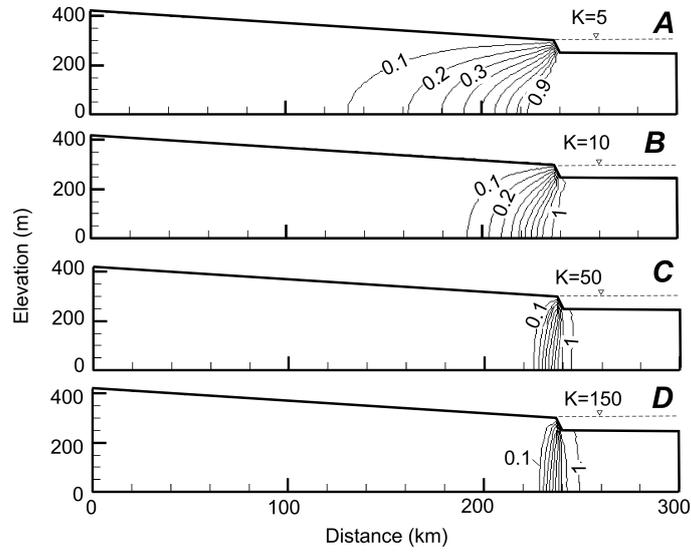


Figure 11. Effect of Hydraulic conductivity on salinity distribution. Parameters are listed in Table 1. Longitudinal dispersivity (αL) is fixed at 50m. Simulation results are at 16,370 years.

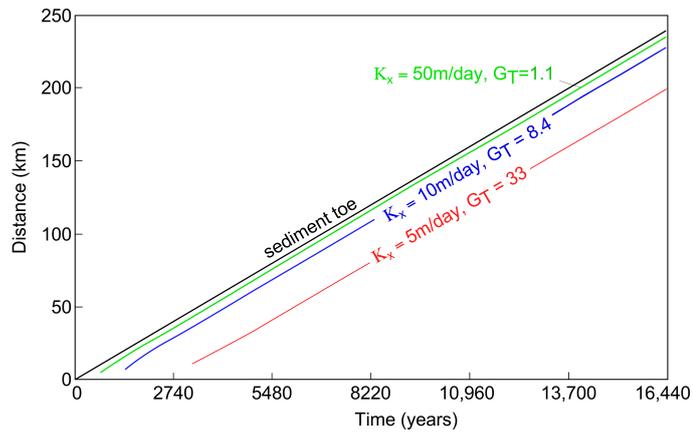


Figure 12. Changes in the position of the shoreline toe (black line) and the toe of the freshwater-saltwater interface (0.05 isochlor) during progradation. Colored lines represent changes in Hydraulic conductivity of 5 *m/day*, The numbers list the value of G_T .

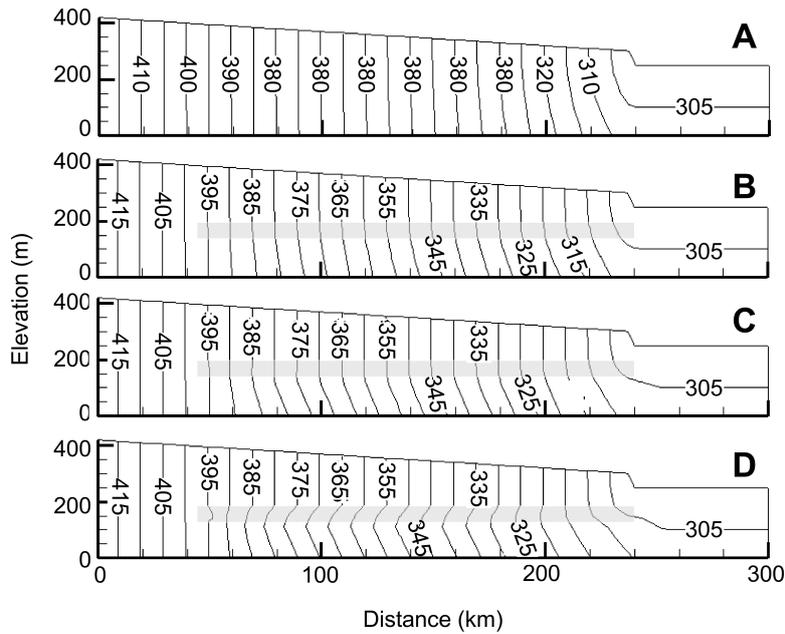


Figure 13. Contour maps of computed heads assuming an aquifer hydraulic conductivity of 5 m/day (K_{aq}) and (A) no confining unit. (B) Confining unit hydraulic conductivity is equal to $K_{aq}/10$. (C) Confining unit hydraulic conductivity is equal to $K_{aq}/100$. (D) Confining unit hydraulic conductivity is equal to $K_{aq}/1000$. The gray rectangle denotes the position of the confining layer. Simulation results are at 16,370 years.

