

ULF Waves in the Foreshock Around the Moon: Statistical Approach

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Abstract

A broad statistical study addresses for the first time an evolution of ultra-low frequency (ULF) waves/fluctuations in the terrestrial foreshock around the Moon generated through the interaction between the back-streaming particles reflected from the bow shock and the incoming solar wind. They propagate sunward but are convected by the solar wind flow back toward the bow shock and their amplitudes grow. However, our study shows that waves could be growing as well as decaying towards the bow shock under the quasi-radial interplanetary magnetic field. We demonstrate that the statistically determined growth rate is positive and larger for compressive variations of the density and magnetic field strength than for its components. We show that even if a possible influence of the Moon and its wake is excluded, the growth rate is decreased by non-linear effects leading to saturation of the wave amplitude.

Figure 1.

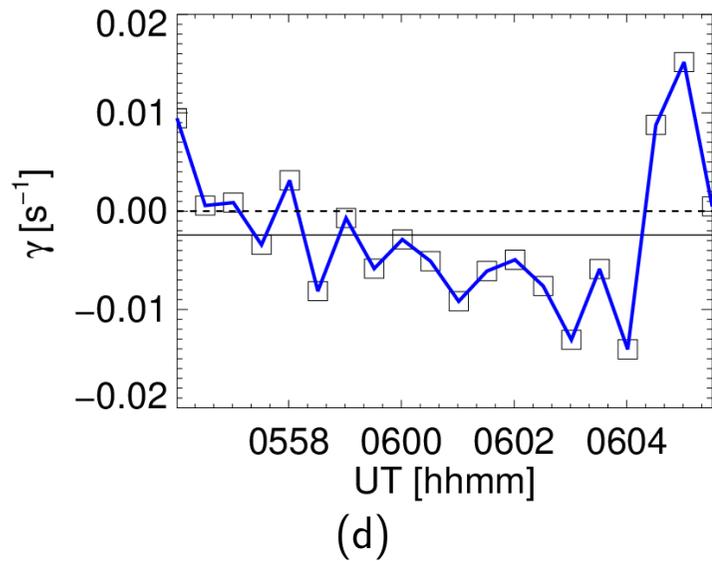
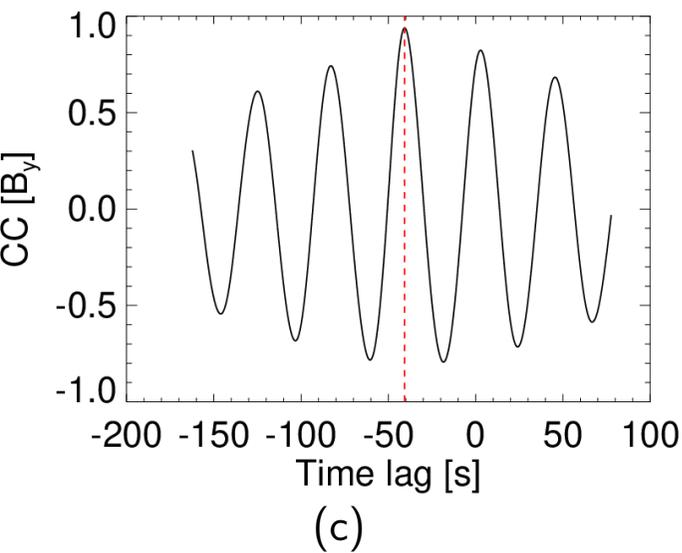
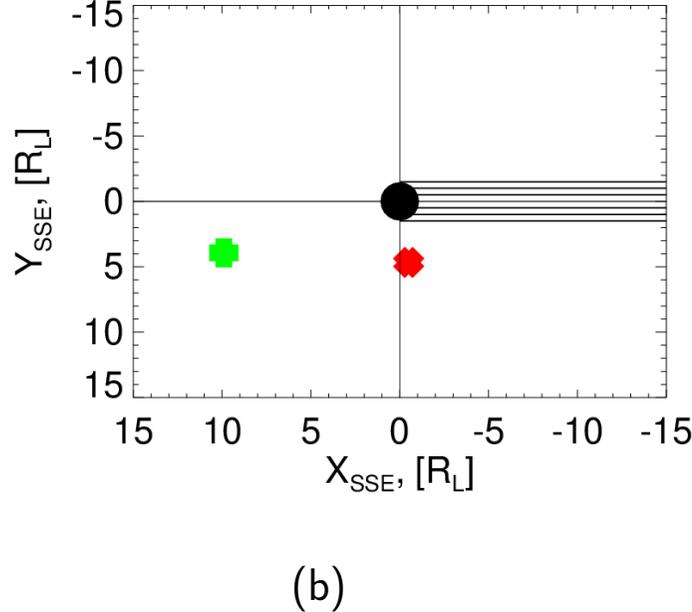
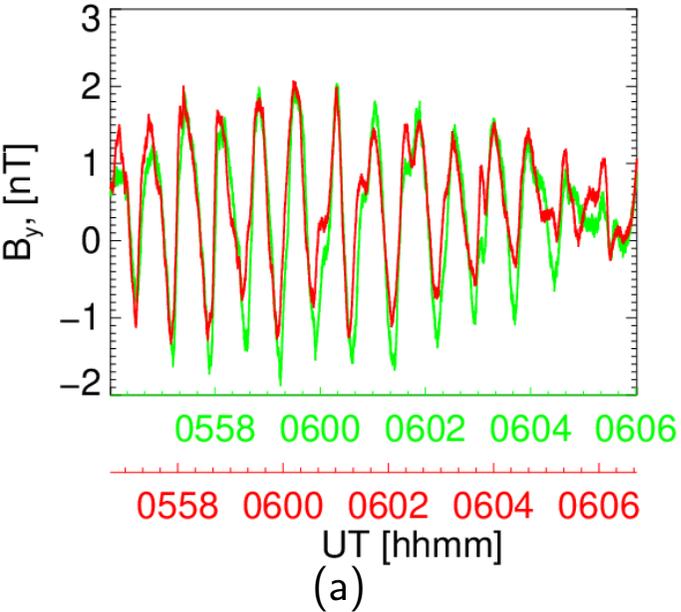


Figure 2.

