Congestus mode invigoration by convective aggregation in simulations of radiative-convective equilibrium

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This study examines how the congestus mode of tropical convection is expressed in numerical simulations of radiative-convective equilibrium (RCE). We draw insights from the ensemble of cloud-resolving models participating in the RCE Model Intercomparison Project (RCEMIP) and from a new ensemble of two-dimensional RCE simulations. About half of the RCEMIP models produce a congestus circulation that is distinct from the deep and shallow circulation modes. In both ensembles, congestus strength is associated with large-scale convective aggregation. Aggregation dries out the upper troposphere, which allows moist congestus outflow to undergo strong radiative cooling. The cooling generates divergence that promotes continued congestus overturning (a positive feedback). This mechanism is fundamentally similar to the driving of shallow circulations by radiative cooling at the top of the surface boundary layer. Aggregation and congestus invigoration are also associated with enhanced static stability throughout the troposphere. Changes in entrainment cooling are found to play an important role in stability enhancement, as has been suggested previously. A modeling experiment shows that enhanced stability is not necessary for congestus invigoration; rather, invigoration itself contributes to midlevel stability enhancement via its impact on the vertical profile of radiative cooling. When present, congestus circulations have a large impact on the mean RCE atmospheric state; for this reason, their inconsistent representation in models and their impact on the real tropical atmosphere warrant further scrutiny.

Congestus mode invigoration by convective aggregation in simulations of radiative-convective equilibrium

Adam B. Sokol¹, Dennis L. Hartmann¹ ¹Department of Atmospheric Sciences, University of Washington, Seattle, WA, USA Key Points: Representation of the congestus mode in RCE varies greatly across models Representation of the congestus mode in RCE varies greatly across models The congestus mode is invigorated by large-scale convective aggregation Tropospheric stability increases with aggregation due to congestus invigoration and reduced entrainment cooling

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10 Abstract

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³⁰ Plain Language Summary

Atmospheric convection over tropical oceans has three distinct types that differ in 31 their vertical reach: a deep mode typically associated with towering cumulonimbus clouds, 32 a shallow mode restricted to the lowest ~ 2 km of the atmosphere, and a congestus mode 33 that falls somewhere in between. This study focuses on the congestus mode, which has 34 received comparatively little attention in the past. We investigate sources of congestus 35 mode variability in simple simulations of the tropical atmosphere. The congestus mode 36 is expressed very strongly in some models but is absent in others. We find that it is stronger 37 when convection is clumped into a limited portion of the model domain rather than dis-38 persed. When present, the congestus mode has a big impact on the distribution of tem-39 perature and moisture throughout the atmosphere. These results are important because 40 they help us better understand the nature of the congestus mode and the climates pro-41 duced by commonly used atmospheric models. 42

43 **1** Introduction

Convection in the tropical atmosphere is known to be trimodal (Johnson et al., 1999). 44 The first and dominant mode is deep convection, marked by towering cumulonimbus clouds 45 extending from the boundary layer to the tropopause. Deep convection is typically front 46 and center in conceptual models of the tropical circulation because of its close relation-47 ship to the Hadley and Walker circulations, which play an important role in global cli-48 mate. The second mode is shallow convection, which produces shallow cumulus clouds 49 (also called trade wind cumulus) at the top of the boundary layer. The final mode, the 50 congestus mode, describes convection that reaches the mid-troposphere. Congestus cloud 51 tops are typically found in the vicinity of the freezing level, distinctly between shallow 52 and deep cumulus. This third mode is the primary focus of this paper. 53

In previous work, the term *shallow* has often been used to refer to any convective feature that is distinct from the deep mode. But such features could be either shallow or congestus in nature; to avoid this ambiguity, we refer to features as *shallow* if they are restricted to pressures greater than 750 hPa and *congestus* if their upper extent lies between 400 and 750 hPa.

The three modes of tropical convection were first recognized by Johnson et al. (1999) 59 in the observed distribution of clouds over tropical oceans. However, overturning circu-60 lations observed in the tropics or derived from global wind reanalyses have generally been 61 only bimodal, with a deep mode and a second mode that is either shallow, congestus, 62 or something in between (Zhang et al., 2004, 2008; Schulz & Stevens, 2018; Y.-C. Chen 63 & Yu, 2021; Trenberth et al., 2000). There are several possible explanations for this dis-64 crepancy. It could be the case that the three modes are not expressed simultaneously, 65 or that the shallow and congestus modes fuse together when averaged over large regions 66 or periods of time. It could also be the case that the relatively fine structures of the shal-67 low mode are not well resolved in reanalyses. Or, perhaps the shallow and congestus modes 68 of convection simply do not translate into distinct modes of the tropical overturning cir-69 culation due to interference from other dynamical factors. 70

The situation is somewhat different in model simulations of radiative-convective 71 equilibrium (RCE), in which each mode of convection is associated with a closed over-72 turning circulation. This is because traditional "RCE-in-a-box" simulations, unlike the 73 real tropics, have no mean large-scale vertical motion, so all convective detrainment must 74 be compensated for by subsidence at the same vertical level. Many model simulations 75 successfully capture the trimodal character of convection (Bretherton et al., 2006; Pos-76 selt et al., 2008; C. J. Muller & Held, 2012; Holloway & Woolnough, 2016; Beydoun & 77 Hoose, 2019; Y.-T. Chen & Wu, 2019), but others produce just two modes (Grabowski 78 et al., 2000; Nolan et al., 2007; Arnold & Putman, 2018). The congestus mode is espe-79 cially fickle, but has received little attention compared to the deep and shallow modes. 80 Our primary goal here is to better understand the variability and sensitivities of the con-81 gestus mode in simulated RCE. 82

Previous work has provided valuable insight into the nature of congestus overturn-83 ing. Yano et al. (2002) argued that cloud-resolving models (CRMs) develop congestus-84 like circulations (what they refer to as "shallow double-cell" circulations) because the 85 deep circulation is linearly unstable when the model domain is a few thousand kilome-86 ters in length. The deviation of model temperature profiles from the real atmosphere has 87 also been implicated (Grabowski et al., 2000). Others have described congestus convec-88 tion as a precursor to deep convection that imports moist static energy until the latent 89 heating is strong enough to support deep updrafts (Wu, 2003; Masunaga & L'Ecuyer, 90 2014; Y.-C. Chen & Yu, 2021). Additionally, congestus clouds have long been associated 91 with mid-tropospheric stable layers, which are thought to inhibit the vertical develop-92 ment of convection by reducing updraft buoyancy and promoting midlevel detrainment. 93 These stable layers have been attributed to various causes, including: latent cooling as-94 sociated with the melting of frozen precipitation from stratiform clouds (B. E. Mapes 95 & Houze, 1995; Johnson et al., 1996; Yasunaga et al., 2006); evaporative cooling of de-96 trained liquid condensate and subsequent radiative cooling (Posselt et al., 2008; Nuijens 97 & Emanuel, 2018); and the radiative (B. E. Mapes & Zuidema, 1996) and microphys-98 ical (Zuidema et al., 2006) responses to dry air intrusions. This previous work suggests that careful consideration of moisture, radiative transfer, and static stability is neces-100 sary in order to fully understand how the congestus mode is expressed in cloud-resolving 101 RCE. 102