257 and silt units (Goodbred Jr et al., 2003; Hoque et al., 2014). Figure 13 presents com-
 258 puted freshwater heads at the end of the simulation period for the base case (i.e., no con-
 259 fining unit) and for three other model runs (8-10) that include a confining unit whose
 260 hydraulic conductivity decreases by a factor of between 10 (Figure 13b), 100 (Figure 13c),
 261 and 1000 (Figure 13d). The aquifer hydraulic conductivity is fixed at 5m/day. In the ab-
 262 sence of a confining unit, the head contours are nearly vertical indicating the dominance
 263 of horizontal flow (Figure 13a). As the confining hydraulic conductivity decreases, the
 264 head contours bend to a sub-horizontal configuration creating a higher component of ver-
 265 tical flow (Freeze & Witherspoon, 1967). As confining unit hydraulic conductivity de-
 266 creased, there as a more entrapment of onshore seawater in the confined aquifer (Fig-
 267 ure 14). Groundwater fluxes are nearly constant across and horizontal within the wa-
 268 ter table aquifer. Within the semi-confined aquifer, there is a progressive decrease in flux
 269 magnitude on the shoreward side of the system (Figure 15). For the lower conductiv-
 270 ity confining unit scenarios, remnant seawater also lingers in in the confining unit near
 271 the shoreline. The magnitude of flux in the confined aquifer varies across the confining
 272 unit and decreases towards the shore but more slowly than in the overlying confined aquifer
 273 (Figure 15).

274 4 Discussion

275 Coastal aquifers in rapidly prograding deltas around the world are observed to have
 276 saline water tens of kilometers inland (Howard & Lloyd, 1983; Manzano et al., 2001; Cus-
 277 todio, 2010; Van Weert et al., 2009; Ravenscroft & McArthur, 2004; Shamsudduha, 2013).
 278 We argue here that brackish to saline water entrapped onshore can be the result of rapid
 279 progradation of the shoreline.

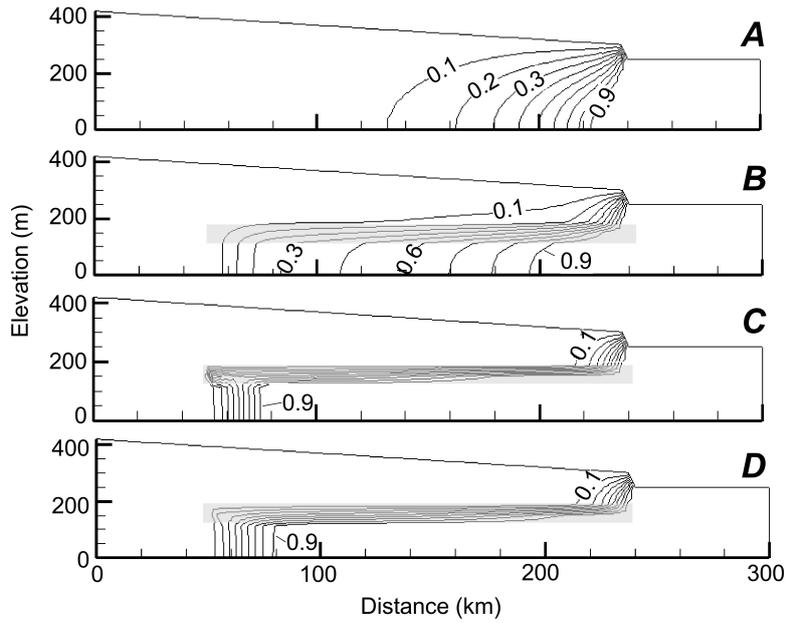


Figure 14. Effect of confining unit salinity on salinity patterns. Aquifer hydraulic conductivity 5 m/day (K_{aq}). (A) No confining unit. (B) Confining unit hydraulic conductivity is equal to $K_{aq}/10$. (C) Confining unit hydraulic conductivity is equal to $K_{aq}/100$. (D) Confining unit hydraulic conductivity is equal to $K_{aq}/1000$. The gray rectangle denotes the position of the confining layer. Simulation results are at 16,370 years.