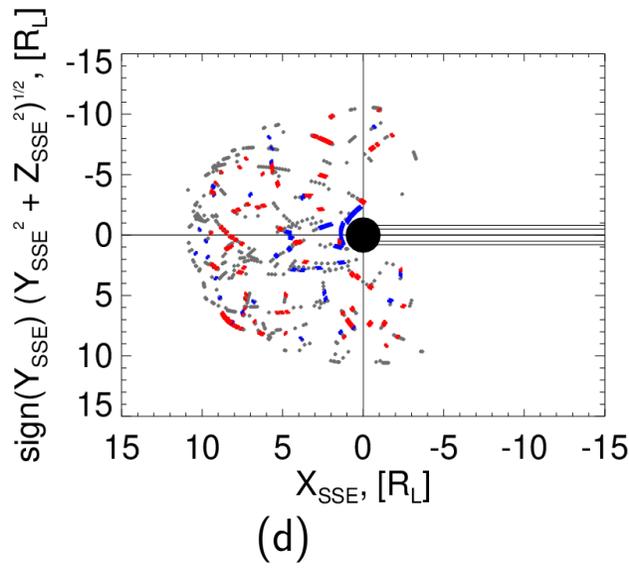
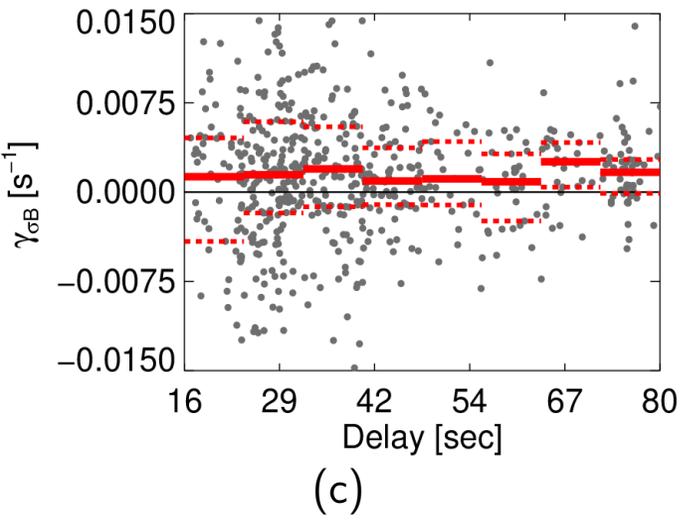
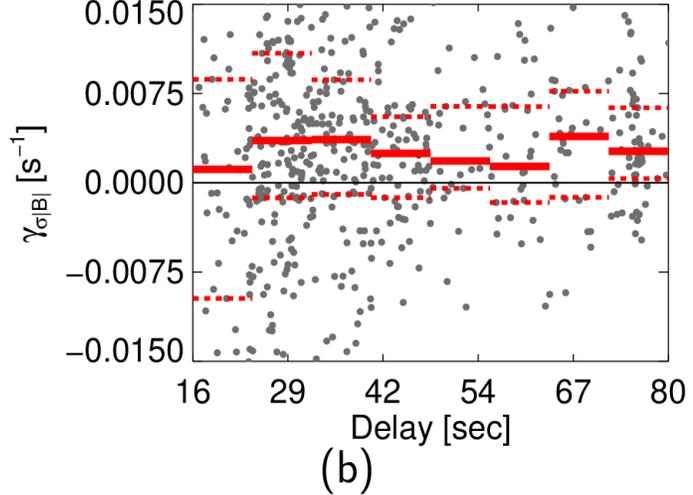
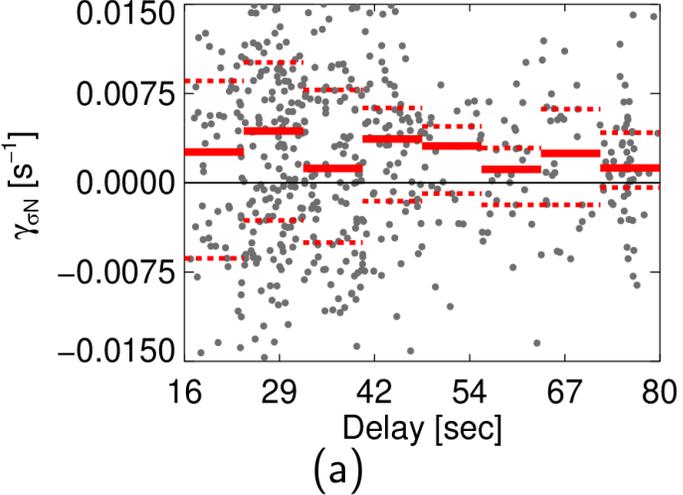


Figure 3.