103 The apparent linkages to moisture and static stability also beg the question of how the congestus mode is affected by the large-scale self-aggregation of convection (aggre-104 gation for brevity). Aggregation describes the process by which convection spontaneously 105 organizes into distinct regions characterized either by mean ascent (the moist or con-106 *vecting* regions) or by radiatively driven subsidence (the dry or nonconvecting regions). 107 The convecting and nonconvecting regions correspond to the rising and subsiding branches, 108 respectively, of the convectively coupled circulation modes. Aggregation affects the mean 109 RCE climate in several important ways, two of which will be especially relevant through-110 out this paper. First, the troposphere becomes warmer and more stable (Held et al., 1993; 111

Bretherton et al., 2005; Wing & Cronin, 2016). Because stable layers are thought to pro-112 mote congestus-level detrainment, we may a priori expect the congestus circulation to 113 strengthen in response to aggregation. Second, the troposphere becomes drier on aver-114 age as the dry, nonconvecting regions grow to occupy a large fraction of the horizontal 115 area (Bretherton et al., 2005). Dryness aloft allows for strong radiative cooling at the 116 top of the moist boundary layer in nonconvecting regions, which is thought to play an 117 important role in driving shallow circulations (Nigam, 1997; Bretherton et al., 2005; Nis-118 hant et al., 2016; Naumann et al., 2017, 2019). These shallow circulations have been shown 119 to support aggregation by transporting moist static energy up-gradient from nonconvect-120 ing to convecting regions (Bretherton et al., 2005; C. J. Muller & Held, 2012; C. Muller 121 & Bony, 2015; Schulz & Stevens, 2018). Despite extensive study of convective aggrega-122 tion, its impact on congestus circulations has, to our knowledge, not been investigated. 123

Here, our approach to studying congestus variability in cloud-resolving RCE is two-124 fold. In the first part of the paper, we examine the circulation structures produced by 125 the ensemble of CRMs participating in the Radiative-Convective Equilibrium Model In-126 tercomparison Project (RCEMIP; Wing et al., 2018). Beyond contributing to the on-127 going exposition of RCEMIP results, which is valuable in its own right, this analysis will 128 illustrate that different models produce very different RCE circulations even when the 129 experimental configurations are identical. It will also show that the congestus circula-130 tion is subject to a positive feedback involving vertical gradients in moisture and radia-131 tive cooling. But the RCEMIP models differ in countless ways, which makes it difficult 132 to isolate sources of congestus variability. In the second part of the paper, we overcome 133 this difficulty by performing a new set of idealized, two-dimensional RCE simulations 134 that use a single model but span a wide range of aggregation states. This provides a more 135 compelling account of the relationship between aggregation, static stability, and conges-136 tus strength. 137

The rest of the paper is organized as follows. In section 2, we describe the RCEMIP model output, explain the transformation to "moisture space" used to characterize atmospheric circulations, and discuss the RCEMIP results. In section 3, we introduce the new, 2-D simulation ensemble and examine why the congestus circulation is stronger when convection is aggregated. Section 4 focuses on static stability, its dependence on aggregation, and its relationship to the congestus mode. In section 5, we summarize and discuss our results.

¹⁴⁵ 2 Circulation variability in the RCEMIP CRM ensemble

2.1 Simulations and Output

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The RCEMIP simulation protocol is described in Wing et al. (2018). We use output from the "RCE_large300" CRM runs obtained from the public RCEMIP repository hosted by the German Climate Computing Center. We refer to the different models using the same naming conventions as in Wing et al. (2020). There are twelve CRMs for which full RCE_large300 output is available at the time of writing; all are included in our analysis with the exception of the UKMO-RA1-T-nocloud simulation, which differs from the UKMO-RA1-T run (which we include) only in that that sub-grid cloud scheme is disabled.

The RCE_large300 simulations use a domain size of \sim 6000 km × \sim 400 km, a horizontal grid spacing of 3 km, and a uniform sea surface temperature (SST) of 300 K. There is no rotation. Each model run was integrated for at least 100 days. Our analysis uses the last 25 days of each simulation, for which instantaneous 3-D output is available at six-hour intervals. An exception to these specifications is the DAM model, which has 2.5km horizontal grid spacing and 3-D output available at 24-hour intervals. The RCEMIP CRMs use a variety of vertical coordinates. To facilitate comparison across models, we



Figure 1. CRH percentiles for the RCEMIP CRMs (RCE_large300 simulation). The CRH variance σ_{CRH}^2 for each model is given in parentheses.

convert all output to pressure coordinates by taking the time- and domain-averaged pressure at each vertical level.

In addition to the 11 RCEMIP simulations, we conduct a new, RCEMIP-style run using the System for Atmospheric Modeling (SAM; Khairoutdinov & Randall, 2003) with the Predicted Particle Properties (P3) microphysics scheme (Morrison & Milbrandt, 2015) and RRTM radiation (Iacono et al., 2000; Mlawer et al., 1997). We will refer to this run as SAM-P3 to distinguish it from the RCEMIP SAM-CRM run, which uses a different microphysics scheme. The SAM-P3 run uses a 6144×384-km² domain. All other specifications (horizontal resolution, vertical grid, insolation, trace gases, etc.) follow the RCEMIP protocol.

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2.2 Transformation to Moisture Space

We will examine atmospheric circulations in "moisture space", as has been done 173 in the past (e.g. Bretherton et al., 2005; Holloway & Woolnough, 2016; Schulz & Stevens, 174 2018; Beydoun & Hoose, 2019). In this approach, vertical columns of the atmosphere 175 are rearranged and binned according to some measure of column-integrated moisture; 176 here, we use the column relative humidity (CRH) percentile. Because horizontal tem-177 perature gradients are weak in the tropics (Sobel et al., 2001), CRH corresponds closely 178 to the column-integrated moist static energy. We use all of the model output from the 179 25-day compositing period to compute the mean atmospheric state as a function of CRH 180 percentile. The result is a transformation of the modeled atmosphere from four dimen-181 sions (x, y, p, t) to two (CRH percentile, p). The circulations that emerge from this trans-182 formation reflect the exchange of mass between moist regions typically associated with 183 convection and dry regions associated with subsidence. 184