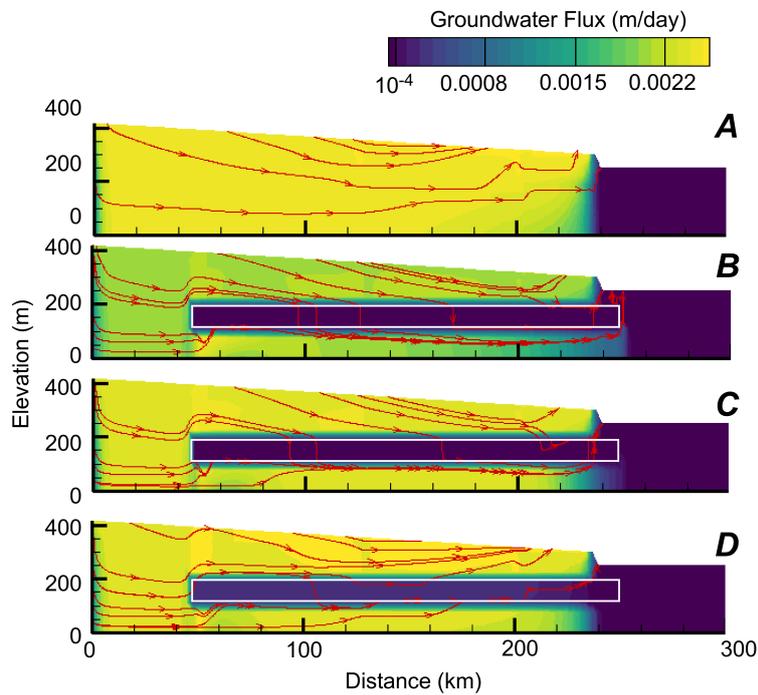


Figure 15. Contour maps of computed flux for the base case with no confining unit (A). (B) Confining unit hydraulic conductivity is equal to $K_{aq}/10$. (C) Confining unit hydraulic conductivity is equal to $K_{aq}/100$. (D) Confining unit hydraulic conductivity is equal to $K_{aq}/1000$. The white rectangle denotes the position of the confining layer. Simulation results are at 16,370 years.

Table 3. Global delta progradation rates over the Holocene

| River | Country | Progradation Rate (m/yr) | Source |
|--------------------|------------|--------------------------|----------------------------|
| Ganges-Brahmaputra | Bangladesh | 15-20 | (Kuehl et al., 2005) |
| Mississippi | USA | 100-150 | (Chamberlain et al., 2018) |
| Pearl | China | 29 | (Zong et al., 2009) |
| Mekong | Vietnam | 19-20 | (Tanabe et al., 2003) |
| Mekong | Vietnam | 50 | (Zoccarato et al., 2018) |
| Yangtze | China | 80 | (Hori et al., 2001) |
| Amazon | Brazil | 1-10 | (Nittrouer et al., 1996) |

280 The coupled sediment transport-coastal hydrogeologic model developed as part of
 281 this study reveals that inland seawater is the result of rapid progradation of the shore-
 282 line ($\sim 10m/yr$). The distance that saline to brackish water is trapped onshore is sen-
 283 sitive to both aquifer hydraulic conductivity and solute dispersivity; in homogeneous aquifers
 284 there is an indication that trends follow the dimensionless group G_T defined in eq.(15).
 285 The presence of a confining unit, however, probably has the greatest impact in seques-
 286 tering onshore seawater. Our results show that, even a contrast in aquifer/confining unit
 287 permeability of one order of magnitude, can trap significant amounts of seawater onshore.

288 We ran two additional simulations to provide field support for the concept that rapid
 289 progradation can entrap seawater on shore. The “best-fit” parameters used in these sim-
 290 ulations are listed in Table 3 for the Bengal Delta (Run 11) and Mississippi River Delta
 291 (Run 12). We modified the geometry of the model domain and hydrogeology of the Mis-
 292 sissippi River and Bengal Deltas to approximate field conditions. For the Bengal Delta
 293 model run, we only considered the unconfined and uppermost confined aquifers. The base
 294 of the Bengal Delta model was assumed to be the top of a tight confining unit. The Mis-
 295 sissippi River Delta model only considered the unconfined aquifer system because our
 296 observational data only extended that deep (Stanton et al., 2017). We set the progra-
 297 dation rates equal to those reported in Table 3 for these two venues. We projected ob-
 298 served salinity data onto these idealized cross sections for comparison purposes (Figure
 299 16a and 16d). There was general agreement between the computed and observed salin-
 300 ity conditions within the Bengal (Figure 16b) and Mississippi River (Figure 16e) Deltas.
 301 The present-day computed salinity conditions for a static grids (i.e., no progradation)
 302 are presented in Figures 16c and 16f for comparison purposes. As can be seen, sediment
 303 progradation dramatically modifies computed onshore salinity conditions. These model
 304 runs are not intended to represent calibrated models for the Mississippi River or Ben-
 305 gal Deltas. Rather, they are intended to illustrate that proof of concept that sediment
 306 progradation can play an important role in entrapping onshore seawater.