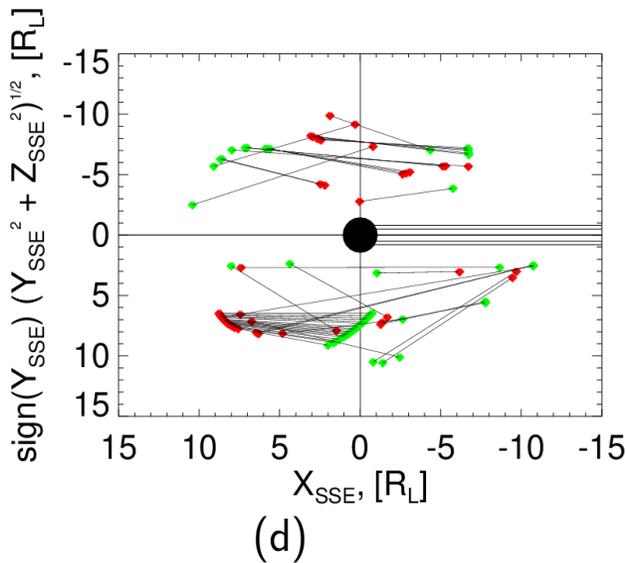
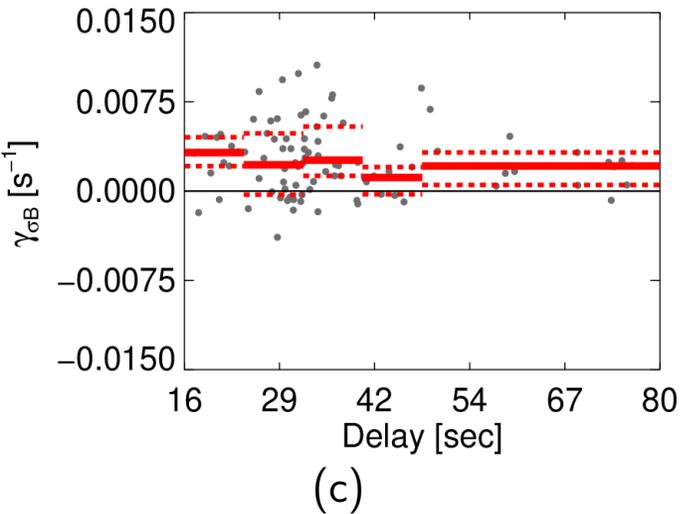
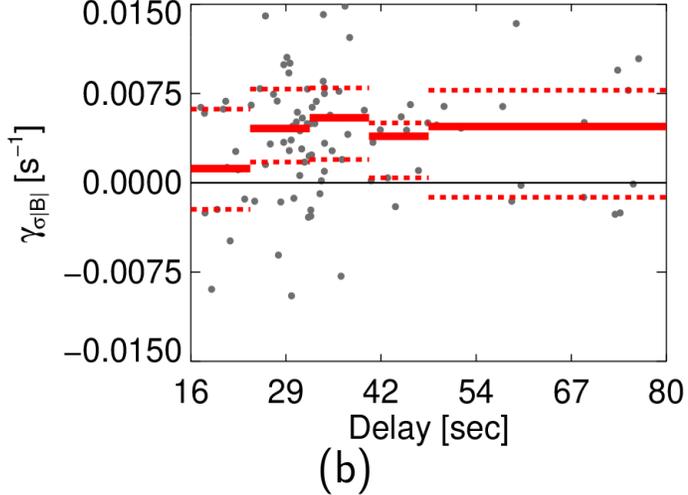
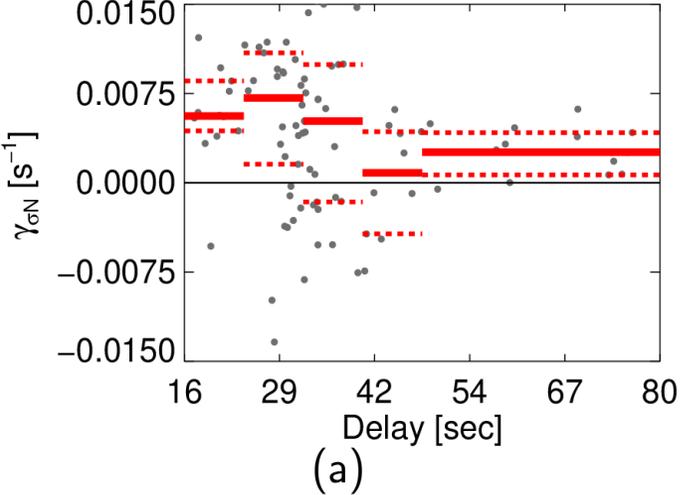
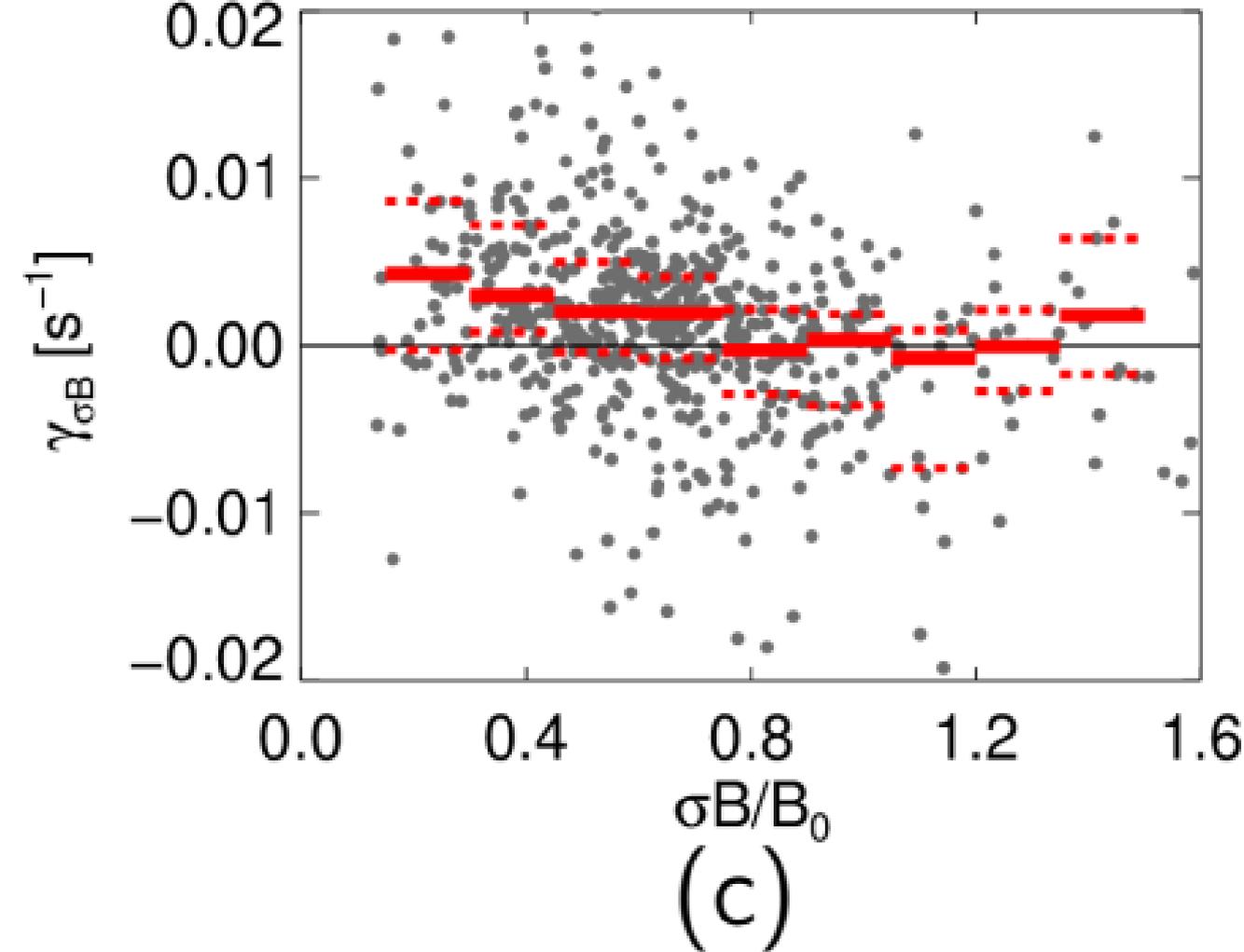
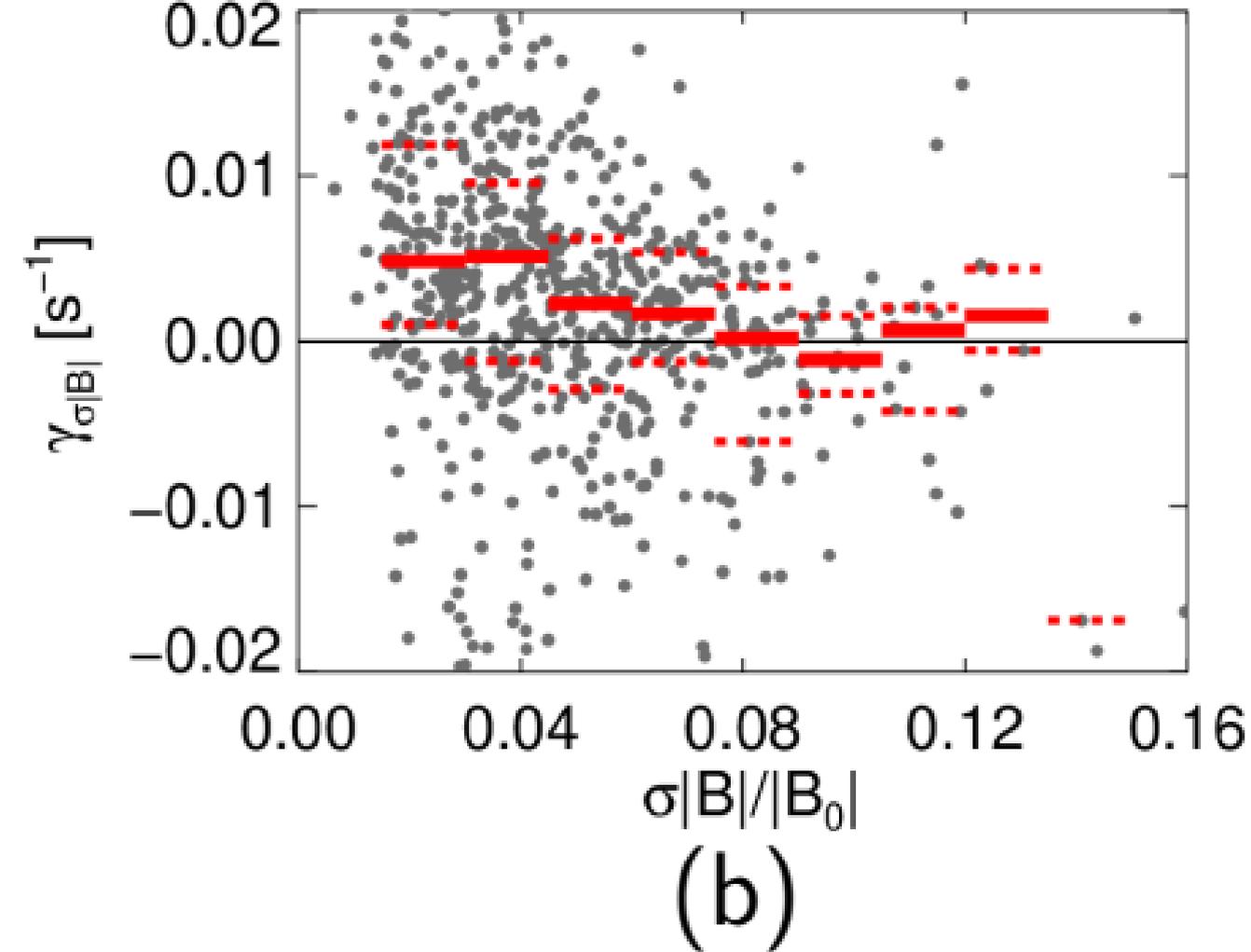
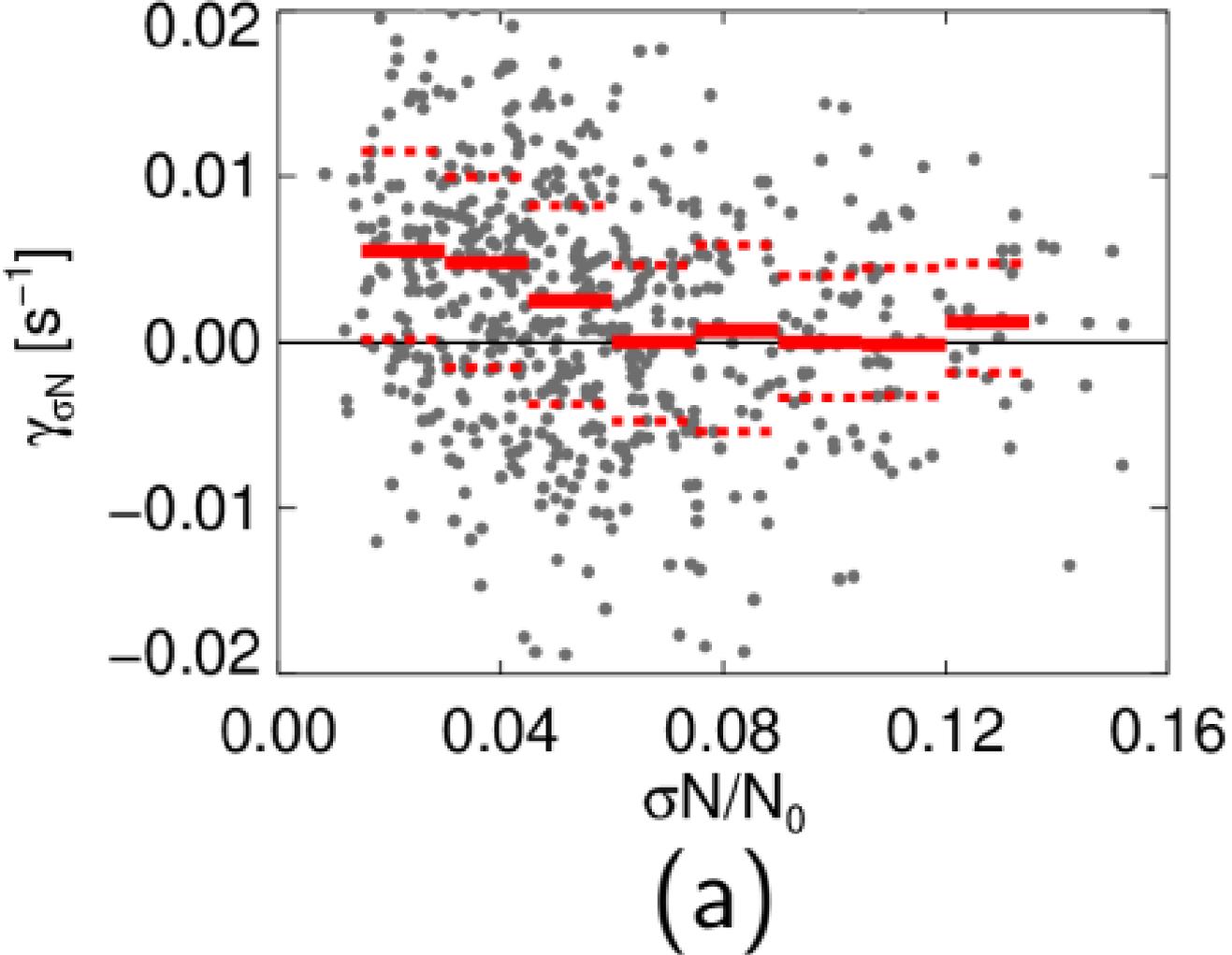