For each simulation, we begin by computing CRH for each grid cell at every time 185 step in the 25-day compositing period for which 3-D output is available. CRH is com-186 puted from the column-integrated water vapor and saturation column-integrated water 187 vapor fields included in the 2-D output. The calculation of saturation vapor pressure is not specified in the RCEMIP protocol and therefore varies from model to model. CRH 189 percentiles are then assigned to each grid cell at each time step; the percentiles are com-190 puted relative to the entire set of CRH values for the 25-day compositing period, as op-191 posed to the values from each individual time step. The grid cells are then sorted by CRH 192 percentile into 100 equally sized bins, with each bin thus representing 1% of the domain 193 area over time. 194

Fig. 1 shows the CRH percentiles for each of the RCEMIP models. Differences in the curves reflect intermodel differences in how moisture is distributed across the domain,

which are closely related to differences in the degree of convective aggregation. In this 197 paper, we quantify the degree of aggregation using the spatial and temporal variance of 198 CRH (σ_{CRH}^2) , which has been used by others in the past (Wing et al., 2020). We pre-199 fer this metric because it is simple and physically intuitive within the moisture space con-200 text. Fig. 1 shows that the models are tightly clustered when it comes to the CRH in 201 the moistest part of the domain. The intermodel spread is much larger in the driest re-202 gions, suggesting that σ_{CRH}^2 is determined primarily by how dry the dry regions become. 203

Following Schulz and Stevens (2018), we compute the mass streamfunction Ψ (kg $m^{-2} s^{-1}$) in pressure coordinates as

$$\Psi_i(p) = \Psi_{i-1}(p) + \frac{\alpha}{g}\omega_i(p) \tag{1}$$

where i is the CRH percentile bin rank (1-100), ω is the bin-averaged vertical velocity 204 in pressure coordinates, q is the acceleration due to gravity, and $\alpha = 0.01$ is the frac-205 tion of total grid boxes contained in the *i*-th bin. The algebraic sign of Ψ is such that 206 flow is counterclockwise around Ψ maxima and clockwise around Ψ minima in all sub-207 sequent figures. 208

From Ψ , we can compute the horizontal velocity in moisture space, v, as

$$v_i(p) = -g \frac{\partial \Psi_i(p)}{\partial p}.$$
(2)

v represents the horizontal exchange of mass between CRH percentile bins. It has un-209 conventional units of time $^{-1}$ because, in moisture space, "distance" is measured as a di-210 mensionless fraction of the domain area. We have chosen these particular formulations 211 of Ψ and v because they are independent of domain size, which varies slightly across the 212 RCEMIP ensemble for computational reasons. They are also easily applicable in both 213 two and three dimensions, allowing us to use the same formulations in our analysis of 214 the 2-D ensemble in section 3. 215

- 2.3 Results 216
- 217

2.3.1 Circulation

Streamfunctions (Ψ) for the RCEMIP models are shown in Fig. 2a. While there 218 is clearly great diversity among the models, there are some common features to note. All 219 models produce a dominant deep circulation that extends from the lower troposphere 220 to ~ 200 hPa. The rising branches of the deep cells are confined to the top few CRH per-221 centiles, meaning that the upward convective mass flux is concentrated within a small 222 horizontal area. A majority of the models have negative Ψ near the surface in the top 223 few CRH percentiles, which is the signature of below-cloud downdrafts driven by the evap-224 orative cooling of rain (i.e., cold pools). 225

The deep circulation in ICON-NWP is unique in several ways. First, the rising branch 226 extends to much lower CRH percentiles than in the other runs. This does not mean that 227 updrafts occupy a larger fraction of the domain (they do not), but that ω is not tightly 228 linked to CRH in ICON-NWP. This could be because updraft speed in ICON-NWP is 229 weak (not shown), which could prevent the simultaneous saturation of an entire atmo-230 spheric column. Second, the deep overturning circulation is weak compared to those in 231 the other models. This is consistent with the previous finding that the integrated, at-232 mospheric radiative cooling rate is smaller in ICON-NWP than in any other RCEMIP 233 model, including the general circulation models (see R_{Net} in Table A2 in Wing et al., 234 2020). There are two explanations for the anomalously weak atmospheric cooling: the 235 mean temperature profile is ~ 4 K colder than the ensemble mean throughout most of 236 the troposphere, and high cloud fraction is especially high. Both of these factors reduce 237 the longwave cooling rate and weaken the overturning circulation. Lastly, the deep cir-238 culation does not extend as high as in the other models, and between 150-300 hPa there 239



Figure 2. (a) Streamfunction Ψ , (b) relative humidity, and (d) radiative heating rate in moisture space for the RCEMIP CRMs. Flow is counterclockwise around Ψ maxima. The black contours in (b,c) show Ψ and have a spacing of 1 g m⁻² s⁻¹ (the outermost contour is 1 g m⁻² s⁻¹). The orange contour in (b) indicates a cloud fraction of 0.1 using a cloud condensate threshold of 10⁻⁵ kg kg⁻¹. The hatching in (c) shows where the radiatively driven divergence $D_{\rm rad}$ exceeds 0.05 day⁻¹; hatching is only shown between 350 and 750 hPa.

is a separate circulation that flows in the opposite sense as the deep cell, with ascent in 240 dry regions and subsidence in moist regions. This, too, can be explained by the ubiq-241 uity of high clouds and their associated radiative effects (Fig. 2b-c). In the dry regions, 242 where the high clouds are thin and undergo radiative heating throughout, there is mean 243 radiative heating between 250-300 hPa. On the other hand, there is radiative cooling at 244 the same level in the moist regions, where the clouds are fresher and thicker and undergo 245 strong longwave cooling at cloud top (Ackerman et al., 1988). The differential radiative 246 heating between the moist and dry regions drives a circulation in the opposite direction 247 as the deep cell. 248

Shallow circulations centered near the top of the boundary layer are present in a majority of the models. As one would expect from previous work, the models with strong shallow circulations are generally those with strong radiative cooling at the top of the dry-region boundary layer (Fig. 2c). This cooling is remarkably strong in UCLA-CRM due to the combination of high humidity and cloud fraction within the boundary layer and low humidity immediately above.