307 In all model runs, we have assumed sea-level was static when in fact, it rose by about
 308 25m during the Holocene. Since the onshore topography increases due to progradation
 309 between 60m-140m, we feel this simplifying assumption is justified.

310 Observations of seawater entrapment could be improved by running controlled source
 311 electromagnetic surveys along inland river channels. These electromagnetic surveys would
 312 help fill in the gaps of sparse well data. Land based time domain electromagnetic or mag-
 313 netotelluric soundings would also be useful though more time consuming.

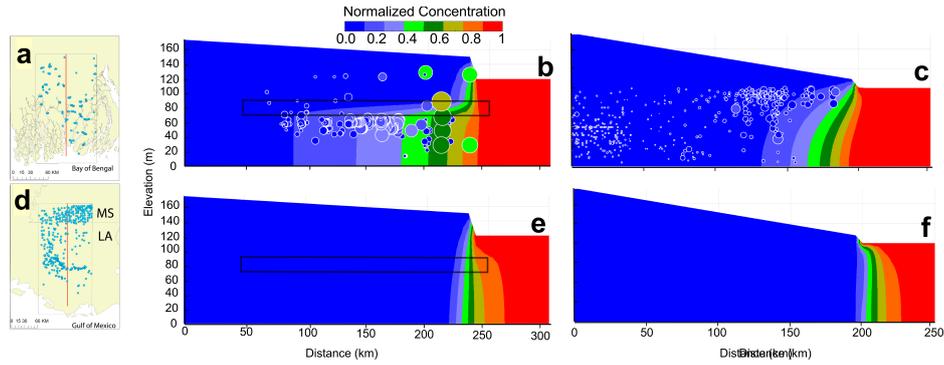


Figure 16. Location of Bengal Delta (a) and Mississippi River Delta (d) cross sections onto which salinity data was interpolated. Best fit model simulation results at the present day are shown in 16b and 16c for the Bengal Delta and Mississippi River Delta. Computed salinity levels using the same parameters using a static grid (no progradation) for the Bengal Delta and Mississippi River Delta venues are presented in (e) and (f) respectively. Parameters used in these model runs are presented in Table 1. Parameters in Runs 11 and 12 in Table 1 refer to the Bengal and Mississippi River Deltas, respectively. The colored circles represent normalized salinity conditions. A salinity level of 1.0 is seawater salinity conditions. The circle size also reflects salinity levels.

314 5 Conclusions

315 In this study, we have developed a coupled sediment transport -coastal hydrogeologic
 316 model using the control volume finite element method. The code was verified using
 317 the Henry solution (Fahs et al., 2016). The code included a novel mesh generation
 318 algorithm to take into account sediment deposition and shoreline progradation. We found
 319 that the entrapment of seawater onshore can be described by the product of two dimensionless
 320 number groups (eq. 15). One is the ratio of the sediment (shoreline) toe and ground-
 321 water velocities (eq. 13). The other dimensionless number group is the Peclet number
 322 (eq. 14).

323 We conducted a sensitivity study in which we varied sediment hydraulic conduc-
 324 tivity and dispersivity. Some simulations include a lower permeable, semi-confining unit.
 325 Assuming a lateral shoreline velocity of 14.6 m/yr, we found that an aquifer hydraulic
 326 conductivity of less than 10m/day and a longitudinal dispersivity of less than 50m could
 327 sequester onshore seawater. The presence of a confining unit had the largest impact on
 328 onshore seawater entrapment. Conducting towed electromagnetic surveys along inland
 329 rivers and onshore in undeveloped delta regions will help to better constrain the distri-
 330 bution of onshore seawater.

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 335 Any opinions, findings, and conclusions or recommendations expressed in this material
 336 are those of the authors and do not necessarily reflect the views of the National Science
 337 Foundation.

338 Data availability: on acceptance of the paper links to data depositories contain-
 339 ing key data and model (MATLAB) code will be provided.

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