Figure 4.



ULF Waves in the Foreshock Around the Moon: Statistical Approach

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Key Points:

- Ultra-low frequency fluctuations in the foreshock at lunar distances are statistically analyzed for the first time
- Statistically determined growth rate is positive and larger for compressive variations under a radial IMF
- As the wave growth rate can be positive or negative for individual time intervals, effects affecting the growth rate are discussed

Abstract

A broad statistical study addresses for the first time an evolution of ultra-low frequency (ULF) waves/fluctuations in the terrestrial foreshock around the Moon generated through the interaction between the back-streaming particles reflected from the bow shock and the incoming solar wind. They propagate sunward but are convected by the solar wind flow back toward the bow shock and their amplitudes grow. However, our study shows that waves could be growing as well as decaying towards the bow shock under the quasi-radial interplanetary magnetic field. We demonstrate that the statistically determined growth rate is positive and larger for compressive variations of the density and magnetic field strength than for its components. We show that even if a possible influence of the Moon and its wake is excluded, the growth rate is decreased by non-linear effects leading to saturation of the wave amplitude.

1 Introduction

Ultra-low frequency (ULF) waves in the frequency range of 0.001 – 0.3 Hz are a continually present feature of the region upstream of the quasi-parallel shock (Russell et al., 1987; Burgess et al., 2012). At quasi-parallel shocks (characterized by the angle between the upstream magnetic field and bow shock normal, θ_{Bn} smaller than 45°), a portion of the solar wind particles is reflected back into the upstream region forming the foreshock (Hoppe & Russell, 1983; Eastwood et al., 2005) and driving the growth of ULF waves (Wilson III, 2016) traveling upstream. The reflected field-aligned ion beams (Thomsen, 1985; Meziane et al., 2013) are observed for $\theta_{Bn} < 45^\circ$ (Eastwood et al., 2005) and excite waves propagating upstream along the interplanetary magnetic field (IMF). However, these waves need some time to grow toward an observable level, thus they are detected farther downstream in a conjunction with the intermediate distribution (Paschmann et al., 1979). The waves propagate through the regions exhibiting strong density gradients of suprathermal particles, thus they gain a compressive component (Kajdič et al., 2017).

The interaction between the solar wind (SW) and ions reflected at the bow shock has the resonant and non-resonant character and may lead to particle acceleration and plasma heating (Treumann & Pottellette, 2002; Selzer et al., 2014). Instabilities are a primary mechanism exciting transverse waves, propagating mostly parallel and anti-parallel to the IMF. Waves traveling along the ion beam are resonant (Landau resonance), while

45 waves propagating anti-parallel to the beam become unstable in the presence of temper-
 46 ature anisotropy (Sentman et al., 1981; Gary et al., 1998). The excited waves propagate
 47 upstream and they are growing but they are convected toward the Earth in the super
 48 Alfvénic SW flow (Hoppe et al., 1981; Burgess, 1997), thus the waves of larger ampli-
 49 tudes are observed closer to the bow shock. A presence of waves leads to the SW beam
 50 deceleration (Urbář et al., 2019) and deflection (Gutynska et al., 2020).