The most notable difference between the model circulations is the representation 255 of the congestus mode. In the moisture-space framework, the clearest marker of the con-256 gestus circulation is its upper branch, which manifests as a layer of moist-to-dry outflow 257 (negative v) in the mid-troposphere. UCLA-CRM and SAM-P3 produce distinct con-258 gestus cells with outflow between 400-600 hPa. MESONH also has a trimodal circula-259 tion with lower outflow layers at 400-500 and 650-800 hPa. UKMO-CASIM and DAM 260 both have weak congestus outflow layers, although in DAM the flow is restricted to low 261 CRH percentiles, which suggests that it may not originate from surface-based convec-262 tion. Interestingly, UKMO-RA1-T produces a circulation with four distinct cells, the mid-263 dle two of which have outflow in the congestus range. The remaining models produce 264 bimodal circulations without a congestus cell. 265

When present, the congestus circulation has a large impact on relative humidity 266 (RH; Fig. 2b) and radiative cooling (Fig. 2c). Congestus outflow layers are associated 267 with plumes of moisture extending from the convective regions into the nonconvective 268 regions, which tend to be drier in the runs with strong congestus cells. As the moist out-269 flow travels away from its convective source, the atmosphere above it becomes increas-270 ing dry, and a strong vertical gradient in RH develops at the top of the outflow layer. 271 The sharp drop-off in RH with height allows for strong radiative cooling, which causes 272 the layer to gradually subside as it moves further from convection. This structure is most 273 evident in UCLA-CRM, UKMO-RA1-T, and SAM-P3. 274

The sharp vertical gradients in RH and radiative cooling are similar in many respects to those thought to induce shallow circulations at the top of the boundary layer (Bretherton et al., 2005; Naumann et al., 2017). It is easy to envision an analogous mechanism acting as a positive feedback on congestus detrainment. Because horizontal temperature gradients in tropical RCE are weak, the dominant thermodynamic balance in the free troposphere in nonconvective regions is that between radiative cooling and subsidence warming. The rate of subsidence needed to exactly balance radiative cooling is $\omega_{\rm rad} = Q_{\rm rad}/s$, where $Q_{\rm rad}$ is the radiative cooling rate and s the static stability. In nonconvective regions, where radiative cooling is the principal diabatic process, $\omega_{\rm rad}$ is a good approximation of mean ω . Vertical gradients in $\omega_{\rm rad}$ produce radiatively driven divergence

$$D_{\rm rad} = \frac{\partial}{\partial p} \omega_{\rm rad}.$$
 (3)

To satisfy mass continuity, radiatively driven divergence in nonconvective regions must be filled by horizontal outflow from convective regions at the same vertical level. These outflow plumes undergo strong cooling, which generates radiatively driven divergence and, in turn, leads to more congestus outflow. We will refer to this as the radiative-divergence feedback.



Figure 3. Domain-averaged static stability *s* for each RCEMIP CRM. Dots indicate the freezing level for each run.

The hatching in Fig. 2c indicates $D_{\rm rad}$ in excess of 0.05 day⁻¹. While every model produces widespread divergence above 300 hPa associated with the deep mode, hatching is only shown between 350-750 hPa for clarity. About half of the models have notable divergence within this pressure range. In the two ICON models, the divergence is associated with cloud radiative heating. In the others, it is coincident with the top of the congestus outflow layer, where the radiative cooling rate rapidly decreases with height. This shows that the patterns of radiative cooling produced by congestus detrainment are consistent with the radiative-divergence feedback mechanism.

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2.3.2 Static Stability and Aggregation

As previously discussed, static stability may also play an important role in congestus dynamics. Fig. 3 shows the mean static stability for each RCEMIP model, which in pressure coordinates is given by

$$s = -\frac{T}{\theta} \frac{\partial \theta}{\partial p} \tag{4}$$

All of the models produce relative maxima somewhere between 400-650 hPa. In a few 289 of the models, the maxima are located very close to the freezing level (indicated by the 290 colored dots), suggesting that they are directly related to microphysical phase transitions. 291 In the other models, the maxima are generally located above the freezing level. Apart 292 from large differences in stability at the top of the boundary layer, the intermodel spread 293 is greatest near the midlevel maxima. This is likely due to differences in entrainment and 294 microphysical processes between the models. Vertical gradients in $Q_{\rm rad}$ may also con-295 tribute to the spread in stability, as will be discussed in section 4. There is much better model agreement in the upper troposphere (250-400 hPa), where water vapor is scarce 297 and the lapse rate is constrained to be close to the dry adiabatic limit. 298

We turn now to the question of how stability, aggregation, and congestus strength covary across the RCEMIP ensemble. Correlation coefficients for these three factors, along with the midlevel $D_{\rm rad}$ in nonconvective regions, are provided in Table 1. Congestus strength

Table 1. Correlation coefficients for measures of convective aggregation (σ_{CRH}^2), congestus strength (v_{cong}), midlevel stability (s), and radiatively driven divergence (D_{rad}) across the RCEMIP CRM ensemble.

	$\sigma^2_{ m CRH}$	$v_{\rm cong}{}^a$	s^b	$D_{\rm rad}{}^c$
$\sigma^2_{ m CRH}$	1.00	-0.82	0.52	0.84
$v_{\rm cong}{}^a$	-0.82	1.00	-0.63	-0.81
s^b	0.52	-0.63	1.00	0.66
$D_{\rm rad}{}^c$	0.84	-0.81	0.66	1.00

 $^a~v_{\rm cong}$ decreases with increasing congestus strength

 $^{b}400-600-hPa$ mean.

^c400-750-hPa and 1-50th-CRH percentile mean.

is quantified as $v_{\rm cong}$, equal to the mass average of the negative values of v between 400-750 hPa at the 50th CRH percentile. The 400-750 hPa range was chosen because it excludes outflow associated with the deep and shallow circulations but captures the range of congestus detrainment heights produced by the different models. If v is positive throughout this entire range (as it is in SCALE and WRF-COL-CRM), $v_{\rm cong}$ is set to zero. More negative values of $v_{\rm cong}$ indicate greater congestus strength.

As expected from previous work, aggregation is generally associated with greater midlevel stability. But σ_{CRH}^2 explains only about a quarter of the variance in stability $(r^2=0.52^2=0.27)$, suggesting that other factors are just as important. This is not particularly surprising; the many differences in model physics across the RCEMIP ensemble will impact the stability in a variety of ways, which limits the explanatory power of any single quantity such as σ_{CRH}^2 .

Congestus strength is generally associated with greater midlevel stability and aggregation. Our *a priori* reasoning was that aggregation could invigorate the congestus circulation precisely through its impacts on stability. Therefore, it is somewhat surprising that v_{cong} is more tightly linked to σ_{CRH}^2 than to *s* (Table 1). This alone does not dismiss the importance of stability, but it does invite us to consider alternative explanations for why the congestus circulation strengthens with aggregation.

One such explanation may be the radiative-divergence feedback identified in the 320 previous section. Congestus-level $D_{\rm rad}$ and $v_{\rm cong}$ are strongly correlated across the RCEMIP 321 ensemble, which is to be expected from basic mass continuity constraints. Less obvious 322 is the strong relationship between $D_{\rm rad}$ and $\sigma_{\rm CRH}^2$, which we may expect now given both 323 variables' relationships with $v_{\rm cong}$ but which we did not expect a priori. These results 324 raise the possibility that congestus invigoration is caused not by increasing stability but 325 rather by an increase in the efficiency of the radiative-divergence feedback. If this is the 326 case, the relationship between stability and $v_{\rm cong}$ may be spurious, reflecting underly-327 ing changes in aggregation rather than a causal link. Of course, it is possible that increases 328 in stability and radiative-divergence feedback efficiency both contribute to congestus in-329 vigoration. 330

We have now identified two distinct mechanisms of congestus invigoration: the stability mechanism—in which increasing stability with aggregation reduces updraft buoyancy and promotes congestus-level detrainment—and the radiative-divergence mechanism, in which aggregation increases the efficiency of the radiative-divergence feedback. This leaves us with two important questions: How, physically, does aggregation boost the efficiency of the radiative-divergence feedback? And what is the relative importance of the two mechanisms? It is difficult to pursue these questions further using the RCEMIP output, since the output variables are limited and the various relationships in question are complicated by myriad differences in model physics. For these reasons, we turn now to the new ensemble of 2-D simulations.

³⁴¹ **2.4 In Sum**

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- Some RCEMIP CRMs simulate trimodal convection, while others produce bimodal convection. One model produces a circulation with four modes.
- Through its impacts on moisture and radiative cooling, the congestus circulation is subject to a positive feedback (the radiative-divergence feedback).
- Aggregation is associated with congestus invigoration and with midlevel increases in stability and radiatively driven divergence.

³⁴⁸ 3 Congestus invigoration in two-dimensional RCE

3.1 Model Simulations

Our goal with the new 2-D simulations is to examine the relationship between aggregation, stability, and congestus strength in the absence of other changes in model physics. To do this, we will use a single model (SAM) and microphysics scheme (P3) to generate a range of equilibria with varying degrees of aggregation and tropospheric stability. The two-dimensional domain makes the runs computationally efficient and allows us to simulate a large number of aggregation states.

The control run is a normal RCE run with uniform 300-K SSTs. In the other runs, we apply small adjustments to the model physics or configuration that are though to impact aggregation and stability in some way. The adjustments are listed in Table 2. With the exception of the control run, each simulation uses a unique combination of up to three adjustments. There are 20 runs in total.

This experimental approach allows us to interpret ensemble trends with confidence. 361 On their own, each model adjustment may introduce confounding factors that would make 362 it difficult to interpret changes in congestus strength. But any physical relationships gath-363 ered from the full ensemble of simulations are unlikely to be spurious, since the adjust-364 ments target completely different parts of the model setup and code. The full ensem-365 ble thus constitutes a powerful tool for addressing our scientific questions. Moreover, it 366 not important whether each adjustment actually achieves its intended effect listed in Ta-367 ble 2, so long as the full ensemble encompasses a range of aggregation states. 368

Apart from the various adjustments, all other aspects of the 2-D simulations follow the RCEMIP protocol. The domain is 5,832 km long with 3-km horizontal resolution. For computational reasons, the vertical grid excludes the uppermost two levels of the standard RCEMIP grid. The runs are initialized with an equilibrium sounding from a 3-D RCE run with 300-K SSTs and are integrated for 150 days, with full instantaneous output collected every 3 hours. The final 60 days of each run are used to perform the transformation to moisture space described in section 2.2.

376 **3.2 Results**

The various model adjustments used in the 2-D runs successfully produce a range of aggregation states (Fig. S1), and the ensemble captures several known impacts of aggregation on mean climate. These trends are illustrated in Fig. 4, in which the color of each line corresponds to degree of aggregation (red is high σ_{CRH}^2). Aggregation is associated with tropospheric warming (Fig. 4a), greater midlevel stability (4b), lower mean

Notation	Description	Intended Effect	
u0	Domain-averaged horizontal wind is nudged to zero on a one-hour timescale	promote aggregation ^{a}	
SSTa1	Sinusoidal SST distribution (299 K at domain edges and 301 K in the center with a mean of 300 K)	promote aggregation since convection clusters over the warmest $SSTs^b$	
sfchomo	Interactively computed surface fluxes are horizon- tally homogenized to the domain average at each time step	inhibit aggregation c	
radhomo	Interactively computed radiative heating rates are horizontally homogenized to the domain average at each time step	inhibit aggregation c	
noacre	Cloud radiative effects are turned off.	inhibit aggregation ^{d}	
5xVT	The fall speed of rain is multiplied by a factor of 5 to shorten the residence time of rain in the atmosphere and reduce evaporative cooling	promote aggregation by inhibiting the formation of cold pools^e	
5xACC	The rate of accretion of cloud droplets by rain is multiplied by a factor of 5 to decrease cloud droplet residence time	inhibit stable layer for- mation due to cloud droplet evaporation ^{f}	
nomelt	Ice cannot melt; it must either sublimate (which can only occur at $T~<~273.15~{\rm K}$) or fall to the surface	inhibit stable layer for- mation due to $\operatorname{melting}^g$	
RADCAM	Uses the radiation scheme from the Community Atmosphere Model 3^h rather than RRTM	provide another possible climate realization	

 Table 2.
 Model adjustments used in the 2-D simulation ensemble

^{*a*}Held et al. (1993). ^{*b*}Lindzen and Nigam (1987). ^{*c*}Bretherton et al. (2005). ^{*d*}Pope et al. (2021). ^{*e*}Jeevanjee and Romps (2013). ^{*f*}Posselt et al. (2008). ^{*g*}B. E. Mapes and Houze (1995). ^{*h*}Collins et al. (2004).



Figure 4. Selected mean profiles from the 2-D SAM runs, with the color of each line corresponding to the degree of aggregation (red is high σ_{CRH}^2). (A) temperature anomaly ΔT with respect to the control run, (B) static stability, (C) mean RH, (D) cloud fraction, (E) radiative cooling rate Q_{rad} , (F) radiatively driven divergence D_{rad} , (G) horizontal velocity v in moisture space, and (H) RH within 9 km of a convective updraft.

RH (4c), and reduced high cloud fraction (4d). The profiles shown in Fig. 4 are domain
averages; Figs. S2-S5 show the complete distributions of RH, radiative heating, static
stability, and cloud fraction in moisture space.

The circulation response to aggregation can be seen in Fig. 5, which shows Ψ for 385 each 2-D run in order of increasing σ_{CBH}^2 . Nearly all of the simulations produce a tri-386 modal circulation, and the relative strength of the three modes clearly changes with ag-387 gregation. As in the RCEMIP ensemble, the congestus cell strengthens with aggrega-388 tion and even dominates the deep circulation in the most aggregated runs. Congestus 389 invigoration evidently comes at the expense of the shallow circulation, which is also ap-390 parent in the mean profiles of v (Fig. 4g). In the unaggregated runs, there is strong shal-391 low outflow (negative v) at ~ 900 hPa and very weak congestus outflow. In the aggre-392 gated runs, the congestus outflow strengthens by a factor of 3-4 and the shallow outflow 393 almost completely disappears. An inflow layer also develops between 700-850 hPa that 394 is absent in the unaggregated runs. 395

The ensemble produces two surprising results with regard to the shallow circulation. First is the general weakening of the shallow circulation with aggregation. This is unexpected because previous work has found that the shallow circulation promotes ag-



Figure 5. Streamfunctions for the 2-D RCE ensemble. The simulations are ordered by increasing σ_{CRH}^2 , which is given in the top left corner of each plot.

gregation (Bretherton et al., 2005). Second, the shallow circulation is relatively unaffected by the horizontal homogenization of radiative heating rates (*radhomo* simulation), which is surprising considering that gradients in radiative cooling are thought to be central to its dynamics (Naumann et al., 2017, 2019). These two findings suggest that shallow circulation dynamics may be fundamentally different in SAM than in other models. While they are worthy of further study, they will not be addressed further here.