51 Simulations (Blanco-Cano et al., 2006; Omid, 2007; Palmroth et al., 2015) have
 52 shown that the foreshock geometry and plasma parameters change with the IMF orien-
 53 tation. Under a nearly radial IMF, the foreshock is permeated by two types of wave modes:
 54 the weakly compressive quasi-sinusoidal waves and the magnetosonic compressive fluc-
 55 tuations (Berdichevsky et al., 1999). The weakly compressive waves can propagate at
 56 angles up to 30° to the ambient field, in contrast to magnetosonic waves, propagating
 57 at larger angles. Weakly compressive waves are dominant far from the bow shock, the
 58 second population of ULF fluctuations is observed close to the foreshock edge (Meziane
 59 et al., 2004; Palmroth et al., 2015).

60 Howard et al. (2017) presented a case study of two-point ARTEMIS observations
 61 of right-hand polarized ULF waves and reflected SW ions in the lunar environment. The
 62 Moon lacks a global magnetic field but it possesses localized crustal magnetic fields (Halekas
 63 et al., 2001; Mitchell et al., 2008) and these large-scale magnetic anomalies reflect a part
 64 of incoming SW ions before they impact the lunar surface. The reflected ions excite waves
 65 that interact with the waves already present in this environment through various mech-
 66 anisms. Nakagawa et al. (2011, 2012) and Halekas et al. (2013) have reported waves driven
 67 by resonant interactions with reflected protons in frequencies ranging from 0.0083 to 10 Hz
 68 with both left- and right-hand polarizations in the spacecraft frame. Howard et al. (2020)
 69 examined their characteristics and the conditions under which they are likely to occur.

70 Dorfman et al. (2017) reported the ULF wave growth rate in the foreshock. They
 71 applied the data of two ARTEMIS spacecraft orbiting the Moon to characterize reflected
 72 ion beams and relatively monochromatic ULF waves. The distance between both space-
 73 craft along the SW flow was $\approx 2.5 R_E$ (Earth radii) and IMF was nearly radial. They
 74 estimated the ULF wave growth rate as 0.010 s^{-1} and the normalized growth rate as $\gamma/\Omega_i \approx$
 75 0.035 (Ω_i is the proton gyroperiod).

76 Motivated by these investigations, we performed a systematic statistical study fo-
 77 cused on conditions under which waves/fluctuations are growing in the lunar surround-
 78 ing because, according to Jurac and Richardson (2001), the foreshock can extend behind
 79 $50 R_E$ and several events resembling waves of the ion foreshock origin were observed $250 R_E$
 80 upstream (Berdichevsky et al., 1999). We use observations of two ARTEMIS spacecraft
 81 during intervals of a nearly radial IMF when the foreshock occupies a large volume in
 82 front of the dayside bow shock. Our analysis is based on standard deviations of the ion
 83 density, IMF magnitude and its components computed over 10-minute intervals. We have
 84 found that the fluctuation amplitude (standard deviation) of all analyzed quantities can
 85 grow but it can be also damped toward the bow shock and we estimate factors influenc-
 86 ing the growth rate of ULF fluctuations like spacecraft configurations with respect to the
 87 Moon and its wake and permanently changing SW and IMF conditions.

88 2 Case study

89 We use the data collected by the twin ARTEMIS probes from 2012 till 2020 years.
 90 Probes (referred as THB and THC herein) are in stable equatorial orbits around the Moon
 91 with an orbital period of 26 hour. The orbits are highly eccentric with altitudes rang-
 92 ing from ≈ 100 to ≈ 19.000 km. Two probes move in opposite directions and this al-
 93 lows a large number of different orbital configurations (Angelopoulos, 2008, 2011).

94 Each spin-stabilized probe carries particle and field instruments. The fluxgate mag-
 95 netometer provides the magnetic field vector with sampling rate up to 64 Hz (Auster et
 96 al., 2008). The electrostatic analyzer (ESA) measures the ion velocity distribution from
 97 1.6 eV to 25 keV (McFadden et al., 2008) with a spin (≈ 3 s) time resolution. We use
 98 also data of the solid state telescope (SST) (Angelopoulos, 2008) for monitoring ener-
 99 getic particle fluxes.

100 In order to demonstrate peculiarities of the wave propagation and amplification,
 101 we present one 10-minute subinterval where we apply the similar approach as Dorfman
 102 et al. (2017). Variations of the B_y IMF component for the upstream (green) and down-
 103 stream (red) spacecraft are shown in Figure 1a for January 16, 2018, 0556 to 0606 UT;
 104 Figure 1b presents the mutual position of spacecraft in selenocentric solar ecliptic (SSE)
 105 coordinates. Figure 1c shows the cross-correlation of the B_y components as measured
 106 by both spacecraft that peaks at a time lag of -42 s and this lag is also applied in the

107 panel 1a. The value of cross-correlation coefficient ($R = 0.96$) ensures that both space-
 108 craft observe the same wave packet. The ratio of amplitudes determined on 30 s subin-
 109 tervals is then used for a computation of the growth rate. This rate is plotted in Fig-
 110 ure 1d as a function of time and one can see that the growth rate is positive at both ends
 111 of the studied interval, but it is negative at its center. The average value of the growth
 112 rate along this interval is -0.0024 s^{-1} (full horizontal line in Figure 1d), thus the waves
 113 are rather decaying in a statistical sense. We should note that the result is qualitatively
 114 similar to that shown by Dorfman et al. (2017) in their Figure 3 (panel 3) but our con-
 115 clusion is that it is difficult to say whether the wave is growing or not. In order to elu-
 116 cidate an evolution of foreshock fluctuations, we perform this extensive study.

117 3 Selection of data and their processing

118 The case analysis in the previous section used data transmitted in the ARTEMIS
 119 burst mode but such intervals are rare. For this reason, we use data with a spin reso-
 120 lution, thus the study is limited to the frequencies from 0.005 Hz (10-minute interval)
 121 to 0.3 Hz (spacecraft spin period). First, we have selected time intervals (with minimum
 122 duration of ≈ 30 minutes) of a radial IMF with the cone angle (an angle between the
 123 magnetic field vector and Sun-Earth line) lower than 25° . Identified intervals were di-
 124 vided into 10-minute subintervals that are used throughout the study.

125 We use only data when the Moon is at $X_{GSE} > 30 R_E$ in the Geocentric Solar
 126 Ecliptic (GSE) coordinate system and we rejected data when one of the spacecraft was
 127 located in the lunar wake. We defined boundaries of the lunar wake as a prism with di-
 128 mensions of $-15 R_L < X_{SSE} < +1 R_L$; $-1.5 R_L < Y_{SSE} < +1.5 R_L$ and $-1.5 R_L <$
 129 $Z_{SSE} < +1.5 R_L$ ($R_L \approx 1737$ km, Moon radius). Intervals selected in this way (6128
 130 10-minute subintervals) include different spacecraft configurations around the Moon and
 131 its wake.