The 2-D ensemble exhibits the various components of the radiative-divergence feedback and allows us to assess why the feedback is more efficient when convection is aggregated. Fig. 4f shows that the aggregated runs have a peak in radiatively driven divergence at the congestus level, while the unaggregated runs are approximately nondivergent there. This difference arises from a change in the vertical structure of the radiative cooling rate $Q_{\rm rad}$ (Fig. 4e). In the unaggregated runs, $Q_{\rm rad}$ is relatively uniform above the boundary layer. As convection aggregates, $Q_{\rm rad}$ nearly doubles in the mid-troposphere and decreases slightly aloft, creating a sharp gradient between 400-600 hPa. The shift generally reflects changes in the nonconvective regions, which occupy a majority of the domain (Fig. S3).

The changes in $Q_{\rm rad}$ and $D_{\rm rad}$ with aggregation are ultimately driven by changes 415 in the distribution of moisture. Aggregation is associated with a reduction in RH through-416 out the free troposphere, but the 600-700 hPa layer is an important exception. At that 417 level, the aggregated runs are moistened by congestus outflow and have a mean RH sim-418 ilar to the unaggregated runs (Fig. 4c). Despite similar RH there, the aggregated runs 419 undergo much stronger radiative cooling because aggregation reduces the emissivity of 420 the upper troposphere. The reduction in emissivity results from upper tropospheric dry-421 ing and reduced high cloud amount, which simultaneously allow the midlevel moist layer 422 to cool more efficiently and inhibit cooling aloft, since there is less water vapor there to 423 do the emission. The combination of stronger congestus-level cooling and weaker cool-424 ing aloft creates the large $Q_{\rm rad}$ gradient that ultimately generates midlevel divergence. 425

The important insight here is that aggregation strengthens the radiative-divergence feedback via its impact on moisture. The formation of a dry patch with aggregation is crucial because it fosters radiatively driven divergence at the congestus level. Without aggregation, the upper troposphere stays moist, congestus outflow plumes cannot cool as strongly, and there is little or no divergence.

The radiative-divergence mechanism of congestus invigoration is distinct, but not 431 mutually exclusive, from the stability mechanism. To understand the relative importance 432 of the two, we conduct another 2-D simulation in which we artificially inflate $D_{\rm rad}$ in the 433 absence of aggregation. To do so, the radiative cooling rate is prescribed as the mean 434 $Q_{\rm rad}$ profile from one of the highly aggregated runs (here we use $u0 \ 5xVT$, but the re-435 sults are similar if another aggregated run is used). Everything else is identical to the 436 control run. Aggregation does not occur in the prescribed radiation (PR) run because 437 the $u\theta$ and 5xVT adjustments are not applied and because the prescribed cooling is hor-438 izontally uniform. The horizontally uniform cooling also means that $D_{\rm rad}$ is approximately 439 uniform; this differs from the aggregated runs, in which radiatively driven divergence is 440 limited to nonconvective regions. A consequence of the horizontally uniform $D_{\rm rad}$ is that 441 the circulation in the PR run is not well organized in moisture space, and midlevel v is 442 not a suitable measure of congestus strength. Instead, we compute the convergence of 443 the in-cloud mass flux, which is averaged across the entire domain such that it reflects 444 mean circulation strength rather than in-cloud vertical velocity. 445

Results from the PR run are shown in Fig. 6. The temperature profile in the PR 446 run is free to vary but stays within 1 K of the control run profile up to 300 hPa. As a 447 result, midlevel stability remains close to the control (Fig. 6a). On the other hand, the 448 vertical structure of $D_{\rm rad}$ is more similar to the aggregated run, which is by design (Fig. 449 6a). In essence, the PR run allows the radiative-divergence feedback to operate, albeit 450 artificially, without the increase in stability that would normally accompany it. How does 451 this affect the congestus circulation? At 500-650 hPa, the cloud mass flux convergence 452 in the PR run is similar to the aggregated run, even exceeding it slightly (Fig. 6d). This 453 suggests that the radiative-divergence mechanism can fully invigorate the congestus cir-454 culation without any change in static stability. This result is to be expected for an at-455 mosphere in RCE; since convective heating must exactly balance radiative cooling, the 456 prescribed decrease in $Q_{\rm rad}$ with height between 600 and 400 hPa requires the convec-457 tive heating rate to also decrease with height. This manifests as convective mass flux con-458 vergence (i.e., detrainment) within the 400-600 hPa layer. 459

The takeaway from the experimental PR run is that an increase in static stability is not necessary for congestus invigoration in RCE. This leads us to our final ques-



Figure 6. Results from the 2-D RCE run with prescribed radiative cooling (dashed blue line). (a) Static stability. (b) Radiative cooling rate. (c) Radiatively driven divergence. (d) Convergence of the in-cloud mass flux averaged across the entire domain. Clouds are defined as grid boxes with a cloud condensate mixing ratio exceeding 10^{-5} kg/kg.

462	tion: what is the nature of the stability response to aggregation? Does it have anything
463	to do with congestus invigoration?

464 **3.3 In Sum**

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- Congestus overturning is invigorated by aggregation in the 2-D RCE ensemble.
 - The radiative-divergence feedback becomes more effective with aggregation because the emissivity of the upper troposphere is reduced.
- A simulation with prescribed radiation shows that radiatively driven divergence
 invigorates the congestus circulation even when there is no increase in static stability.

471 4 Why does static stability increase with aggregation?

We focus now on the increase in tropospheric static stability that accompanies aggregation and congestus invigoration (Fig. 4b). While we have established that the stability increase is not critical for congestus invigoration in the 2-D RCE runs, we remain interested in its causes and its relationship to the congestus mode.

To simplify our discussion, we compute mean stability profiles for the most and least aggregated terciles of the 2-D ensemble runs (there are 7 runs in each tercile). The yellow line in Fig. 7b shows the change in domain-averaged stability between the unaggregated and aggregated terciles. Stability increases everywhere between 250-950 hPa, with the largest increases at the congestus level and the top of the boundary layer. Our goal here is to determine the causes of the stability increase and to explain its vertical structure.



Figure 7. Difference between aggregated and unaggregated 2-D runs in (a) differential radiative cooling and (b) three different static stability profiles. Yellow: domain-averaged stability; red: stability in grid boxes containing active convection; blue: stability of a undiluted moist adiabat computed as described in the text.