132 The above case study uses the correlation for a determination of the time delay be-
 133 tween the upstream and downstream spacecraft. However, this approach cannot be ap-
 134 plied on the spin resolution data, thus we use a prediction of SW propagation time and
 135 calculated as: $\Delta t = (X_{US} - X_{DS})/V_X$, where $(X_{US} - X_{DS})$ is the average distance
 136 between the spacecraft along the X_{GSE} axis and V_X is the average SW velocity com-

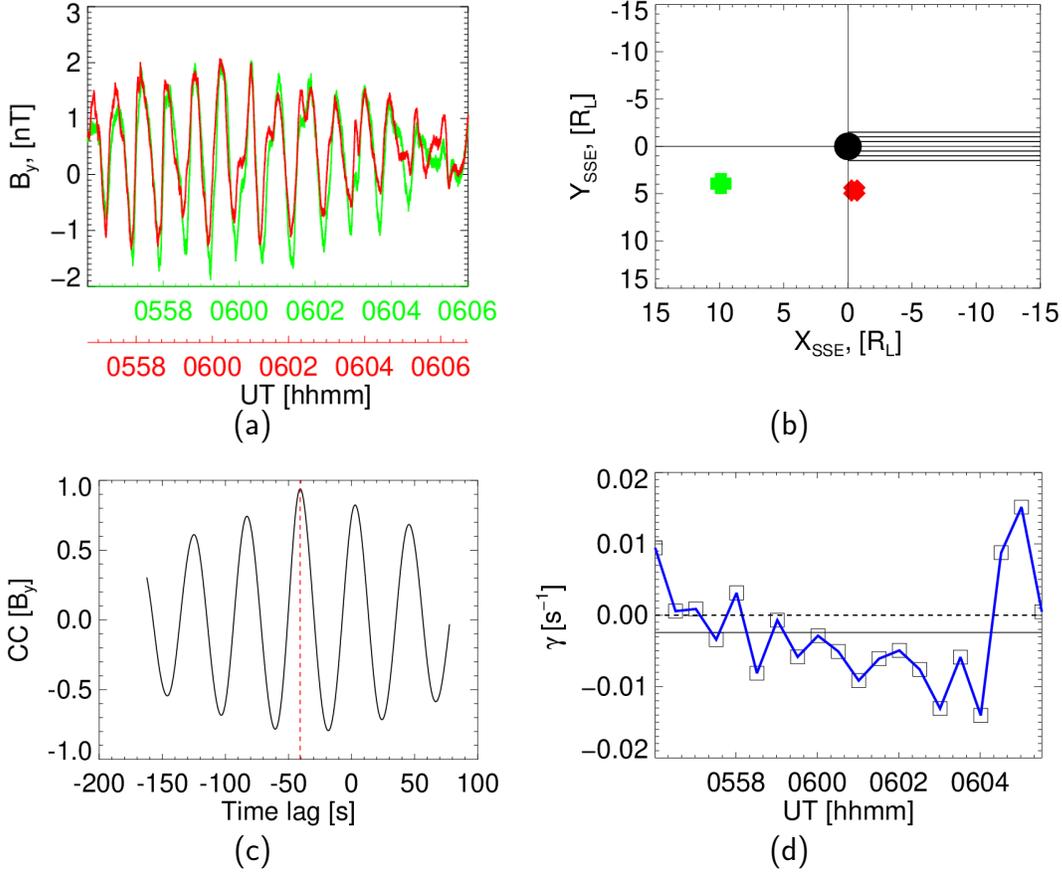


Figure 1. (a) An example of ULF waves observed by THB (red) and THC (green) from 0556 to 0606 UT on January 16, 2018; (b) Locations of THB and THC around the Moon in SSE coordinates; (c) The cross-correlation of the B_y components as a function of the time lag between both probes; (d) The growth rate γ as a function of time. Note that the black dotted line stands for $\gamma = 0$ and the black full line presents the average value of γ on the whole time interval.

137 ponent observed by the upstream spacecraft. The propagation times range from a few
 138 seconds up to ≈ 80 s.

139 To be sure that the spacecraft are actually located in the foreshock, we further checked:

- 140 1. In SST observations of energetic ions reflected from the bow shock, we use only inter-
 141 vals with the averaged energy flux in the lowest energy channel exceeding $200 \text{ keV}/(\text{cm}^2 \cdot \text{s} \cdot \text{str} \cdot \text{keV})$
 142 at both probes. This condition reduces our set from 6128 to 3709 intervals.
- 143 2. The θ_{Bn} angle at the intersection between the IMF line coming through the space-
 144 craft and the model bow shock (Jeřáb et al., 2005) is lower than 45° and the in-

145 intersection is closer than $-7 R_E$. After applying these conditions, we got 1188 data
146 points.

- 147 3. We limited the intersection of the IMF line with the model bow shock to $X_{BS} <$
148 $25 R_E$ because the Jeřáb et al. (2005) model can fail in extreme upstream condi-
149 tions. This particular limit reduces the number of intervals to 1178.
- 150 4. Since we investigate the growth rate, we should let the waves a sufficient time to grow
151 and thus we discarded all intervals that did not pass the threshold $X_{US} - X_{DS} >$
152 $5 R_L$. After applying this condition, we obtained 640 data points that represent
153 a basic data subset for the determination of the wave growth rate.

154 4 Statistical study

155 We estimate the growth rate, γ using standard deviations computed over 10-minute
156 intervals for the ion density and IMF data. We define it as:

$$\ln \frac{\sigma A_{DS}}{\sigma A_{US}} = \gamma \Delta t \quad (1)$$

157 where σA_{DS} and σA_{US} are the standard deviations of variables observed by the down-
158 stream and upstream spacecraft, respectively. If $\gamma > 0$, the downstream spacecraft ob-
159 serves the wave amplification whereas $\gamma < 0$ indicates the wave decay. The standard
160 deviations were computed for the IMF magnitude, $\sigma|B|$ and for all components, $\sigma B =$
161 $(\sigma B_x^2 + \sigma B_y^2 + \sigma B_z^2)^{1/2}$. Note the difference between $\sigma|B|$ and σB – whereas the for-
162 mer represents the amplitude of a compressive component of fluctuations, the latter rather
163 refers to Alfvénic variations because compressive fluctuation components would be small
164 under the radial IMF orientation (Palmroth et al., 2015). The same procedure was ap-
165 plied for ion density variations, σN .

166 The resulting growth rates are shown in Figure 2 as a function of the time of solar
167 wind propagation from the upstream to downstream spacecraft (delay = Δt). The
168 gray dots represent values obtained for particular intervals, the red bars stand for me-
169 dian values computed in delay bins and the dashed lines indicate 0.25 and 0.75 quartiles.
170 The growth rates would not depend on the spacecraft separation; the figure demonstrates
171 it in a statistical sense. A detailed examination of Figure 2 reveals that although the fluc-
172 tuations of all parameters exhibit growing trend in average (the median growth rates are
173 given in Table 1), our set contains a large number of intervals that exhibit wave damp-
174 ing.

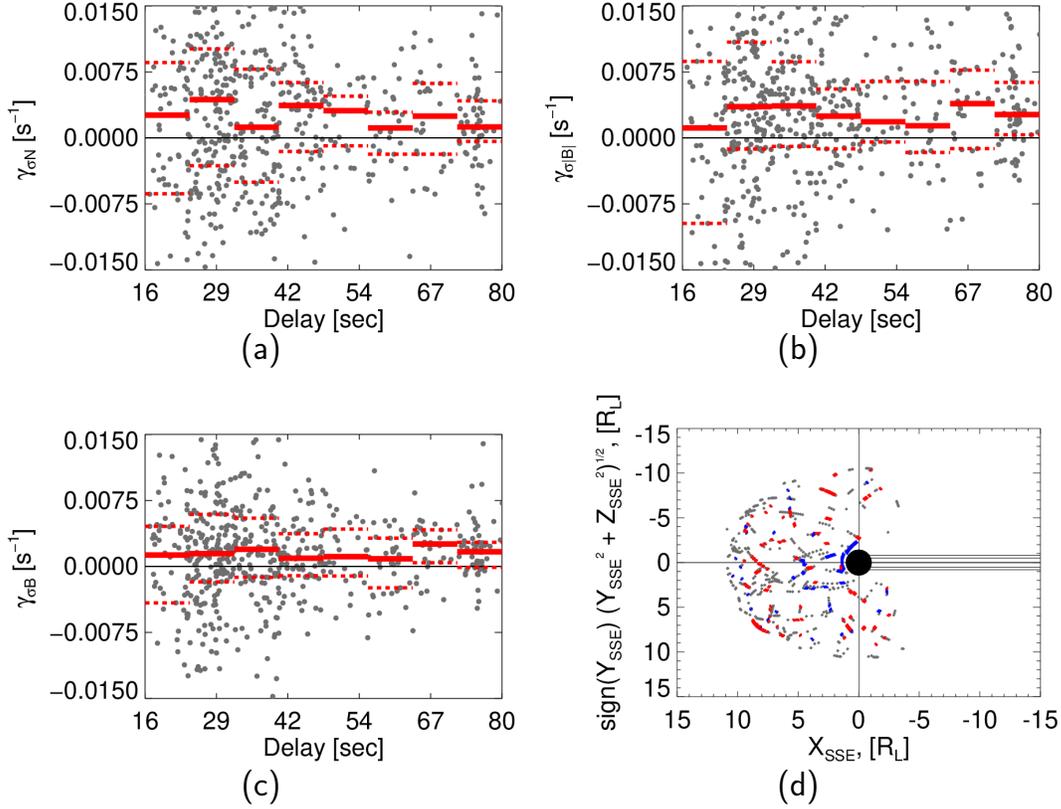


Figure 2. Growth rates of (a) σN ; (b) $\sigma|B|$; and (c) σB as a function of the time delay; in all panels, the grey dots (640 data points) represent individual events; the red bars mark the medians in $2R_L$ windows; the dashed lines indicate 0.25 and 0.75 quartiles; (d) The locations of the upstream spacecraft in SSE for intervals with growing (red) and damped (blue) waves.

175 A deeper analysis shows that the criteria used for event selection are too soft and
 176 leave a number of events when both spacecraft are still in different environments. More-
 177 over, the situation when we observe positive growth rate in one parameter and negative
 178 in other parameters is very frequent. To demonstrate it, we selected events exhibiting
 179 positive/negative growth rate in all parameters and plotted the locations of the upstream
 180 spacecraft in Figure 2d. Altogether we found 255 events with a positive (red points) and
 181 86 with negative (blue dots) growth rates. The blue dots are concentrated upstream of
 182 the Moon or in its vicinity, thus the reflected particles from the lunar surface or from
 183 magnetic anomalies (Halekas et al., 2001; Mitchell et al., 2008) can excite new waves and
 184 the upstream fluctuations can have larger amplitudes than the original foreshock waves.
 185 Under such circumstances, the growth rate computed from the standard deviations could
 186 be negative.

Table 1. Median growth rates of σN , $\sigma|B|$, and σB for three sets of the selection criteria (see text for their definition). Note that in the last row, only positive and negative growth rates in all parameters are analyzed.

Conditions	$\gamma_{\sigma N}$	$\gamma_{\sigma B }$	$\gamma_{\sigma B}$
Thresholds 1-4 (640 intervals)	0.0030	0.0026	0.0014
Thresholds 1-7 (99 intervals)	0.0057	0.0055	0.0032
Thresholds 1-7 (48 intervals)	0.0077	0.0630	0.0046

187 Since the analysis of the Moon influence on the foreshock waves is out of the scope
 188 of the present study, we applied additional criteria:

- 189 5. The angle between average IMF vectors registered by THB and THC is lower than
 190 8° . This limitation ensures that both spacecraft are magnetically connected to sim-
 191 ilar points on the bow shock surface; it leaves 517 events from 640.
- 192 6. Energetic particle fluxes registered by the first SST energy channel on both probes
 193 are similar (their ratio lies in the range of 0.3–9). The range is relatively broad
 194 because it should reflect slightly different energy ranges of THB and THC tele-
 195 scopes. This threshold discarded a large number of events; only 362 intervals re-
 196 main.
- 197 7. The line connecting both spacecraft does not cross the Moon or its wake defined above.
 198 This threshold is very strong, it leaves only 99 points from the original data set.
 199 Among them, 46 events exhibit positive and 2 negative growth rates in all ana-
 200 lyzed parameters simultaneously ($\sigma|B|, \sigma N, \sigma B$).

201 The growth rate of fluctuations in time intervals passing the above thresholds (99 points)
 202 is plotted in Figure 3; Figure 3d shows the locations of both spacecraft connected by thin
 203 lines, indicating that the analyzed fluctuations would not be affected by the Moon sig-
 204 nificantly.

205 Looking at Figure 3, one note that additional criteria do not change the distribu-
 206 tion of growth rates significantly because the spread of individual points is still large,
 207 the growth rate varies from -0.005 to $+0.008$. As it can be seen in the second row of
 208 Table 1, the median growth rates are by a factor of about 1.4 larger than prior to ap-

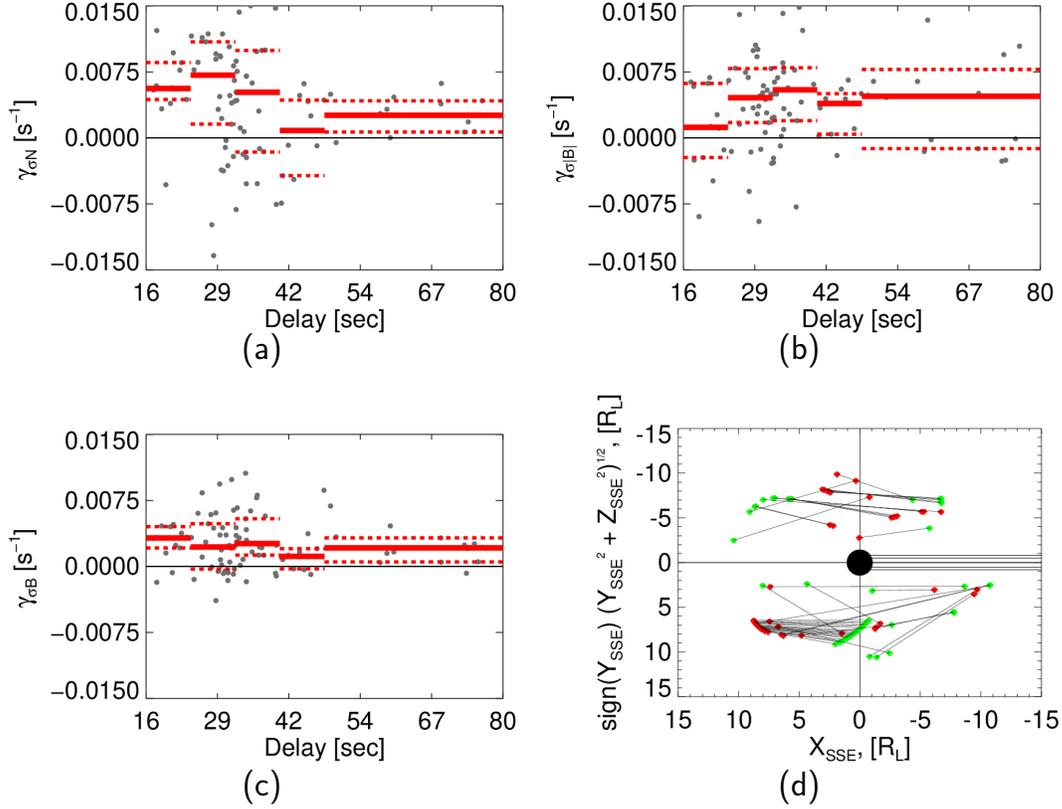


Figure 3. Growth rates of (a) σN ; (b) $\sigma |B|$; and (c) σB for 99 points as a function of the time lag in the same format as Fig. 2; (d) The locations of both spacecraft (THB–red and THC–green) for intervals with growing fluctuations (46 events).