Previous work has typically attributed the stability increase to changes in convec-483 tive processes (we will discuss the exact mechanisms shortly). The red line in Fig. 7b 484 shows the change in stability within portions of the model domain that are actively con-485 vecting, which we define as those with a 400-600-hPa mean ω less than -5 Pa s^{-1} and 486 total condensate mixing ratio greater than 10^{-5} kg kg⁻¹. Within active convection, sta-487 bility increases with aggregation at all tropospheric levels. But the vertical structure of 488 the stability change looks nothing like that of the change in domain-averaged stability. 489 At the congestus level and at the top of the boundary layer, the increase in domain-averaged 490 stability is much greater than one would expect from the changes within active convec-491 tion, while the opposite is true other levels. This tells us that the mean RCE temper-492 ature profile is not simply "set" by deep convection. While changes in convective pro-493 cesses provide a baseline increase in stability throughout the troposphere, radiative pro-494 cesses are also important, and the effect of these processes on the mean temperature pro-495 file evidently changes with aggregation. In the remainder of this section, we discuss and 496 evaluate the convective and radiative sources of enhanced stability. 497

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4.1 Convective Sources

Why does the static stability within active convection increase with aggregation? Here, we discuss two explanations from the literature and evaluate their importance in the 2-D ensemble.

The first explanation is that aggregation increases the initial moisture content of 502 convective updrafts, which causes convection to follow a warmer, more stable moist adi-503 abat. Held et al. (1993) suggested that the increase in initial moisture content occurs 504 because convection begins deeper within the boundary layer, where it more humid. But 505 in the 2-D ensemble, actively convecting grid boxes are *less* likely to have upward mo-506 tion throughout the boundary layer when convection is aggregated (not shown), so this 507 mechanism does not explain the present results. Alternatively, Bretherton et al. (2005) 508 found that the near-surface RH in convective regions increases with aggregation, which 509

would boost the initial moisture content of updrafts without any change in their initi-510 ation height. In the 2-D ensemble, aggregation is indeed associated with an increase in 511 boundary layer RH in convective regions. We assess the impact of this increase on sta-512 bility by computing moist adiabatic temperature profiles (and associated stability pro-513 files) for each run, using as the starting point the 1000-hPa temperature and RH in the 514 top CRH percentile, where most of the upward convective mass flux occurs. The blue 515 line in Figure 7b shows the change in moist adiabatic stability between the aggregated 516 and unaggregated terciles. The magnitude of the increase is far too small to account for 517 the increase in stability within active convection, so we can conclude that changes in sur-518 face RH play only a minor role in the stability response to aggregation. This result is 519 not sensitive to the exact level at which the moist adiabats are initialized. 520

The second explanation deals not with the initial moisture content of convection 521 but with the impact of entrainment mixing once convection has begun. The tropical tem-522 perature profile deviates from a perfect moist adiabat due to the entrainment of unsat-523 urated air into convective updrafts, which leads to evaporation and causes the lapse rate 524 to exceed that of an undiluted plume (Singh & O'Gorman, 2013). It has been hypoth-525 esized that aggregation mitigates this entrainment cooling (B. Mapes & Neale, 2011; Feng 526 et al., 2015), leading to an increase in stability. Large-eddy and convection-permitting 527 simulations support this prediction, but with an important caveat: the reduction in en-528 trainment cooling does not occur because entrainment itself is reduced (in fact, the op-529 posite occurs) but rather because the entrained environmental air is more humid and thus 530 cannot cause as much evaporative cooling (Becker et al., 2018; Becker & Hohenegger, 531 2021). In essence, aggregation creates a "moist shell" that protects convective plumes 532 from entrainment cooling (Becker et al., 2018). This is physically intuitive, considering 533 that what it means to be aggregated in the first place is that convection occurs in the 534 vicinity of other convection, where it is already likely to be moist. But aggregation as 535 indicated by large σ_{CRH}^2 by no means guarantees the presence of a moist shell. First of 536 all, CRH is skewed towards the RH of the warm lower troposphere and therefore pro-537 vides limited information about RH at higher levels. Furthermore, as shown by Figs. 1 538 and S1, variability in σ_{CRH}^2 is driven mostly by how dry the dry regions are, which tells 539 us nothing about the RH distribution in moist regions. 540

Is a moist shell detectable in our 2-D simulations? We define the convective shell 541 as the portion of the model domain that is within three grid boxes (9 km) of active con-542 vection but is not actively convecting itself. Fig. 4h shows that the mean shell RH in-543 creases with aggregation throughout the entire troposphere. It is not surprising to see 544 this result at the level of congestus detrainment, since congestus invigoration itself moist-545 ens the convective shell there. But the greatest difference in shell RH (10-15%) is found 546 below this level, between 700-900 hPa. Relative to a unaggregated shell RH of 80%, a 547 10-15% increase constitutes a 50-75% reduction in saturation deficit, suggesting that the 548 moist shell effect has a substantial impact on the efficiency of entrainment cooling. Within 549 the 700-900 hPa layer, the within-convection stability becomes increasingly sensitive to 550 aggregation with height (Fig. 7b), which is consistent with the accumulating impact of 551 the moist shell on a rising parcel. Of course, some of the impact may be offset if the en-552 trainment rate increases with aggregation, as was found by Becker et al. (2018). While 553 an in-depth study of entrainment rates is beyond our scope here, the development of a 554 moist shell with aggregation and the insufficiency of the alternative explanations both 555 suggest that the moist shell plays an important role in stability enhancement. These re-556 sults are not sensitive to the threshold used to define the convective shell. 557

558 4.2 Radiative Sources

We have now shown that decreases in entrainment cooling are more important than increases in surface RH when it comes to the increase in stability within active convection. We now turn to radiative sources of increased stability.



Figure 8. Stability and radiative cooling in a highly aggregated run (u0 SSTa1 5xVT). (a) Colored shading shows the instantaneous radiative heating rate. The black contour indicates static stability in excess of 0.075 K hPa⁻¹ and the red contour relative humidity above 60%. (b) Blue shading shows the domain-averaged radiative heating rate over a ten-day period. Black contours indicate domain-averaged stability of 0.065 and 0.073 K/day.