209 plication of criteria 5–7. The last row in Table 1 shows that the medians for the events
 210 exhibiting positive or negative growth rates simultaneously for all investigated param-
 211 eters increase but even this selection does not change their values substantially. If we
 212 compare the values in rows, we can note that γ_N and $\gamma_{\sigma |B|}$ are comparable but $\gamma_{\sigma B}$ is
 213 by a factor of nearly 2 lower in all sets. We believe that this difference is connected with
 214 the character of fluctuations described by these quantities.

215 5 Discussion

216 Our statistical analysis demonstrates that close to the Moon ($\approx 2\text{--}3 R_L$), ULF fluc-
 217 tuations are predominantly damped while in a more distant upstream, the waves rather
 218 grow. We assume that the reason is that the flux of back streaming ions from the bow
 219 shock is shadowed by the Moon (or the lunar wake) and it influences a transfer of en-

220 ergy from particles to waves but this idea should be confirmed by a further investiga-
221 tion. On the other hand, Harada et al. (2015) characterized the large-scale morphology
222 of the region upstream of the Moon and its wake which contains Moon-related particles
223 and waves. SW ions reflected from the unshielded surface and by crustal magnetic fields,
224 together with heavy ions of lunar exospheric origin, are picked up by the solar wind mag-
225 netic and electric fields. The authors observed ≈ 0.01 Hz and ≈ 1 Hz magnetic field
226 fluctuations that partially coincide with populations of the Moon-related ions and found
227 that the morphology of the Moon-related ion and wave distributions is well organized
228 by the upstream magnetic field direction. Our criteria 5–7 would exclude the region po-
229 tentially influenced by these effects but they still leave intervals exhibiting a negative growth
230 rate. In a follow-up study, we will concentrate on these effects because it is possible that
231 the downstream and upstream spacecraft observe waves of different origin and thus the
232 determination of the growth rate is misleading in such cases.

233 Depending on the subset used for the growth rate determination, we have found
234 its median value between 0.003 and 0.007 s^{-1} with individual values reaching 0.015 s^{-1} .
235 The median values are a little lower than 0.01 s^{-1} determined in the case study by Dorfman
236 et al. (2017). However, foreshock fluctuations are highly non-linear and thus, there is a
237 question what this growth rate means. Applications of obtained values on the wave growth
238 from the Moon to the subsolar bow shock would lead to a ratio of amplitudes of the or-
239 der of 20–100 that is unrealistic if the initial fluctuation amplitude in the solar wind is
240 taken into account. The most probable scenario of an evolution of foreshock variations
241 would start with the seed population of turbulent fluctuations that are brought to the
242 outer edge of the foreshock region by the SW flow. The frequency spectrum of such fluc-
243 tuations is broad and, depending on the instantaneous conditions, a part of this spec-
244 trum is amplified. The waves grow but the non-linear effects lead to a saturation of their
245 growth and to excitation of new wave modes. However, new modes are growing at the
246 expense of existing waves and the standard deviations do not increase accordingly. This
247 scenario implies that the initial overall growth rate would be close to the upper limit of
248 rates determined by our study and it would decrease with the fluctuation amplitude. In
249 order to check this idea, we plotted the growth rate as a function of the normalized am-
250 plitude of fluctuations of each particular quantity in Figure 4. In order to have sufficient
251 statistics, we use the intervals (640 data points) passing first four thresholds that are used
252 also in Figure 2. Figure 4 shows that the median values of growth rates of all quanti-

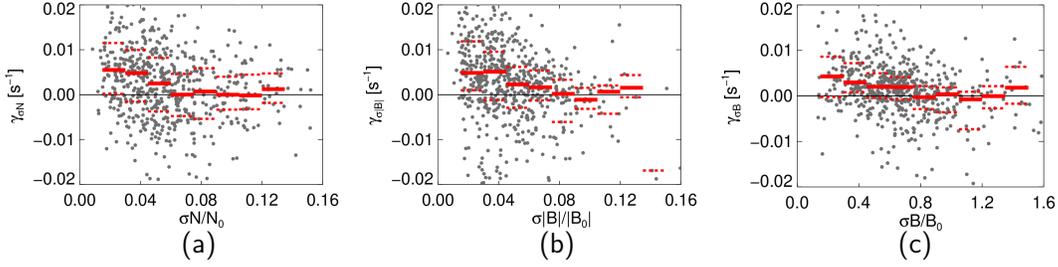


Figure 4. Growth rates of (a) σN ; (b) $\sigma|B|$; and (c) σB as a function of the normalized level of fluctuations of a particular quantity (the same description as in Fig. 2).

253 ties exhibit a clear decreasing trend with an increasing relative fluctuation level that is
 254 consistent with our suggestion. We should point out that a saturation of the growth rate
 255 can be also seen in Figures 2 and 3 because the medians computed in the time delay bins
 256 exhibit a notable decreasing trend, especially for density fluctuations.

257 Another question is the wave mode which the determined growth rate refers to. We
 258 have analyzed fluctuations of the IMF vector, magnitude and ion density. It is expected
 259 that the last two parameters are connected with compressive waves whereas the fluctu-
 260 ations of the magnetic field vector describe a level of the weakly compressive Alfvénic
 261 component. The previous research revealed that the distant foreshock is predominantly
 262 occupied by weakly compressive waves (Meziane et al., 2004; Palmroth et al., 2015), con-
 263 sistent with our observations. Whereas the normalized level of compressive fluctuations
 264 $\sigma(|B|/|B_0|)$ does not exceed 0.15, $\sigma(B/|B_0|)$ can reach 1.5 in individual cases. However,
 265 dominance of weakly compressive fluctuations is also a typical feature of the SW because
 266 a survey of Wind observations at L1 provided median values of $\sigma(|B|/|B_0|) \approx 0.04$ and
 267 $\sigma(B/|B_0|) \approx 0.15$. It means that the growth of the non-compressive component starts
 268 from a higher level and thus it can reach the saturation level earlier. Other possible ex-
 269 planation can be associated with the suggestion of Kajdič et al. (2017) that the growth
 270 of compressive waves requires a sufficient gradient of suprathermal particles, forming deeper
 271 in the foreshock. Table 1 shows that the median growth rate of weakly compressive waves,
 272 $\gamma_{\sigma B}$ is about one-half of the growth rate of the compressive component in all sets. The
 273 question whether these fluctuations grow more slowly or whether they are already close
 274 to the saturation level under our conditions cannot be answered by the study that mixes
 275 observations at different distance from the foreshock edge.

276 6 Conclusion

277 We present a systematic study addressing a behavior of ULF waves in the distant
 278 foreshock. Using two-point ARTEMIS observations, we analyze the growth rates of waves
 279 under nearly radial IMF computing standard deviations of the IMF magnitude, its com-
 280 ponents and ion density. Although the fluctuations of all parameters are growing toward
 281 the bow shock in a statistical sense, we found also cases exhibiting wave decay. We can
 282 conclude that the Moon and its surrounding (wake, particles reflected from the Moon
 283 surface) affect the growth rate of waves/fluctuations of foreshock origin significantly and
 284 time intervals of foreshock waves should be carefully selected. Such selection allowed us
 285 to demonstrate a reduction of the growth rate due to non-linear effects.

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