Posselt et al. (2008) suggested that differential radiative cooling at the top of con-562 gestus outflow layers could lead to enhanced stability. As we have already shown, the 563 vertical gradient of $Q_{\rm rad}$ in the mid-troposphere is stronger when convection is aggre-564 gated. This is illustrated again in Fig. 7a, which shows the difference in $-\partial_p Q_{\rm rad}$ (where 565 $\partial_p = \partial/\partial p$ between the aggregated and unaggregated terciles. At levels where $-\partial_p Q_{\rm rad}$ 566 increases with aggregation (350-650, 825-900 hPa), changes in the $Q_{\rm rad}$ profile are act-567 ing to increase stability. Comparison of Figs. 7a and 7b shows that this occurs where 568 the increase in domain-averaged stability exceeds that within active convection. The op-569 posite is true where changes in $-\partial_p Q_{\rm rad}$ act to decrease stability. The structural sim-570 ilarity between the changes in differential radiative cooling and the changes in domain-571 averaged stability suggest that the former plays an important role in shaping the latter. 572

How can we be sure that the link between differential radiative cooling and enhanced 573 mean stability is causal? Examining their association over space and time provides com-574 pelling evidence. Fig 8a shows an instantaneous snapshot of stability and $Q_{\rm rad}$ in one 575 of the highly aggregated runs (u0 SSTa1 5xVT). The convective region is in the center 576 of the domain, where the SST is slightly elevated. The sloping bands of strong radiative 577 cooling mark the top of the congestus outflow layer. Stable layers, enclosed by the black 578 contours, are found at the top of the outflow layer and remain linked to it as it subsides. 579 In the driest regions (both ends of the periodic domain), the stable layer has detached 580 from the outflow layer and is located just above it (see also Fig. S4). We speculate that 581 this has to do with the horizontal spreading of stability anomalies by gravity waves em-582 anating out from convection. After detrainment, stability anomalies grow via differen-583 tial cooling at the top of the outflow layer as it subsides. Eventually, the stability anoma-584

lies are "ripped off" of the outflow layer by gravity waves, which work to erase the hor izontal temperature gradients that develop from the vertical displacement of the stabil ity anomaly.

The link between stability and differential radiative cooling can also be seen over 588 time. Fig. 8b shows the domain-averaged stability and $Q_{\rm rad}$ over a 10-day period in the 589 same aggregated run. Bands of strong radiative cooling originate at the congestus out-590 flow level approximately every 2.5 days. These oscillations have been noted in previous 591 work and have a period that depends on the size of the model domain (Grabowski et al., 592 2000). Stability anomalies can be seen growing at the top of the outflow plumes and sub-593 siding with them. At a fixed pressure level, stability is greatest when there is strong dif-594 ferential radiative cooling. 595

4.3 In Sum

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The static stability response to aggregation in the 2-D ensemble is shaped by both convective and radiative processes; both are of similar importance.
In convective regions, a reduction in entrainment cooling with aggregation is the primary driver of increased stability; changes in surface RH play a lesser role. These changes are not directly related to congestus invigoration.
In nonconvective regions, strong differential Q_{rad} at the top of congestus outflow plumes act to increase midlevel stability. This change is directly tied to conges-

tus invigoration.

5 Discussion

This paper began with a discussion of the third mode of tropical convection: the congestus mode. We examined congestus representation and variability in the RCEMIP CRM ensemble and in a new ensemble of 2-D RCE simulations conducted with SAM, a widely used cloud-resolving model. A wide variety of congestus representations were found in both ensembles, underscoring the need to better understand the nature of the congestus mode in cloud-resolving RCE.

The most significant finding of this work is that the congestus mode is invigorated 612 by large-scale convective aggregation. The invigoration mechanism is, at its core, very 613 similar to that which is thought to drive shallow circulations at the top of the bound-614 ary layer. Both rely on the presence of sharp vertical gradients in the longwave cooling 615 rate, which are ultimately caused by sharp gradients in moisture. In the shallow circu-616 lation case, these gradients are found at the top of the moist boundary layer, whereas 617 in the congestus case they are found at the top of congestus outflow plumes. Aggrega-618 tion is an important part of this process because it dries out the upper troposphere in 619 nonconvecting regions, which allows for stronger cooling at the top of the moist layer. 620 This invigoration mechanism relies on basic principles of radiative transfer and mass con-621 servation, and its components are present in both the RCEMIP and 2-D RCE ensem-622 bles. While the impact of aggregation on congestus overturning is clear, whether or not 623 the congestus mode affects initiation and development of aggregation remains uncertain. 624

This work also examined how static stability affects and is affected by congestus 625 invigoration. Previous work has largely assumed that mid-tropospheric stable layers are 626 the cause of congestus-level detrainment. With this logic, congestus invigoration might 627 be attributed to an increase in midlevel stability. But the results presented in sections 628 3.2 and 4 suggest that enhanced stability is largely the result, rather than the cause, of 629 congestus invigoration. The crux of this finding was a model experiment showing that 630 invigoration can occur without any change in stability if the radiative cooling rate is pre-631 scribed to induce congestus-level divergence. It is important to reiterate that this result 632 may be inevitable in simple RCE simulations such as these, in which any imposed gra-633

dient in radiative cooling must be matched by a gradient in convective heating. For this reason, we caution that this specific result may be limited in scope, and it is unclear to what extent it applies to the real tropics, where approximate RCE is realized only on large spatial and time scales (Jakob et al., 2019).

In section 4, we asked why the mean static stability increases as convection aggre-638 gates. Much of this stability enhancement can be attributed to congestus invigoration: 639 stability anomalies grow by differential radiative cooling atop congestus outflow plumes 640 before being spread across the domain by gravity waves. The stability increase is also 641 supported by a moistened convective shell, which reduces the efficiency of entrainment 642 cooling and allows convecting parcels to adhere more closely to a moist adiabatic tem-643 perature profile. Aggregation also increases the surface RH in convecting regions, but 644 this has a relatively small impact on stability compared to the other factors. These re-645 sults are helpful for understanding the sensitivity of mean climate to aggregation, and 646 they illustrate how the response to aggregation can be significantly affected by conges-647 tus dynamics. Our understanding of the stability response to aggregation would ben-648 efit from simulations with finer horizontal resolution, which would provide a more com-649 plete picture of entrainment processes. 650

This work leaves us with many questions worthy of further study. How is conges-651 tus overturning affected by climate warming? The answer to this question will almost 652 certainly depend on how warming affects the degree of convective aggregation, which re-653 mains very uncertain. And how may the congestus circulation itself affect the climate 654 sensitivity of the RCE state? Given its impacts on moisture and radiative transfer, we 655 suspect that congestus strength has a direct bearing on the surface and top-of-atmosphere 656 energy budgets. Perhaps most importantly, how realistic are model representations of 657 the congestus mode? Without a doubt, the findings reported here are helpful for under-658 standing RCE simulated by cloud-resolving models. Their applicability to the real world 659 remains an open question. 660

Deepening our knowledge of how clouds, convection, and circulation interact is a pressing priority within climate science and is critical to the advancement of the field (Bony et al., 2016). Cloud-resolving RCE simulations, such as those discussed here, have proven to be a valuable research tool in this endeavor. As we have shown, RCE climates can be greatly affected by the congestus mode. Careful interpretation of cloud-resolving RCE therefore requires continued study of the "forgotten mode" of tropical convection.

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Figure 1.



Figure 2.

a) Streamfunction Ψ



CRH percentile

Figure 3.



Figure 4.



Figure 5.



Figure 6.



Figure 7.

Aggregated – Unaggregated



Figure 8.

